

# *Stratification of canopy magnetic fields in a plage region:*

*Constraints from a spatially-regularized weak-  
field approximation method*

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# CHROMOSPHERIC HEATING PROBLEM:

→ The chromosphere is not in radiative equilibrium.

What kind of physical processes can provide the energy necessary to sustain the radiative losses that are observed?

Key ingredient:



**Magnetic Fields**

Dynamics

Energy balance

Atmospheric  
structure

Cannot be directly observed

→ Imprint in the polarization properties of spectral lines

→ **Stokes parameters**

# Spatially-regularized WFA

**WFA** (for  $B_{||}$ ):  $V(\lambda) = -C_1 B_{||} \frac{dI}{d\lambda} \rightarrow \chi^2 = \frac{1}{N} \sum_{i=\lambda_0}^{\lambda_n} \left( \frac{V_{obs}^i - V_{synt}^i}{\sigma_i} \right)^2 = \frac{1}{N} \sum_{i=\lambda_0}^{\lambda_n} \frac{1}{\sigma_i^2} \left( V_{obs}^i - \left( -C_1 \frac{dI_i}{d\lambda} B_{||} \right) \right)^2$

Added Tikhonov regularization to the WFA:

For a given linear problem  $\mathbf{Ax} = \mathbf{b}$

USUAL APPROACH:  $||\mathbf{Ax} - \mathbf{b}||^2 = 0$

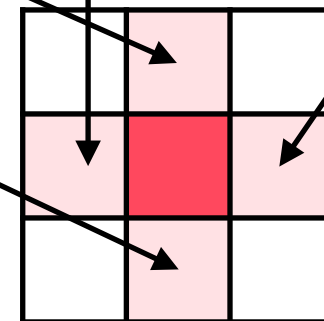
WITH TIKHONOV REG.:  $||\mathbf{Ax} - \mathbf{b}||^2 + ||\mathbf{\Gamma x}||^2 = 0$

**Spatially-regularized WFA** (for  $B_{||}$ ):

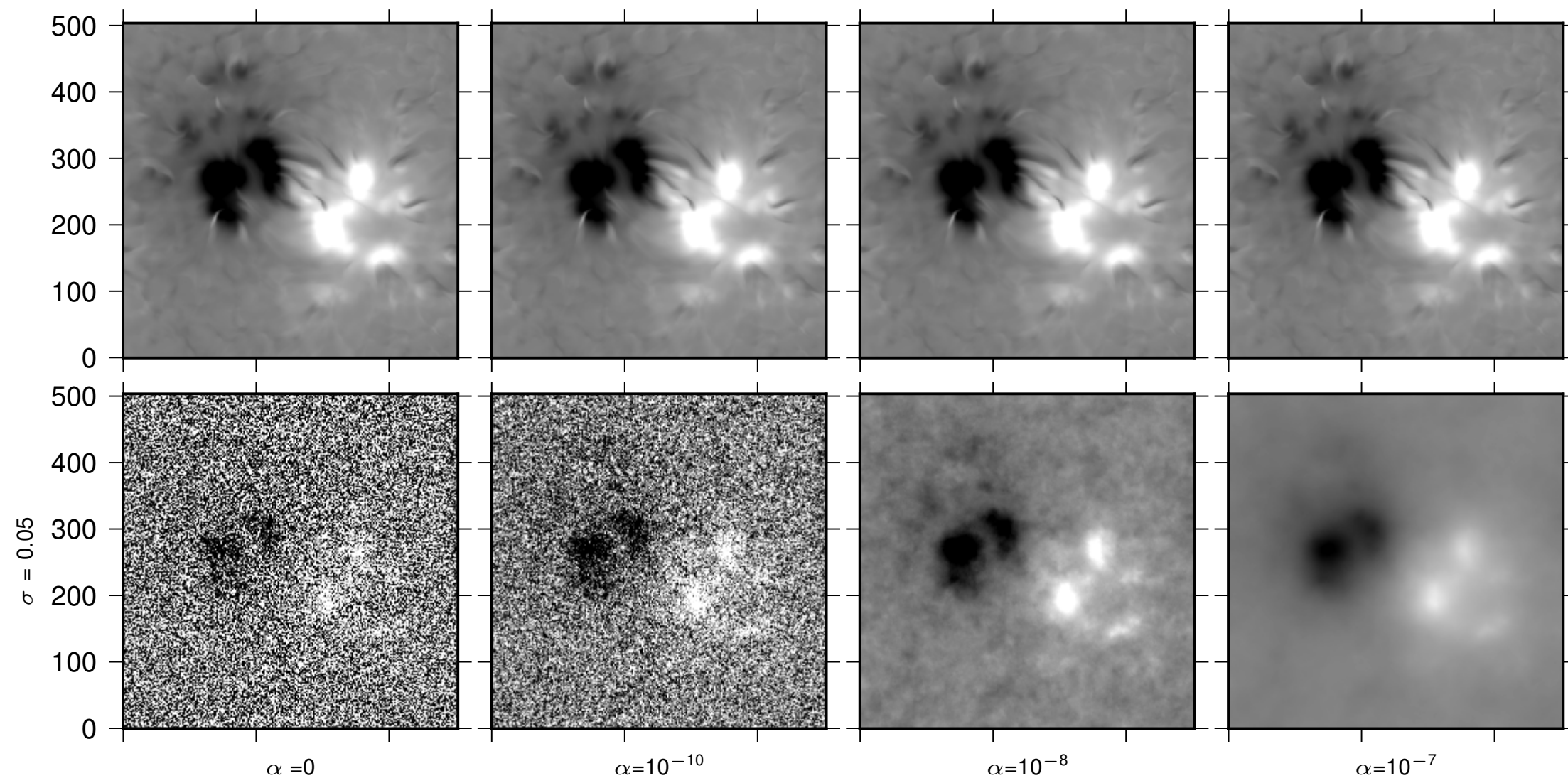
$$\chi^2 = \sum_{i=\lambda_0}^{\lambda_n} \left( V_i - C_1 \frac{dI_i}{d\lambda} B_{||}^{(x,y)} \right)^2 + \alpha \left[ \left( B_{||}^{(x,y)} - B_{||}^{(x,y-1)} \right)^2 + \left( B_{||}^{(x,y)} - B_{||}^{(x,y+1)} \right)^2 + \left( B_{||}^{(x,y)} - B_{||}^{(x-1,y)} \right)^2 + \left( B_{||}^{(x,y)} - B_{||}^{(x+1,y)} \right)^2 \right]$$

Now the problem becomes **global** and the solution for the entire FOV needs to be computed.

Similar procedure for  $B_{\perp}$  and  $\phi$ .



# Test on synthetic data



Top row:  $B_{||}$  obtained from MHD model

Bottom row:  $B_{||}$  obtained when a noise value  $\sigma$  is applied to the data for three different value of the regularization parameter  $\alpha$



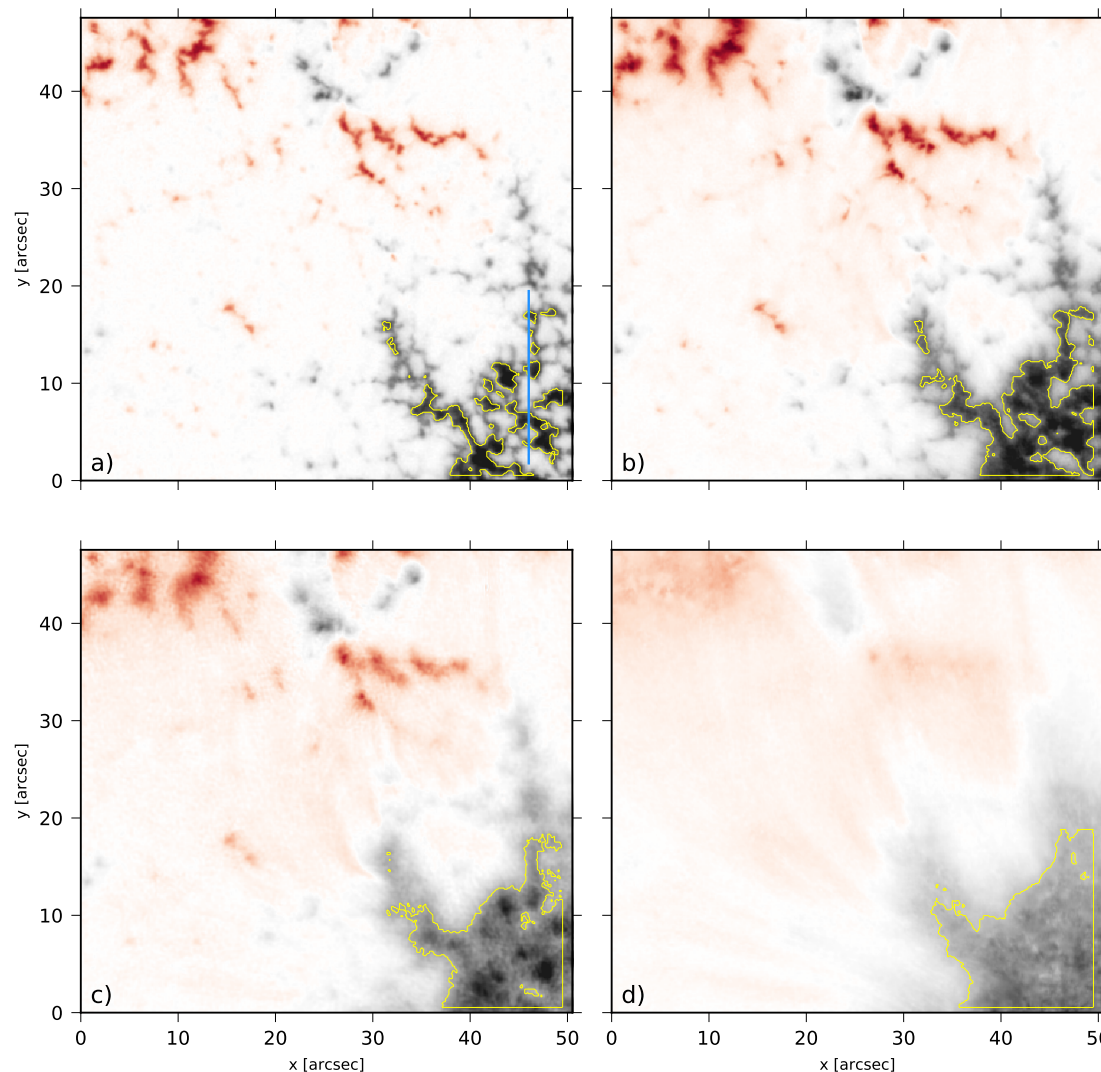
# Application to real data

> Swedish 1-m Solar Telescope (SST) with CRisp Imaging Spectro-Polarimeter (CRISP)

> 2018-06-19 at 07:33:14 UT

> Plage region at  $(X,Y)=(229'',61'')$ ,  $\mu=0.97$

| Label | Atom  | Line [ $\text{\AA}$ ] | $\bar{g}_{\text{eff}}$ | G    | $\lambda_i$ [m $\text{\AA}$ ]       | $\langle z \rangle$ [km] | $\langle B_{\parallel} \rangle$ [G] | $\langle B_{\parallel} \rangle$ [G] (2D) |
|-------|-------|-----------------------|------------------------|------|-------------------------------------|--------------------------|-------------------------------------|--|
| a)    | Na I  | 5895.824              | 1.33                   | 1.33 | $[-360, -300, -240, 240, 300, 360]$ | $157 \pm 18$             | $398 \pm 206$                       | $719 \pm 88$                             |
| b)    | Na I  | 5895.824              | 1.33                   | 1.33 | $[-120, 60, 60, 120]$               | $474 \pm 40$             | $546 \pm 161$                       | $692 \pm 94$                             |
| c)    | Mg I  | 5172.684              | 1.75                   | 2.87 | $[-40, 0, 40]$                      | $760 \pm 45$             | $502 \pm 118$                       | $558 \pm 103$                            |
| d)    | Ca II | 8542.091              | 1.10                   | 1.21 | $[-110, -55, 0, 55, 110]$           | $1168 \pm 122$           | $417 \pm 69$                        | $444 \pm 83$                             |



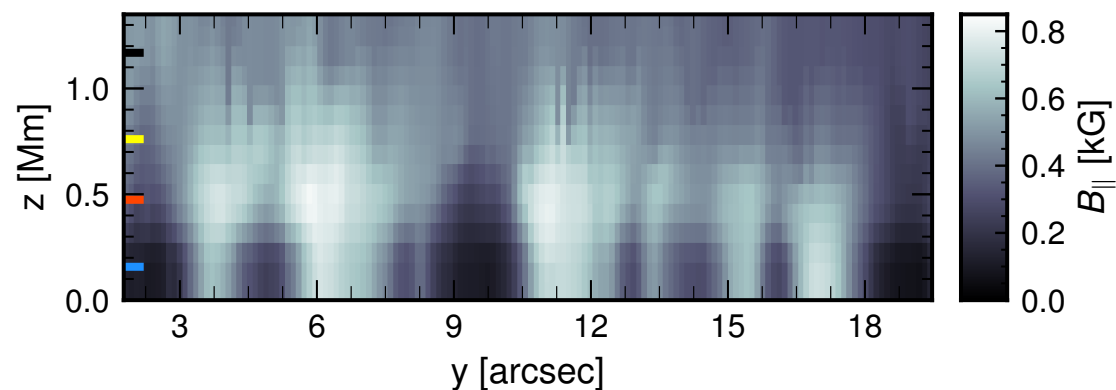
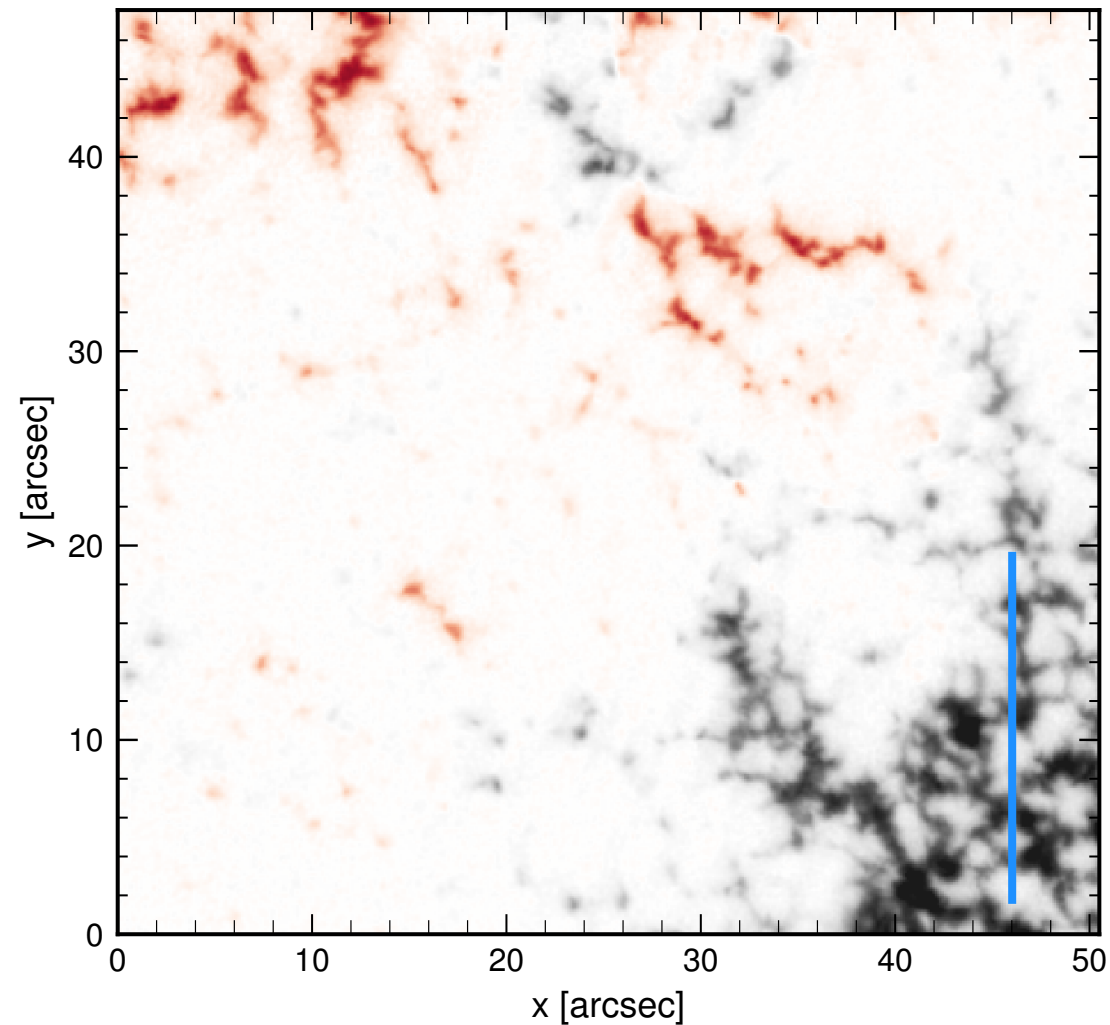
Panel (a): Photosphere, far wings of the Na I 5896  $\text{\AA}$  line.

Panel (b): Upper photosphere, inner wings of the Na I 5896  $\text{\AA}$  line.

Panel (c): Lower chromosphere, core of the Mg I 5173  $\text{\AA}$  line.

Panel (d): Chromosphere, core of the Ca II 8542  $\text{\AA}$  line.

# Stratification of **B**



- > Edge of the magnetic canopy: between 300km and 600km
- >  $\langle B_{||} \rangle = 449$  G at  $z = 1000$ km
- > Pietrow et al. (2020) in a parallel study (using a different technique) recovered very similar values.

Colored ticks = mean formation region:  
blue : panel (a)  
red : panel (b)  
yellow : panel (c)  
black : panel (d)

# ~Summary~

- Adding spatial constraints to WFA allows improving the fidelity of the reconstruction of **B**;
- The reconstructed stratification is consistent with a topology in which  $P_{gas}$  dominates in the photosphere and  $P_B$  in the chromosphere: **B** can expand forming a hot magnetic canopy in the chromosphere;
- *Chromospheric heating* in plage is expected to be dominated by processes associated with the presence of **B**: by setting constraints on topology and strength we can help to discern which mechanisms are more likely to happen over plage.

On GitHub:

[https://github.com/morosinroberta/spatial\\_WFA](https://github.com/morosinroberta/spatial_WFA)