

## **Poster Session 3.6**





Probing multiscale properties of plasma turbulence in space and time at sub-ion scales with Iterative Filtering.

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# THE NEED FOR A MULTISCALE STUDY OF PLASMA TURBULENCE

- There is a long standing debate about what causes the turbulent energy cascade at sub-ion scales.
- Nonlinear wavelike interactions via, e.g. Kinetic-Alfvénwave interactions (or other wave-like non-linear interactions) may continue the turbulent cascade below d<sub>i</sub>, as suggested by several observational studies of the solar wind [2,3].
- But the intermittency observed in both simulations and observations [4], together with the measure of enhanced dissipation in localized structures [5,6], puts doubts on the validity of such models.

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• A full space-time analysis can indeed help to shed light on this relatively long-standing problem,

#### HOWEVER...

 We need novel space-time analysis techniques able to deal with the intrinsic multiscale nature of turbulence (nonlinearity, non stationarity, presence of impulsive events).



Power spectrum of magnetic fluctuations shows the multiscale turbulence of the solar wind. In particular, the well-known -5/3 MHD inertial range, and the transition to the sub-ion range. (from ref. [1])

Measure of the reduced magnetic helicity in the solar wind. The signature consistent with KAW (righthand polarization) is found between  $\sim$ 70° and  $\sim$ 120°. (from ref [2])





Kurtosis measured in the solar wind and in numerical simulations highlighting the presence of intermittencty. (from ref [4]).

## MULTISCALE ANALYSIS IN SPACE AND TIME WITH FTFIF

#### NUMERICAL DATASET

• Periodic 2D Hall-MHD simulation with  $1024^2$  grid points and a box size of  $128 d_1$ .

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- Freely-decaying turbulence in presence of a mean out-of-plane magnetic field  $B_0$  (plasma  $\beta = 2$ ).
- Alfvénic-like fluctuations with  $b_{rms}$ : 0.24 B<sub>0</sub> are introduced, at large scales ( $k_{\perp}d_i < 0.3$ ).



#### SPACETIME ANALYSIS

Building a  $k\omega$ -power spectrum of fully developed turbulence

We use Fourier Transform (FT) in space and Fast iterative Filtering (FIF) in time to measure the distribution of magnetic energy in wavenumber-frequency ( $k\omega$ ) space.

- 1. At the maximum of turbulent activity and for each quantity (e.g.  $B_z$ ), we take a datacube of  $1024^2x2001$  points and with a resolution of  $0.125d_i \times 0.125d_i \times 0.01\Omega_i^{-1}$ .
- 2. We perform a 2D FFT to obtain  $B_z(k_x, k_y, t)$ .
- 3. For each pair  $(k_x,k_y)$ , we perform a FIF decomposition and calculate average frequency and amplitude of each IMC.
- 4. We Interpolate the corresponding power to a  $(k, \omega)$  grid and sum up the power over all found frequencies (~2.000.000 complex IMFs found per field).

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# $k\omega$ -power spectra of velocity and magnetic field



- 1. Clear signature of fast/whistler branch.
- 2. The signature of KAW activity is seen better in velocity (top).
- 3. In all the fields, most of the energy is at low frequencies, not clearly related to wave activity.



 k<sub>∞</sub>-power spectrum obtained from the FTFIF decomposition of the perpendicular component of the ion-fluid velocity (left) and magnetic field (top) at the maximum of turbulent activity. The dispersion relation is calculated using the the distribution of the angle between the magnetic field and the simulation plane.

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## POWER SPECTRA IN *k*-SPACE: WAVES ENERGETICS



Energetic contribution from waves and from low-frequencies is measured by integrating in frequency over selected areas of the  $k\omega$ -space (see left figure). Bottom: Whistler (violet curve) and KAW (orange curve) k-power spectra, together with the spectrum obtained by integrating in  $\omega$  over the whole area (black solid curve), which correspond to the classic Fourier 1D spectrum (dashed red curve).

But low-frequency Energy could still be generated by slow/lon-Cyclotron (S/IC) activity and/or low-



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# ASSESSING THE NATURE OF LOW-FREQUENCY FLUCTUATIONS

### $\delta B_{||}^2/\delta \rho^2$

### $\delta u_{\perp}^2/\delta u_z^2$



- The ratios of the power spectra from the wave branches (violet and orange) confirm that they are of wave origin.
- $\delta B_{||}^2/\delta \rho^2$  (panel a) of the total spectra (black solid curve) matches with the approximate KAW ratios [9] and with the S/IC ratio

#### HOWEVER,

•  $\delta u_{\perp}^2/\delta u_z^2$  (panel b) does not match! This rules out any relevant wavelike energetic contribution at low frequencies.

### Grošelj et al. 2019 [10]



The ratio of the total spectra (black solid line of panel a in the left plot) are in agreement with the KAW ratios measured both in 3D FULL-PIC simulations and observations (top right figure). This suggests that our results may hold also in more realistic numerical models, as well as in space plasma environments.

### CONCLUSIONS: sub-ion scales turbulence is more structure-like than wave-like!

## REFERENCES

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# FAST ITERATIVE FILTERING

#### A. Cicone, Numerical Algorithms 85, 811 (2020)

 $\widehat{F}_2$ 

**F** :

 $\widehat{\boldsymbol{F}}_{\boldsymbol{N}}$ 

Fast Iterative Filtering (FIF) [7] is an adaptive technique for the analysis of nonstationary non-linear signals similar to the Empirical Mode Decomposition [8].

A given signal, f(x) (e.g. a time series) is decomposed into a finite number N of • Intrinsic Mode Components  $\widehat{F}_{i}(x)$  (IMCs) (whose average frequency is well behaved) plus a residual  $r_{f,N}(x)$ :

$$f(\mathbf{x}) = \sum_{j=1}^{N} \widehat{F}_{j}(\mathbf{x}) + r_{f,N}(\mathbf{x}),$$

• Each IMC  $\hat{F}_{i}(x)$  is the result of an iterative procedure that, by using a low-pass filter  $w_{\lambda_i}(t)$ , isolates a high-frequency fluctuating component whose frequency is well-behaved:

High-pass filter operato

or: 
$$S_{\lambda_j}[s(\mathbf{x})] = s(\mathbf{x}) - \int_{-\lambda_j}^{\lambda_j} s(\mathbf{x} + \mathbf{t}) w_{\lambda_j}(\mathbf{t}) d^k t$$

IMC definition: 
$$\widehat{F}_j(x) = \lim_{n \to \infty} S^n_{\lambda_j} \left[ f(x) - \sum_{l=1}^{j-1} \widehat{F}_l(x) \right]$$

