Different periodic behaviours of magnetic helicity flux in flaring and non-flaring AR cases Sz. Soós,^{1,4} M. B. Korsós,^{2,1,4} H. Morgan,² and R. Erdélyi^{3,1,4}

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- Focus on the observational property of **magnetic helicity flux** in δ -type ARs.



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- Berger (1984):

$$\frac{dH}{dt}\Big|_{S} = 2\int_{S} \left(\vec{A}_{p} \cdot \vec{B}_{h}\right) \vec{v}_{\perp z} dS - 2\int_{S} \left(\vec{A}_{p} \cdot \vec{v}_{\perp h}\right) \vec{B}_{z} dS$$



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- Their conjecture was that EM/SH/T have a common period before flare onset.4



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 - the AR cannot be associated with fast CMEs (Here, we define \geq 750 km s⁻¹).



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- **Local maxima** in the WPS using an implementation of the o-th dimensional persistent homology method (Huber 2021).











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• Such a **clear harmonic property** is not detected in the different flux components of flaring or non-flaring ARs.



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 - the **AR has a \delta-spot**,
 - **shorter** oscillatory **periods** appear **in** the **EM flux data**, and
 - these periods show the **presence of a harmonic oscillatory resonator**.