

How does numerical diffusion affect high resolution two-fluid simulations of magnetized turbulence?

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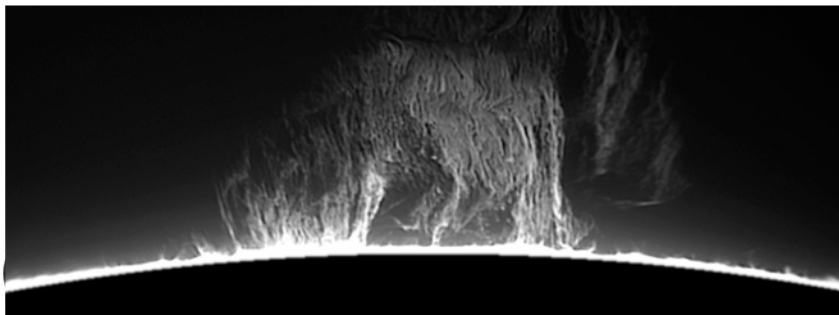
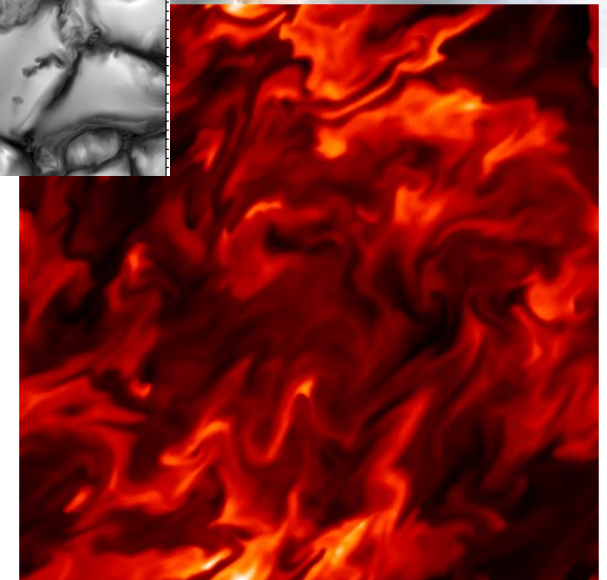
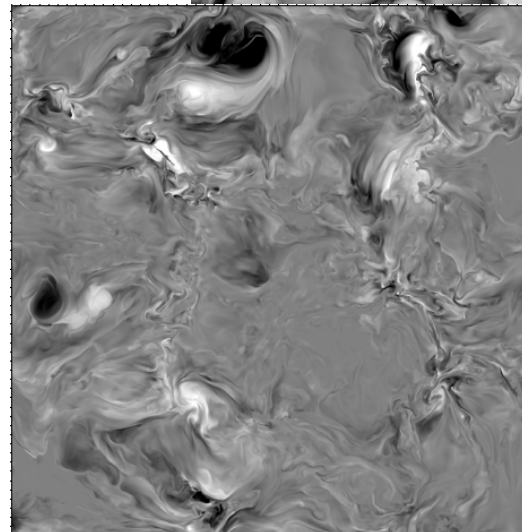
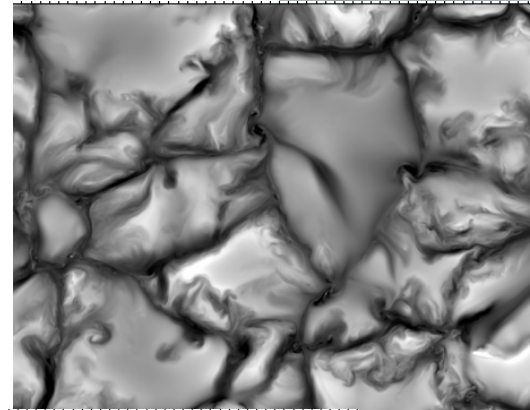
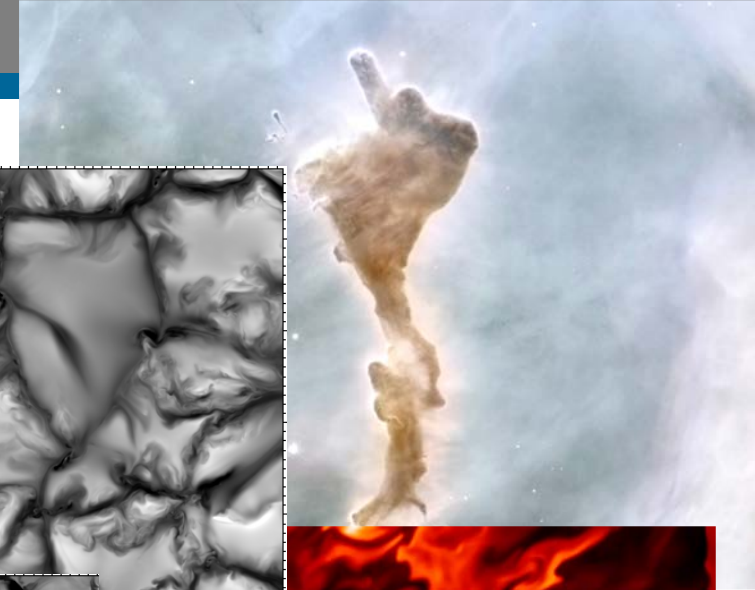
[References to related presentations Ids:](#) 391, 327, 502, 444



TURBULENCE

Turbulence in weakly ionized plasmas is common in astrophysical environments

- (*) Molecular clouds ::
ionization degree 10^{-7} , weak collisional coupling
- (*) Solar photospheric turbulent convection ::
ionization degree 10^{-4} , strong collisional coupling
- (*) Solar chromosphere ::
ionization degree 10^{-2} , intermediate collisional coupling
- (*) Turbulence associated to solar prominences ::
conditions similar to the chromosphere



TWO-FLUID APPROACH

Mancha-2F :: Popescu Bralleanu et al 2019

Neutrals

Charges

Momentum evolution x 2 =

Advection
Hydrodynamic forces
Viscose force
Collisional force

Advection
Hydrodynamic forces
Magnetic force
Viscose force
Collisional force

+ not easy to determine numerical diffusivity of the code

Energy evolution x 2 =

Advection
Radiation
Frictional heating
Thermal exchange

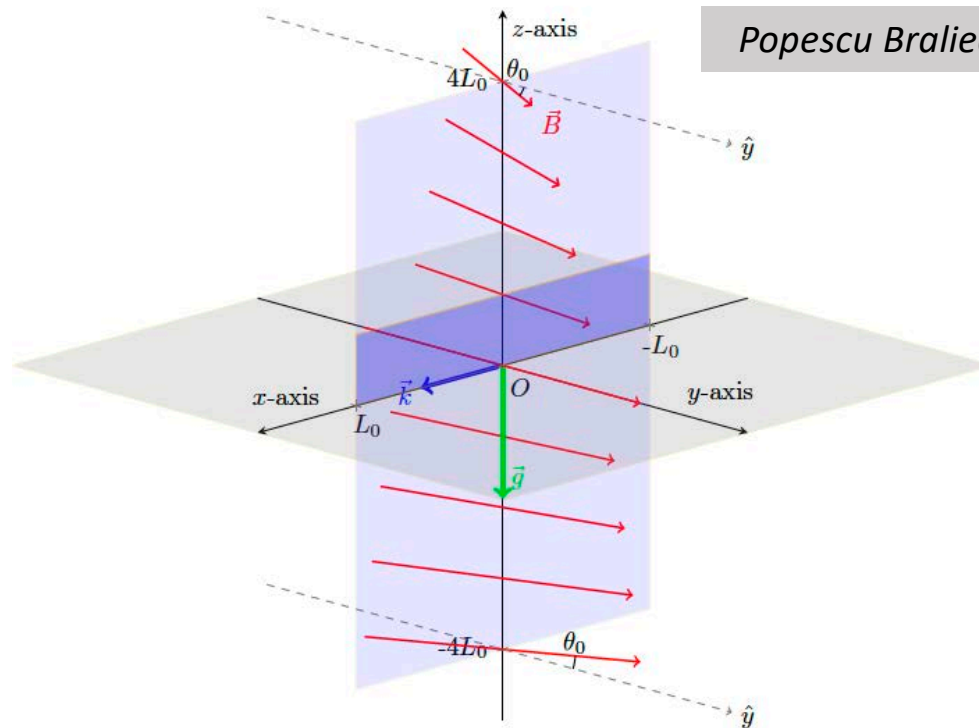
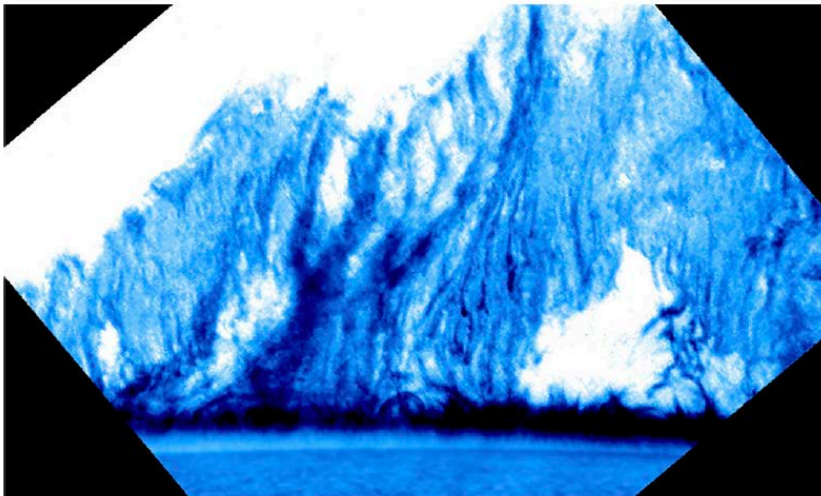
Advection
Radiation
Ohmic heating
Frictional heating
Thermal exchange

OBJECTIVES & METHODS

OBJECTIVES ::

(*) Evaluate an equivalent of the Ohmic-like numerical diffusion coefficient for multi-fluid simulations

(*) Estimate the order of dissipation of the numerical scheme.



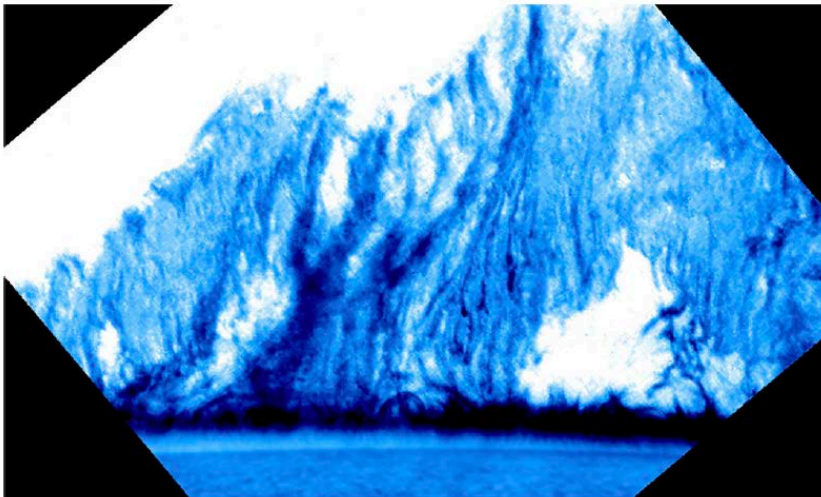
- Numerical box 2048 x 8192 grid; $dx=dz=1$ km
- Smooth prominence – corona interface
- Magnetic field out of plane and sheared
- **3 sets of numerical diffusion parameters for Mancha-2F code**

OBJECTIVES & METHODS

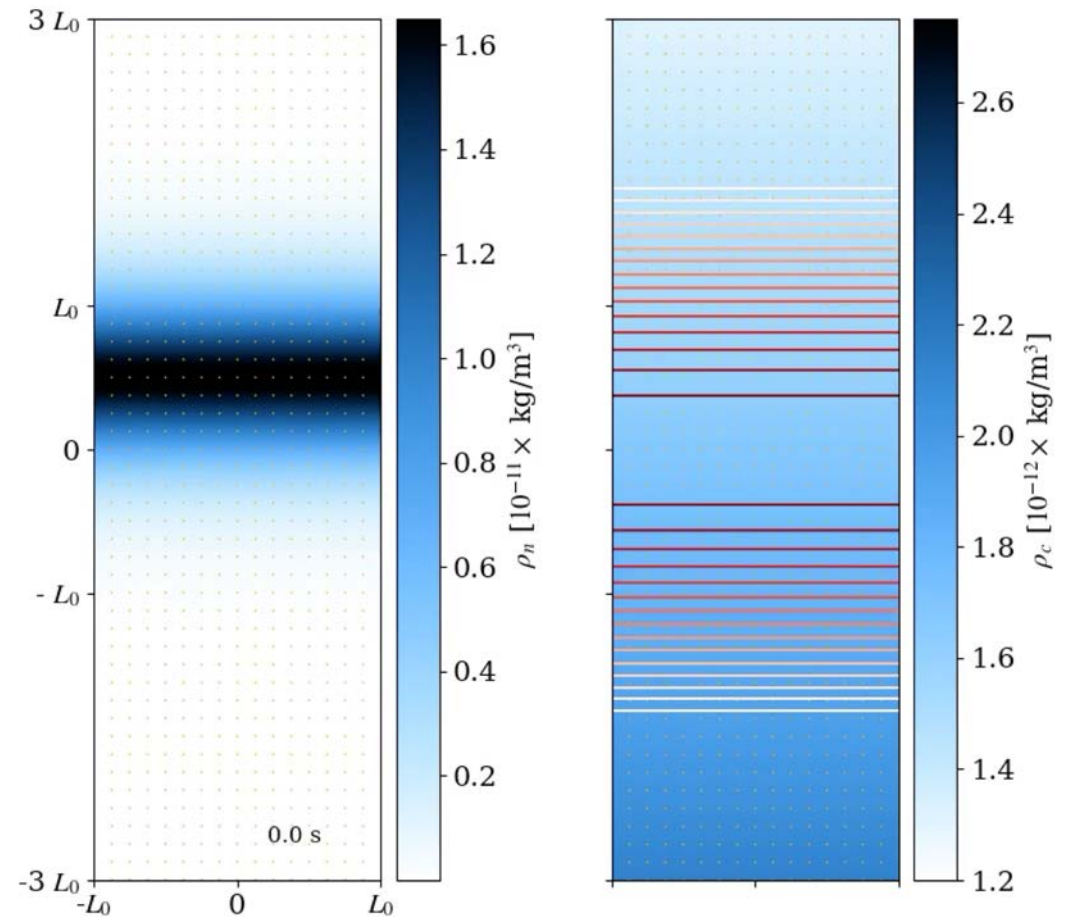
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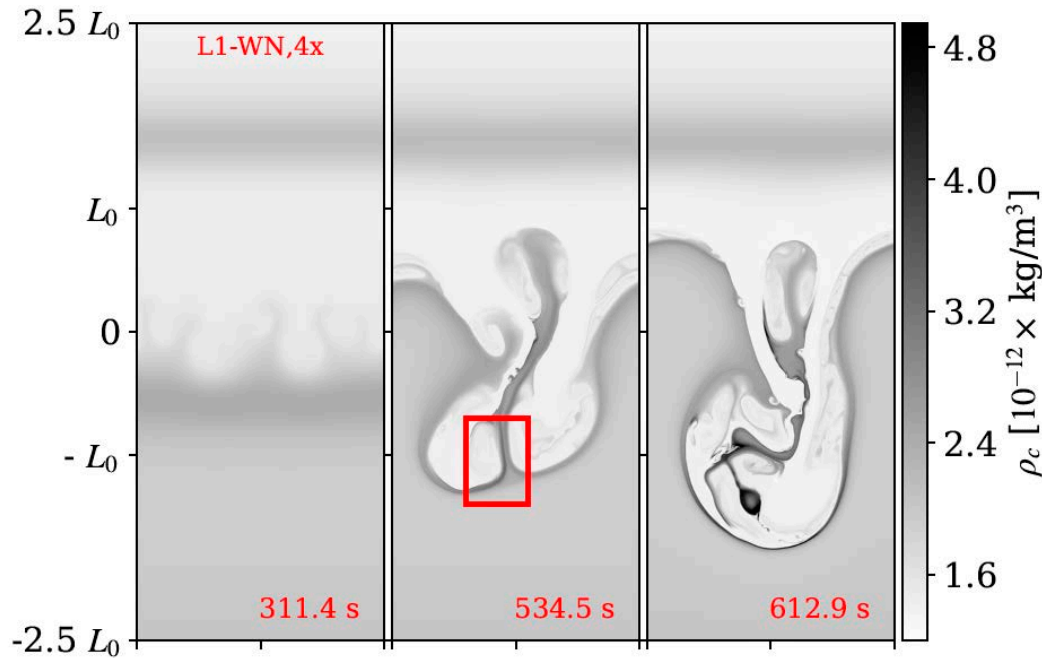


EVOLUTION of NEUTRAL & PLASMA DENSITIES

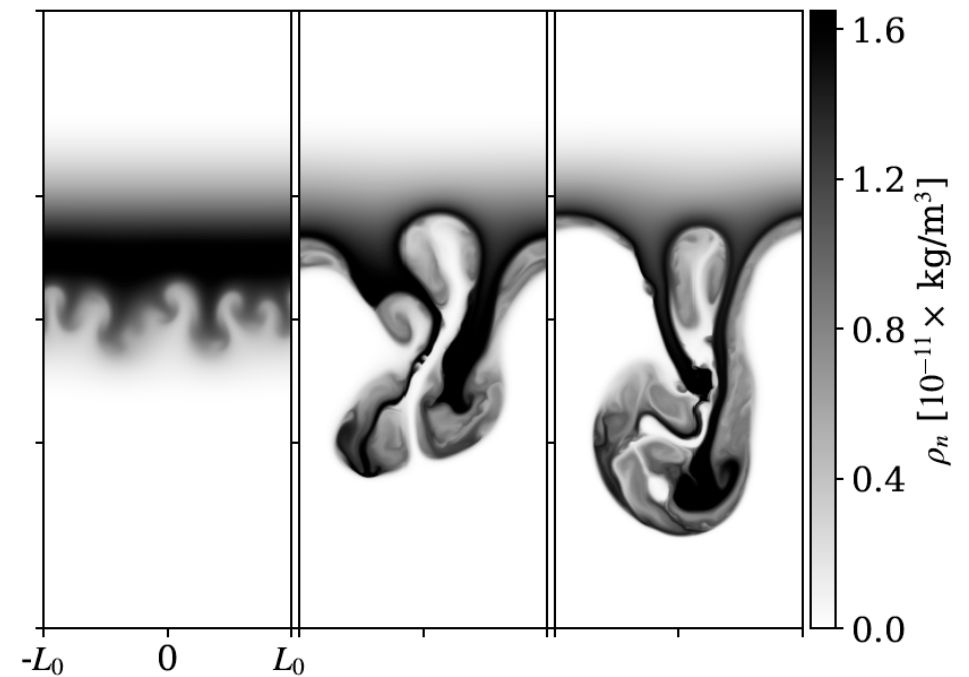


DYNAMICS

PLASMA DENSITY



NEUTRAL DENSITY



- Neutral drops are brought together by plasma dynamics
- Current sheet formation in between
- Reconnection and formation of magnetic islands filled with coronal material

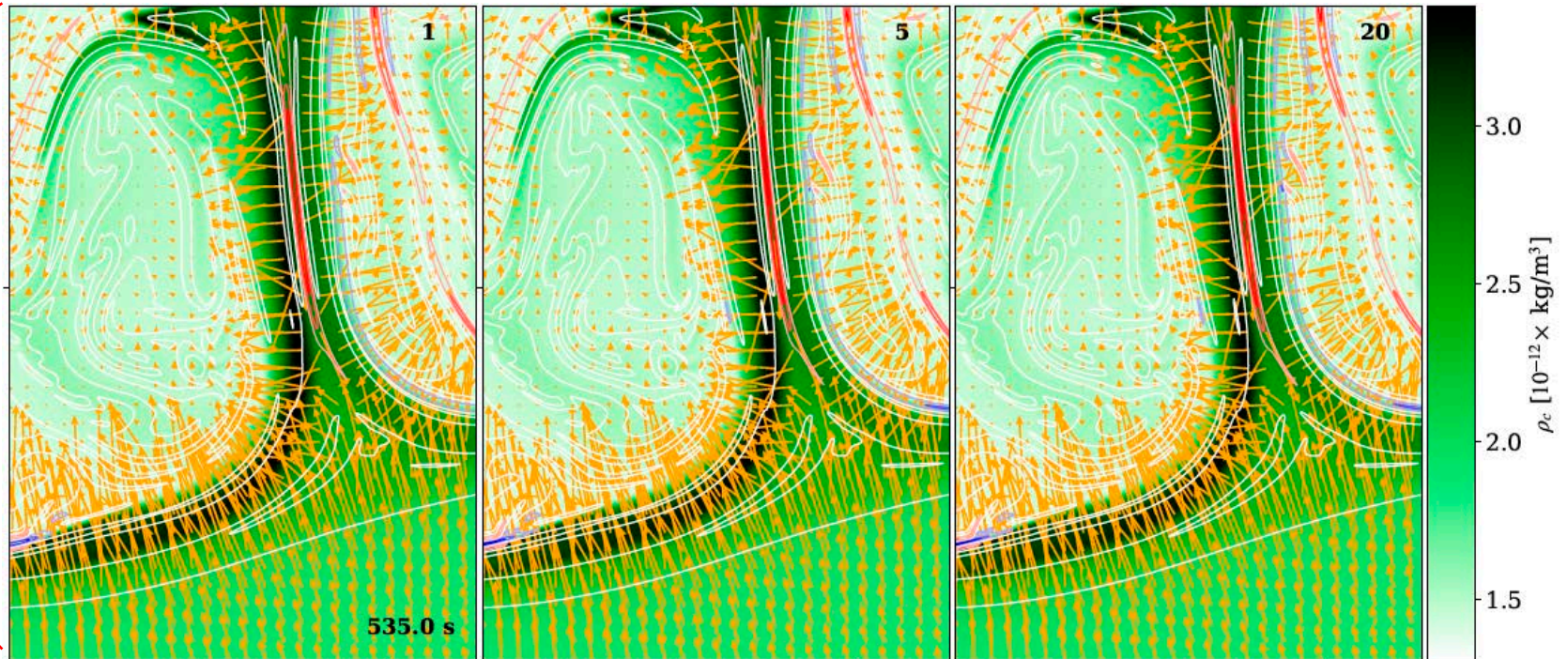
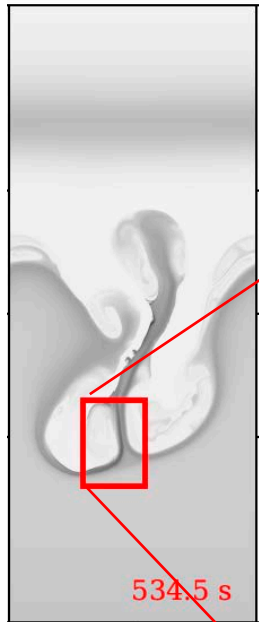
DYNAMICS of the CURRENT SHEET :: 3 NUMERICAL SETS

Snapshots of plasma density for three parameters of code's simulation filtering frequency

Filter every 1 time step

Filter every 5 time steps

Filter every 20 time steps

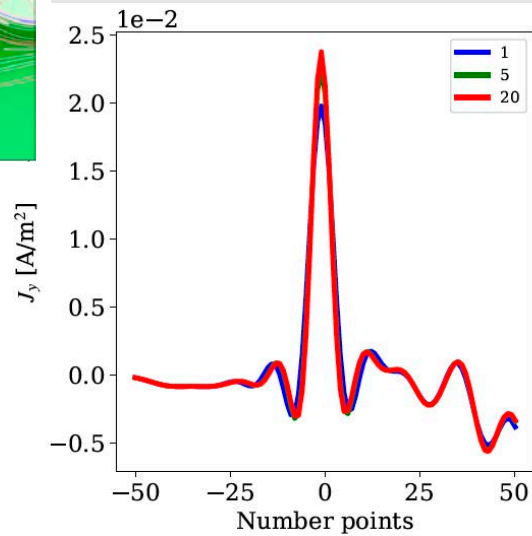


- Slight, but important differences after running with different filtering for a short time

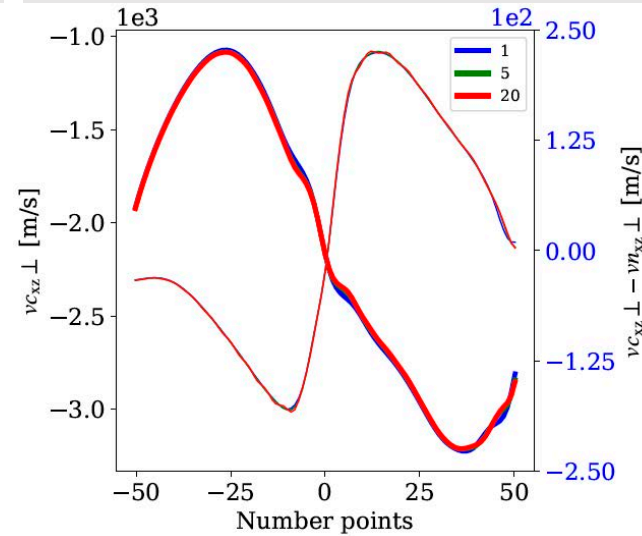
DYNAMICS of the CURRENT SHEET :: 3 NUMERICAL SETS



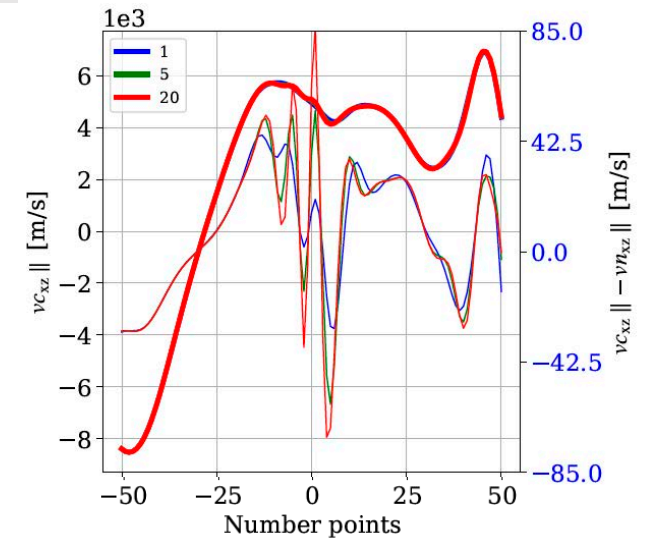
Out of plane current density



Velocity & velocity decoupling perpendicular to the current sheet



Velocity & velocity decoupling parallel to the current sheet



- Filter every 1 time step
- Filter every 5 time steps
- Filter every 20 time steps

- Slight, but important differences after running with different filtering for a short time
- Differences in the strength of J_y and in the outflow decoupling

EVALUATION of EFFECTIVE DIFFUSIVITY

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times [\mathbf{v} \times \mathbf{B}] + \left(\frac{\partial \mathbf{B}}{\partial t} \right)_{\text{diff}}$$

Assume diffusivity is Ohmic-like & constant in space

$$\left(\frac{\partial \mathbf{B}}{\partial t} \right)_{\text{diff}} = \nabla \times \left[-\eta_{\text{scheme}} \mathbf{J} \right] = \eta_{\text{scheme}} \Delta^2 \mathbf{B}$$

$$\mathbf{y} = \eta_{\text{scheme}} \mathbf{x} + \mathbf{c},$$

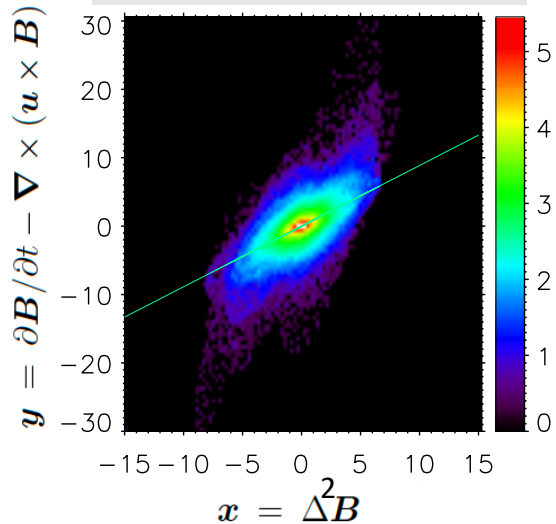
where

$$\mathbf{x} = \Delta^2 \mathbf{B},$$

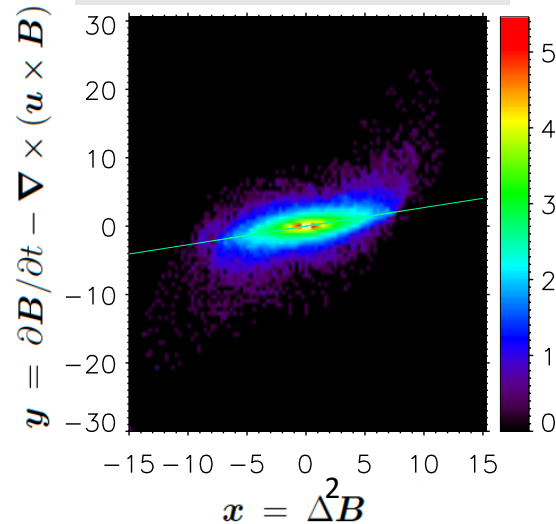
$$\mathbf{y} = \partial \mathbf{B} / \partial t - \nabla \times (\mathbf{u} \times \mathbf{B}).$$

$$\eta_{\text{scheme}} = \begin{Bmatrix} 0.9 \\ 0.3 \\ 0.08 \end{Bmatrix} \times 10^6 \text{ m}^2/\text{s}$$

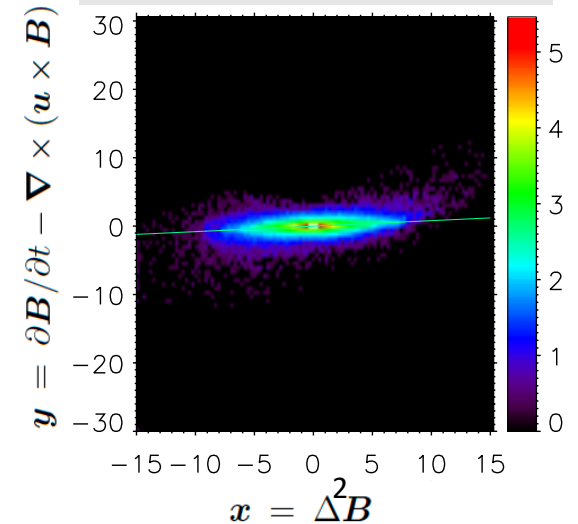
Filter every 1 time step



Filter every 5 time steps



Filter every 20 time steps



EVALUATION of EFFECTIVE DIFFUSIVITY

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times [\mathbf{v} \times \mathbf{B}] + \left(\frac{\partial \mathbf{B}}{\partial t} \right)_{\text{diff}}$$

Assume hyper-diffusivity constant in space

$$\left(\frac{\partial \mathbf{B}}{\partial t} \right)_{\text{diff}} = \eta_{\text{hyper}} \Delta^4 \mathbf{B}$$

$$y = \eta_{\text{hyper}} x + C$$

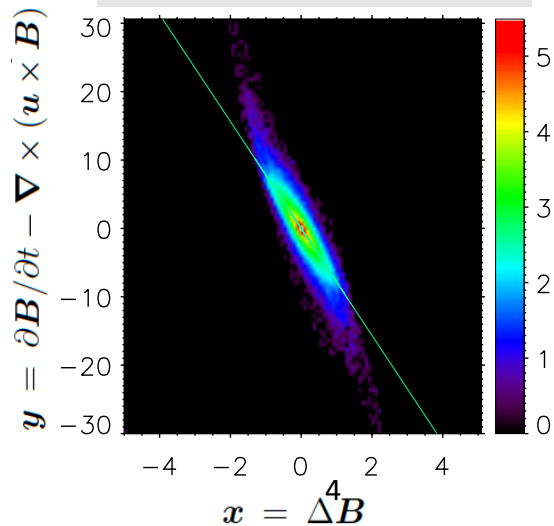
where

$$x = \Delta^4 B,$$

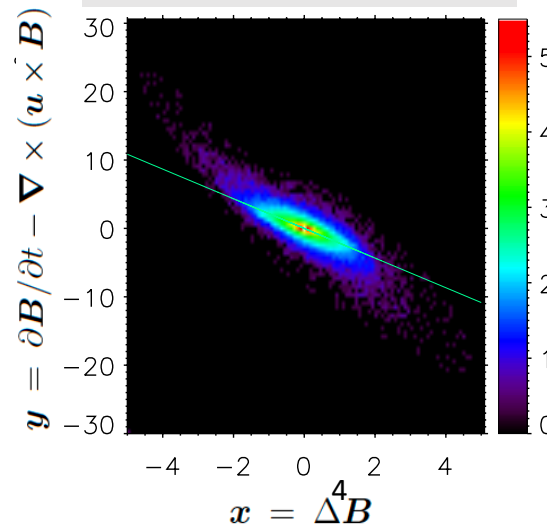
$$y = \partial B / \partial t - \nabla \times (\mathbf{u} \times \mathbf{B}).$$

$$\eta_{\text{hyper}} = \begin{Bmatrix} 7.8 \\ 2.2 \\ 0.63 \end{Bmatrix} \times 10^{12} \text{ m}^4/\text{s}$$

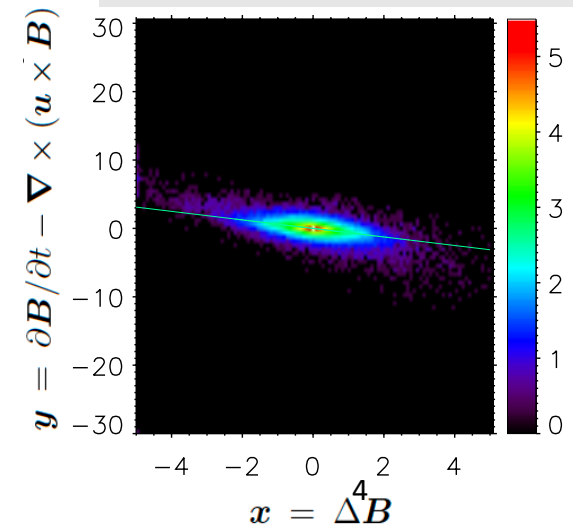
Filter every 1 time step



Filter every 5 time steps



Filter every 20 time steps



SUMMARY

- Simulations of magnetized turbulence are frequently affected by numerical properties of the code
- Two-fluid simulations require scales of plasma-neutral interactions to be resolved
- We propose how to evaluate the numerical diffusion in the explicit two fluid code Mancha-2F
- Our method is clearly sensitive to the numerical parameters of the simulation (filtering frequency)
- The method allows to estimate the order of dissipation of the numerical scheme

References:

- Khomenko, E. Vitas, N. Collados, M. de Vicente, A. “Numerical simulations of quiet Sun magnetic fields seeded by the Biermann battery”, A&A, 2017, 604, id.A66
- Popescu Braileanu, B.; Lukin, V. S.; Khomenko, E. “Two-fluid simulations of waves in the solar chromosphere. I. Numerical code verification”, A&A, 2019, 627, id.A25
- Popescu Braileanu, B.; Lukin, V. S.; Khomenko, E. “Two-fluid simulations of Rayleigh-Taylor instability in a magnetized solar prominence thread. I. Effects of prominence magnetization and mass loading” A&A, 2021, 646, id.A93
- Popescu Braileanu, B.; Lukin, V. S.; Khomenko, E. “Two-fluid simulations of Rayleigh-Taylor instability in a magnetized solar prominence thread. Effects of collisionality” A&A, 2021, 650, id.A181