

# Bayesian Stokes inversion with Normalizing flows

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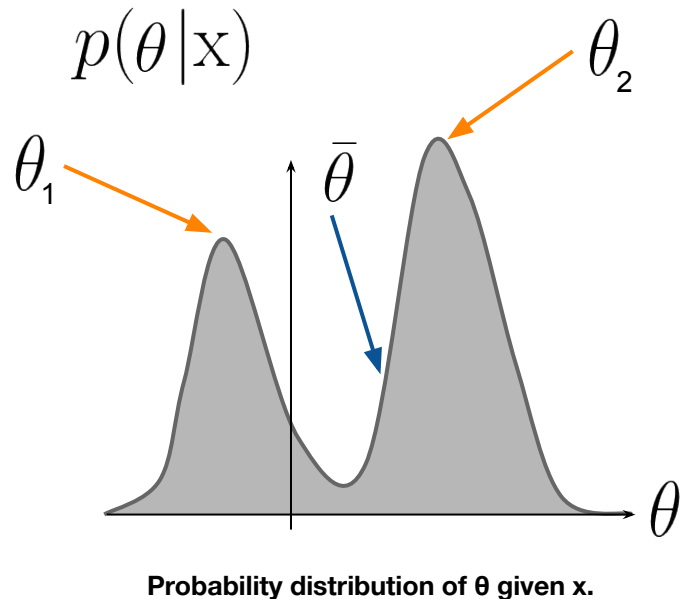
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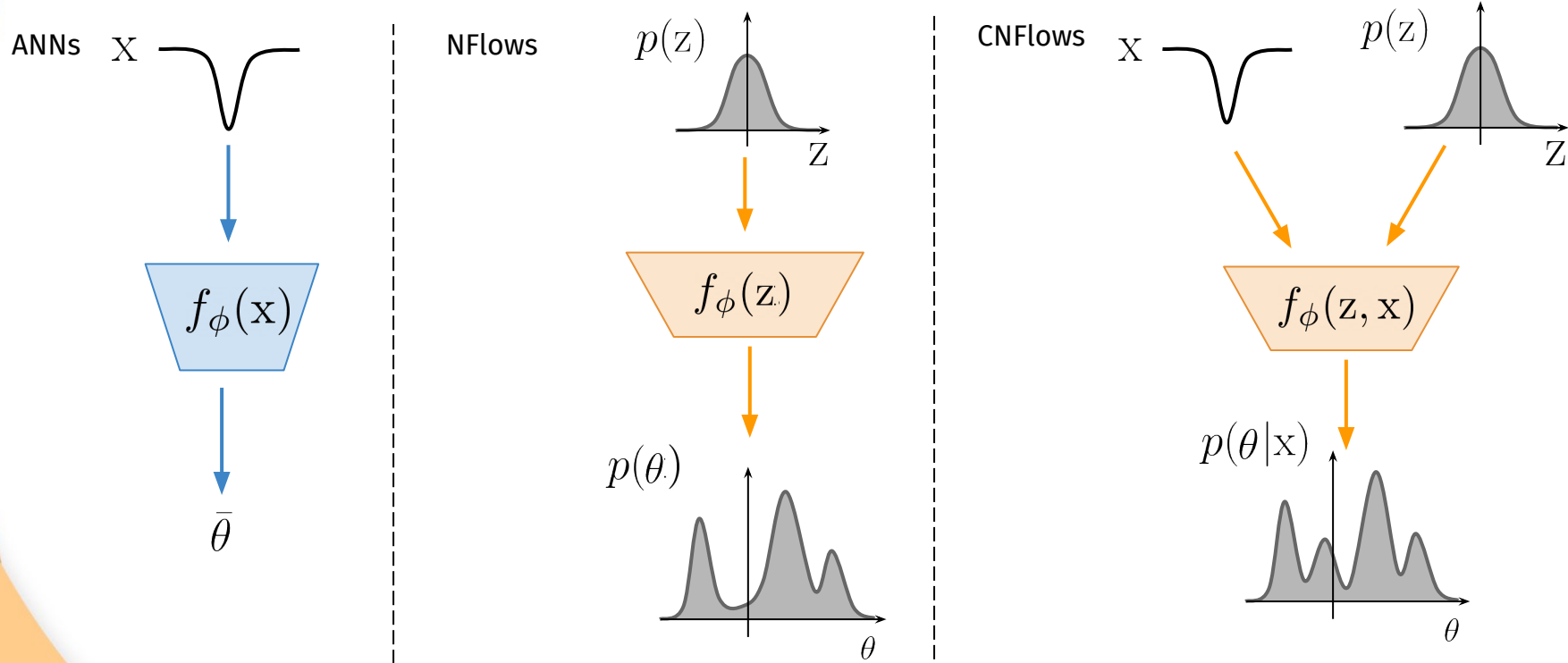
# Introduction

- Inversion codes estimate the **maximum likelihood values (best fit)**.
- Standard neural networks **are much faster but learn the “average” mapping**.
- Bayesian inference give us much more information: **uncertainty, correlations, multimodality, etc.**
- Bayesian sampling methods are very computationally expensive.



Is there any way to perform fast Bayesian inference?

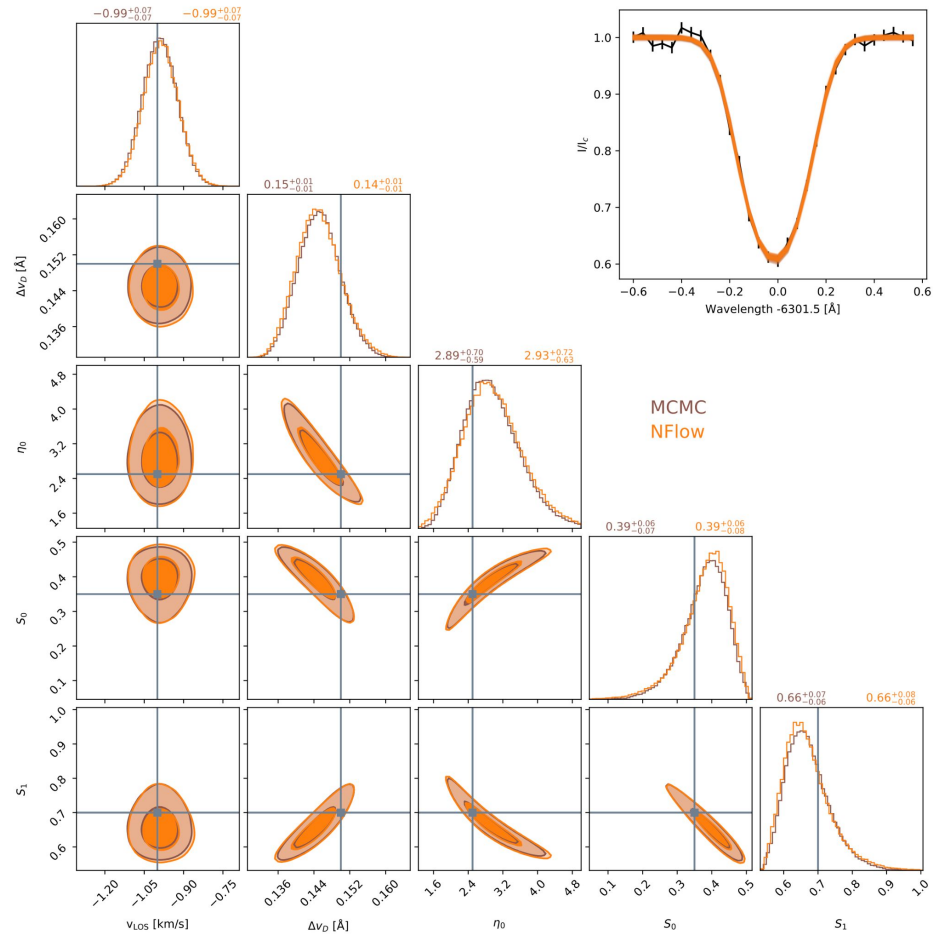
# Normalizing flows (Rezende & Mohamed 2015, Dinh et al. 2016)



Normalizing flows transform a simple distribution into an approximation of any other complex distribution.

# Milne-Eddington model

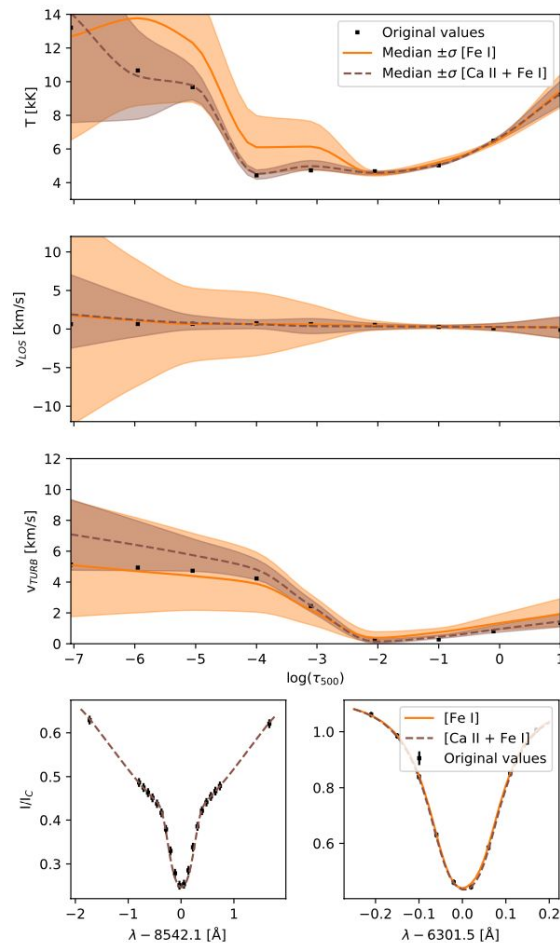
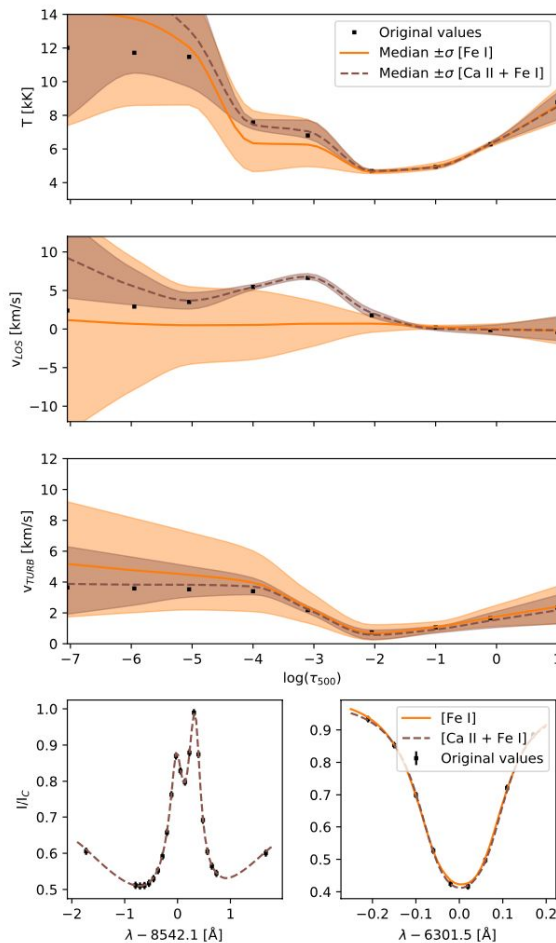
- We have created a database of  $10^6$  pairs of samples (parameters vs spectra).
- Once trained, **NFlow** can get the distribution for any given observation as accurate as the **MCMC** sampling.



Joint and marginal posterior distributions for the physical parameters involved in the Milne-Eddington model.

# N-LTE inversion

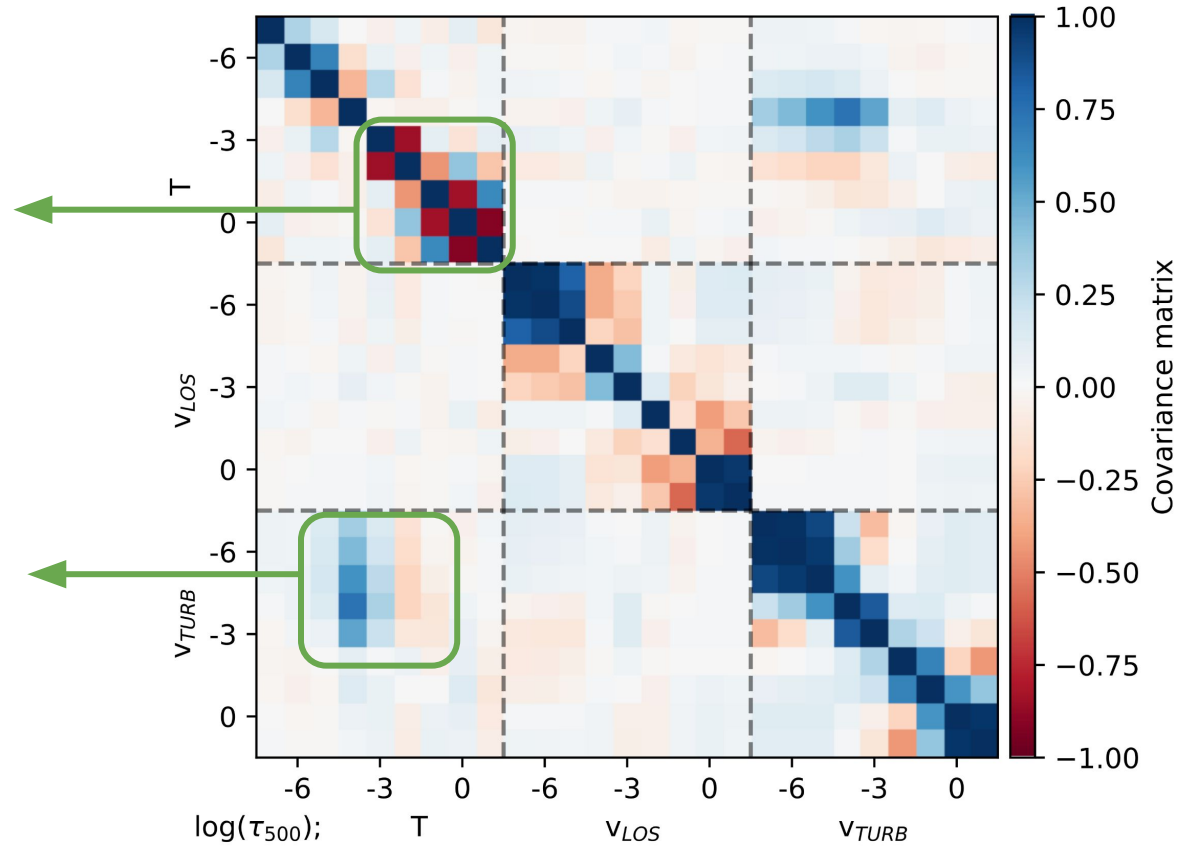
- Two flows were trained:
  - **the orange solution is inferred only using the Fe I line**
  - **the brown solution also uses the Ca II profile.**
- Just from the database, the flow learns the range of sensitivity of each line given by width of the solution.
- It takes 1 second (producing  $10^4$  samples) while an MCMC would take hours/days.



Atmospheric stratification. The colored bands of each curve indicate the standard deviation of each distribution.

# N-LTE inversion

- We found checkerboard patterns associated with changes in temperature that can produce a similar fit.
- We found correlations between the broadening of the microturbulent velocity and the temperature.



Correlations between different physical quantities and locations along the stratification for a N-LTE inversion.

# Summary and perspectives

- A promising approach for inferring the parameter values and uncertainty in spectroscopic inversions.
- Next step is to extend it to magnetic field inference from polarimetric data.
- Given the generality of the technique, it can be applied to other inverse problems.

More details in the manuscript:

<https://arxiv.org/abs/2108.07089>

The source code is at

<https://github.com/cdiazbas/bayesflows>