



16th  
European  
Solar  
Physics  
Meeting



# HISTORICAL TSI RECONSTRUCTION: A NEW APPROACH

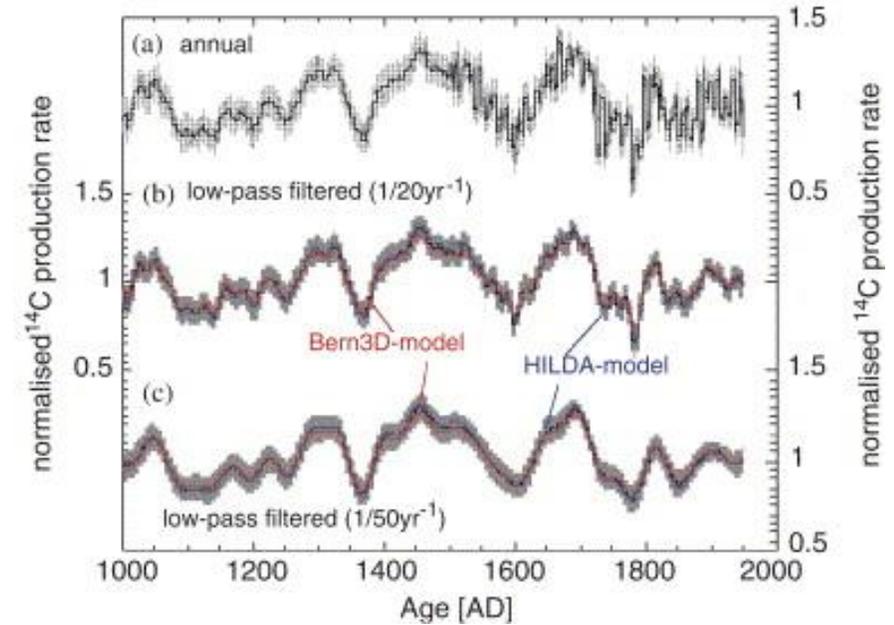
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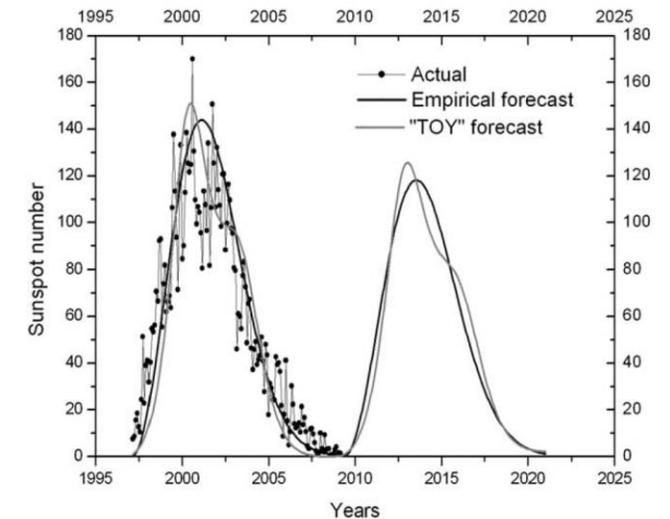
# Model Formulation

- The contribution of sunspot, faculae and quiet sun to irradiance variability is estimated from different components of the solar modulation potential  $\phi$  (Muscheler *et al.*, 2007).
- To estimate the long-term modulation in the TSI, and separate the possible contributions to the TSI of the different solar magnetic structures, we compute the temporal modes present in the solar potential  $\phi$  to determine the principal components and to carry out appropriate reconstructions that dismiss common components.
- To separate the components of different time scales and therefore extract the trend in the variability of the solar potential  $\phi$  we use the empirical mode decomposition (EMD) algorithm (Huang *et al.*, 1998).
- To estimate the time dependence of the bright (plage/network) and dark (sunspot) area coverages we describe each cycle through a monoparametric functional form (Volobuev, 2009).



The Shape of The Sunspot Cycle: A One-Parameter Fit

329



**Figure 7** Predicted shape of the cycles #23 and 24. "Actual" is for the Monthly International Sunspot Number. "Empirical forecast" uses the empirical one-parameter fit, Equations (5), (9). "TOY" forecast uses the one-parameter fit with the functional derived from the "TOY" dynamo Equation (11).

We characterize the cycles through the monoparametric functional form

(Volobuev, 2009, *Solar Physics*, 258, 319):

$$x_k(t) = \left( \frac{t - T0_k}{Ts_k} \right)^2 e^{-\left( \frac{t - T0_k}{Td_k} \right)^2} \quad \text{for } T0_k < t < T0_k + \tau_k$$

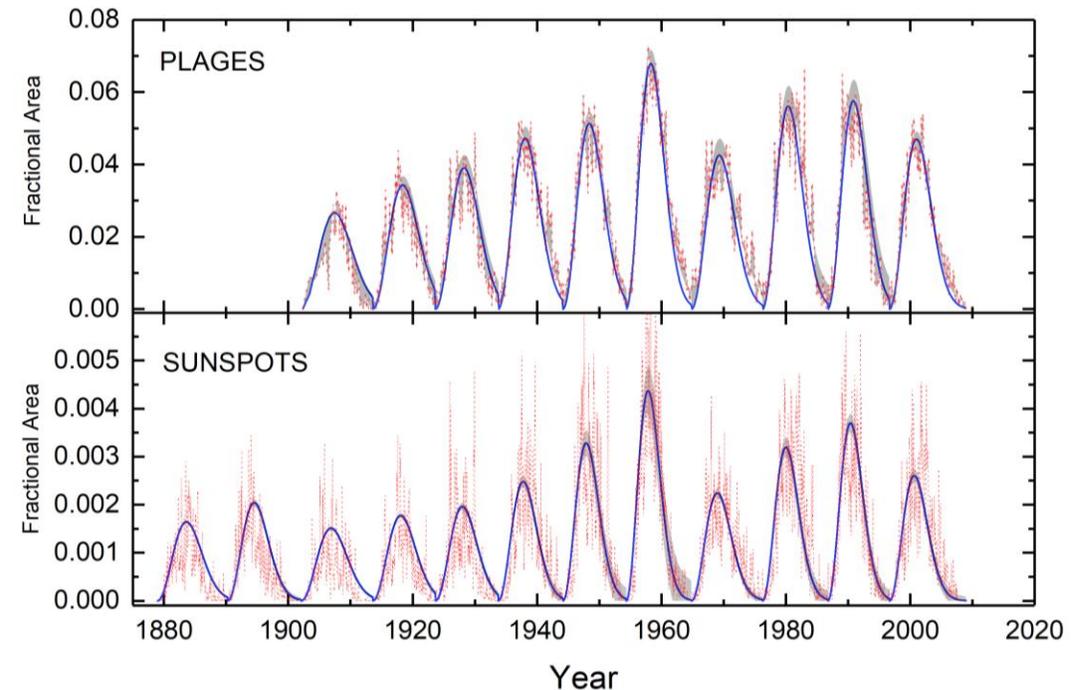
$T0_k$  = initial time of k-cycle

$\tau_k$  = duration of k-cycle

Each cycle proxy  $A(t)$  can be reconstructed once the  $Ts_k$  parameters are known, because  $Td_k$  and  $Ts_k$  are related to each other. We obtain  $Ts_k$  values from a parametric fit of **plage and sunspot composites** (Chatzistergos et al., 2019, *A&A*, 625, 22; Mandal et al., 2020, *A&A*, 640, A78)

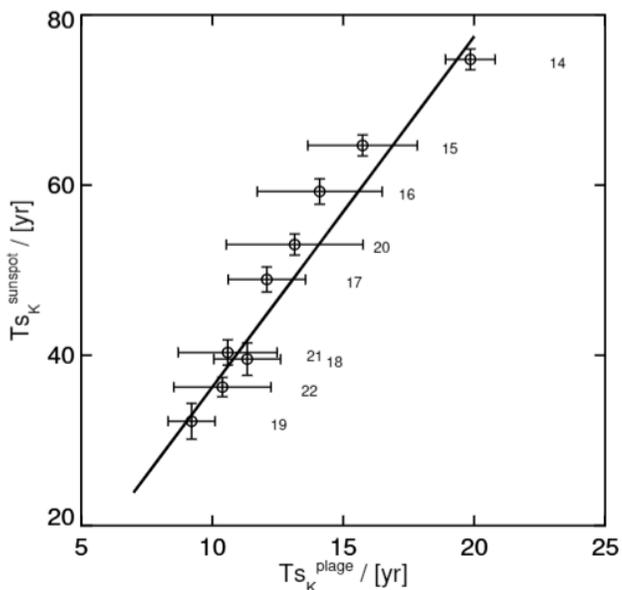
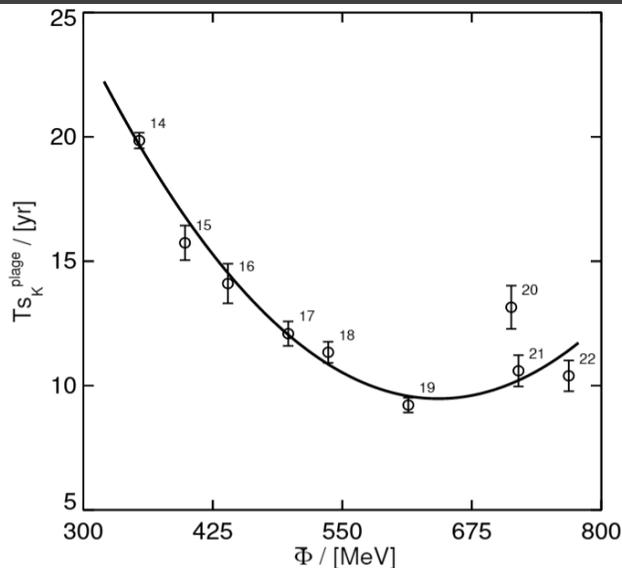
COMPARISON  
BETWEEN DATA AND  
PARAMETRIC  
RECONSTRUCTION

$$A(t) = \sum_k x_k(t)$$



The correlation between the parameters  $T_{S_k}$  (plage and sunspots) and the correlation with the Solar Modulation Potential  $\phi$  (integrated over the k-cycle) are used for the plage and sunspot area coverage reconstructions.

We use the annual estimates of the Solar Modulation Potential derived from the analysis of the  $^{14}\text{C}$  (Muscheler et al. 2007).



$\Phi_k$



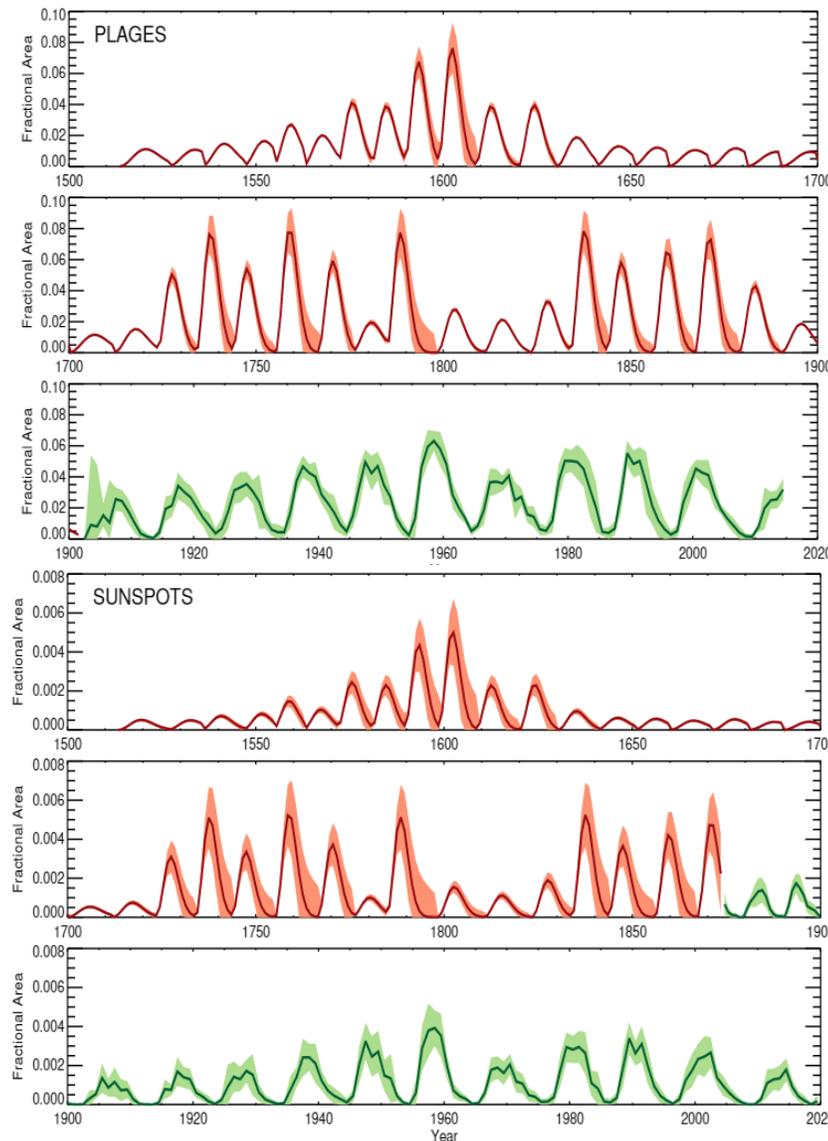
$T_{S_k} \text{ (plage)}$



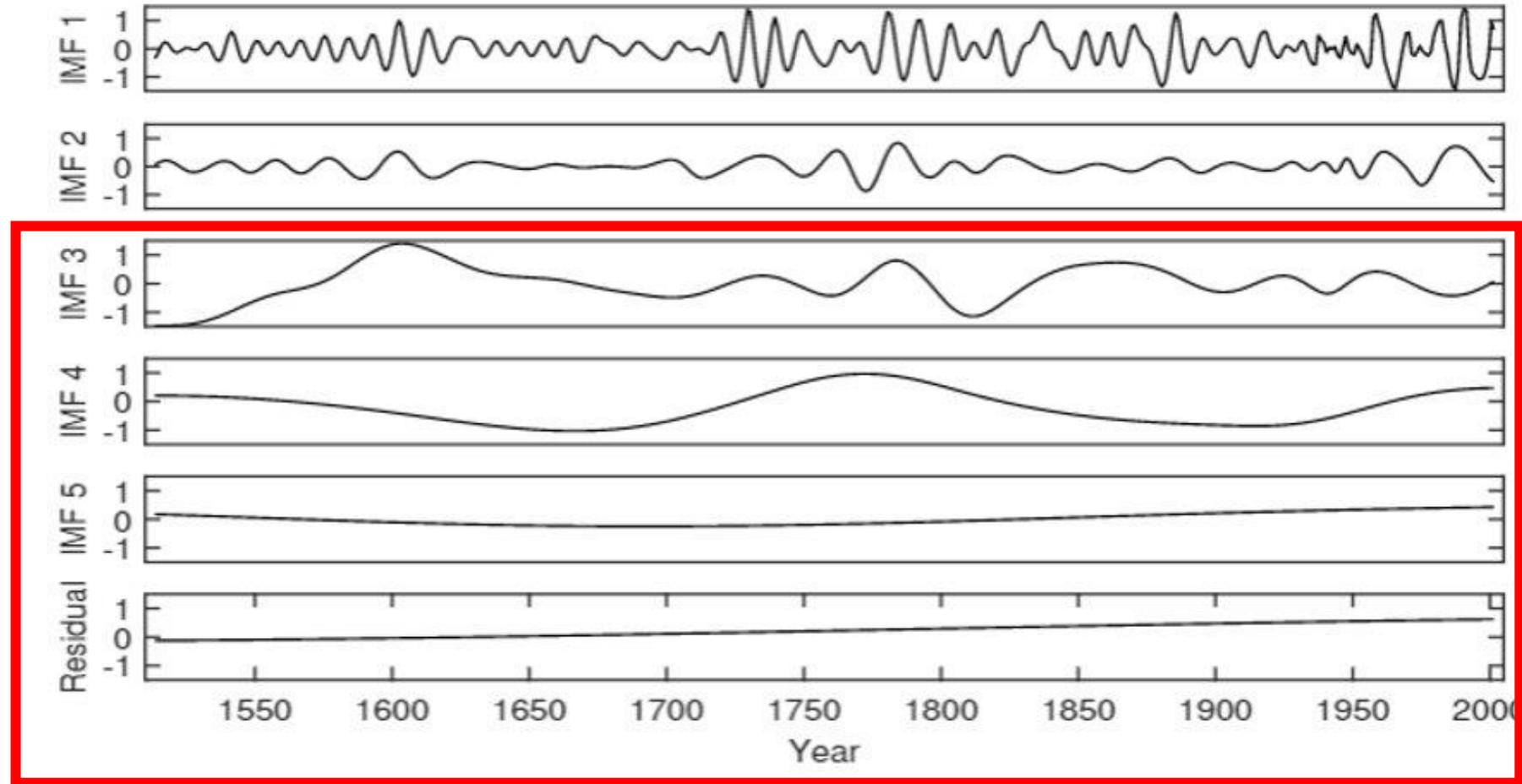
$T_{S_k} \text{ (sunspot)}$



$\alpha_p(t)$  and  $\alpha_s(t)$

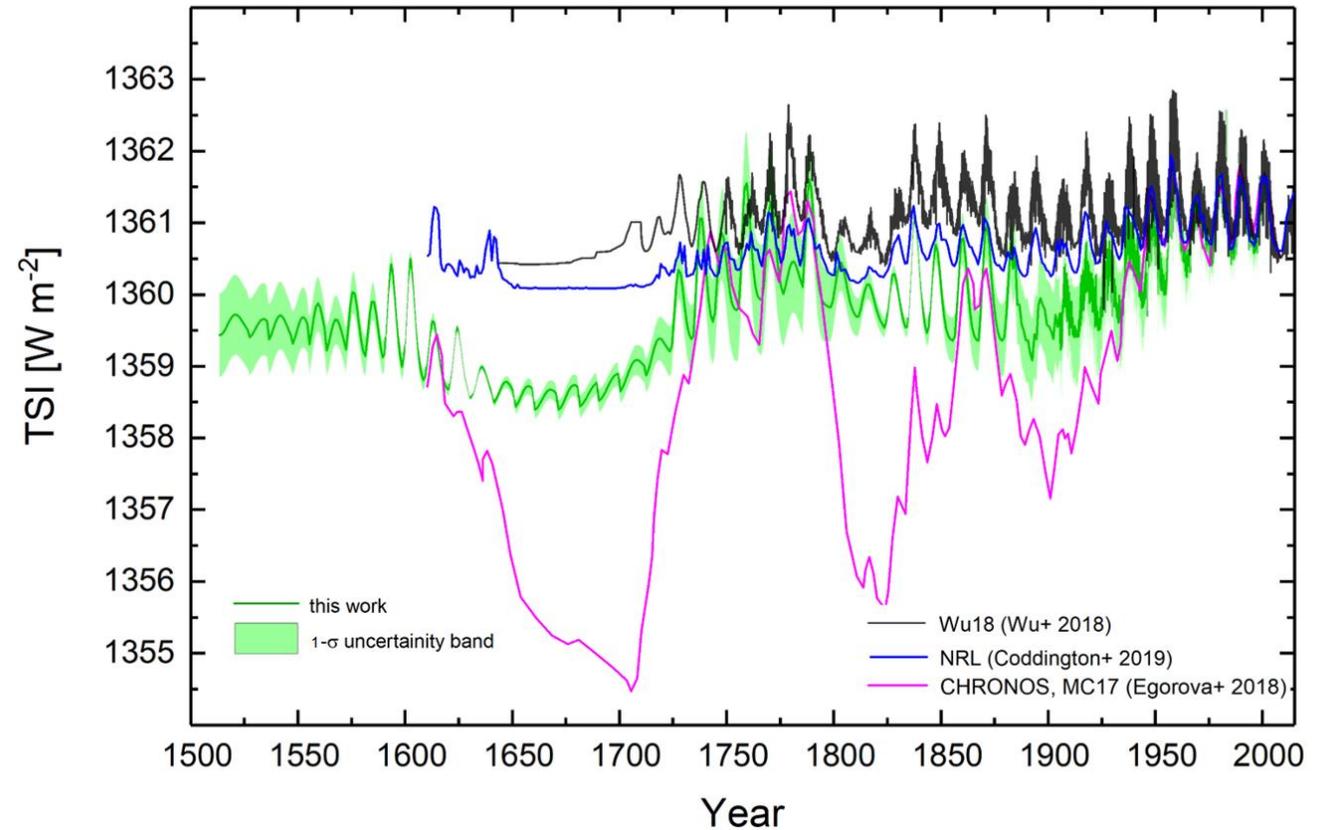


Empirical  
Mode  
Decomposition  
of  
Solar  
Modulation  
Potential



To capture the low-frequency modulation from the solar function  $\phi$  : 
$$\sum_{i=3}^5 C_i \cdot IMF_i(t) + C_R \cdot R(t)$$
 the signal  $\phi$  is primarily decomposed as superposition of simpler quasi-periodic components called Intrinsic Mode Functions (IMFs).  $C_i$  are the weights associated with the different IMFs derived from the EMD procedure.

# TSI RECONSTRUCTION



$$\delta F(t) = \underbrace{C_n \text{mod}(\phi)}_{\text{Long-term component}} + \underbrace{\alpha_f \delta_{fn}}_{\text{Bright component}} + \underbrace{\alpha_s \delta_s}_{\text{Dark component}}$$

Long-term component

Bright component

Dark component

The contrasts ( $\delta$ ) and  $C_n$  are derived by fitting the TSI PMOD composite (1985-2010)

# Conclusions

- We reconstruct, cycle for cycle, the plage and sunspot coverage from 1513 to 2000, by using correlation between the cycle parameter and Solar Modulation Potential  $\phi$
- We derive a low-frequency modulation through the Empirical Mode Decomposition of the Solar Modulation Potential  $\phi$
- We reconstruct the Total Solar Irradiance from 1513 to 2000. The obtained TSI shows an intermediate behavior if compared to the many reconstructions proposed in the literature.
- In particular we find a modulation of the facula and spots coverage in the Maunder minimum. This minimum has an average difference of approximately  $2.5 \text{ W m}^{-2}$  with respect to the current TSI value.
- In the first half of the last century (1900-1950) we observe a growth of the TSI of about  $1.5 \text{ W m}^{-2}$ .