

# Stellar and Exoplanetary Atmospheres

## Bayesian Analysis Simultaneous Spectroscopy



Giuseppe Morello

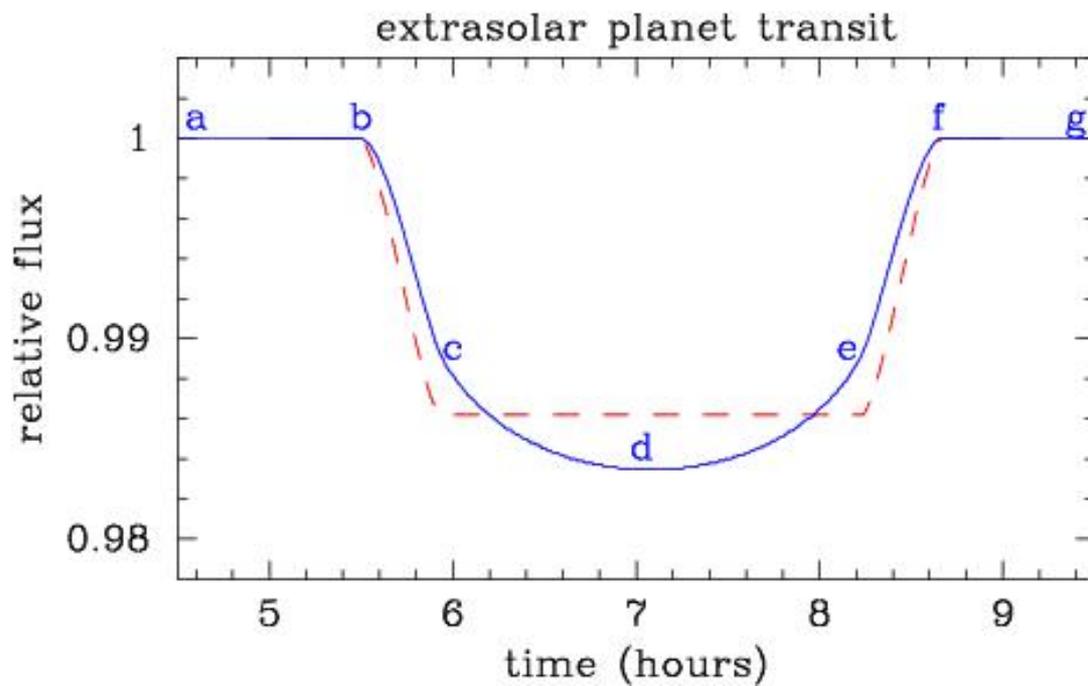
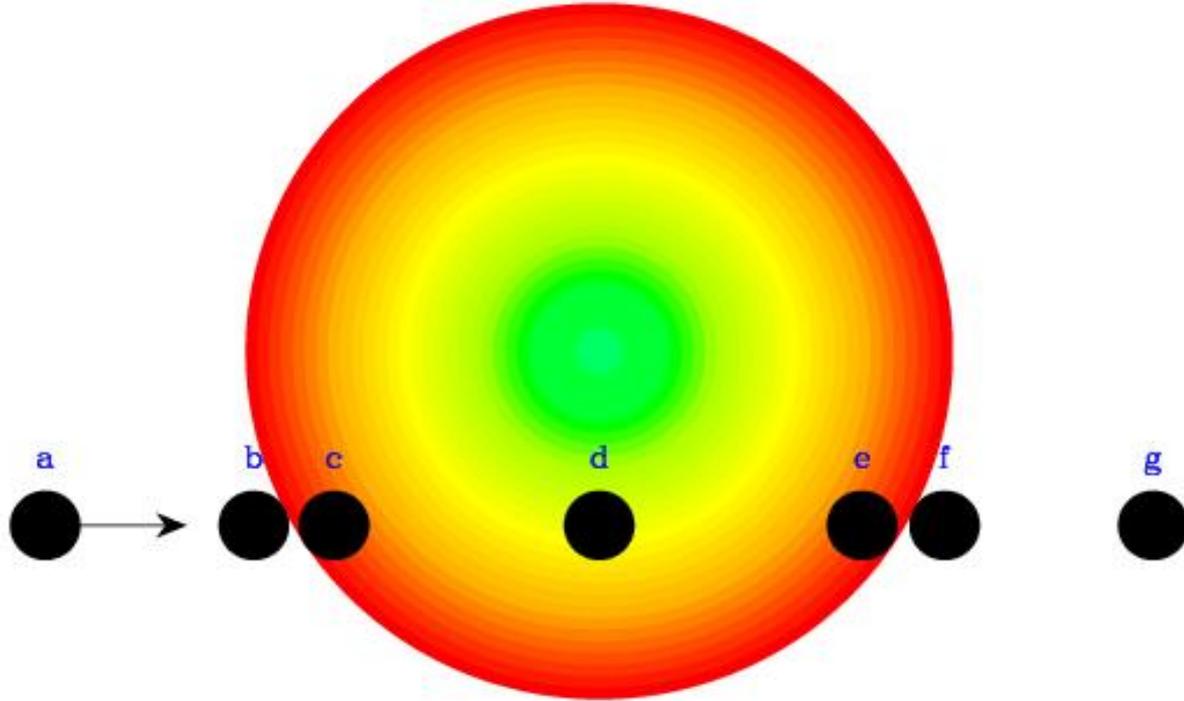
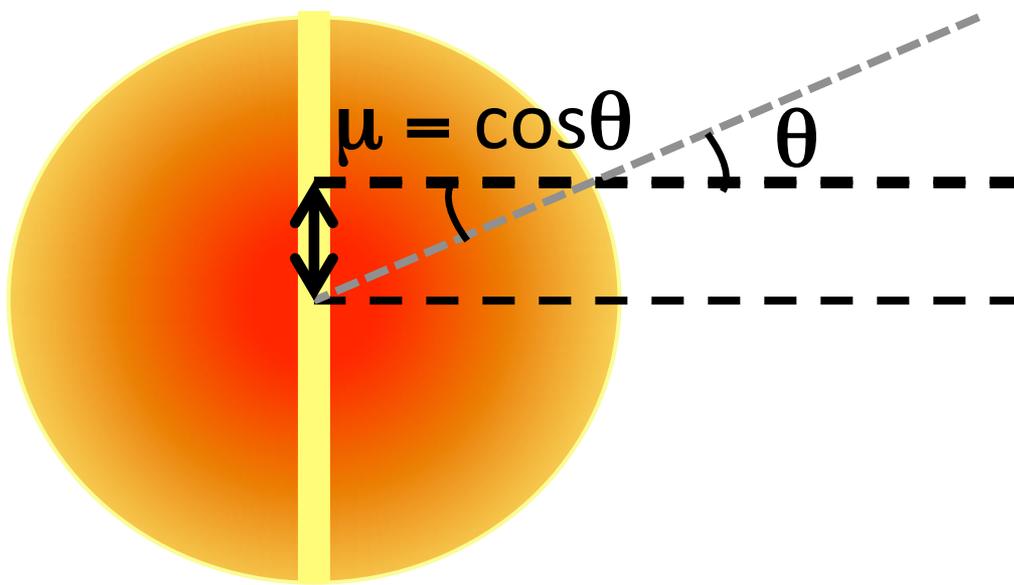


Image credit:  
Coughlin, J. F.  
(PhD thesis)



observer

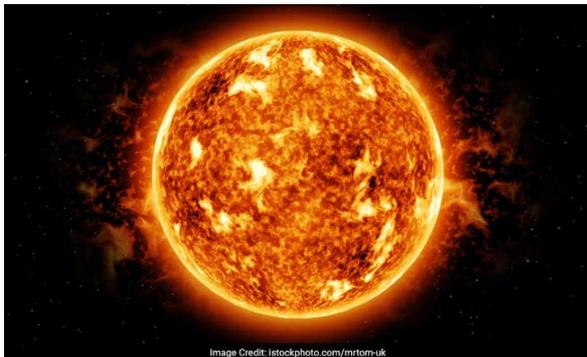
### Limb-darkening laws

}	2-coefficients	Quadratic	$\frac{I_\lambda(\mu)}{I_\lambda(1)} = 1 - u_1(1 - \mu) - u_2(1 - \mu)^2$	
	Square-root	$\frac{I_\lambda(\mu)}{I_\lambda(1)} = 1 - v_1(1 - \sqrt{\mu}) - v_2(1 - \mu)$		
	<b>NEW</b> Power-2	$\frac{I_\lambda(\mu)}{I_\lambda(1)} = 1 - c(1 - \mu^\alpha)$		
	Claret-4	$\frac{I_\lambda(\mu)}{I_\lambda(1)} = 1 - \sum_{n=1}^4 a_n (1 - \mu^{n/2})$		
				Espinoza & Jordan 2016; Morello et al. 2017; Maxted 2018

# Why fitting for the stellar limb-darkening coefficients?

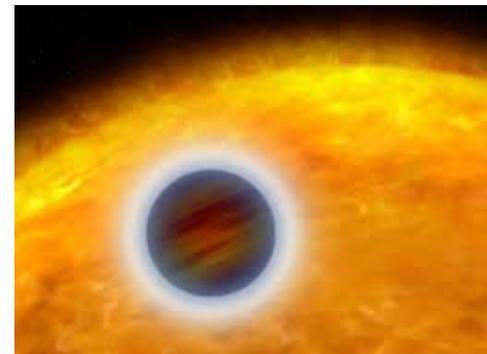
## Stellar science

- Testing the stellar-atmosphere models
- The effect of stellar activity is not well known
- No other techniques are available (in almost all cases)



## Exoplanetary science

- Avoiding potential biases in the exoplanet radius and orbital parameters
- Wrong radius  $\rightarrow$  mean density  $\rightarrow$  structure model
- Avoiding potential biases in the transmission spectrum of the exoplanetary atmosphere



# But

Strong parameter degeneracies may hamper convergence of the light-curve fits

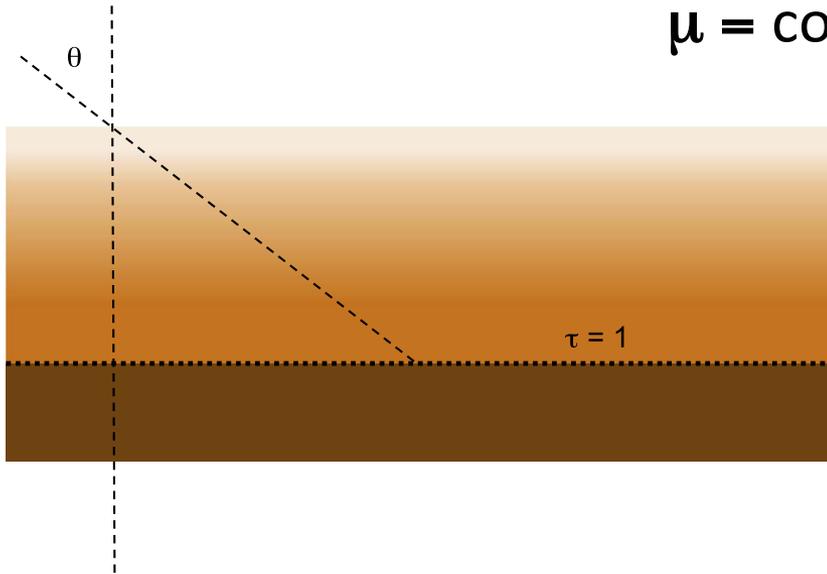


# Impact of geometric approximations



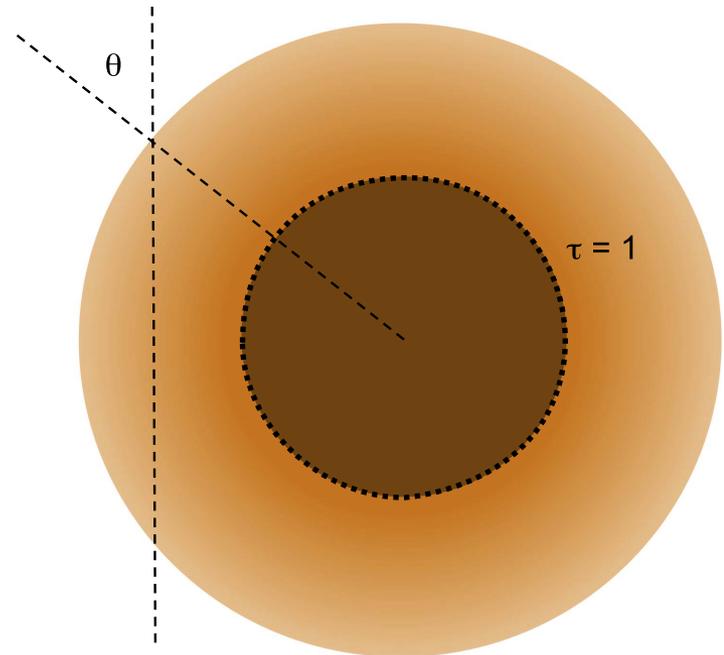
# Geometry of stellar-atmosphere models

Plane-parallel



$$\mu = \cos\theta$$

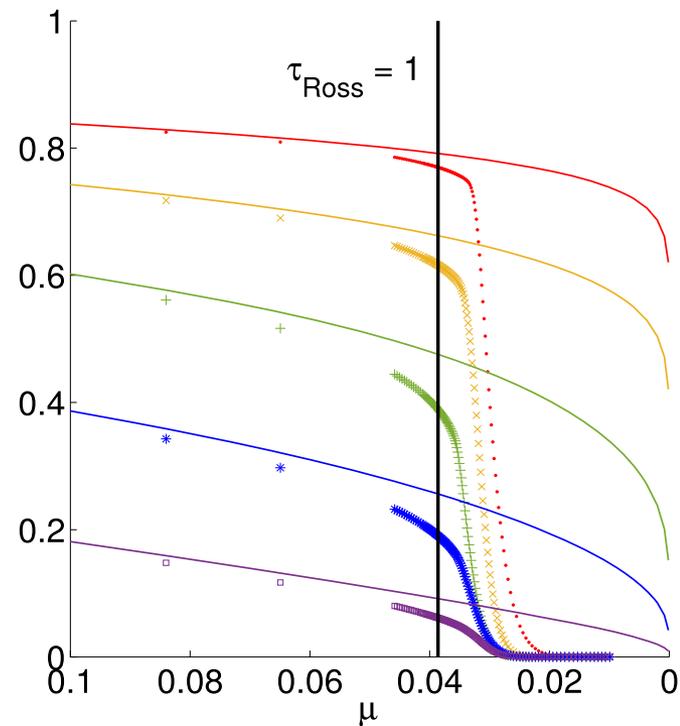
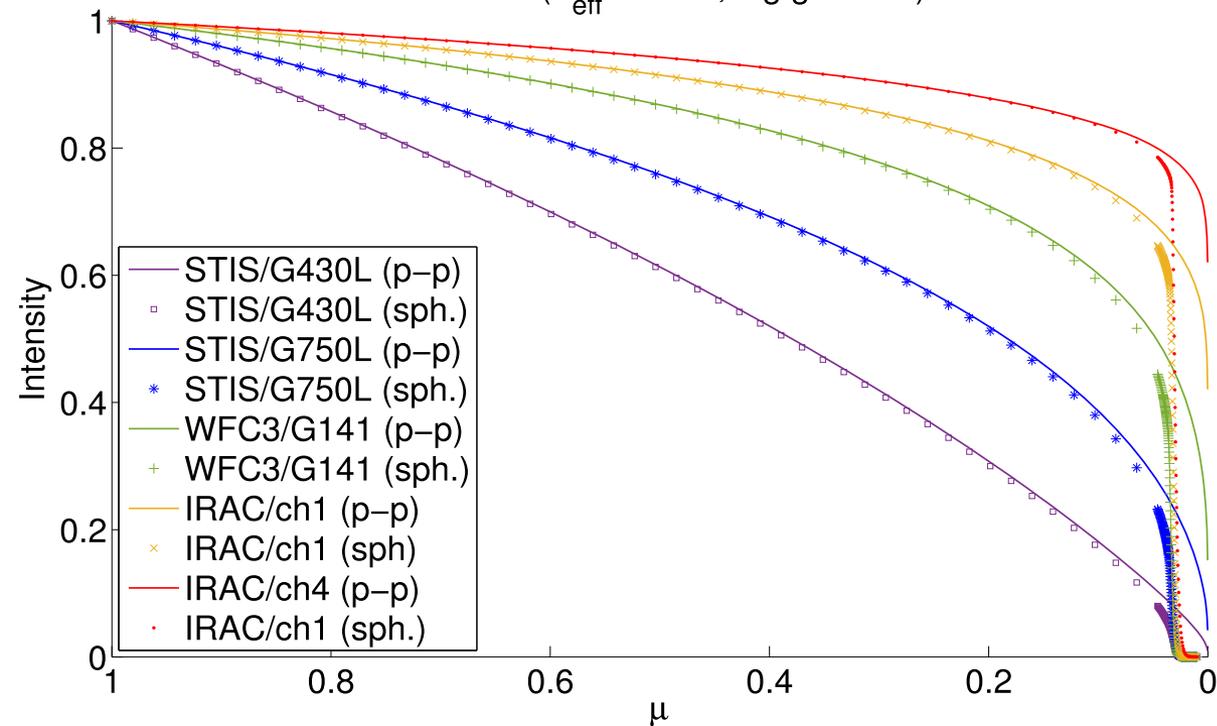
Spherical



# Stellar intensity profiles

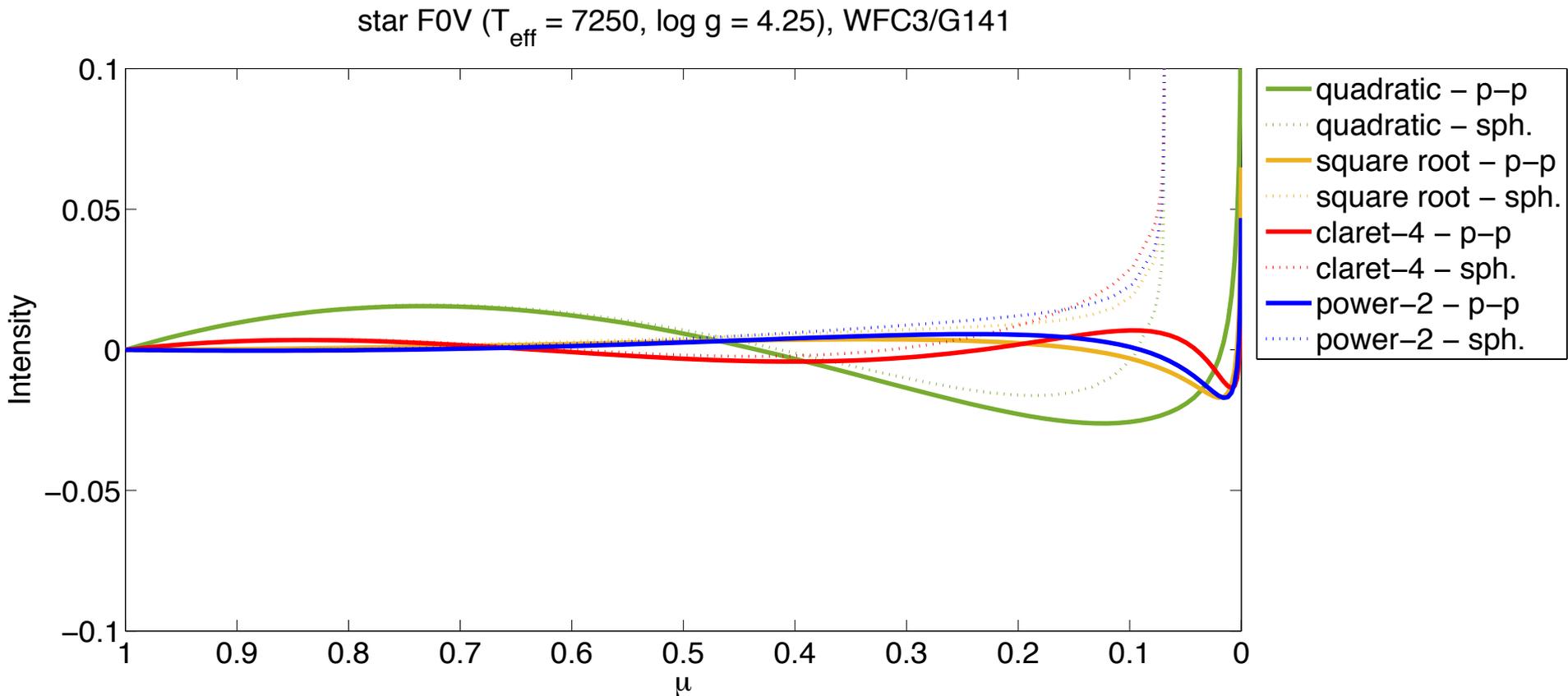
$$\mu = \cos\theta$$

star M5V ( $T_{\text{eff}} = 3084$ ,  $\log g = 5.25$ )



# Parametric intensity profiles (1)

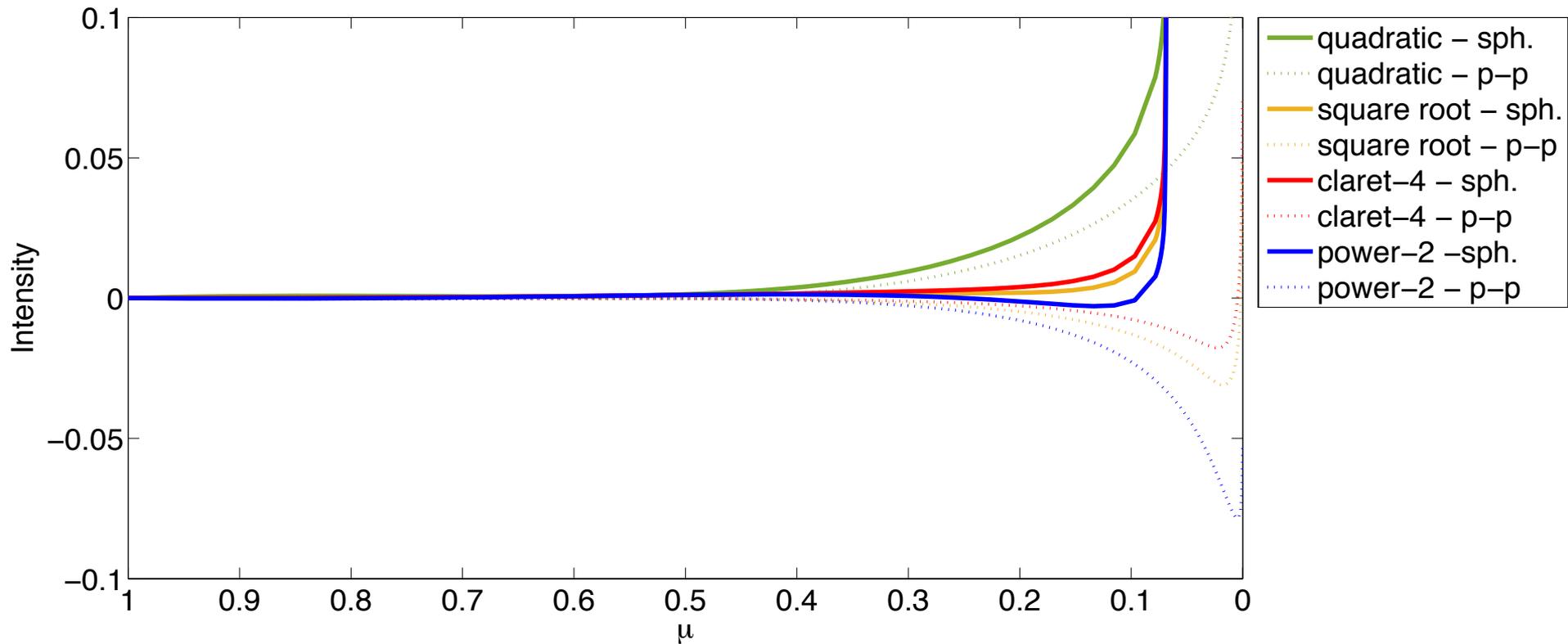
With *theoretical* limb-darkening coefficients (best-fit  $I(\mu)$ )



# Parametric intensity profiles (2)

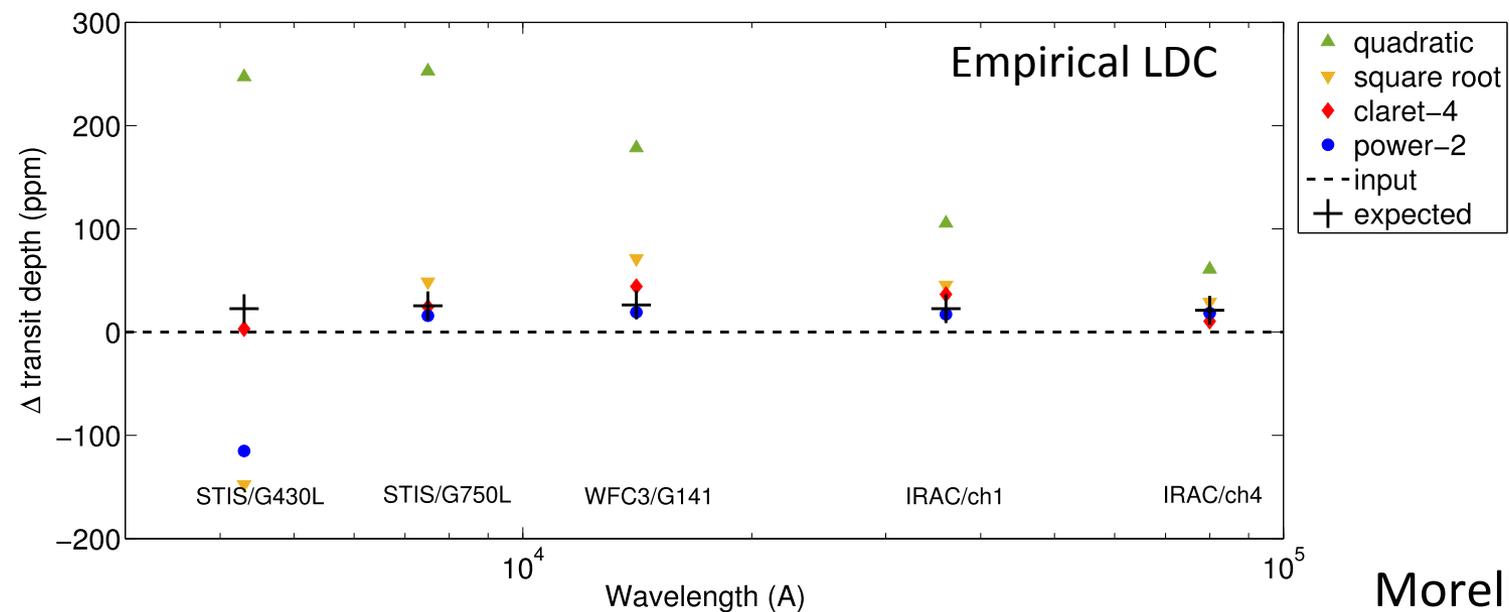
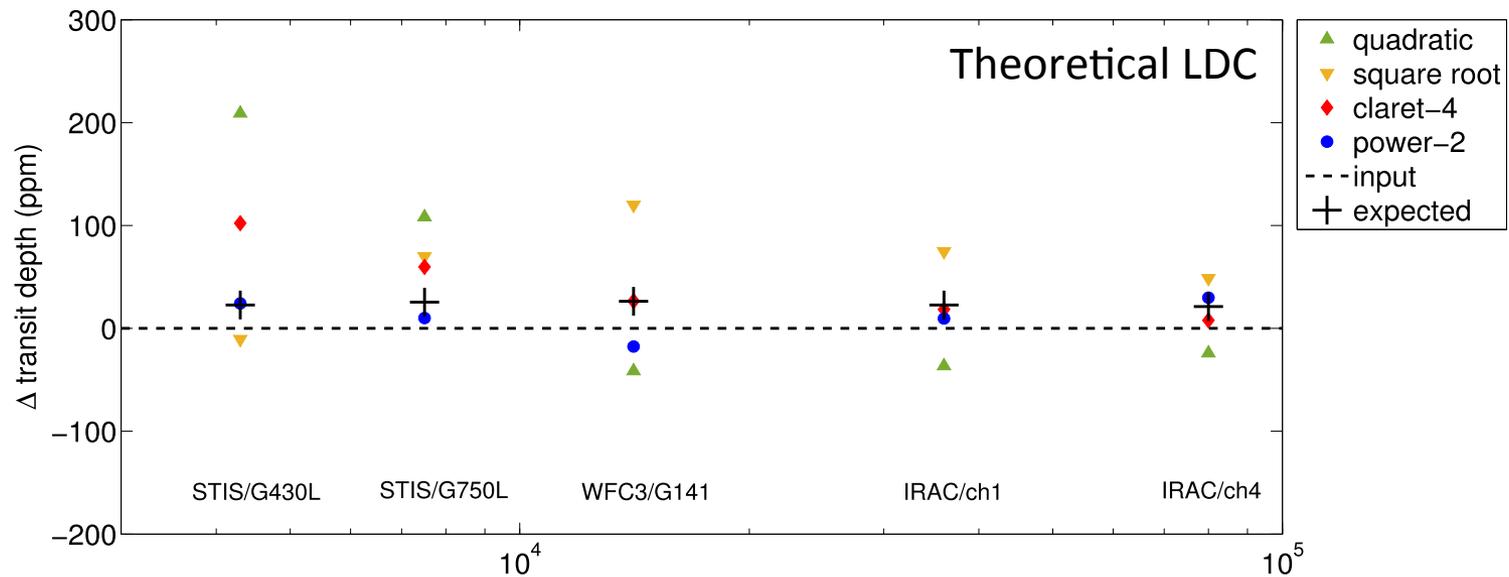
With *empirical* limb-darkening coefficients (best-fit light-curve)

star F0V ( $T_{\text{eff}} = 7250$ ,  $\log g = 4.25$ ), WFC3/G141



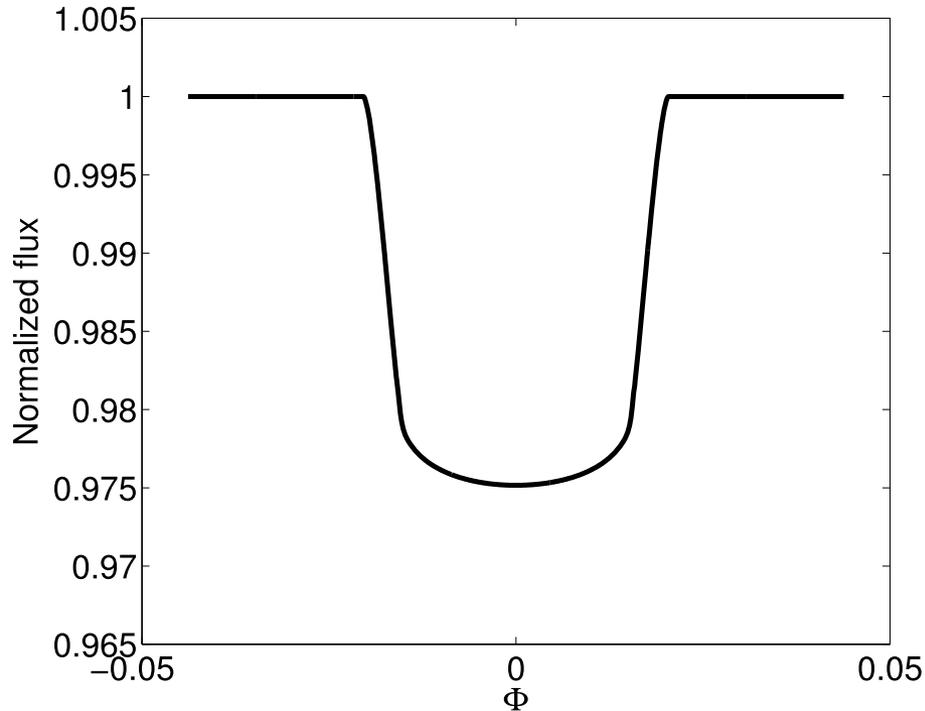
# Transit depth bias

star M5V ( $T_{\text{eff}} = 3084$ ,  $\log g = 5.25$ )

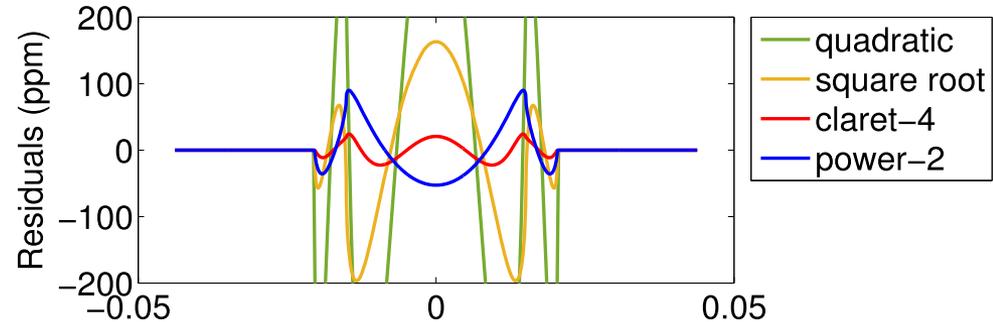


# Transit light-curve models

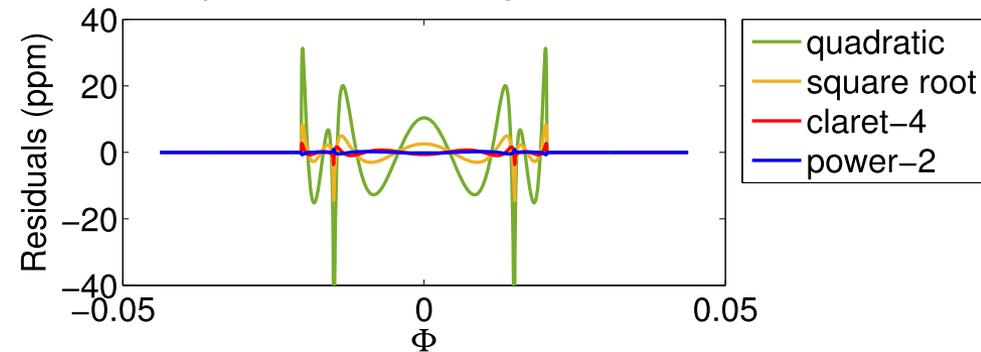
star M5V ( $T_{\text{eff}} = 3084$ ,  $\log g = 5.25$ ), WFC3/G141



Theoretical limb darkening coefficients



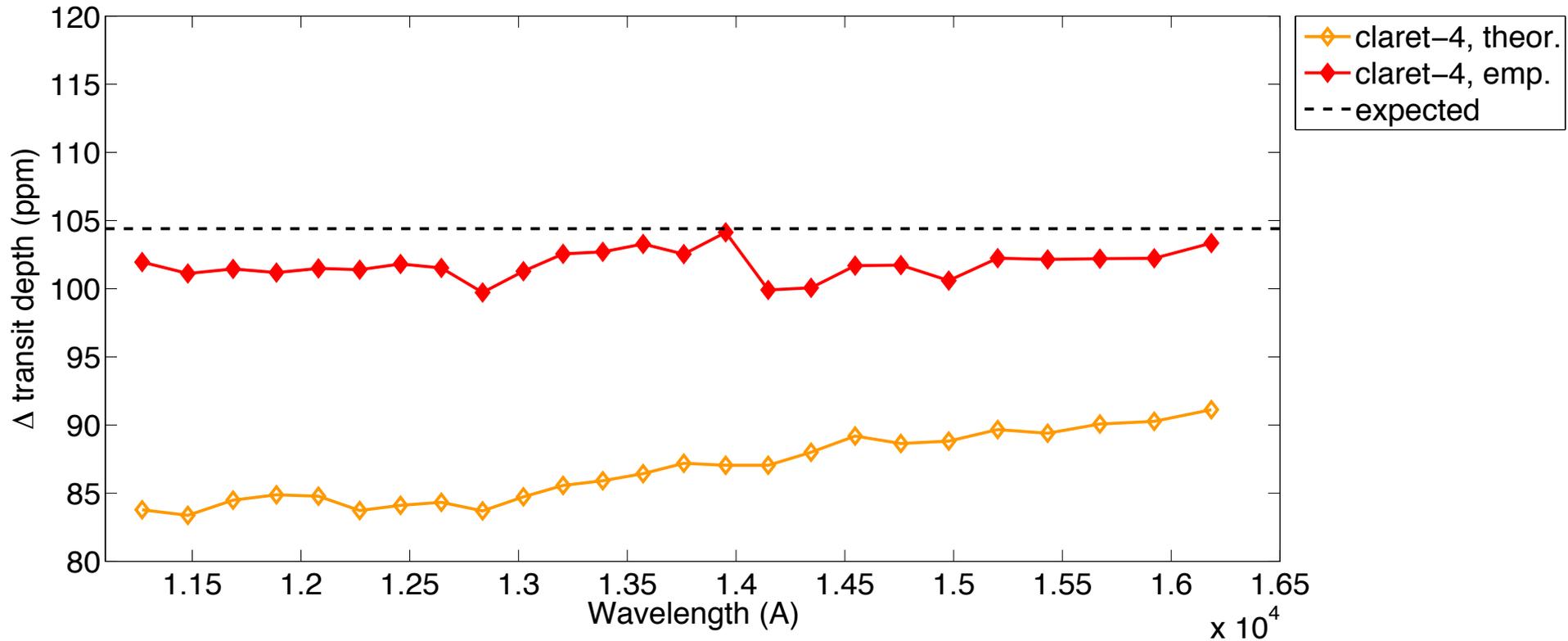
Empirical limb darkening coefficients



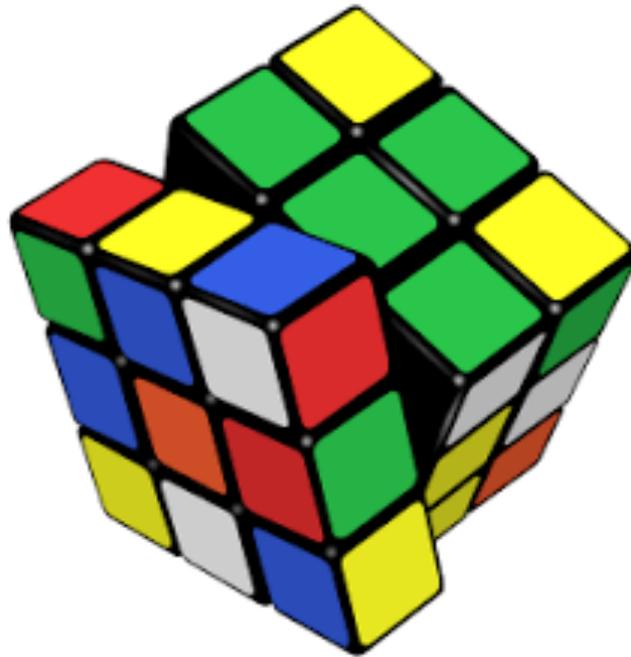
NOTE: Because of parameter degeneracies the transit depth and orbital parameters can be significantly biased even if the fitting residuals are very small!

# WFC3-like exoplanet spectroscopy

star F0V ( $T_{\text{eff}} = 7250$ ,  $\log g = 4.25$ ), WFC3/G141

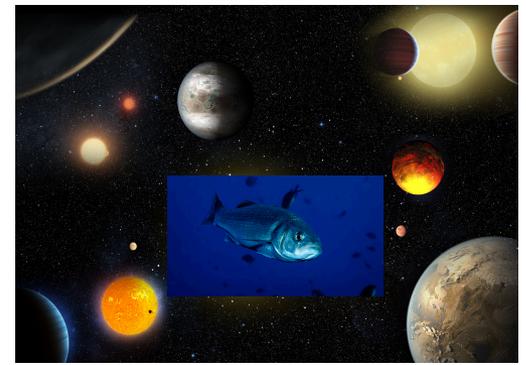


# Methods and results



# SEA BASS

Stellar and Exoplanetary Atmospheres  
Bayesian Analysis Simultaneous Spectroscopy

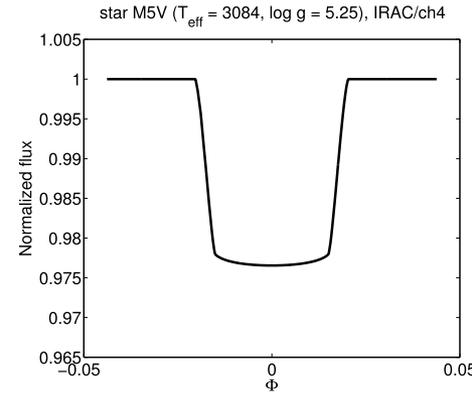


## INFRARED TRANSITS

1

- ✓ Two-coefficient limb-darkening laws,  
or
- ✓ Fixed limb-darkening coefficients

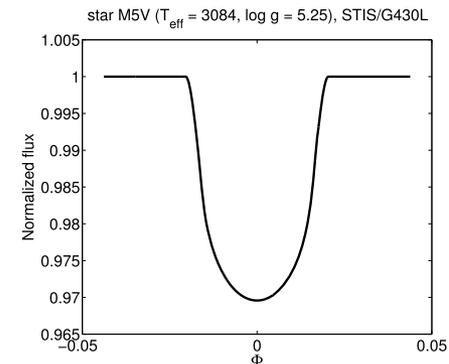
=> geometric parameters (orbital, transit duration)



## VISIBLE/UV TRANSITS

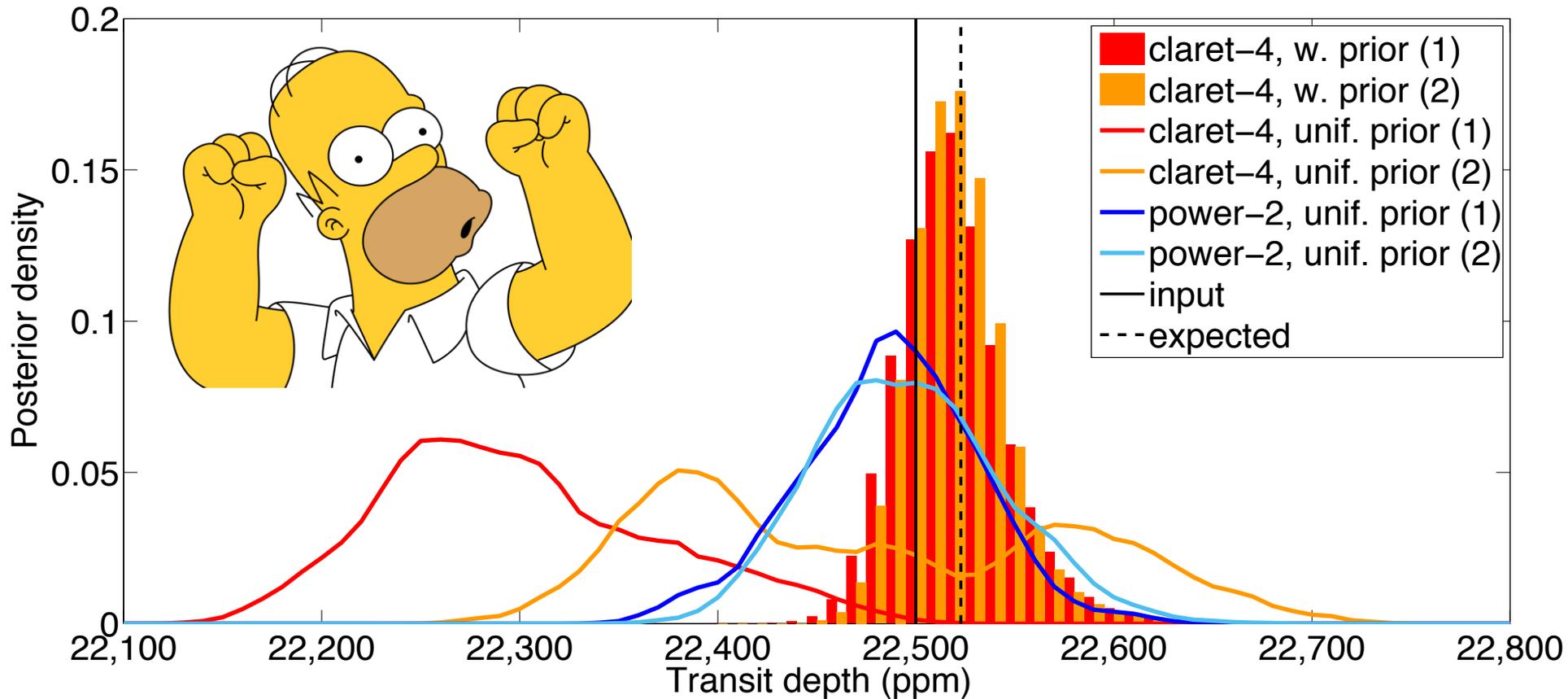
2

- ✓ Informative Bayesian priors on the geometric parameters
- ✓ Fully empirical four-coefficient limb-darkening

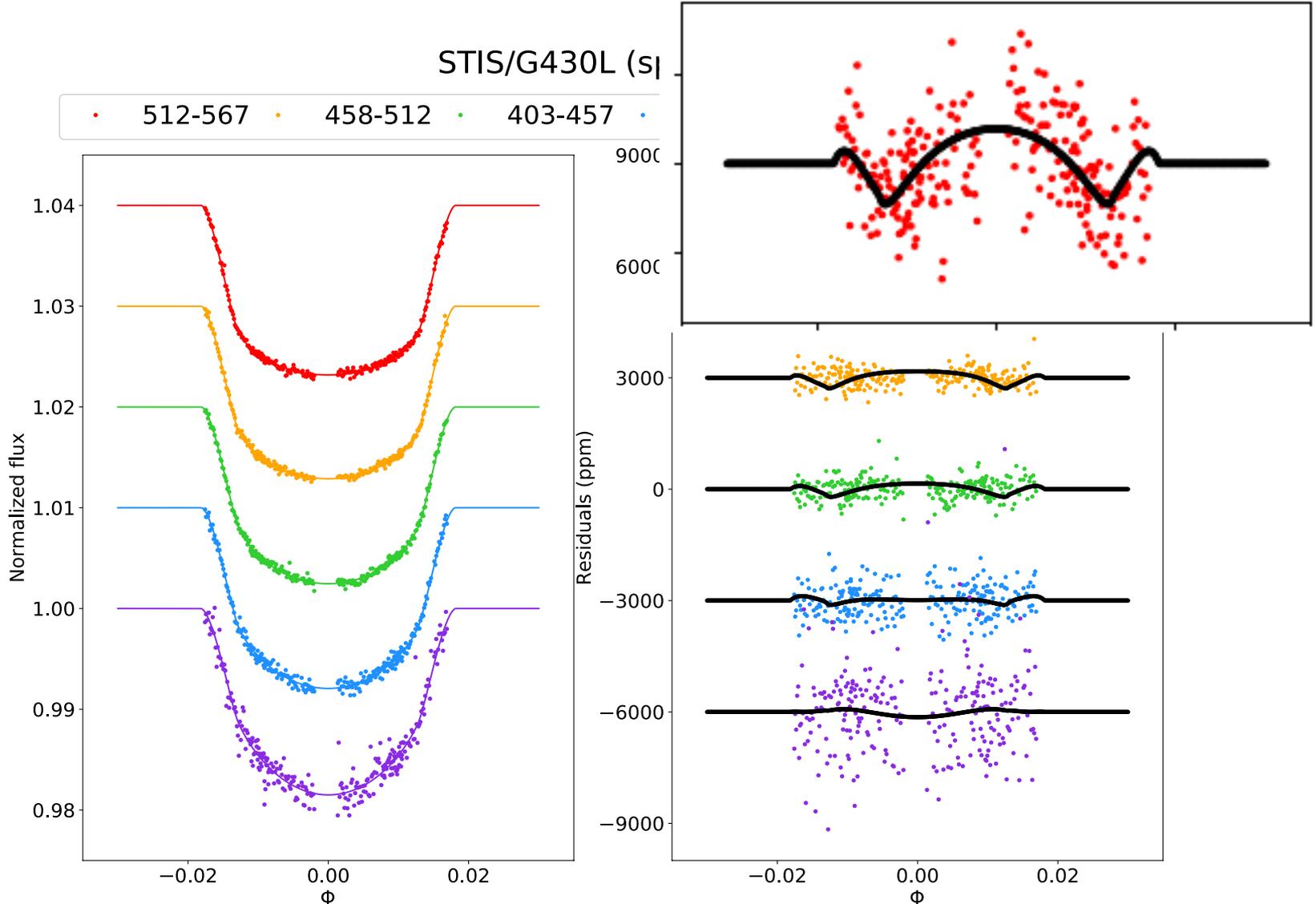


# Simulation results

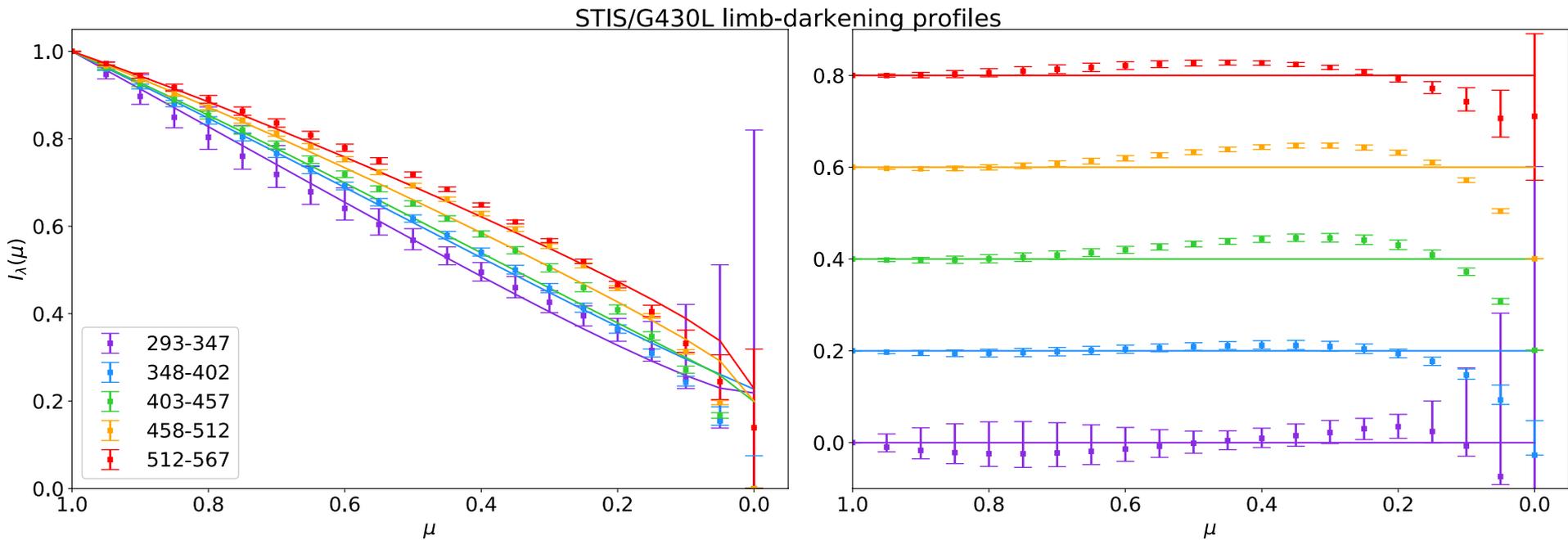
star M5V ( $T_{\text{eff}} = 3084$ ,  $\log g = 5.25$ ), STIS/G430L



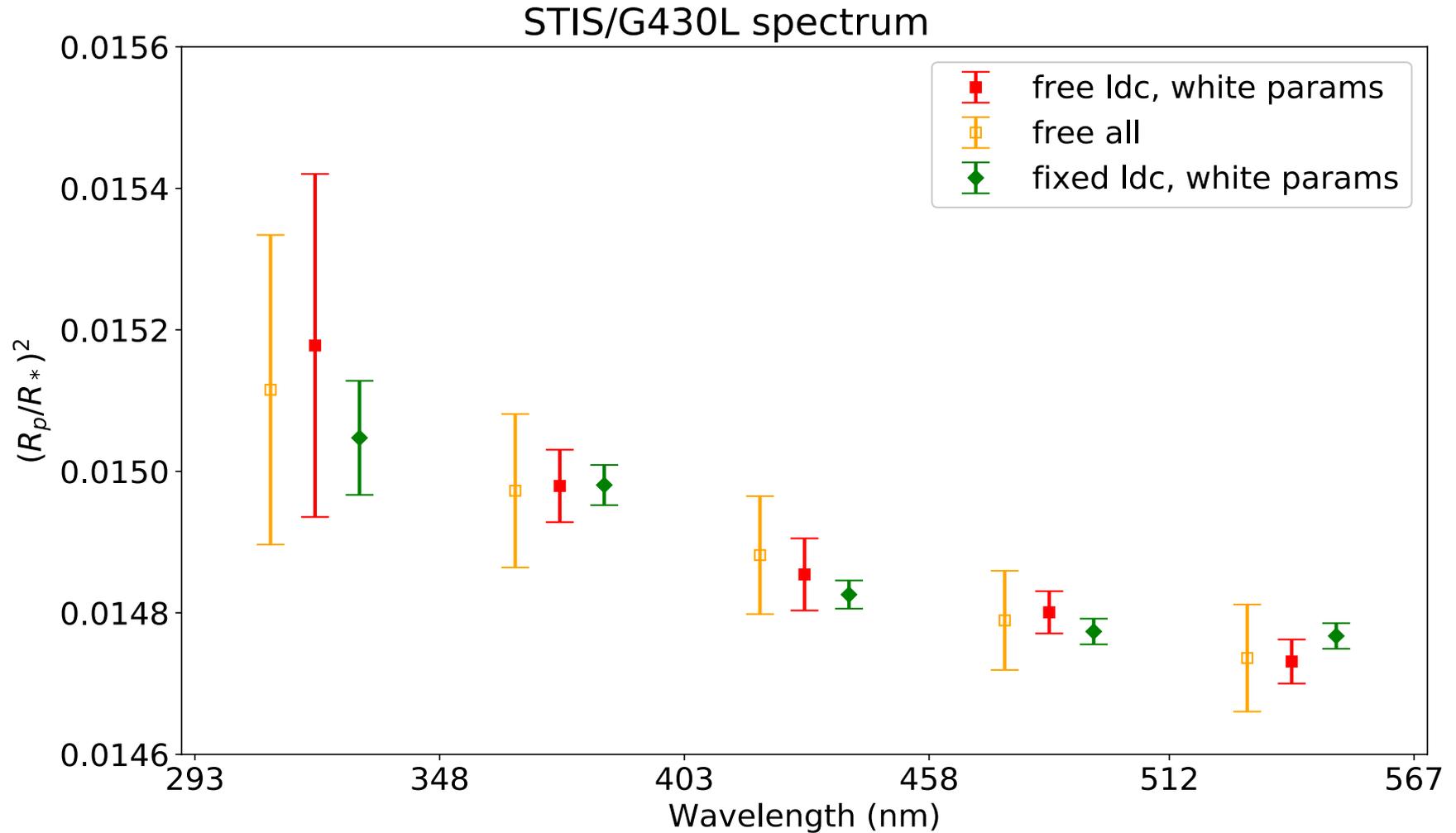
# Spitzer/IRAC + HST/STIS observations (1)



# Spitzer/IRAC + HST/STIS observations (2)

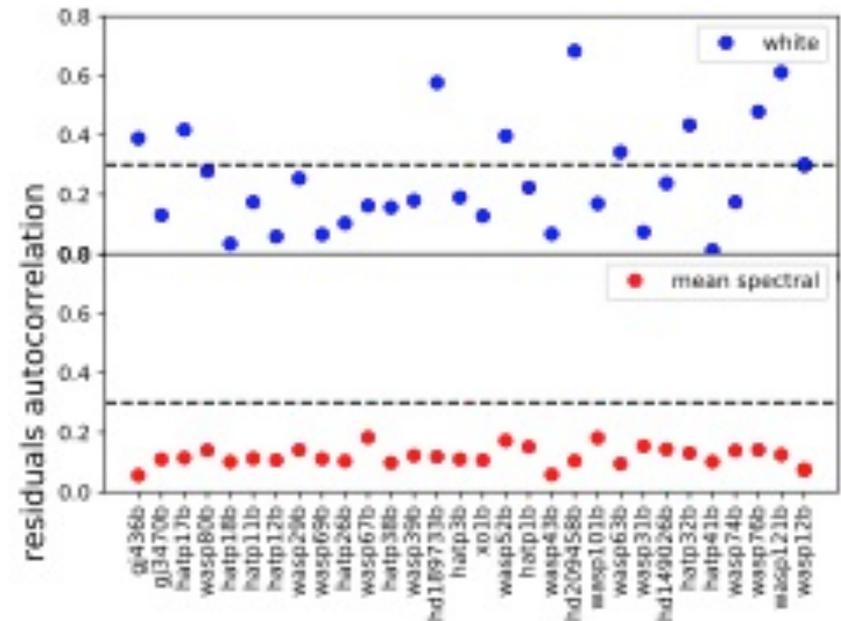
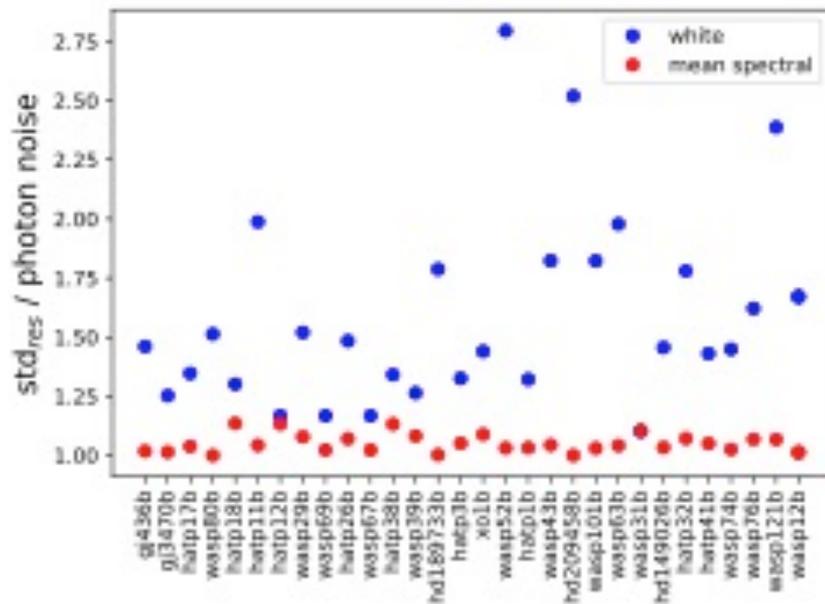


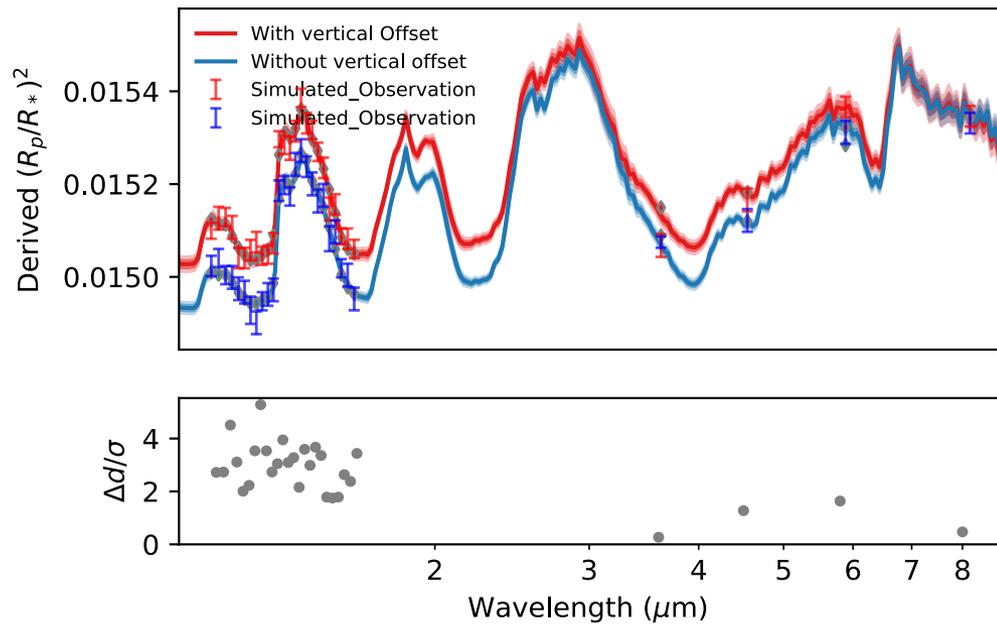
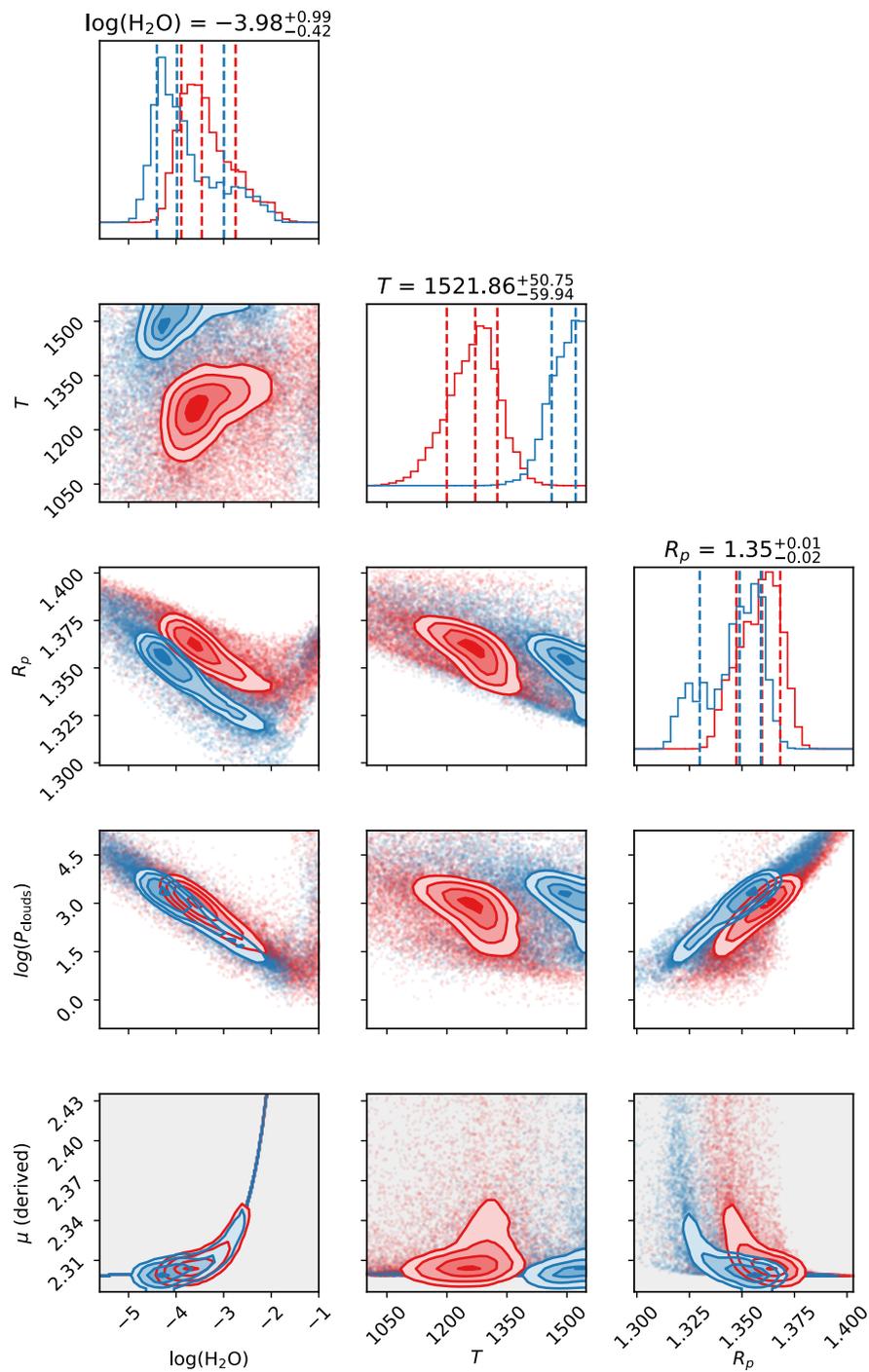
# Spitzer/IRAC + HST/STIS observations (3)





~50% of *HST*/WFC3 transits have systematic residuals when limb-darkening is not fitted

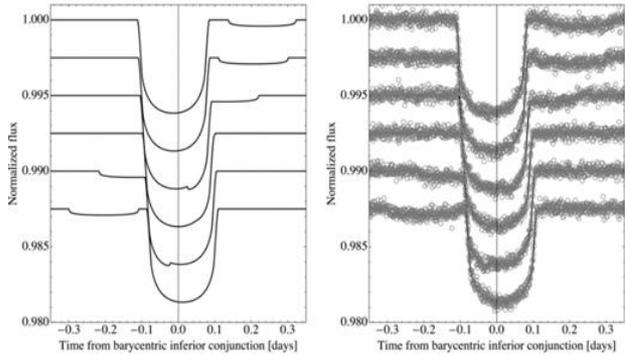
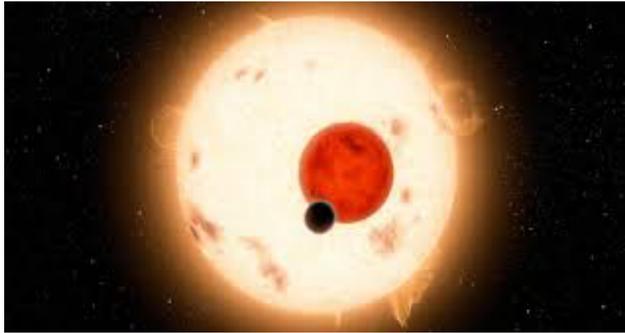




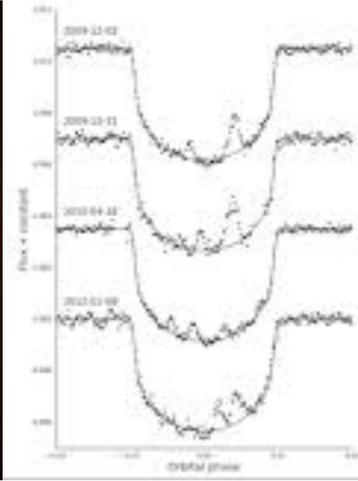
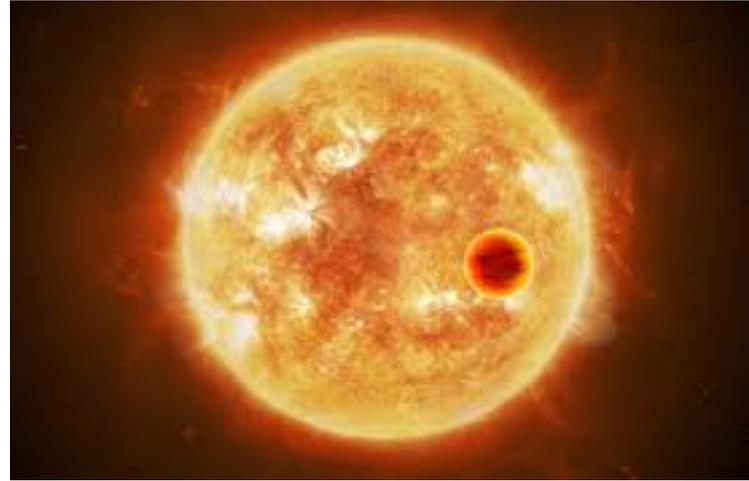
Plots provided by  
Kai Hou Yip (Gordon)

# Other disturbing effects

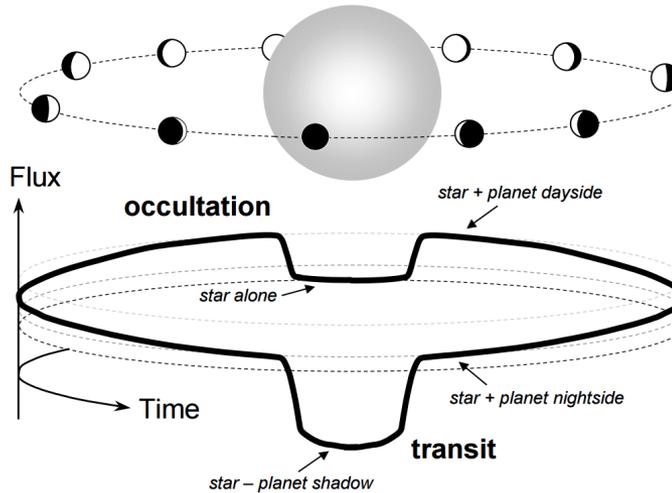
## Exomoons



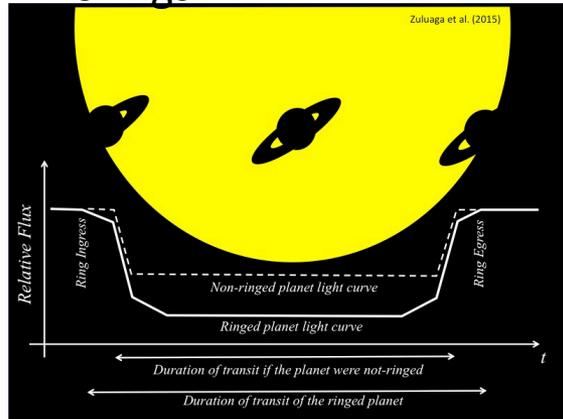
## Stellar activity



## Exoplanet phase-curve



## Exorings



Kipping 2009a, b, 2011; Zuluaga et al. 2015; Sarkar et al. 2018; Showman & Guillot 2002; Morello et al. (in prep.)

# Conclusions

- Fitting for (four) stellar limb-darkening coefficients in transit light-curve fits to avoid biases in the exoplanet parameters;
- Also important for exoplanet spectroscopy;
- Highly significant for *HST*/WFC3 and next-generation instruments onboard JWST and ARIEL;
- Multiwavelength Bayesian approach (SEA BASS) to minimize the biases and break parameter degeneracies;
- Successfully applied to HST/STIS observations of HD209458b;

## Next steps:

- Priors from stellar physics (testing stellar models on Kepler/K2, TESS data);
- Disentangling other astrophysical signals.

**Thank you**