



Università degli Studi “Aldo Moro” di Bari  
Chemistry Department

INAF – Istituto Nazionale di Astrofisica  
Osservatorio di Arcetri



# Primordial $H_2$ formation in the early Universe



Osservatorio Astronomico di Trieste

Foto by News Cjapan



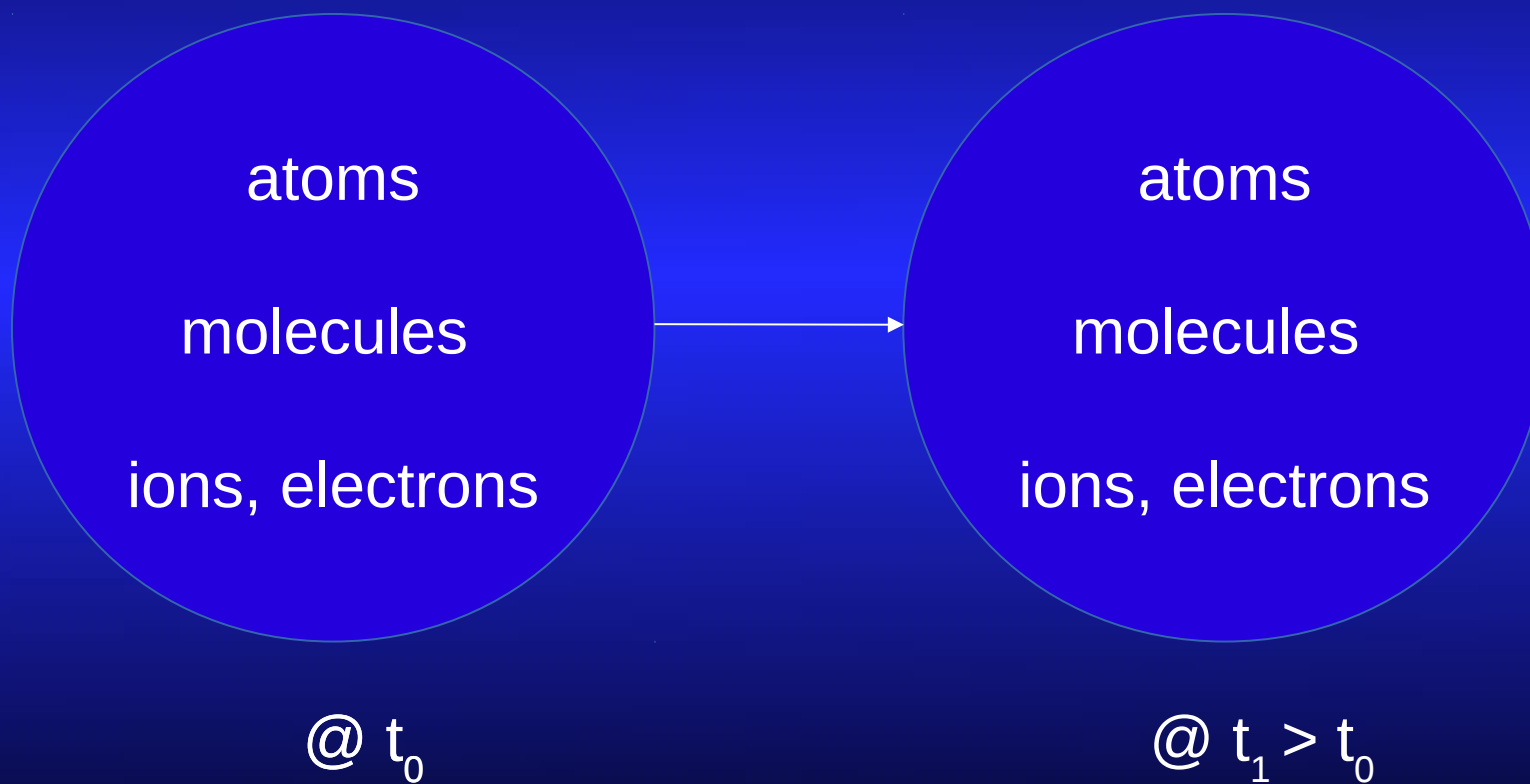
15<sup>th</sup> October 2014

Carla Maria Coppola

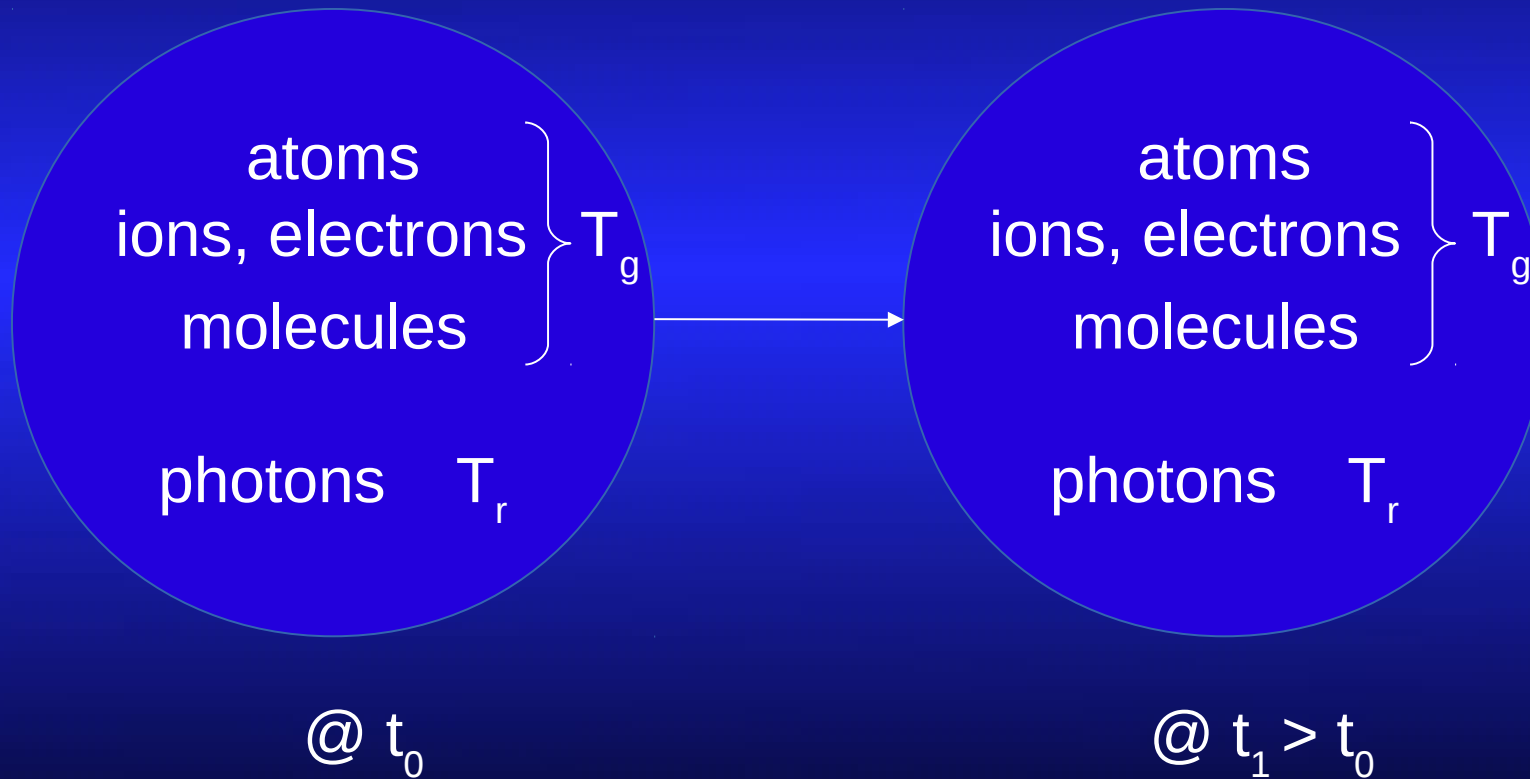
## OUTLINE:

1. **early Universe: the “standard” chemistry**
2. **non-equilibrium distributions**
  - molecular internal states resolution:
    - vibration;
  - **spectral distortions:**
    - primordial atomic recombination;
    - molecular processes;
    - dark matter annihilation
3. **“modified” chemistry**
4. **chemistry in pre-galactic shocks**

# CHEMICAL KINETICS: DEFINITIONS AND EQS (I)



## CHEMICAL KINETICS: DEFINITIONS AND EQS (II)



## KINETIC MODEL: ODEs SYSTEM (III)

$$\frac{dn_i}{dt} = k_{form}(T) n_j n_k - k_{dest}(T) n_i + \dots$$

- initial conditions  $n_i(t_0)$

- reaction rates  $k(T)$

## DENSITIES AND TEMPERATURE RANGES: THE ISM

Warm ionized medium (densities  $\sim 0.3 \text{ cm}^{-3}$  -  $T \sim 10000 - 8000 \text{ K}$ )

Warm neutral medium (densities  $\sim 0.3 \text{ cm}^{-3}$  -  $T \sim 8000 \text{ K}$ )

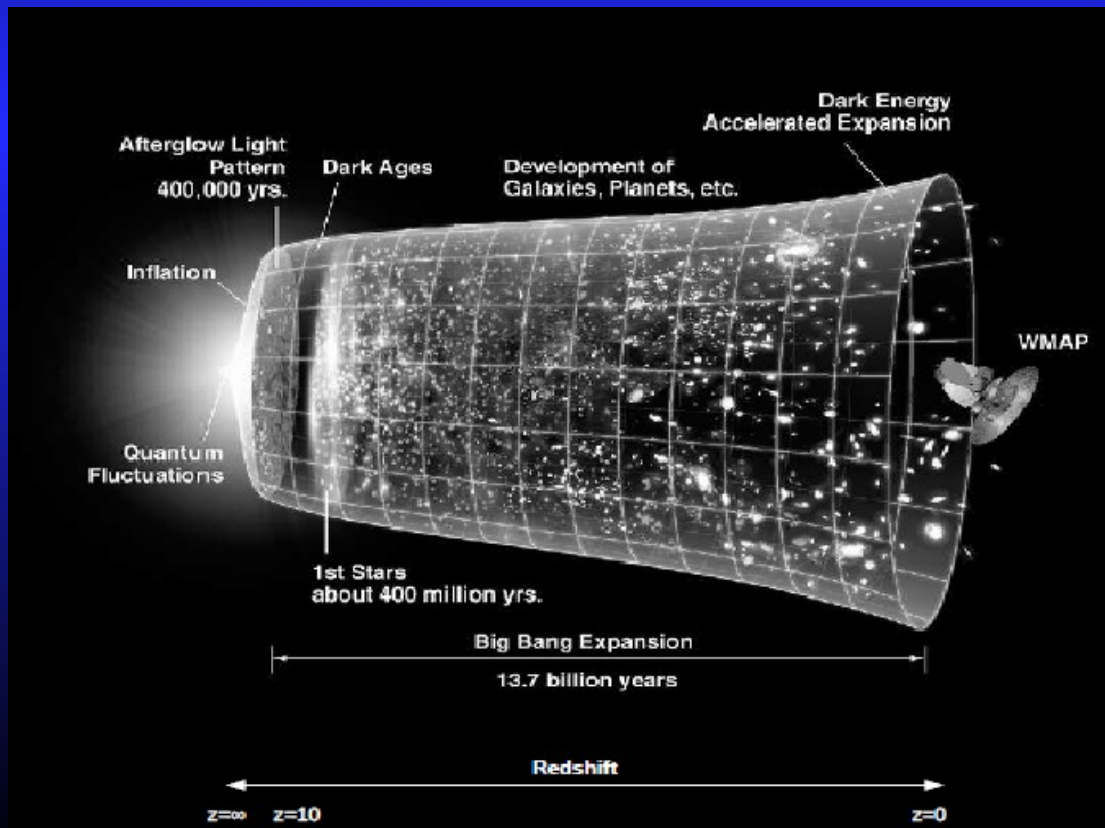
Cold neutral medium (densities  $\sim 30 \text{ cm}^{-3}$  -  $T \sim 50 \text{ K}$ )

Molecular clouds (densities  $> 100 \text{ cm}^{-3}$  -  $T > 10 \text{ K}$ )



# DENSITIES AND TEMPERATURE RANGES: PRIMORDIAL UNIVERSE CHEMISTRY

Densities  $\sim 10^5 - 10^{-7} \text{ cm}^{-3}$   
 $T \sim 30000 \text{ K} - 0.003 \text{ K}$



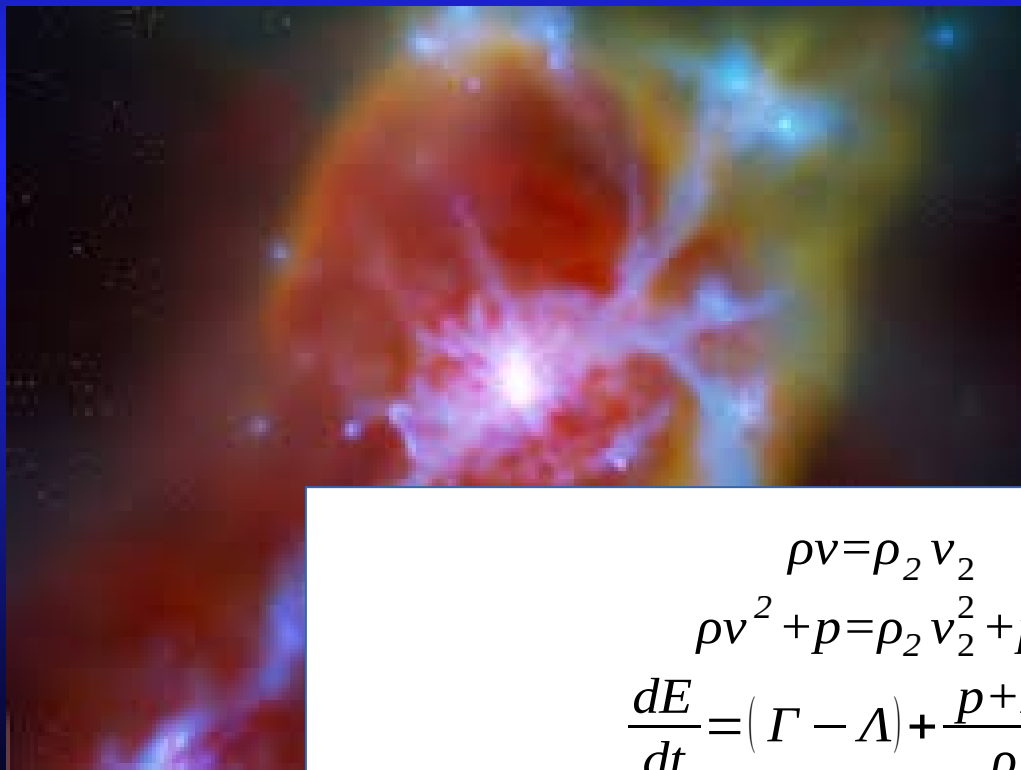
$$\frac{dn_i}{dt} = k_{form} n_j n_k - k_{dest} n_i + \dots$$

$$\frac{dn_i}{dz} = \frac{dt}{dz} \frac{dn_i}{dt}$$

$$n(z) = \Omega_b n_{cr} (1+z)^3$$

# DENSITIES AND TEMPERATURE RANGES: PRIMORDIAL STAR FORMATION/ MOLECULAR CLOUDS COLLAPSE

Densities  $\sim 1- 10^{23} \text{ cm}^{-3}$   
 $T \sim 100,000 \text{ K} - \text{few K}$



$$\begin{aligned} \rho v &= \rho_2 v_2 \\ \rho v^2 + p &= \rho_2 v_2^2 + p_2 \\ \frac{dE}{dt} &= (\Gamma - \Lambda) + \frac{p+E}{\rho} \frac{d\rho}{dt} \end{aligned} \quad \left. \begin{array}{l} \text{mass} \\ \text{momentum} \\ \text{energy} \end{array} \right\} \text{conservation}$$

$$E = \frac{\sum p_i}{\gamma_i - 1}; \quad p_i = n_i K T; \quad \frac{1}{n} \frac{dn}{dt} = -\frac{1}{T} \frac{dT}{dt}$$



DIFFERENT ASTROPHYSICAL APPLICATIONS...

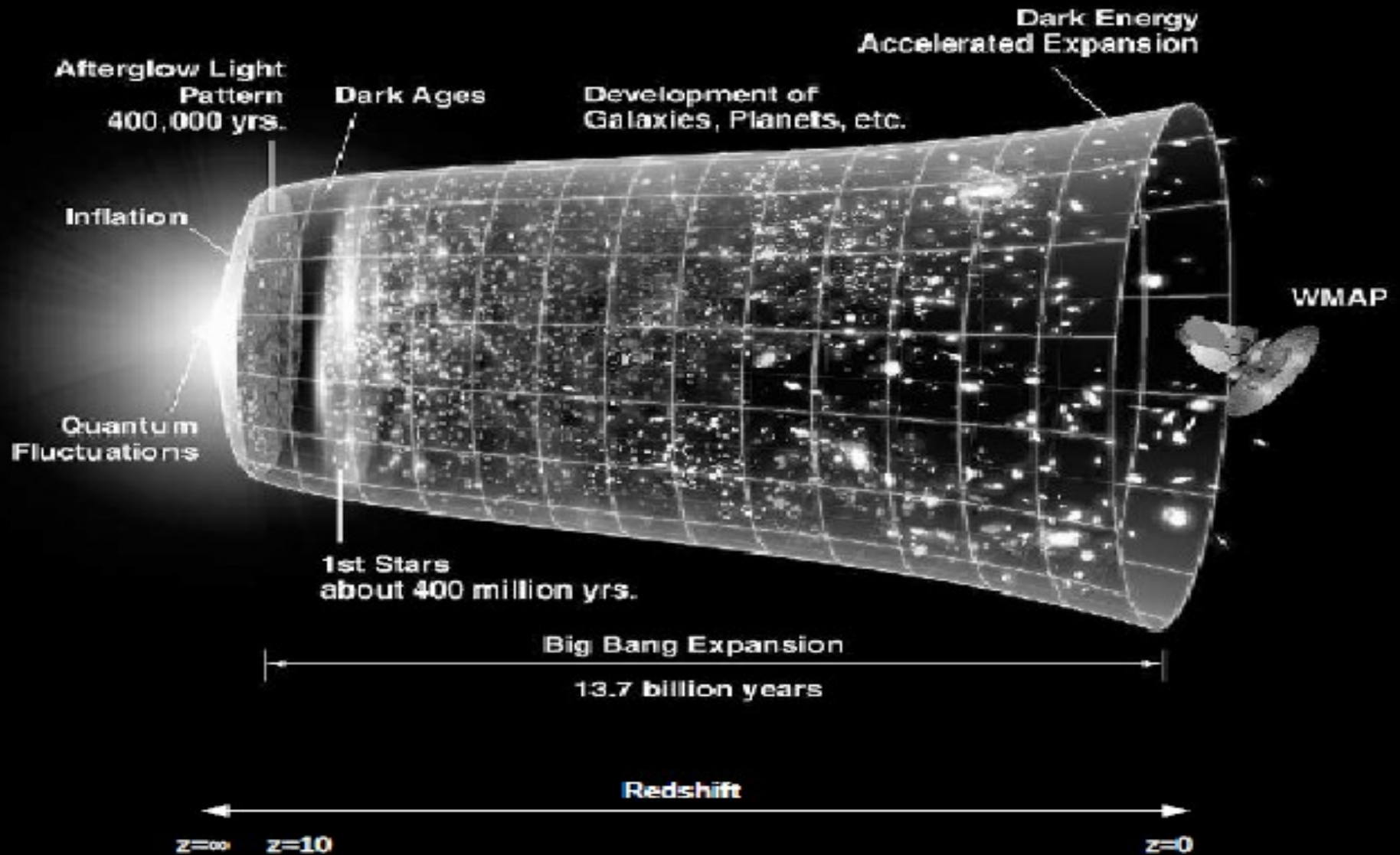
SAME PROBLEM:

WIDE RANGES OF TEMPERATURES AND DENSITIES...

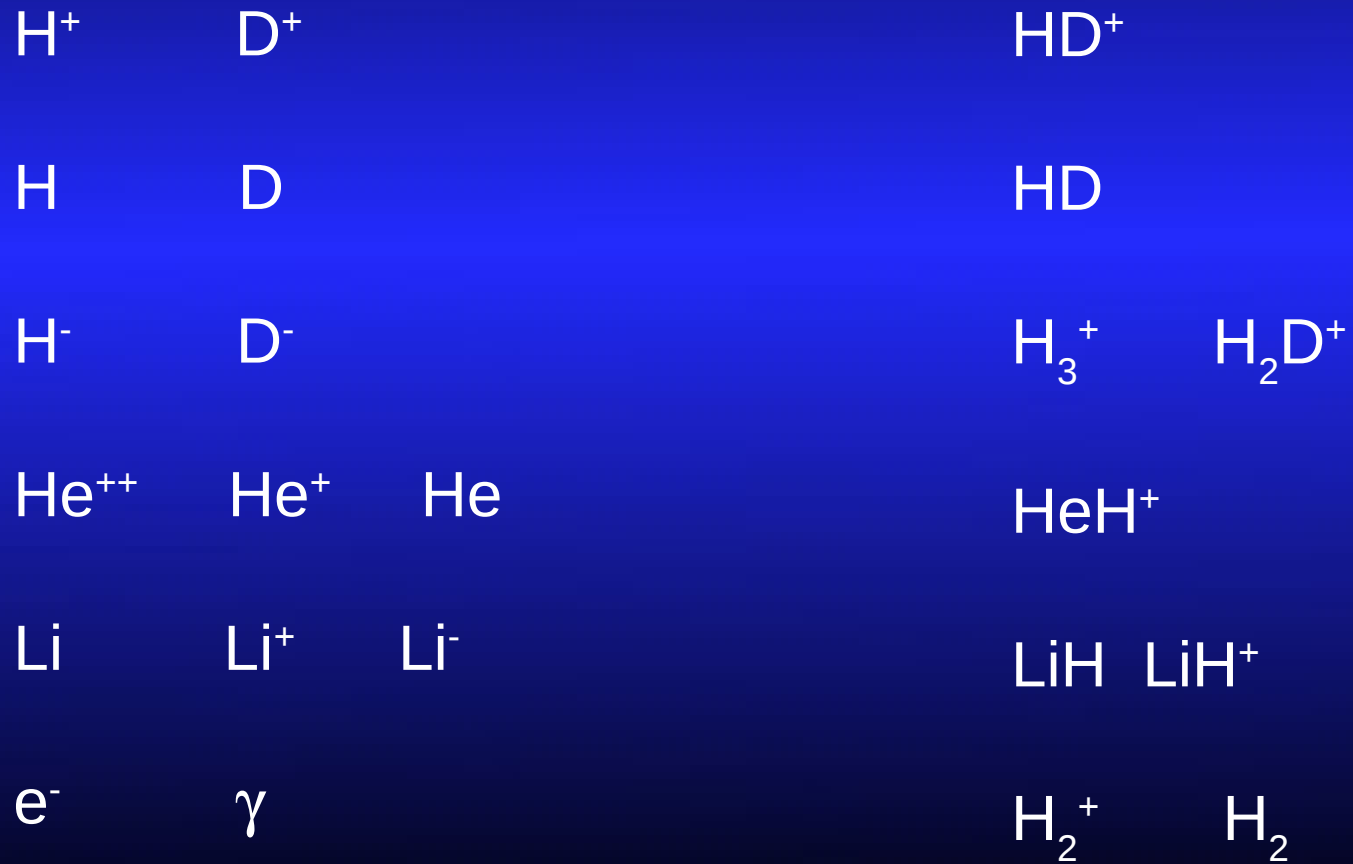
## SEARCH FOR CHEMICAL DATA



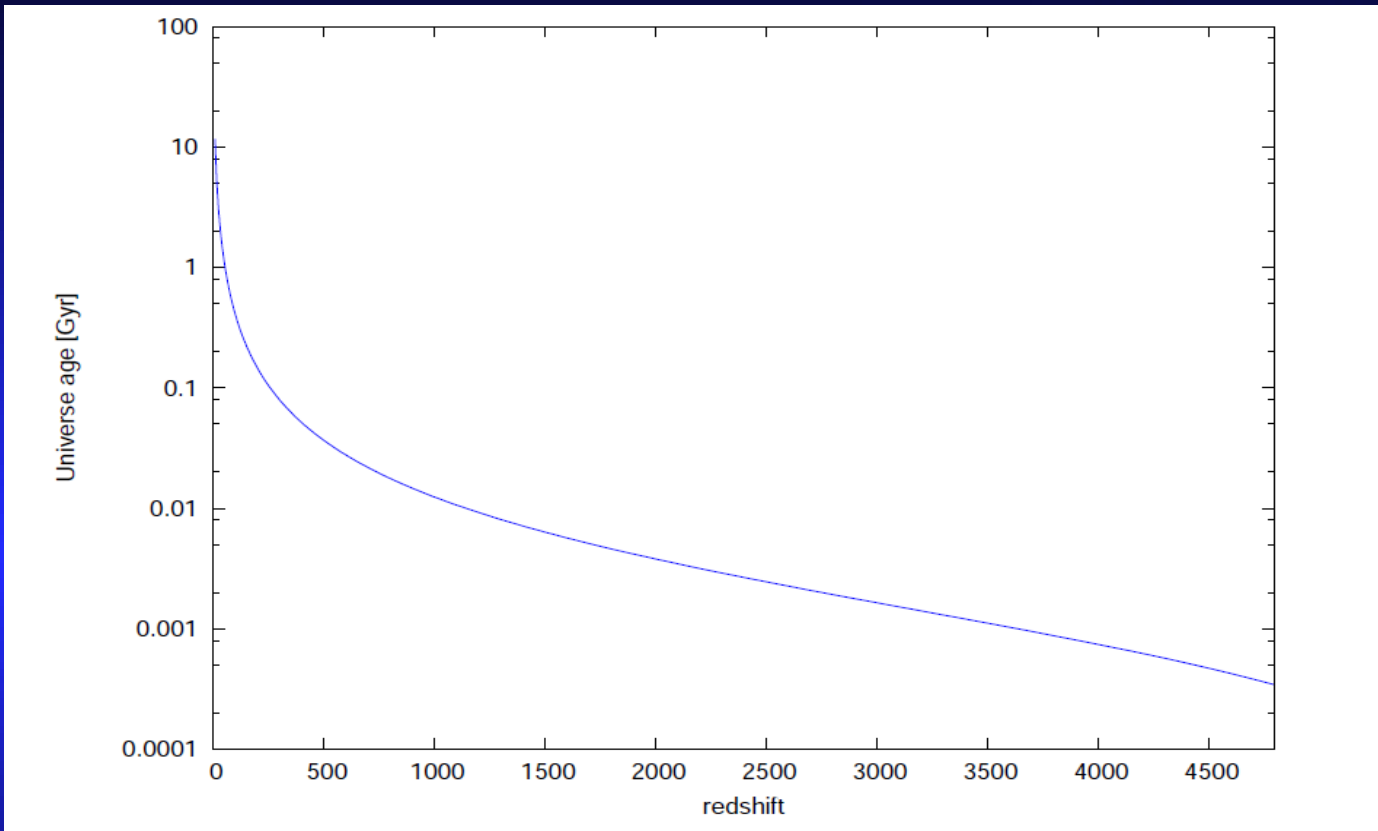
# UNIVERSE HISTORY...



# KINETIC MODELS: CHEMICAL SPECIES



# SOME COSMOLOGY DEFINITIONS...



$$1 + z = \frac{a(t_0)}{a(t)} \equiv \frac{a_0}{a(t)}$$

$$\frac{dt}{dz} = -\frac{1}{(1+z)H(z)}$$

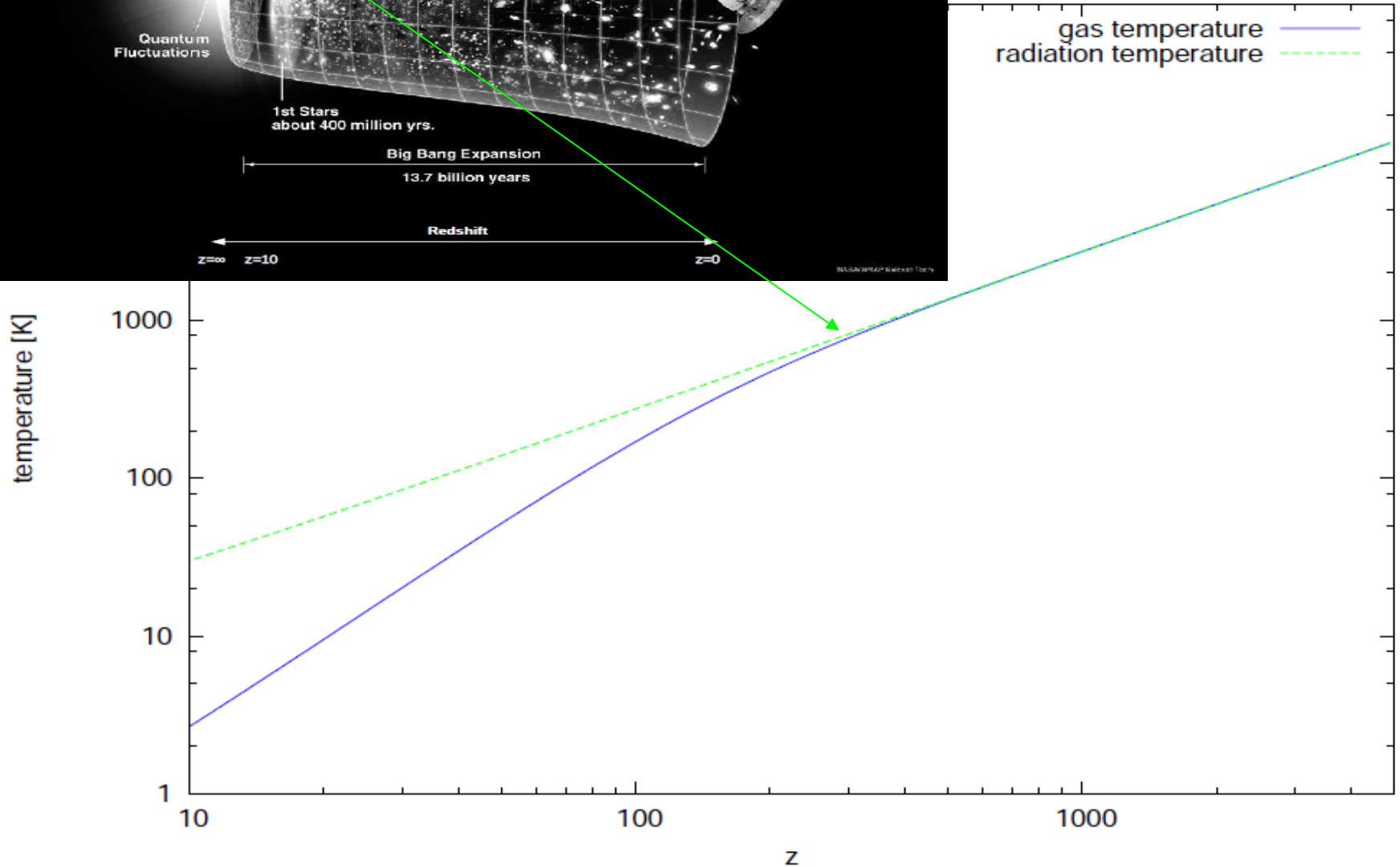
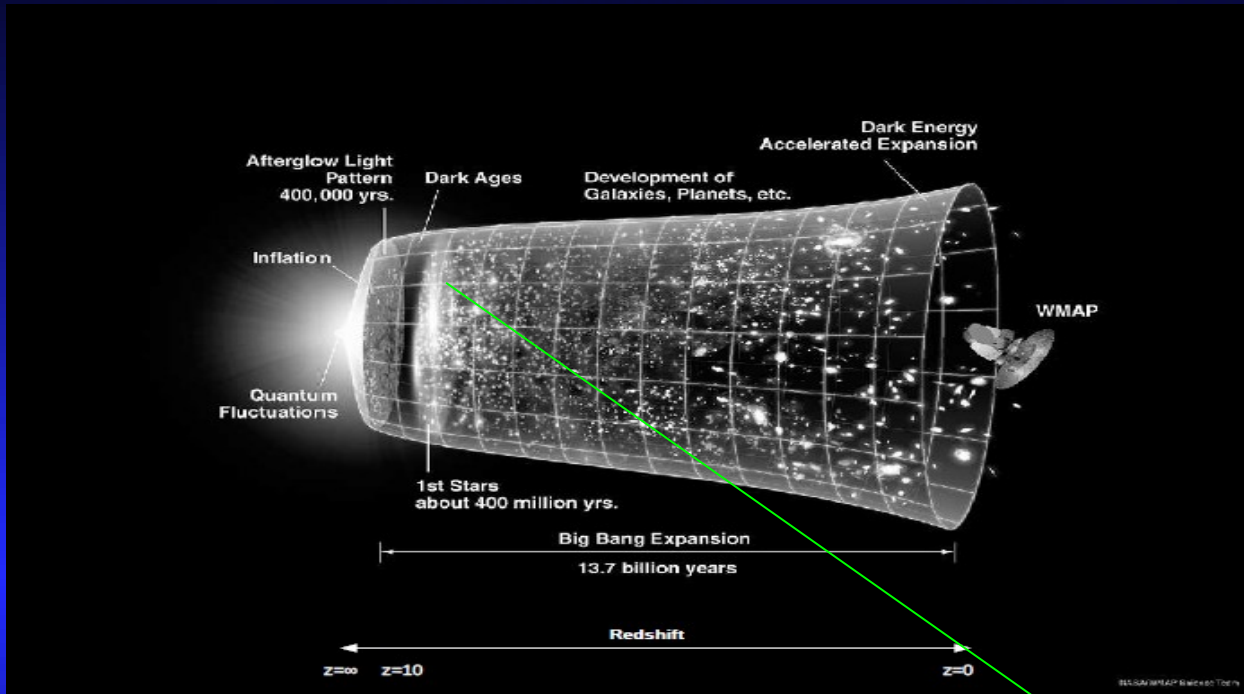
$$H(z) = H_0 \sqrt{\Omega_r(1+z)^4 + \Omega_m(1+z)^3 + \Omega_K(1+z)^2 + \Omega_\Lambda}$$

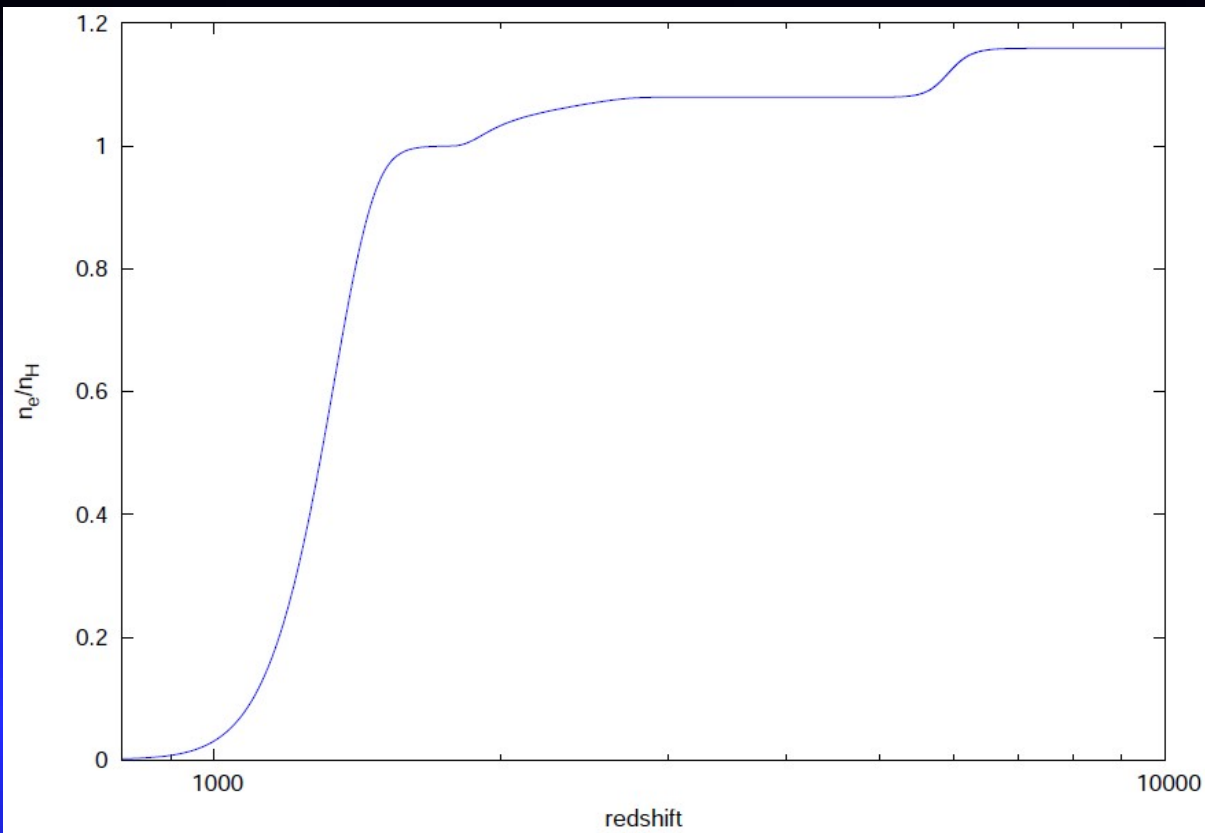
**COSMIC TIME  
VS  
REDSHIFT**

# KINETIC MODELS IN PRIMORDIAL UNIVERSE CHEMISTRY: A BRIEF OVERVIEW...

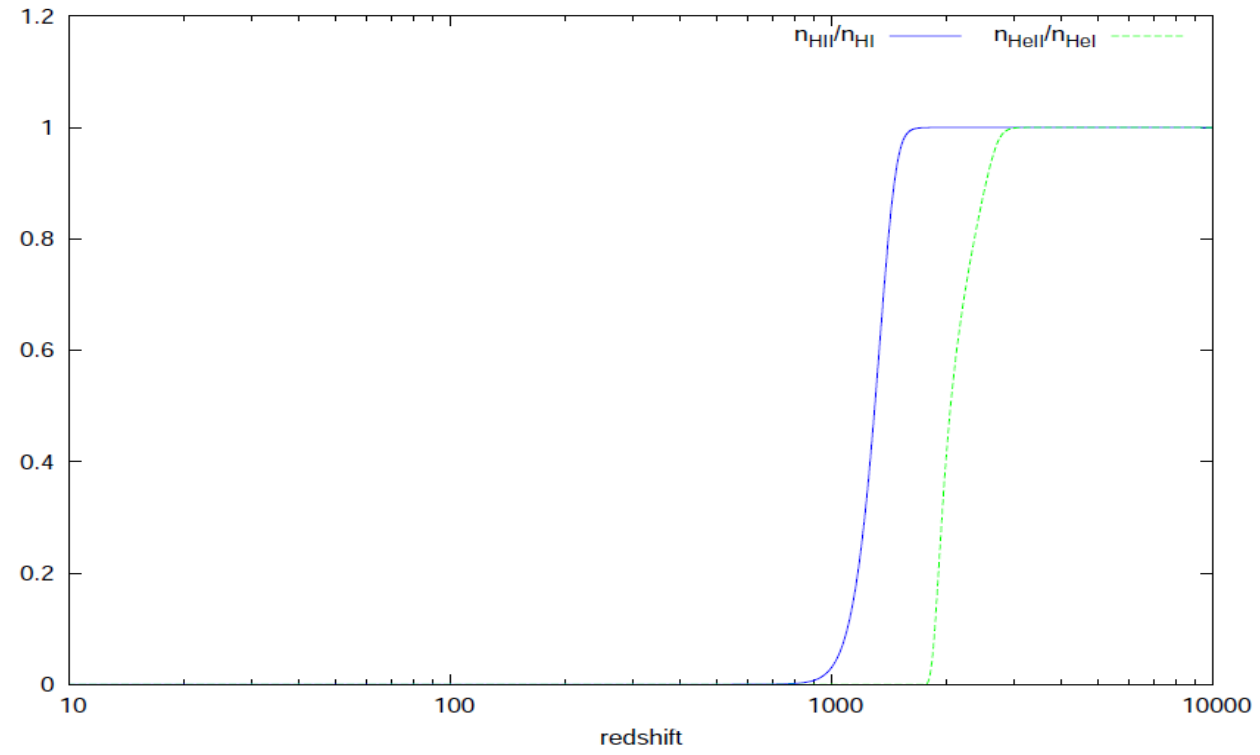
- '60s: studies on elementary processes useful in molecular hydrogen formation in the early Universe (Saslaw & Zipoy (1967), Peebles & Dicke (1968))
- Chemical kinetics in the early Universe:
  - Dalgarno & Lepp (1987)
  - Black (1990)
  - Shapiro (1992)
  - Puy et al. (1993,1996)
  - Dalgarno & Fox (1994)
  - Lepp, Stancil & Dalgarno (1996), Lepp & Stancil (1998)
  - Bougleux & Galli (1997)
  - Galli & Palla (1998, 2002)
  - Schleicher et al. (2008)

# RADIATION AND MATTER TEMPERATURES

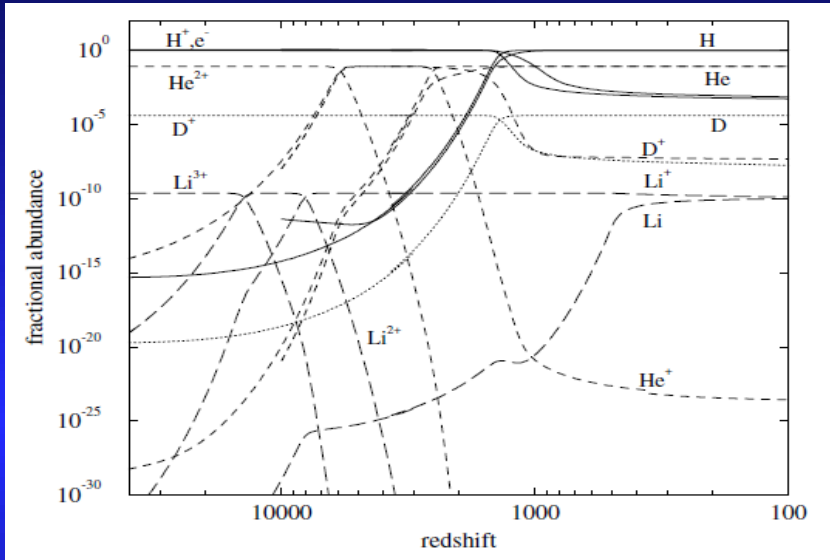




# IONIZATION FRACTION & IONIZATION POTENTIALS



# KINETIC MODEL: FRACTIONAL ABUNDANCES

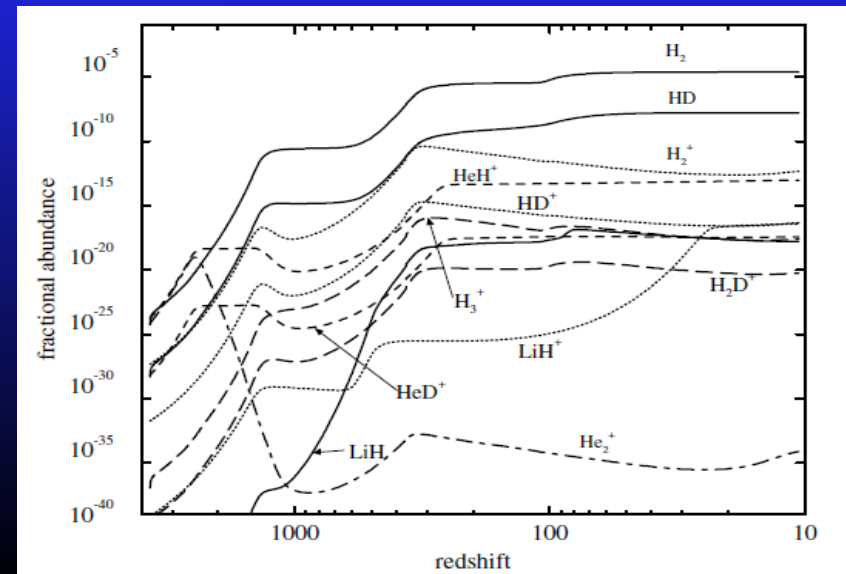


$$\frac{dn_i}{dt} = k_{form} n_j n_k - k_{dest} n_i + \dots$$

$$\frac{dn_i}{dz} = \frac{dt}{dz} \frac{dn_i}{dt}$$

$$n(z) = \Omega_b n_{cr} (1+z)^3$$

Lepp, Stancil & Dalgarno,  
2002, J. Phys. B: At. Mol. Opt. Phys. 35, R57–R80





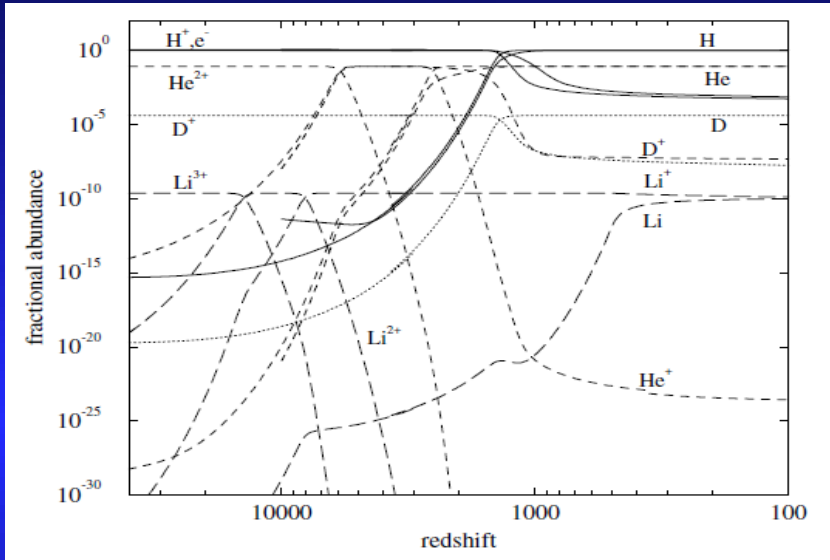
# KINETIC MODEL: CHEMICAL PROCESSES

Chemical process	Rate coefficient [MKS]
1] $H + e^- \rightarrow H^- + h\nu$	$1.4 \times 10^{-24} T_m^{0.928} e^{-T_m/16200}$
2] $H^- + e^- \rightarrow H + 2e^-$	fit from reference
3] $H^- + H \rightarrow 2H + e^-$	fit from reference
4] $H^- + H^+ \rightarrow 2H$	$1.40 \times 10^{-13} \left(\frac{T_m}{300}\right)^{-0.487} e^{T_m/29300}$
5] $H^- + h\nu \rightarrow H + e^-$	$0.01 T_r^{2.13} e^{T_m/29300}$
6] $D^- + h\nu \rightarrow D + e^-$	estimated by rc 5
7] $HD^+ + h\nu \rightarrow D + H^+$	$\frac{1}{2} 1.63 \times 10^7 e^{-32400/T_r}$
8] $HD^+ + h\nu \rightarrow D^+ + H$	$\frac{1}{2} 1.63 \times 10^7 e^{-32400/T_r}$
9] $HD^+ + h\nu \rightarrow H^+ + D^+ + e^-$	$9.0 \times 10^{11} T_r^{1.48} e^{-335000/T_r}$
10] $HD + h\nu \rightarrow HD^+ + e^-$	$2.9 \times 10^{12} T_r^{1.56} e^{-178500/T_r}$
11] $D + H^+ \rightarrow D^+ + H$	$2.0 \times 10^{-16} T_m^{0.402} e^{-37.1/T_m} - 3.31 \times 10^{-23} T_m^{1.48}$
12] $D^+ + H \rightarrow D + H^+$	$2.06 \times 10^{-16} T_m^{0.396} e^{-33.0/T_m} + 2.03 \times 10^{-15} T_m^{-0.332}$
13] $D + H \rightarrow HD + h\nu$	see reference in Schleicher et al [11]
14] $HD^+ + H \rightarrow HD + H^+$	$6.4 \times 10^{-16}$
15] $D + H^+ \rightarrow HD^+ + h\nu$	$dex(-19.38 - 1.523 \log_{10}(T_m) + 1.118 \log_{10}^2(T_m) - 0.1269 \log_{10}^3(T_m))$
16] $D^+ + H \rightarrow HD^+ + h\nu$	$dex(-19.38 - 1.523 \log_{10}(T_m) + 1.118 \log_{10}^2(T_m) - 0.1269 \log_{10}^3(T_m))$
17] $HD^+ + e^- \rightarrow D + H$	$7.2 \times 10^{-14} T_m^{-0.5}$
18] $D^+ + e^- \rightarrow D^- + h\nu$	$3.0 \times 10^{-22} \left(\frac{T_m}{300}\right)^{0.95} e^{-T_m/9320}$
19] $D^+ + D^- \rightarrow 2D$	$1.96 \times 10^{-13} \left(\frac{T_m}{300}\right)^{-0.487} e^{T_m/29300}$
20] $H^+ + D^- \rightarrow D + H$	$1.61 \times 10^{-13} \left(\frac{T_m}{300}\right)^{-0.487} e^{T_m/29300}$
21] $H^- + D \rightarrow H + D^-$	$6.4 \times 10^{-15} \left(\frac{T_m}{300}\right)^{0.41}$
22] $D^- + H \rightarrow D + H^-$	$6.4 \times 10^{-15} \left(\frac{T_m}{300}\right)^{0.41}$
23] $D^- + H \rightarrow HD + e^-$	$1.5 \times 10^{-15} \left(\frac{T_m}{300}\right)^{0.1}$
24] $D + H^- \rightarrow HD + e^-$	rc 22
25] $H^- + D^+ \rightarrow D$	$1.4 \times 10^{-24} T_m^{0.928} e^{-T_m/16200}$
26] $He + H^+ \rightarrow He$	
27] $He^+ + H \rightarrow He$	A&A 490, 521–535 (2008)
28] $He + H^+ \rightarrow He$	DOI: <a href="https://doi.org/10.1051/0004-6361/200809861">10.1051/0004-6361/200809861</a>
radiative association	© ESO 2008
29] $He + H^+ + h\nu \rightarrow$ stimulated radiative	
30] $He^+ + H \rightarrow He$	
31] $He^+ + e^- \rightarrow He$	
32] $HeH^+ h\nu \rightarrow He$	
33] $HeH^+ h\nu \rightarrow He$	

## Effects of primordial chemistry on the cosmic microwave background

D. R. G. Schleicher<sup>1</sup>, D. Galli<sup>2</sup>, F. Palla<sup>2</sup>, M. Camenzind<sup>3</sup>, R. S. Klessen<sup>1</sup>, M. Bartelmann<sup>1</sup>, and S. C. O. Glover<sup>4</sup>

# KINETIC MODEL: FRACTIONAL ABUNDANCES

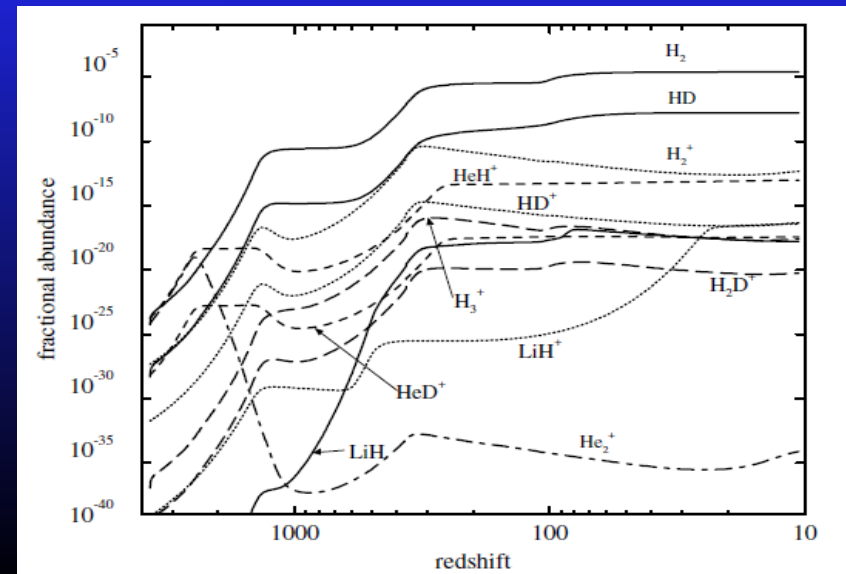


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Lepp, Stancil & Dalgarno,  
2002, J. Phys. B: At. Mol. Opt. Phys. 35, R57–R80



# KINETIC MODEL: CHEMICAL PROCESSES

MASSIVE PARTICLES  
SCATTERING

$$k(T) = \left(\frac{2}{k_B T}\right)^{3/2} \frac{1}{\sqrt{\mu\pi}} \int_0^\infty dE E e^{-\frac{E}{k_B T}} \sigma(E)$$

$$n_b = 1.123 \times 10 \cdot (1 - Y_p) \Omega_b h^2 (1 + z)^3 \quad [m^{-3}]$$

PHOTONIC PROCESSES

$$k_{rad}(T_{rad}) = 4\pi \int_0^\infty \frac{\sigma(\nu)}{h\nu} J_\nu(T_{rad}) d\nu$$

$$J_\nu(T_{rad}) = \frac{2h\nu^3}{c^2} \frac{1}{e^{h\nu/kT_{rad}} - 1}$$

# KINETIC MODEL: MATTER AND RADIATION TEMPERATURE

$$\frac{dT_m}{dt} = -2H(t)T_m + \frac{8\sigma_t a T_r^4 (T_r - T_m) x_e}{3m_e c} + (\Gamma - \Lambda)_{\text{mol}}$$

$$T_r = 2.7(1 + z)$$

## RECFAST

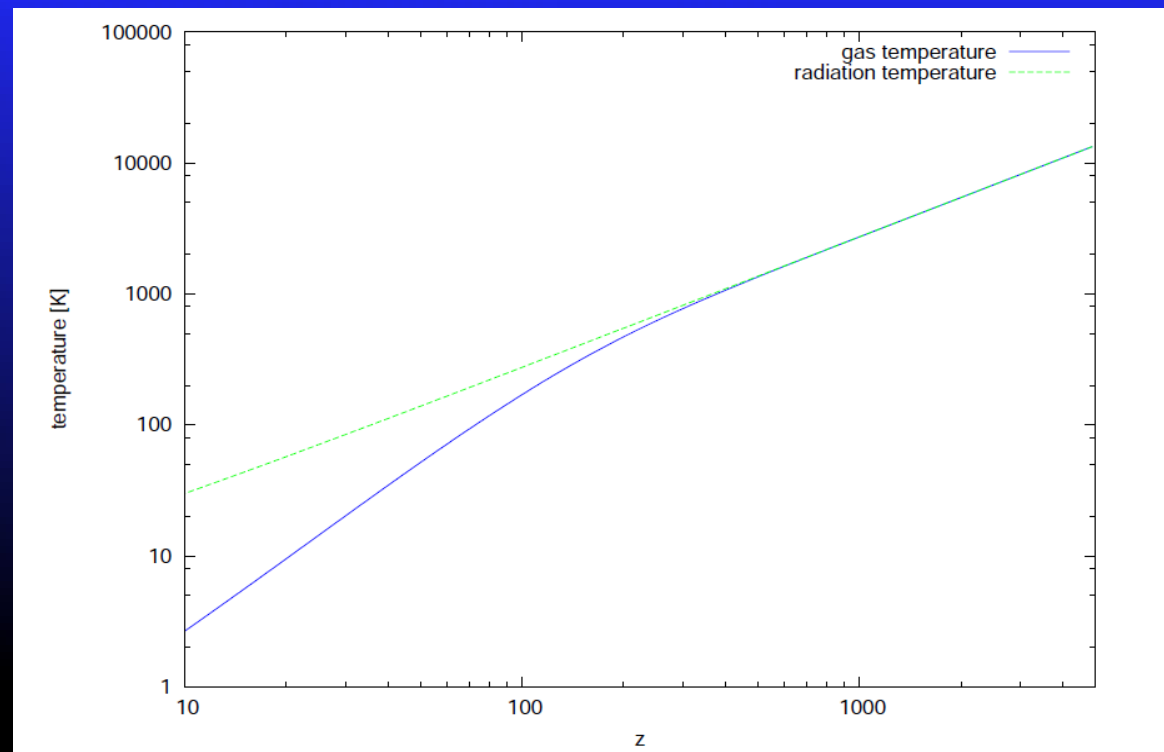
Wong et al.

2008, MNRAS, **386**, 1023-1028

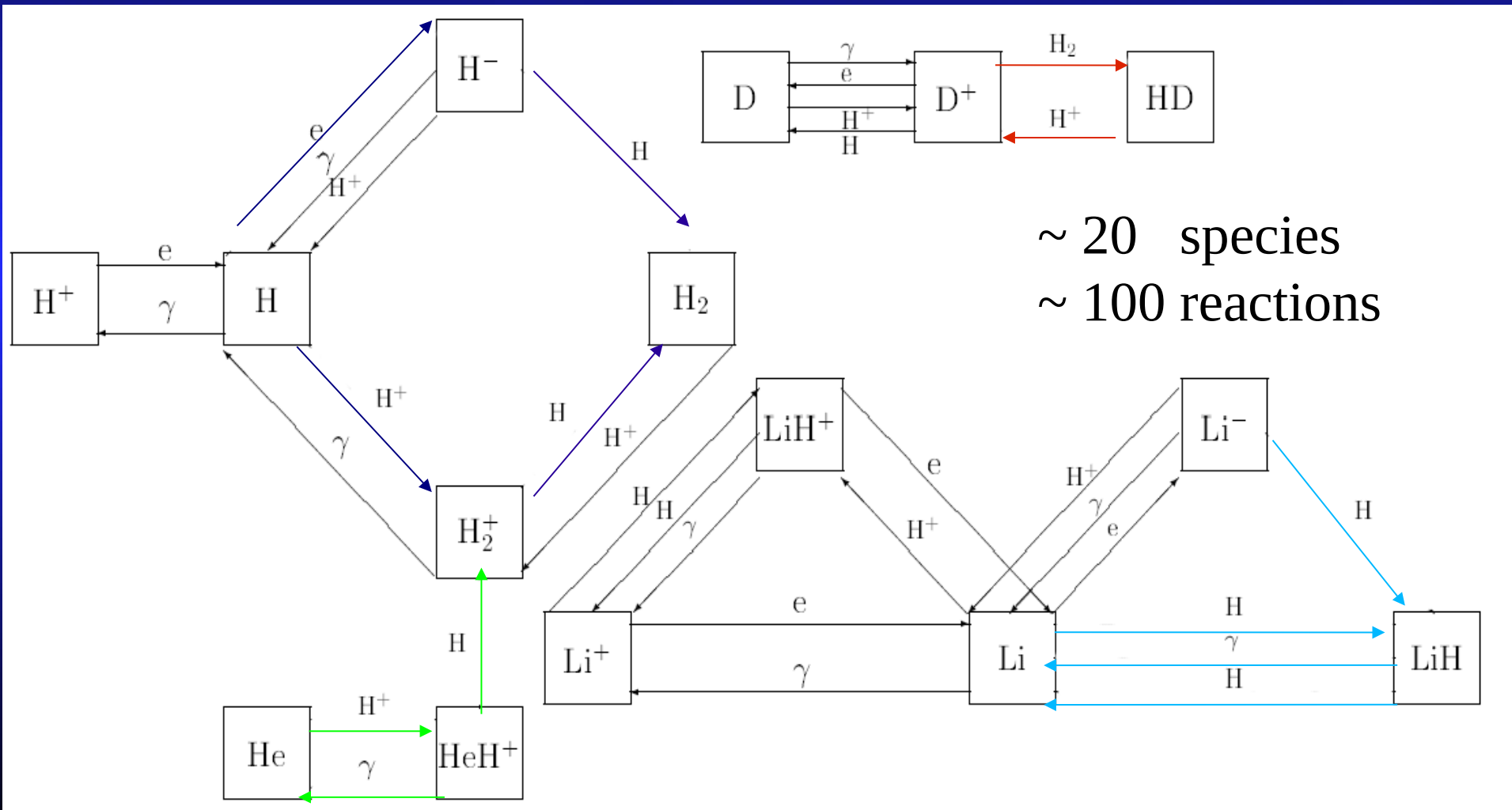
## CosmoRec

Rubiño Martín et al.

2010, MNRAS, **403**, 439-452



# KINETIC MODEL: CHEMICAL PROCESSES



# BEYOND THE “STANDARD” KINETICS...

Non-equilibrium effects:

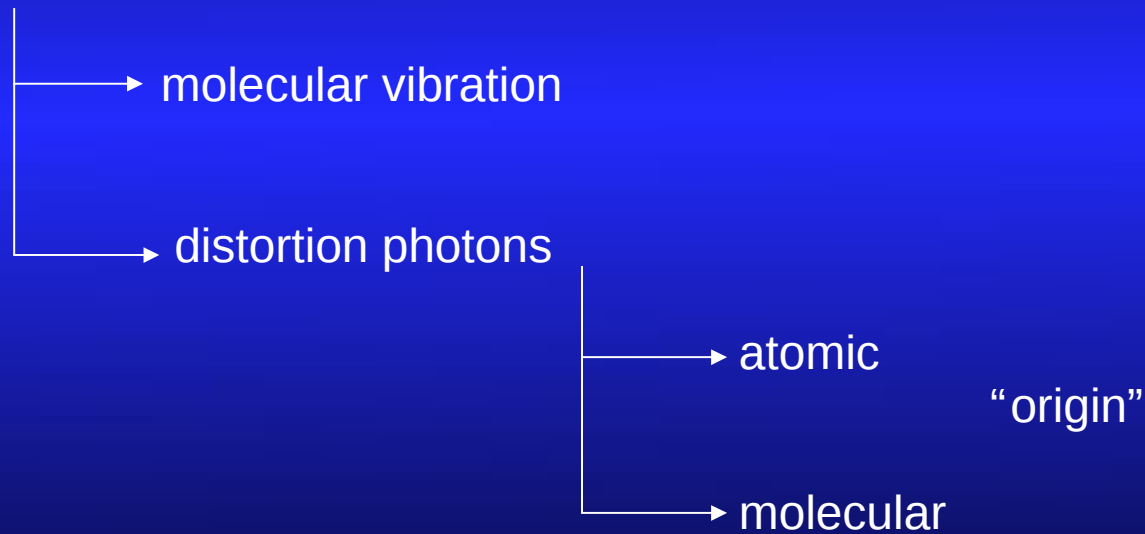
- state-to-state kinetics  Maxwell-Boltzmann's distributions

?

- CMB photons  Planck's distributions

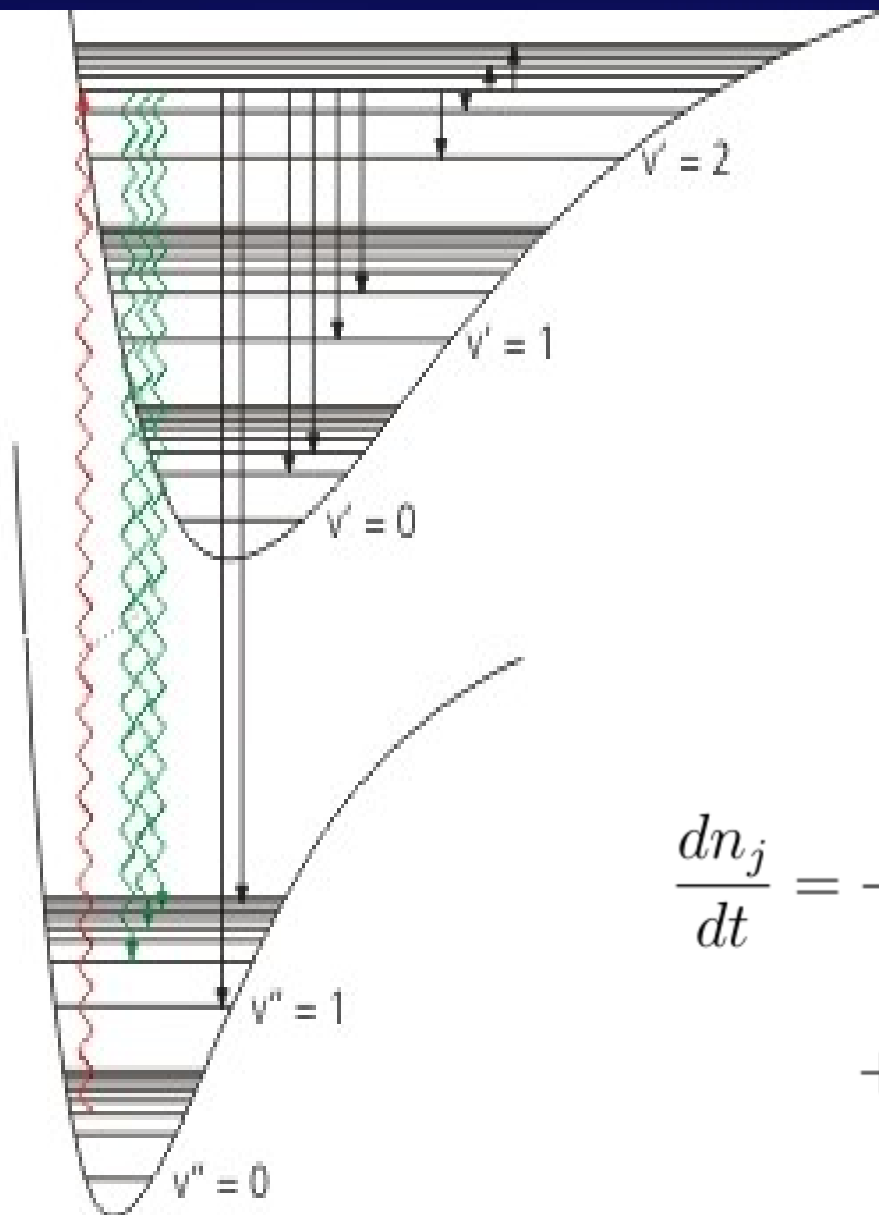
# BEYOND THE “STANDARD” KINETICS...

- non-equilibrium distributions:



- “chemical feedback on the chemistry”

# STATE-TO-STATE APPROACH



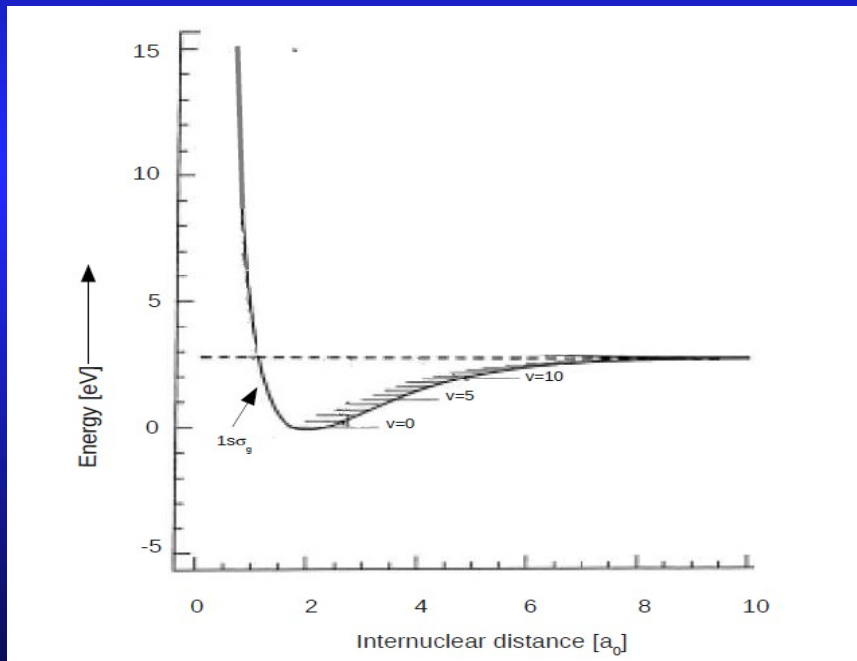
- Electronic
- Vibrational
- Rotational

$$\frac{dn_j}{dt} = -n_j \sum_{j'} (R_{jj'} + P_{jj'} + C_{jj'} n_{j'}) + \sum_{j'} R_{jj'} n_{j'} + \sum_{j'} \sum_{j''} C_j^{j'j''} n_{j'} n_{j''}$$

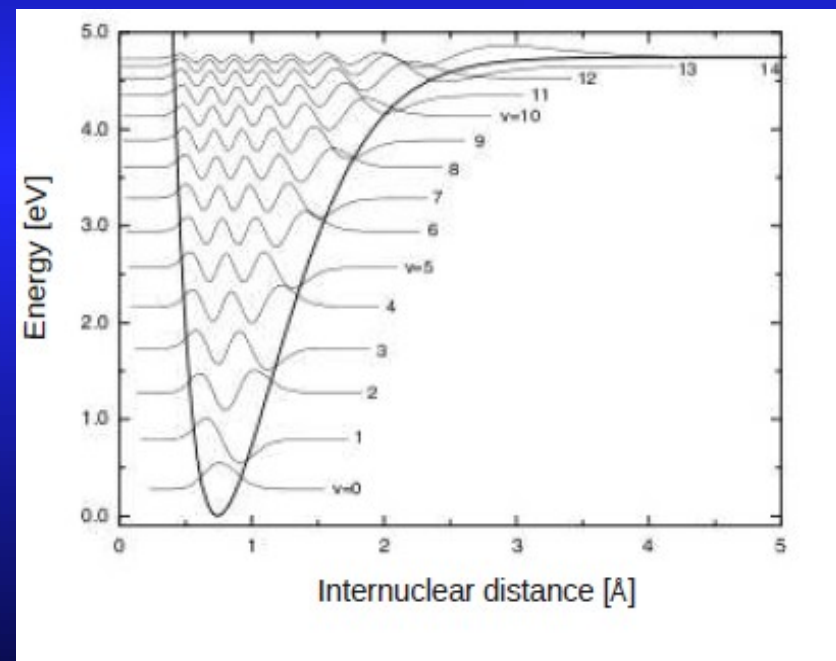


# KINETIC MODEL: CHEMICAL SPECIES

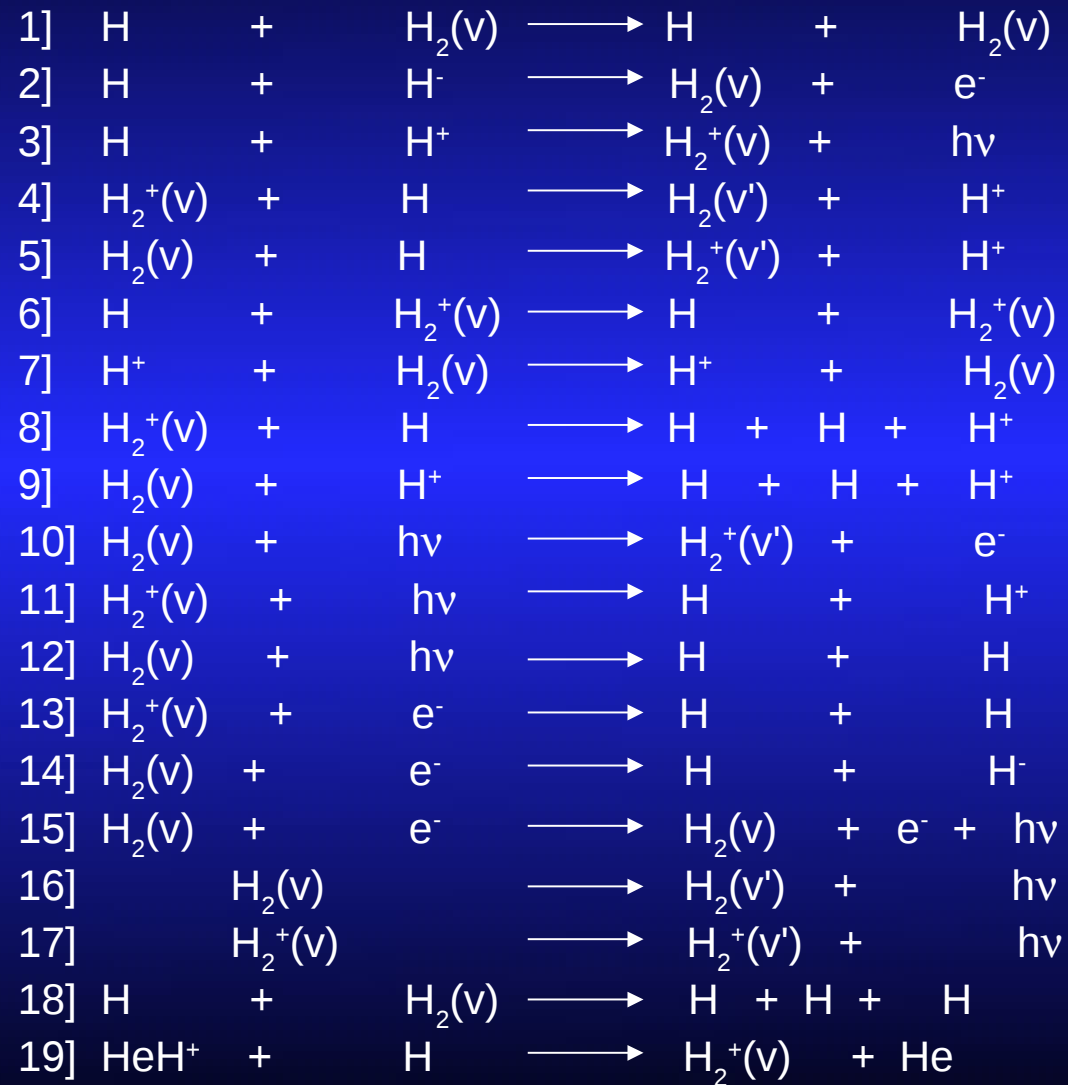
$H_2^+$  → 18 levels



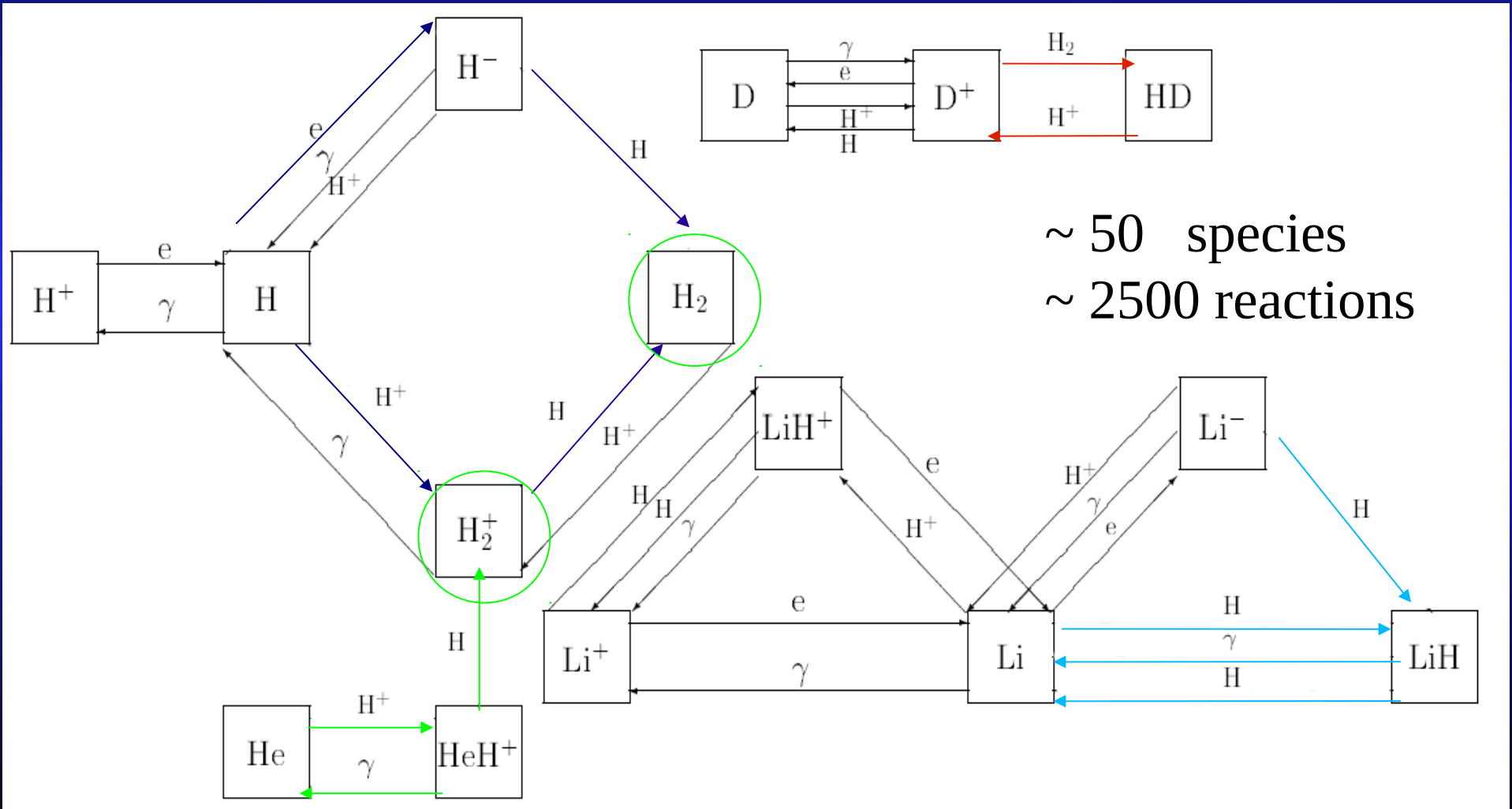
$H_2$  → 15 levels



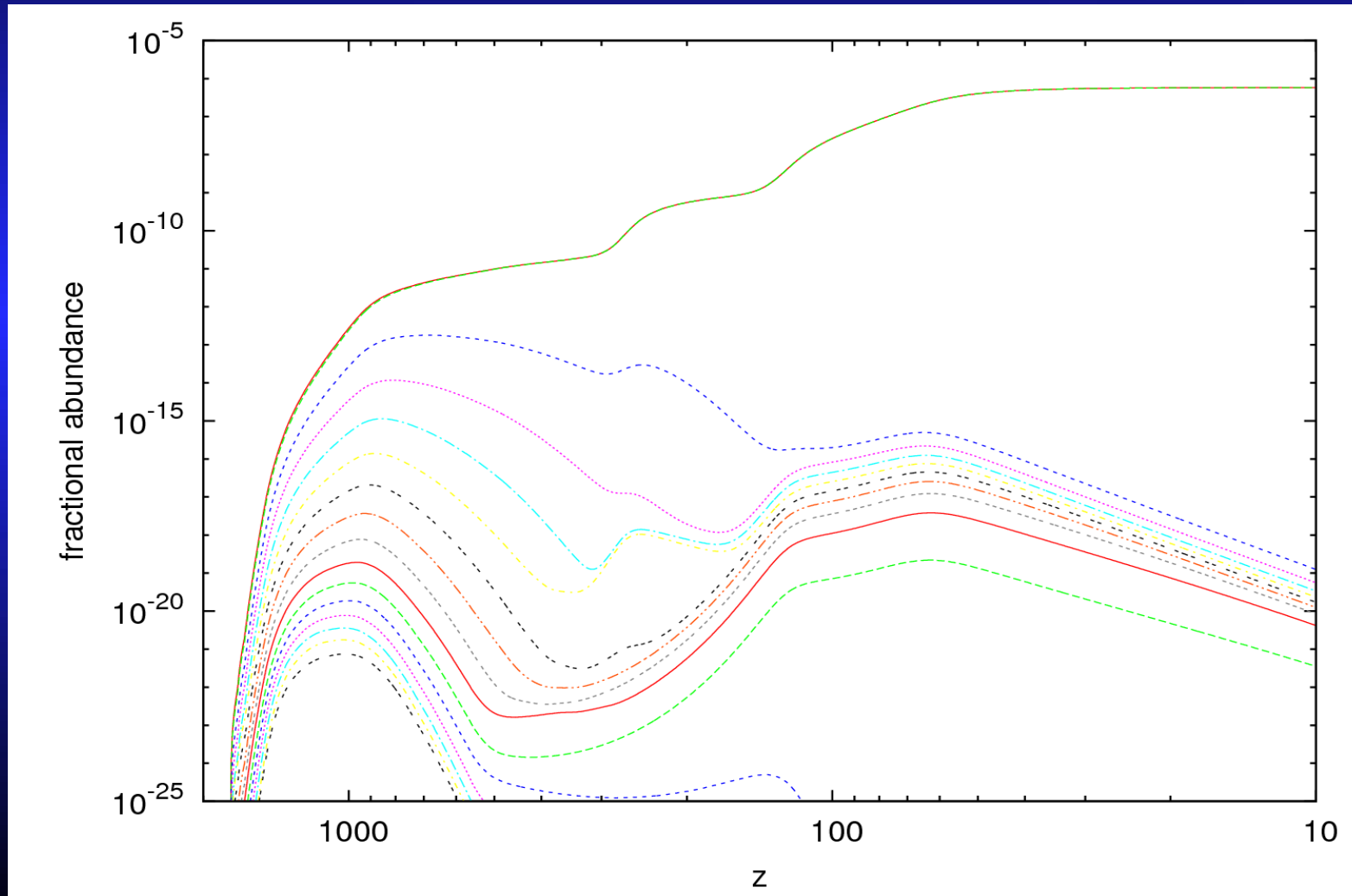
# KINETIC MODEL: CHEMICAL PROCESSES



# KINETIC MODEL: STATE-TO-STATE KINETICS

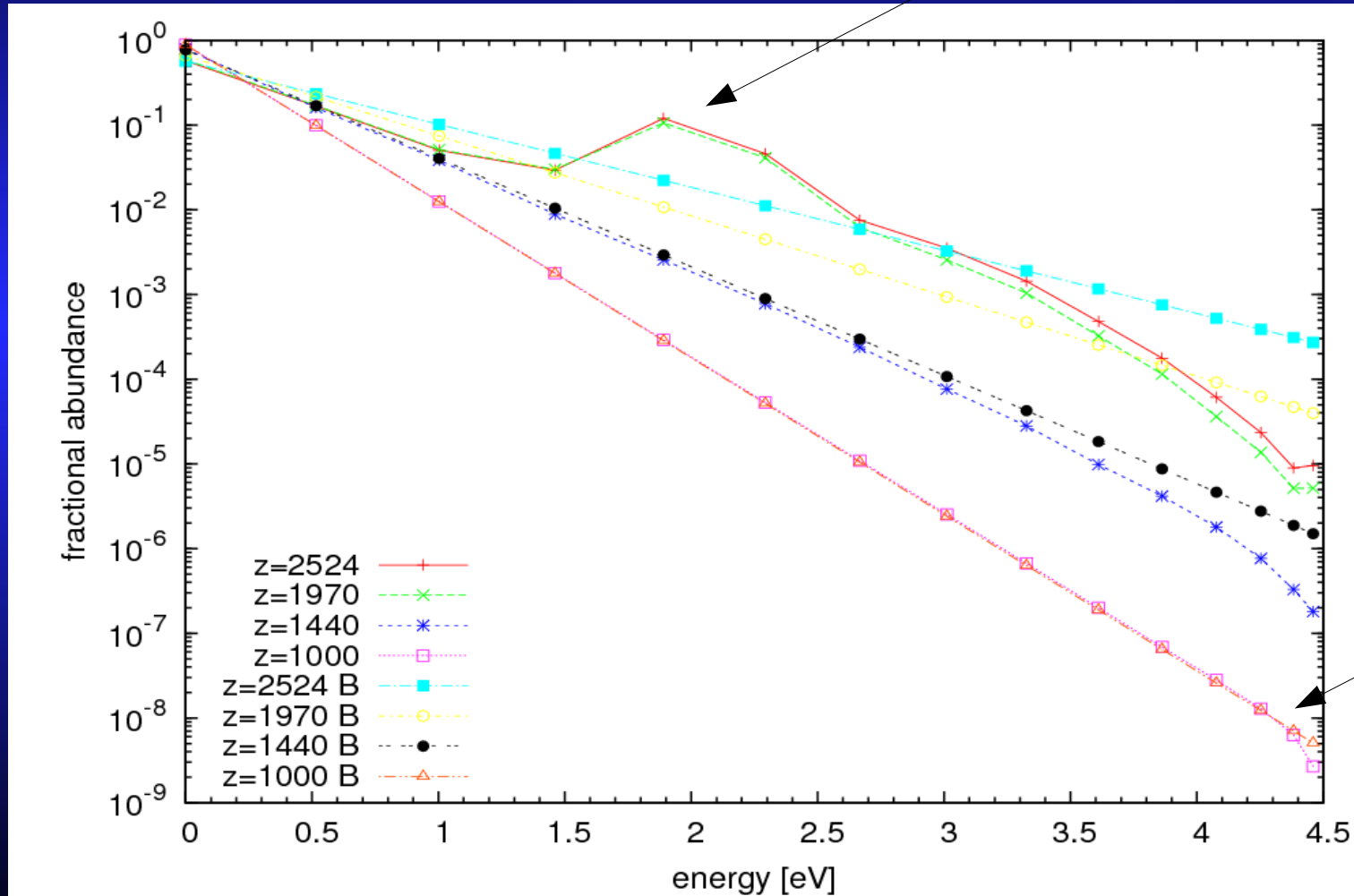


# RESULTS: VDF $H_2$ (I)

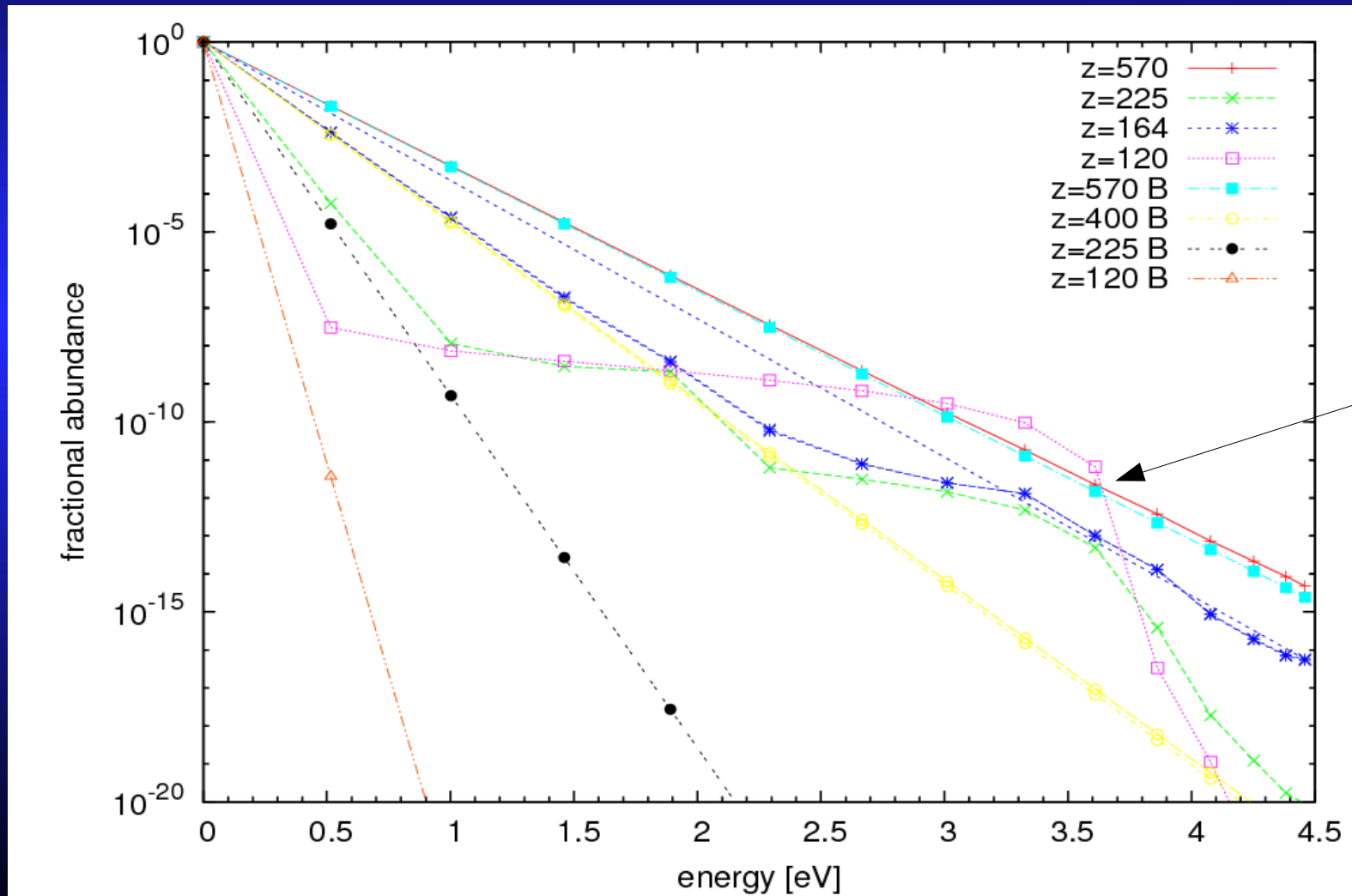


# RESULTS: VDF H<sub>2</sub> (II)

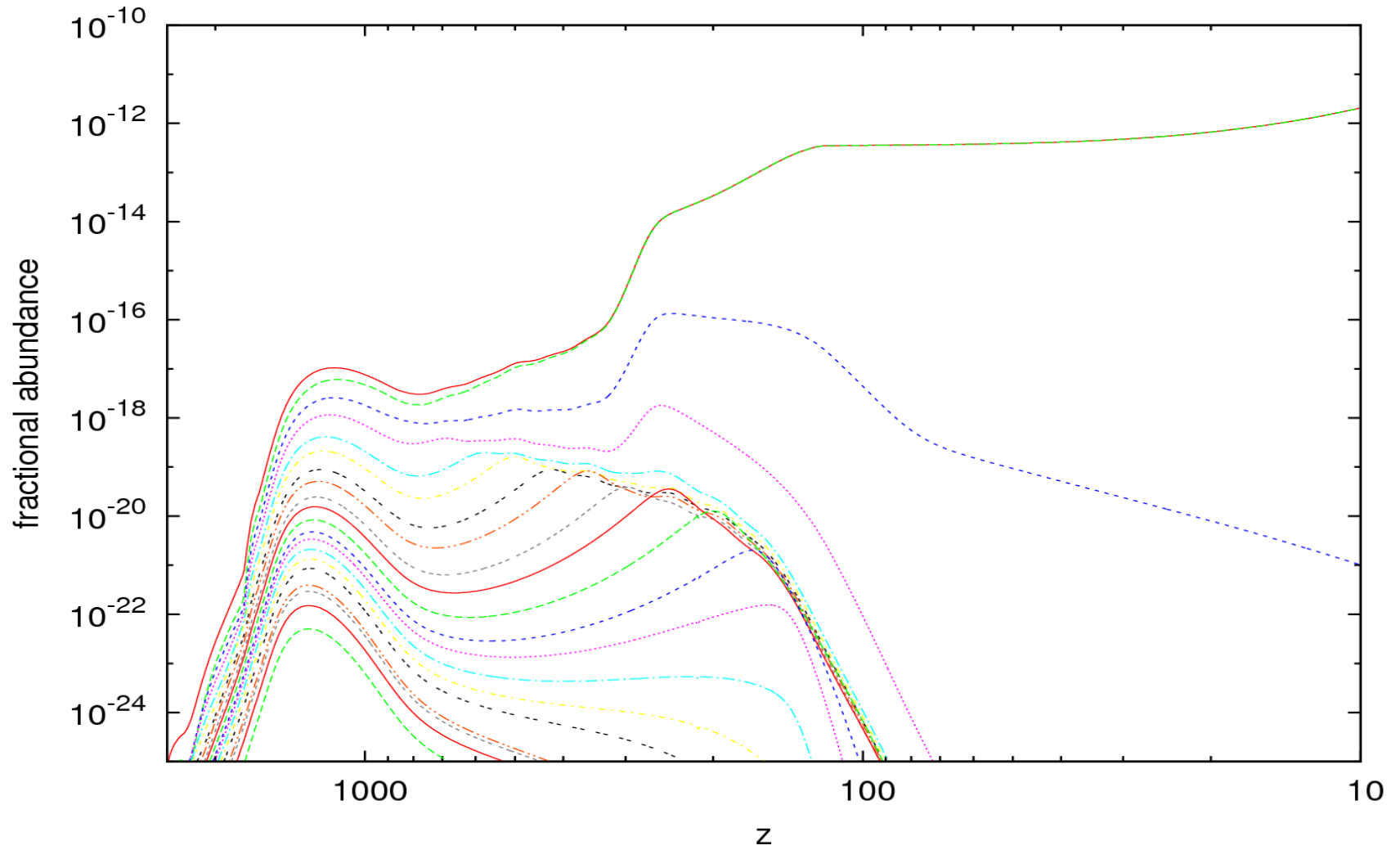
H<sub>2</sub><sup>+</sup> channel



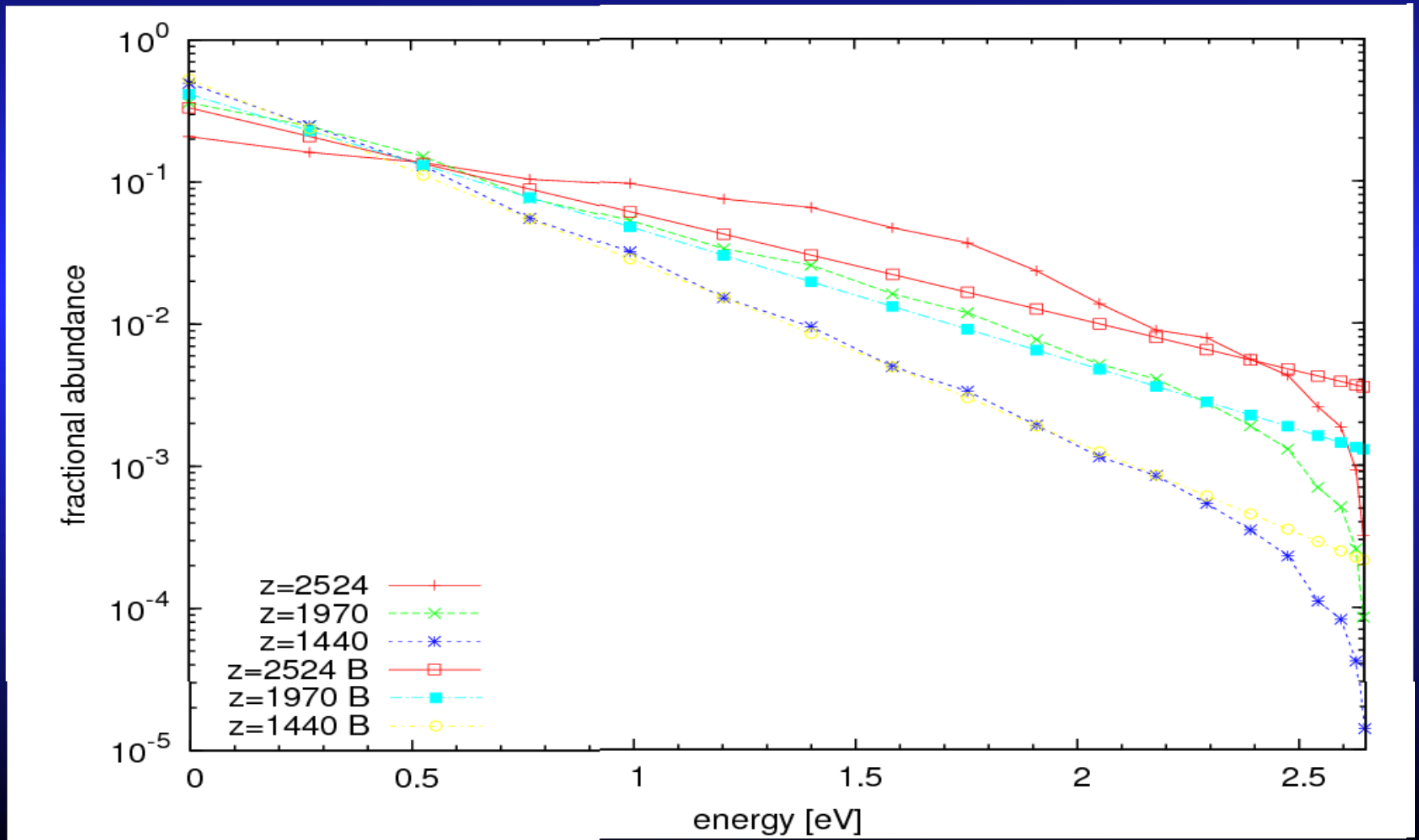
# RESULTS: VDF H<sub>2</sub> (III)



# RESULTS: VDF $H_2^+$ (I)

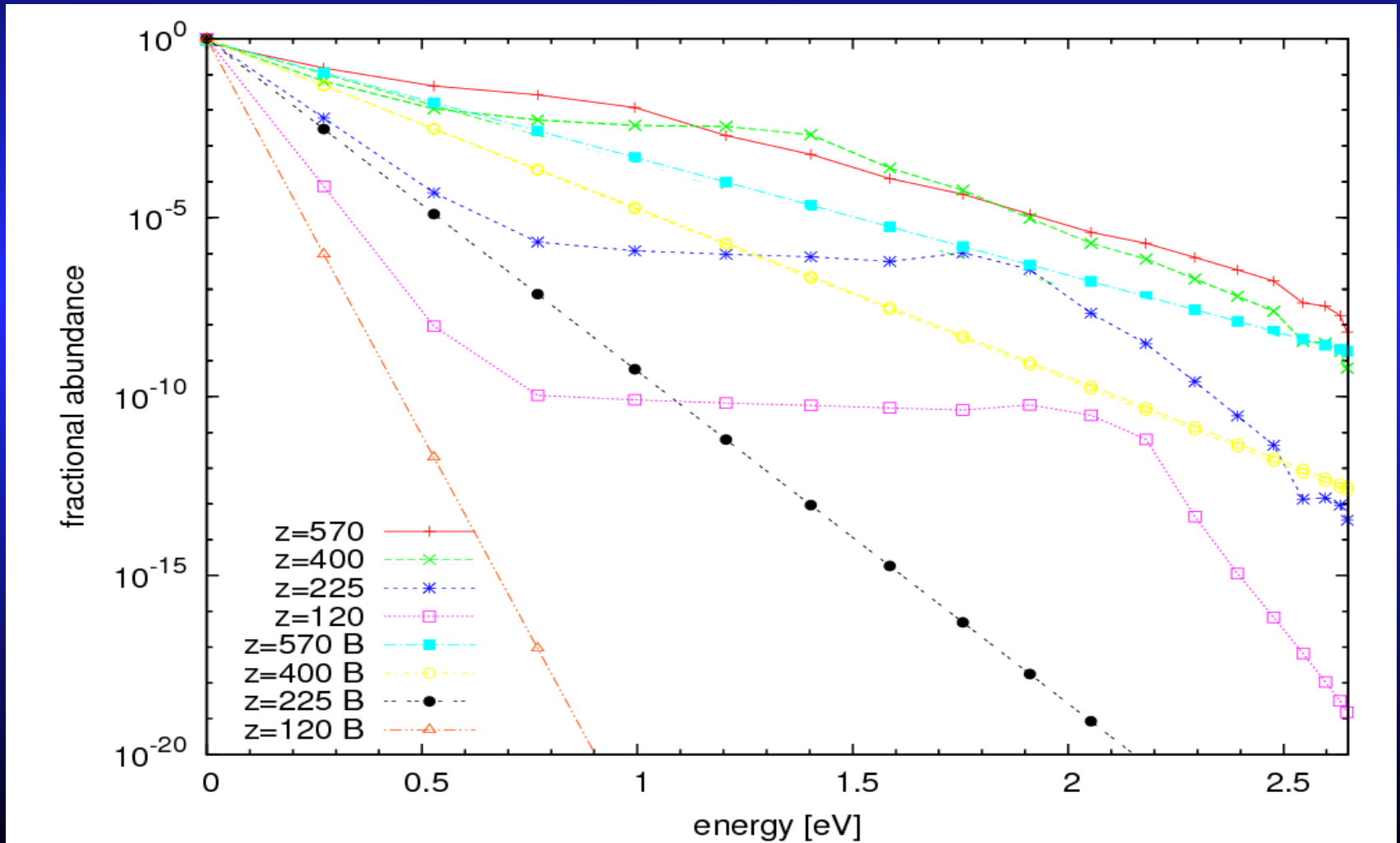


# RESULTS: VDF H<sub>2</sub><sup>+</sup> (II)

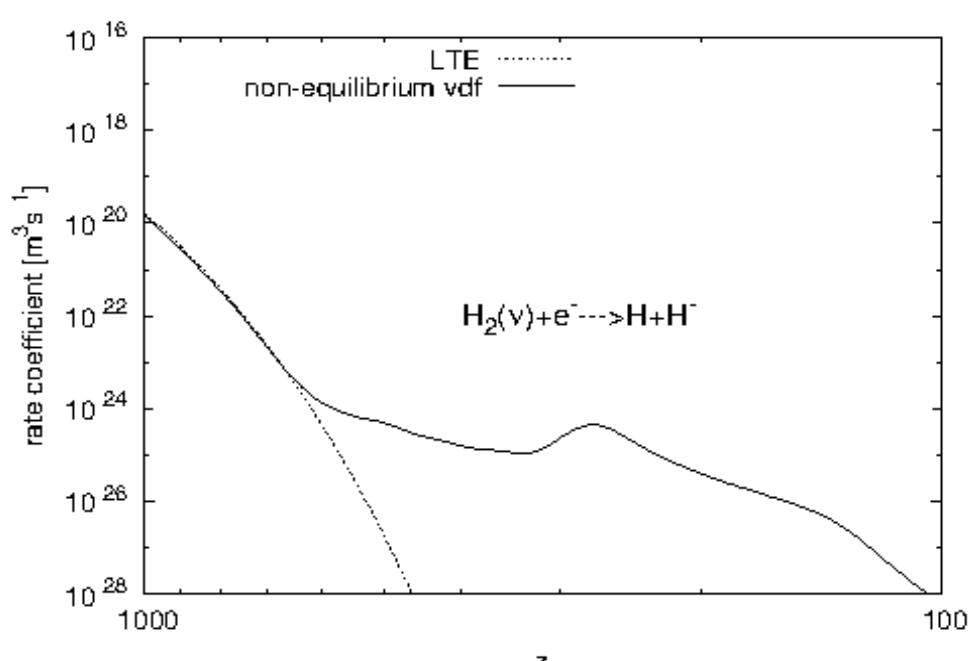
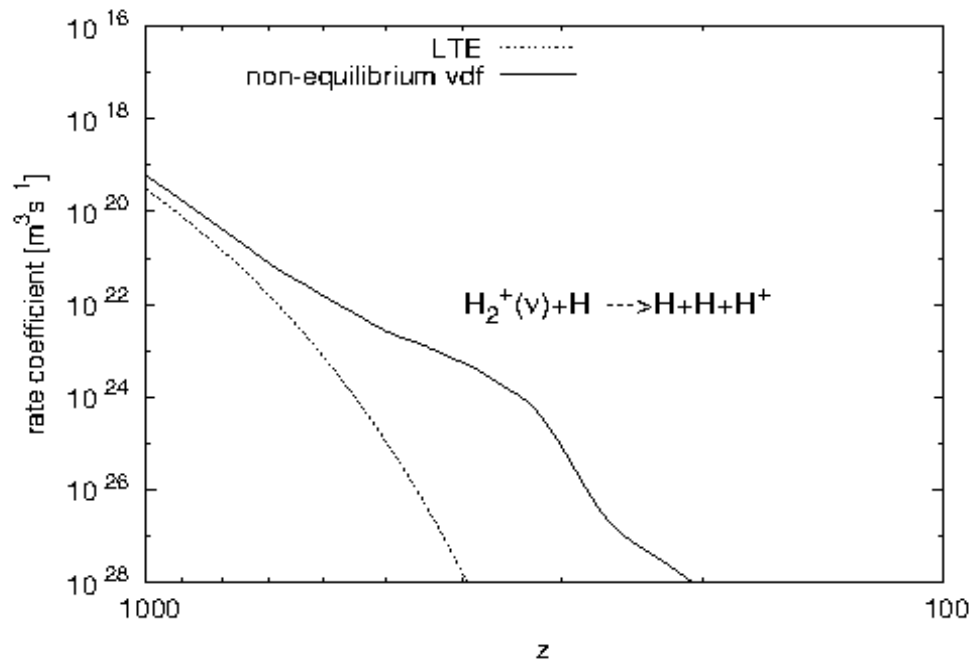
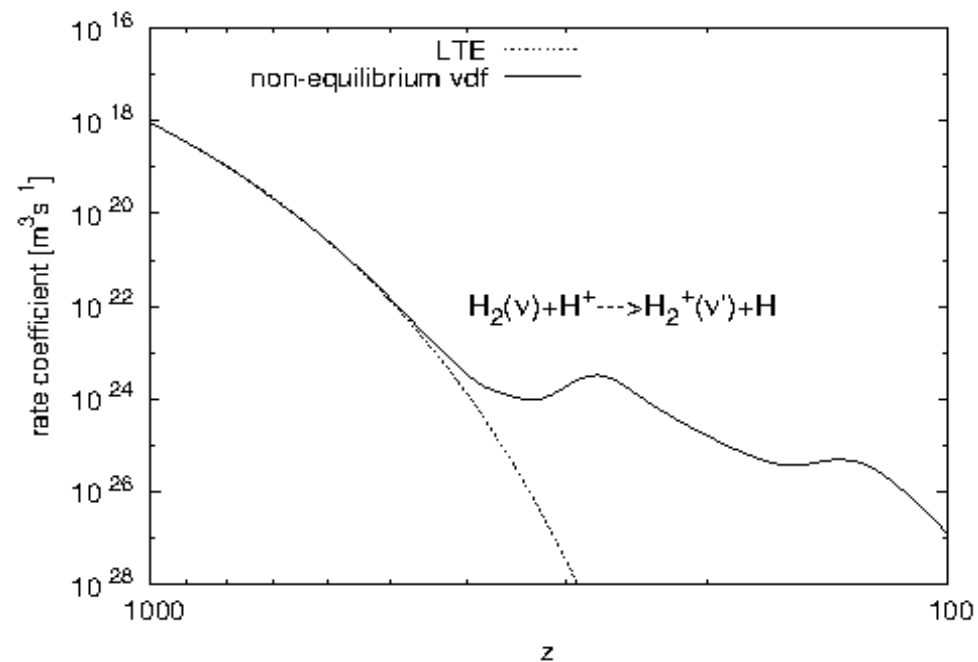
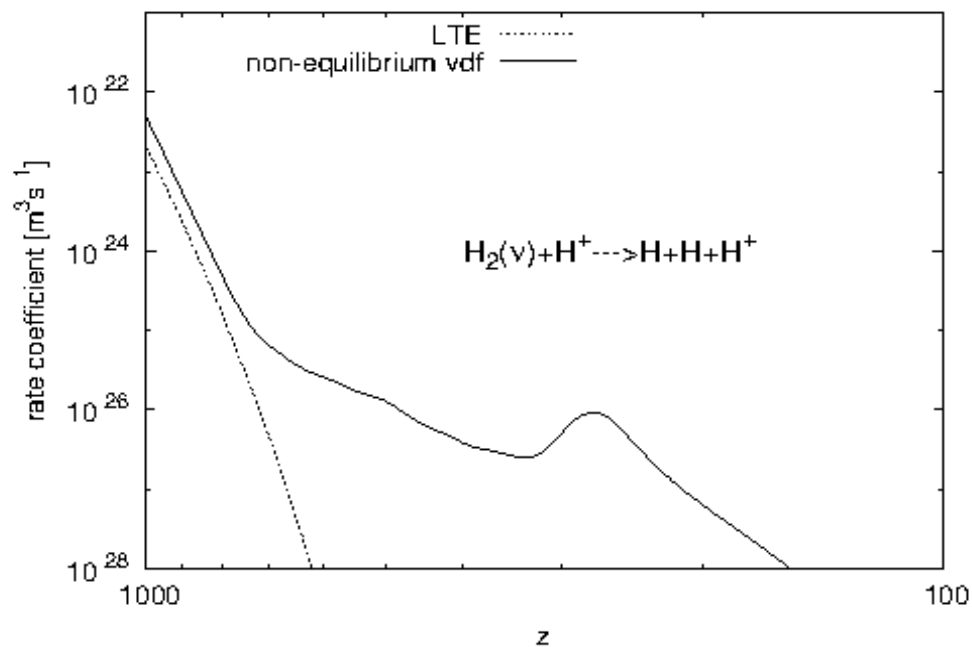




# RESULTS: VDF $H_2^+$ (III)

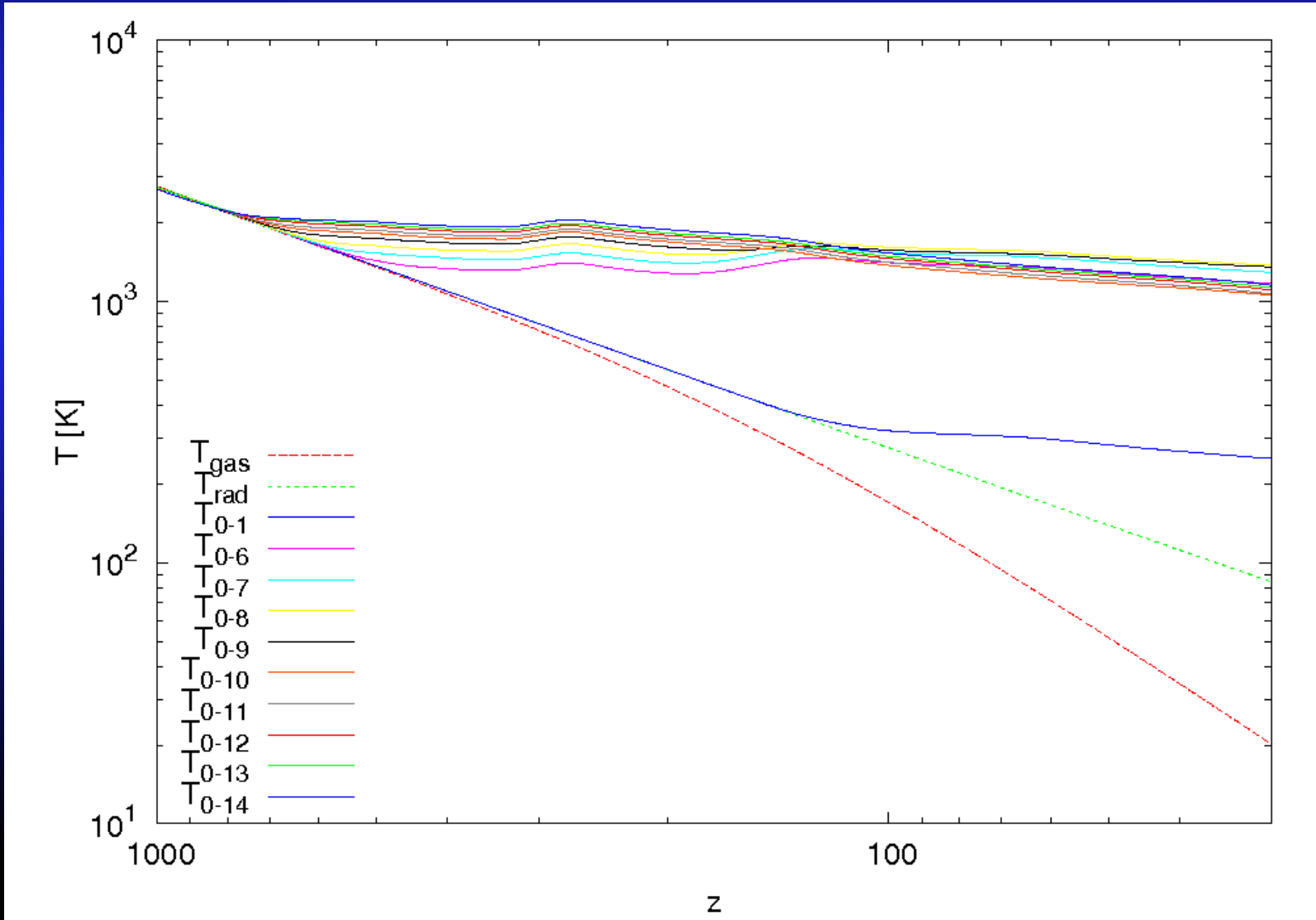


# “MODIFIED” RATE COEFFICIENTS



# EXCITATION TEMPERATURES

$$T_{0-v} = \frac{E_v - E_0}{k_B \ln(n_0/n_v)}$$



# BEYOND THE “STANDARD” KINETICS...

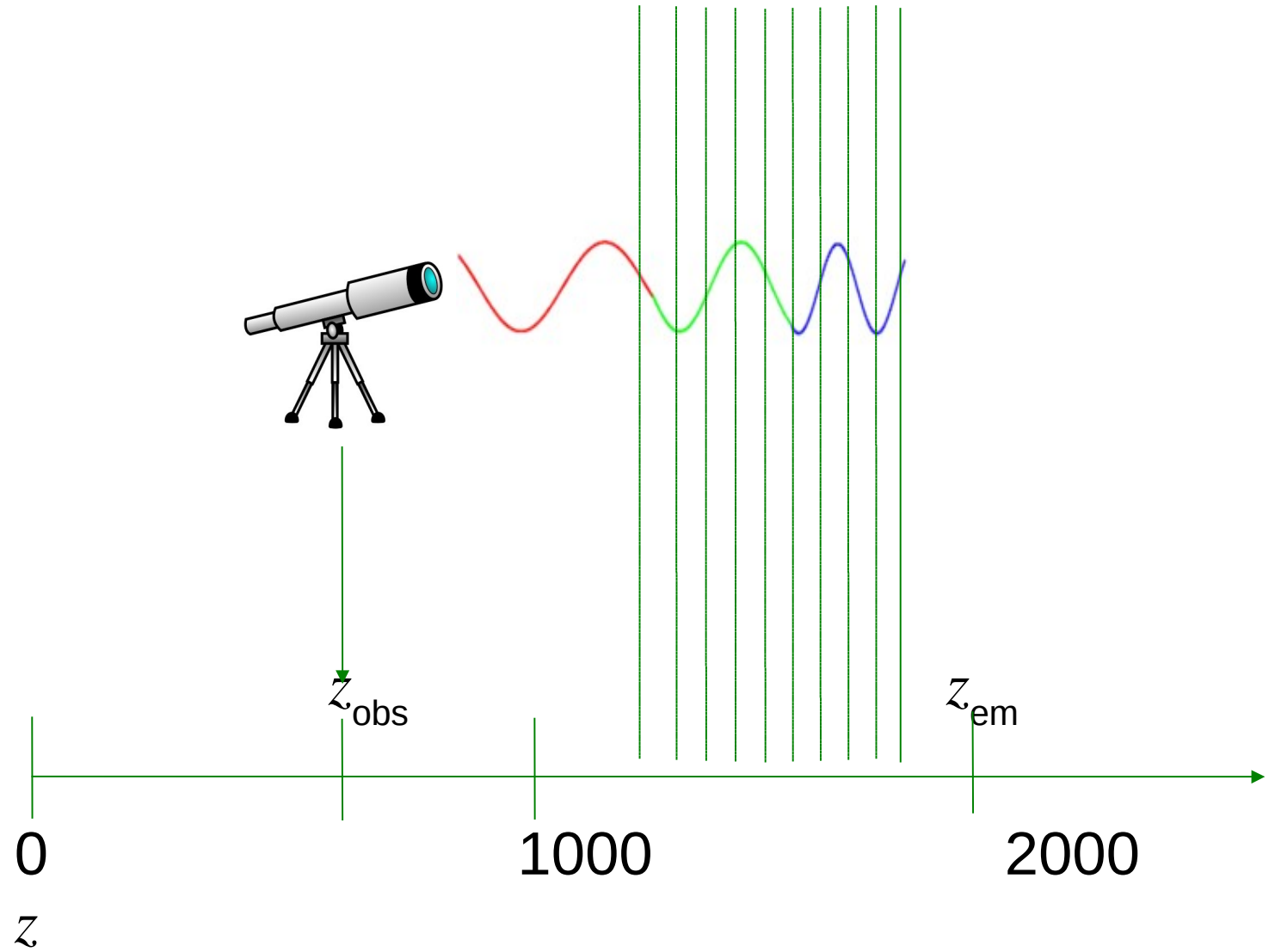
Non-equilibrium effects:

- state-to-state kinetics  Maxwell-Boltzmann's distributions

?

- CMB photons  Planck's distribution

# SPECTRAL DISTORTIONS




## SPECTRAL DISTORTIONS

$$\dot{j}_{\nu_{ij}}(z) = h\nu_{ij} \Delta R_{ij}(z) \phi(\nu(z))$$

$$\Delta R_{ij}(\nu) = A_{ij} N_i \frac{e^{h\nu_{ij}/kT_r}}{e^{h\nu_{ij}/kT_r} - 1} \left[ 1 - \frac{N_j}{N_i} e^{-h\nu_{ij}/kT_r} \right]$$

$$I_{ij}^{z_{obs}}(\nu) = \frac{c}{4\pi} \int_{z_{em}}^{z_{obs}} \frac{\dot{j}_{\nu_{ij}}(z)}{(1+z)^3} (1+z_{obs})^3 \left| \frac{dt}{dz} \right| dz$$


$$I_{ij}^{z_{obs}}(\nu) = \frac{ch}{4\pi} \frac{\Delta R_{ij}(z_{em})}{H(z_{em})} \frac{(1+z_{obs})^3}{(1+z_{em})^3}$$

# SPECTRAL DISTORTIONS

$$\frac{1}{c} \frac{dJ_\nu}{dz} = \frac{\kappa_\nu J_\nu - j_\nu}{H_0(1+z)^2 \sqrt{1+\Omega_0 z}} + \frac{3J_\nu}{c(1+z)}$$

$$\kappa_\nu = \frac{c^2}{8\pi\nu^2} n_l A_{ul} \frac{g_u}{g_l} \left(1 - \frac{g_l n_u}{g_u n_l}\right) \phi(\nu - \nu_{ul})$$

$$j_\nu = \frac{h\nu}{4\pi} n_u A_{ul} \phi(\nu - \nu_{ul})$$

$$\left. \frac{\Delta J_\nu}{J_\nu} \right|_{z=0} = [R(z_i) - 1] [1 - e^{-\tau(z_i)}]$$

$$R(z_i) = \left[ \frac{g_u n_l(z_i)}{g_l n_u(z_i)} - 1 \right]^{-1} \left\{ \exp \left[ \frac{h\nu_{ul}}{kT_r(z_i)} \right] - 1 \right\}$$

# SPECTRAL DISTORTIONS

- matter/antimatter annihilation
- decaying particles
- interaction with matter

.....

- primordial atomic recombination ( $z \sim 1100$ )

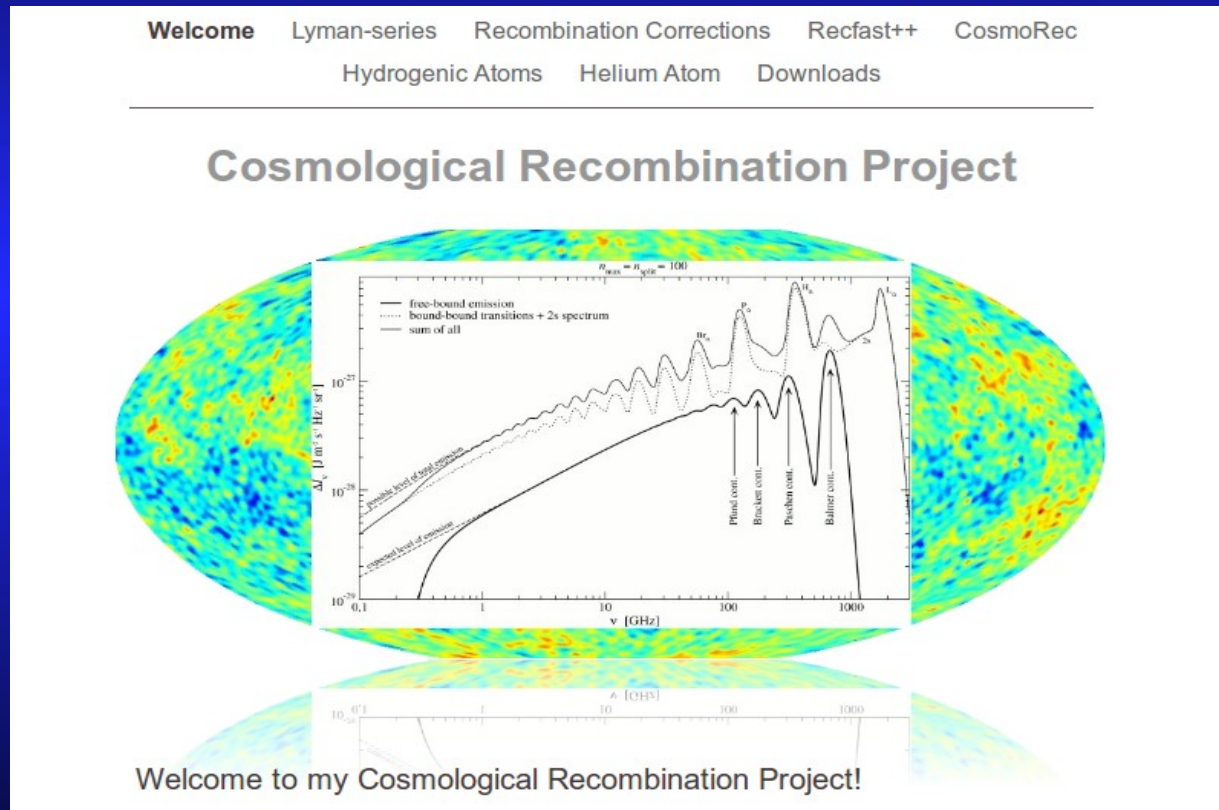


- molecular radiative cascade





# PRIMORDIAL ATOMIC RECOMBINATION



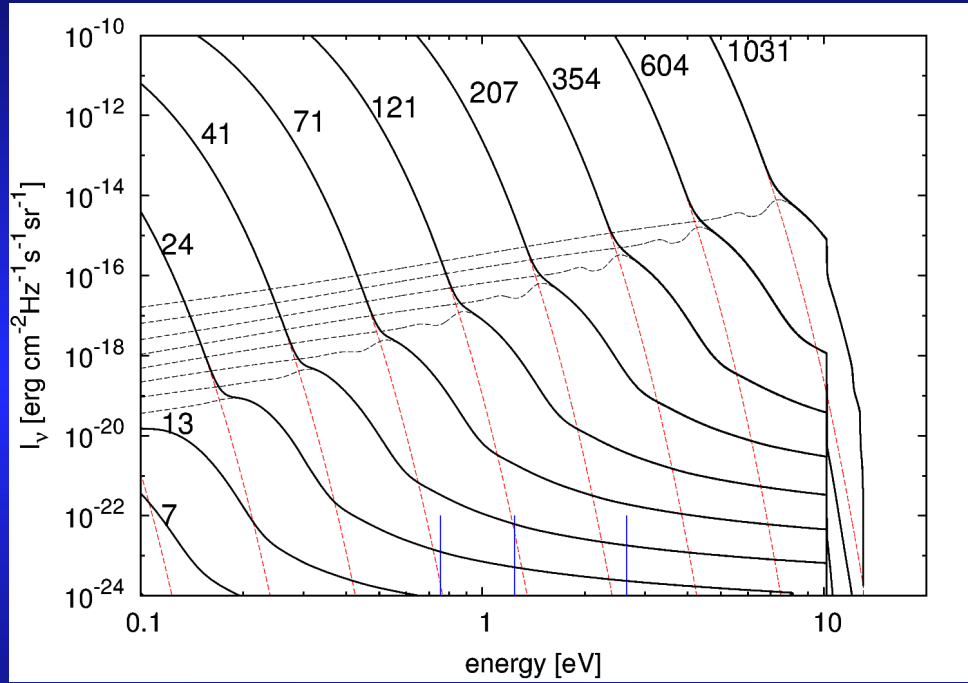
CosmoRec

by

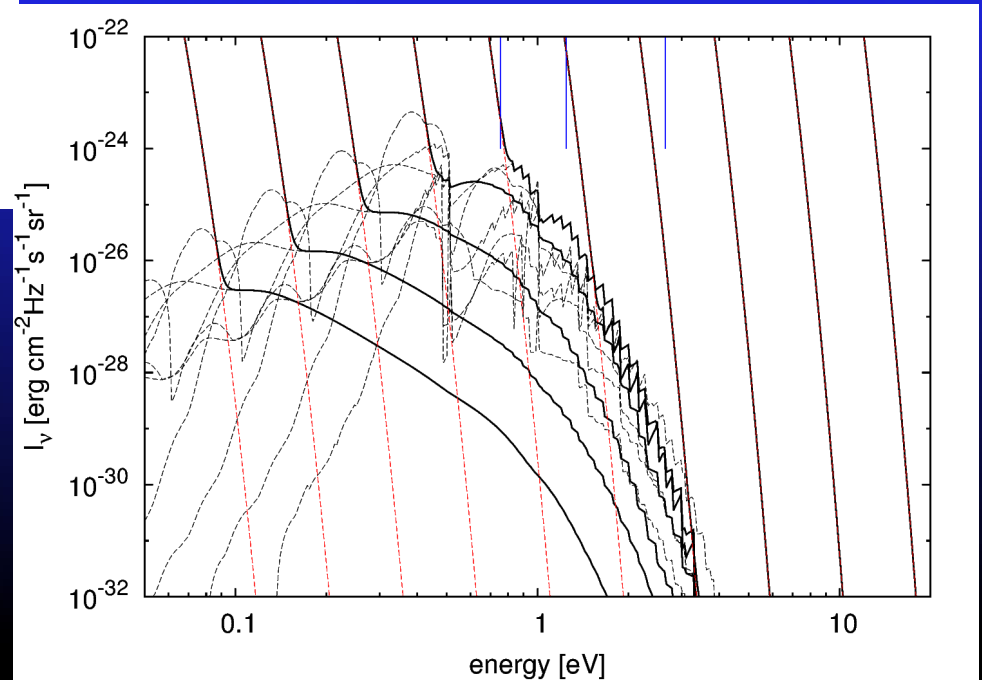
Jens Chluba

- effective multi-level approach;
- fast and accurate ( $\sim 1.3$  sec)
- solves a detailed radiative transfer problem for Ly-n
- available @ [www.Chluba.de/CosmoRec](http://www.Chluba.de/CosmoRec)

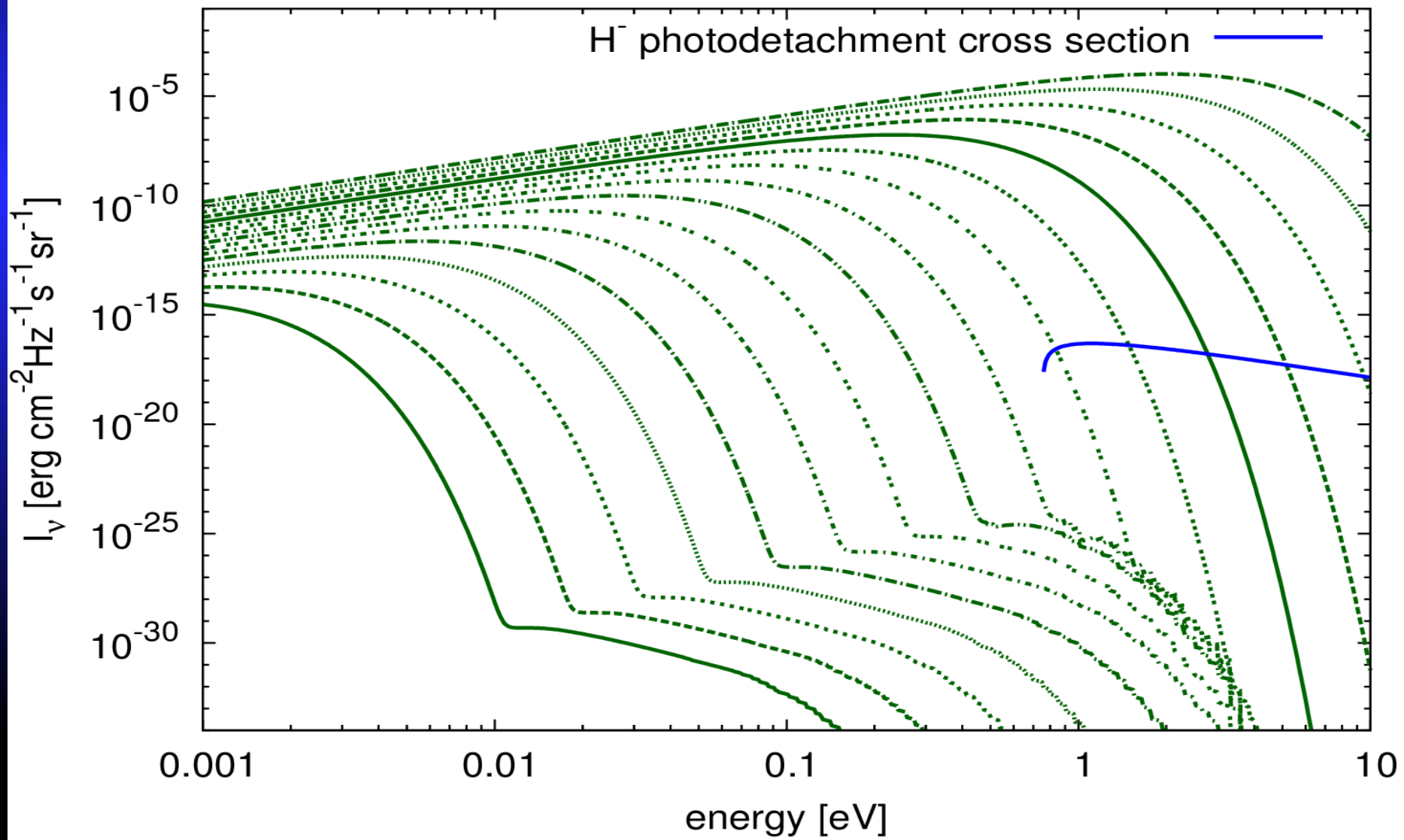
# SPECTRAL DISTORTIONS



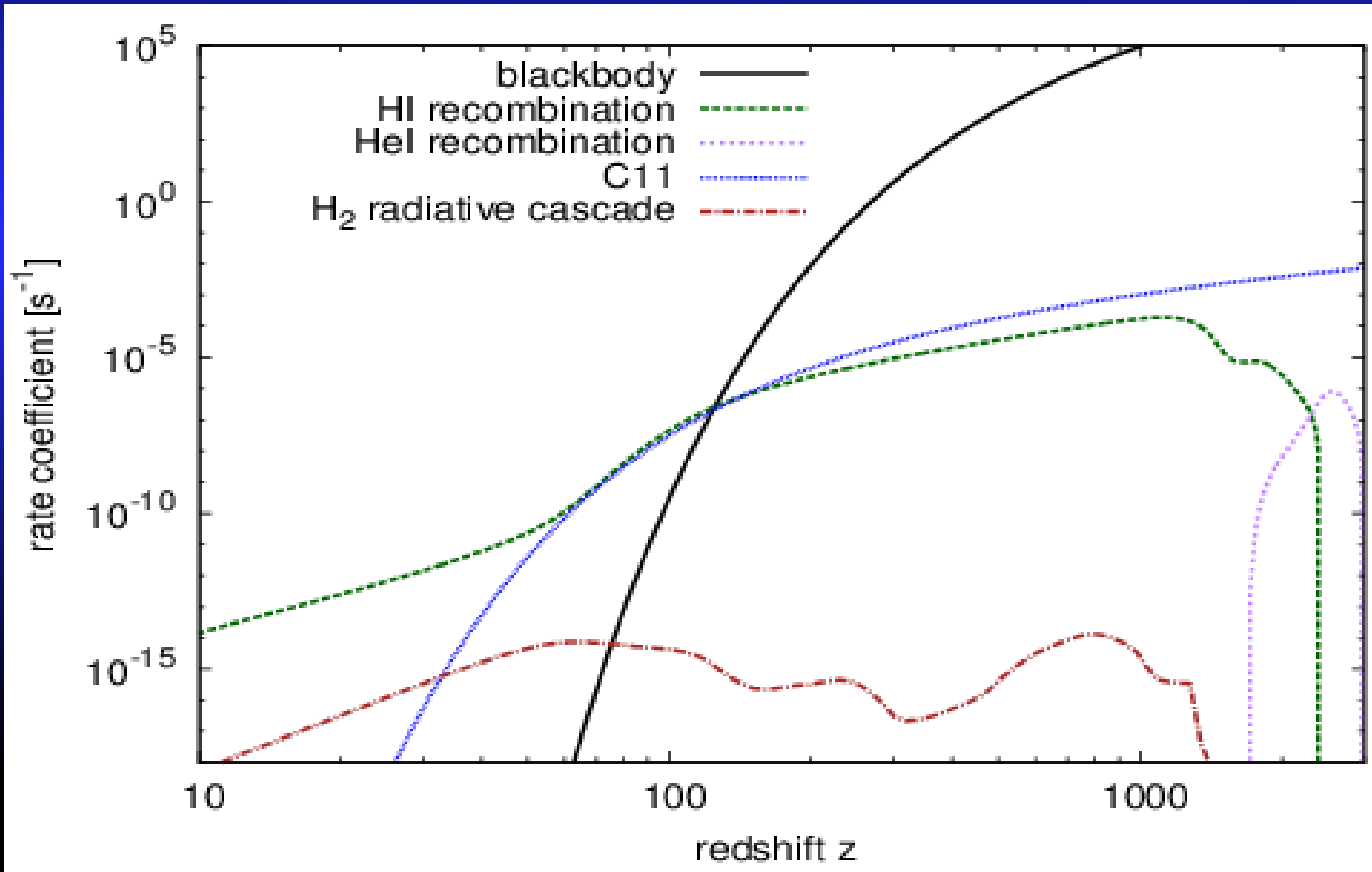
Coppola et al. 2013  
MNRAS **434** (1) 114-122



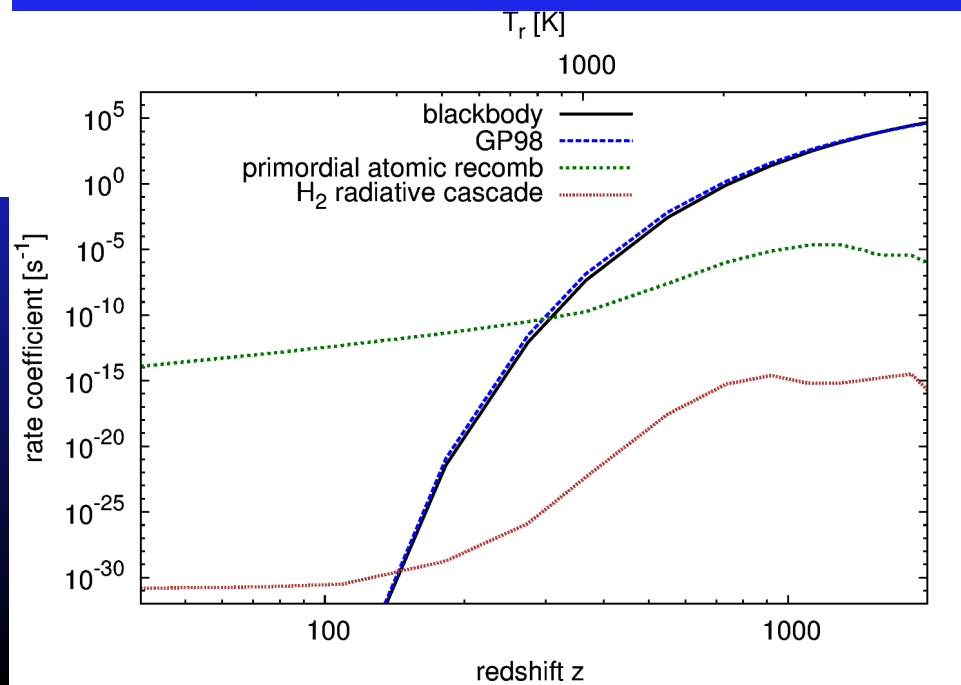
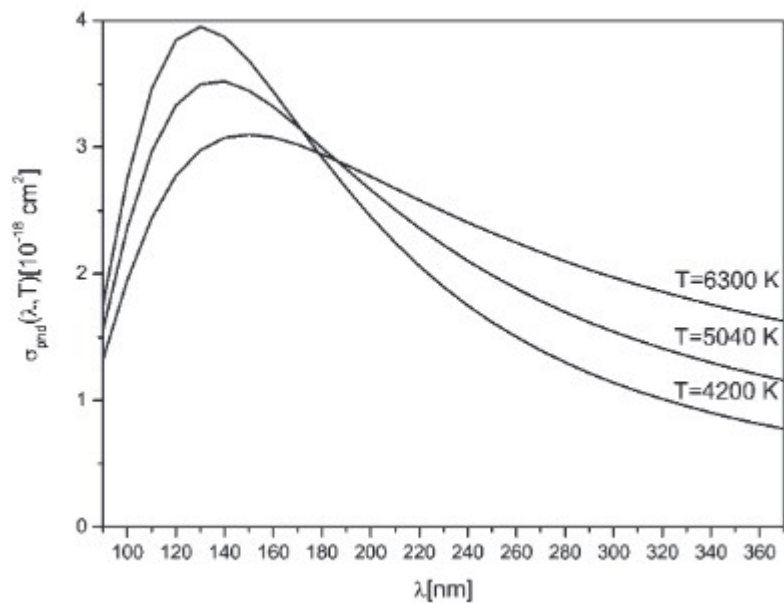
# SPECTRAL DISTORTIONS



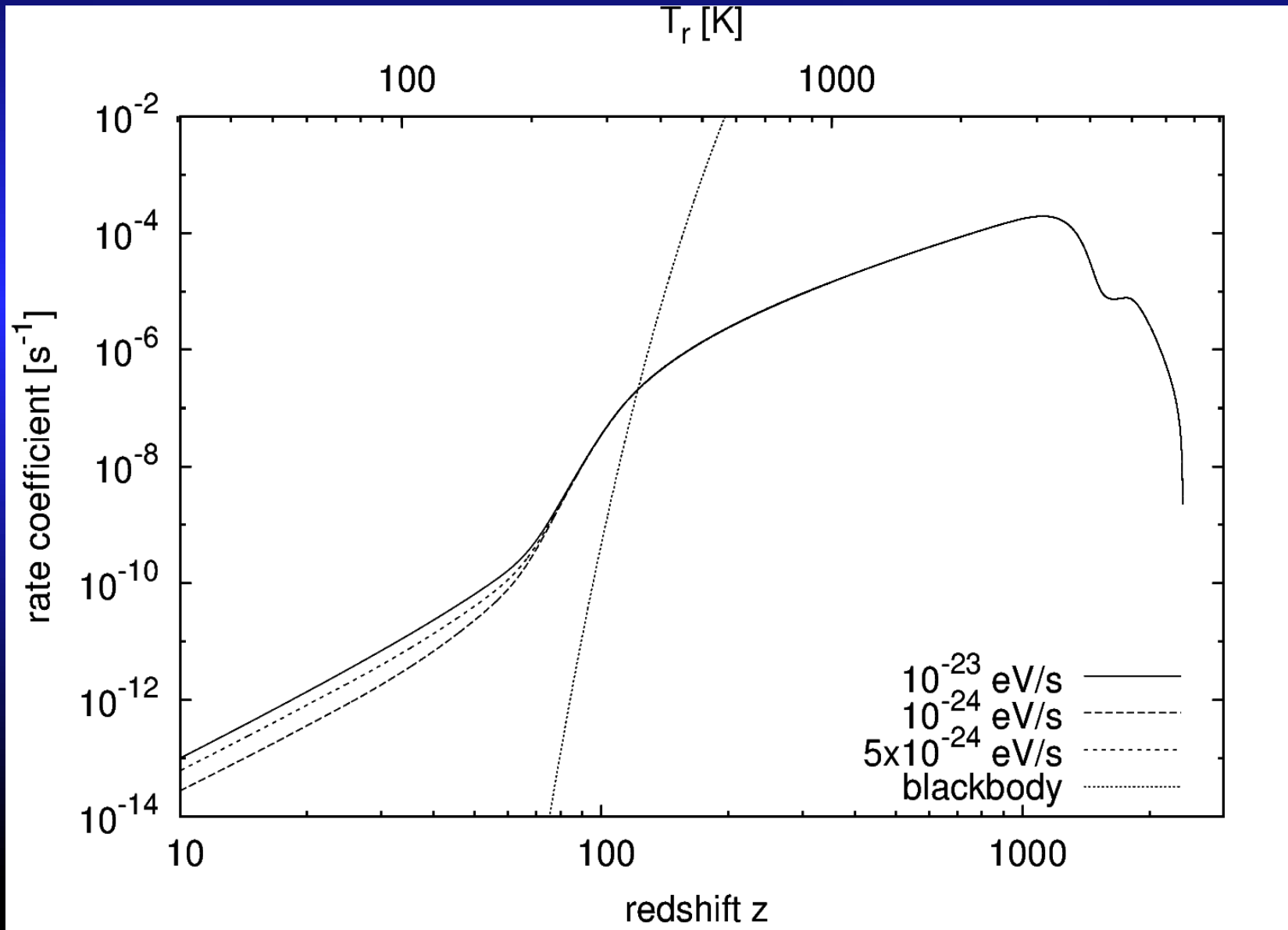
# SPECTRAL DISTORTIONS: $H^-$ photodetachment



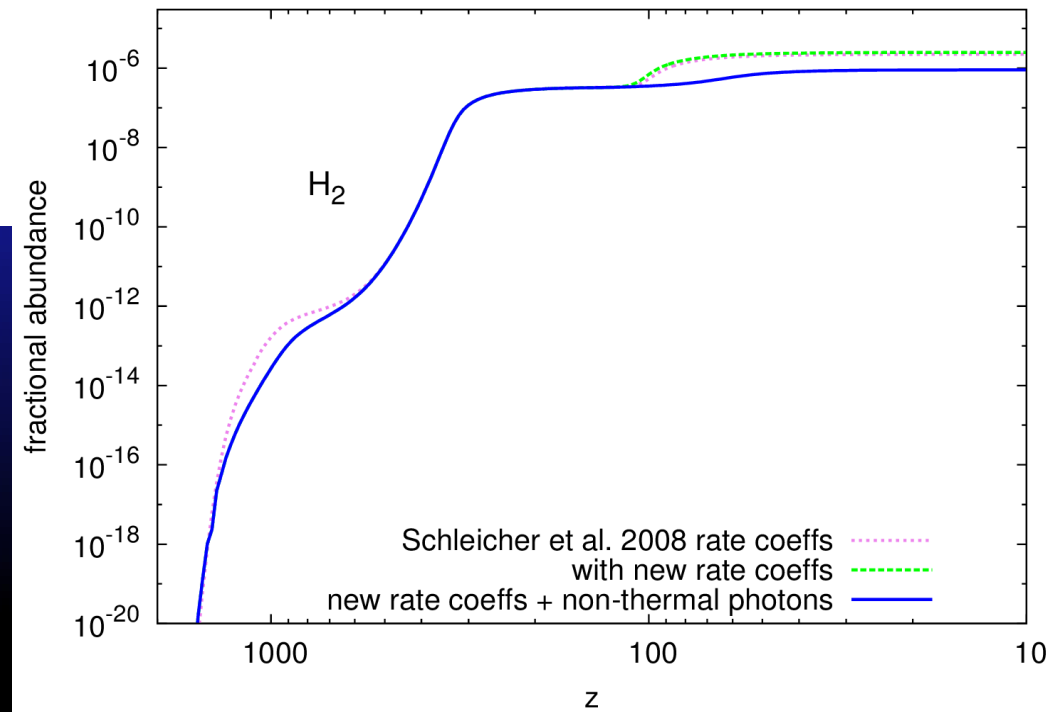
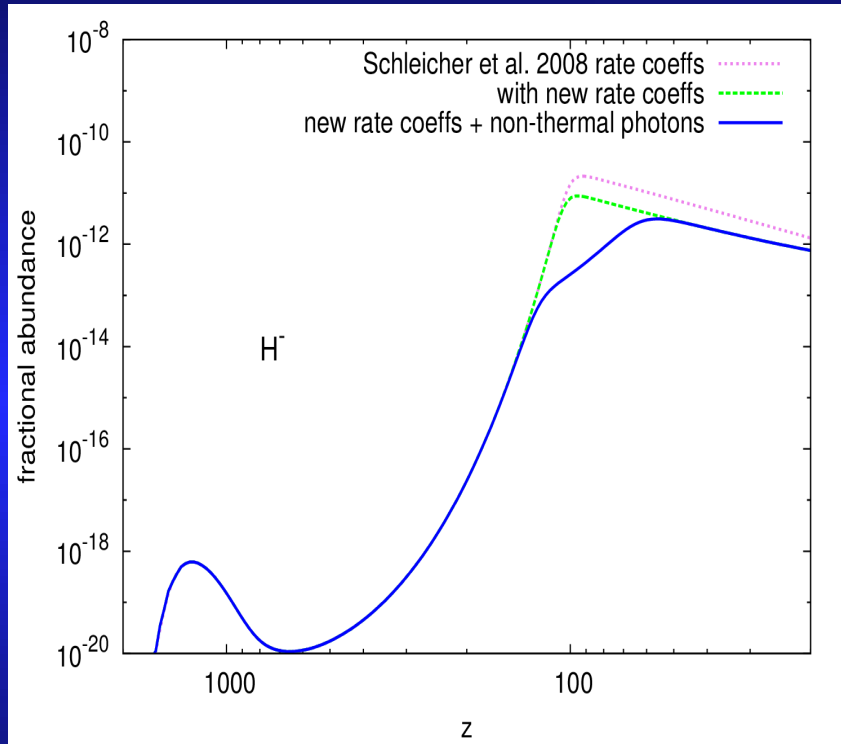
# SPECTRAL DISTORTIONS: $H_2^+$ photodissociation



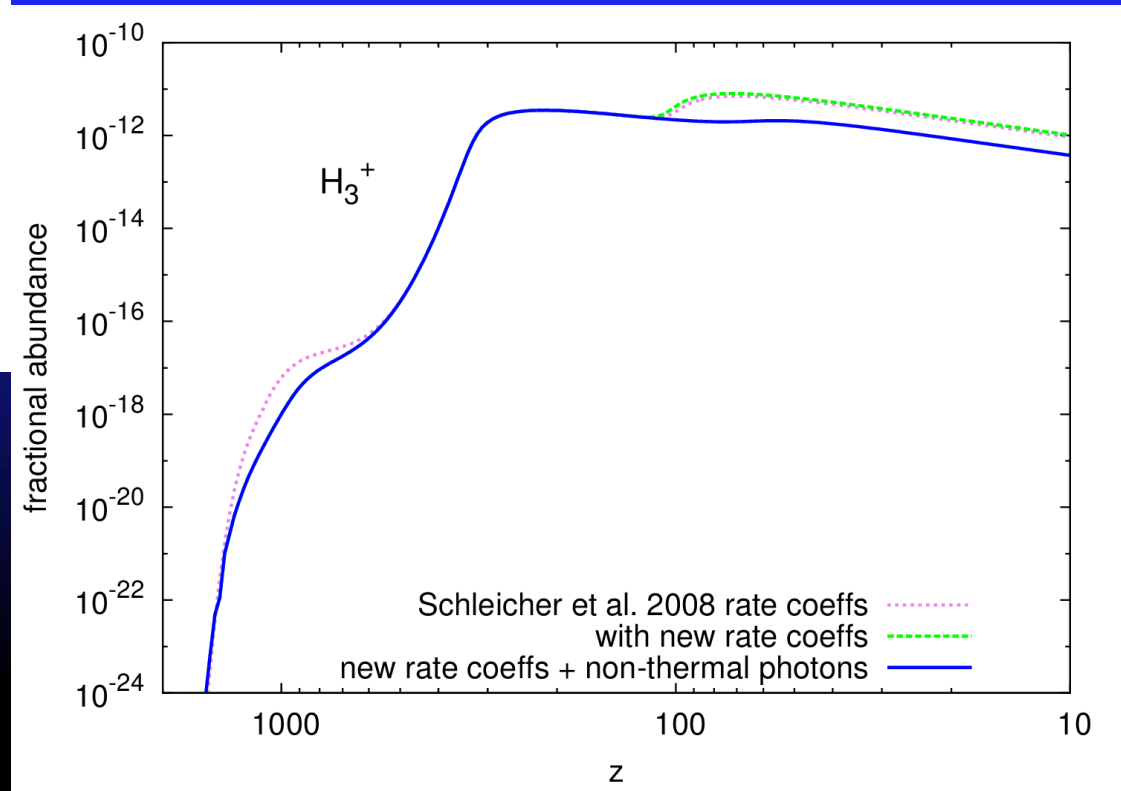
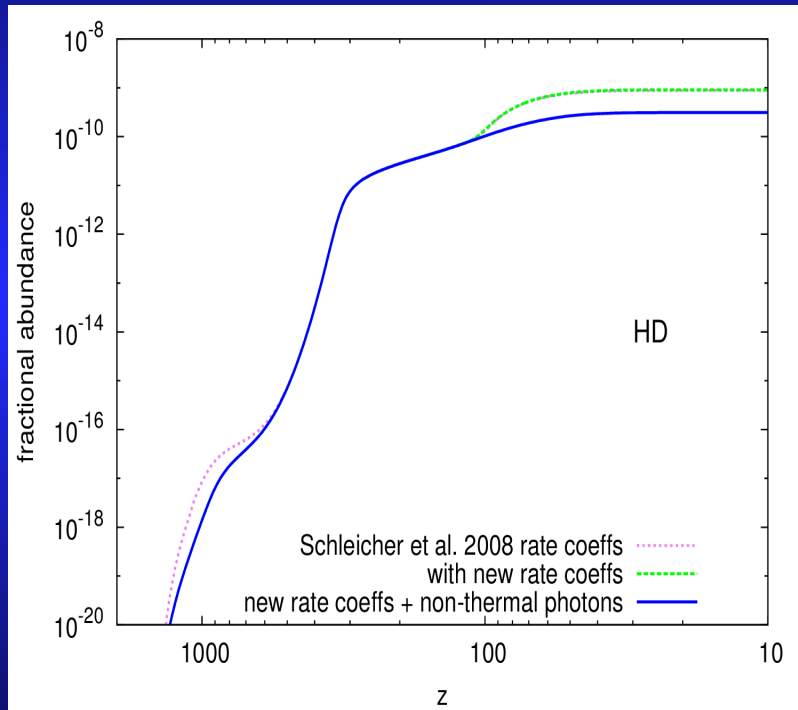
# SPECTRAL DISTORTIONS: DARK MATTER ANNIHILATION



# SPECTRAL DISTORTIONS

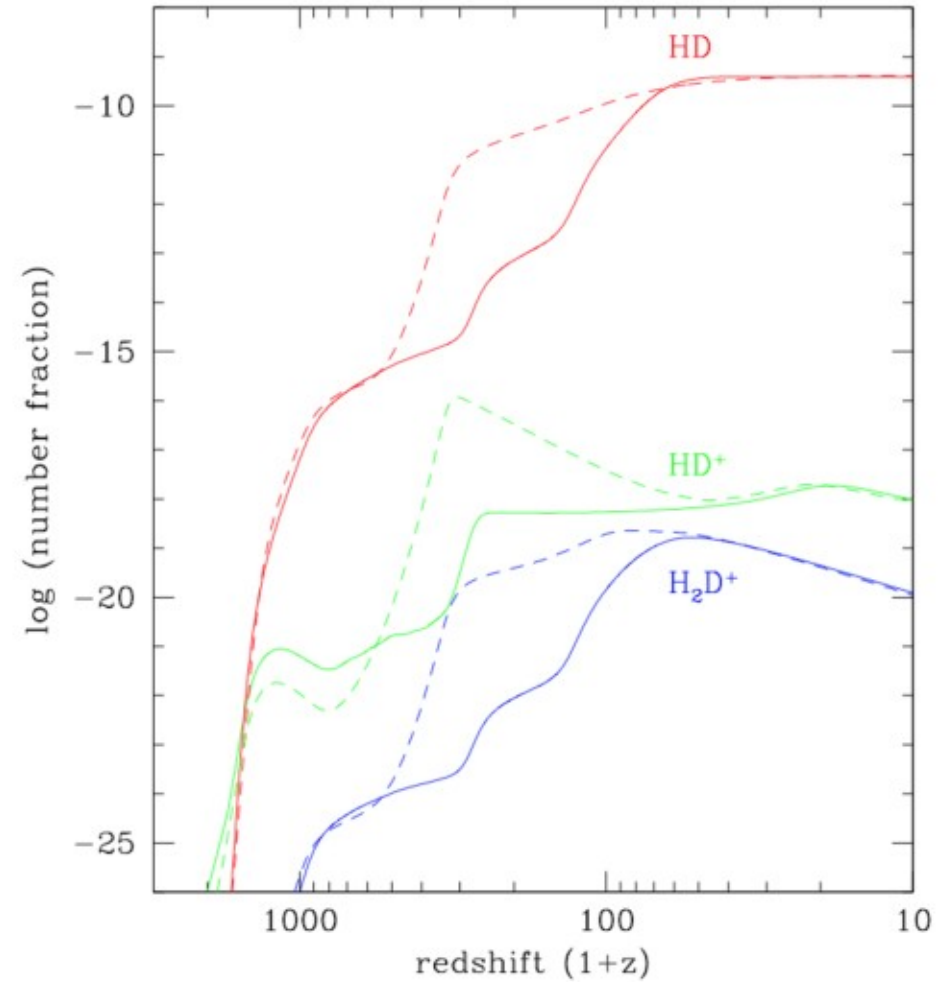
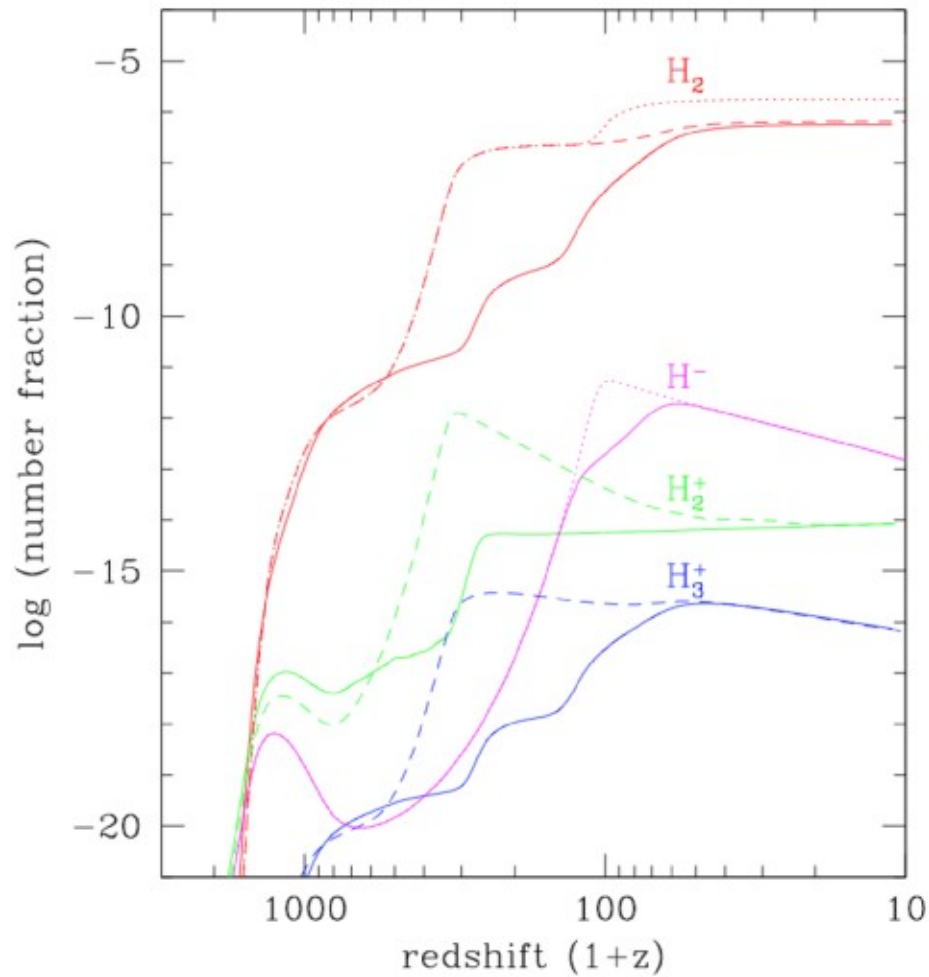


# SPECTRAL DISTORTIONS



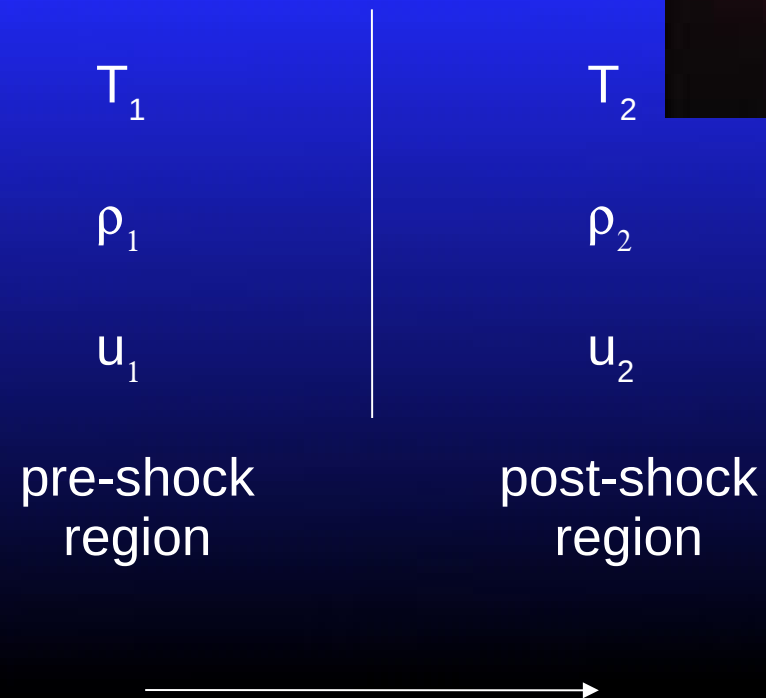


# “MODIFIED” FRACTIONAL ABUNDANCES



# MOVING TO PREGALACTIC SHOCKS...

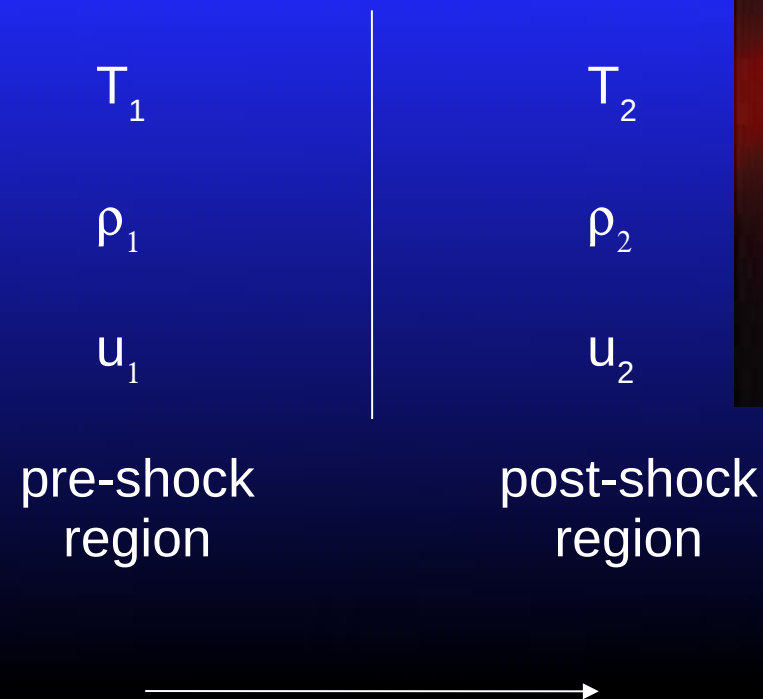
- Steady state shock
- 1D, plane symmetric
- Homogeneous IGM @ fixed  $z$



# PREGALACTIC SHOCKS: APPROXIMATIONS

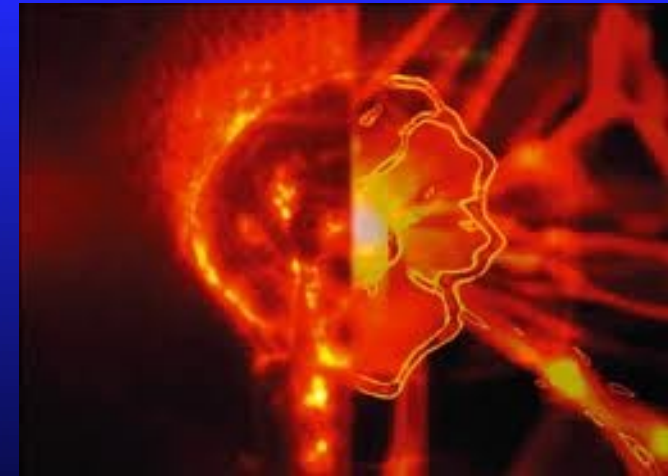
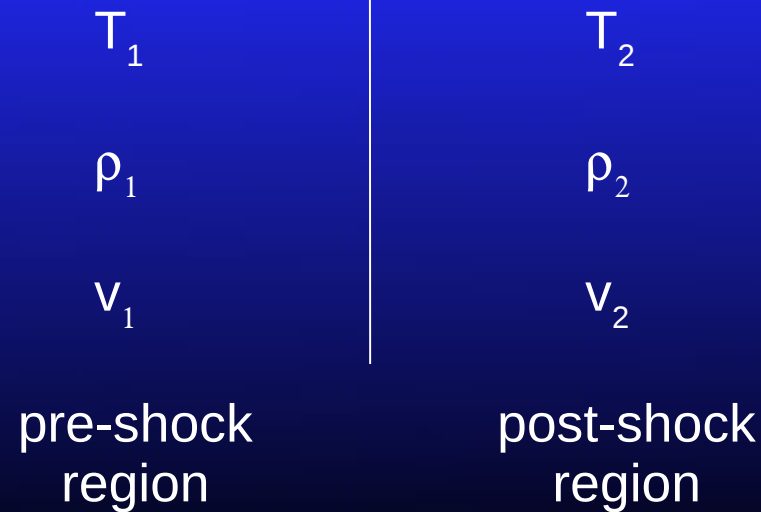
$J\nu \longrightarrow$  CMB @  $z = 10$

- no external radiation field (only CMB);
- steady, plane-parallel shock wave propagating through the homogeneous medium which is at rest and consists of a pure hydrogen gas
- no gravitational forces from external sources
- cosmological adiabatic cooling neglected

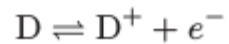


# PREGALACTIC SHOCKS: JUMP CONDITIONS ACROSS THE SHOCK FRONT

$$\begin{aligned}
 & \rho_2 v_2 = \rho_1 v_s && \text{mass} \\
 & \rho_2 v_2^2 + p_2 = \rho_1 v_s^2 + p_1 && \text{momentum} \\
 & v_2 \left( \frac{\rho_2 v_2^2}{2} + \frac{\gamma_2}{\gamma_2 - 1} p_2 \right) = v_s \left( \frac{\rho_1 v_s^2}{2} + \frac{\gamma_1}{\gamma_1 - 1} p_1 \right) && \text{energy}
 \end{aligned}
 \left. \vphantom{\begin{aligned} \rho_2 v_2 = \rho_1 v_s \\ \rho_2 v_2^2 + p_2 = \rho_1 v_s^2 + p_1 \\ v_2 \left( \frac{\rho_2 v_2^2}{2} + \frac{\gamma_2}{\gamma_2 - 1} p_2 \right) = v_s \left( \frac{\rho_1 v_s^2}{2} + \frac{\gamma_1}{\gamma_1 - 1} p_1 \right) } \right\} \text{conservation}$$



# PREGALACTIC SHOCKS: INITIAL CONDITIONS



$$\rho_1 u_1 = \rho_2 u_2$$

$$p_1 + \rho_1 u_1^2 = p_2 + \rho_2 u_2^2$$

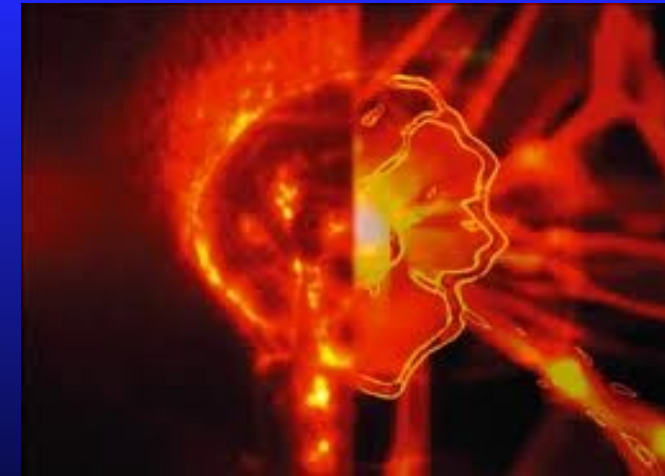
$$h_1 + \frac{u_1^2}{2} = h_2 + \frac{u_2^2}{2}$$

$$h_1 = \frac{5}{2} \frac{n_1 k_B T_1}{\rho_1}$$

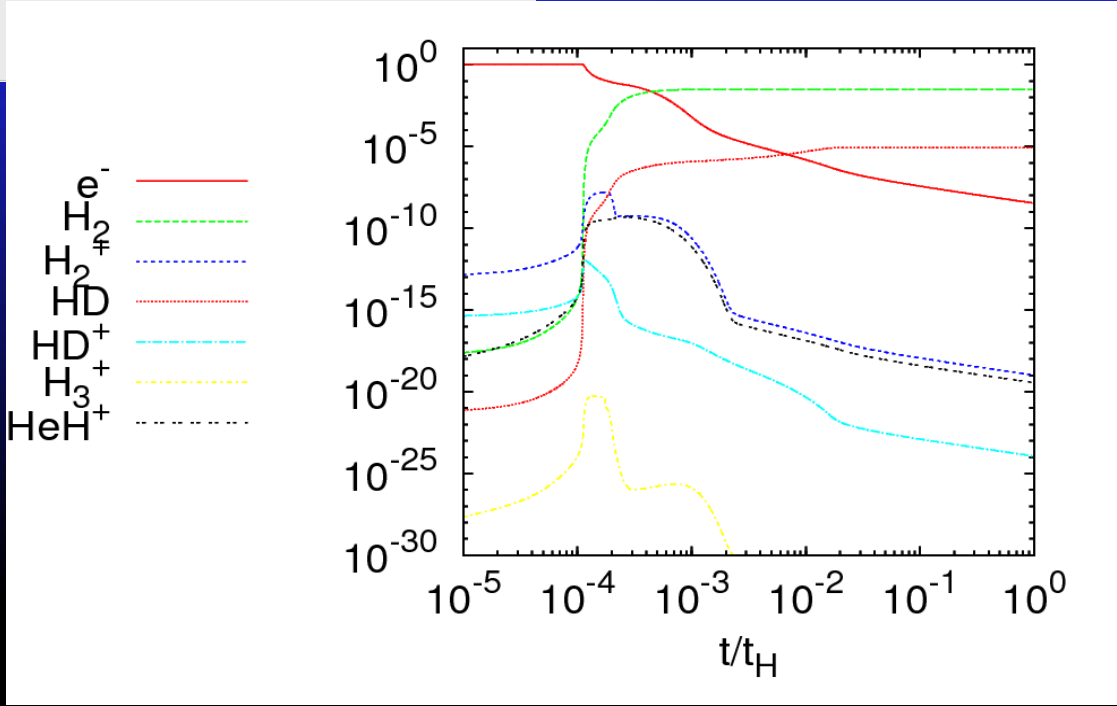
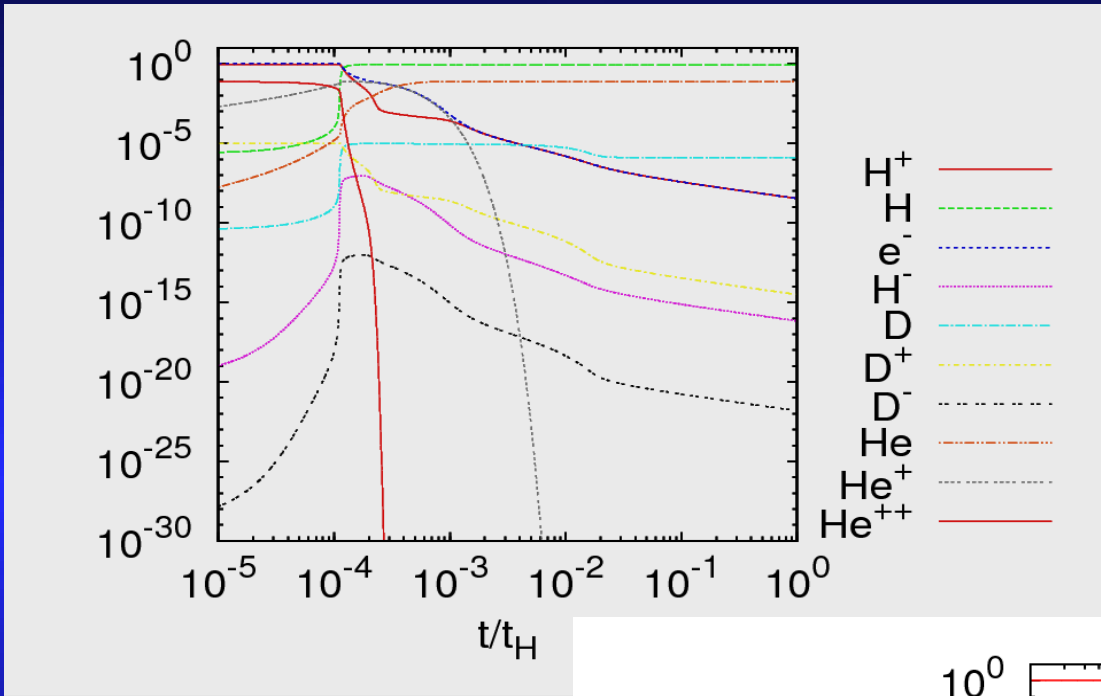
$$h_2 = \frac{5}{2} \frac{n_2 k_B T_2}{\rho_2} + \frac{(n_{2,\text{H}^+} I_{\text{H}} + n_{2,\text{D}^+} I_{\text{D}} + n_{2,\text{He}^+} I_{\text{He}})}{\rho_2}$$

$$v = 200 \text{ km/s}$$

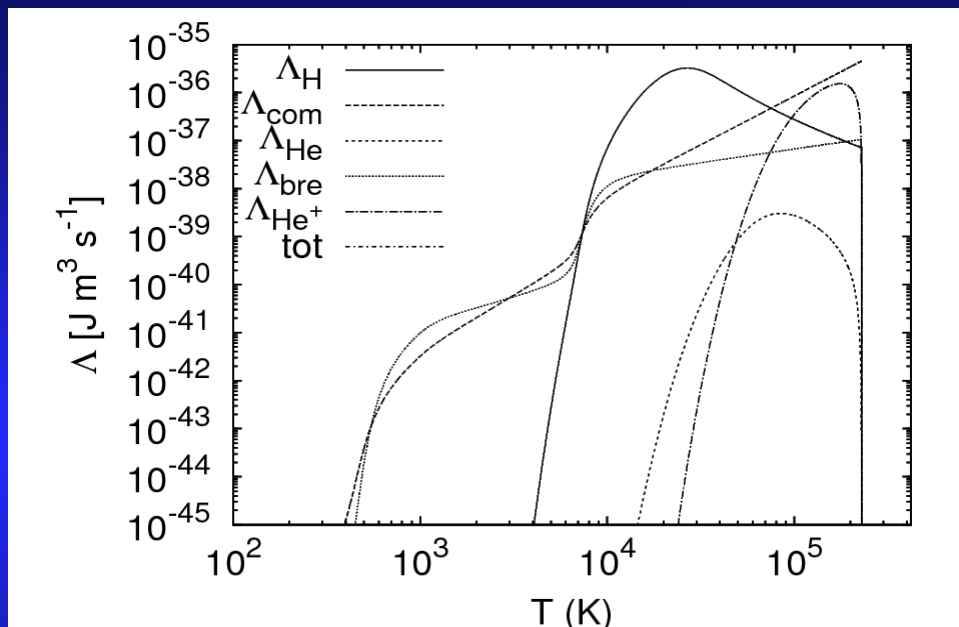
$$4v_1^2 y^2 - 5 \left( v_1^2 + \frac{kT_1}{m_1} \right) y + v_1^2 + 5 \frac{kT_1}{m_1} - 2 \times I = 0$$



# PREGALACTIC SHOCKS: FRACTIONAL ABUNDANCES

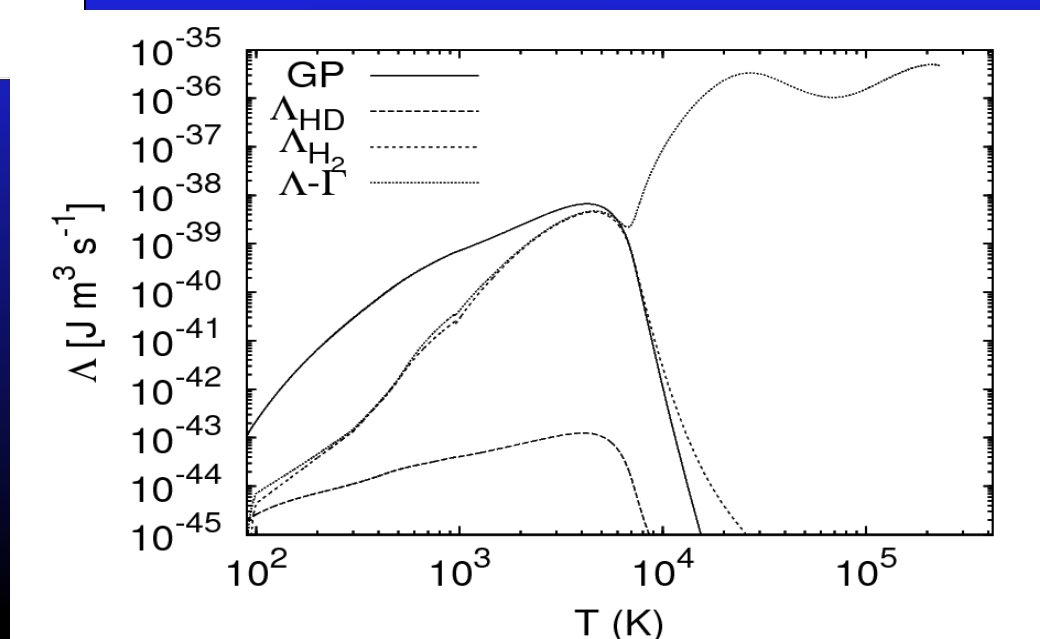


# PREGALACTIC SHOCKS: COOLING FUNCTIONS

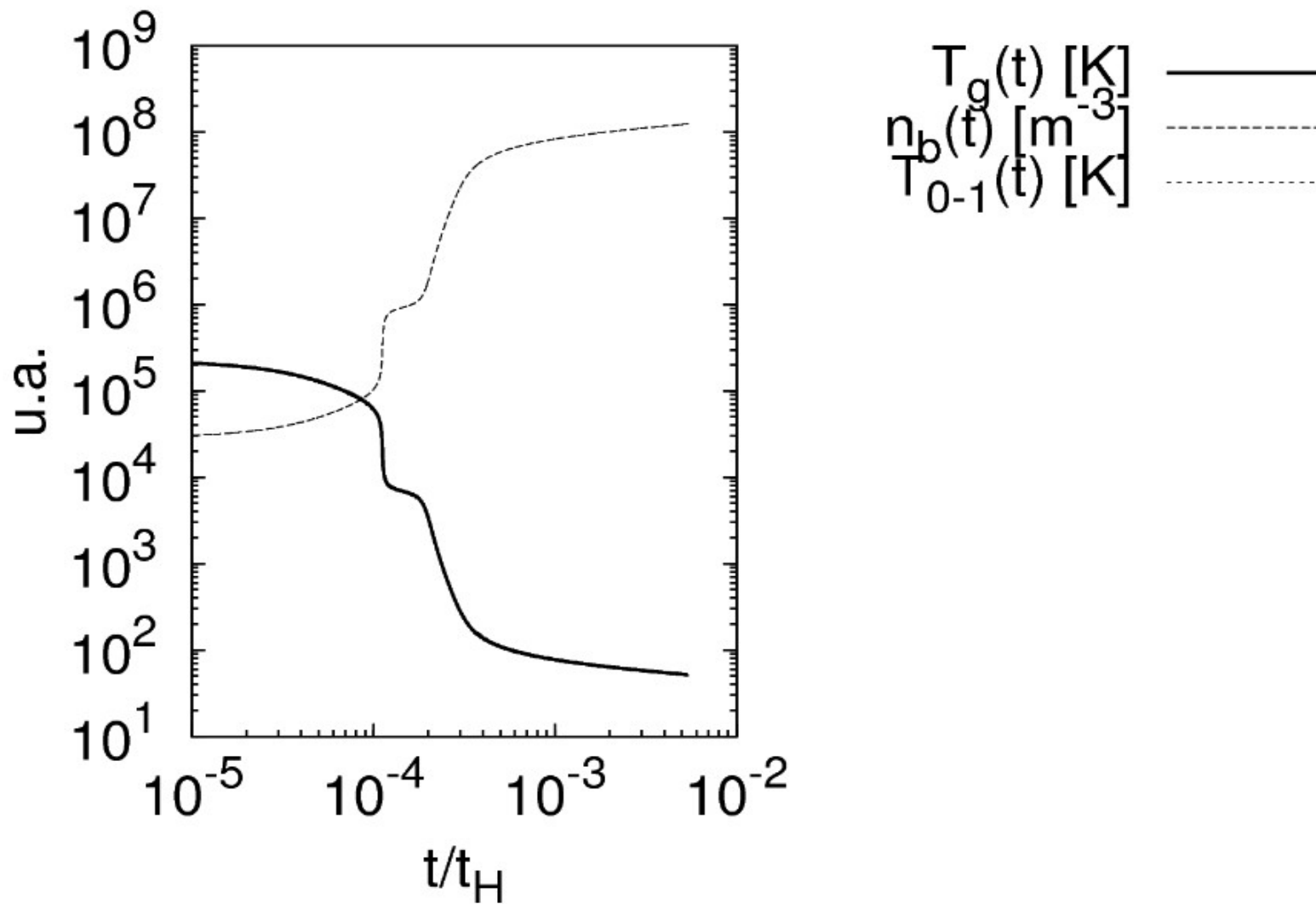


... @ high temperatures

... @ low temperatures

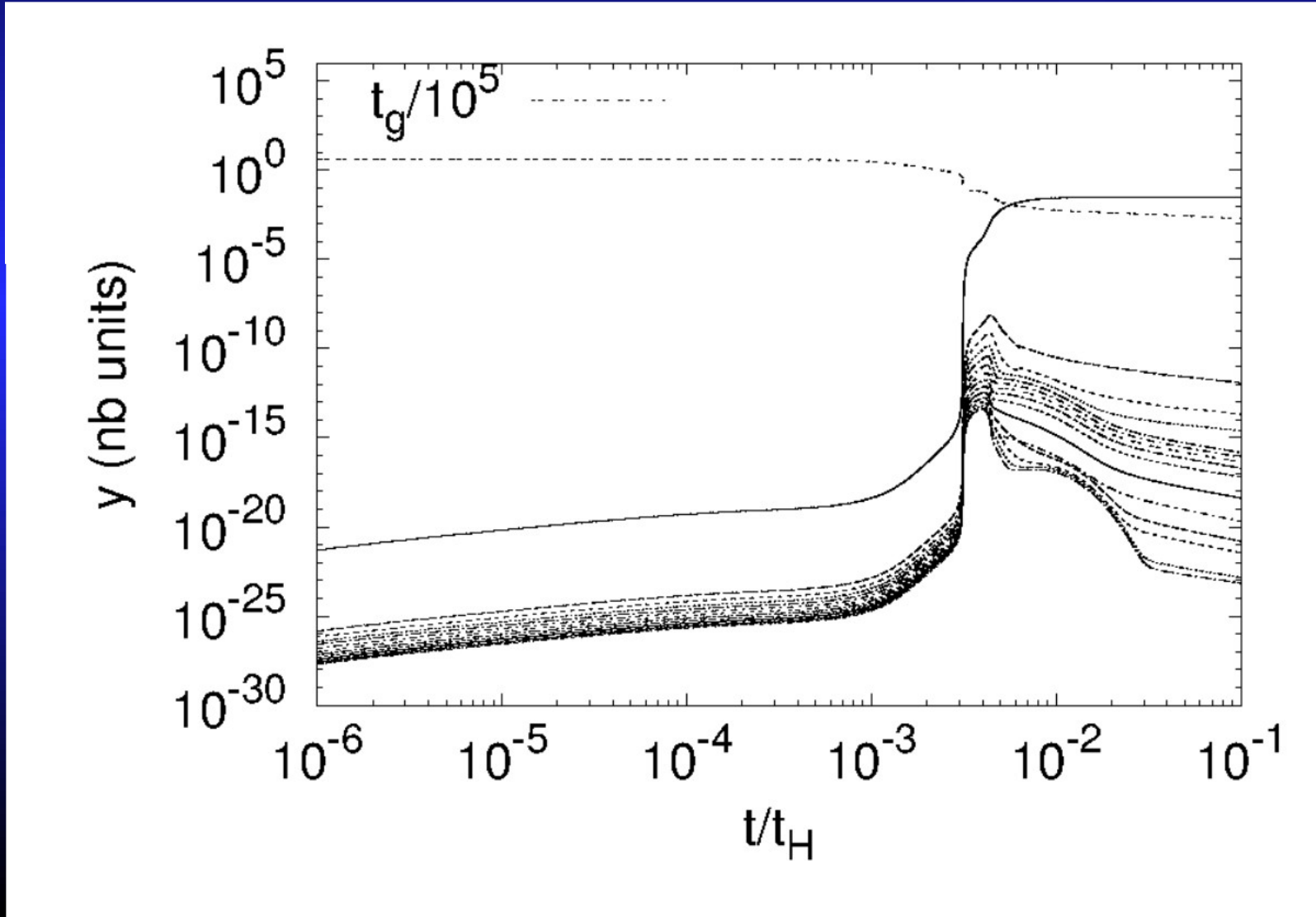


# PREGALACTIC SHOCKS: TEMPERATURE AND DENSITY PROFILES

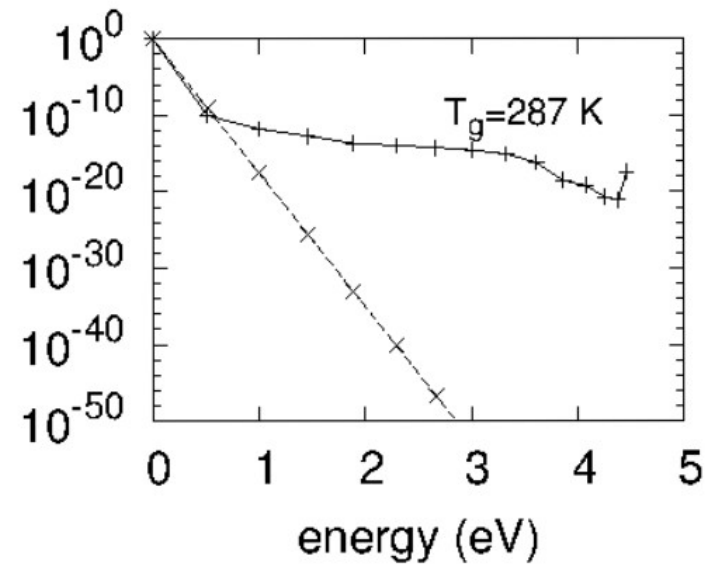
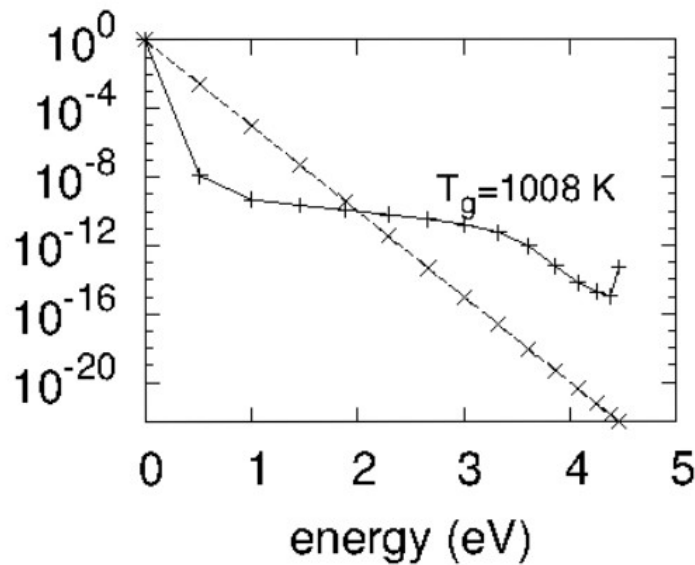
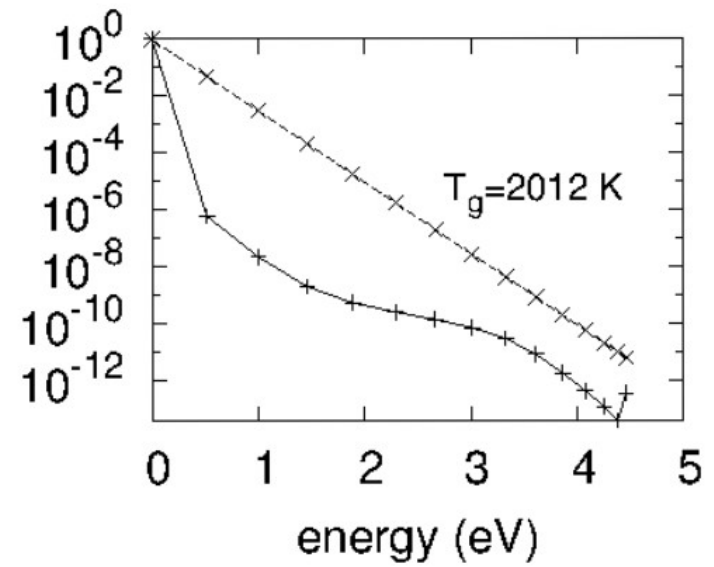
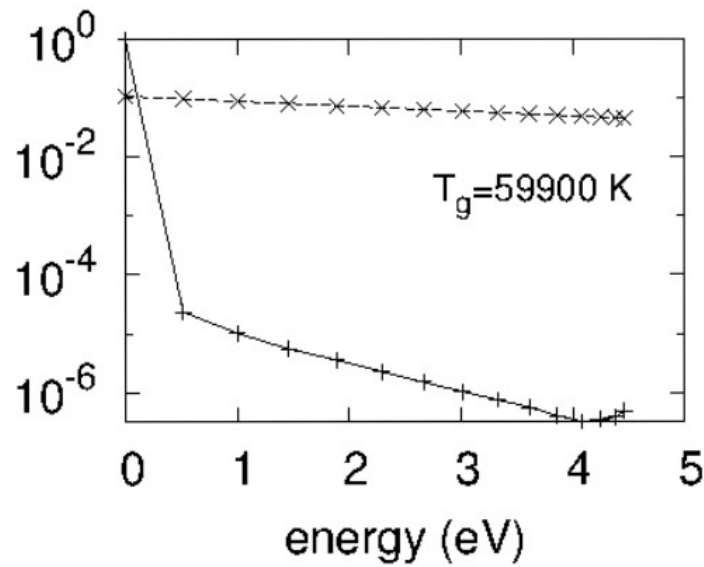




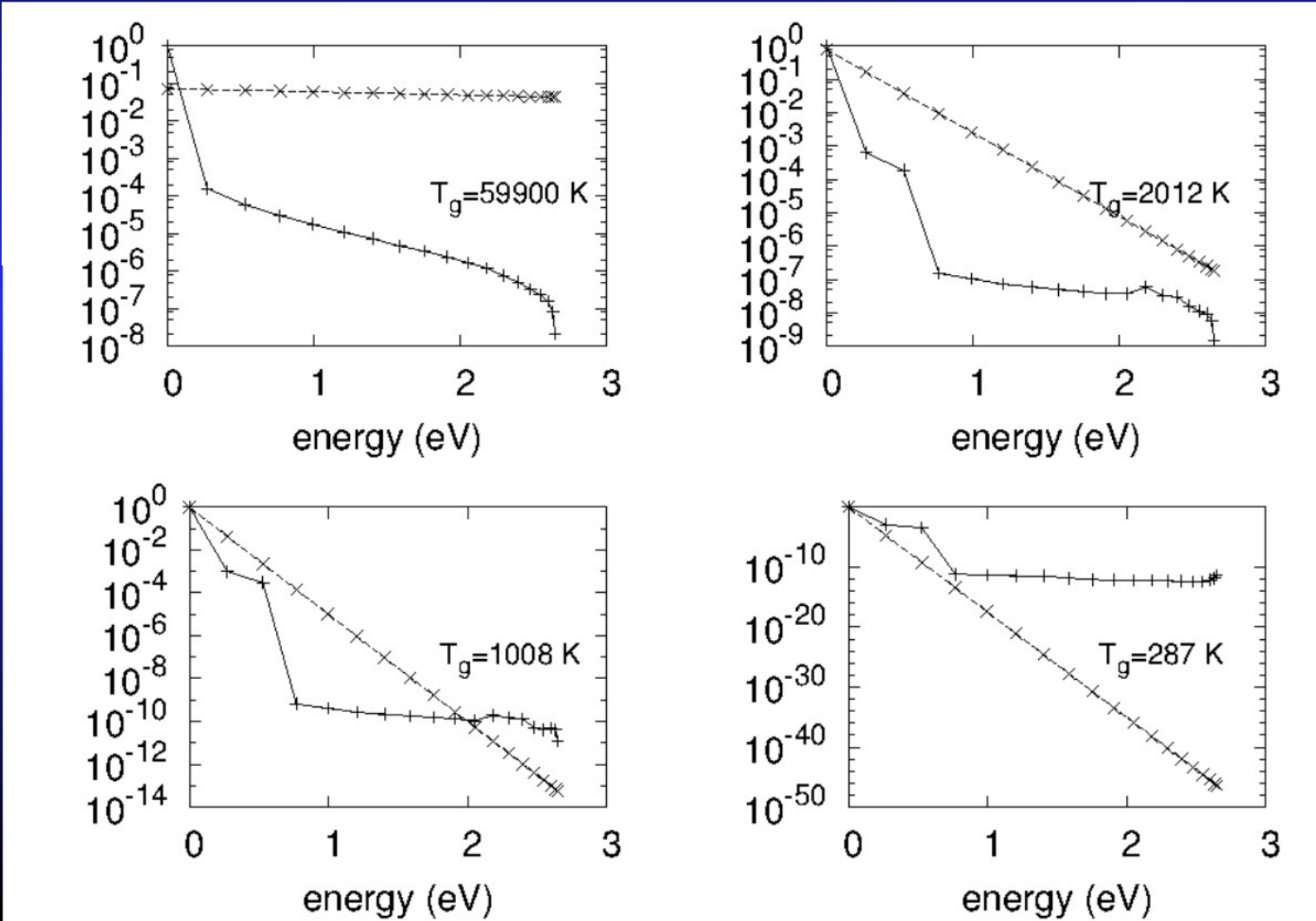
# PREGALACTIC SHOCKS: H<sub>2</sub> DISTRIBUTION FUNCTIONS



# PREGALACTIC SHOCKS: $H_2$ DISTRIBUTION FUNCTIONS



# PREGALACTIC SHOCKS: $H_2^+$ DISTRIBUTION FUNCTIONS



## COMMENTS AND PERSPECTIVES...

- state-to-state chemistry allows to estimate equilibrium/non-equilibrium distributions arising from the net of formation/destruction/"thermalization" processes introduced in the model

↙  
molecular vibration:

non-equilibrium distribution function: high deviations from LTE

- Non-equilibrium effects on photon distribution function → effects on the chemistry
- Effects on physical observables:
  - excitation temperatures
  - rate coefficients
  - heat transfer function
  - distortion photons
- What's going on...
  - state-to-state approach for:**
    - **rotational levels (GS v)**
    - **electronic molecular resolution**
    - **non-equilibrium kinetics HD**
    - **1-zone model**

FOR MORE DETAILS...

***“Vibrational level population of  $H_2$  and  $H_2^+$  in the early Universe”***

Coppola CM, Longo S., Capitelli M., Palla F., Galli D.  
ApJS 2011 193 7

***“Non-equilibrium  $H_2$  formation in the early Universe: energy exchanges,  
rate coefficients and spectral distortions”***

Coppola CM, D'Introno R., Tennyson J., Galli D., Longo S.  
ApJS 2012 198 1

***“Non-thermal  $H_2$  formation in the early Universe”***

Coppola CM, Galli D., Palla F., Longo S., Chluba J.  
MNRAS 2013 **434** (1) 114-122

## COLLABORATORS LIST...

**Savino Longo (Università degli Studi di Bari - Dipartimento di Chimica / CNR-IMIP)**

**Daniele Galli-Francesco Palla (INAF - Osservatorio di Arcetri)**

**Jonathan Tennyson (University College London)**

**Jens Chluba (Johns Hopkins University – Baltimore)**

**Roberto D'Introno – Giovanni Mizzi (Università degli Studi di Bari - Dipartimento di Fisica)**

## ...ONGOING PROJECTS...

**EUROPA: Early Universe: Research on Plasma Astrochemistry  
International Space Science Institute (Bern)**





THANKS...