

Searching for LIV effects with SSTs and ASTRI



SEXTEN CENTER
FOR ASTROPHYSICS
RICCARDO GIACCONI

**From 9 to 40: the SST Telescopes and
Gamma-Ray Science with ASTRI and CTAO
Haus Sexten, 24 July 2026**

Tomislav Terzić

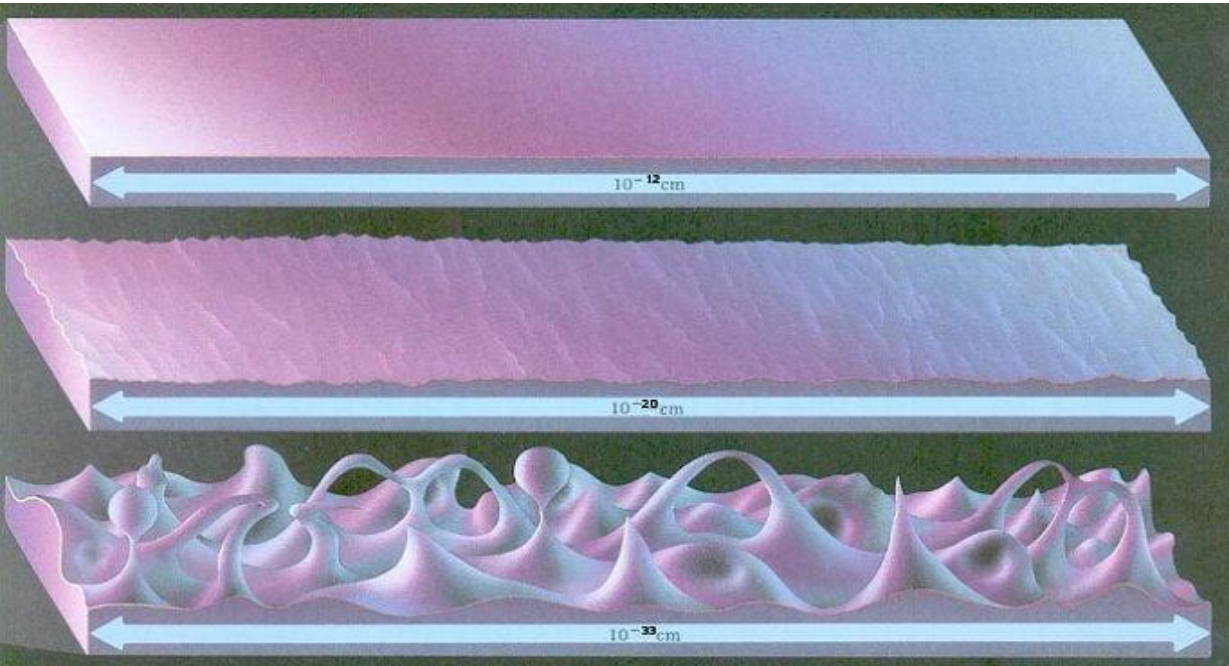
FIZRI Faculty of Physics
University of Rijeka

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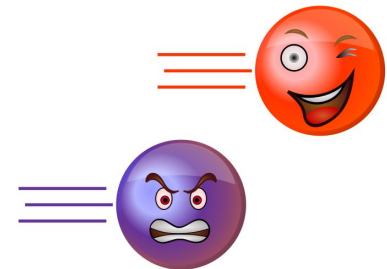
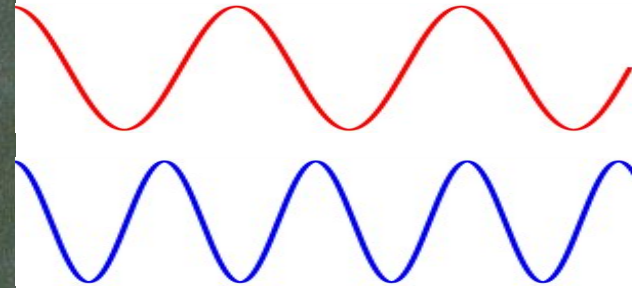
 **HRZZ**
Hrvatska zaklada
za znanost

IP-2022-10-4595

Lorentz invariance violation (LIV)



<http://universe-review.ca/R01-07-quantumfoam.htm>



Lorentz invariance violation (LIV)

- Modified photon dispersion relation
- Usual starting point in searches for effects of QG with gamma rays

$$E^2 = p^2 c^2 \times \left[1 + \sum_{n=1}^{\infty} S_n \left(\frac{E}{E_{\text{QG},n}} \right)^n \right]$$

Expectation:
 $E_{\text{QG},n} = \mathcal{O}(E_{\text{Pl}}) \simeq 1.22 \times 10^{19} \text{ GeV}$

Annotations in the diagram:

- $S = \pm 1$ (points to S_n)
- photon energy (points to E)
- QG energy scale (points to $E_{\text{QG},n}$)

- Not a direct consequence of any particular QG model
- Simple way of parametrizing “out of the ordinary” behaviour

Consequences of MDR

LIV reviews:

- Addazi et al. 2022 (arXiv:[2111.05659](#)) for a comprehensive review of QG models and tests with cosmic messengers
- Terzić et al. 2021 (arXiv:[2109.09072](#)) for a review focused on tests with gamma rays

- Energy dependent photon group velocity
- Modified reaction thresholds & cross sections
 - Breit-Wheeler $\gamma + \gamma_{EBL} \longrightarrow e^+ + e^-$
 - Bethe-Heitler $\gamma + N \longrightarrow e^+ + e^-$
 - Compton scattering $\rightarrow$ see [Abdalla & Böttcher \(2018\)](#); σ_{KN} needs to be derived in LIV framework
 - Synchrotron emission $\rightarrow$ energy range below ASTRI domain
 - Photon decay
 - Spontaneous gamma-ray emission } currently being revisited at theoretical level
 - ...
- Vacuum birefringence $\rightarrow$ requires polarisation measurements
- ...

Tiny but **cumulative** effects!

Energy dependent photon group velocity

$$v_\gamma = \frac{\partial E}{\partial p} \simeq c \left[1 + \sum_{n=1}^{\infty} S_n \frac{n+1}{2} \left(\frac{E}{E_{QG,n}} \right)^n \right]$$

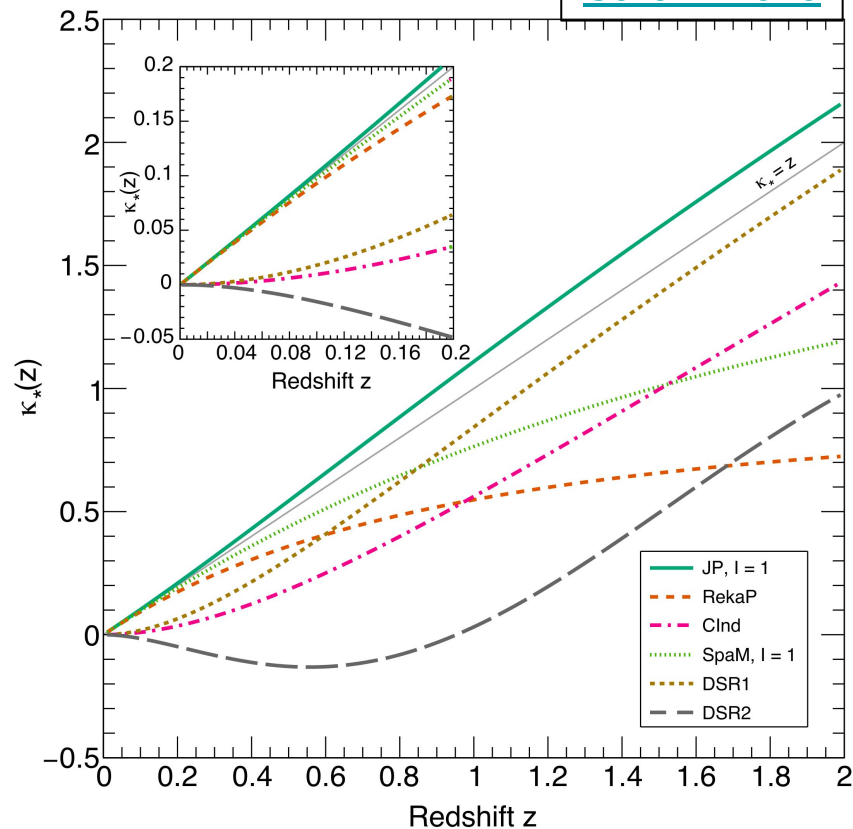
$$\Delta t_n \simeq \pm \frac{n+1}{2} \frac{E_h^n - E_l^n}{H_0 E_{QG}^n} \kappa_n(z)$$

for JP model

$$E_{QG,1} \propto E_{\max} t_{\text{var}}^{-1} z_s^{\sim 1}$$

$$E_{QG,2} \propto E_{\max} t_{\text{var}}^{-1/2} z_s^{\sim 2/3}$$

Caroff+ 2025



SST / ASTRI role

BL Lac flare sources for ASTRI and SSTs ?

Andreas Zech on Wednesday:

Some BL Lac / FR I sources to watch out for **VHE flares at the highest energies** :

Mrk 421 : spectrum during 2010 flare extends beyond 10 TeV, detected by ASTRI-1 and SST-1M

Mrk 501 : spectrum observed up to 20 TeV

M87 : spectrum observed up to 20 TeV

PKS 2155-304 : frequent and spectacular flares, spectrum observed up to ~5 TeV

1ES 1727+502 : VHE flaring detected with LHAASO > 1 TeV in 2024

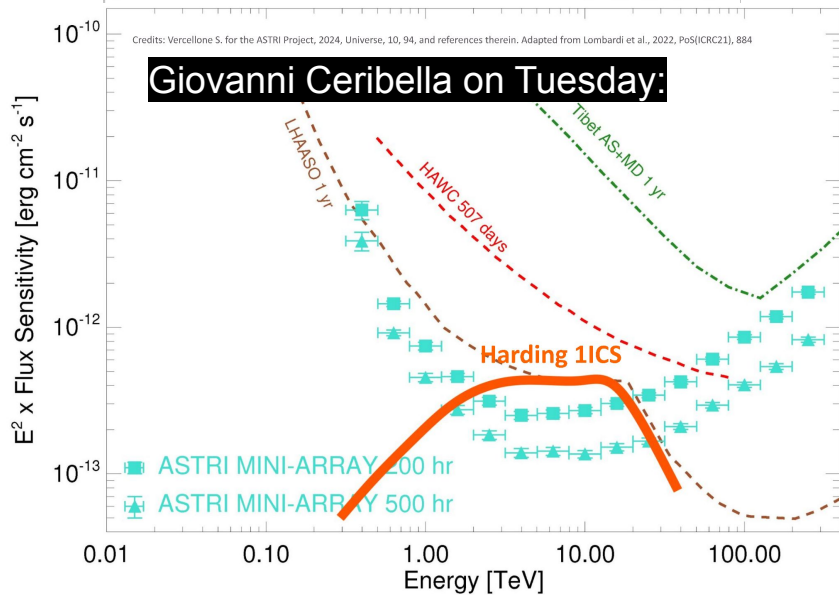
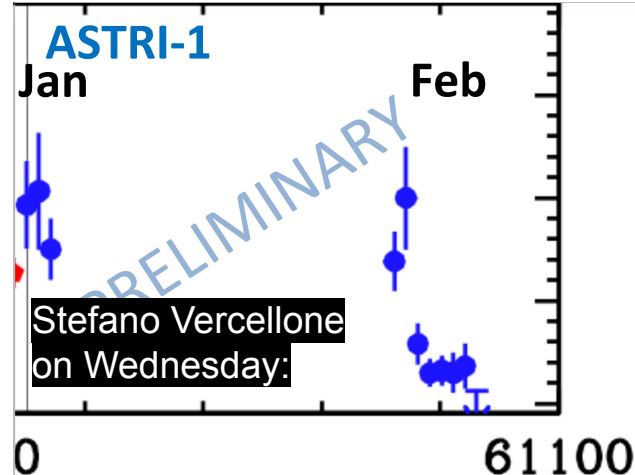
1ES 1426+428 : elevated state detected by VERITAS in 2021, spectrum extends >1 TeV

VER J0521+211 : large flare detected by VERITAS in 2020, spectrum extends >1 TeV

BL Lacertae : bright flare detected by LST-1 in 2022, spectrum extends >1 TeV

$$E_{\text{QG},1} \propto E_{\text{max}} t_{\text{var}}^{-1} z_s^{\sim 1}$$

$$E_{\text{QG},2} \propto E_{\text{max}} t_{\text{var}}^{-1/2} z_s^{\sim 2/3}$$



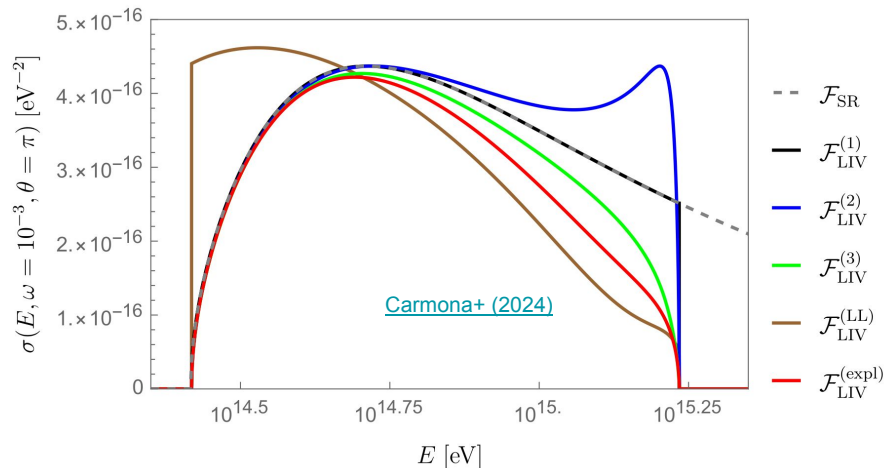
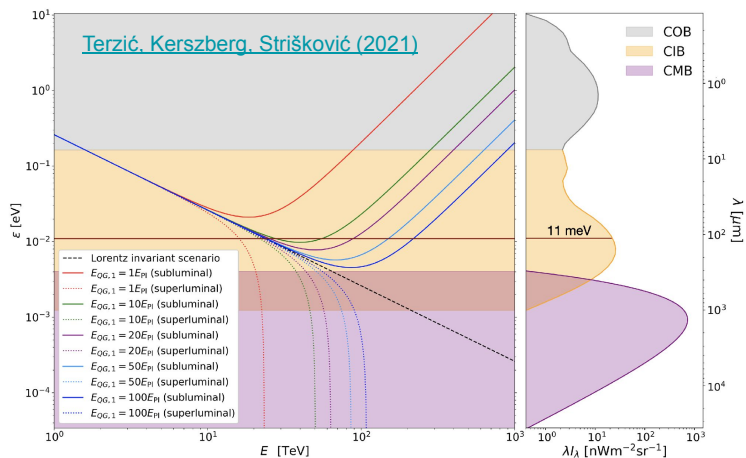
yLIV Working Group

- Present collaboration:
H.E.S.S. – LST – MAGIC – VERITAS
- Energy range: ~ 20 GeV – 100 TeV
- Combining all available data
 - Increases statistics
 - Sources at different distances
 - Redshift dependency on the LIV effect
 - Different (types of) sources
 - Reduces the influence of source intrinsic effects
- Analysis code written and tested
- Currently analysing real data for the paper

[Bolmont+ 2022](#)



LIV-modified gamma-ray absorption

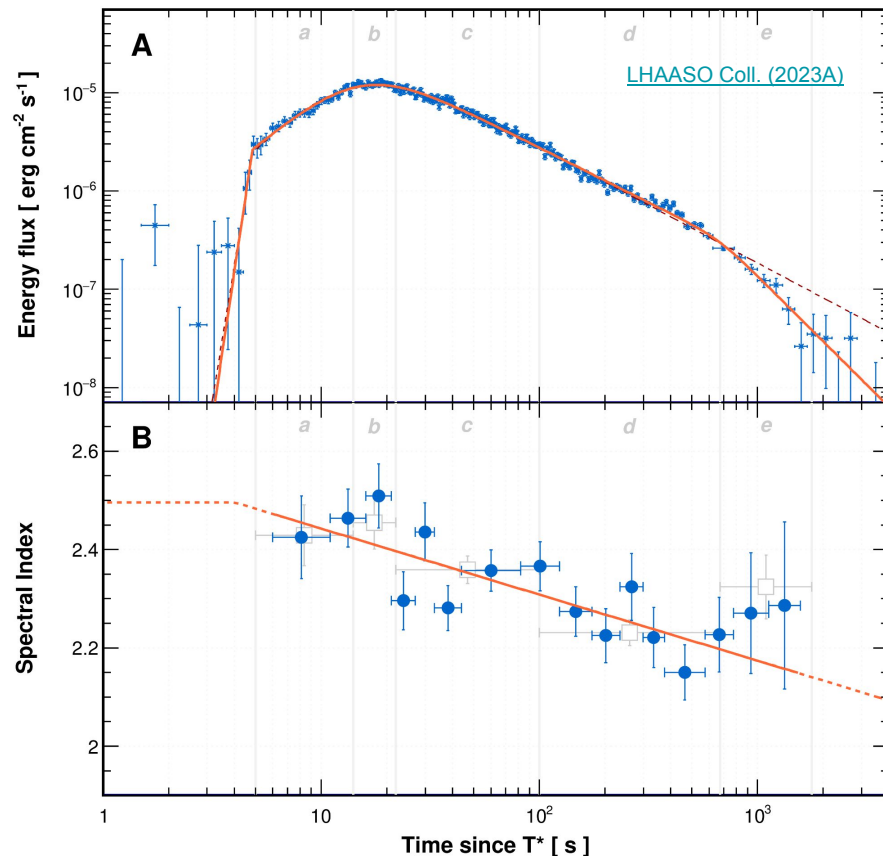


Favourable source characteristics

- Bright source → high γ-ray flux → rich statistics
- Hard spectrum → ample events at the highest energies
- Steady spectrum → lower systematic uncertainties
- Faraway source → accumulated LIV effect
- But not too far → complete γ-ray absorption regardless of LIV

GRB 221009A

- Long GRB observed by LHAASO
([2023A](#), [2023B](#)): $T_0 - T_0 + \sim 6000$ sec
- BOAT (Brightest of all time) ✓
- The LHAASO-WCDA: $> 6.4 \times 10^4$ y-rays in
[200 GeV, 7 TeV] range ✓
- LHAASO-KM2A: y-rays up to ~ 13 TeV ✓
- $\alpha \sim \log(t)$ ✗ (but we've got it covered)
- redshift $z = 0.151$ ✓
- $T_0 + 4536$ s Carpet-2 detected a single
photon-like event of $E = 300$ TeV from BOAT
direction ([Carpet-3 Coll. 2025](#))



Looking for LIV in BOAT

- Maximum measured energy: $E_{\max} = 13$ TeV
- Intrinsic spectrum:
 - reconstructed intrinsic spectrum in the $T_0 + 231 - T_0 + 2000$ s (first 5 reported time bins) and weight-averaged over time (procedure from [Miceli+ 2024](#))
 - scale flux to fit the flux points from the $T_0 + 231 - T_0 + 240$ s (yellow points in the plot)
 - power-law with exponential cutoff to motivate $E_{\max}$

$$\frac{dN_{\text{int}}}{dE} = N_0 \left(\frac{E}{E_0} \right)^{-\alpha} \exp(-E/E_{\text{cut}})$$

$$\alpha = 2.3, E_0 = 1 \text{ TeV}, E_{\text{cut}} = 13 \text{ TeV}$$

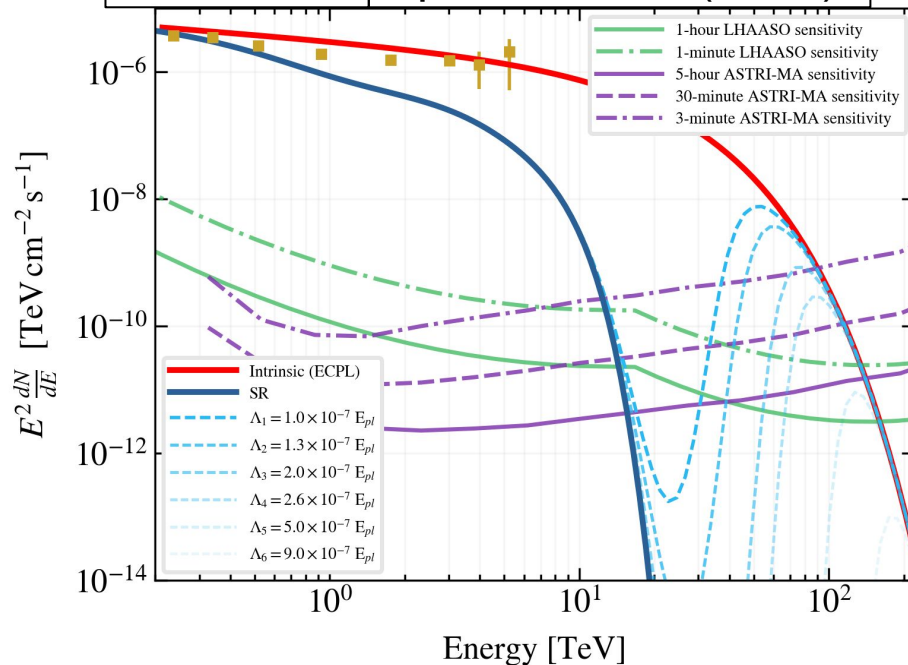
- EBL model: [Saldana-Lopez \(2021\)](#)
- LHAASO sensitivity curves

$$\text{Sens}(T_{\text{obs}}) = \text{Sens}(1\text{y}) \sqrt{1 \text{ year}/T_{\text{obs}}}$$

Adapted from

[Reščič+ \(2026\)](#)

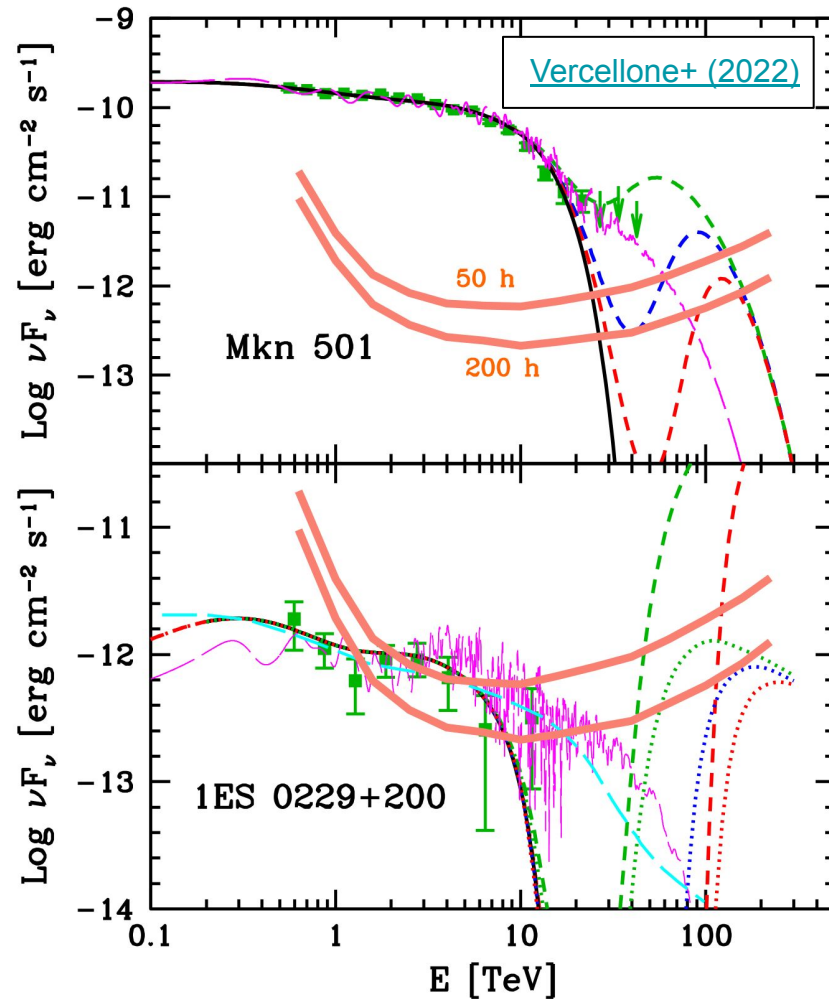
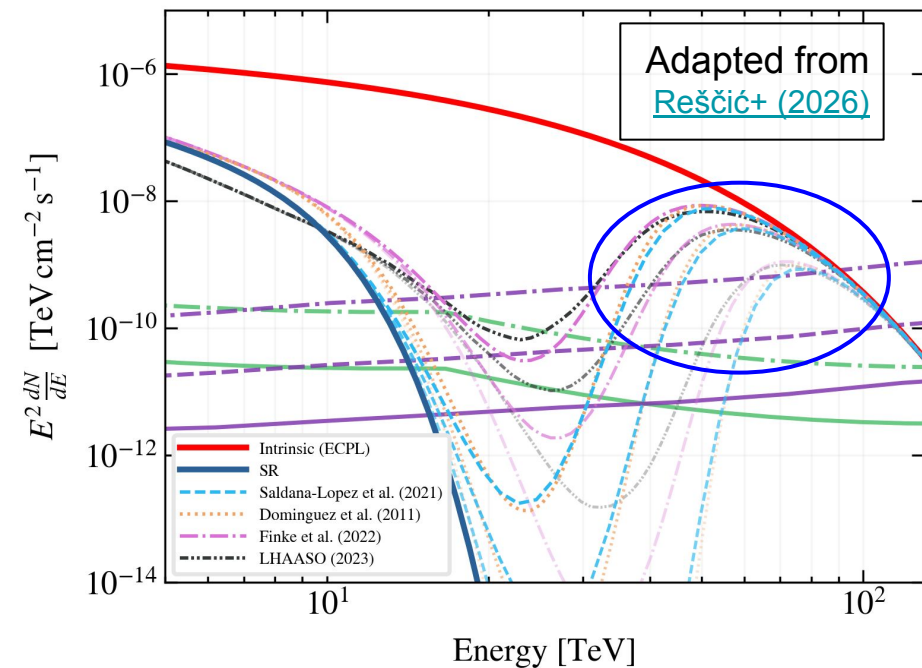
quadratic LIV ($n = 2$)



- ASTRI sens. curves provided by S. Vercellone (Grazie mille!!), update of [S. Lombardi+ \(2022\)](#)
- Caveat: ASTRI sens. curves for $Z_d = 20$ deg, GRB 221009A location from Canarias $Z_d = 30 - 55$ deg

EBL model dependence

- EBL models: [Saldana-Lopez \(2021\)](#), [Finke \(2022\)](#), [Dominguez \(2011\)](#)



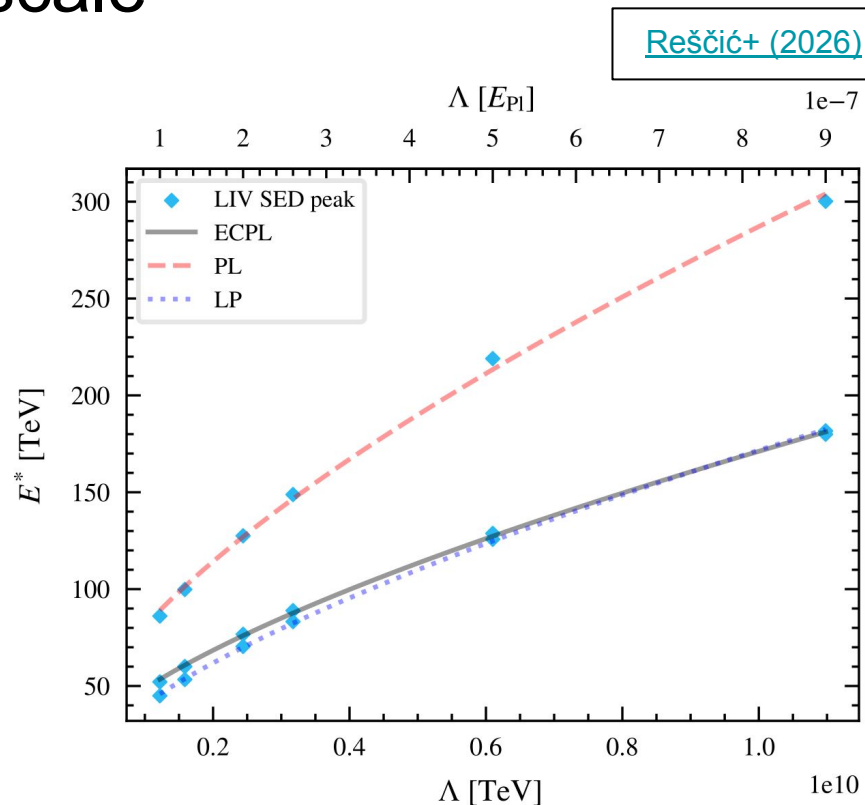
Maximum flux vs LIV energy scale

- LIV energy scale vs. Maximal measured energy

$$E^*(\Lambda) = a\Lambda^{2/3} + b$$

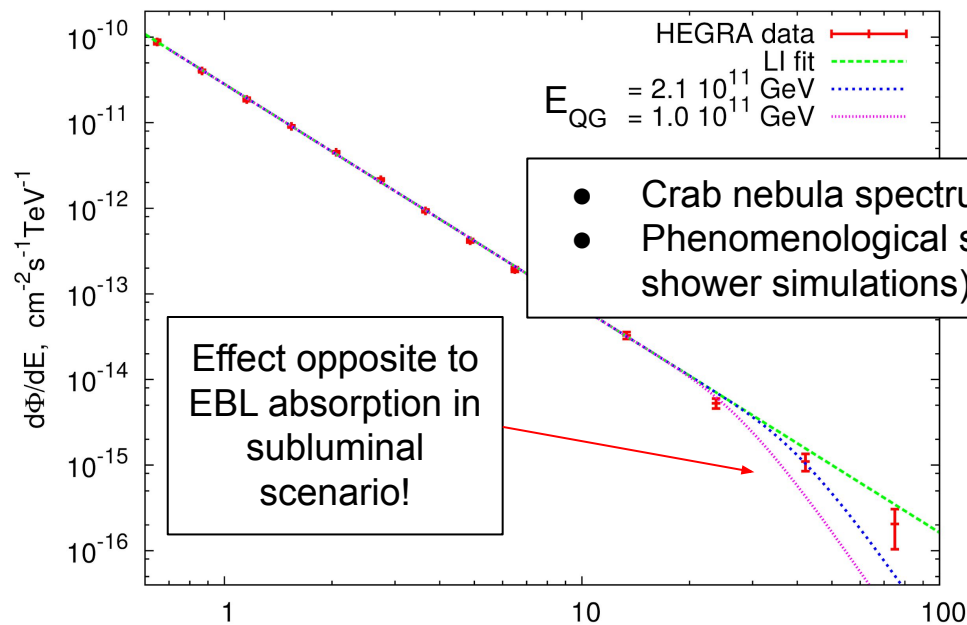
- Relation invariant of the intrinsic spectrum

Spectral model	a	b
ECPL	3.4×10^{-5}	1.5×10^1
PL	5.7×10^{-5}	2.4×10^1
LP	3.6×10^{-5}	4.8



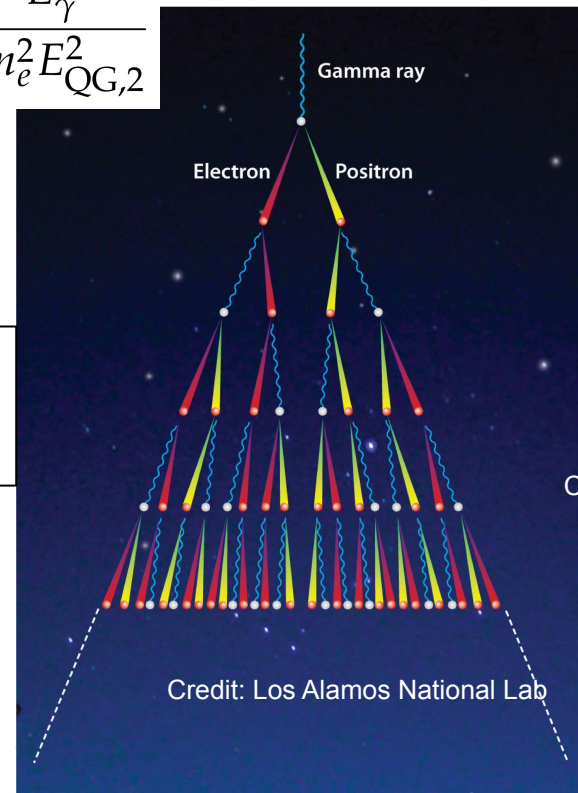
LIV impact on gamma-ray detection

$$\sigma_{\text{BH}} = \frac{28Z^2\alpha^3}{9m_e^2} \left(\log \frac{183}{Z^{1/3}} - \frac{1}{42} \right) \longrightarrow \frac{\sigma_{\text{BH}}^{\text{LIV}}}{\sigma_{\text{BH}}} \simeq \frac{12m_e^2 E_{\text{QG},2}^2}{7E_\gamma^4} \cdot \log \frac{E_\gamma^4}{2m_e^2 E_{\text{QG},2}^2}$$



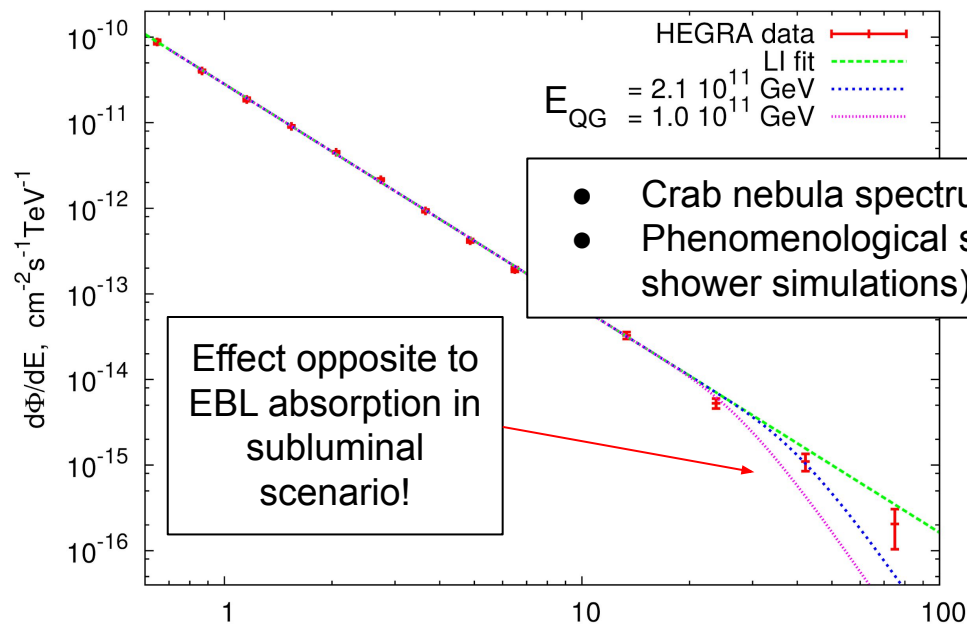
- Crab nebula spectrum ([Rubtsov+ 2017](#))
- Phenomenological study (no LIV-modified shower simulations)

Effect opposite to
EBL absorption in
subluminal
scenario!



LIV impact on gamma-ray detection

$$\sigma_{\text{BH}} = \frac{28Z^2\alpha^3}{9m_e^2} \left(\log \frac{183}{Z^{1/3}} - \frac{1}{42} \right) \longrightarrow \frac{\sigma_{\text{BH}}^{\text{LIV}}}{\sigma_{\text{BH}}} \simeq \frac{12m_e^2 E_{\text{QG},2}^2}{7E_\gamma^4} \cdot \log \frac{E_\gamma^4}{2m_e^2 E_{\text{QG},2}^2}$$



- Crab nebula spectrum ([Rubtsov+ 2017](#))
- Phenomenological study (no LIV-modified shower simulations)

**Shower simulations
with LIV**



BridgeQG



Combining LIV effects

$$\mathcal{L} = i\bar{\psi}\gamma^\mu D_\mu\psi - m\bar{\psi}\psi - \frac{1}{4}F_{\mu\nu}F^{\mu\nu} + i\kappa\bar{\psi}\gamma^i D_i\psi + \frac{ig}{M^2}D_j\bar{\psi}\gamma^i D_i D_j\psi + \frac{\xi}{4M^2}F_{kj}\partial_i^2 F^{kj},$$

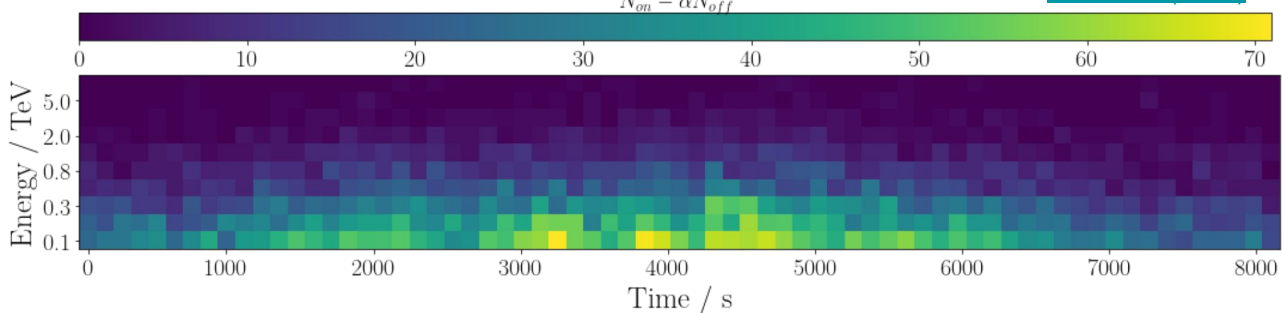
[Rubtsov+ 2012](#)

- n = 1: time delays + modified interactions + vacuum birefringence
- n = 2: time delays + modified interactions (Rubtsov+ case)

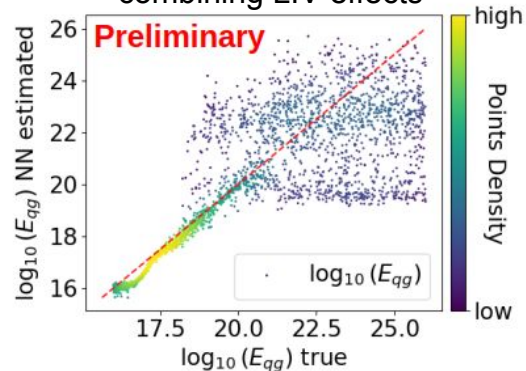
Mrk 421 MAGIC flare 2014

$$N_{on} - \alpha N_{off}$$

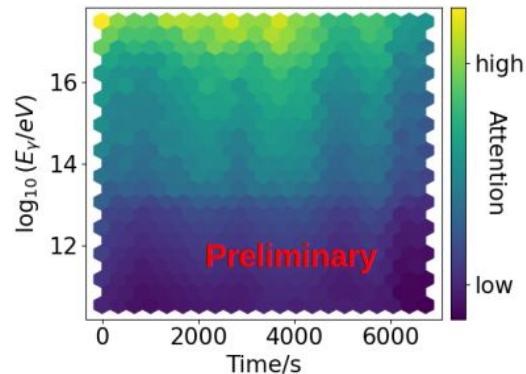
[Strišćković \(2025\)](#)



ANN-VIL – attempt at combining LIV effects



[Terzić & Mrakovčić \(2025\)](#)



Takeaways

- SSTs and ASTRI window towards LIV wide open
- Main advantage: sensitivity to highest energies among Cherenkov telescopes
- Time delays
 - Focus on highly variable sources in the $E > 1$ TeV domain (blazars, pulsars, GRBs?)
- gamma-ray absorption
 - Focus on spectral recovery region (no absorption $\rightarrow$ no EBL-model dependence)
 - Use proper LIV-modified reaction thresholds and cross sections
- EM atmospheric showers development $\rightarrow$ the higher the energy, the better
- Testing coexisting LIV effects on individual samples



Backup

ToF systematics

[Bolmont+ 2022](#)

Table A1. Summary of systematic uncertainties for all sources and combinations simulated for the J&P case.

Source	Correction order	Template statistics (s.TeV ⁻ⁿ)	Energy scale (s.TeV ⁻ⁿ)	Background normalization (s.TeV ⁻ⁿ)	Uncertainty on power law index (s.TeV ⁻ⁿ)	Distance/redshift uncertainty (s.TeV ⁻ⁿ)	Reconstruction uncertainty (s.TeV ⁻ⁿ)	All syst. combined (s.TeV ⁻ⁿ)
GRB 190114C	$n = 1$	17.8	6.9	8.0	9.4	< 7.7	3.0	25.6
	$n = 2$	9.4	12.4	1.7	15.4	< 9	4.2	24.1
PKS 2155-304	$n = 1$	101	11.7	< 20	< 22	17.8	< 3.3	107
	$n = 2$	21.8	19.3	0.7	8.1	12.0	< 2.2	37.4
Mrk 501	$n = 1$	155	56	< 51	49	1.	< 8.5	197
	$n = 2$	11.2	18.3	< 10.3	9.3	0.19	< 1.6	28.8
PG1553+113	$n = 1$	631	150	324	< 361	112	< 64	727
	$n = 2$	916	638	537	< 552	338	< 112	1282
Crab V	$n = 1$	897	137	< 73	142	145	< 25	1135
	$n = 2$	1141	410	< 264	694	265	< 174	1820
Crab M	$n = 1$	371	66	7	23	74	< 11	416
	$n = 2$	167	64.5	61	24	48	< 72	190
Vela	$n = 1$	1.36×10^4	1.03×10^4	0.46×10^4	$< 1.3 \times 10^4$	1.30×10^3	$< 5.87 \times 10^3$	2.28×10^4
	$n = 2$	1.0×10^5	2.05×10^5	0.48×10^5	$< 1.5 \times 10^5$	1.57×10^5	$< 0.95 \times 10^5$	3.05×10^5
Crab (M+V)	$n = 1$	357	49	< 56	32	61	< 32	398
	$n = 2$	161	59	45	59	38	< 83	197
PSR	$n = 1$	355	52	< 58	38	58	< 11	394
	$n = 2$	90	71	49	24	62	< 55	138
AGN	$n = 1$	89.5	12	< 15	3.7	15.8	< 2.9	94.9
	$n = 2$	10.1	11.1	< 6	6.2	3.4	< 1.3	19.7
AGN+PSR	$n = 1$	85	11	< 18	5	15	< 2.9	91
	$n = 2$	9.6	10.9	< 8	5.9	4.5	< 1.1	17.8
GRB+AGN	$n = 1$	17.8	5.8	6.8	8.3	1.4	3.3	24.5
	$n = 2$	6.8	7.8	< 6.6	9.0	1.7	1.4	16.2
GRB+PSR	$n = 1$	17.5	6.7	7.9	9.1	1.0	3.2	24.9
	$n = 2$	8.1	11.3	1.6	12.7	2.8	< 1.1	19.4
All	$n = 1$	18.0	5.8	6.7	8.2	1.5	4.1	24.8
	$n = 2$	7.5	7.7	< 6.2	8.2	2.4	4.8	16.4

VHE gamma-ray absorption

- Low-energy photon background (CMB, EBL, radio, ...)

- Breit & Wheeler (1934):

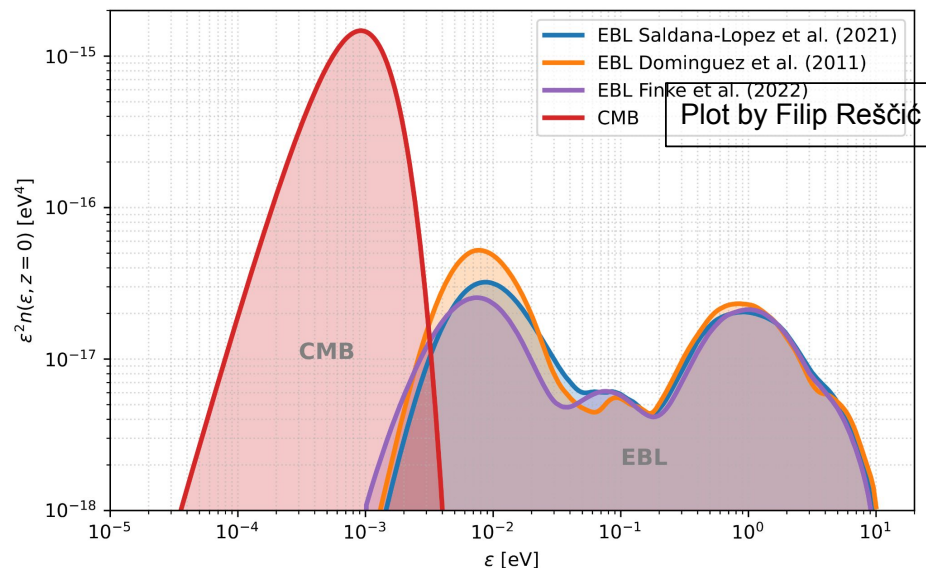
$$\gamma + \gamma_{EBL} \longrightarrow e^+ + e^-$$

- gamma-ray energy determines the dominant target photon field [De Angelis, 2013]:

- $0.1 \text{ TeV} \leq E \leq 100 \text{ TeV} \rightarrow \text{EBL}$
- $100 \text{ TeV} \leq E \leq 10^7 \text{ TeV} \rightarrow \text{CMB}$

- Most recent state-of-the-art EBL models:

- [Saldana-Lopez et al. \(2021\)](#)
- [Finke et al. \(2022\)](#)



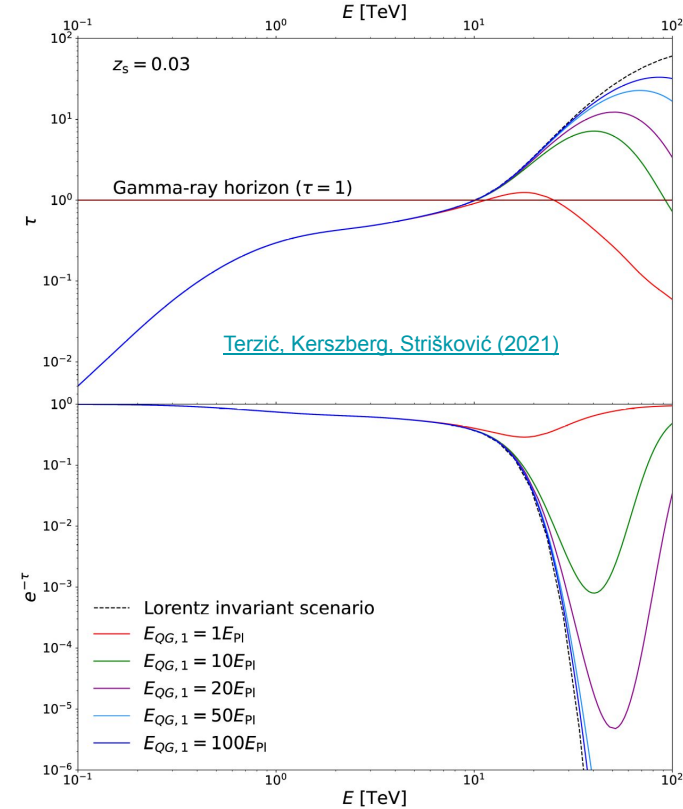
Methodology

1. Intrinsic spectrum: extrapolate reconstructed intrinsic state into the 100 TeV energy range
2. Investigate gamma-ray absorption assuming subluminal quadratic LIV at different LIV energy scales Λ

$$\frac{dN_{\text{obs}}}{dE} = \frac{dN_{\text{int}}}{dE} \times e^{-\tau(E, z_s; \Lambda)}$$

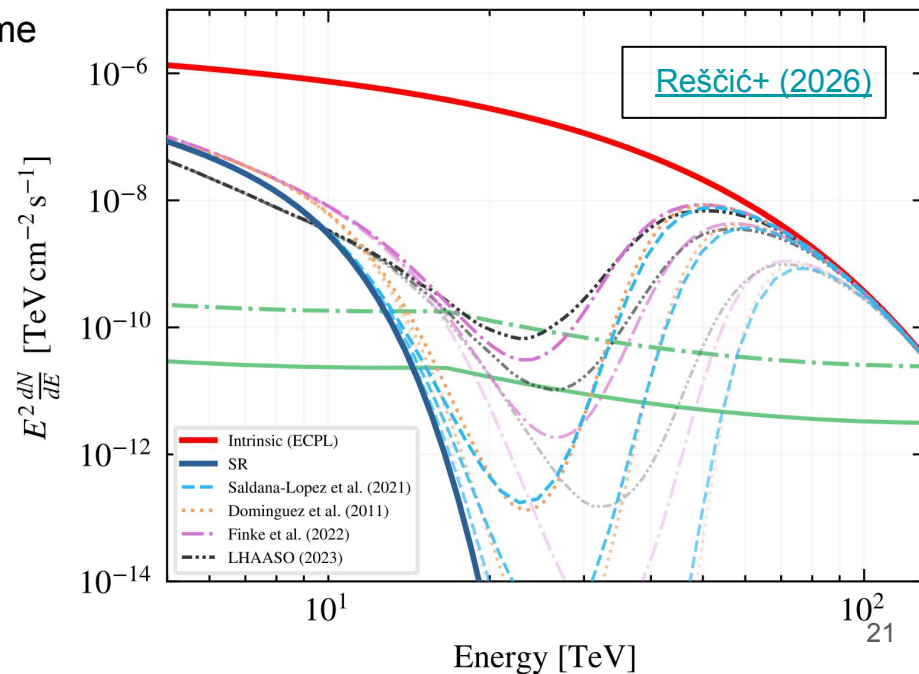
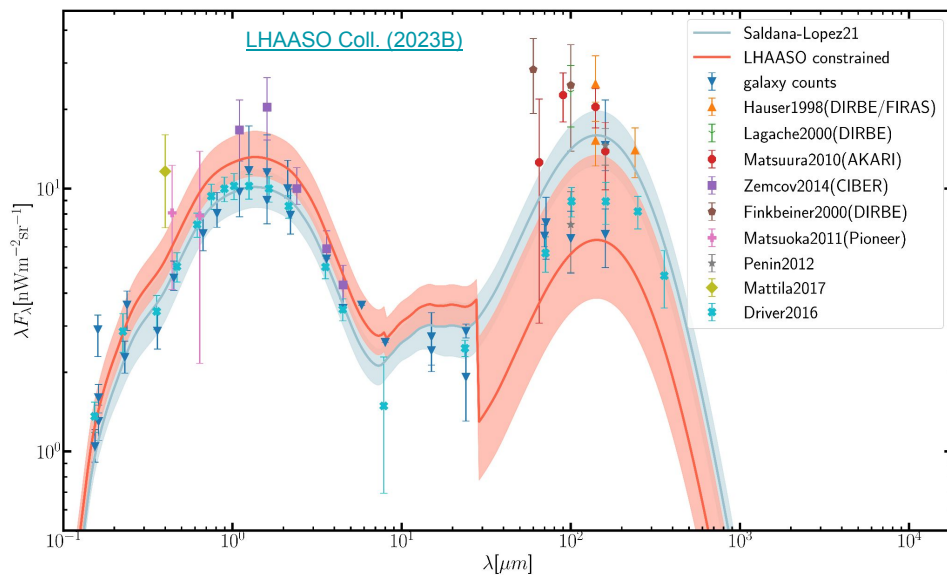
$$\tau(E, z_s; \Lambda) = \int_0^{z_s} dz \frac{dl}{dz} \int_{-1}^1 d\cos\theta \left(\frac{1 - \cos\theta}{2} \right) \times \int_{\epsilon_{\text{thr}}(E, \theta, z; \Lambda)}^{\infty} d\epsilon n(\epsilon, z) \sigma(E(1+z), \epsilon, \theta; \Lambda).$$

3. Identify energy intervals in which LIV-enabled flux recovery could be detected

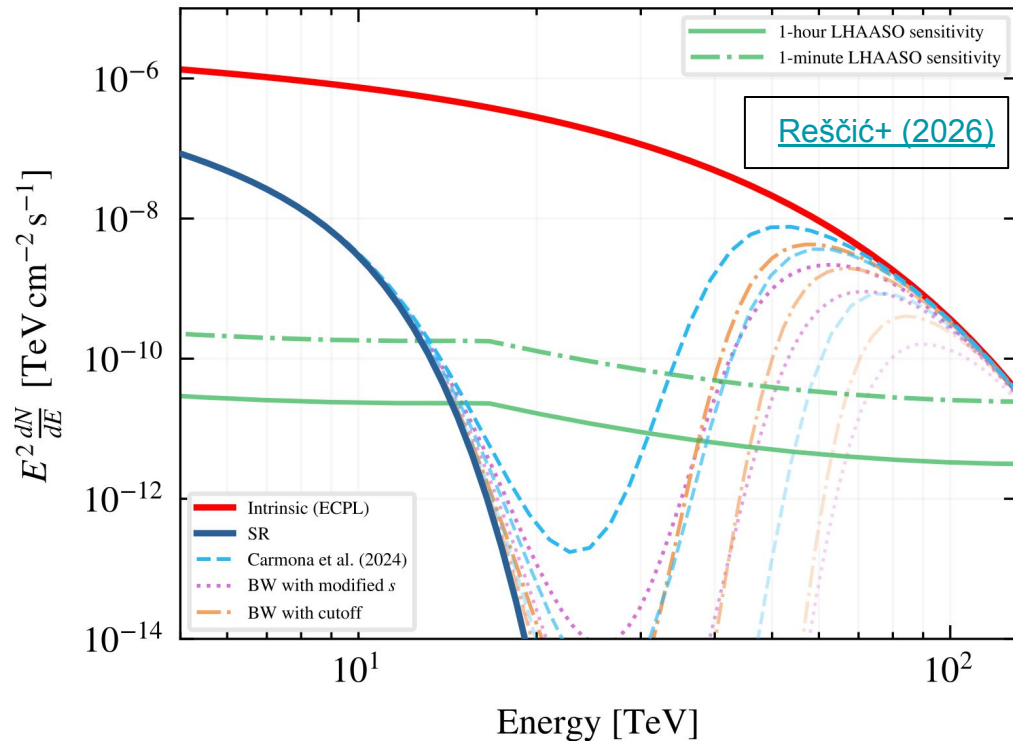
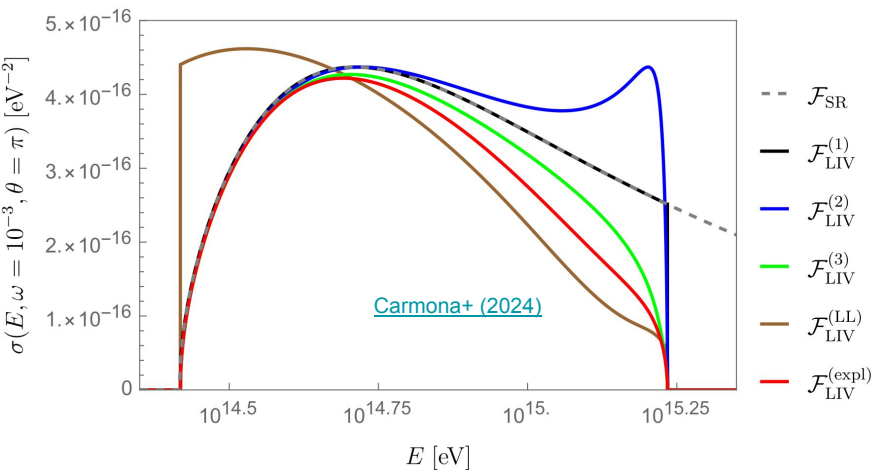


LHAASO scaled EBL

- LHAASO: EBL scaled based on GRB 221009A observations assuming standard physics
 - EBL intensity: 40% Saldana-Lopez (2021) → lower y-ray absorption – same effect as LIV
 - LIV-recovered spectral peaks remain ~ same



LIV-modified cross section influence



- $\square_{\text{LIV}}^{(\text{expl})} \rightarrow \text{Carmona et al. (2024)}$
- $\square_{\text{LIV}}^{(2)} \rightarrow \text{BW with modified } s$
- $\square_{\text{LIV}}^{(1)} \rightarrow \text{BW with cutoff}$