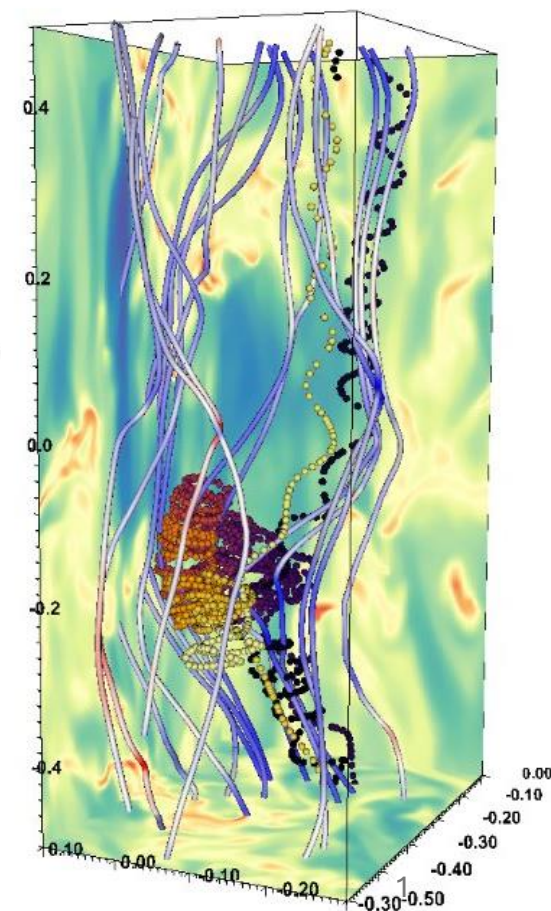
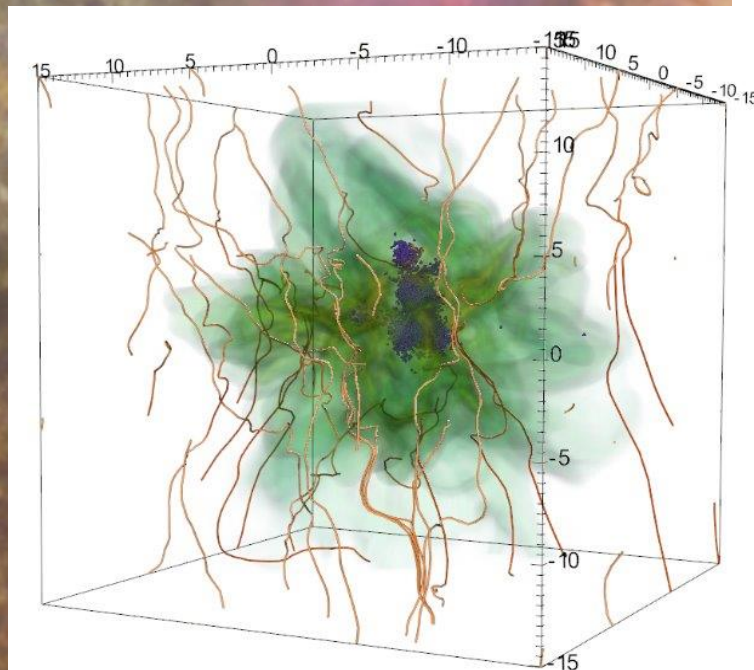


# Probing CR Diffusion Regimes and $\gamma$ -ray emission in Young Massive Stellar Clusters with 3D MHD Simulations

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Universidade de São Paulo

Elisabete de Gouveia Dal Pino, Gaetano di Marco,  
Rafael Alves Batista, Stela Adduci Faria



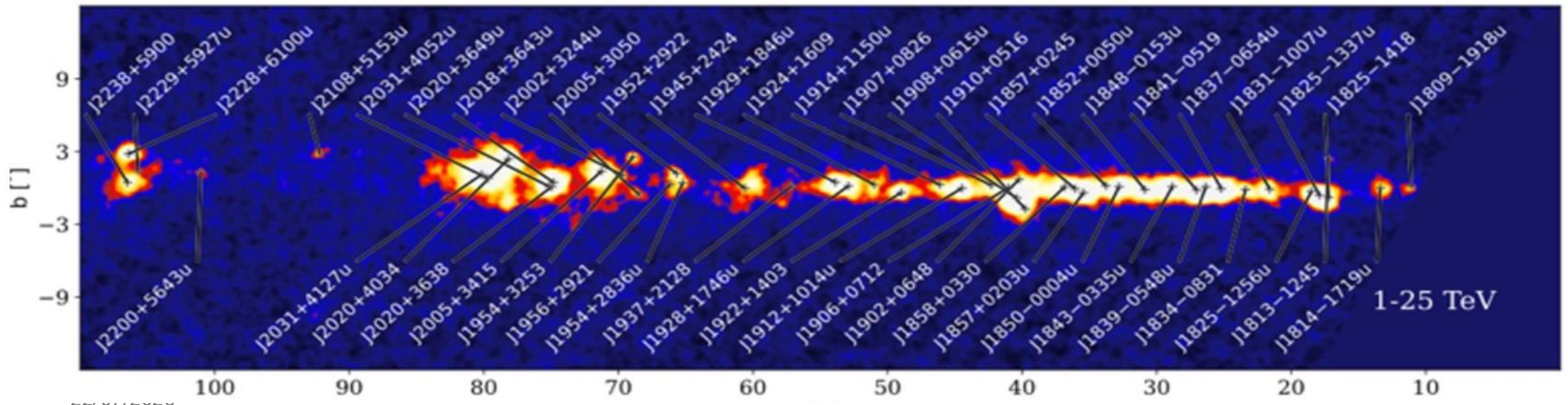
# Turbulence and very high energy (VHE) Cosmic Rays

- Barreto-Mota; de Gouveia Dal Pino; Burkhart; Melioli; Santos-Lima; Kadowaki (2021)
- Barreto-Mota; de Gouveia Dal Pino; Xu; Lazarian (ApJ, 2025)
- Barreto-Mota; de Gouveia Dal Pino; Di Marco; Alves-Batista; Adduci Faria (in prep)



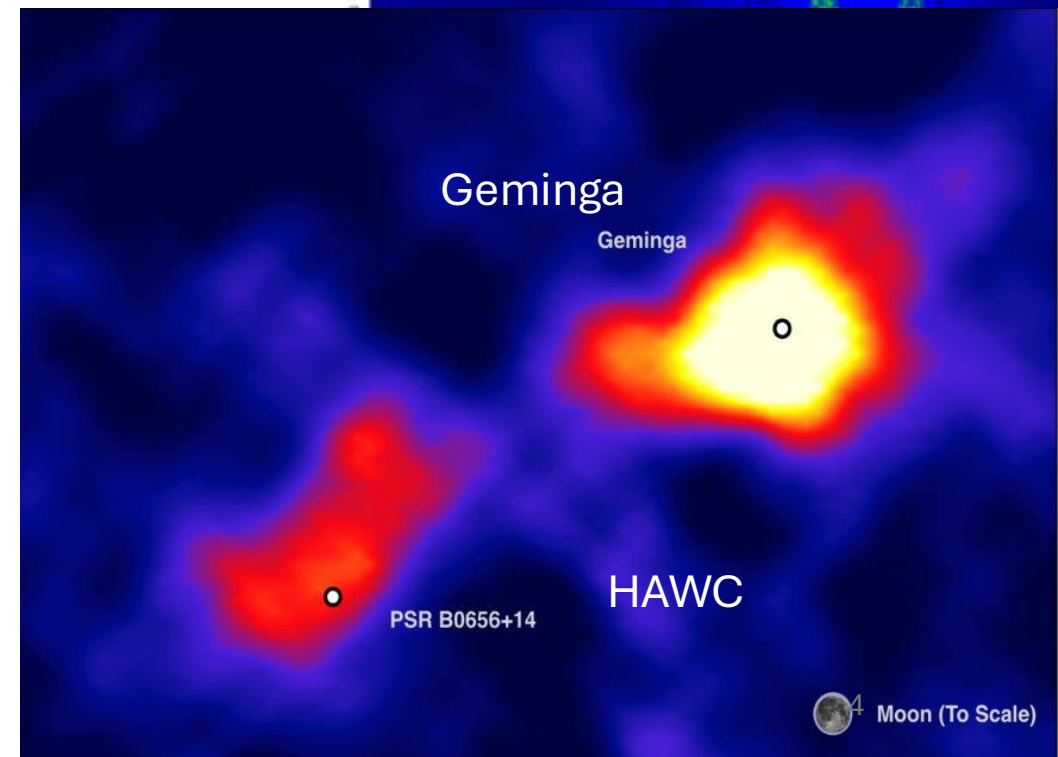
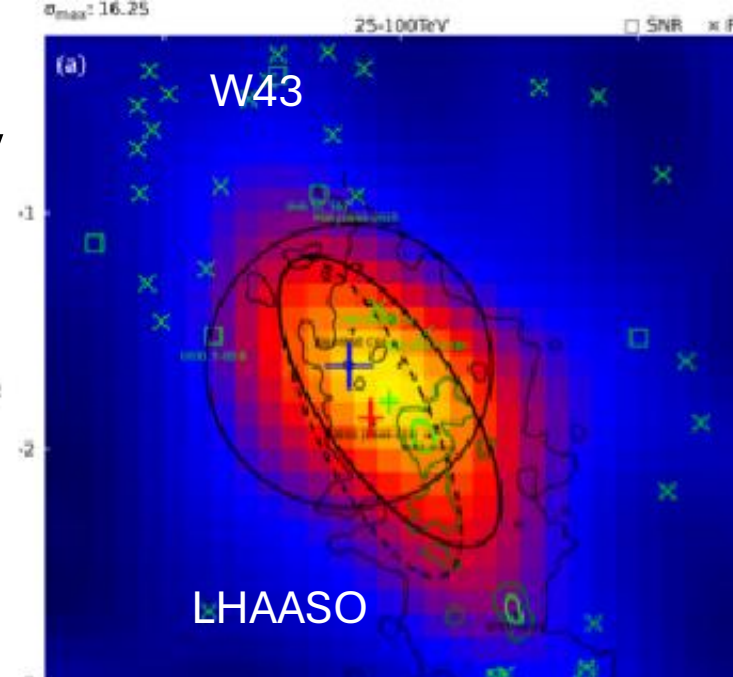
# High energy emission in our Galaxy

- LHAASO observations:
  - SNRs, galactic center, pulsar wind nebulae, young stellar clusters, microquasars?



# High energy emission in our Galaxy

- **VHE observations of extended sources**
  - Up to  $\sim 100$  TeV photons  
(Abeysekara et al. 2017; Huang et al. 2018;  
Abeysekara et al. 2021; Cao et al. 2021;  
LHAASO Coll. 2025)
  - PeVatrons?
- **Observations suggest suppressed diffusion, by as much as two orders of magnitude compared to the ISM at 100 TeV**  
 **$\sim 10^{28} \text{ cm}^2/\text{s}$  or less**
- Usual approach of **quasi-linear theory (QLT)** **cannot explain** (Shalchi, 2009)



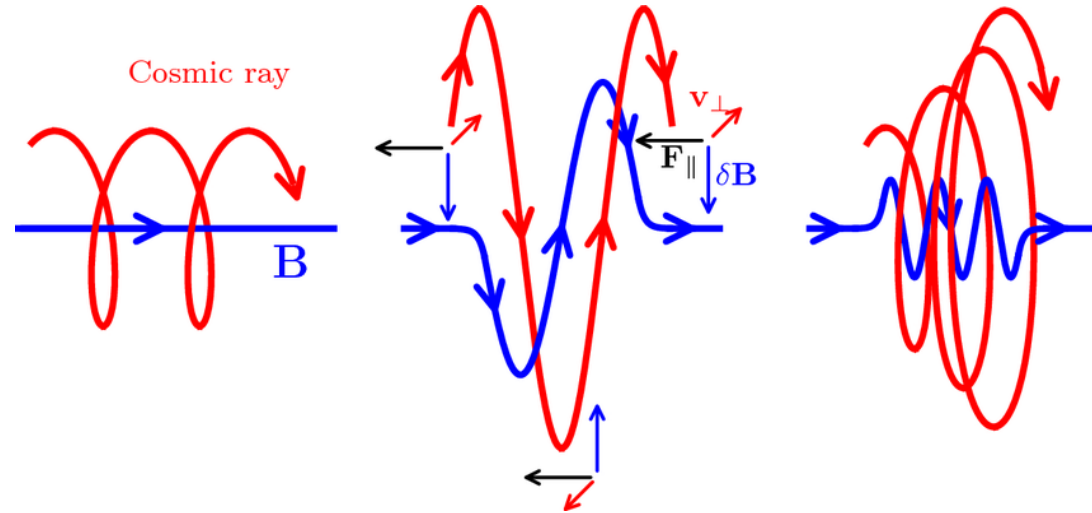


# CR scattering and Quasilinear Theory (QLT)

Ruszkowski & Pfrommer (2023)

- **Resonant pitch angle scattering**

$$k_{\text{res}} 2\pi R_L \simeq \frac{(1 - \cos^2 \theta_{\text{res}})^{0.5}}{\cos \theta_{\text{res}}}$$



- **QLT**

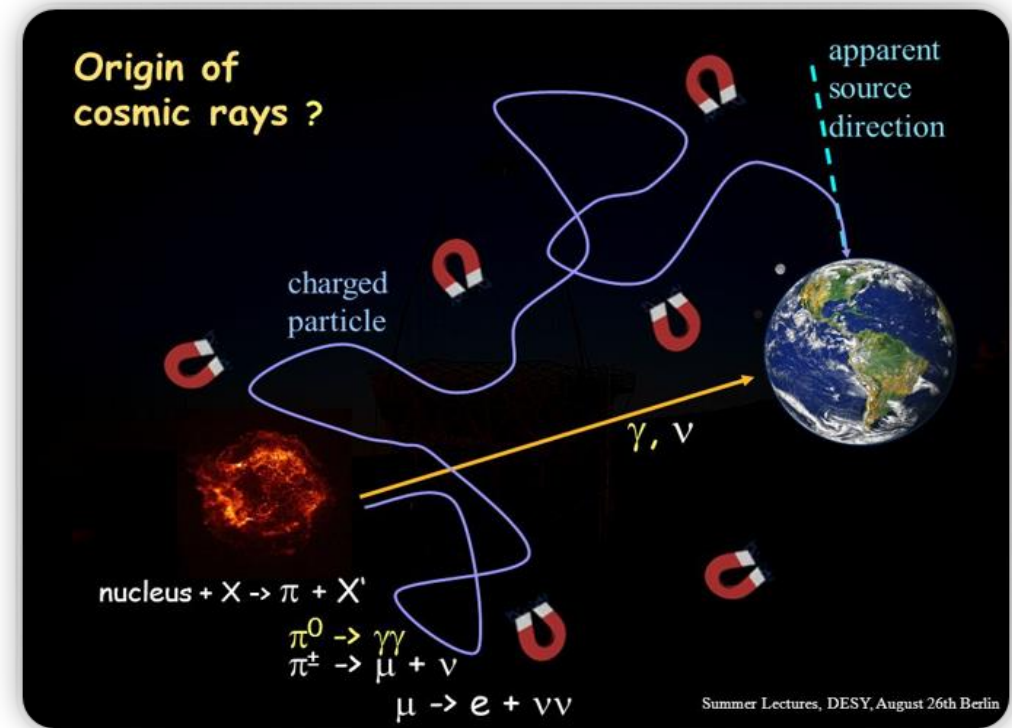
- is comparable to a 1st order perturbation (Jokipii, 1966; Schilikeiser, 2002)
- 90° degree problem (particles cannot change direction)
- Perpendicular diffusion and geometry problem
  - Predictions do not match simulations

Shalchi (2009)

| Geometry        | QLT                                                         | Simulations                                                    |
|-----------------|-------------------------------------------------------------|----------------------------------------------------------------|
| Slab model      | $\langle (\Delta x)^2 \rangle \sim t$<br>(Diffusion)        | $\langle (\Delta x)^2 \rangle \sim \sqrt{t}$<br>(Subdiffusion) |
| Composite model | $\langle (\Delta x)^2 \rangle \sim t^2$<br>(Superdiffusion) | $\langle (\Delta x)^2 \rangle \sim t$<br>(Diffusion)           |

# Cosmic Ray diffusion

- How to explain the slower diffusion?
- **MHD Turbulence is ubiquitous:**
  - External Sources of MHD Turbulence
  - Anisotropic Diffusion
  - Relativistic Diffusion
  - Self-generated
  - Fang (2022)
- Several authors consider phenomenological approach: **HD turbulence (Kolmogorov)**
  - Does not take into account effects due to **MHD turbulence** in the system (Goldreich-Stridhar 95)
- **Mirror Diffusion**  
(Lazarian & Xu 2021; Barreto-Mota et al. 2025; Bell et al. 2025)
  - **Unavoidable in MHD turbulence!**



$$\lambda_{\parallel} \sim \frac{v_A}{\varepsilon^{1/3}} \lambda_{\perp}^{2/3}$$

# Magnetic Mirrors

- **Mirrors naturally occur in MHD flows**

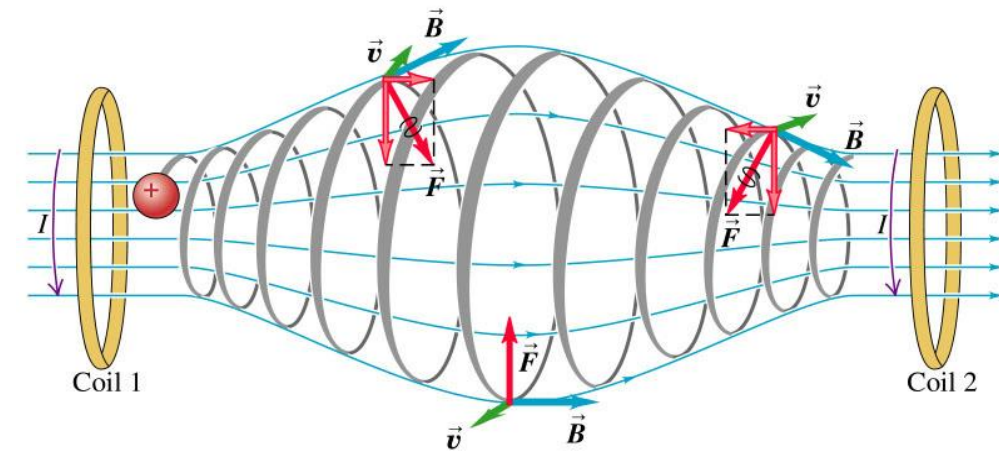
(e.g. Budker 1959; Noerdlinger 1968; Kulsrud & Pearce 1969)

- If  $R_L$  is smaller than the scale of  $B_{\text{mirror}}$  in MHD turbulence:  
(1<sup>st</sup> Adiabatic Invariant)

$$\frac{p_{\perp}^2}{B_0} = \frac{p^2}{B_0 + \delta b}$$

- In turbulence, particles with  $\mu < \mu_{lc}$  (**loss cone for escaping particles**)  
**are subject to mirroring** (Lazarian and Xu 2021):

$$\mu = \cos(\theta)$$
$$\mu_{lc}^2 = \cos^2 \theta_{lc} = \frac{\delta b}{B_0 + \delta b},$$



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# Superdiffusion of Magnetic Fields

- Dispersion of the magnetic field lines:

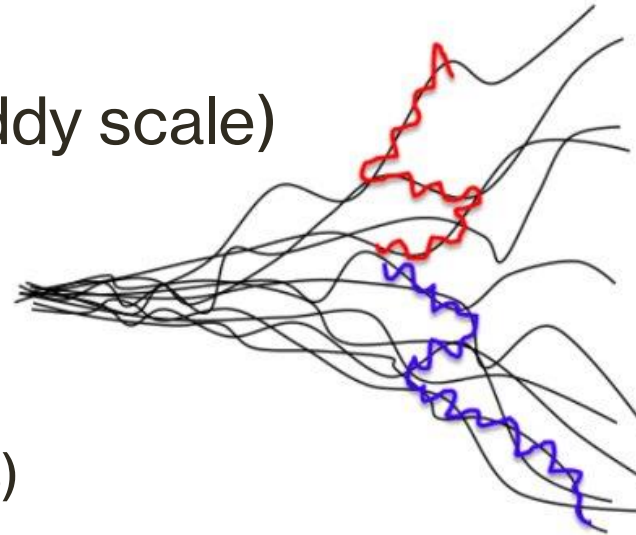
$$d\langle y^2 \rangle \approx l_{\perp}^2 \frac{ds}{l_{\parallel}},$$

$$d\langle y^2 \rangle \approx \langle y^2 \rangle^{2/3} M_A^{4/3} L^{-1/3} ds.$$

Lazarian and Xu, ApJ (2021)

Eyink et al.,  
Nature 497,(2013)

- (Lazarian & Vishniac 1999: // and  $\perp$  eddy scale)
- Extensively studied:
  - Lazarian & Yan (2014), Maiti et al. (2022), Hu et al. (2022), and Zhang and Xu (2023)



**Figure 1.** Because of the perpendicular superdiffusion of particles following diffusing magnetic field lines, particles that undergo bouncing move diffusively along the magnetic field. Thin lines represent magnetic field lines. Thick lines represent the trajectories of two particles whose initial separation is small.



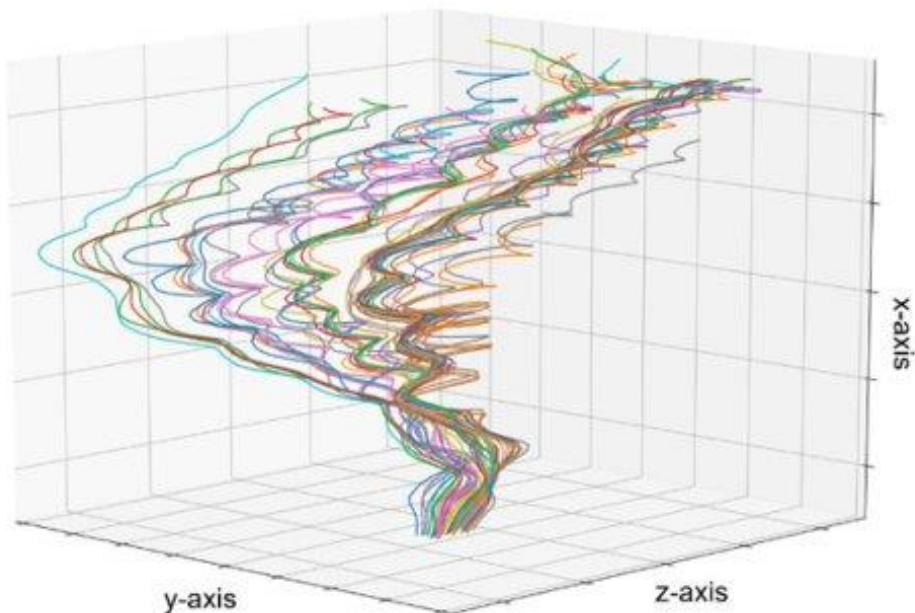


# Superdiffusion+Mirrors = Mirror Diffusion

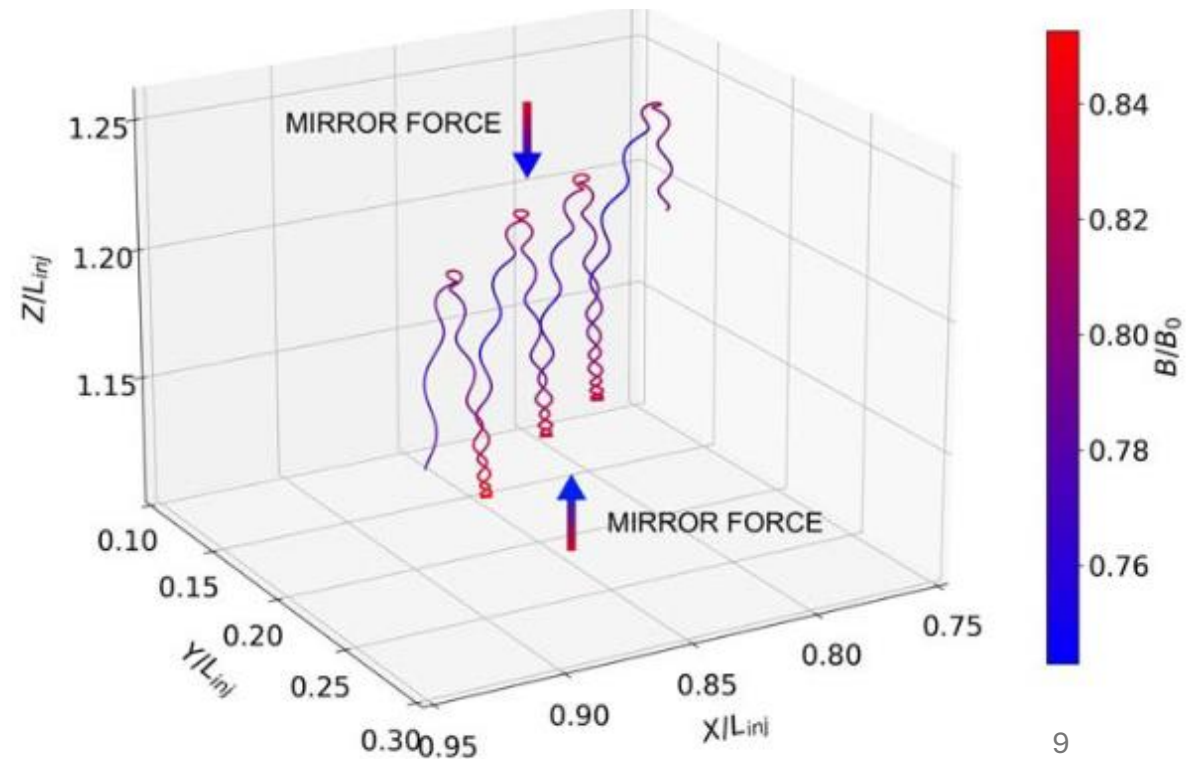
- Lazarian & Xu (2021)
- The only ingredients needed are superdiffusion and turbulence

It solves QLT problems!

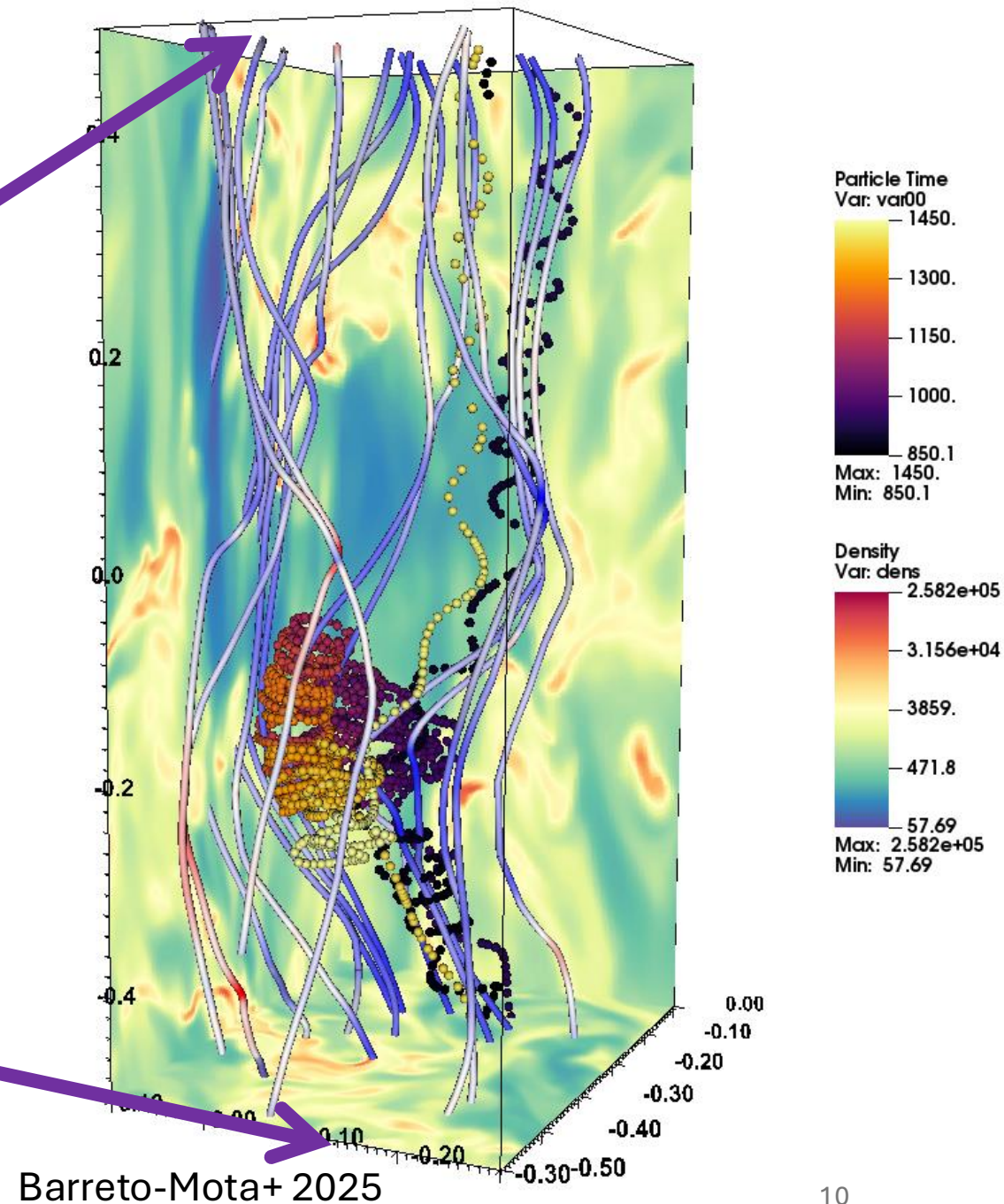
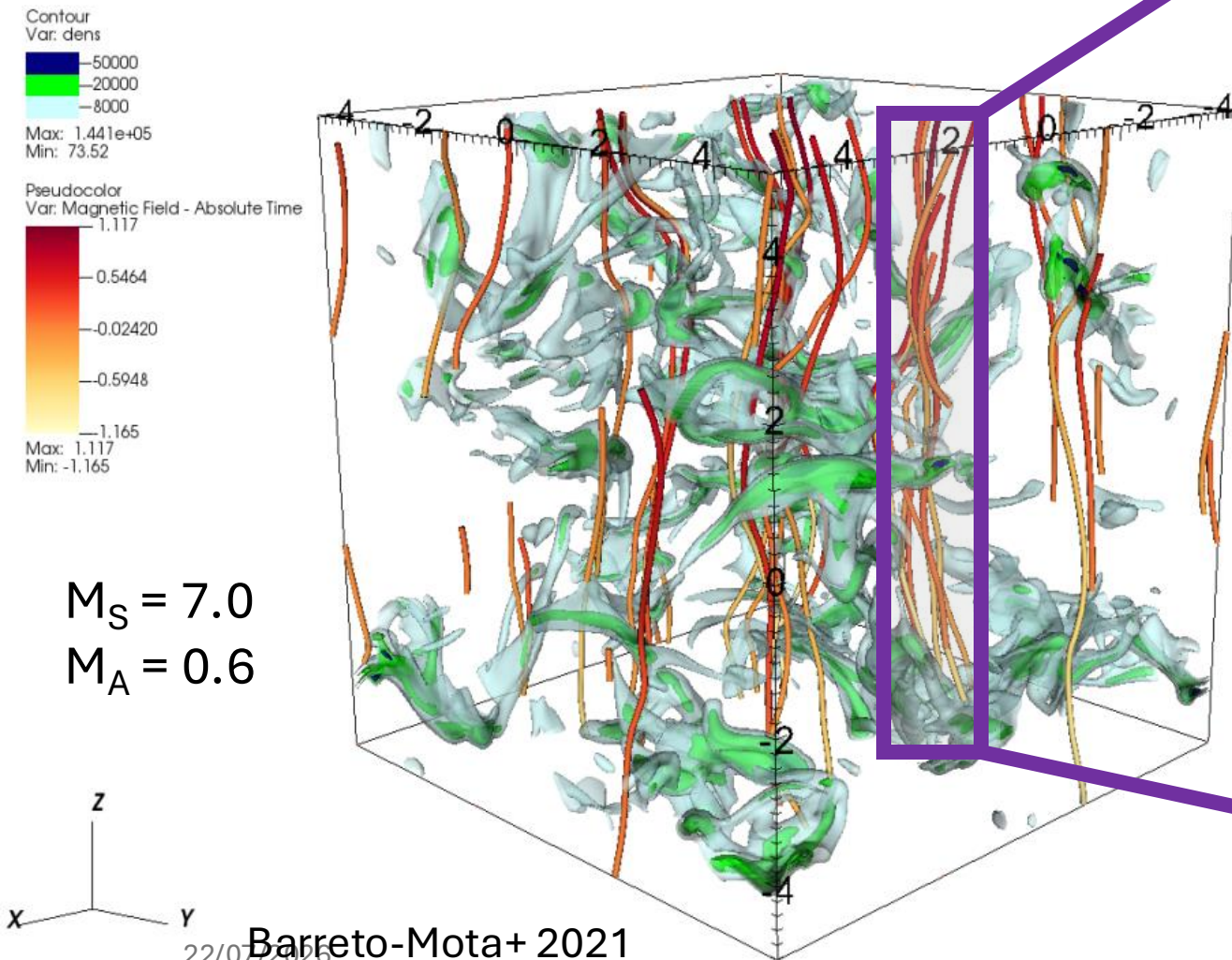
Hu et al. (2022)



Zhang & Xu (2023)



# 3D MHD turbulence simulations with test particles diffusion





# Test particle simulations

## Mirror x Scattering

- Barreto-Mota+ 2025
- We compute the Lorentz force in each point:

$$\frac{d\mathbf{v}}{dt} = \frac{q}{\gamma mc} \mathbf{v} \times \mathbf{B}$$

- **Complete field**

- Mirror + Scattering

- **Smoothed field**

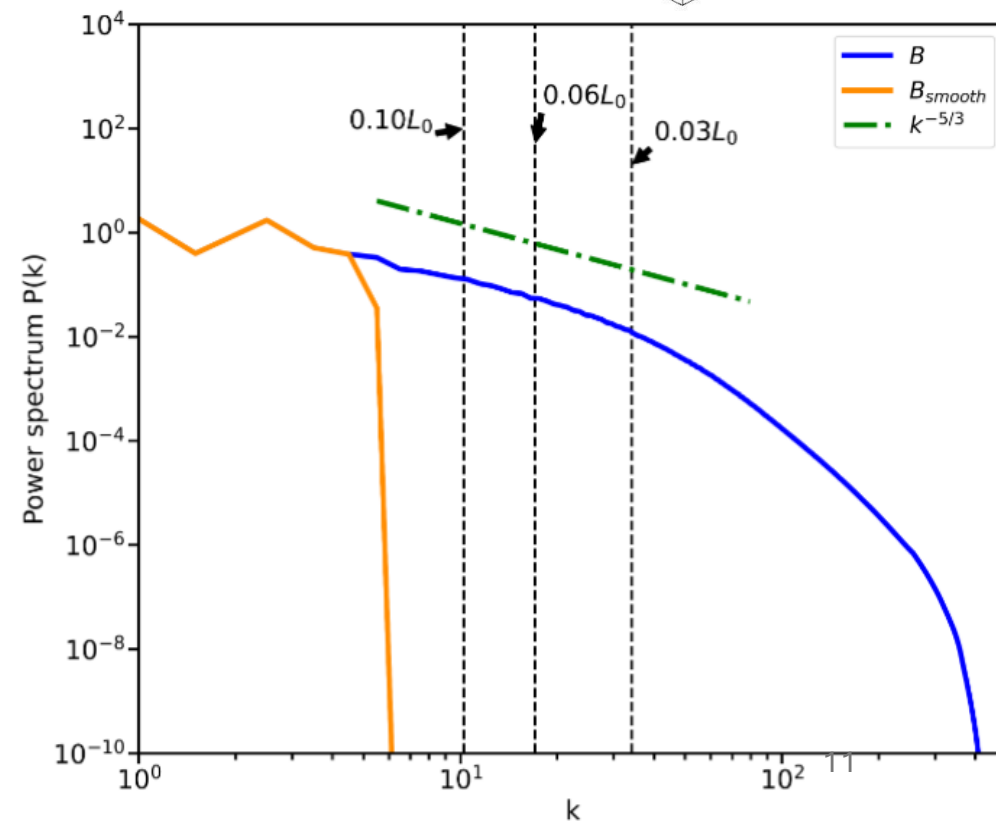
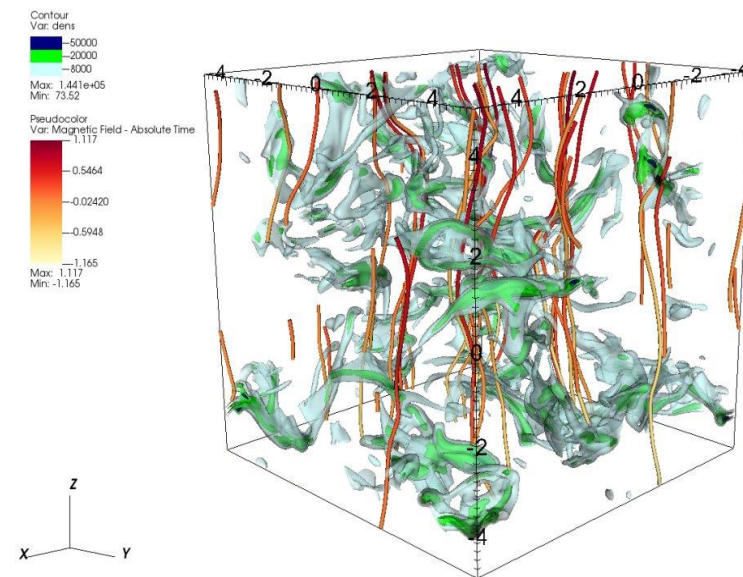
- Mirror only

$$\mu = \cos(\theta)$$

|      |
|------|
| 0.20 |
| 0.80 |

$$R_L/L_0$$

|      |
|------|
| 0.03 |
| 0.06 |
| 0.10 |

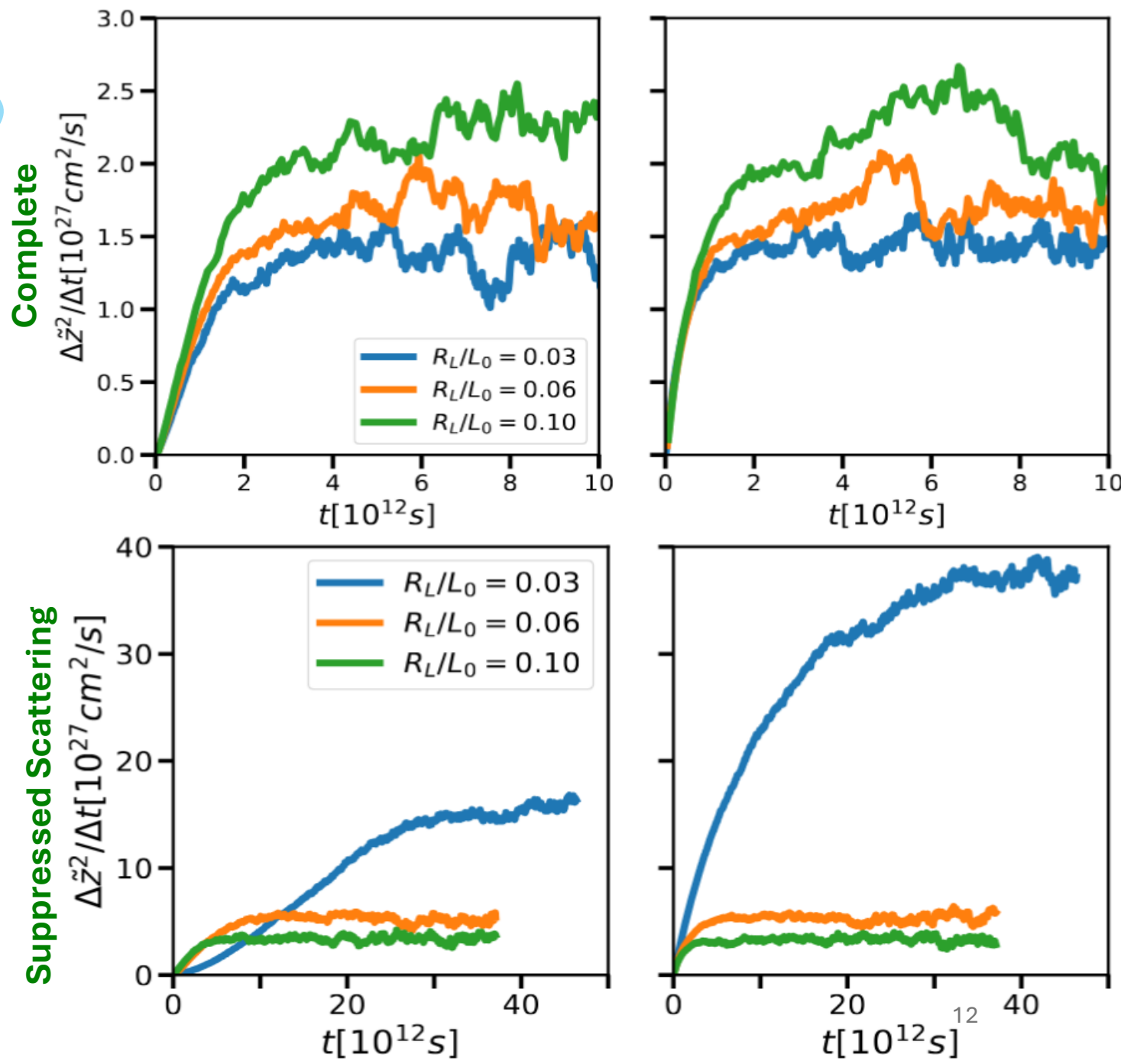




# Mirror+Scattering Diffusion Modeling

- Models scaled to a 3pc box.
  - $3\mu\text{G}$
  - Region around PWN
- $D_{\parallel}$  around  $10^{27}\text{cm}^2/\text{s}$   
(1 PeV)
- Can be effective even with suppressed pitch-angle scattering

$$D_{\parallel} = \frac{\langle (z-z_0)^2 \rangle}{t}$$



# A quick comparison to observations

- Considering different sizes

$$R_L[pc] = 1.084 \frac{(E/1PeV)}{(B/1\mu G)} \left( \frac{v_{\perp}}{c} \right),$$

$$\Omega[s^{-1}] \approx 9.743 \times 10^{-9} \left( \frac{1pc}{R_L} \right),$$

$$D_{\parallel,phys}[cm^2/s] = D_{\parallel} \cdot L_0 c$$

$$= D_{\parallel} \cdot 2.776 \times 10^{29} \left( \frac{L_0}{3pc} \right)$$

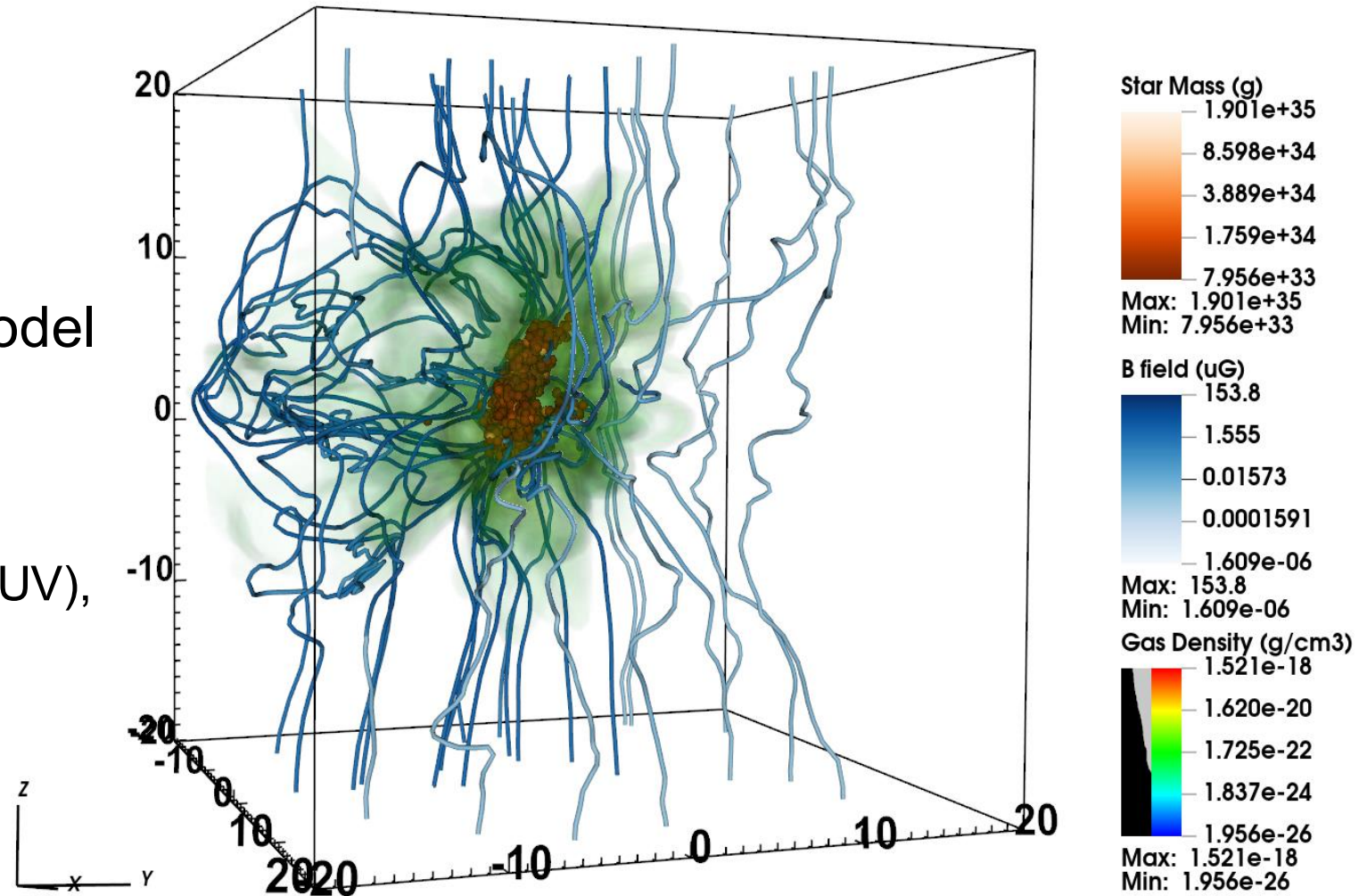
| $B(\mu G)$ | $L_0(pc)$ | $R/L_0$ | E(PeV) | $D_{\parallel}$ | $D_{\parallel,phys}(cm^2/s)$ |
|------------|-----------|---------|--------|-----------------|------------------------------|
| 3.2        | 1         | 0.03    | 0.09   | 0.005           | $4.63 \times 10^{26}$        |
| 3.2        | 1         | 0.06    | 0.18   | 0.006           | $5.55 \times 10^{26}$        |
| 3.2        | 1         | 0.10    | 0.30   | 0.008           | $7.40 \times 10^{26}$        |
| 3.2        | 5         | 0.03    | 0.44   | 0.005           | $2.31 \times 10^{27}$        |
| 3.2        | 5         | 0.06    | 0.89   | 0.006           | $2.78 \times 10^{27}$        |
| 3.2        | 5         | 0.10    | 1.48   | 0.008           | $3.70 \times 10^{27}$        |
| 10         | 5         | 0.03    | 1.40   | 0.005           | $2.31 \times 10^{27}$        |
| 10         | 5         | 0.06    | 2.80   | 0.006           | $2.78 \times 10^{27}$        |
| 10         | 5         | 0.10    | 4.67   | 0.008           | $3.70 \times 10^{27}$        |

- Observed PWNe (Fang, 2022)

| Name              | Parameters of associated pulsars |       |       |          |                        | 100 TeV                | $\eta$ |
|-------------------|----------------------------------|-------|-------|----------|------------------------|------------------------|--------|
|                   | Gl                               | Gb    | $T$   | $D$      | $L$                    | $D_{100}$              |        |
|                   | [deg]                            | [deg] | [kyr] | [kpc]    | $10^{34} [erg s^{-1}]$ | $[cm^2 s^{-1}]$        | [%]    |
| Geminga halo      | 195.13                           | 4.27  | 342   | $0.25^a$ | 3.2                    | $4.6 \times 10^{27} c$ | $5^c$  |
| Monogem halo      | 201.11                           | 8.26  | 111   | 0.288    | 3.8                    | $1.5 \times 10^{28} d$ | $4^d$  |
| LHAASO J0621+3755 | 175.88                           | 10.96 | 208   | $1.6^b$  | 2.7                    | $2.3 \times 10^{27} c$ | $40^c$ |
| HESS J1831-098    | 21.90                            | -0.13 | 128   | 3.68     | 110                    | $9.0 \times 10^{27} e$ | $7^e$  |

# Applying to Young Massive Stellar Clusters

- **3D MHD simulation: background for CR cascading**
  - Polak et al. 2023
- Young massive stellar cluster model (compatible with W43 Cluster)
  - Highly super-sonic
  - $\langle B \rangle$  of a few micro Gauss
  - Includes stars, radiation feedback (UV), dust temperature

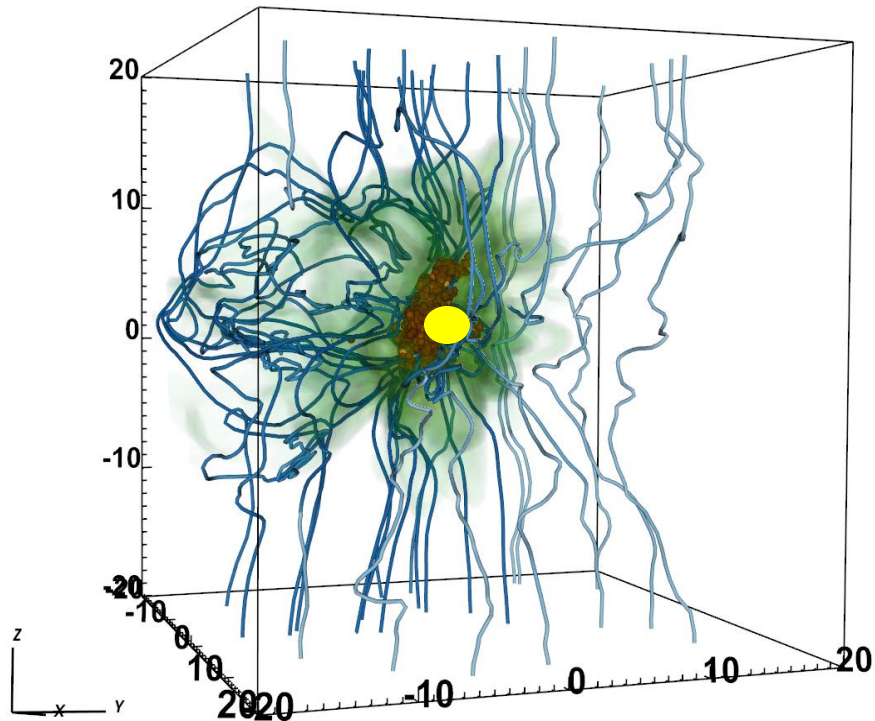




# Two Scenarios for CR production in the YMSC

## CR produced in the center:

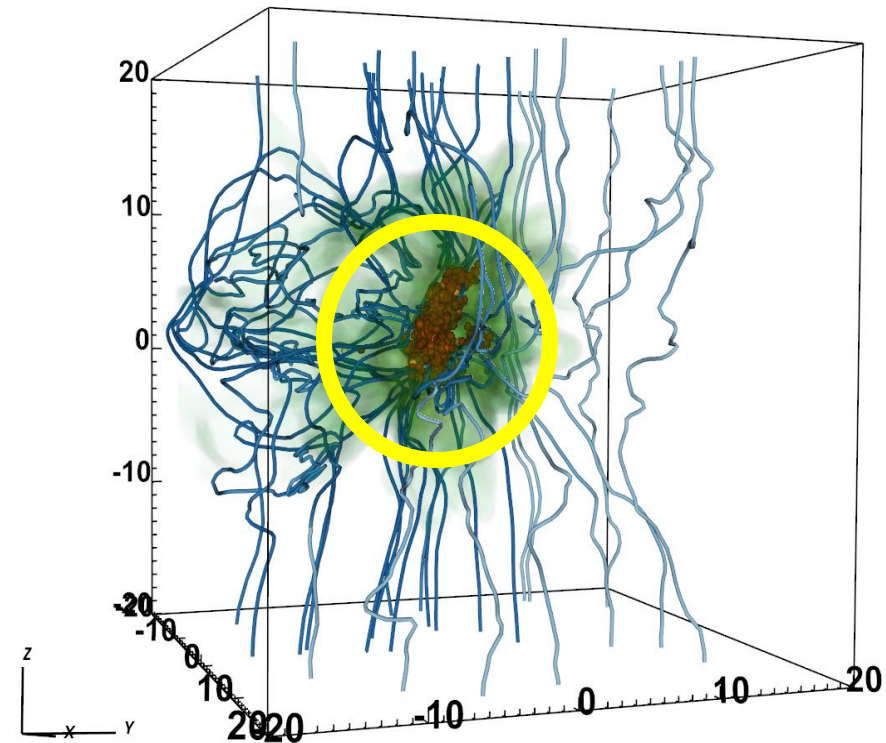
- mimics compact source accelerator, e.g. microquasar



Barreto-Mota, de Gouveia Dal Pino+, (in prep)

## CR produced in a shell around Massive Stars:

- mimics SB-wind shock front accelerator



# Simulating CR diffusion with CRPropa3

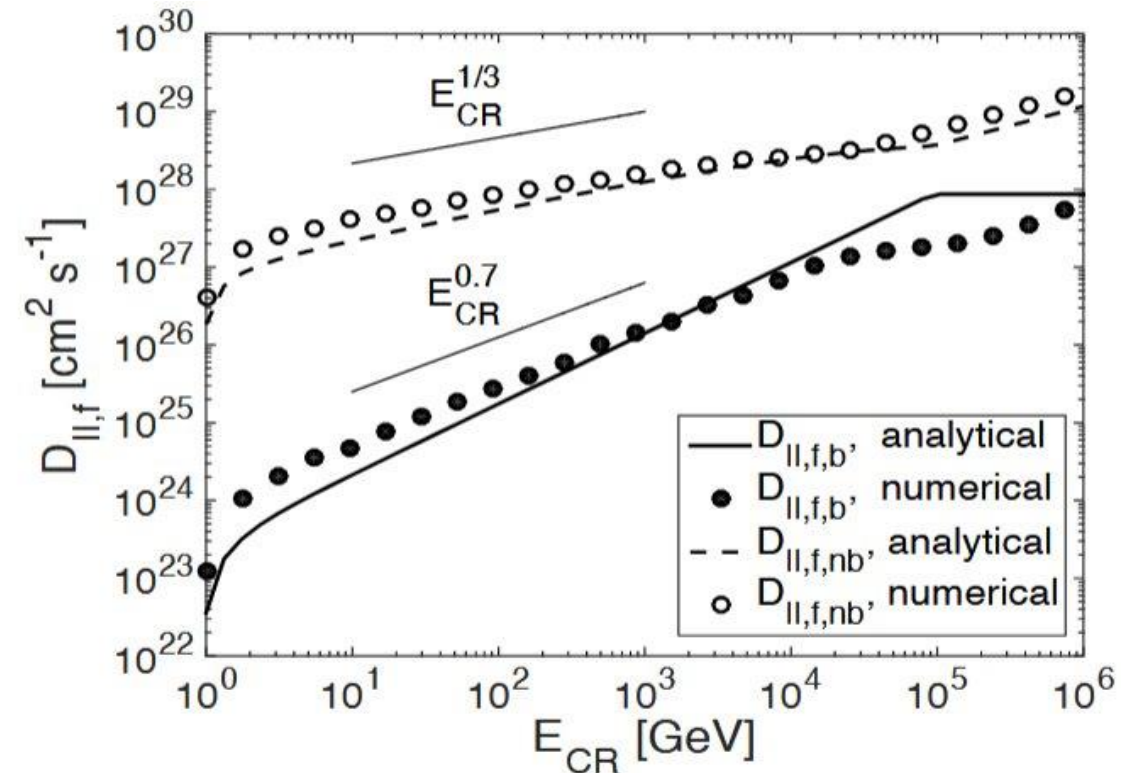
- Monte Carlo code (**CRPropa3**) (Alves-Batista et al. 2016)
- YMSCs simulations as the background (Polak et al. 2023)

We modeled **Mirror Diffusion energy-dependence**:

$D \sim E^{1/3}$  (scattering+mirror)

$D \sim E^{0.7}$  (only mirror)

Lazarian and Xu (2021)



# Target photon fields and Main interactions

We considered following **photon Fields**:

- Blackbody from the stars
- Background insterstellar radiation (ISRF)
- CMB
- Dust

Main interactions:

Proton-Proton chain

$$p + p \rightarrow p + p + \pi^{0,\pm} + X$$

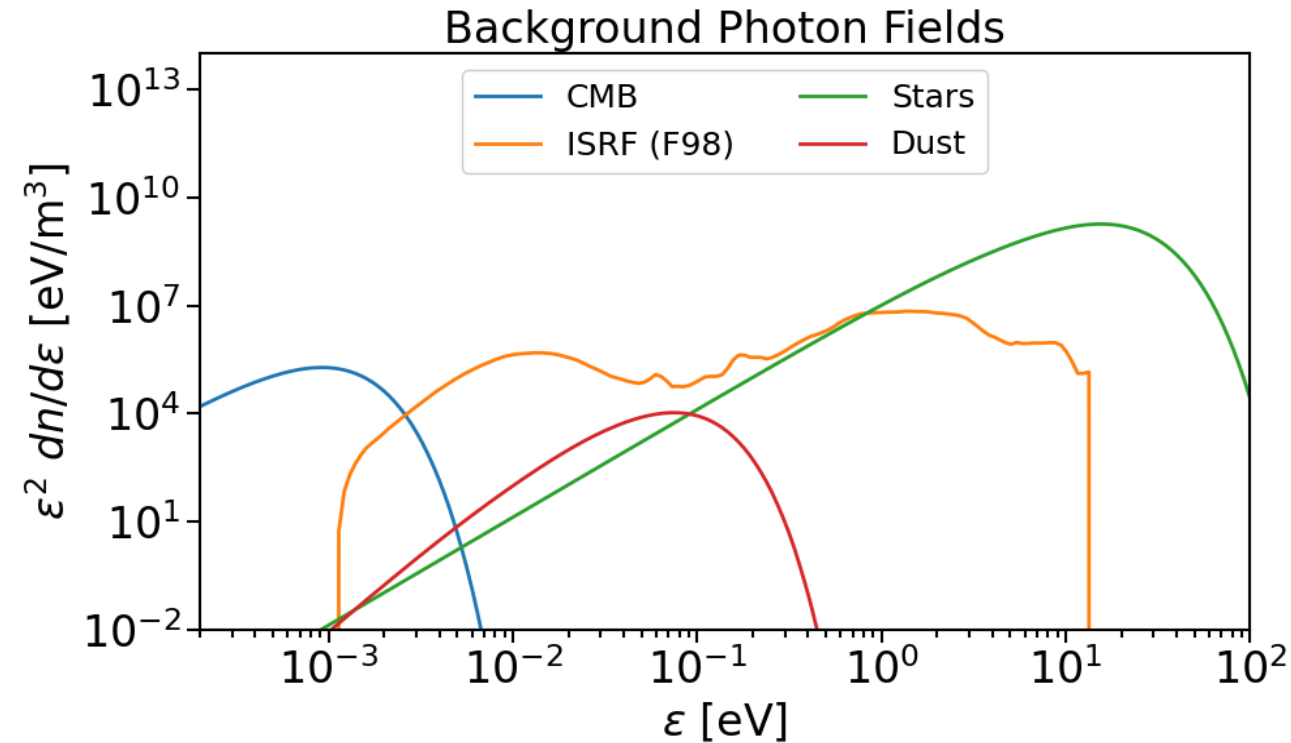
$$\pi^0 \rightarrow 2\gamma$$

$$\pi^\pm \rightarrow \mu^\pm + \nu_\mu(\bar{\nu}_\mu)$$

$$\mu^\pm \rightarrow e^\pm + \nu_e(\bar{\nu}_e) + \bar{\nu}_\mu(\nu_\mu)$$

Inverse Compton

$$e^\pm + \gamma_{\text{bg}} \rightarrow e^\pm + \gamma$$





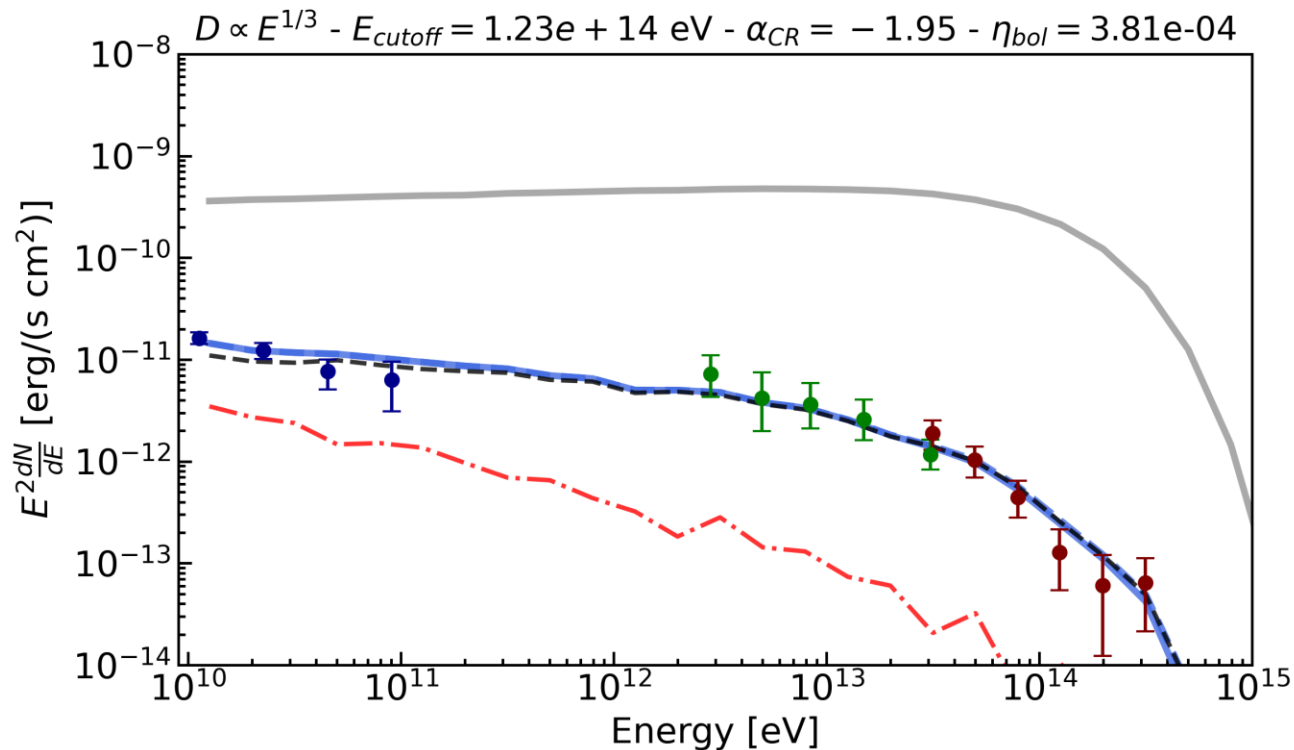
# Resulting $\gamma$ -ray spectrum

Barreto-Mota+ (in prep)

- Source at the center of the cluster
- Slower diffusion needs a harder injection spectra of CRs to fit observations
- Inverse Compton vs Hadronic Interactions (Dependence on the diffusion)
- $D \sim E^{1/3} + E_{inj}^{-2}$  (Fermi-like) – Most likely

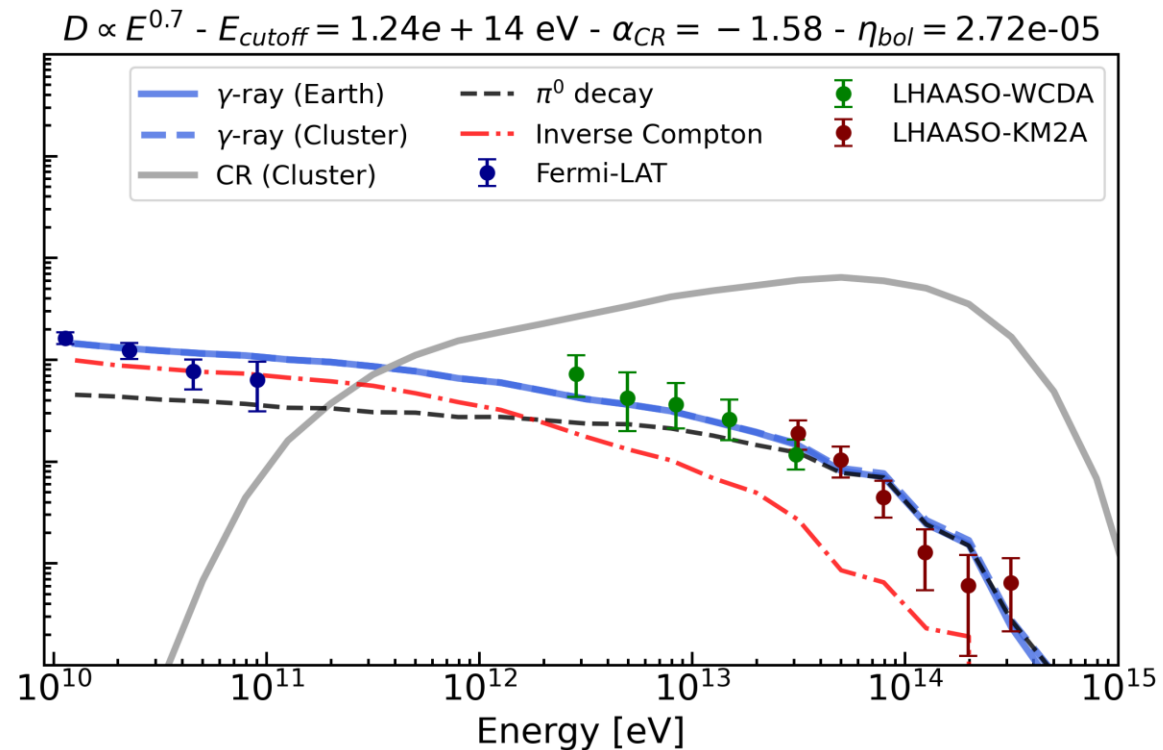
$$D \sim E^{1/3} \quad E_{CR} \sim E^{-2}$$

W43 Observations  
Cao et al. (2025)  
LHAASO Collaboration



$$D \sim E^{0.7}$$

$$E_{CR} \sim E^{-1.6}$$



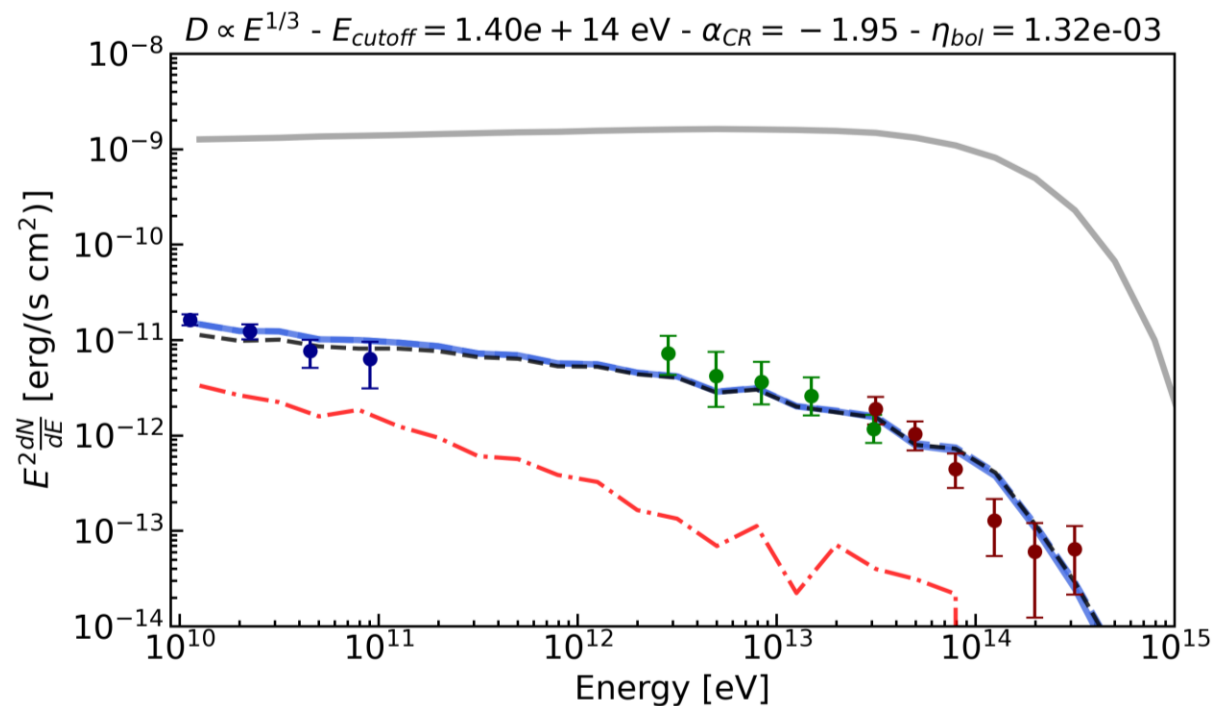
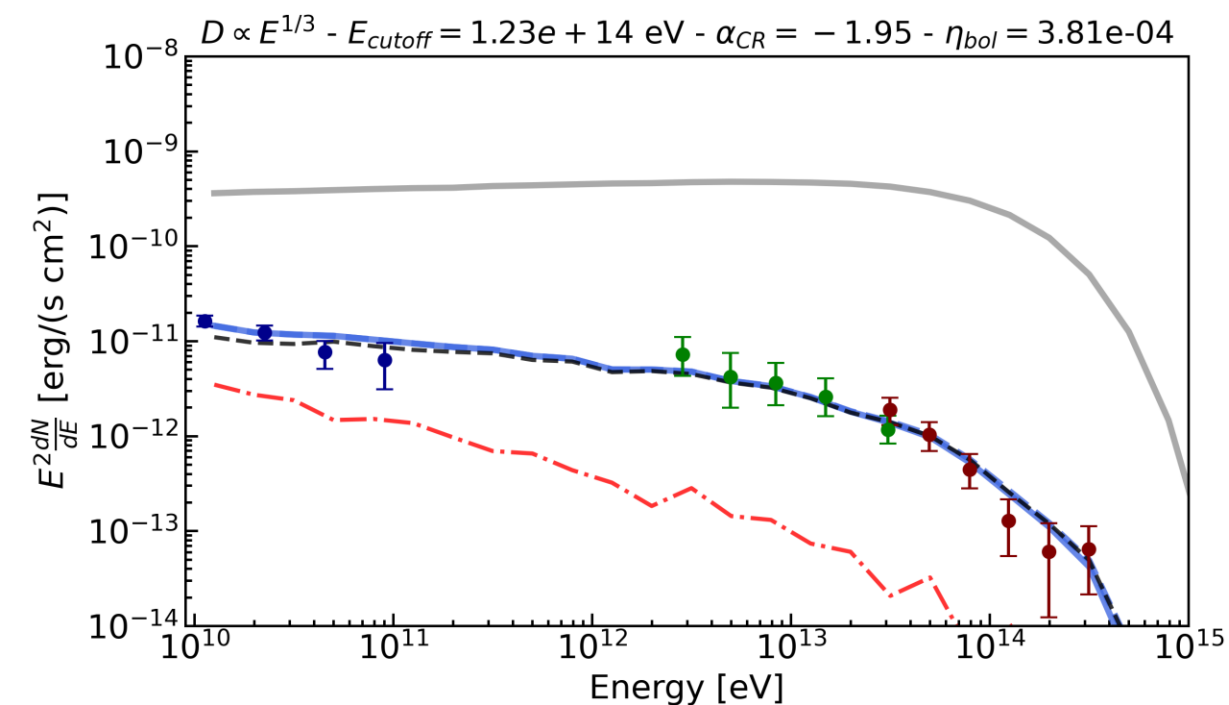
# Resulting $\gamma$ -ray spectrum for YMSC

Source at the  
**center** of the  
cluster

$$D \sim E^{1/3}$$

$$E_{CR} \sim E^{-2}$$

Source at a **shell**  
of the cluster



Barreto-Mota, de Gouveia Dal Pino+, 2026 (in prep.)

# Summary our findings and take home message

- **Mirror diffusion inhibits overall diffusion of CRs (Barreto-Mota et al 2025)**
- **Present in any MHD turbulent system!**
- **Mirror+scattering:**  
    **provides physical explanation for diffusion energy-dependence:  $D \sim E^{1/3}$**
- **Can be effective even with suppressed pitch angle scattering**
  - Even in partially ionized plasmas (Hu et al. 2025)
- **Slower diffusion allows the CRs to be retained near the source**
  - Important implication for **particle acceleration** (Bell et al. 2025)
- **3D Simulations of CR cascading in YMSCs:**
  - **Mirror+scattering can explain the spectrum of W43 (Barreto-Mota et al.; 2026):**  
    **Best solution:  $D \sim E^{1/3}$  and CR power index  $\sim -2$**   
    **(source either at the center or at a shell of the cluster)**
- **Mirror+scattering diffusion may probably explain CR diffusion inhibition in most VHE emission systems; SNRs, GMCs, YMCS, ..**



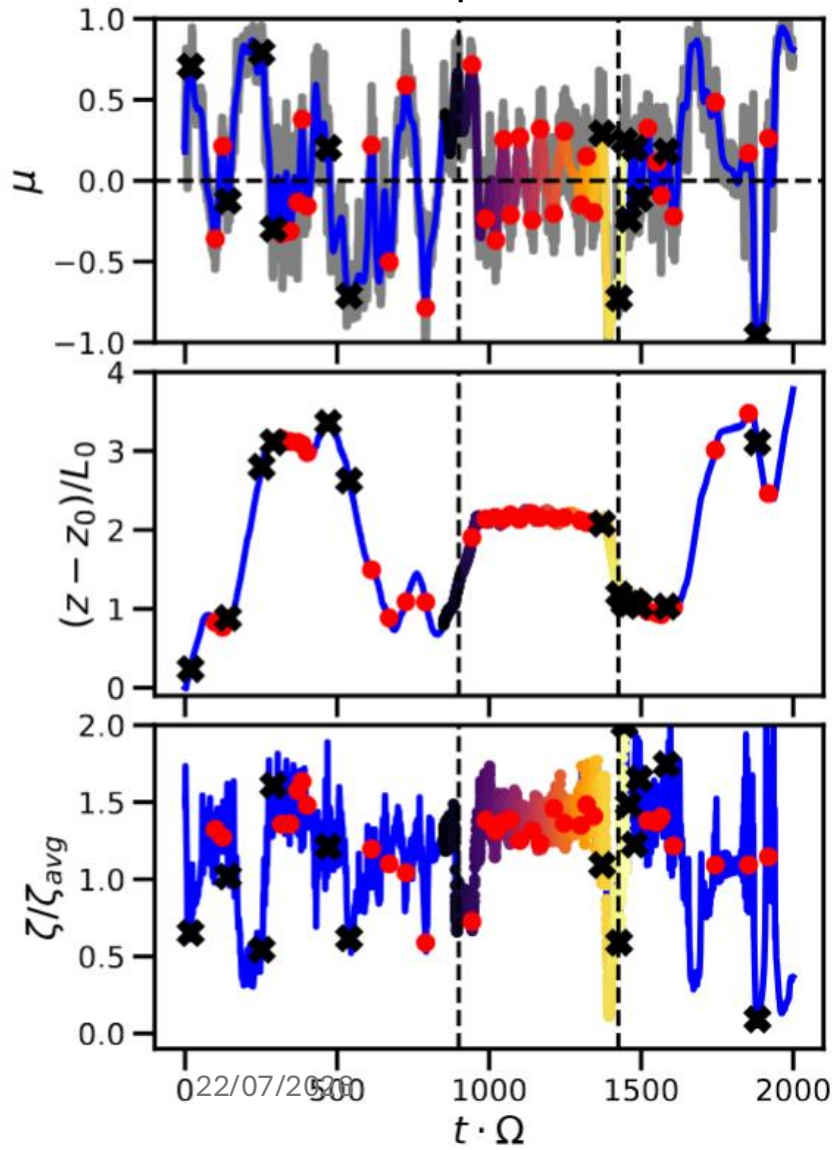


Thank you for your attention!

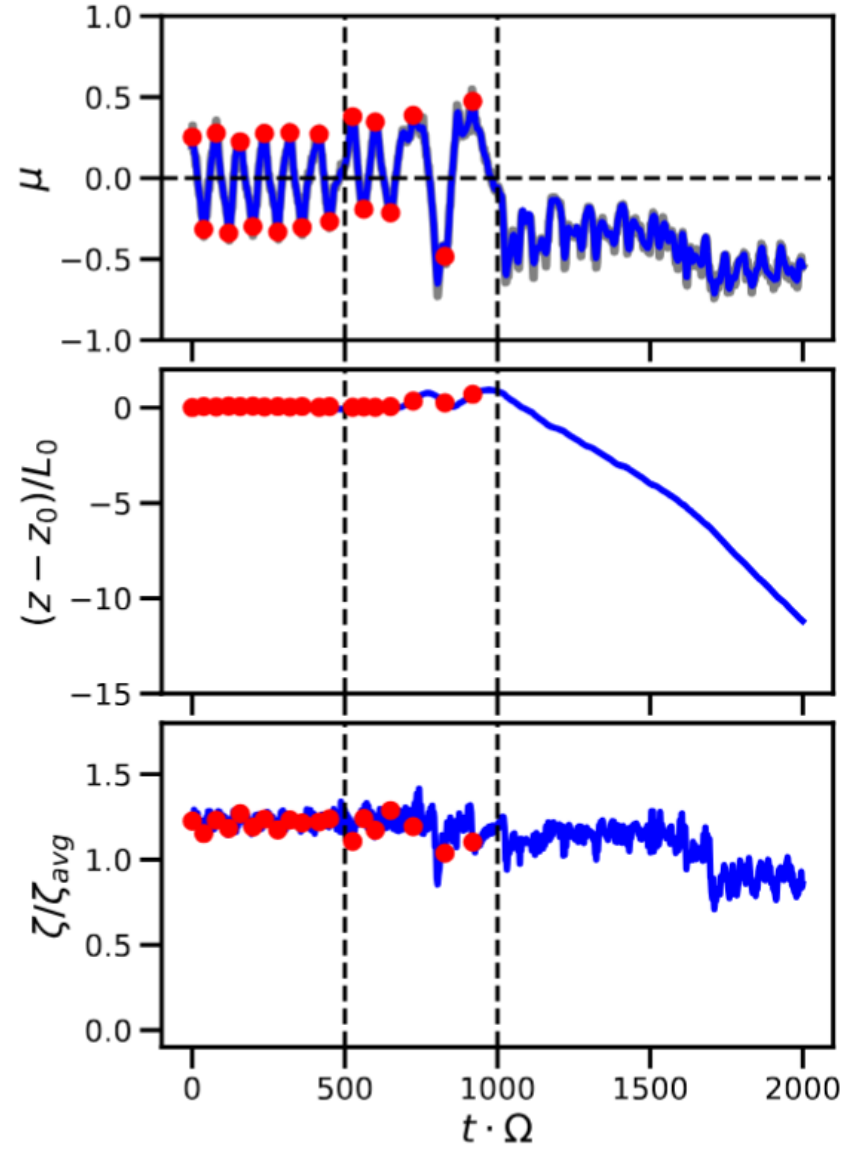
**EXTRA**

# Particle evolution

Complete B



Smoothed B



$$R_L/L_0 = 0.03, \mu_0 = 0.2$$

$$\mu = \cos(\theta)$$

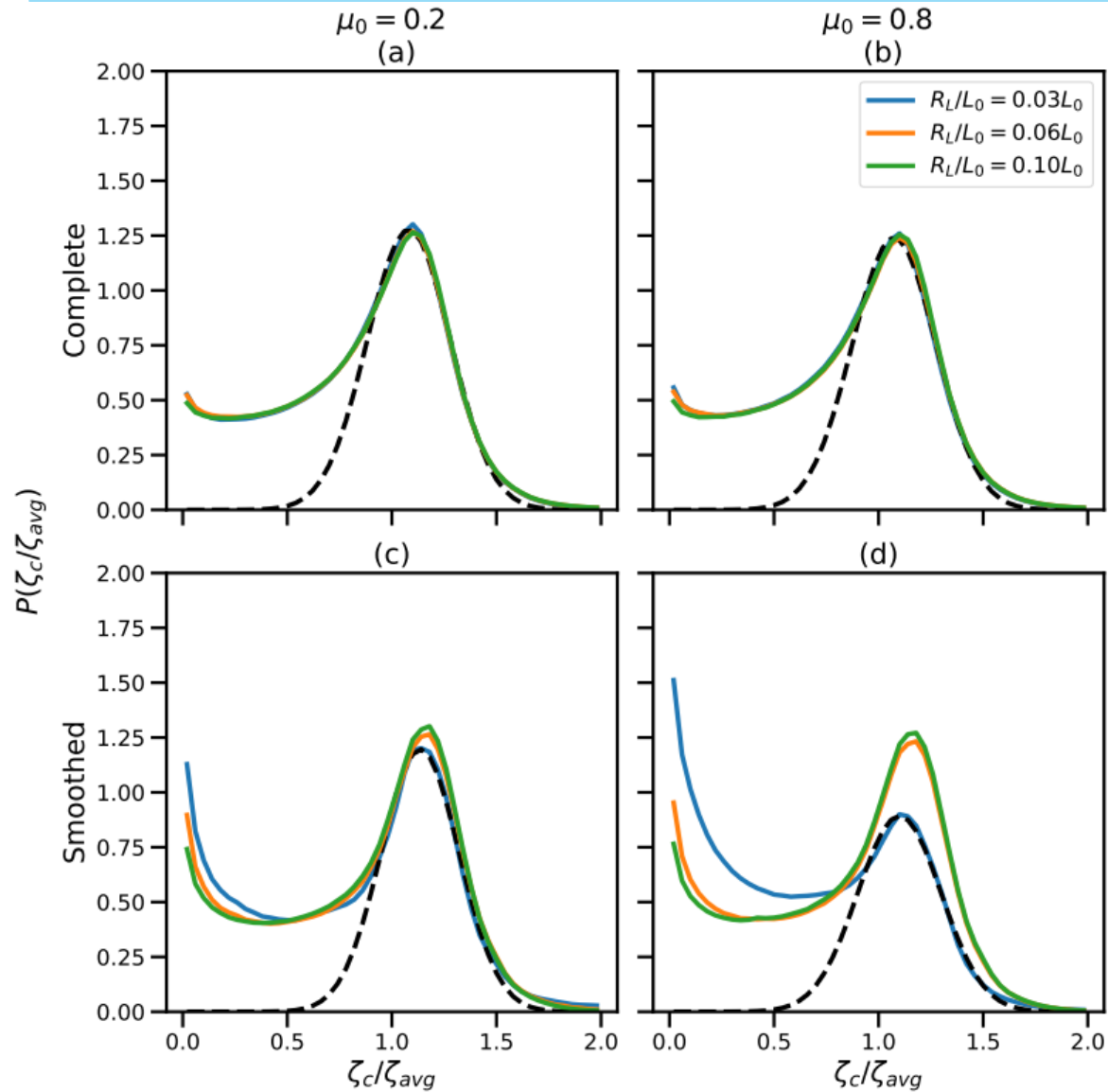
Parallel displacement

Mirror conserves  
magnetic momentum:

$$\zeta(t) = \gamma m v^2 \frac{1 - \mu(t)^2}{2|\mathbf{B}(t)|},$$



# Bounce identification

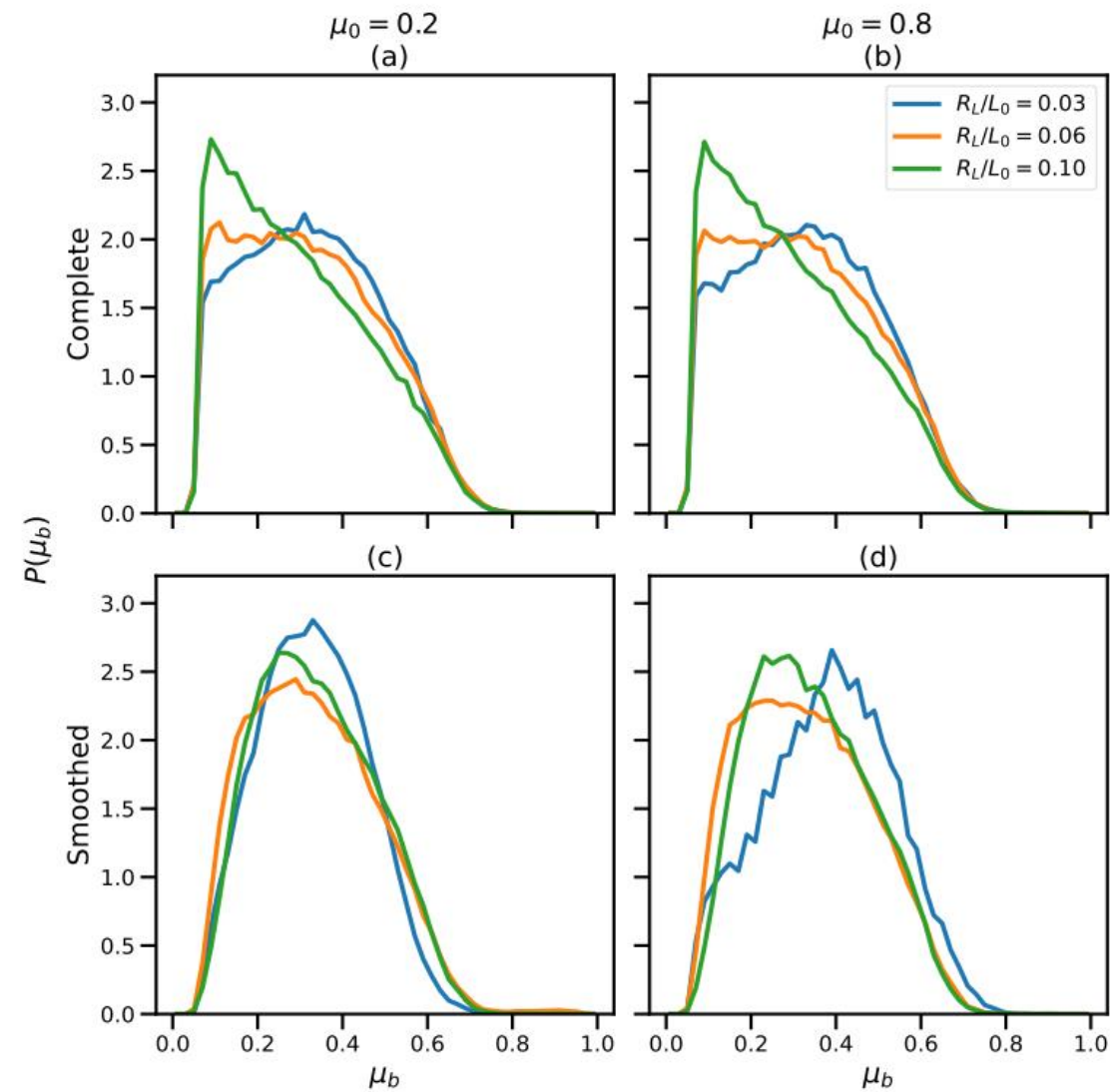
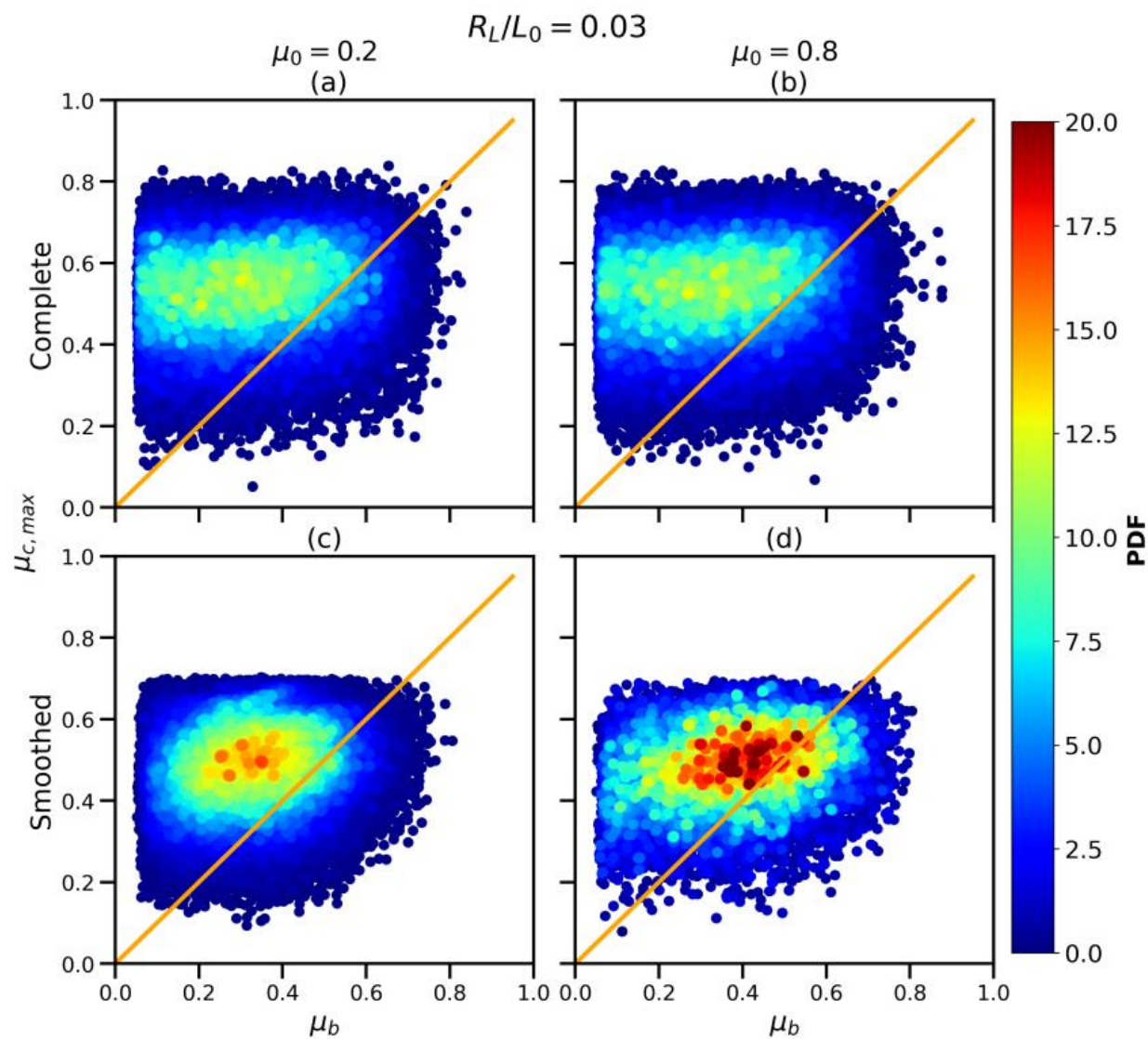


| Complete | $\mu_0 = 0.2$ |               |         | $\mu_0 = 0.8$ |               |         |
|----------|---------------|---------------|---------|---------------|---------------|---------|
|          | $R_L$         | Mirror Bounce | Total   | %             | Mirror Bounce | Total   |
|          | 0.03          | 91361         | 123,859 | 73.76         | 89,931        | 120,331 |
|          | 0.06          | 165,459       | 223,060 | 74.18         | 161,250       | 218,128 |
|          | 0.10          | 246,912       | 322,056 | 76.67         | 234,385       | 307,357 |

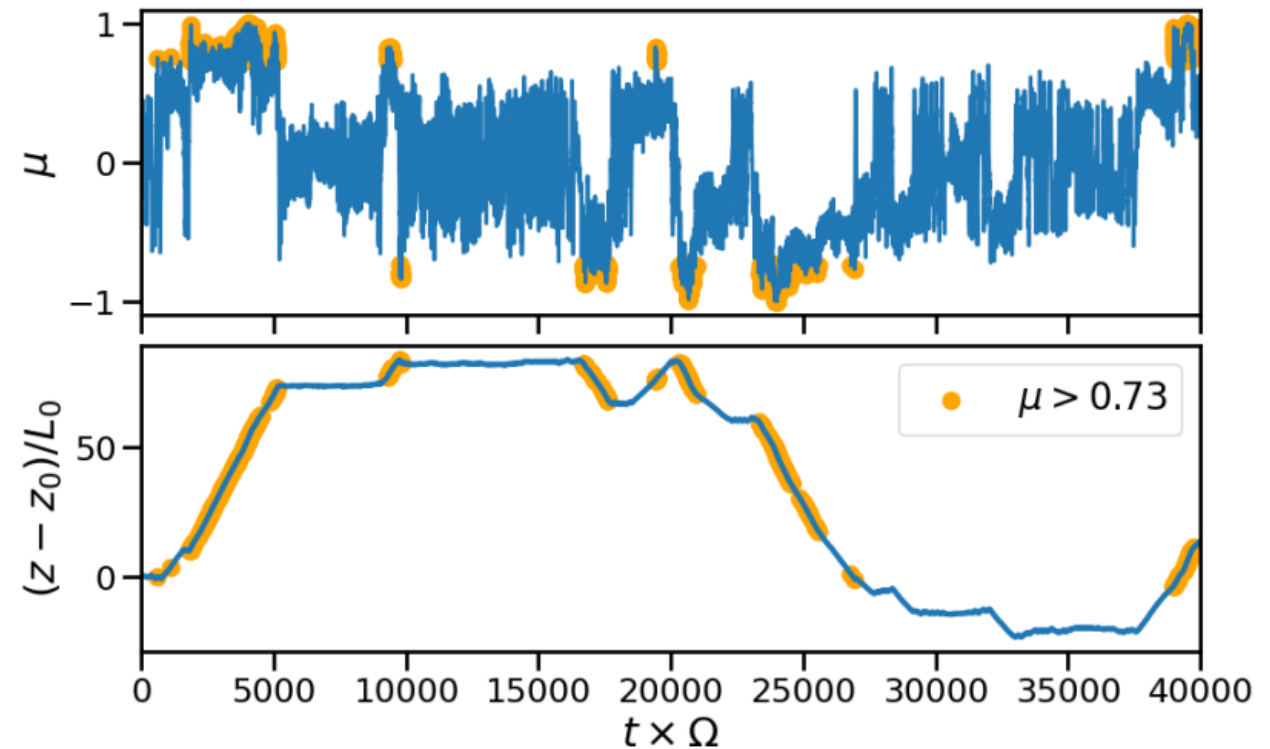
| Smooth | $\mu_0 = 0.2$ |               |         | $\mu_0 = 0.8$ |               |         |
|--------|---------------|---------------|---------|---------------|---------------|---------|
|        | $R_L$         | Mirror Bounce | Total   | %             | Mirror Bounce | Total   |
|        | 0.03          | 247,899       | 354,073 | 70.01         | 110,200       | 152,117 |
|        | 0.06          | 126,401       | 154,984 | 81.56         | 114,512       | 136,214 |
|        | 0.10          | 108,227       | 140,372 | 77.10         | 105,874       | 137,993 |

# Angle distribution



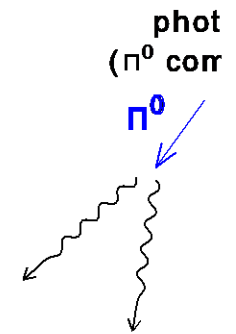
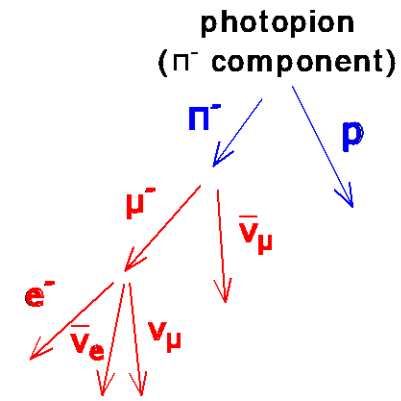
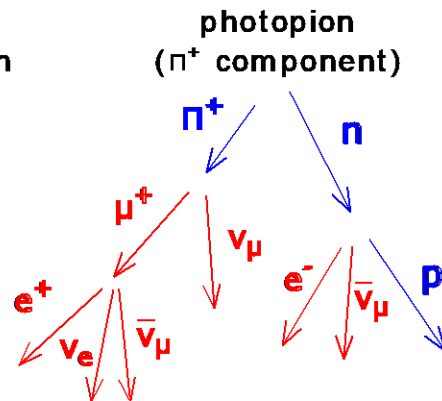
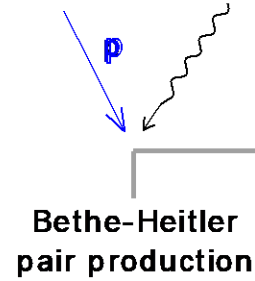
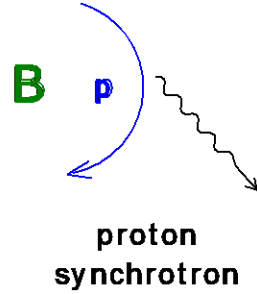
# Scattering vs mirror – smoothed model

$$k_{\text{res}} 2\pi R_L \simeq \frac{(1 - \cos^2 \theta_{\text{res}})^{0.5}}{\cos \theta_{\text{res}}},$$



# Non-thermal processes

hadronic



leptonic

