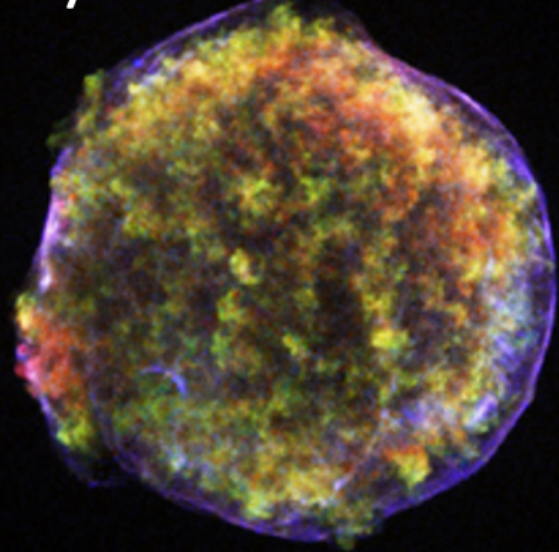
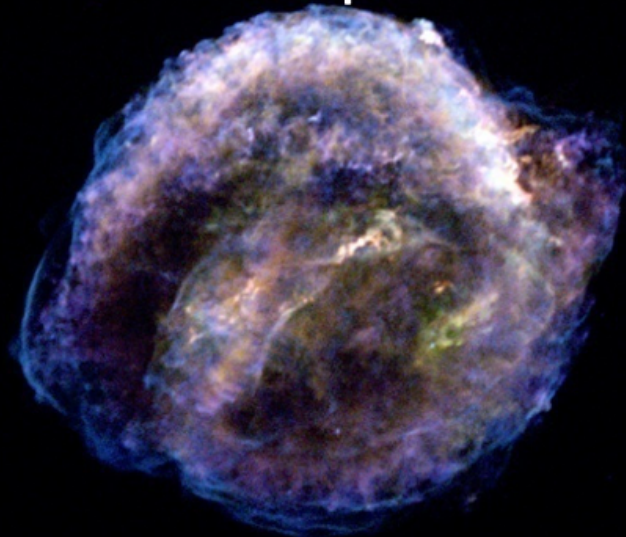


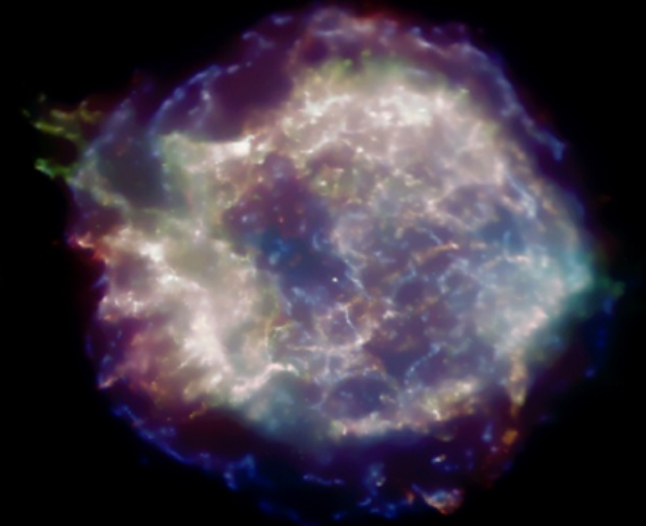
Tycho 1572AD



Kepler 1604AD



SN1006



Cas A 1680AD

Middle-aged supernova remnants as test-bench for the PeVatron scenario



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The SNR paradigm for the origin of Galactic CRs

Enough power in SN explosions to explain CRs



Baade & Zwicky, PNAS 20 (1934) 259



Ginzburg & Syrovatsky, PTPS 20 (1961) 1

SNR shocks $\rightarrow$ acceleration sites

Diffusive Shock Acceleration



Axford et al., ICRC1977, 11 132



Krymskii, AKSSRD 234 (1977) 1306



Bell, MNRAS 182 (1978) 147



Blandford & Ostriker, ApJ 221 (1978)

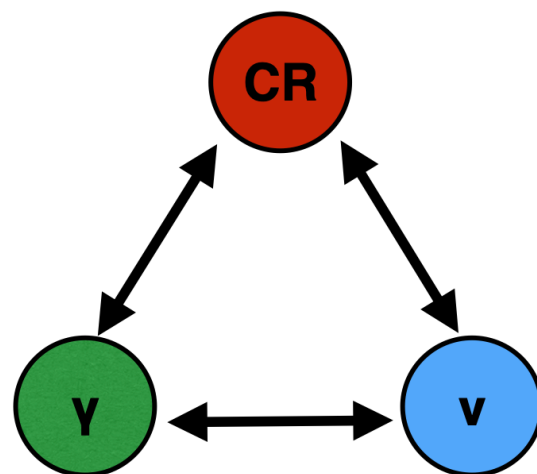
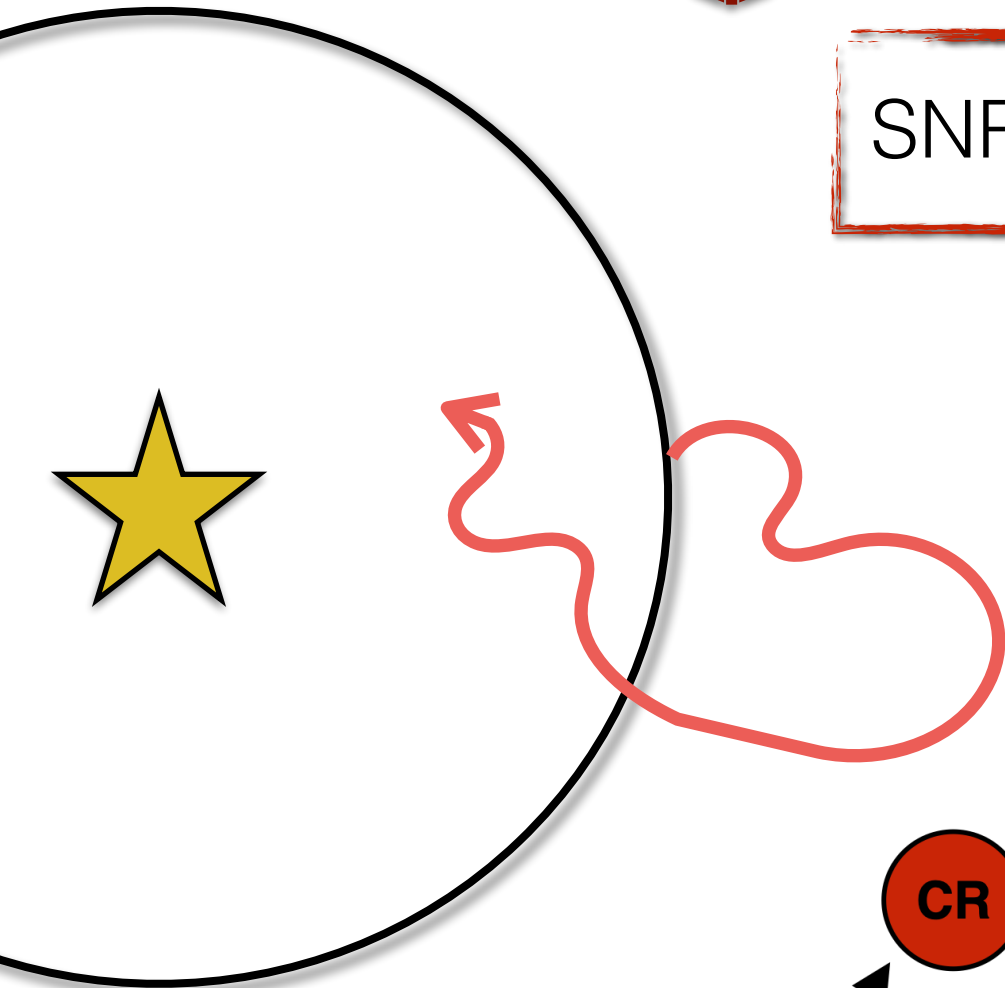
$$\rightarrow f_0(p) \propto p^{-4}$$

pp interaction $\rightarrow$ γ rays and ν



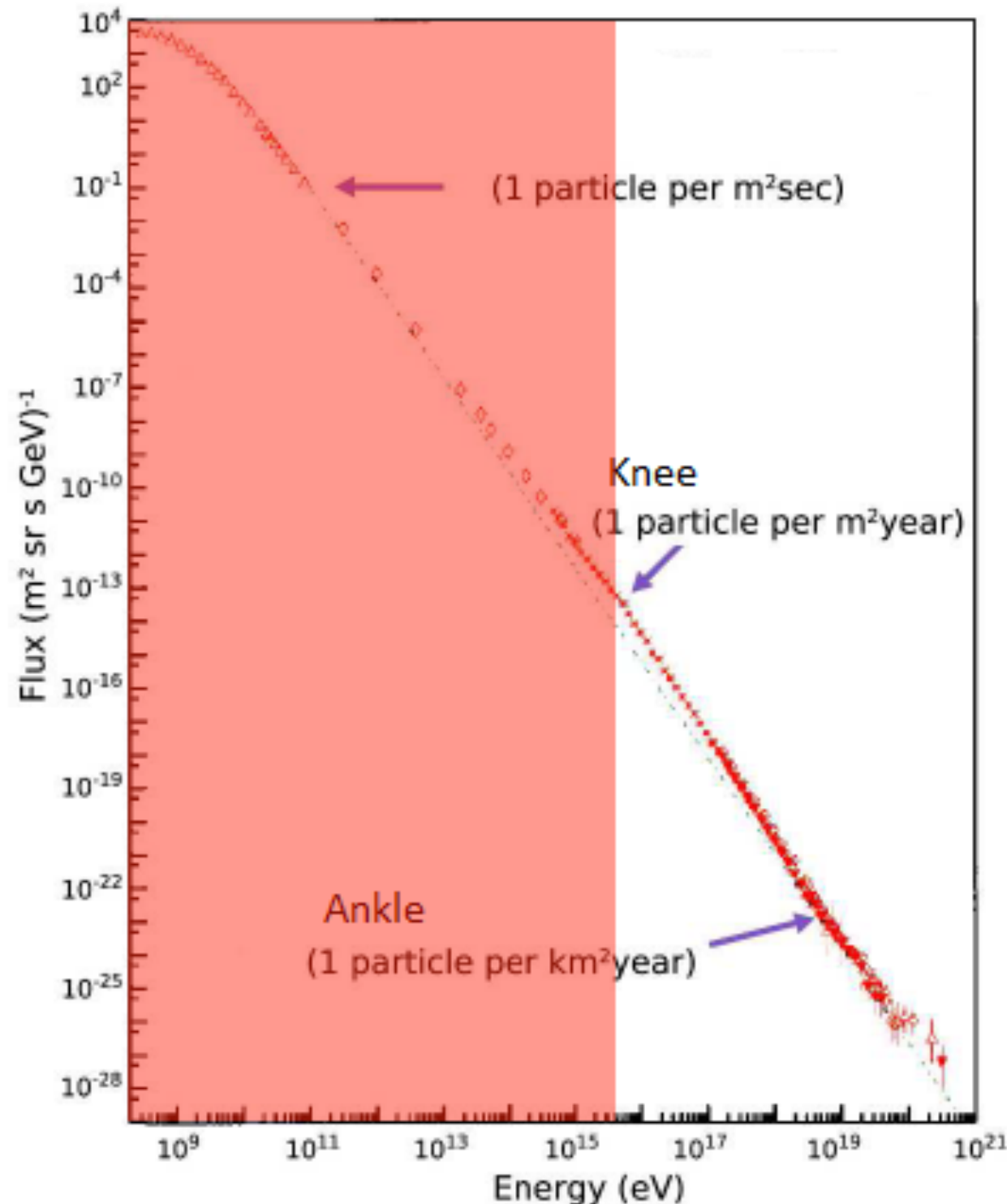
Aharonian et al., A&A 285 (1994) 645A

$$\rightarrow \frac{dN}{dE} \propto E^{-2}$$



Are SNRs proton PeVatrons?

Hillas criterion



$$E_{max} \simeq v_s R B$$

shock speed radius magnetic field

$$E_{max} \simeq 1 \left(\frac{v_s}{10^3 \text{ Km/s}} \right) \left(\frac{R}{\text{pc}} \right) \left(\frac{B}{\mu\text{G}} \right) \text{TeV}$$

3 3 10

$$E_{max} \simeq 100 \text{ TeV}$$

B-field amplification is required to achieve PeV energies

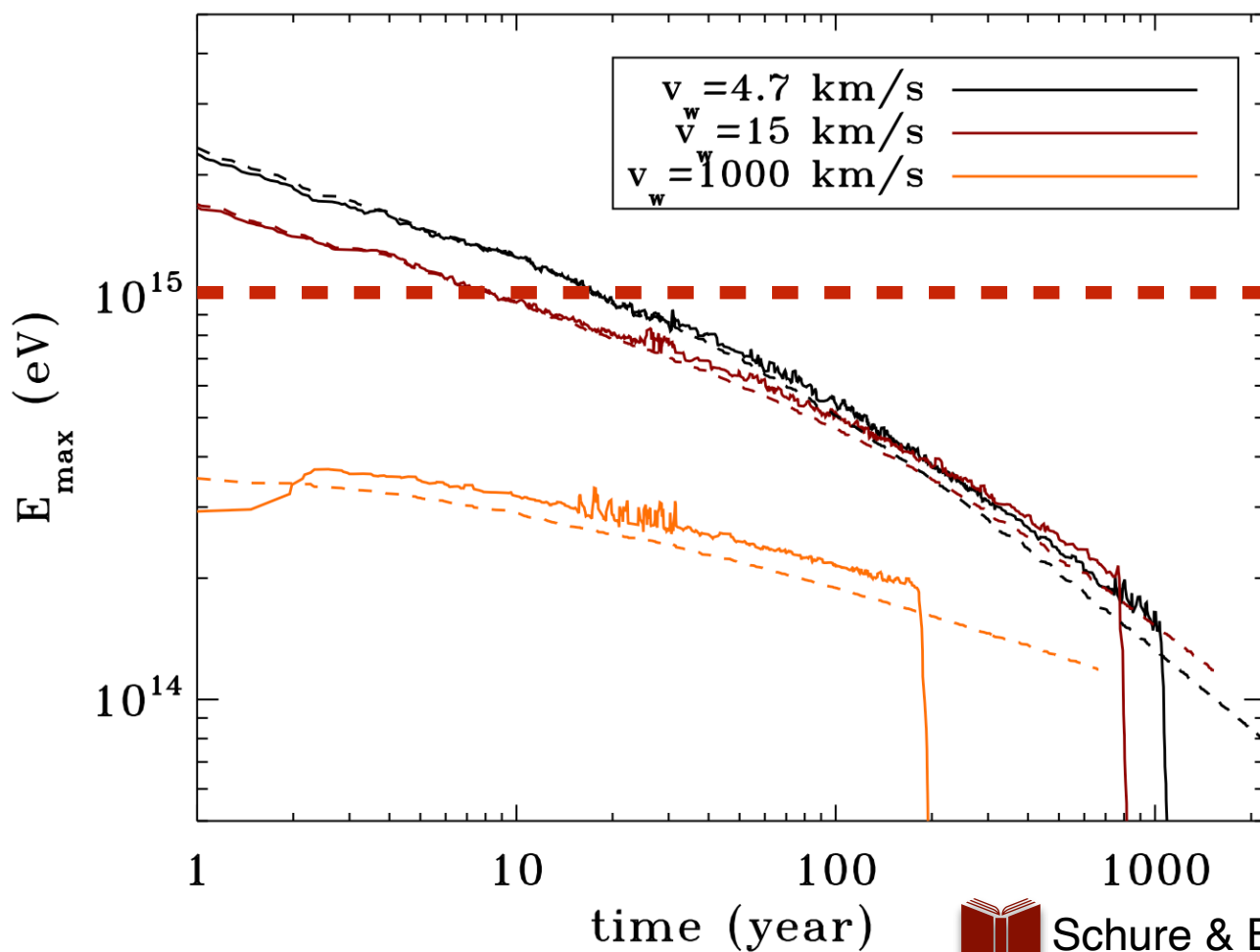


Cesarsky et al., SSRev 36 (1983) 173C

The problem of maximum energy in young SNRs

- Type Ia (e.g. Tycho) → expanding in constant density medium
- Core Collapse (e.g. CasA, RXJ1713.7-3946) → expanding in the dense slow wind of the progenitor star

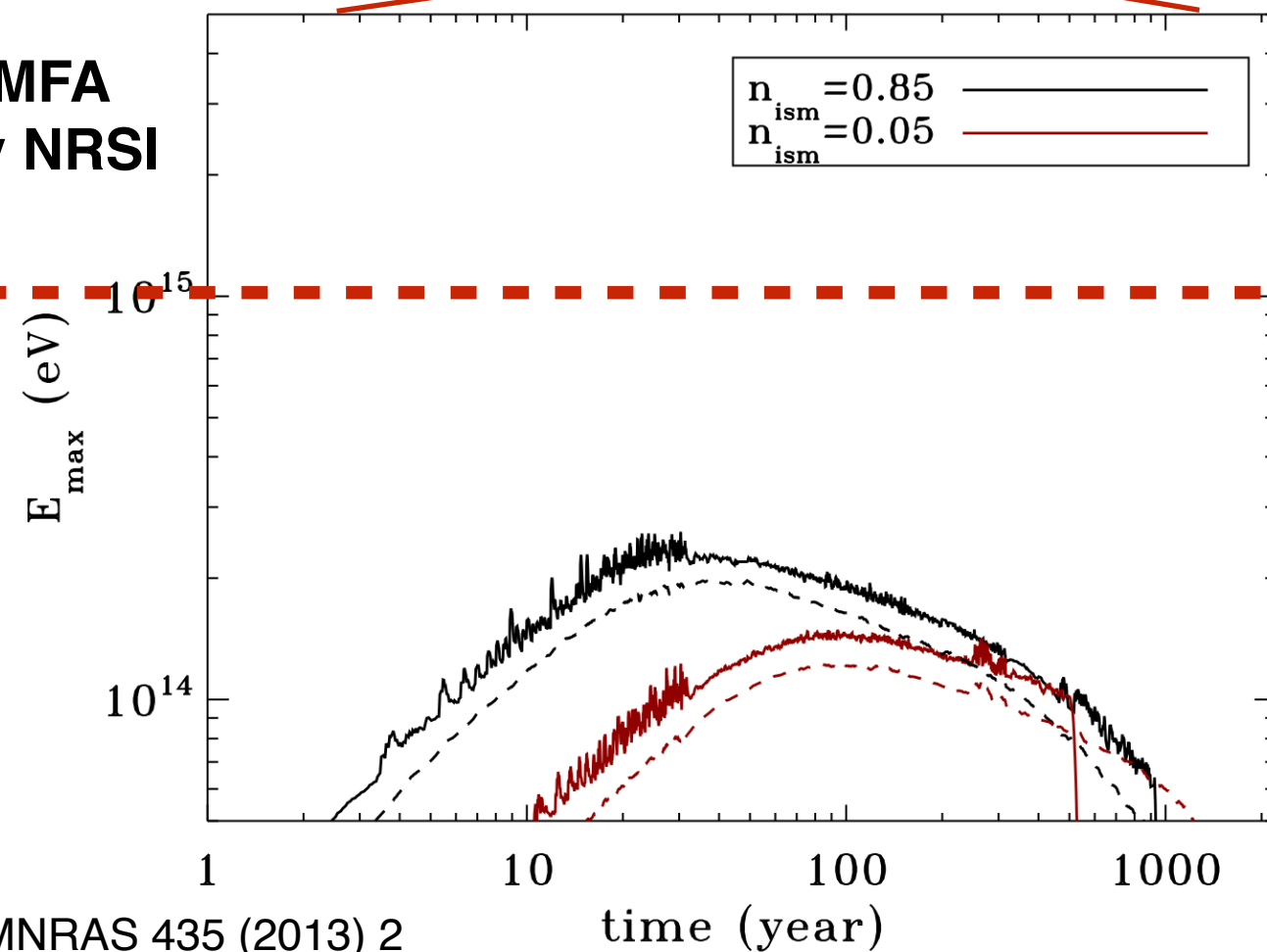
Remnants of type II



Schure & Bell, MNRAS 435 (2013) 2

~~Remnants of type Ia~~

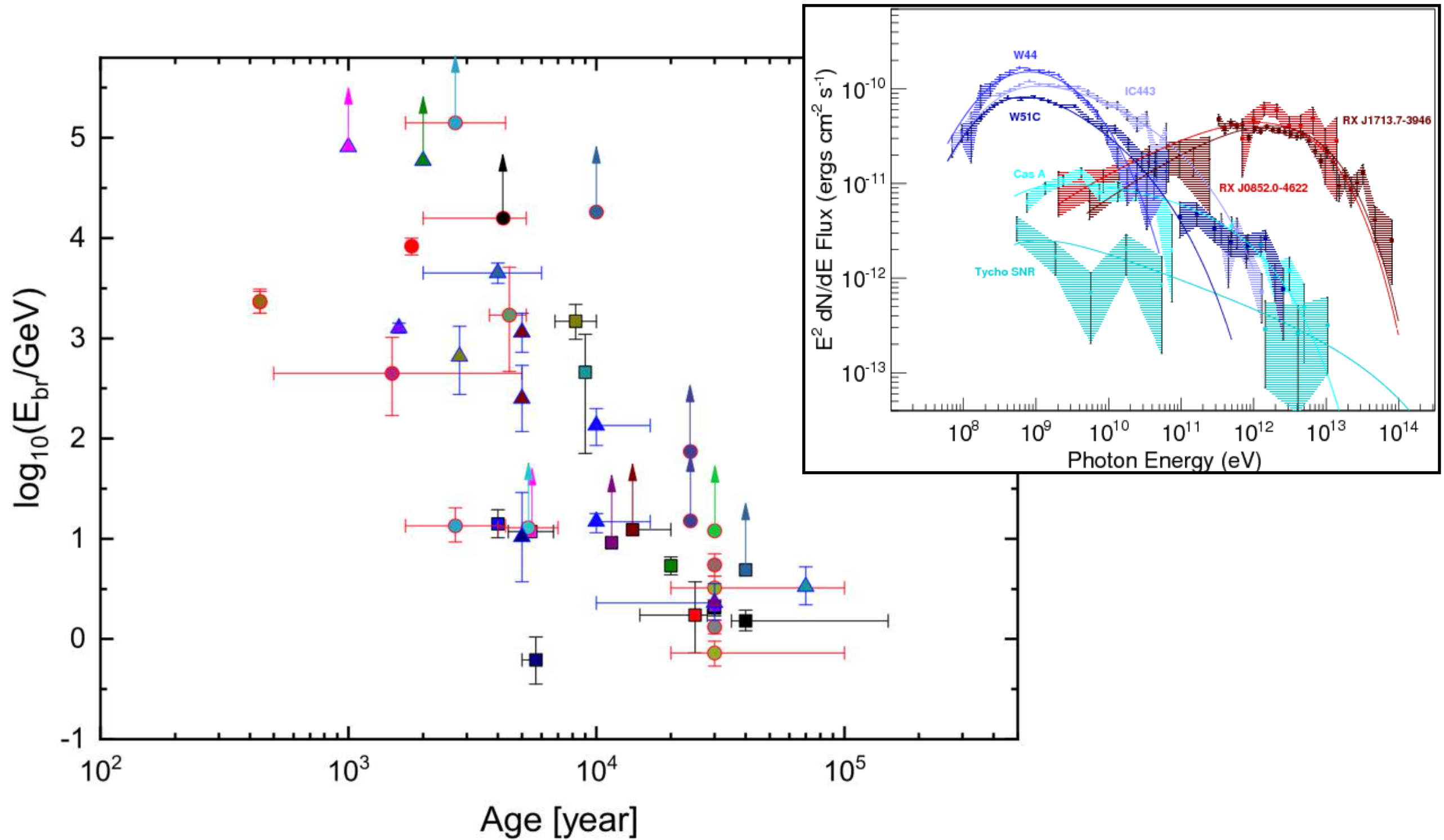
MFA
by NRSI



Only special explosions might achieve the knee



A population study of evolved SNRs



The role of particle escape or how do accelerated particles become CRs?

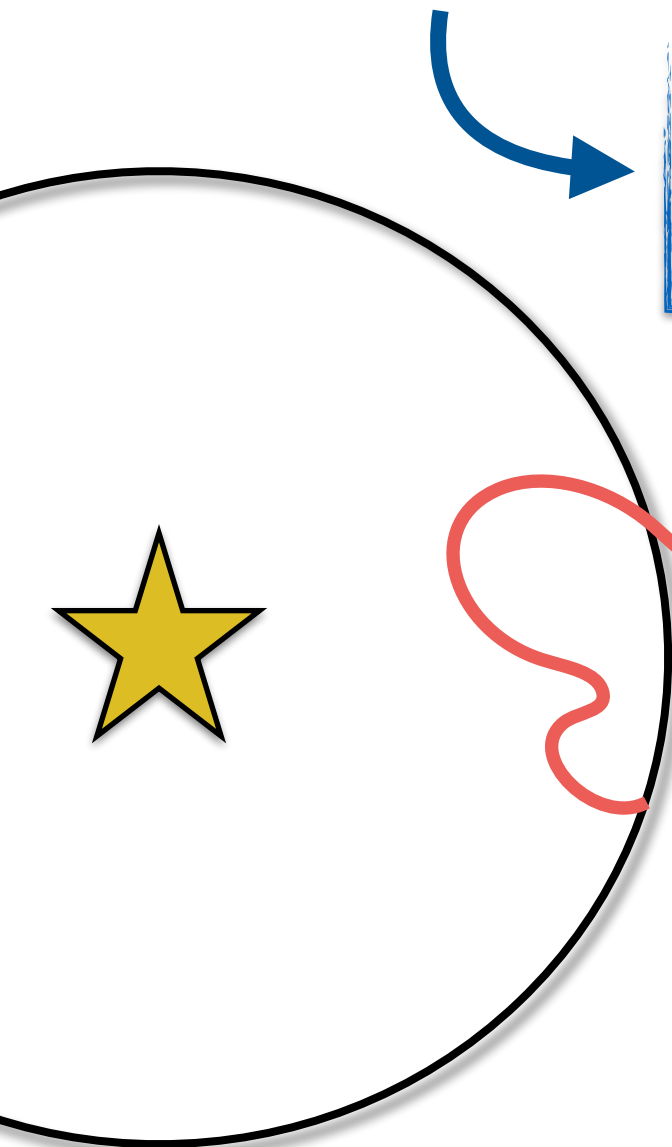
Acceleration at the shock: $f_0(p)$

$$f_0(p) \neq f_{\text{esc}}(p) \neq f_{\text{prop}}(p)$$

Escape from the shock: $f_{\text{esc}}(p)$

Propagation inside the Galaxy: $f_{\text{prop}}(p)$

Observation



The role of particle escape or how do accelerated particles become CRs?

Acceleration at the shock: $f_0(p)$

Escape from the shock: $f_{\text{esc}}(p)$



Ptuskin & Zirakashvili, A&A 429 (2005) 755



Gabici, Aharonian & Casanova, MNRAS (2009)



Ohira, Murase & Yamakazi, A&A (2010) 513



Bell & Shure, MNRAS 437 (2014) 2802



Cardillo, Amato & Blasi, APh 69 (2015) 1

Defines E_{max} and **spectral slope** of both **particles** and **radiation**

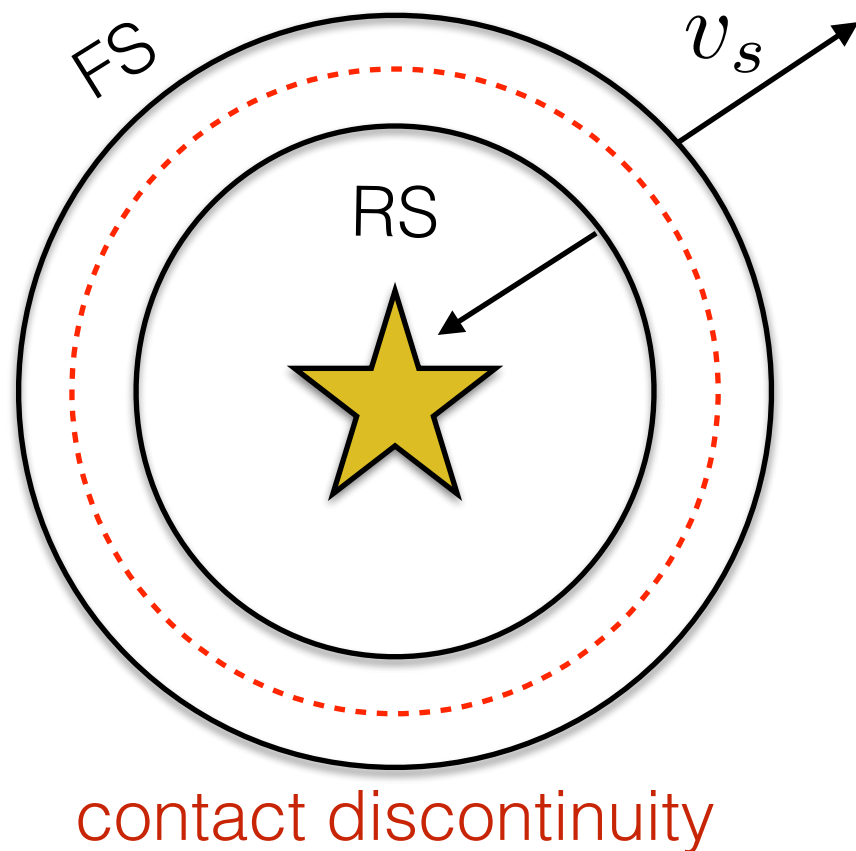


A **phenomenological** model to investigate the particle **escape** through spectral and morphological features of evolved SNRs in the HE and VHE domain.



Celli et al., MNRAS 490 (2019) 3

The hydrodynamical evolution of an SNR



I. Ejecta-dominated (ED) stage

$$M_{\text{ej}} \gg \frac{4}{3}\pi\rho R_s^3(t)$$

→ free expansion

II. Sedov-Taylor (ST) stage

$$M_{\text{ej}} \sim \frac{4}{3}\pi\rho R_s^3(t)$$

→ energy conservation

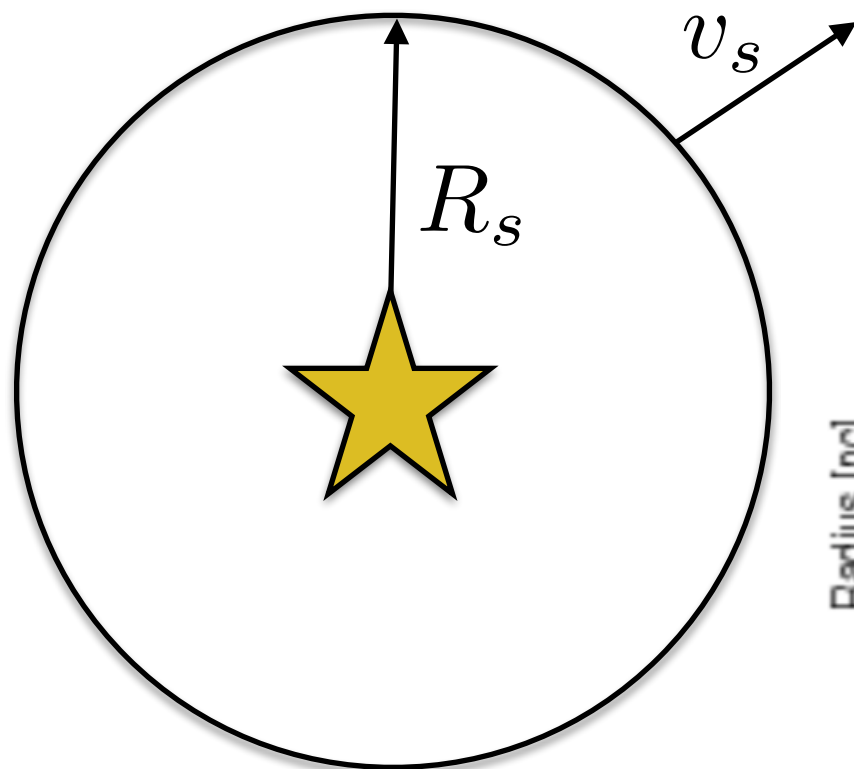
III. Radiative stage

→ momentum conservation

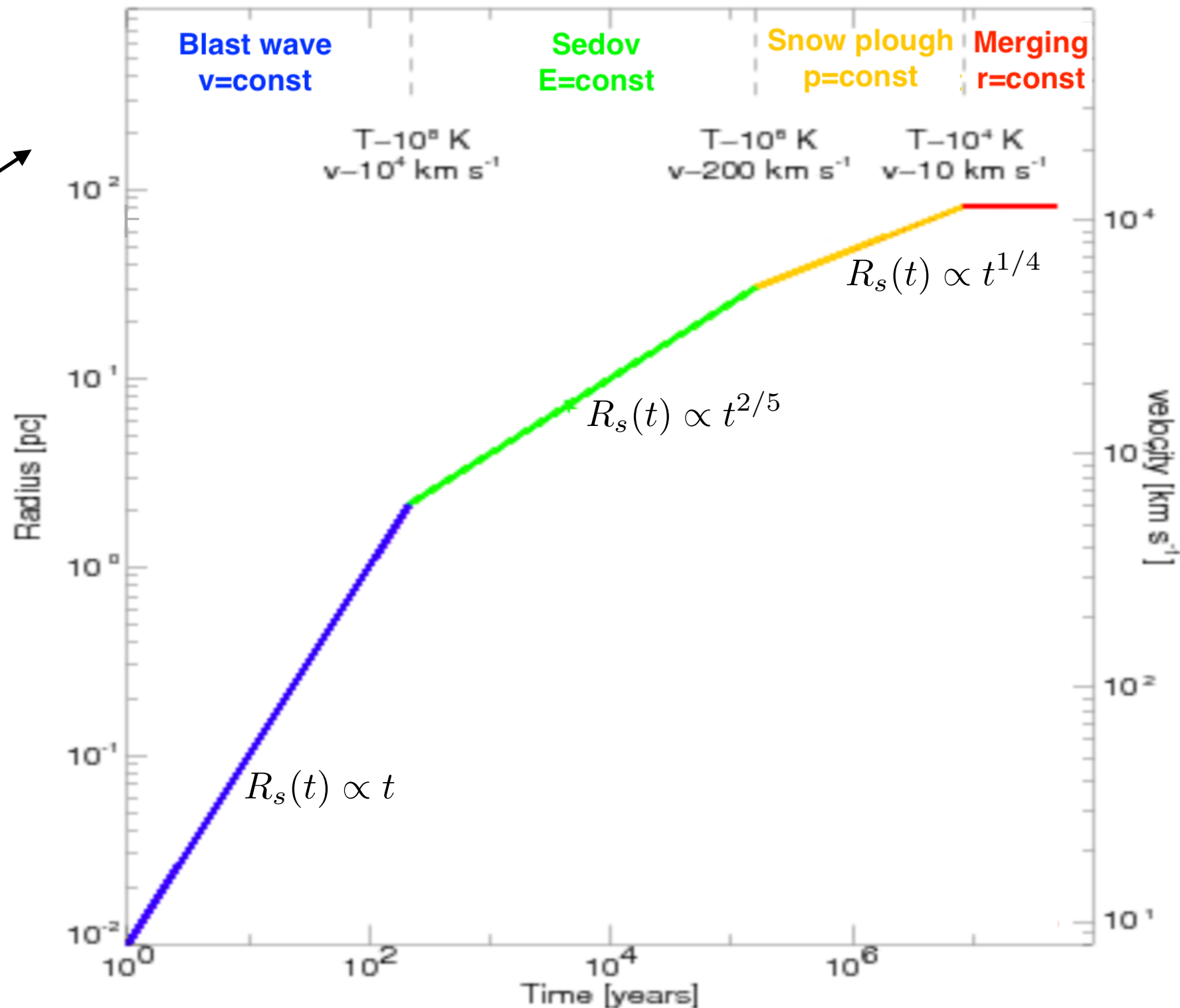
IV. Merging phase

→ pressure comparable to ISM

The hydrodynamical evolution of an SNR

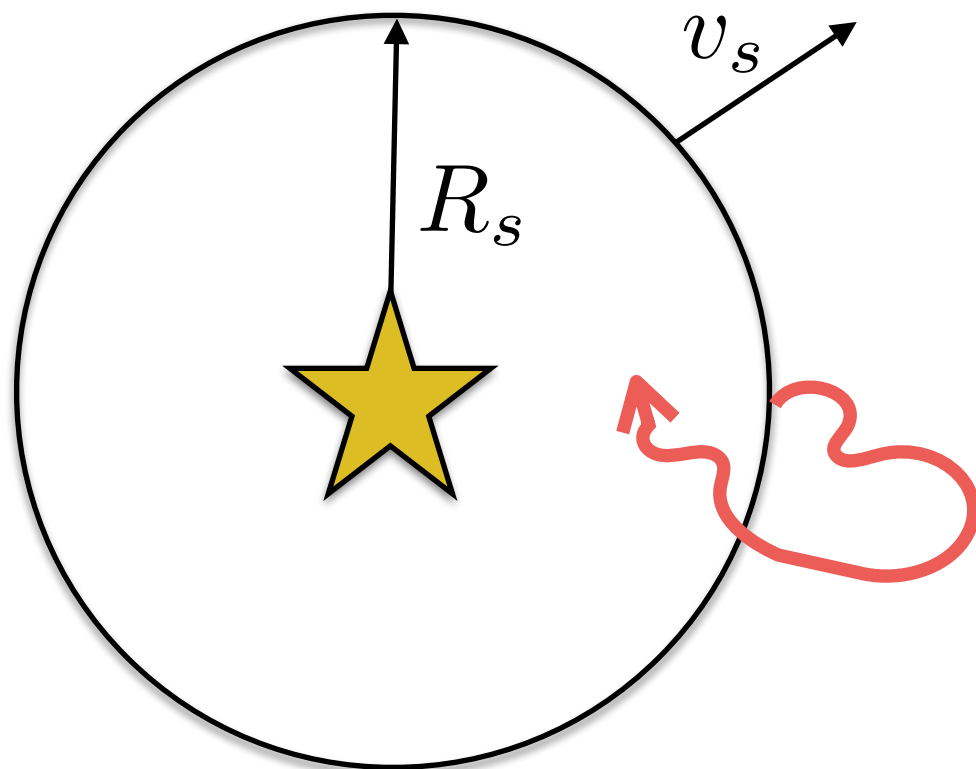


 Vink, A&A Rev 20 (2012) 1



$$t_{\text{Sed}} \simeq 1.6 \times 10^3 \text{ yr} \left(\frac{E_{\text{SN}}}{10^{51} \text{ erg}} \right)^{-1/2} \left(\frac{M_{\text{ej}}}{10 M_{\odot}} \right)^{5/6} \left(\frac{\rho_0}{1 m_{\text{p}}/\text{cm}^3} \right)^{-1/3}$$

Maximum energy in SNRs



- At Sedov time, particles at maximum energy E_M are still confined:

$$\lambda_d(E_M, t_{\text{Sed}}) \simeq R_s(t_{\text{Sed}})$$

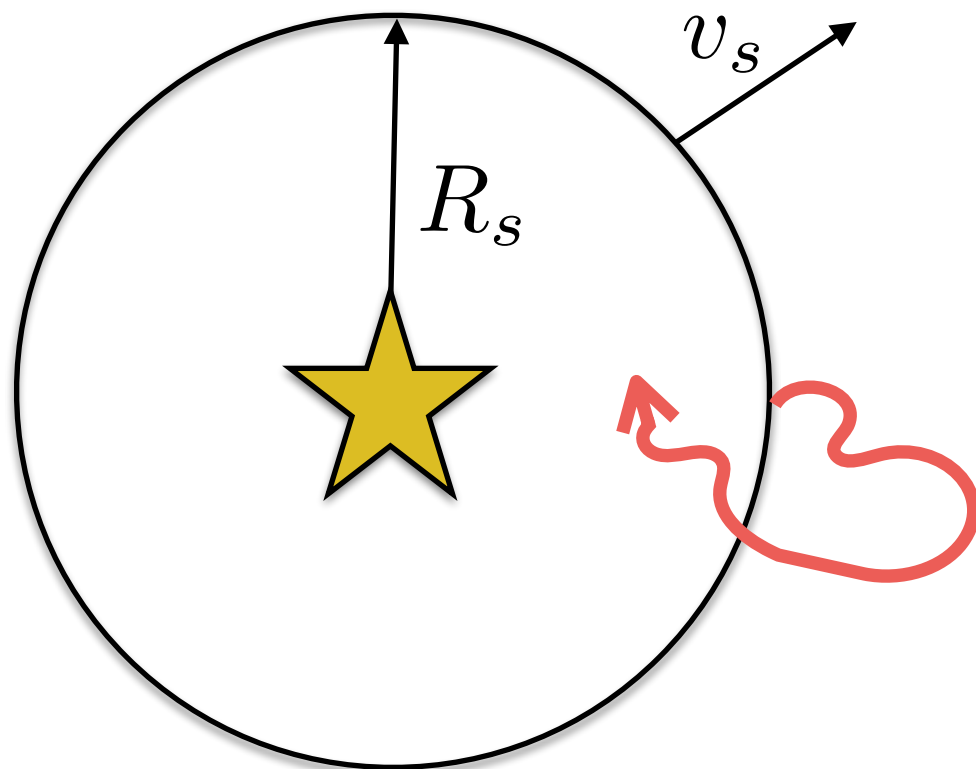
- Later in the evolution, particles diffusion length increases faster than SNR shock size:

$$\lambda_d \simeq D(E_M)/v_s \propto t^{3/5}$$

$$R_s \propto t^{2/5}$$

Particles previously confined will now violate Hillas criterion
→ **escape is expected to occur on shorter timescales for the highest energy particles, but it is not an instantaneous process**

Maximum energy in SNRs



$$t_{\text{acc}} = t_{\text{age}}$$

acceleration
limited by
remnant age

$$\frac{D(p_{\text{max}})}{v_s^2(t)} = t$$

$$\frac{p_{\text{max}}}{B_0 \mathcal{F}(t)} = v_s^2(t) t$$

$$\left(\frac{\delta B(\mathbf{x}, t)}{B_0} \right)^2 = \int \mathcal{F}(k, \mathbf{x}, t) d \ln k$$

$$p_{\text{max},0} \propto \mathcal{F}(t) v_s^2(t) t$$

→ **ED stage:**

$$v_s(t) \simeq \text{const}$$

$$p_{\text{max},0}(t) \propto \mathcal{F}(t) t$$

→ **ST stage:**

$$v_s(t) \simeq t^{-3/5}$$

$$p_{\text{max},0}(t) \propto \mathcal{F}(t) t^{-1/5} \propto t^{-\delta}$$

Maximum energy in SNRs

In the scenario where the maximum momentum of particles confined by the shock is a decreasing function of time, i.e.

$$p_{\max,0}(t) = p_M \left(\frac{t}{t_{\text{Sed}}} \right)^{-\delta} \longrightarrow t_{\text{esc}}(p) = t_{\text{Sed}} \left(\frac{p}{p_M} \right)^{-1/\delta}$$



Ptuskin & Zirakashvili, A&A 429 (2005) 755

$\delta > 0$: high-energy particles escape earlier

- Magnetic field not amplified

$$p_{\max,0}(t) \propto t^{-1/5}$$

- Magnetic field amplification driven by resonant waves

$$p_{\max,0}(t) \propto t^{-7/5}$$

- Magnetic field amplification driven by non-resonant waves

$$p_{\max,0}(t) \propto t^{-2}$$

A model for particle propagation

Solution of the transport equation for accelerated **protons**

$$\frac{\partial f}{\partial t} + \mathbf{v} \cdot \nabla f = \frac{p}{3} \frac{\partial f}{\partial p} \nabla \cdot \mathbf{v} + \nabla \cdot [D \nabla f]$$

**ANALYTICAL DESCRIPTION
WITH A DOWNSTREAM
VELOCITY PROFILE OF:**

$$v(r, t) = \left(1 - \frac{1}{\sigma}\right) \frac{r}{R_s(t)} v_s(t)$$



Celli et al., MNRAS 490 (2019) 3

Particles confined inside the SNR

$$\frac{\partial f_{\text{conf}}}{\partial t} + \mathbf{v} \cdot \nabla f_{\text{conf}} = \frac{p}{3} \frac{\partial f_{\text{conf}}}{\partial p} \nabla \cdot \mathbf{v}$$

$$p \leq p_{\text{max},0}(t)$$

Escaped particles

$$\frac{\partial f_{\text{esc}}}{\partial t} = \nabla \cdot [D \nabla f_{\text{esc}}]$$

$$p > p_{\text{max},0}(t)$$

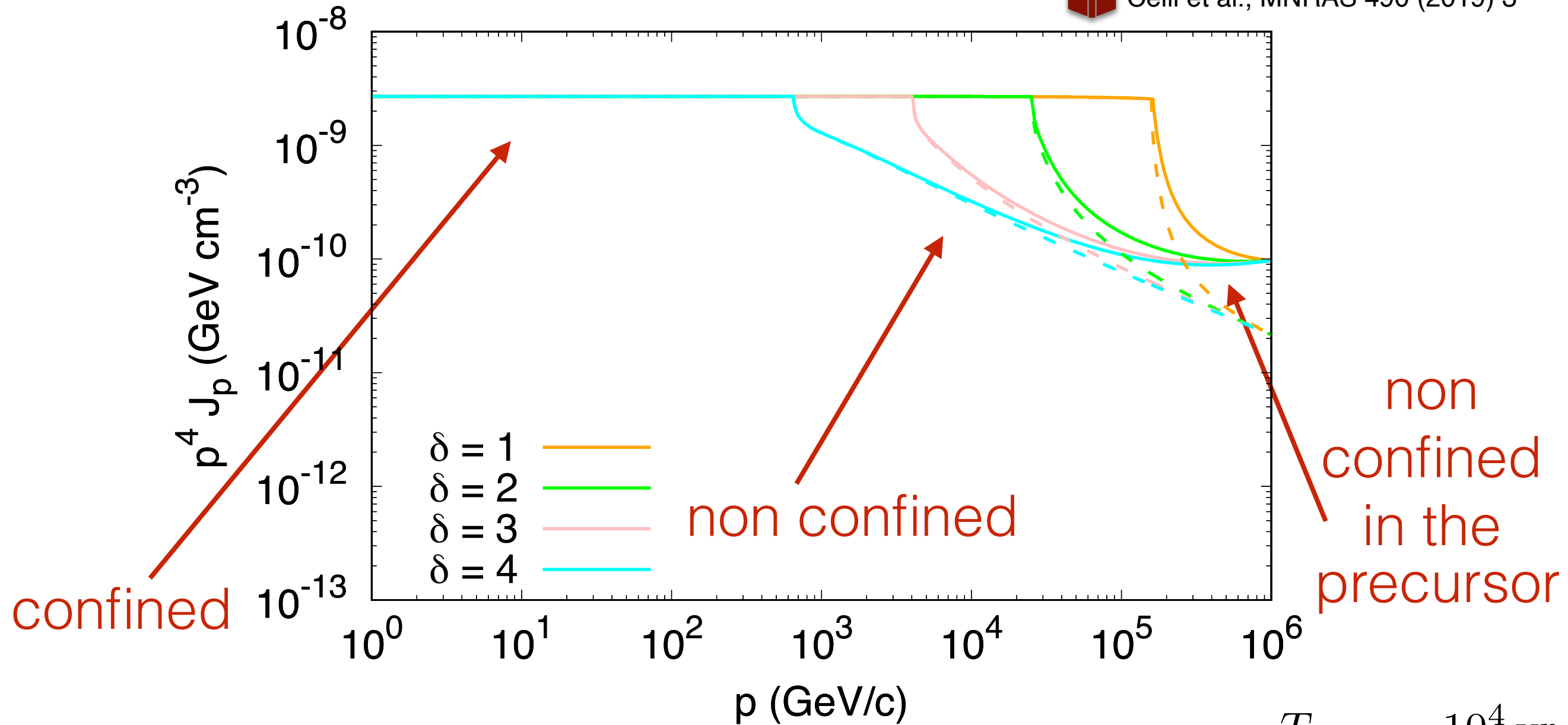
Matching condition: $f_{\text{esc}}(t_{\text{esc}}) = f_{\text{conf}}(t_{\text{esc}})$

The spectrum of protons inside the SNR

$$J_p^{\text{in}}(t, p) = \frac{4\pi}{V_{\text{SNR}}} \int_0^{R_{\text{sh}}(t)} [f_{\text{esc}}(t, r, p) + f_{p,\text{esc}}(t, r, p) + f_{\text{conf}}(t, r, p)] r^2 dr$$



Celli et al., MNRAS 490 (2019) 3



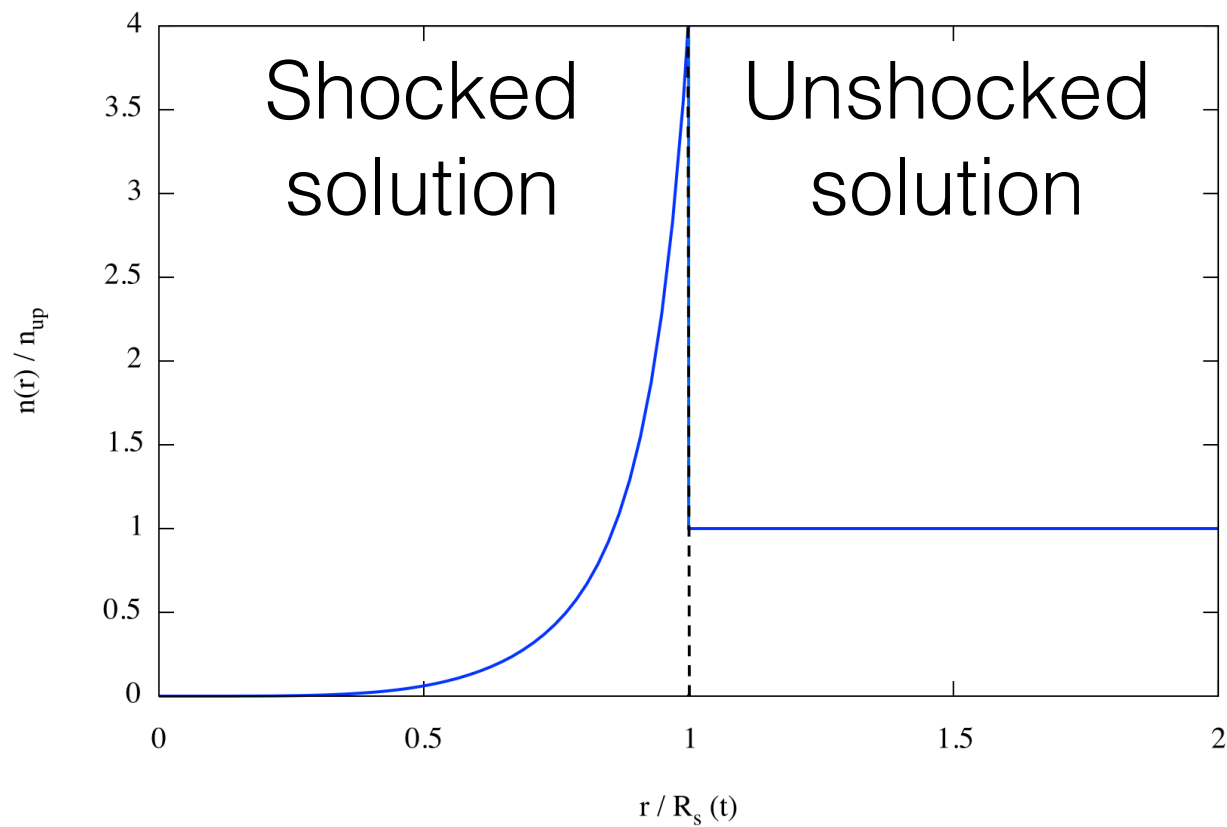
$$D(p) = 10^{27} \left(\frac{pc}{10 \text{ GeV}} \right)^{1/3} \text{ cm}^2 \text{ s}^{-1}$$

$$T_{\text{SNR}} = 10^4 \text{ yr}$$

$$\xi_{\text{CR}} = 10\%$$

$$n_{\text{up}} = 1 \text{ cm}^{-3}$$

Volume integrated gamma-ray emission from hadronic collisions



$$f_0(p) \propto p^{-4}$$

$$D(10 \text{ GeV}/c) = 3 \times 10^{27} \text{ cm}^2/\text{s}$$

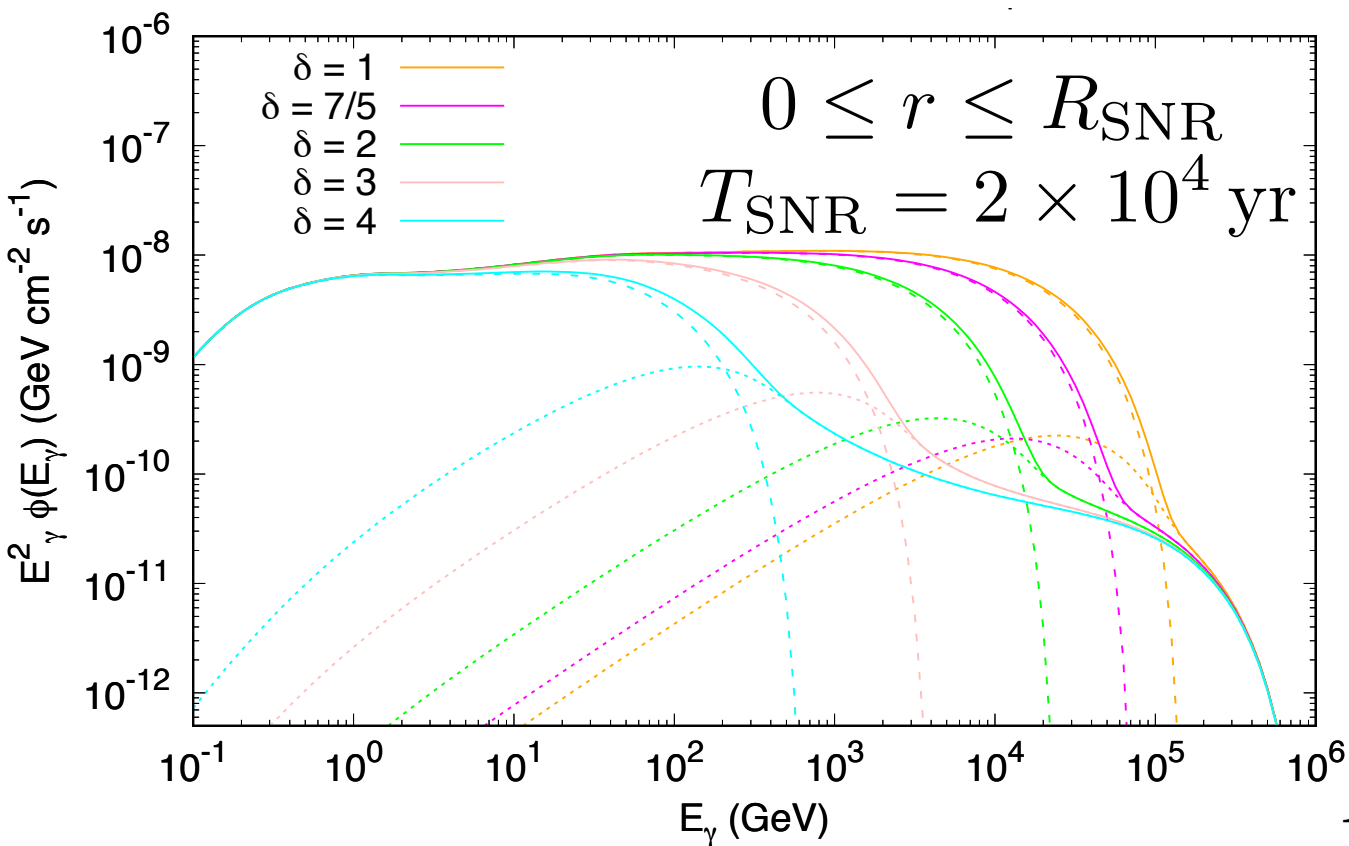
$$\xi_{\text{CR}} = 1 \%$$

$$n_{\text{up}} = 1 \text{ cm}^{-3}$$

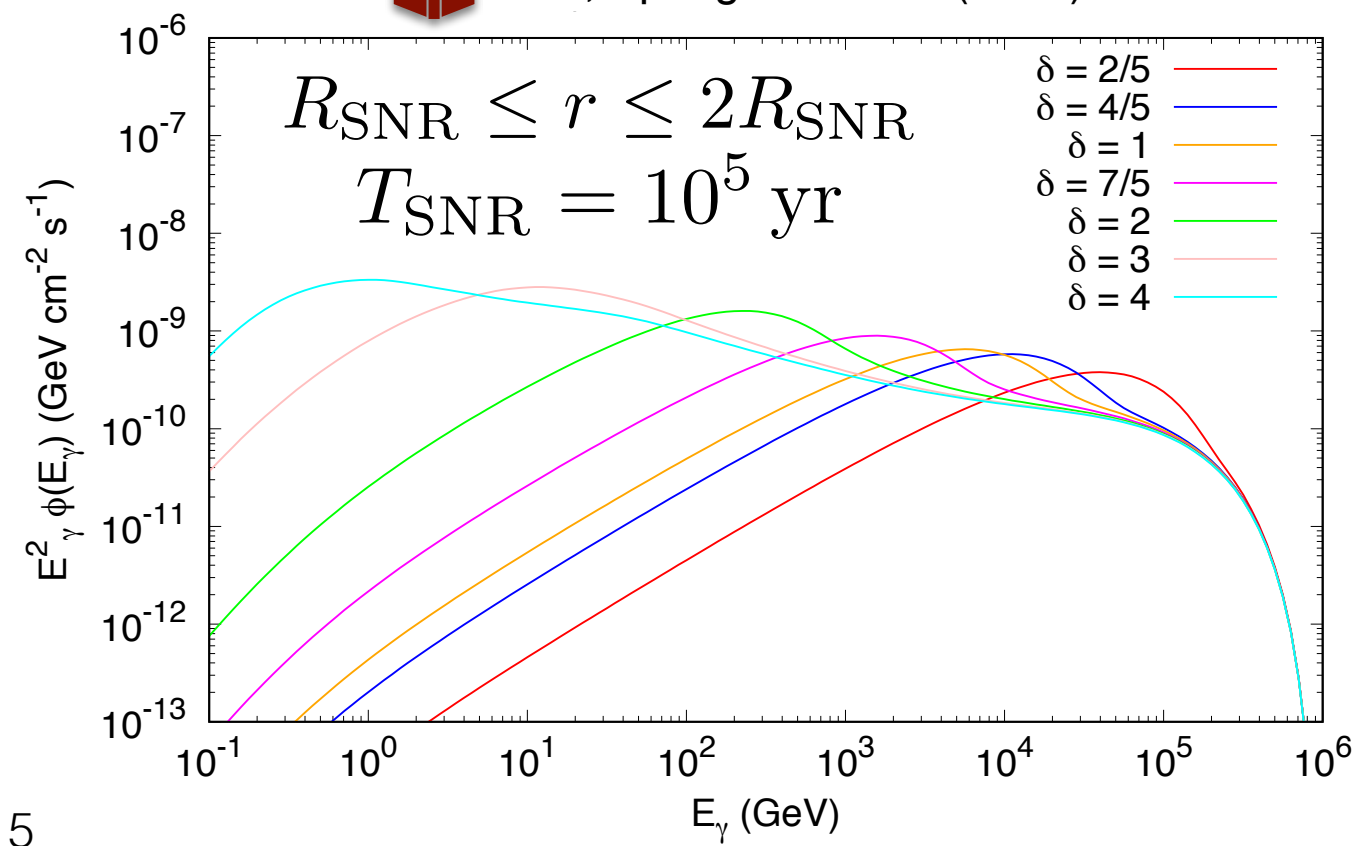
$$d = 1 \text{ kpc}$$



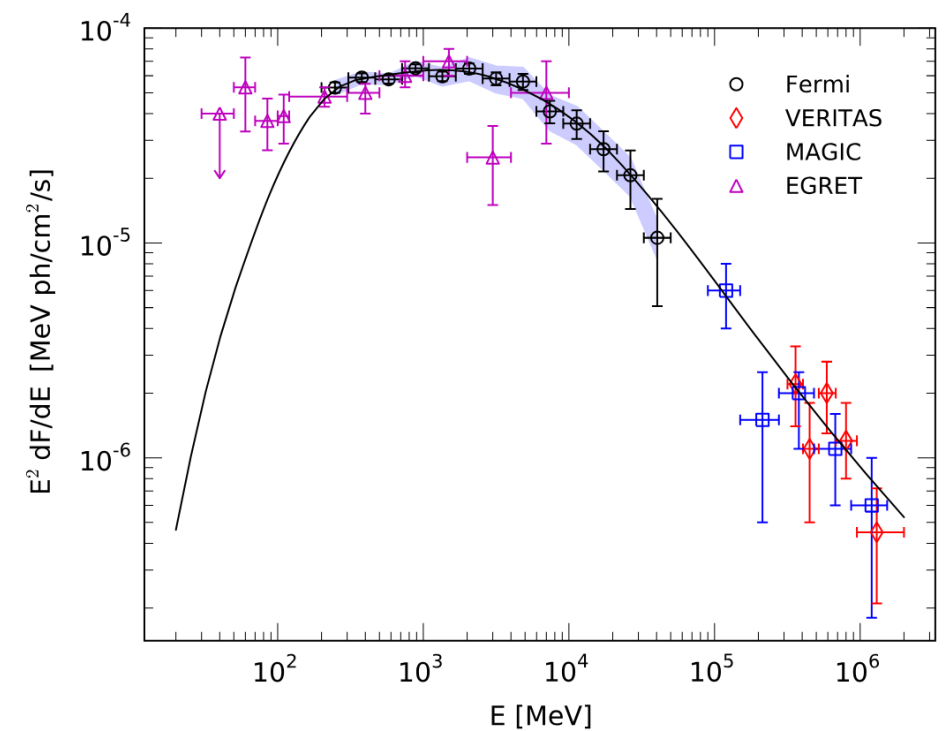
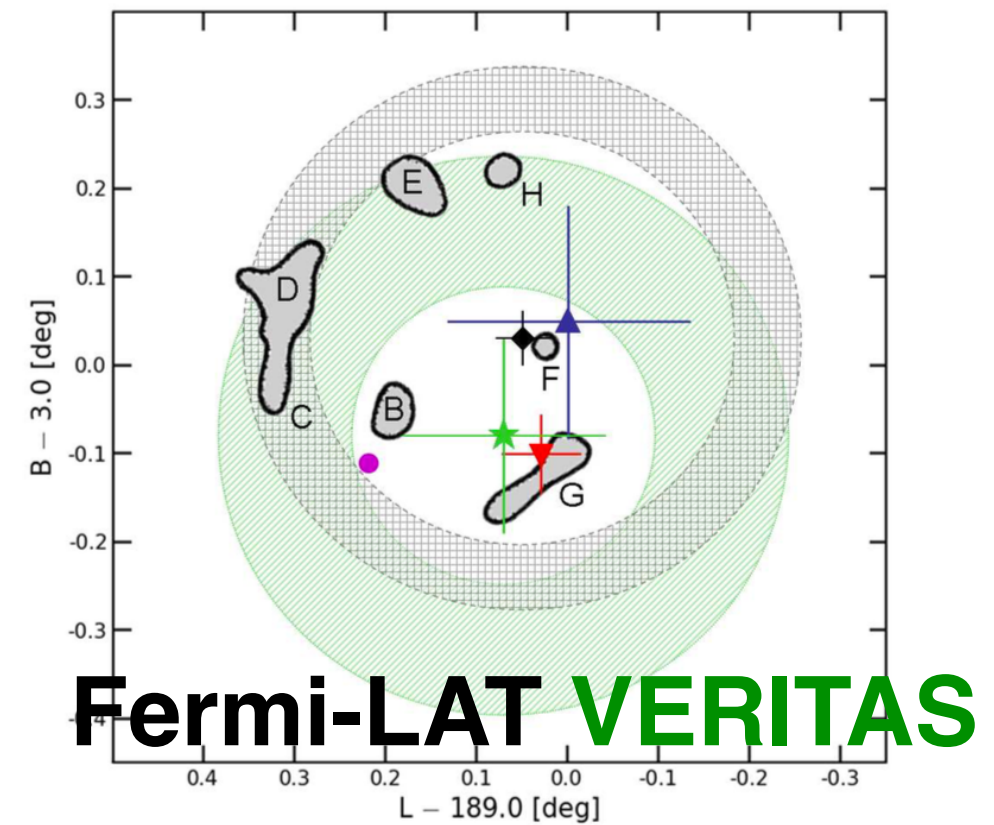
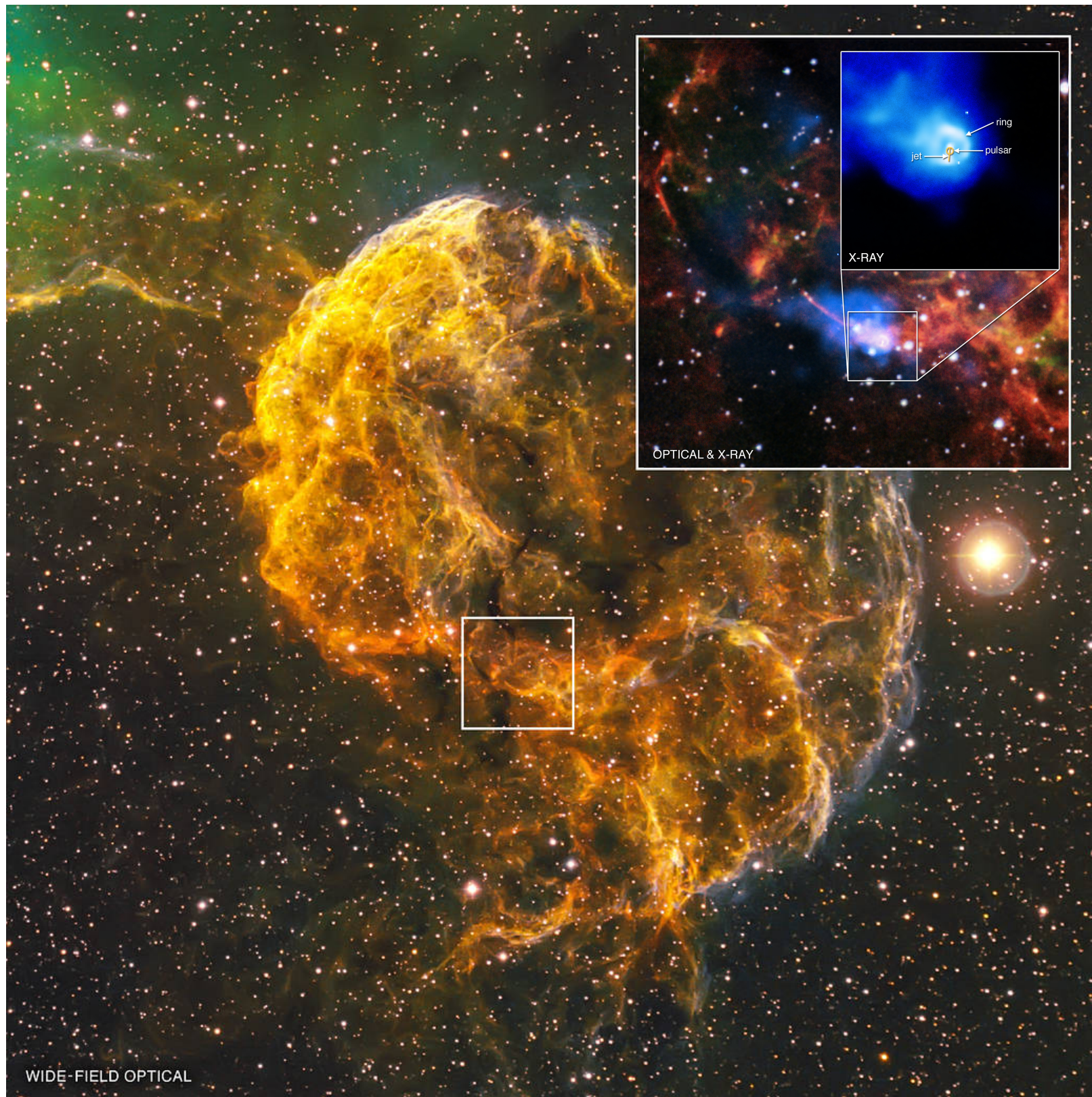
Celli, Springer Theses (2019)



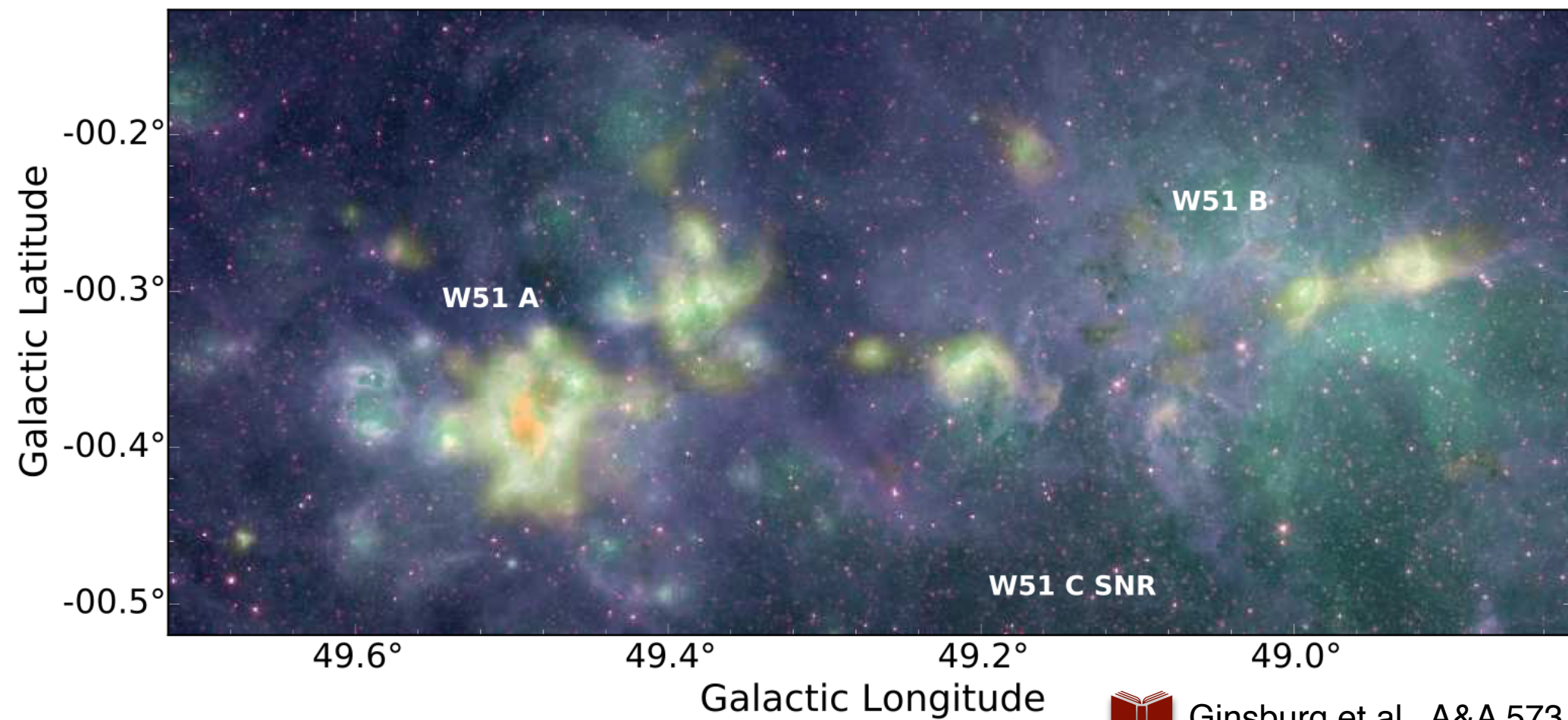
15



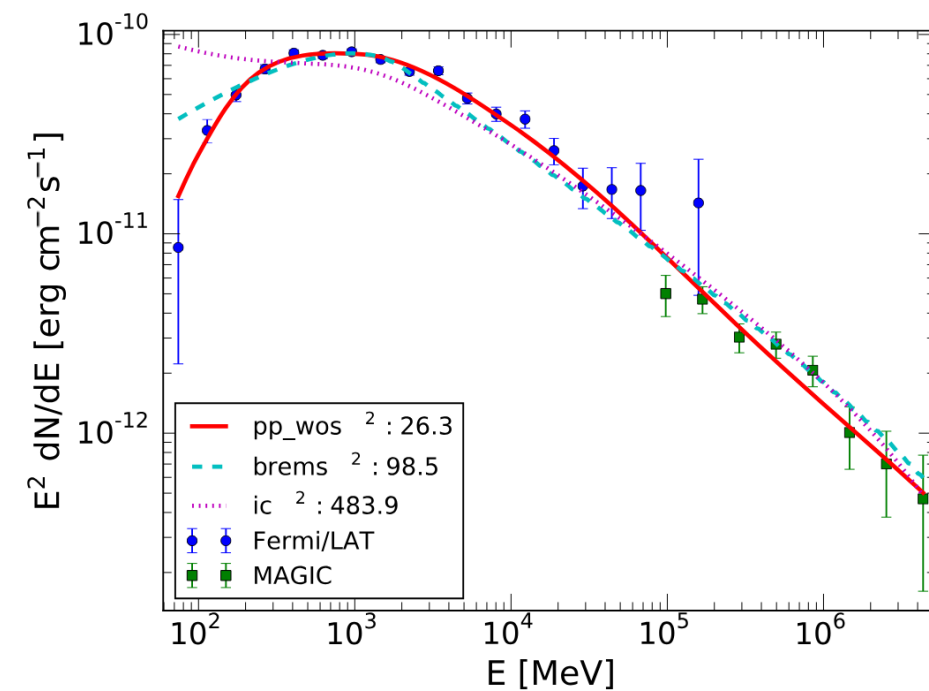
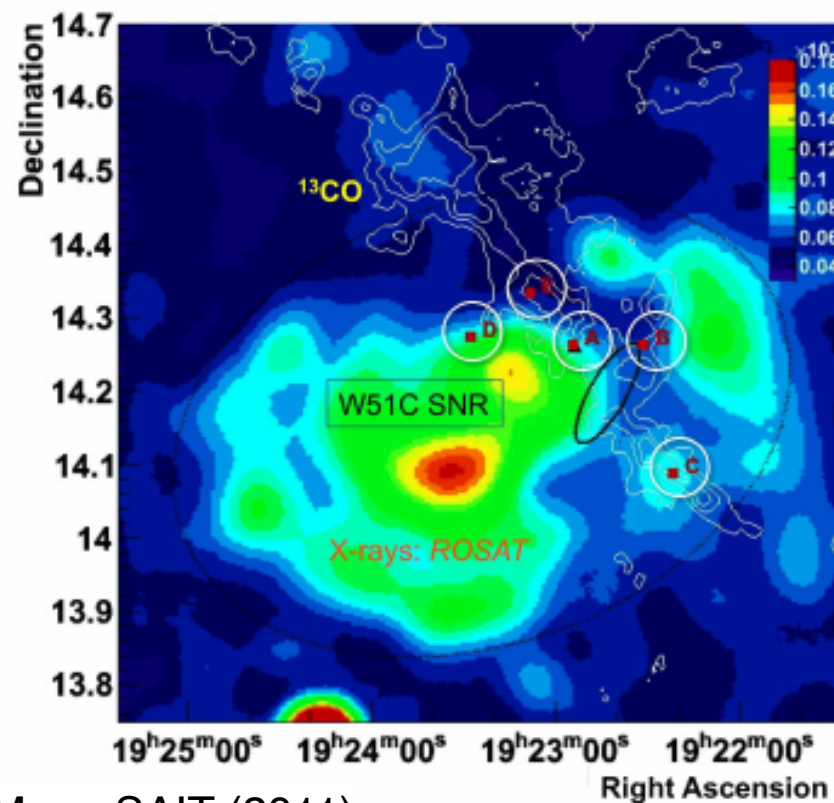
IC 443 or the Jellyfish Nebula



W51C (G49.1-0.1)



Ginsburg et al., A&A 573 (2015) A106



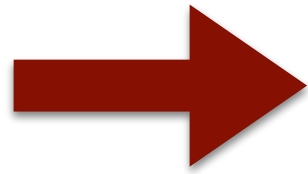
Montmerle, Mem. SAIT (2011)



Jogler & Funk, ApJ 816 (2016) 100

Take-home messages

$$D/D_{\text{Gal}} \leq 0.3$$



Suppression of diffusion coefficient required:

- local turbulence?
- CR-induced turbulence (streaming instability)?



Malkov et al., ApJ 768 (2013) 63

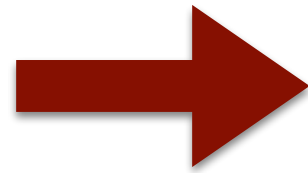


Nava et al., MNRAS 461 (2016) 3552N



D'Angelo et al., MNRAS 474 (2018) 1944D

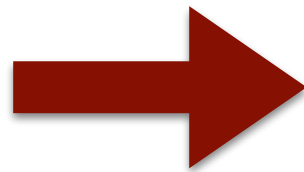
$$\delta \geq 2$$



How does magnetic turbulence evolve with time?

Needs to include damping effects (MHD cascade, ion-neutral friction)

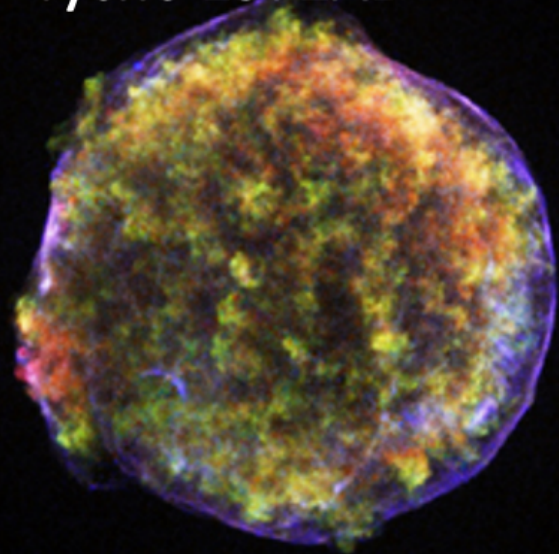
$$p_{\text{M}} < 1 \text{ PeV}/c$$



UHE observations are setting **progressively more stringent constraints** about the role of SNRs as **PeVatron sources**

Thanks for your kind attention!

Tycho 1572AD



Kepler 1604AD



SN1006



Cas A 1680AD

