

A systematic method for determining neutron star parameters from kilohertz quasi-periodic oscillations

**Research Centre for
Computational Physics
and Data Processing**



**Institute of Physics,
Silesian University
in Opava**

Kateřina Klimovičová

Gabriel Török, Gabriela Urbancová, Martin Urbanec, Barbora Bílá, Monika Matuszková



Degeneracy of NS Parameters from HF QPOs

QPO data
and models



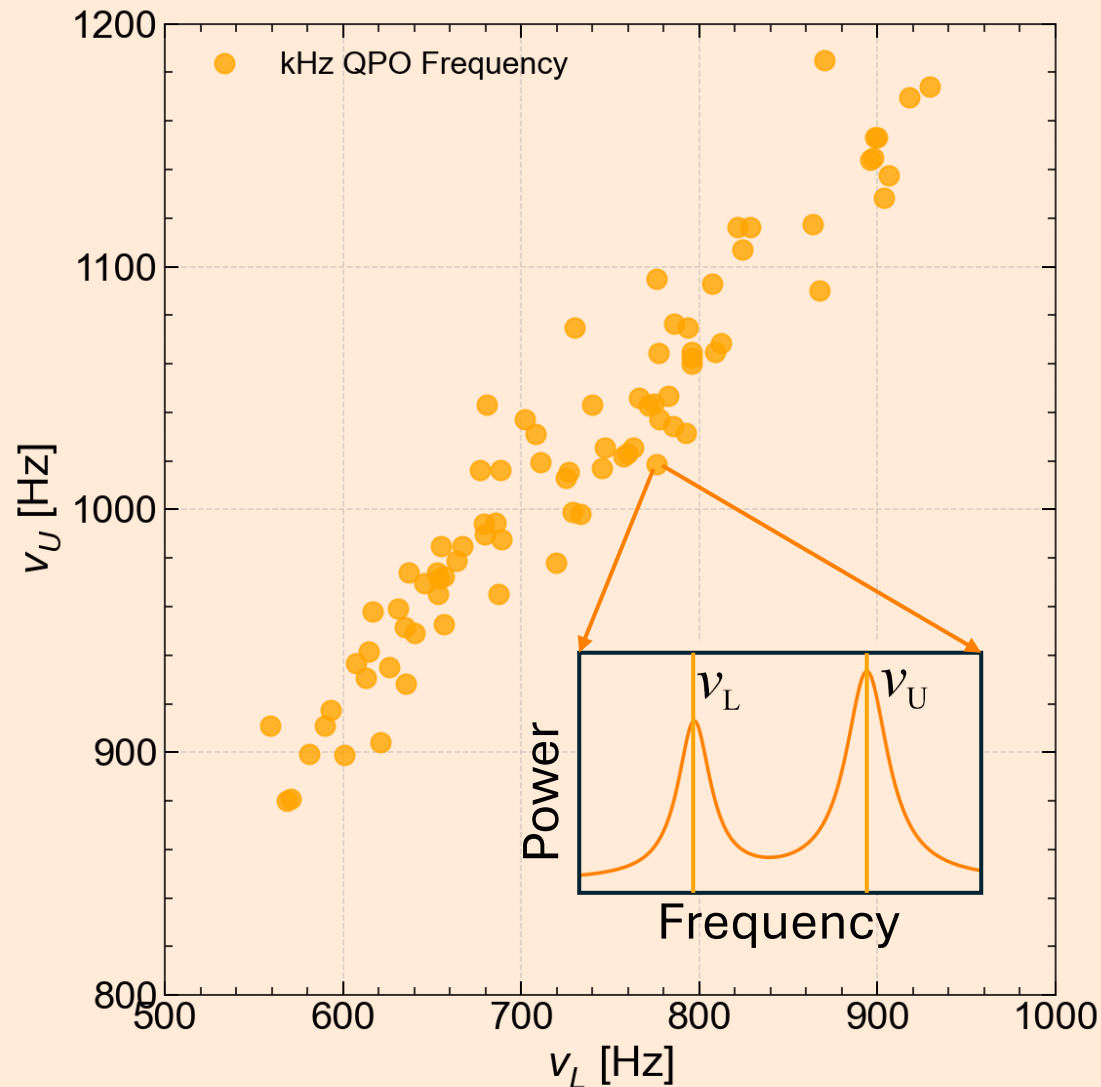
Degeneracy
of NS
Parameters
from
HF QPOs



Limitations
of EOS
Constraints



EOS
Independent
Mass
Estimates



Reference

Ford et al. (1997), van Straaten et al. (2000),
Boutelier et al. (2009), du Buisson et al. (2019),
van Straaten et al. (2003),
van Doesburgh & van der Klis (2017),
Lin et al. (2011), Altamirano et al. (2008),
Barret et al. (2005), Di Salvo et al. (2003),
Jonker et al. (2002), Wijnands et al. (1997),
Barret et al. (2006), Migliari et al. (2003),
van Straaten et al. (2002), Di Salvo et al. (2001),
Mendez & van der Klis (1999), Ford et al. (1998),
Barret et al. (2006), Lin et al. (2011),
Mendez van der Klis (2000),
van der Klis et al. (1996), Wijnands et al. (1997) ...



Degeneracy of NS Parameters from HF QPOs

QPO data
and models



Degeneracy
of NS
Parameters
from
HF QPOs

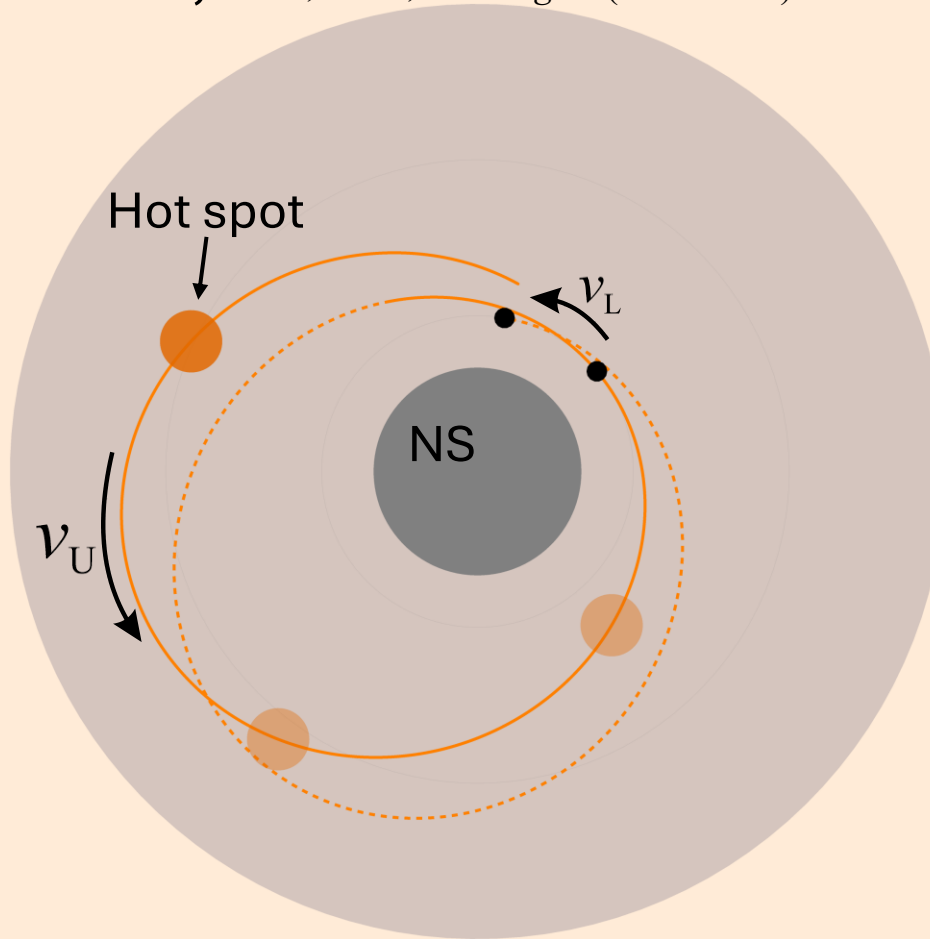


Limitations
of EOS
Constraints



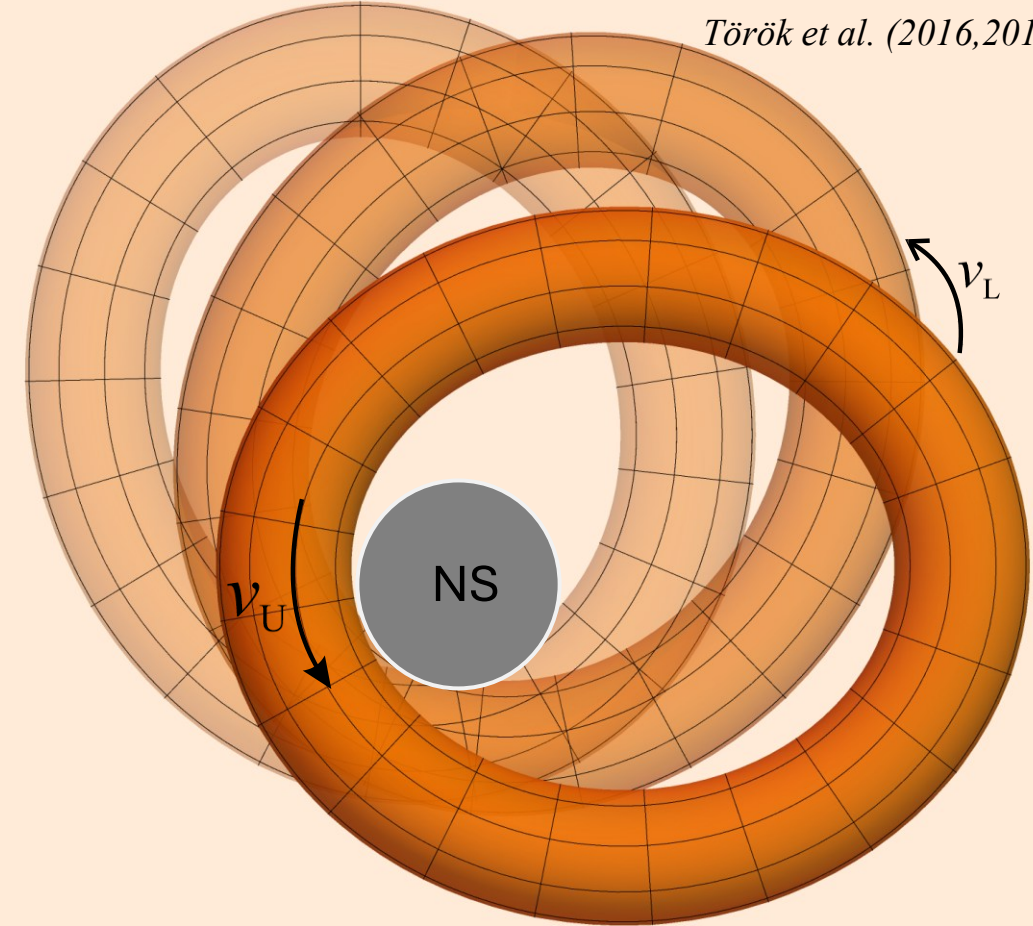
EOS
Independent
Mass
Estimates

RP model, *Stella, Vietri, Morsing ... (1998-2000)*



$\nu_L (M, j, \tilde{q})$ = Orbital frequency of the hot spot
 $\nu_U (M, j, \tilde{q})$ = Periastron frequency

CT model, *Straub & Šrámková (2009), Fragile et al. (2016),
Török et al. (2016,2018)*



$\nu_L (M, j, \tilde{q})$ = Central orbital frequency
 $\nu_U (M, j, \tilde{q})$ = Radial oscillation frequency



Degeneracy of NS Parameters from HF QPOs

QPO data
and models



Degeneracy
of NS
Parameters
from
HF QPOs

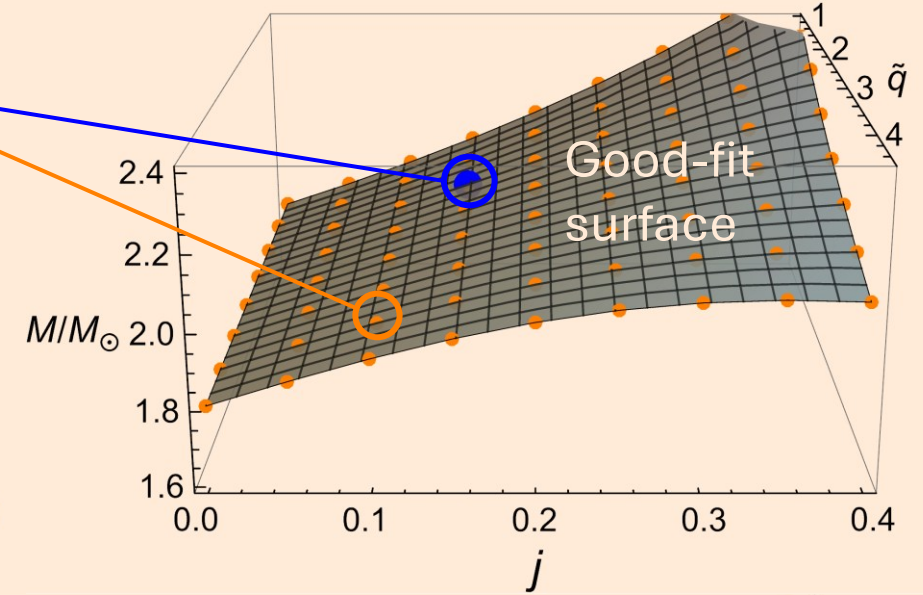
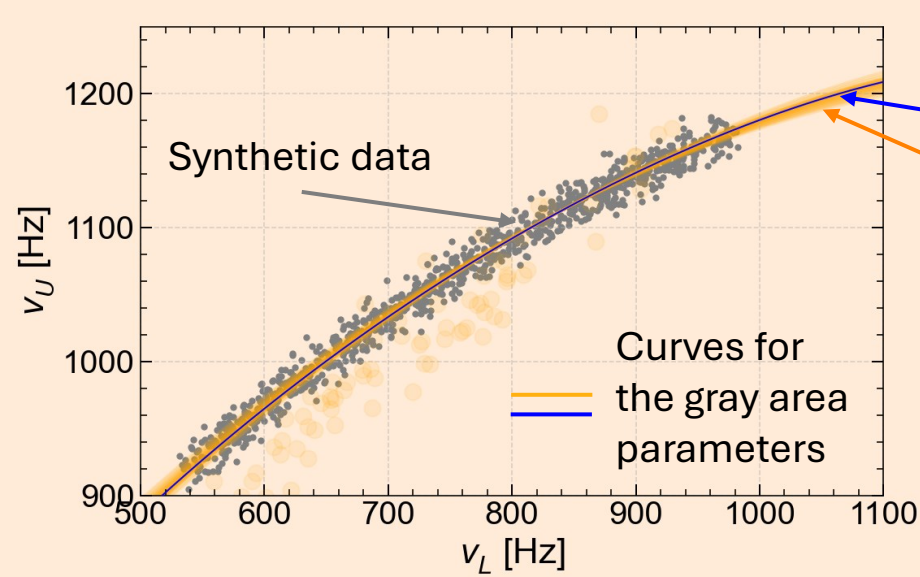


Limitations
of EOS
Constraints

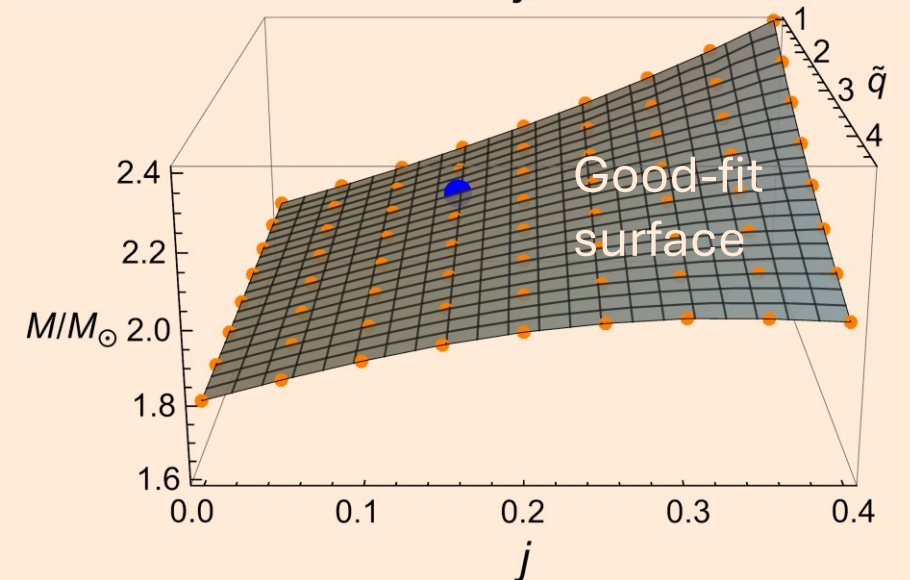
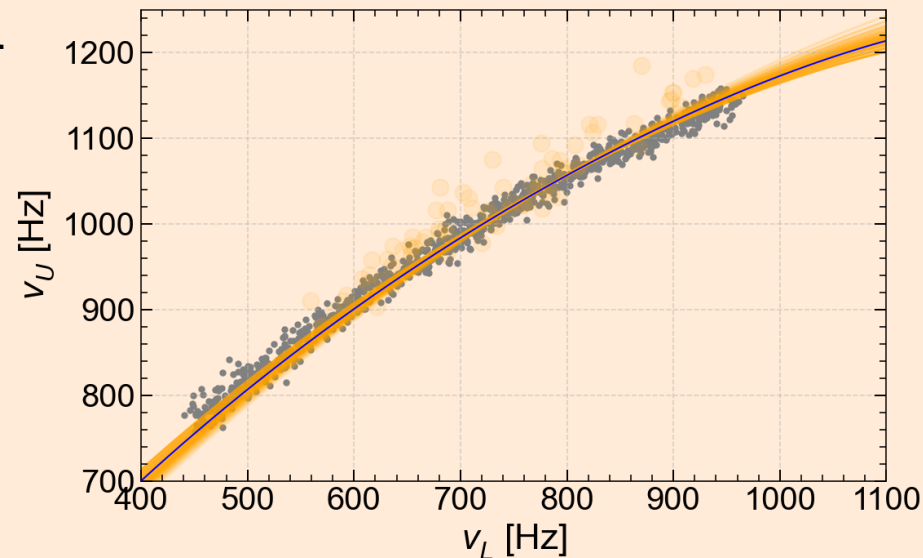


EOS
Independent
Mass
Estimates

RP model



CT model





Limitations of EOS Constraints

QPO data
and models



Degeneracy
of NS
Parameters
from
HF QPOs



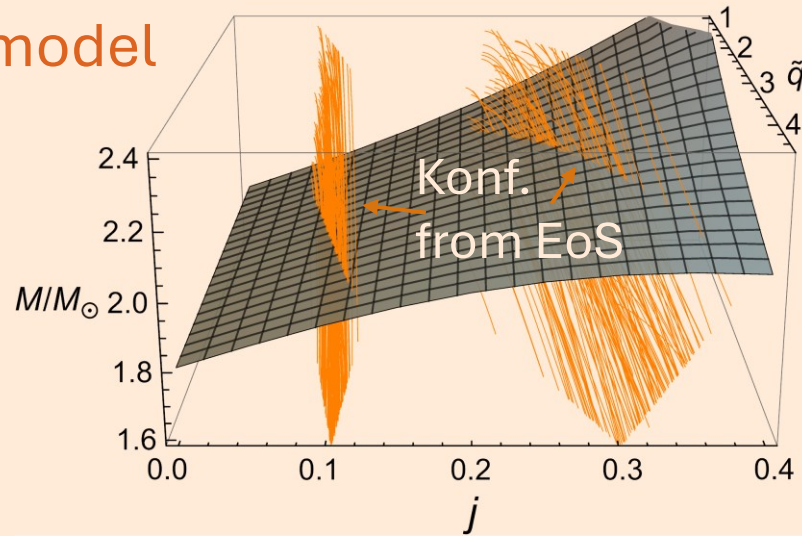
Limitations
of EOS
Constraints



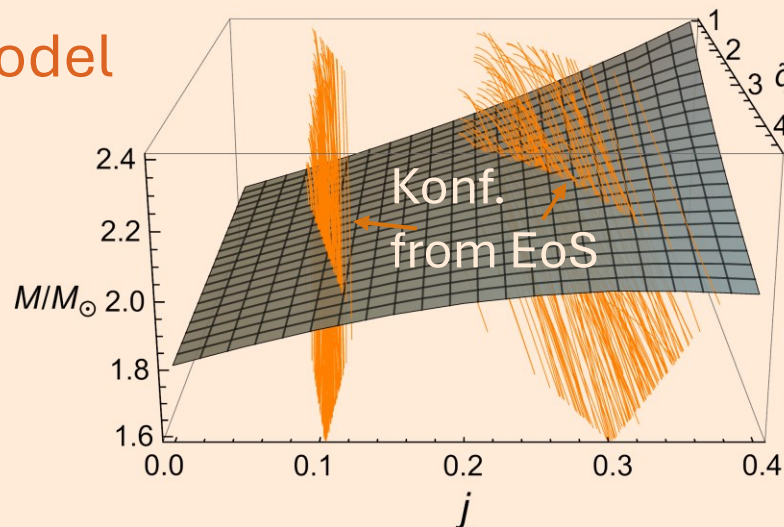
EOS
Independent
Mass
Estimates

Synthetic data

RP model



CT model



Neutron star parameters

Theory: M (NS Mass), j (NS spin),
 q (Quadrupole momentum)

Observations: M_0 , (Non rotating mass),
 f (Rot. freq., Hz), R (NS Radius)

The conversion depends on the choice of the EoS.

Universal relations

(Yagi & Yunes, 2013; Maselli et al. 2013; Urbanec et al. 2013)

$$M = M(M_0, R, f)$$

$$j = j(M_0, R, f)$$

$$q = q(R)$$

For given rot. freq. (in Hz), the NS parameters
lie on one specific surface in $M \times j \times q$ space.



Limitations of EOS Constraints

QPO data
and models



Degeneracy
of NS
Parameters
from
HF QPOs



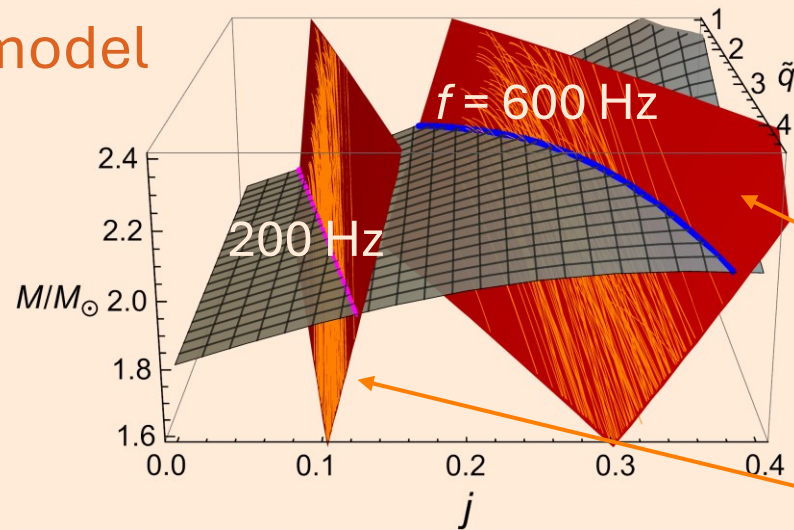
Limitations
of EOS
Constraints



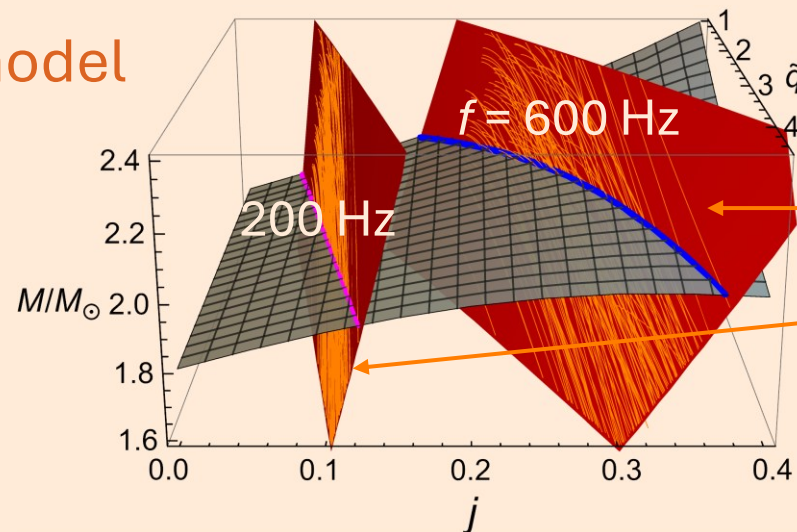
EOS
Independent
Mass
Estimates

Synthetic data

RP model



CT model



Neutron star parameters

Theory: M (NS Mass), j (NS spin),
 $\tilde{q}$ (Quadrupole momentum)

Observations: M_0 , (Non rotating mass),
 f (Rot. freq., Hz), R (NS Radius)

The conversion depends on the choice of the EoS.

Universal relations

(Yagi & Yunes, 2013; Maselli et al. 2013; Urbanec et al. 2013)

$$M = M(M_0, R, f)$$

$$j = j(M_0, R, f)$$

$$q = q(R)$$

=>

$$M = M(M_0, R)$$

$$j = j(M_0, R)$$

$$q = q(R)$$

For given rot. freq. (in Hz), the NS parameters
lie on one specific surface in $M \times j \times \tilde{q}$ space.



EoS independent mass estimates

QPO data
and models



Degeneracy
of NS
Parameters
from
HF QPOs



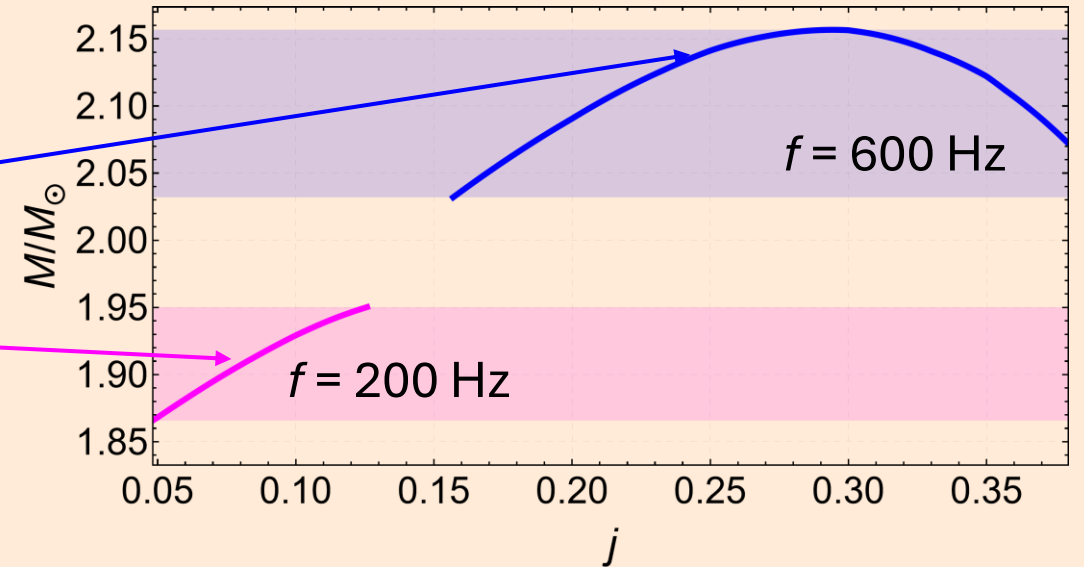
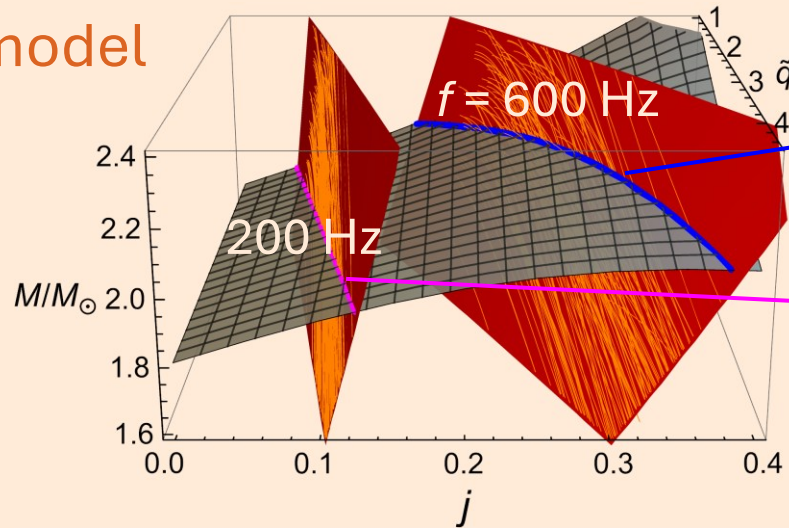
Limitations
of EOS
Constraints



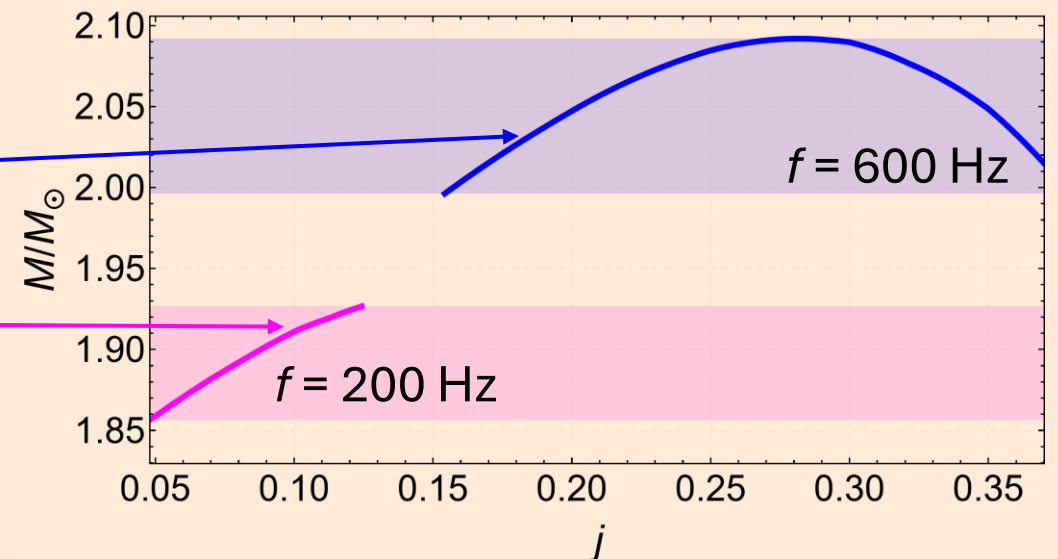
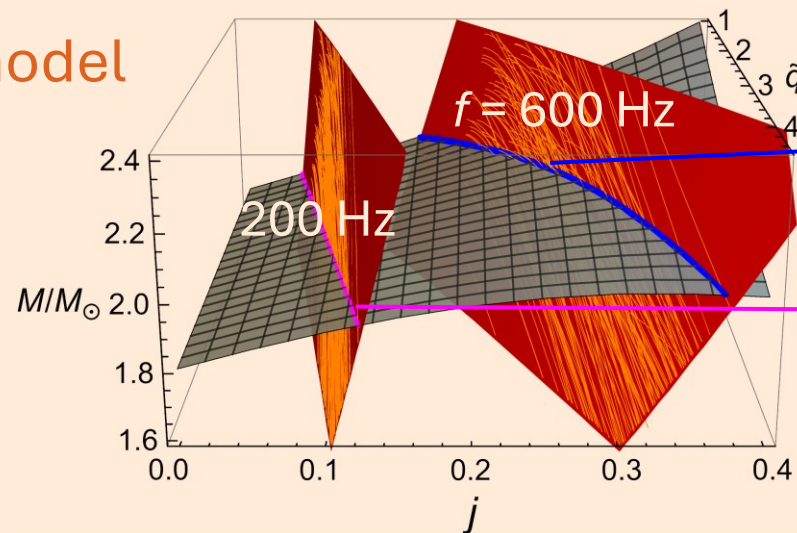
EOS
Independent
Mass
Estimates

Synthetic data

RP model



CT model





EoS independent mass estimates

QPO data
and models



Degeneracy
of NS
Parameters
from
HF QPOs



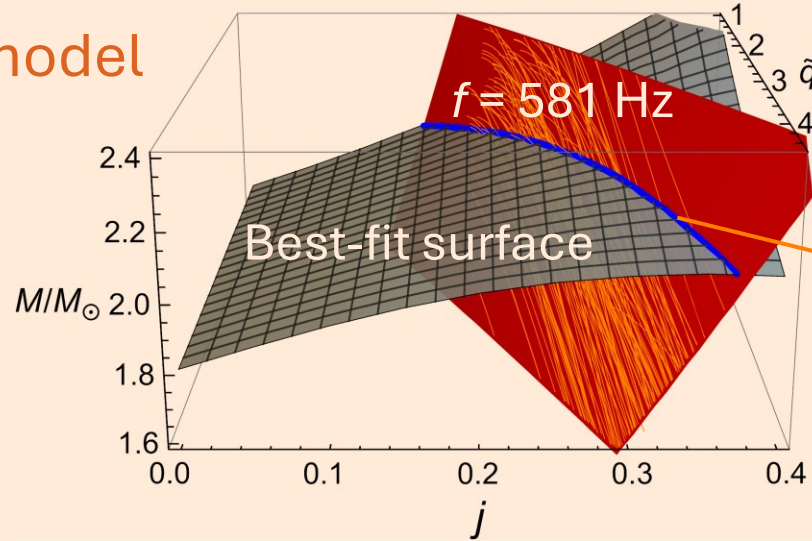
Limitations
of EOS
Constraints



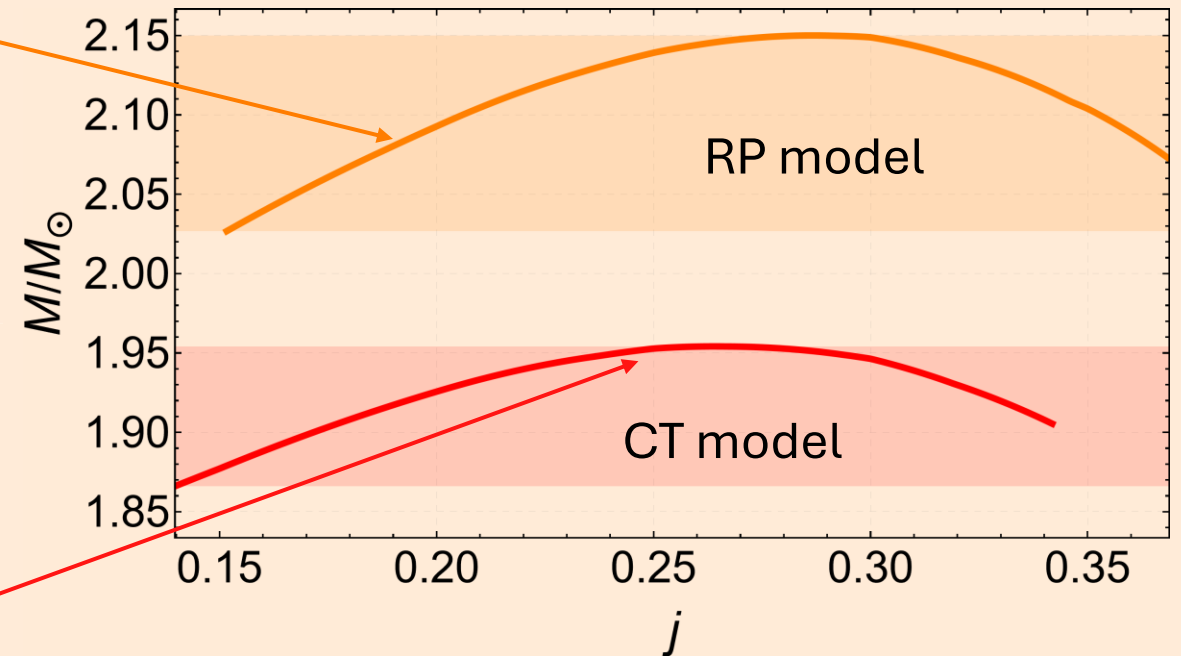
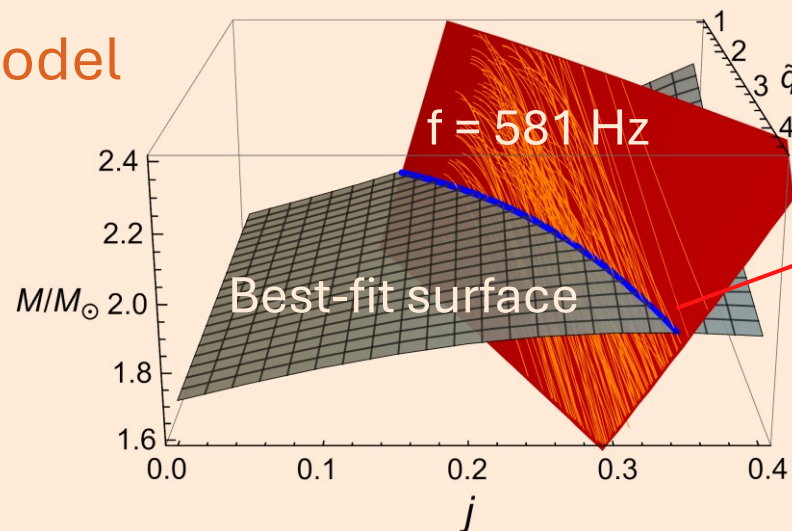
EOS
Independent
Mass
Estimates

4U 1636–53, real data

RP model



CT model





EoS independent mass estimates

QPO data
and models



Degeneracy
of NS
Parameters
from
HF QPOs



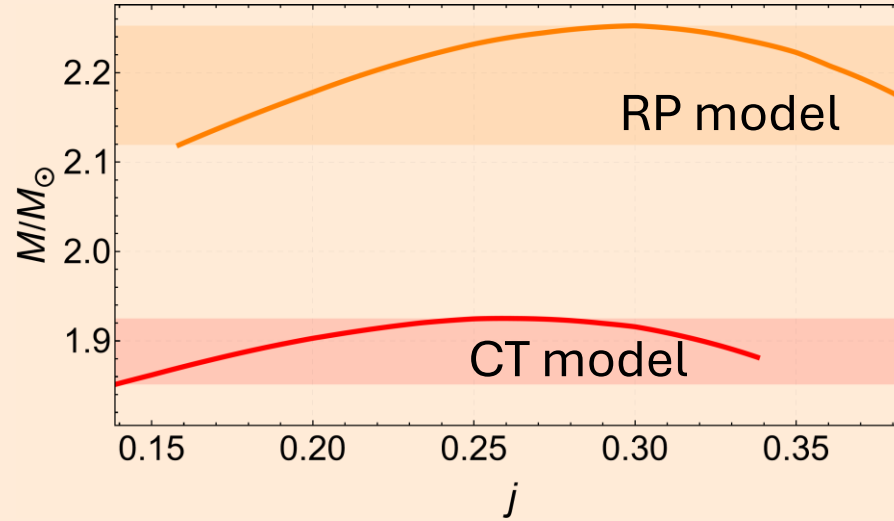
Limitations
of EOS
Constraints



**EoS
Independent
Mass
Estimates**

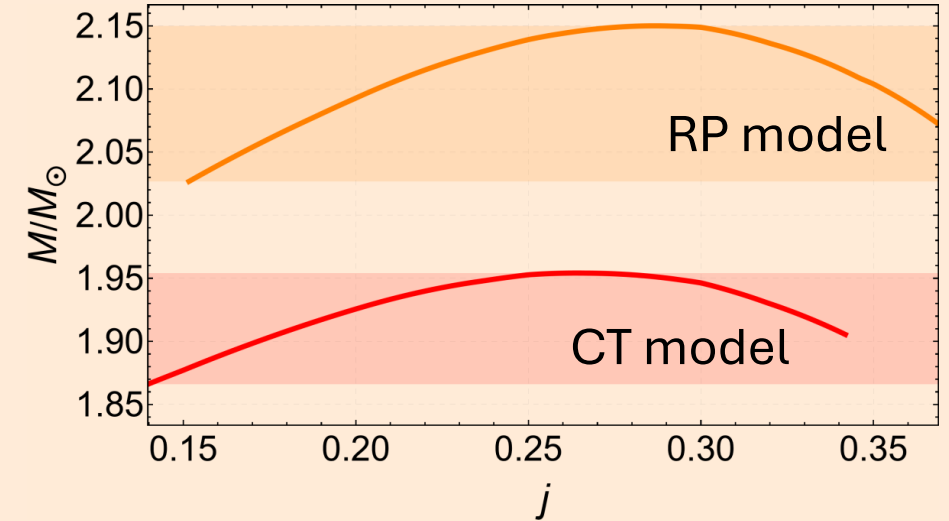
4U 0614+09

$f = 415$ Hz



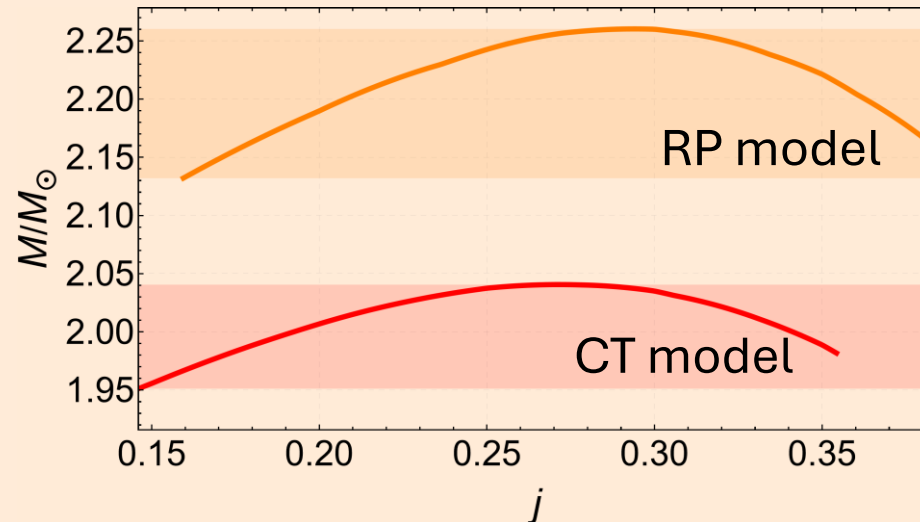
4U 1636-53

$f = 581$ Hz



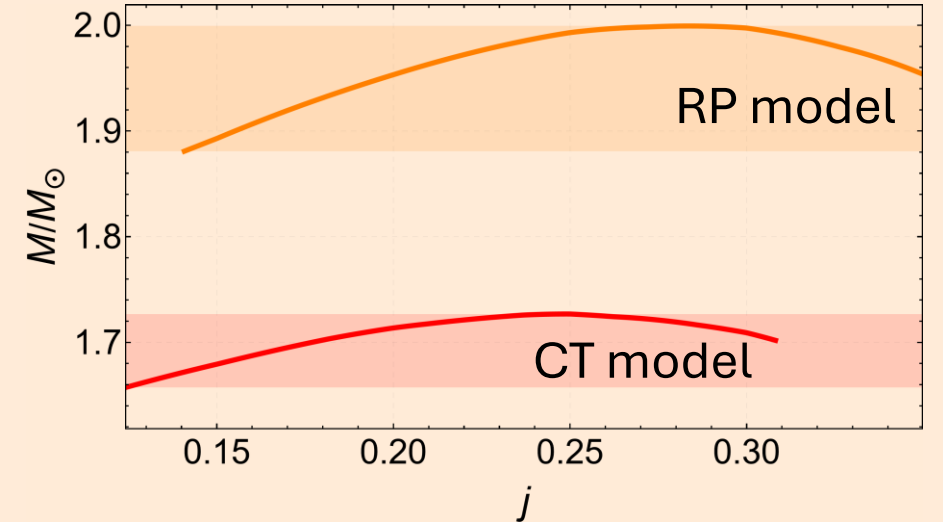
4U 1608-52

$f = 620$ Hz



4U 1728-34

$f = 363$ Hz



Thank you for your attention

