

# Accreting Millisecond X-ray Pulsars: Insights into accretion and spin evolution

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***The many tones of accretion***

to the memory of **Tomaso Belloni**

7-11 September 2026  
Cefalù, Italy



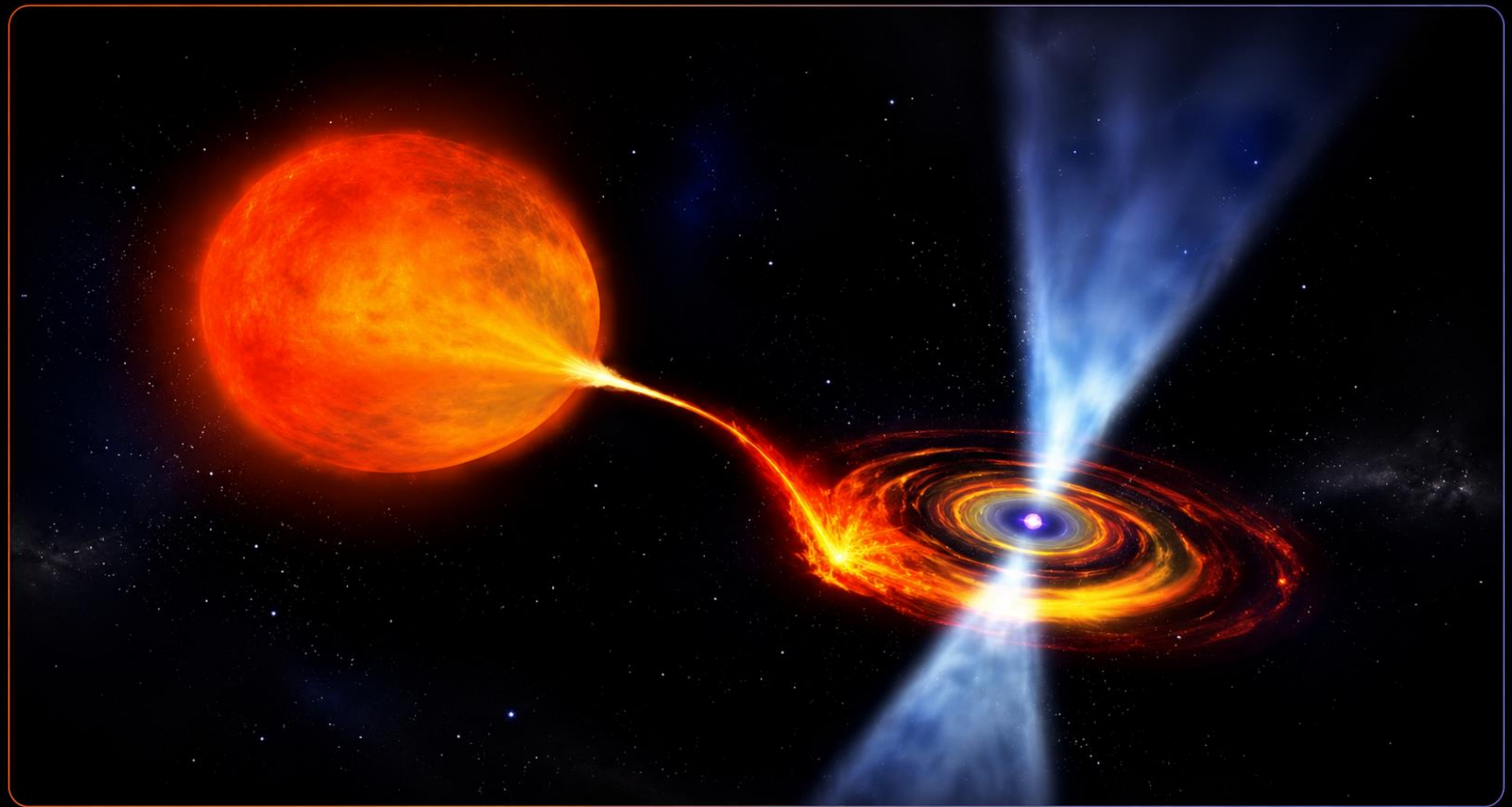
The many tones of accretion - Cefalù – September 8, 2026

# Tomaso

*A colleague, a mentor, and a constant presence in our community.*

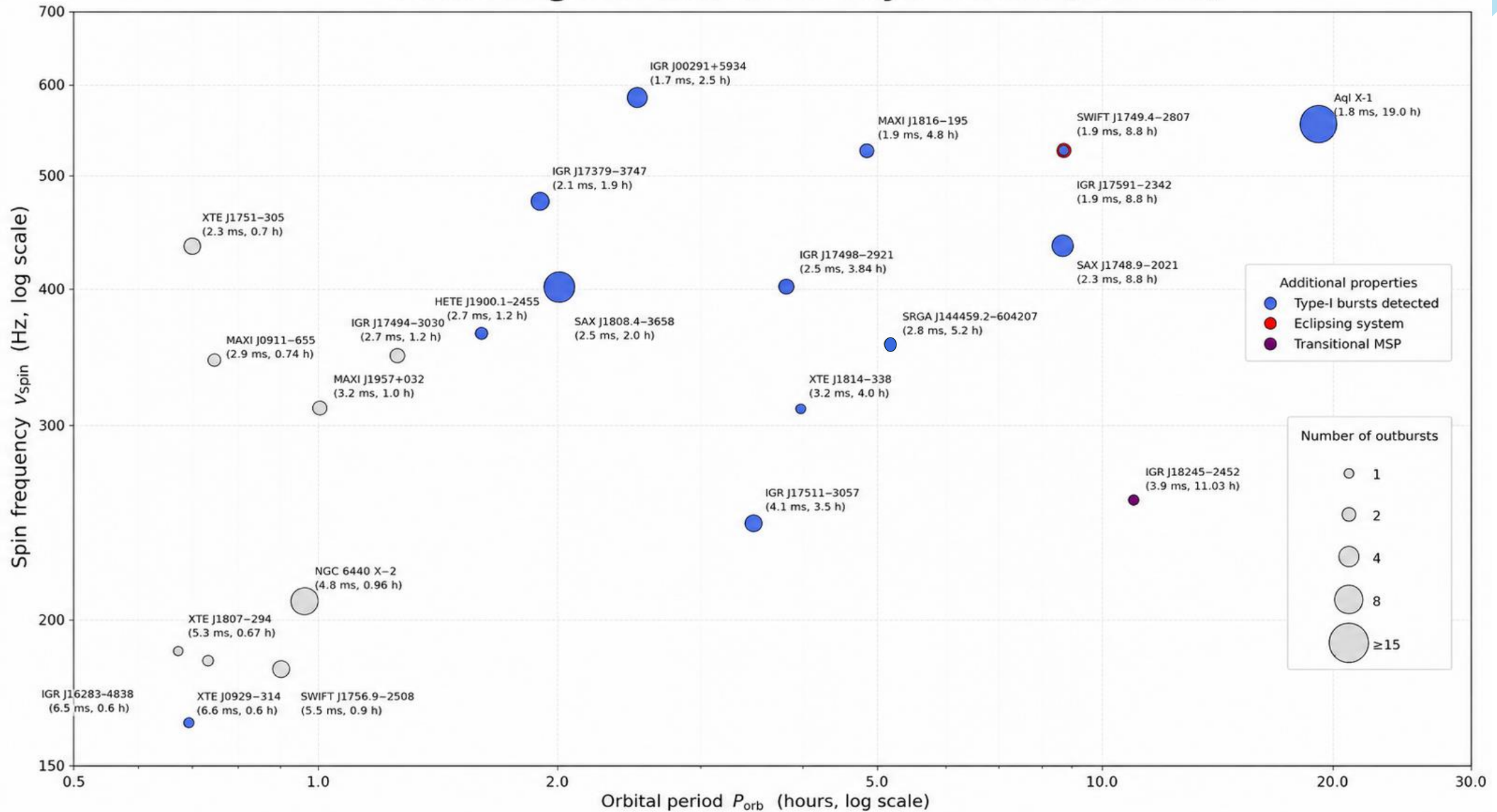




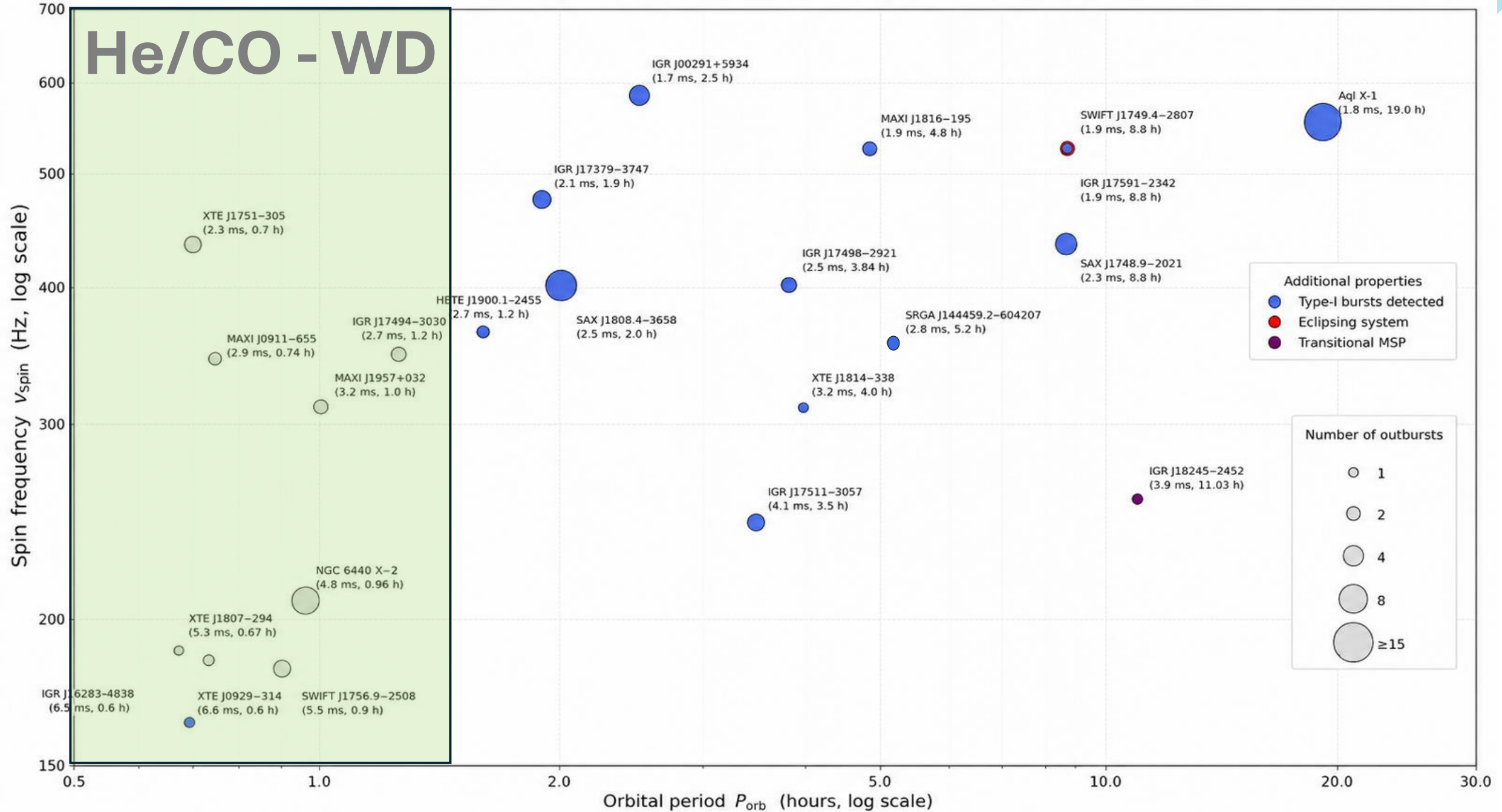


Accreting millisecond X-ray pulsars

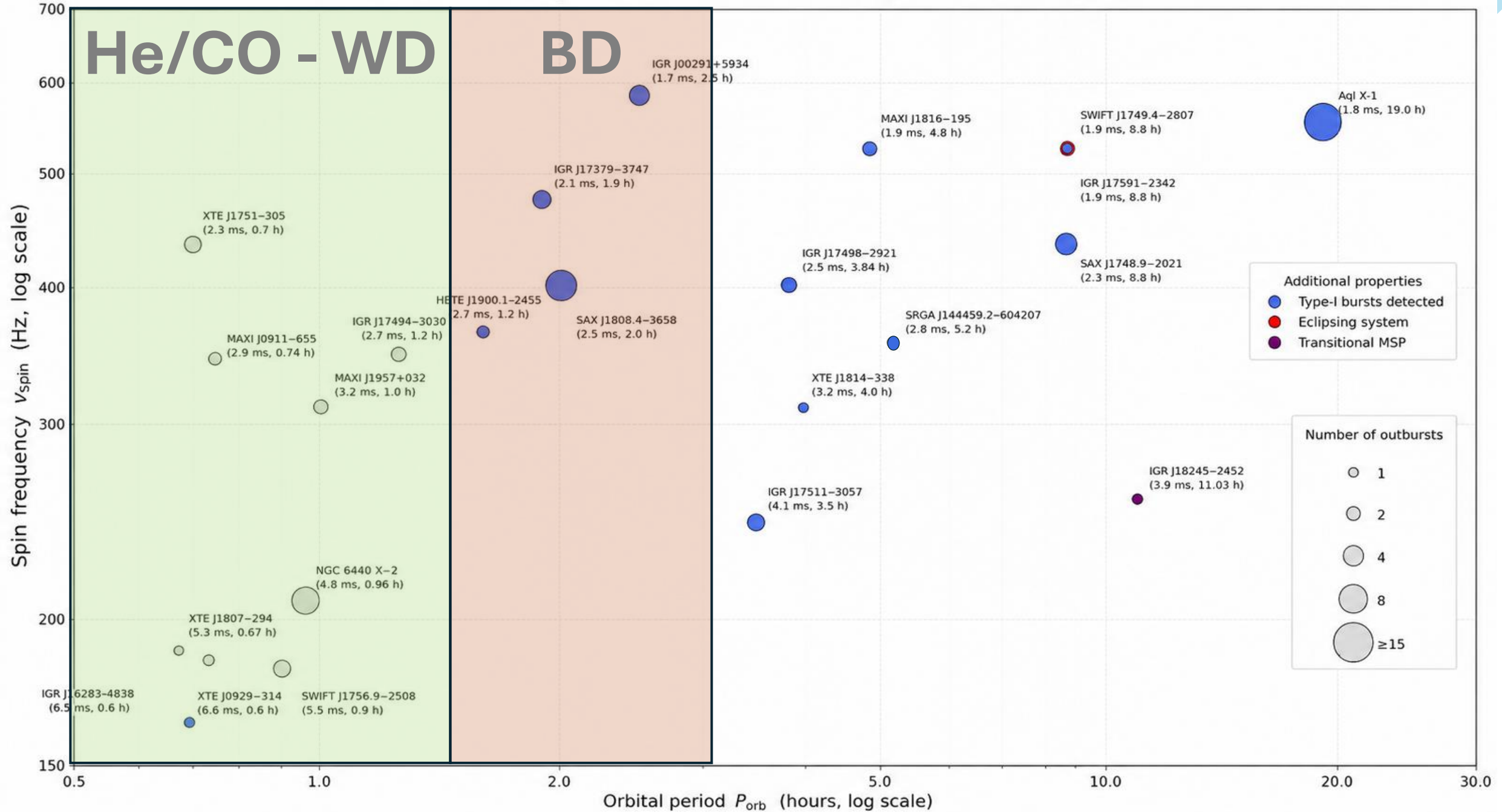
# Accreting Millisecond X-ray Pulsars (AMXPs)



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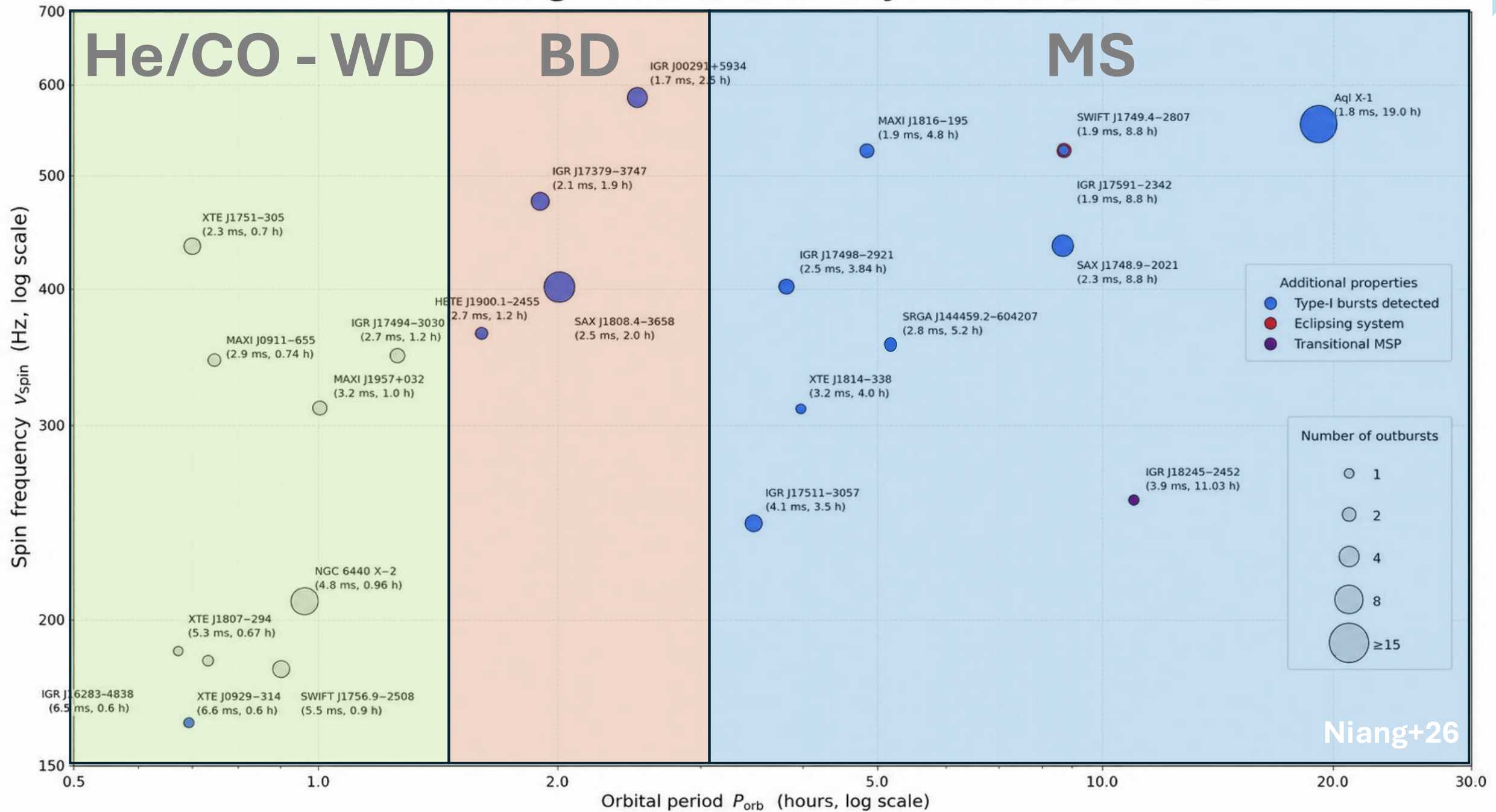


# Accreting Millisecond X-ray Pulsars (AMXPs)





# Accreting Millisecond X-ray Pulsars (AMXPs)



Niang+26

# What timing reveals in AMXPs



## 1. Measure neutron-star spin evolution

Track pulse arrival times to follow the spin of the neutron star.



## 2. Track pulse-profile variability and hotspot geometry

Understand changes in the emitting regions and their visibility.



## 3. Probe accretion torques and magnetosphere-disk coupling

Constrain how matter and magnetic fields exchange angular momentum.

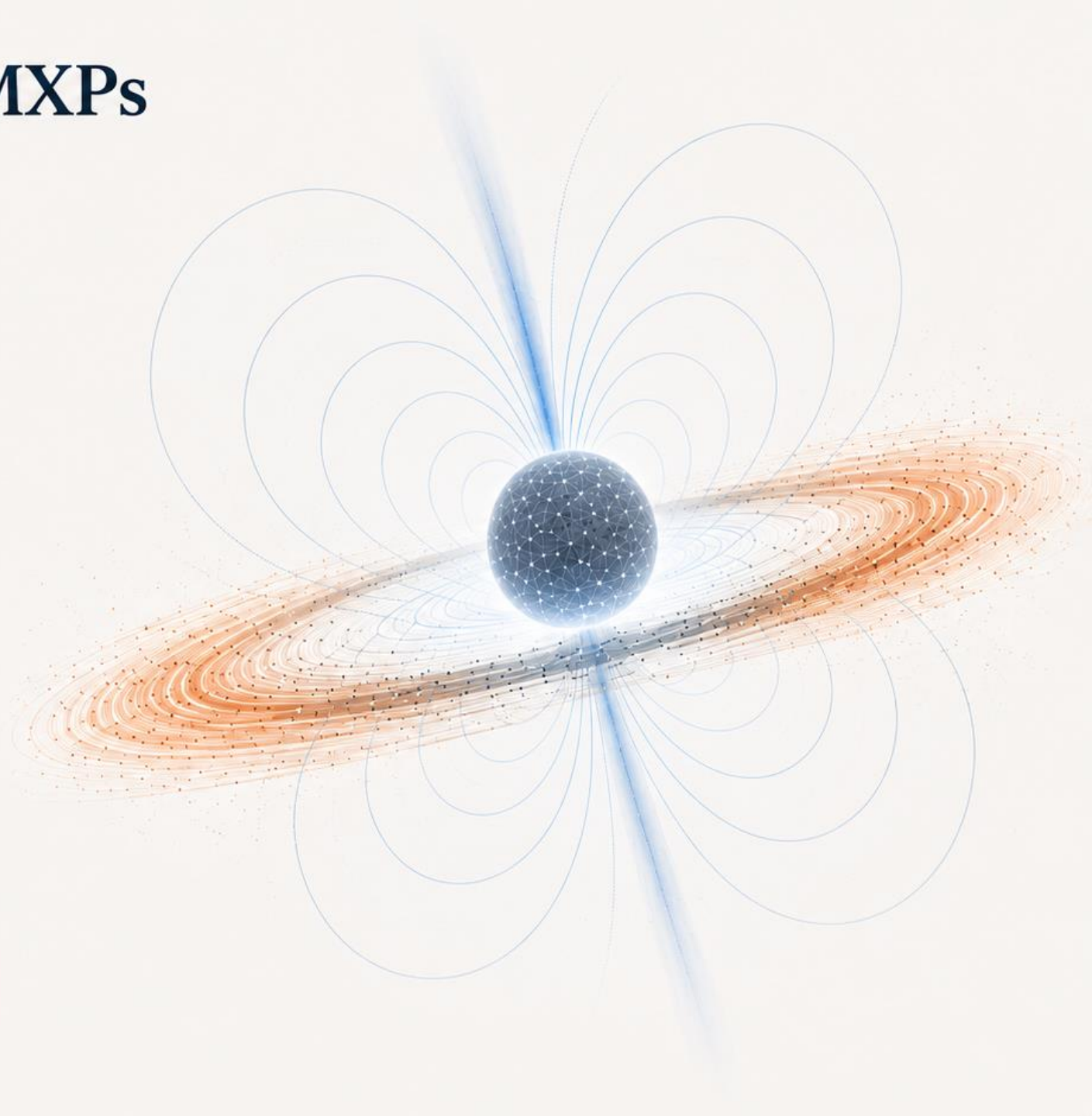


## 4. Trace secular orbital evolution

Measure long-term changes in orbital period driven by mass transfer, angular momentum losses, and companion evolution.



*Pulse phases are **not** always a clean tracer of neutron-star rotation.*





# Pulse phase $\neq$ pure spin phase

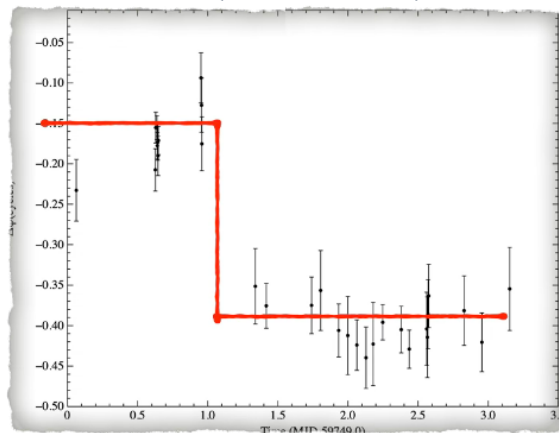
*Phase behavior reveals more than neutron-star rotation*

## MAXI J1957+032:

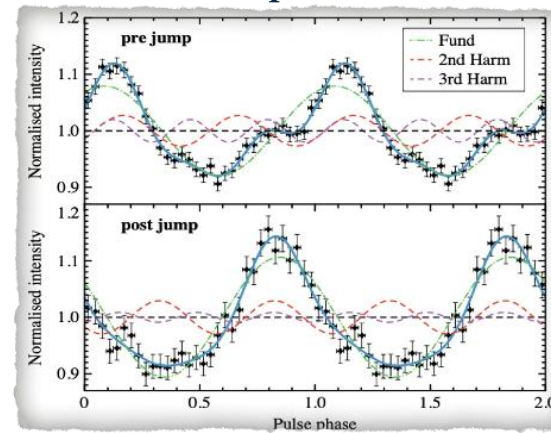
### Pulse phase jumps

- Pulse profiles with high harmonic content
- No clear correlation between phase jumps and X-ray count rate
- Significant variation of the amplitude of harmonic components with time

Phase (fundamental)



Pulse profiles



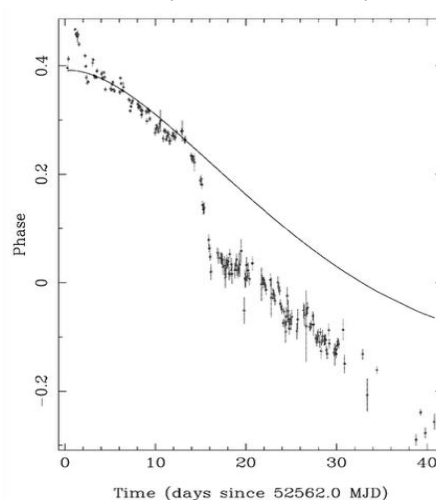
*Sanna+22*

## SAX J1808.4-3658:

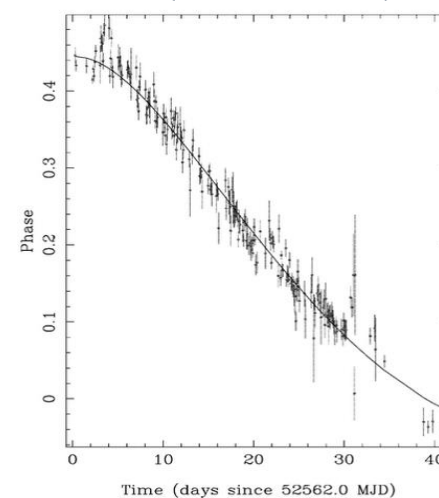
### Pulse phase jumps

- The fundamental phase can shift abruptly
- Harmonic component remains more stable
- Jumps coincide with pulse profile and amplitude evolution

Phase (fundamental)



Phase (2nd harmonic)



*Burderi+06*

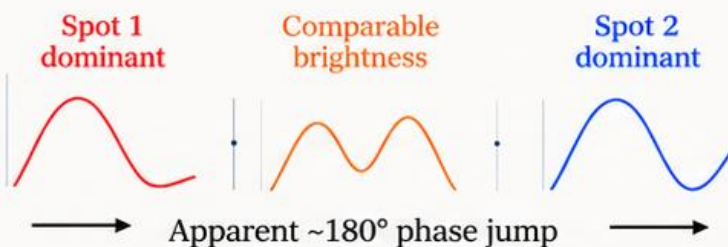
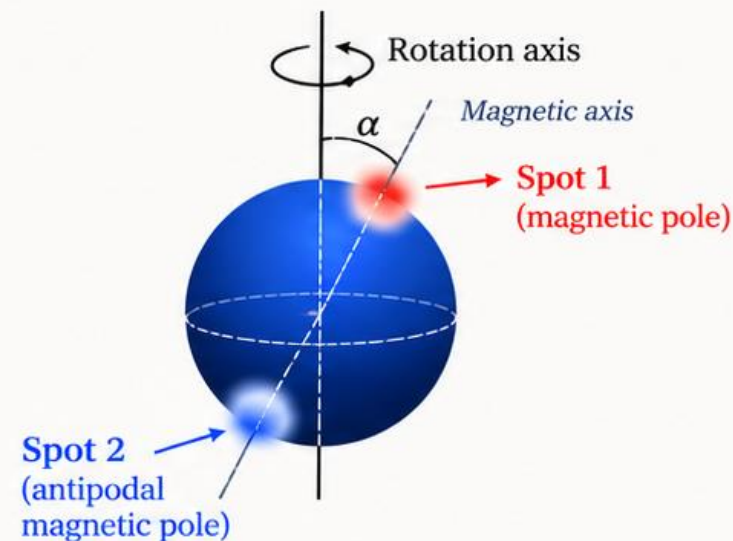
» Pulse phases are **not** always a clean tracer of neutron-star rotation.

# Pulse phase $\neq$ pure spin evolution

Changes in the emitting geometry can mimic spin-phase variations

## A simple geometric picture

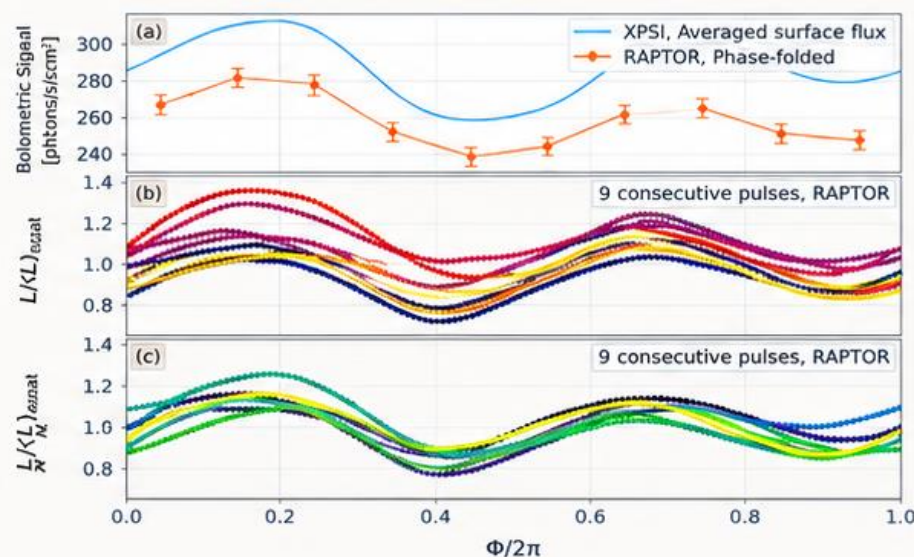
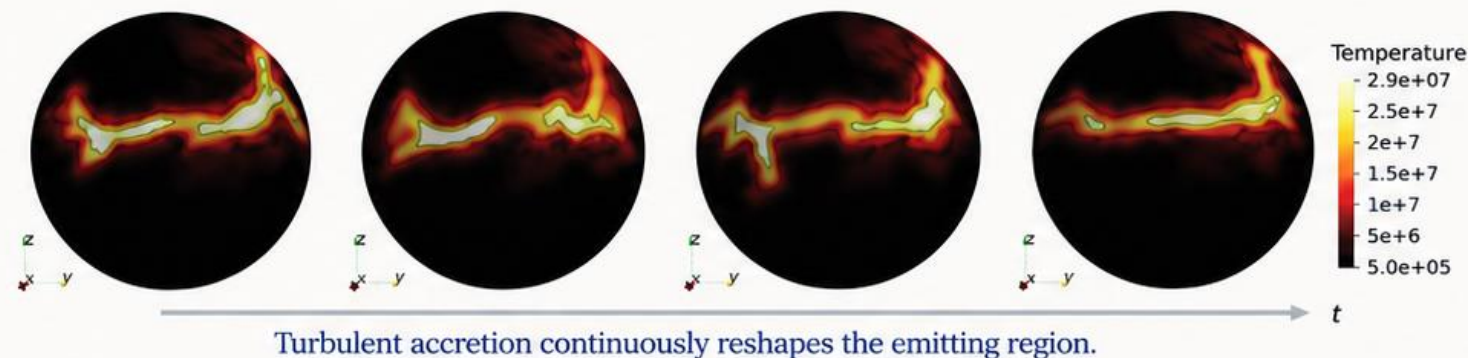
Two antipodal hot spots (oblique geometry)



The dominant emitting region can switch without changing the neutron-star rotation.

## A more realistic picture: dynamic hotspots

3D GRMHD simulations (Das et al. 2025)



➤ **Hotspots are extended and time-dependent**

Their position, shape and temperature vary on timescales comparable to the spin period.

➤ **Pulse-to-pulse variability arises naturally**

Both amplitude and profile shape change from one pulse to the next.

➤ **Fundamental phase is particularly sensitive**

Variations in hotspot geometry can shift the measured phase, even at fixed stellar spin.



Pulse-phase variations do **not** necessarily imply changes in neutron-star spin.

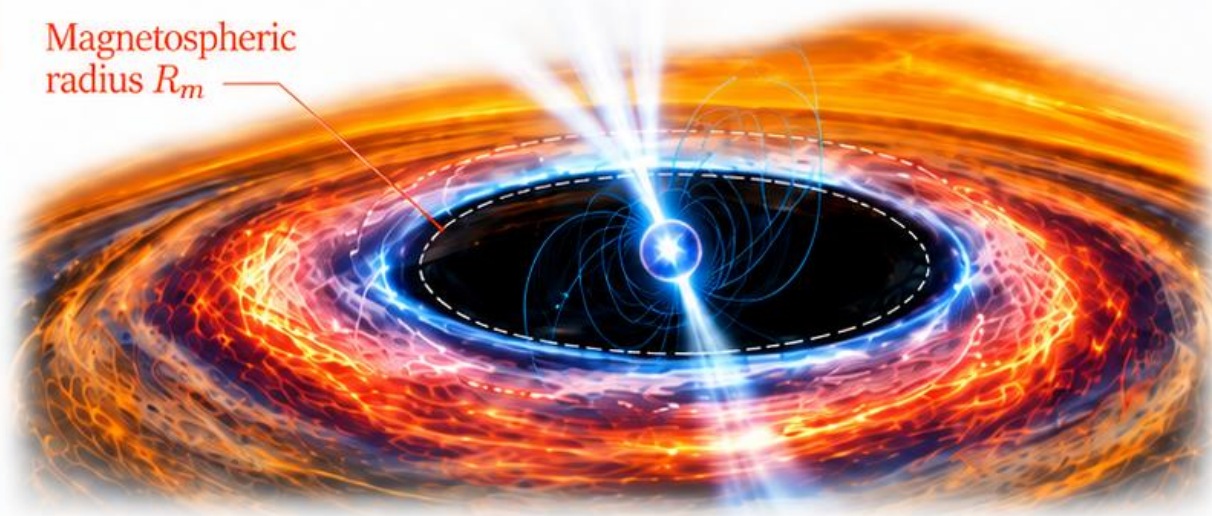
The measured phase responds to both stellar rotation and the evolving emission geometry.



# Spin evolution during outburst: expectation vs observation

Accretion usually spins the neutron star up — but not always.

## STANDARD ACCRETION TORQUE (SPIN UP)



### Accretion torque (spin-up)

$$\Gamma_{\text{acc}} = \dot{M}_* \sqrt{GM r_{\text{in}}} > 0$$

Accreted matter transfers angular momentum to the neutron star.

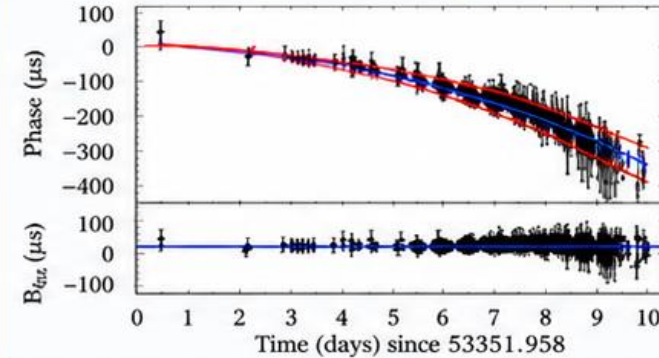
### STANDARD EXPECTATION

$$\dot{\nu} > 0$$

Spin-up

## OBSERVED SPIN EVOLUTION

### IGR J00291+5934 — Spin-up



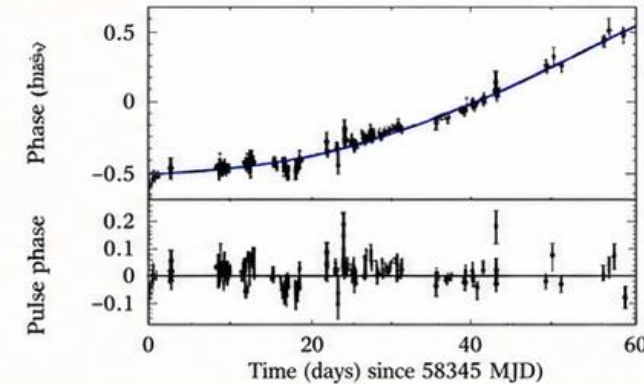
$$\dot{\nu} = (5.1 \pm 0.3) \times 10^{-13} \text{ Hz/s}$$

↑ Spin-up

[Falanga+2005;  
Burderi+2010;  
Papitto+2010]

$$\dot{\nu} > 0 \quad \text{vs} \quad \dot{\nu} < 0$$

### IGR J17591-2342 — Spin-down



$$\dot{\nu} = -(7.4 \pm 0.4) \times 10^{-14} \text{ Hz/s}$$

↓ Spin-down

[Sanna+2020]



**Accretion does not guarantee spin-up.**

The observed spin evolution measures the net torque acting on the neutron star.

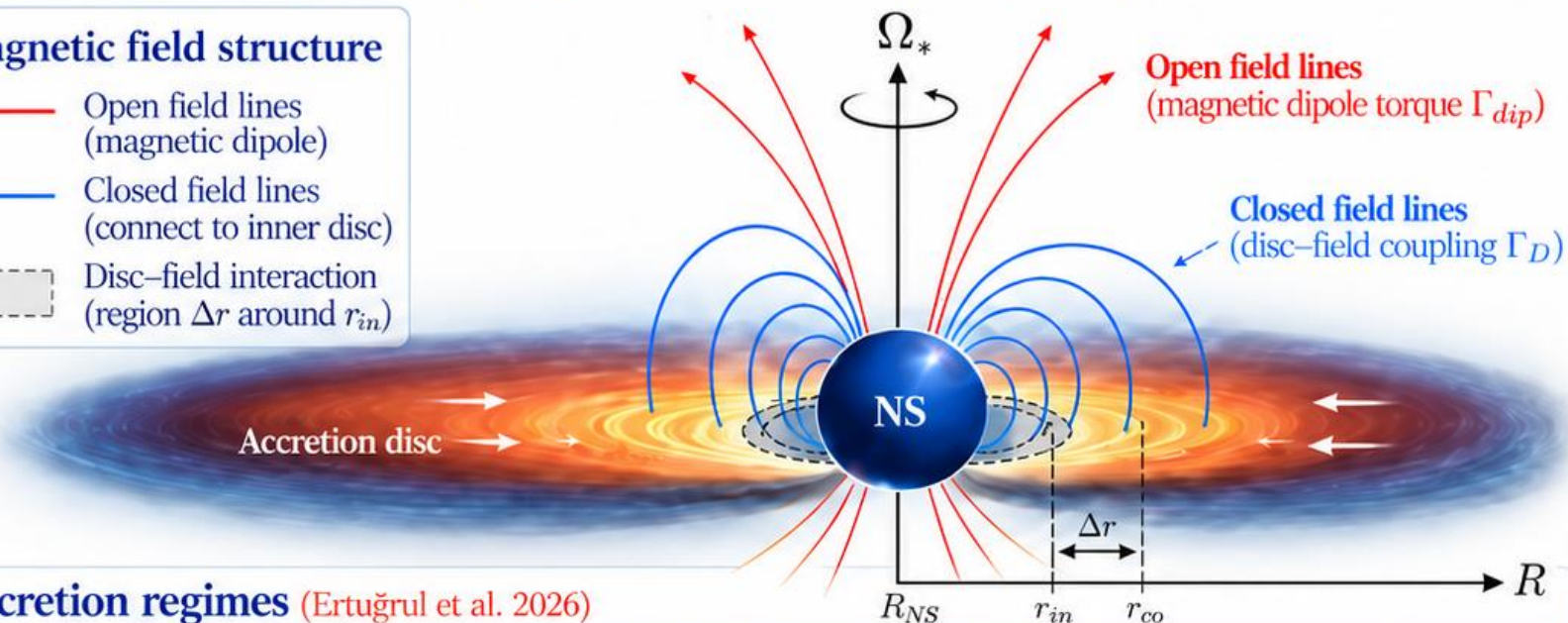


# Torques acting on accreting millisecond X-ray pulsars

Accretion and disc-field coupling can drive either spin-up or spin-down.

## Magnetic field structure

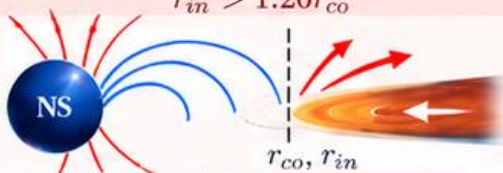
- Open field lines (magnetic dipole)
- Closed field lines (connect to inner disc)
- Disc-field interaction (region  $\Delta r$  around  $r_{in}$ )



## Accretion regimes (Ertuğrul et al. 2026)

### Strong propeller (SP)

$$r_{in} > 1.26 r_{co}$$

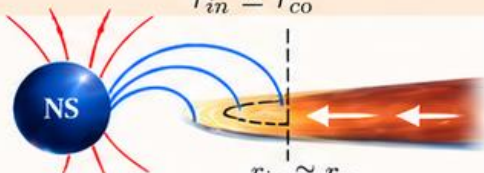


- No accretion onto the neutron star ( $\dot{M}_* = 0$ )
- $\Gamma = \Gamma_D + \Gamma_{dip} < 0$

**Spin-down • no accretion**

### Weak propeller (WP)

$$r_{in} \simeq r_{co}$$

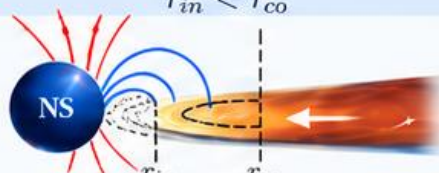


- Accretion is still present ( $\dot{M}_* > 0$ )
- $|\Gamma_D| > \Gamma_{acc} \Rightarrow \Gamma < 0$

**Spin-down while accreting**

### Spin-up (SU)

$$r_{in} < r_{co}$$



- Accretion torque dominates
- $\Gamma_{acc} > |\Gamma_D| \Rightarrow \Gamma > 0$

**Spin-up • accretion dominated**

## Torque contributions (Ertuğrul et al. 2026)

$$\Gamma = \dot{M}_* \sqrt{GM r_{in}} - \frac{\mu^2}{r_{in}^3} \left( \frac{\Delta r}{r_{in}} \right) - \frac{2\mu^2 \Omega_*^3}{3c^3}$$

### Accretion torque $\Gamma_{acc}$ (spin-up)

$$\Gamma_{acc} = \dot{M}_* \sqrt{GM r_{in}} > 0$$

Transfer of angular momentum by the accreted matter at the inner disc radius.

### Disc-field torque $\Gamma_D$ (spin-down)

$$\Gamma_D = - \frac{\mu^2}{r_{in}^3} \left( \frac{\Delta r}{r_{in}} \right) < 0$$

Magnetic stresses between the star and the inner disc remove angular momentum from the star.

### Magnetic dipole torque $\Gamma_{dip}$ (spin-down)

$$\Gamma_{dip} = - \frac{2\mu^2 \Omega_*^3}{3c^3} < 0$$

Open field lines carry away angular momentum. Usually subdominant when the disc is present.



**Accretion does not necessarily imply spin-up.**

The sign of  $\dot{\nu}$  is set by the competition between accretion and disc-field torques.

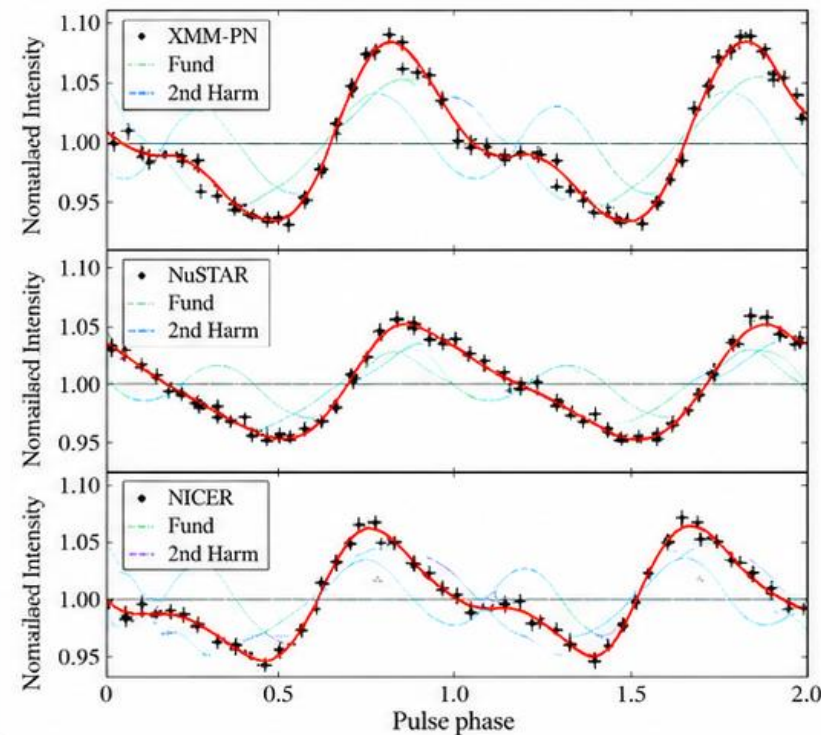


# Pulse profiles encode the emitting geometry

*Harmonic content and pulse morphology trace the structure of the emitting regions.*

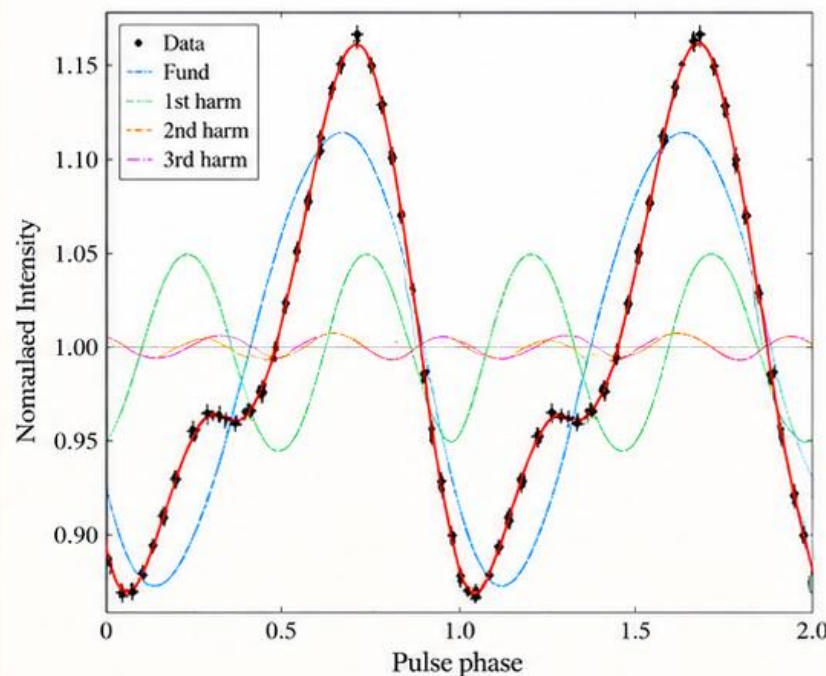
## SWIFT J1756.9–2508

Energy- and instrument-dependent harmonic content

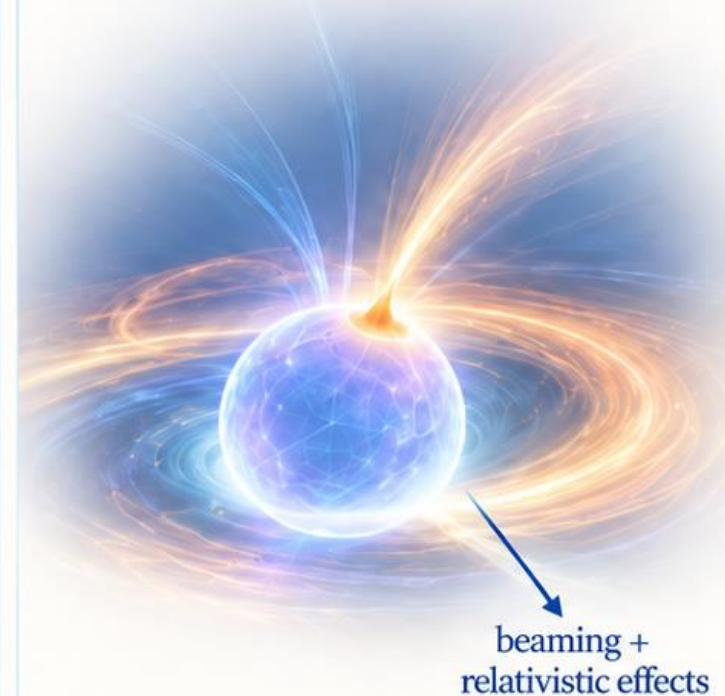


## IGR J17591–2342

Strong non-sinusoidal morphology



## From pulse profile to geometry



Pulse shape



Harmonic content



Emission geometry



But different geometries  
can produce similar pulse profiles.



**Pulse-profile modelling can constrain the hotspot geometry, but degeneracies remain.**  
Additional observables are needed to determine the orientation of the emitting regions.

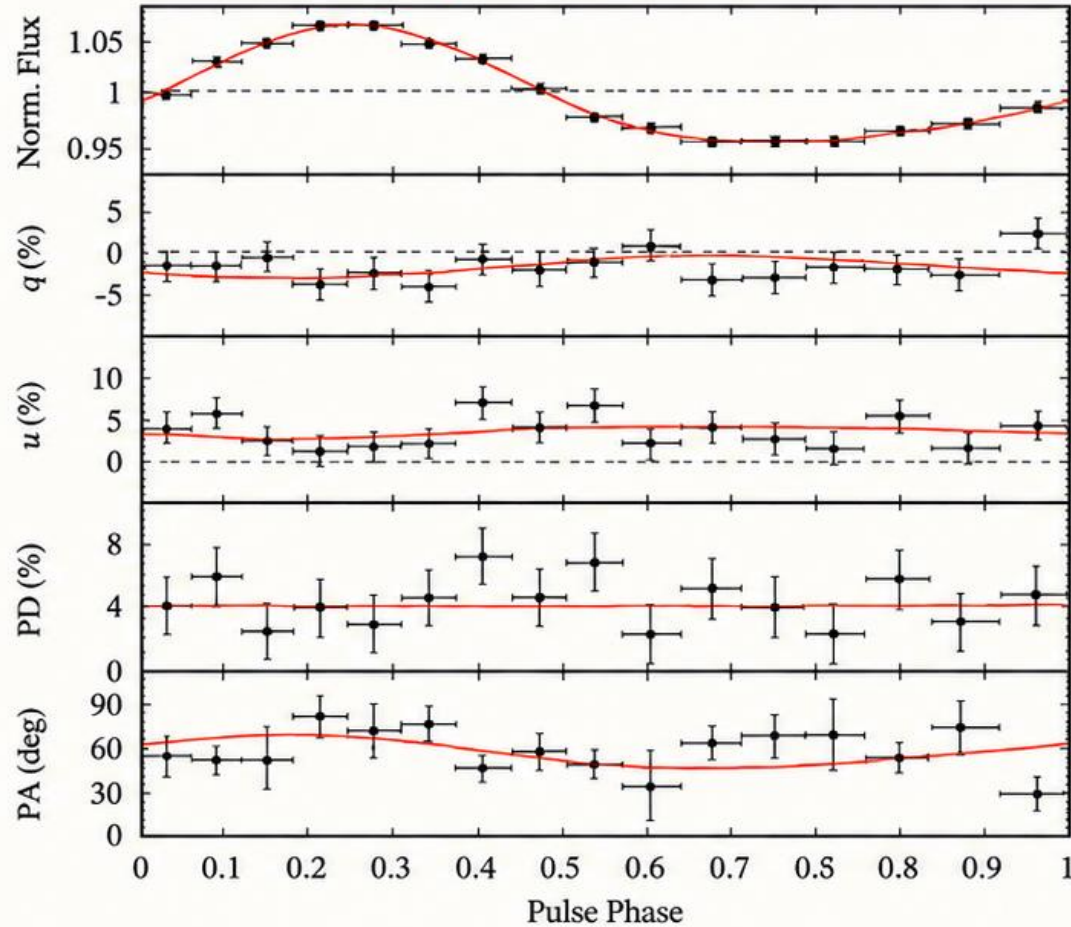


# Polarization adds a new view of the hotspot geometry

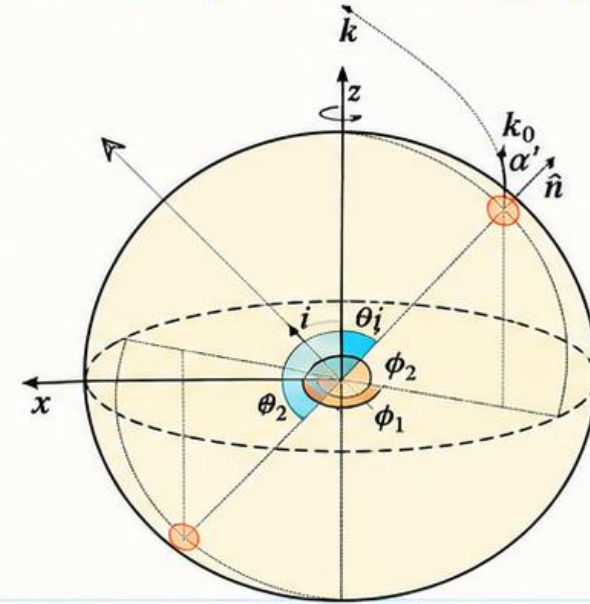
*Intensity and polarization probe complementary aspects of the same emitting regions.*

**SRGA J144459.2–604207**

*First polarized AMXP*



## Geometry of the emitting regions



### Intensity $I(\phi)$

→ pulse morphology and visibility

### Stokes $Q(\phi), U(\phi)$

→ polarization orientation

### PD and PA

→ independent geometric information

### IXPE detection

$PD_{2-8 \text{ keV}} = 2.3 \pm 0.4\%$

$PA = 59^\circ \pm 6^\circ$

$PD_{3-6 \text{ keV}} = 4.0 \pm 0.5\%$

Compatible with two nearly antipodal spots and small magnetic obliquity.



**Polarization provides an independent handle on the orientation of the emitting regions.**

*But weak phase-resolved polarization can still leave substantial degeneracies.*

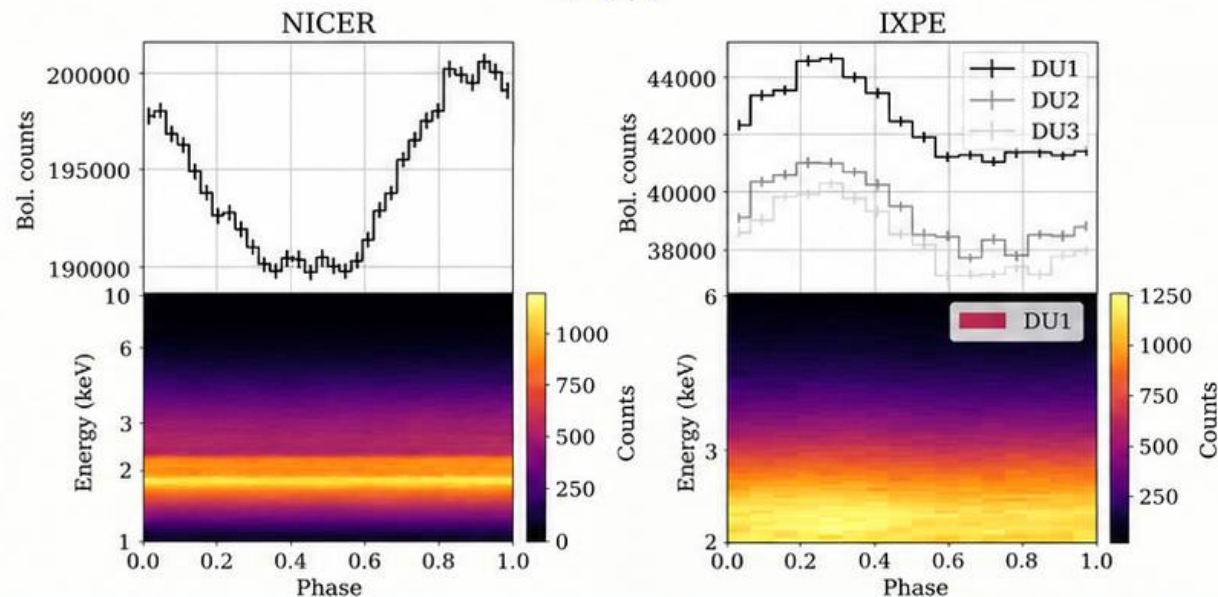


# From polarization detection to **joint inference**

*NICER intensity and IXPE Stokes data can now probe the same hotspot geometry.*

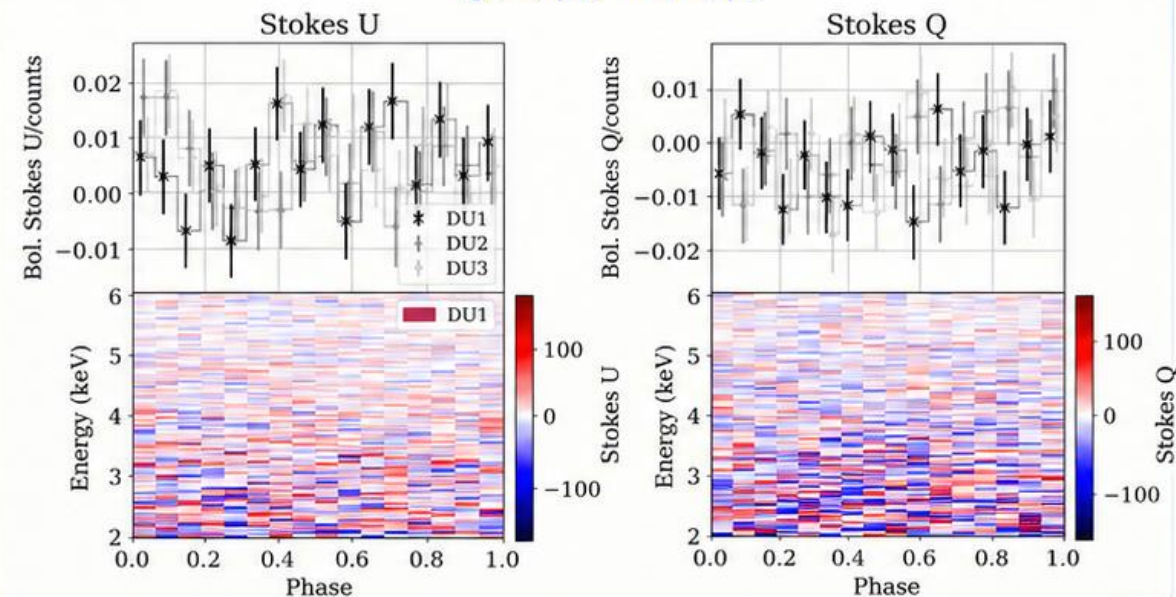
## Intensity information

$$I(E, \phi)$$



## Polarization information

$$Q(E, \phi), U(E, \phi)$$



$$I(E, \phi)_{\text{NICER}}$$

+

$$[I, Q, U](E, \phi)_{\text{IXPE}}$$



**joint hotspot inference**

### Relativistic pulse-profile modelling

- hotspot geometry
- viewing inclination
- emission properties

Polarization modelling predicts the largest information gain when PD and its phase modulation are sufficiently strong.

*Salmi et al. 2025*

**For SRGA J1444, NICER remains more constraining than IXPE.**

The modest polarization degree and weak phase-resolved PA variation limit the current IXPE constraints.



**Timing and polarimetry now probe the same emitting regions with complementary observables.**

The next limitation is increasingly the realism of the hotspot and accretion-flow model.

*Dorsman et al. 2026, MNRAS 551, stag1340*

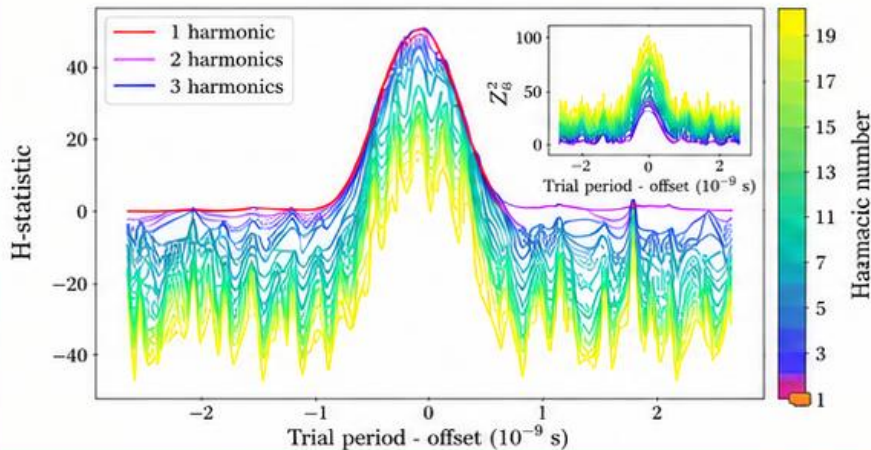
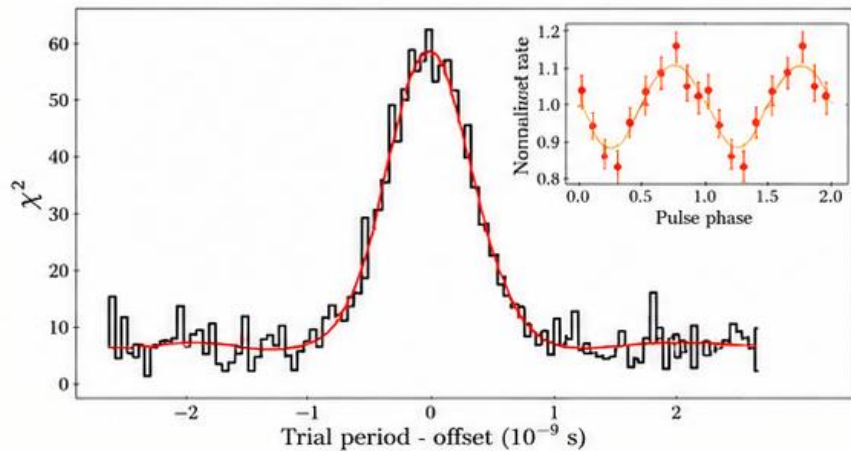
*Salmi et al. 2025, MNRAS 538, 2562*



# How low can accretion-powered pulsations survive?

*IGR J17511–3057 probes the transition between accretion and the propeller regime.*

## Pulsations at very low luminosity



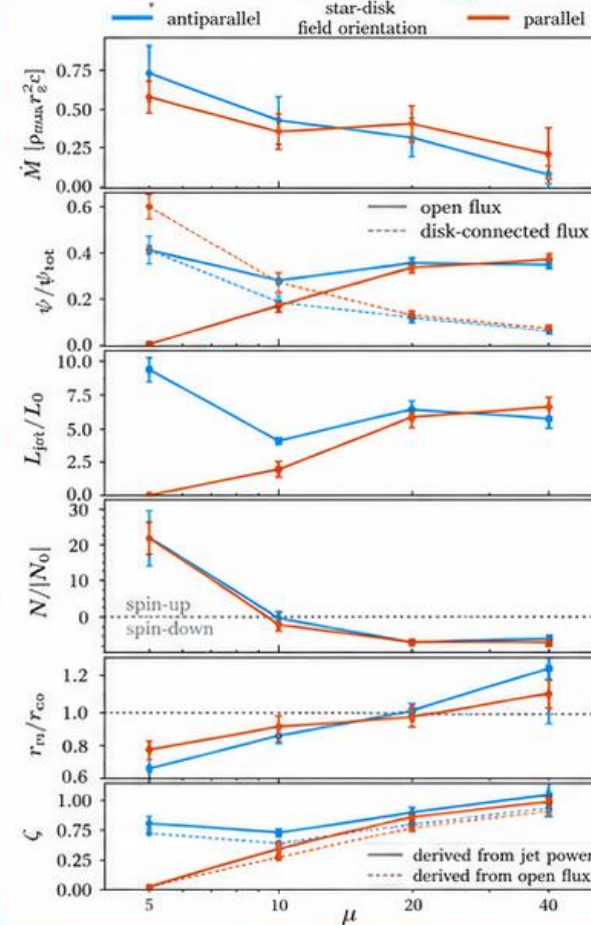
**IGR J17511–3057**

$$L_X \simeq 7 \times 10^{33} \text{ erg s}^{-1}$$

**Coherent  
pulsations  
still detected**

*Illiano et al. 2026*

## GRMHD: a gradual propeller transition

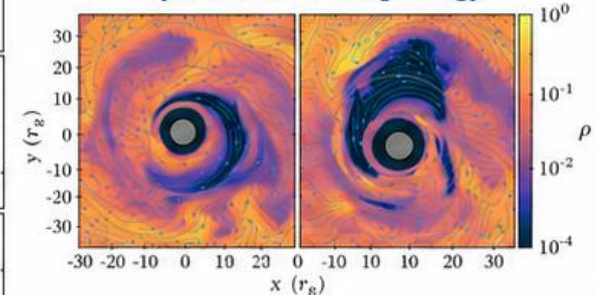


As  $\mu$  increases,  $r_m / r_{\text{co}}$  approaches and exceeds 1

The accretion rate onto the star declines, but does not vanish abruptly

The net torque changes sign near the transition

**dynamic flow morphology**



**Intermittent channelled accretion  
may still occur near the boundary.**

*Parfrey & Tchekhovskoy 2024, ApJ 975, 57*

low  $\dot{M} \rightarrow r_m \rightarrow r_{\text{co}} \rightarrow$  transition region  
*the onset of the propeller need not be a sharp switch*



**The accretion-propeller transition may be gradual rather than abrupt.**  
GRMHD suggests that some accretion can persist near the propeller boundary.

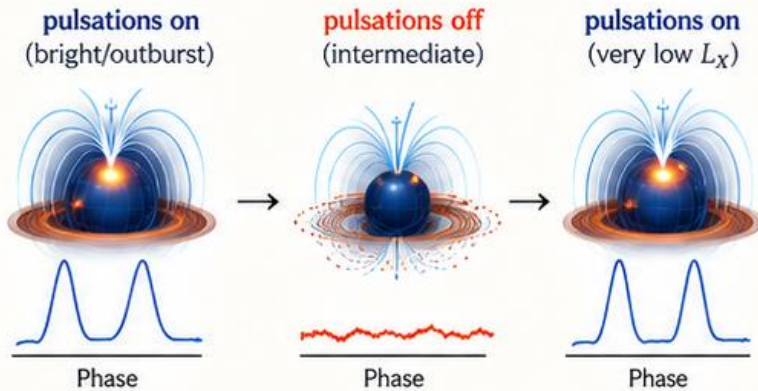


# AMXPs: **what** are we still trying to **understand**?

*Timing, pulse profiles and polarimetry are revealing an increasingly dynamic picture of accretion onto neutron stars.*

## 1 What controls the visibility of pulsations?

Why do pulsations appear, disappear, change harmonic content, and survive at unexpectedly low accretion rates?

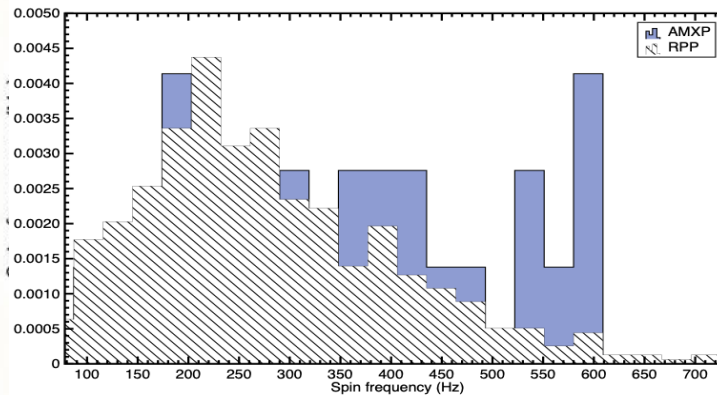


### ➔ Why it matters

Pulsations are our direct tracer of magnetically channelled accretion and of how matter penetrates the magnetosphere, even at very low luminosities (e.g. IGR J17511–3057).

## 2 What sets the neutron-star spin distribution?

Why is the observed distribution truncated well below breakup, and which torques determine spin equilibrium?



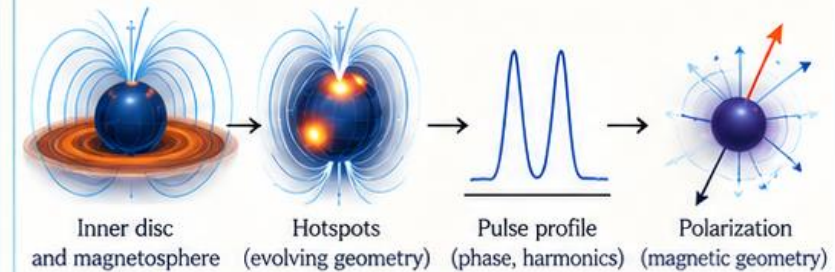
### ➔ Why it matters

The spin distribution encodes the long-term competition between accretion, disc–field coupling and electromagnetic braking.

$$\dot{\nu}_{\text{obs}} = \text{net outcome of competing torques}$$

## 3 What is the geometry of the disc–magnetosphere interaction?

How do the inner disc, magnetic field and hotspots reorganize across an outburst and toward the propeller regime?



### ➔ Why it matters

Geometry drives pulse phases, pulse profiles and polarization, and can mimic changes that would otherwise be attributed to neutron-star spin.



**AMXPs are not simply rotating clocks:**  
their timing signal is shaped by a dynamic interaction between the neutron star, its magnetic field and the accretion flow.

*Connecting spin evolution, pulse morphology and polarization is the route toward disentangling these effects.*



Thanks for listening!

Questions?

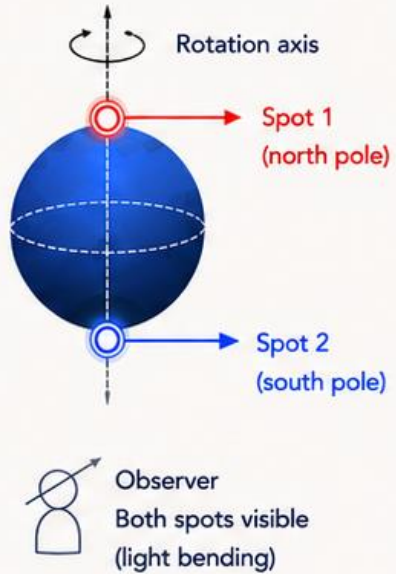
Backup slides



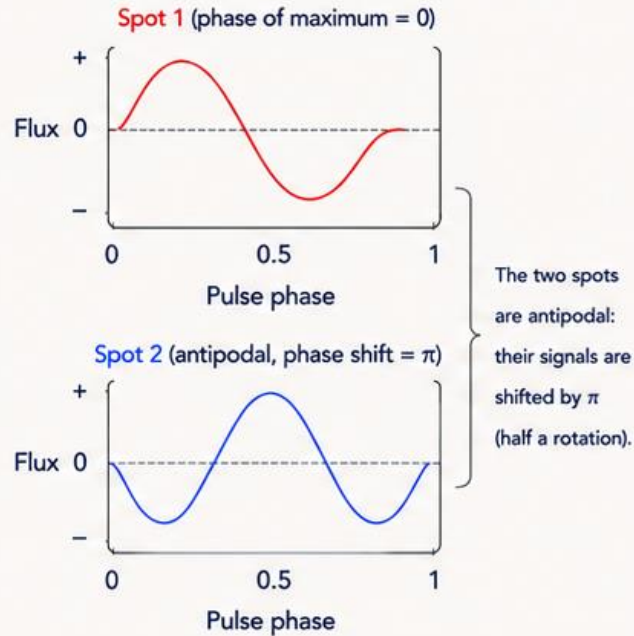
# TWO ANTIPODAL HOT SPOTS

*The observed phase follows the dominant spot*

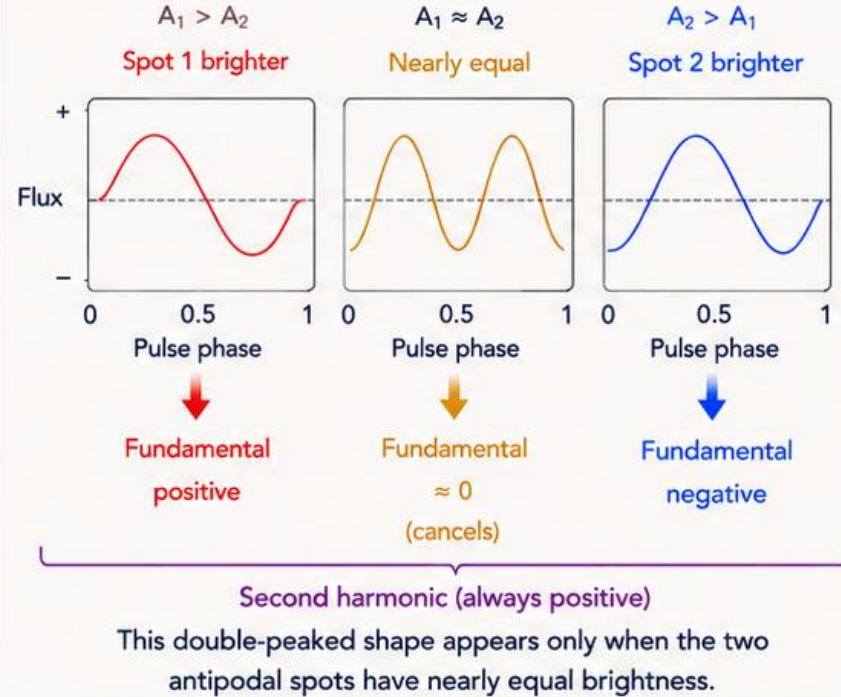
## GEOMETRY



## INDIVIDUAL SPOT PROFILES



## OBSERVED TOTAL PROFILE (SUM OF BOTH SPOTS)



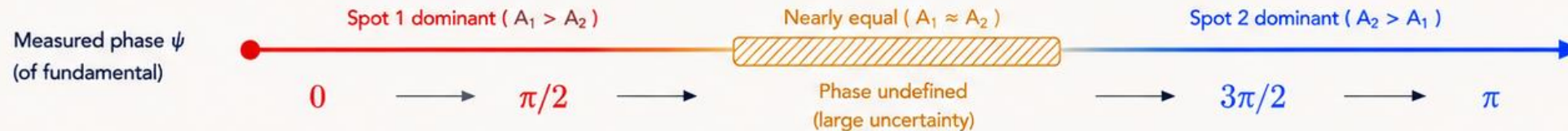
→ The measured phase = phase of the fundamental Fourier component, which is dominated by the brighter spot.

→ When the two spots have nearly equal brightness, the fundamental cancels and the second harmonic dominates. The phase becomes undefined.

→ When the other spot becomes brighter, the sign of the fundamental flips and the phase shifts by  $\sim 180^\circ$ .

## OBSERVED CONSEQUENCE: APPARENT PHASE JUMP

A phase jump arises from pulse-profile evolution, not from a change in the neutron star spin

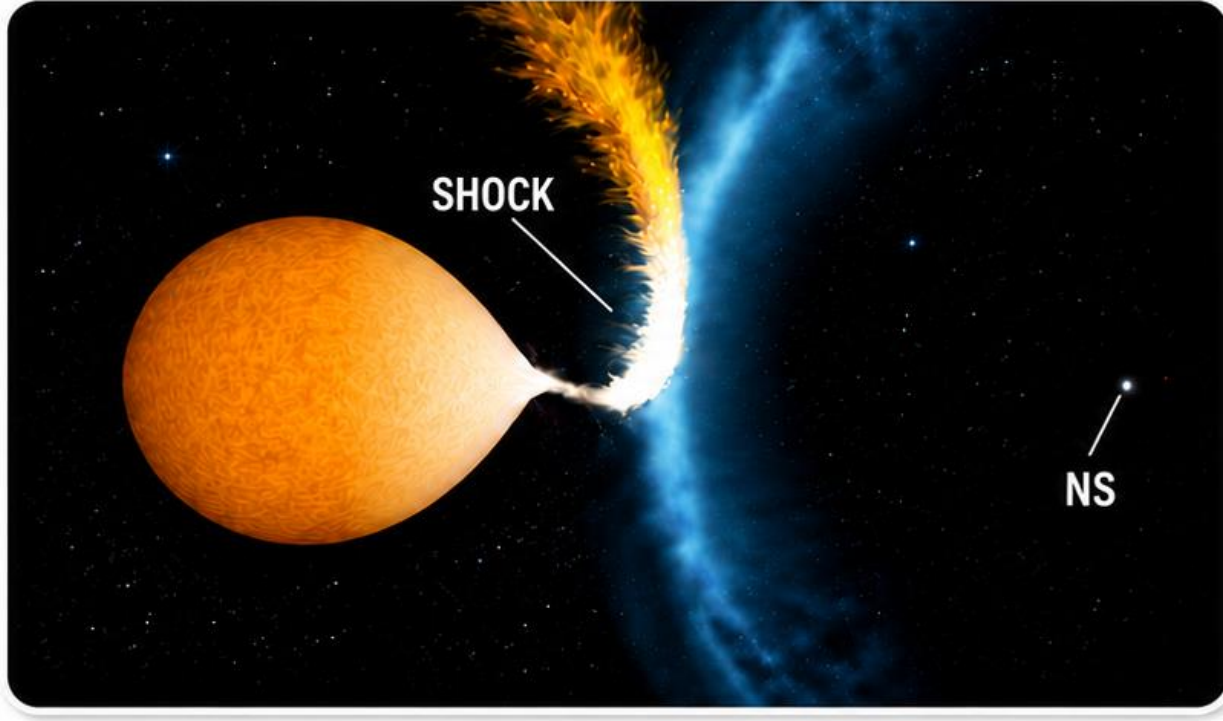


## APPARENT $\sim 180^\circ$ PHASE JUMP

caused by pulse-profile evolution as the dominant hotspot switches.

# What can we learn in the **long term**?

Even in **quiescence**, compact binaries **keep telling us their story**.



We study **quiescent systems** to answer key questions:



**Does accretion stop completely?**

No. We observe **very low X-ray flux** values (below  $10^{33}$  erg/s/cm<sup>2</sup>).

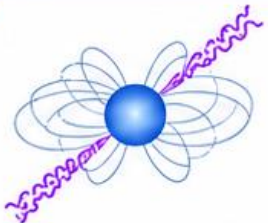


**Does the NS behave as a millisecond radio pulsar?**

Yes. We observe **secular spin-down**.

## WHAT WE CAN MEASURE ON LONG TIMESCALES

1

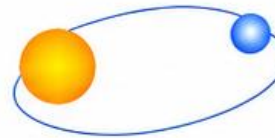


### SPIN-DOWN IN QUIESCENCE

Measuring the loss of **rotational energy** of the neutron star over years.



2



### ORBITAL PERIOD VARIATION

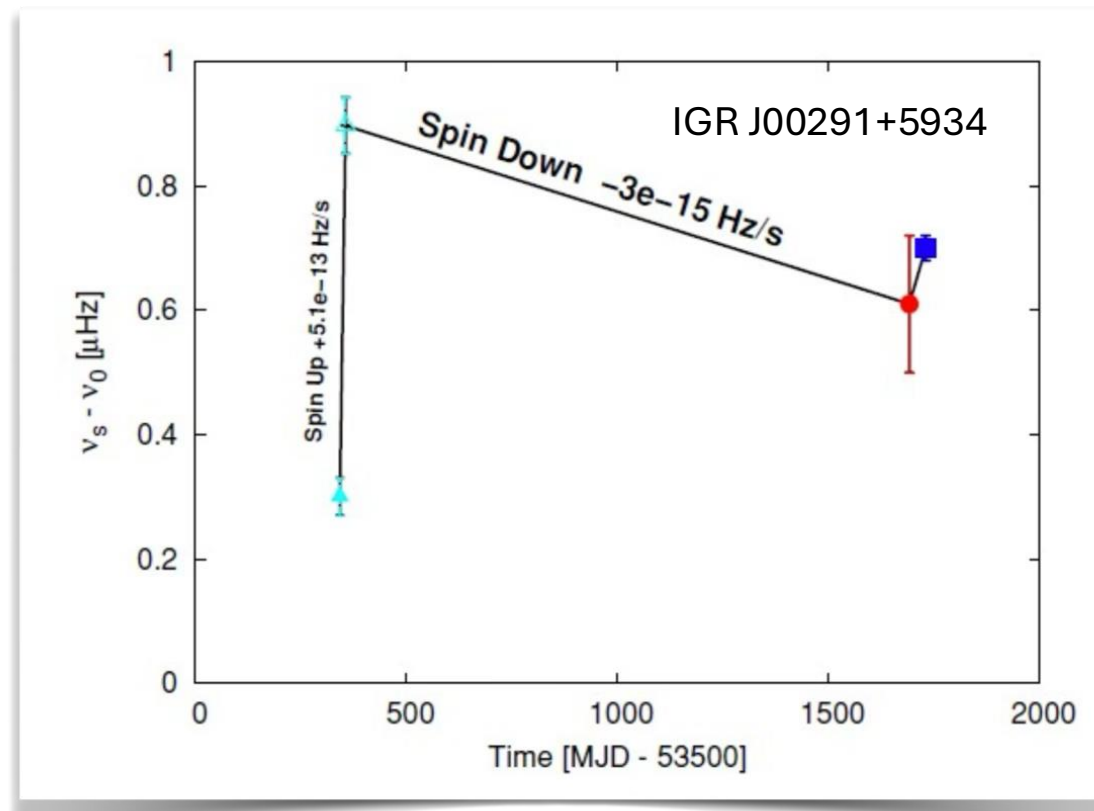
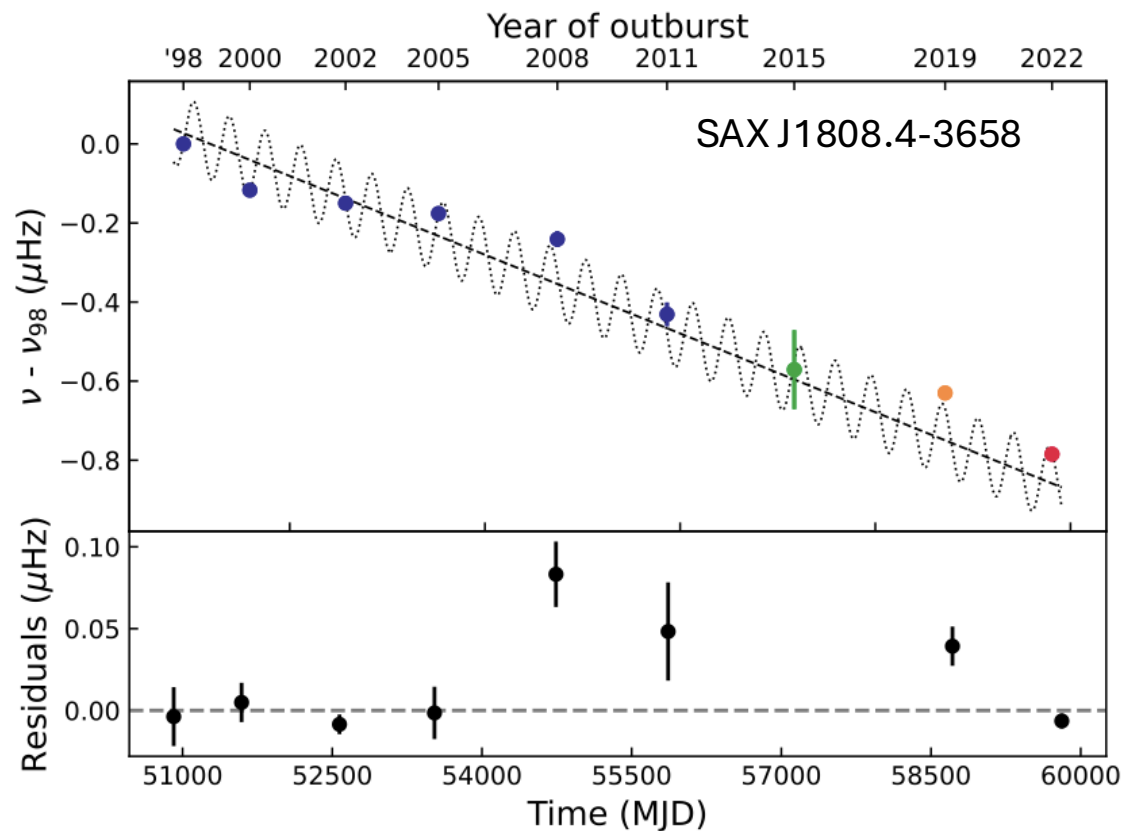
Tracking changes in the **orbital period** over years to decades.



# Long-term (secular) spin evolution

[Illiano+23]

[Hartman+10, Papitto+10, Sanna+17]



$$\dot{\nu} \sim -10^{-15} \text{ Hz/s}$$

Compatible with rotation-powered spin-down for  $B \sim (10^8 - 10^9) \text{ G}$

# Long-term (secular) spin evolution

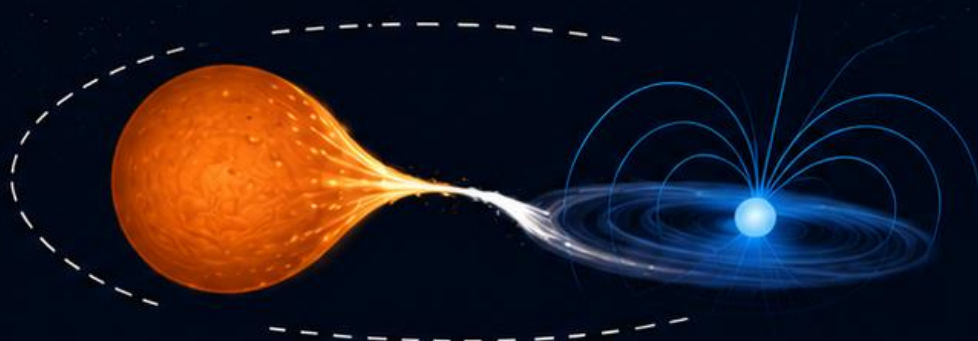
| Source                    | P <sub>spin</sub> (ms) | P <sub>orb</sub> (h) | dP <sub>orb</sub> /dt (s/s)<br>(u.l. at 3 $\sigma$ c.l.) | Ref.                             |
|---------------------------|------------------------|----------------------|----------------------------------------------------------|----------------------------------|
| <b>SAX J1808.4-3658</b>   | <b>2.5</b>             | <b>2</b>             | <b>-1.1(1) 10<sup>-15</sup></b>                          | <b>Illiano+23</b>                |
| <b>IGR J00291+5934</b>    | <b>1.7</b>             | <b>2.5</b>           | <b>-4.1(1.2)10<sup>-15</sup></b>                         | <b>Patruno+10<br/>Papitto+11</b> |
| <b>SAX J1748.9-2021</b>   | <b>2.3</b>             | <b>8.8</b>           | <b>-4.1(2) 10<sup>-15</sup></b>                          | <b>Illiano+24</b>                |
| <b>SWIFT J1756.9-2508</b> | <b>5.5</b>             | <b>0.9</b>           | <b>-4.8(6) 10<sup>-16</sup></b>                          | <b>Sanna+18</b>                  |
| <b>XTE J1751-305</b>      | <b>2.3</b>             | <b>0.7</b>           | <b>-5.5(1.2) 10<sup>-15</sup></b>                        | <b>Riggio+11</b>                 |
| <b>IGR J17511-3057</b>    | <b>4.1</b>             | <b>3.5</b>           | <b>-2.3(1.1) 10<sup>-15</sup></b>                        | <b>Sanna+25</b>                  |
| <b>MAXI J1957+032</b>     | <b>3.2</b>             | <b>1.0</b>           | <b>-2.2(0.4) 10<sup>-14</sup></b>                        | <b>Sanna+25</b>                  |
| <b>IGR J17494-3030</b>    | <b>2.7</b>             | <b>1.2</b>           | <b>-2.1(7) 10<sup>-14</sup></b>                          | <b>Ng+21</b>                     |



# Secular orbital evolution in AMXPs

*Orbital period derivatives measured (or constrained) over years–decades.*

What drives the orbital evolution?



Positive  $\dot{P}_{\text{orb}}$   
(orbit expanding)



Negative  $\dot{P}_{\text{orb}}$   
(orbit shrinking)

Key mechanisms



Mass transfer  
and loss



Angular momentum  
losses



Irradiation-driven  
effects



Gravitational  
waves



AMXPs show both **positive** and **negative**  $\dot{P}_{\text{orb}}$ .  
Understanding the balance of these processes is key.

| Source                  | $P_{\text{spin}}$<br>(ms) | $P_{\text{orb}}$<br>(h) | $dP_{\text{orb}}/dt$ (s/s)<br>(u.l. at $3\sigma$ c.l.) | Ref.                   |
|-------------------------|---------------------------|-------------------------|--------------------------------------------------------|------------------------|
| <b>SAX J1808.4–3658</b> | 2.5                       | 2                       | <b><math>1.7(5) \times 10^{-12}</math></b>             | Bult+19<br>Sanna+17    |
| IGR J00291+5934         | 1.7                       | 2.5                     | $(-6.6 \div 6.5) \times 10^{-13}$                      | Patruno+16<br>Sanna+17 |
| SAX J1748.9–2021        | 2.3                       | 8.8                     | $(-0.7 \div 8.4) \times 10^{-11}$                      | Sanna+22               |
| SWIFT J1756.9–2508      | 5.5                       | 0.9                     | $(-4.1 \div 7.1) \times 10^{-12}$                      | Sanna+18<br>Bult+18    |
| IGR J17379–3747         | 2.1                       | 1.9                     | $(-9.4 \div 4.4) \times 10^{-12}$                      | Sanna+18               |
| XTE J1751–305           | 2.3                       | 0.7                     | $(-2.7 \div 0.7) \times 10^{-11}$                      | Riggio+11              |
| IGR J17511–3057         | 4.1                       | 3.5                     | $-2.55(7) \times 10^{-11}$                             | Sanna+25               |



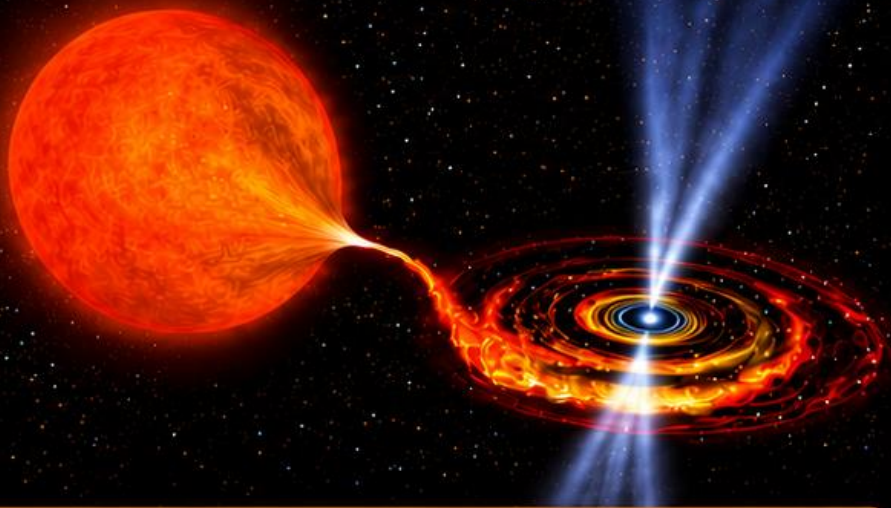
# THE RADIO-EJECTION HYPOTHESIS

*A unified model for the state transition in accreting millisecond pulsars*



## OUTBURST: ACCRETION PHASE

- Active accretion from the donor
- Matter accumulates in the inner disc
- X-ray emission is high



Dominated by accretion-powered **X-ray** emission

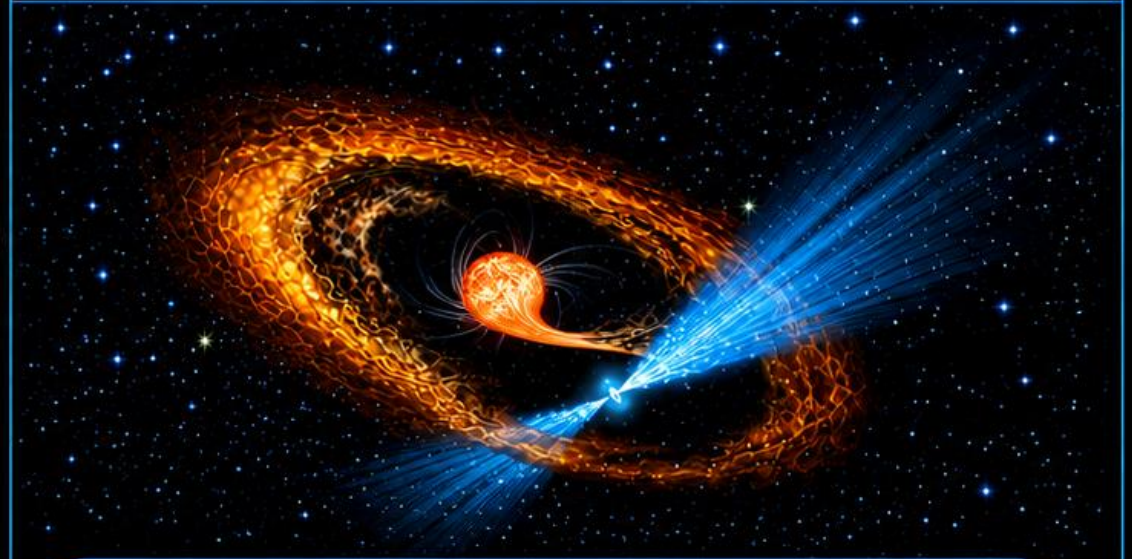
## STATE TRANSITION

Drop in accretion rate  
(below a critical threshold)



## QUIESCENCE: RADIO EJECTION

- Accretion is suppressed
- A radio pulsar wind is ejected
- Radio emission dominates



Powered by rotation: **radio** pulsar wind ejection



**KEY IDEA:** The system switches from an **accretion-dominated (X-ray)** state to a **rotation-powered (radio)** state via the ejection of a radio pulsar wind.



Explains the low X-ray luminosity and is consistent with a **rotation-powered** state in quiescent AMXPs.

*(Burderi et al. 2001, Di Salvo et al. 2008)*



# SAX J1808.4-3658: APPLGATE-SHAHAM MODEL

## Periodic Orbital Modulations via Gravitational Quadrupole Changes (GQC)

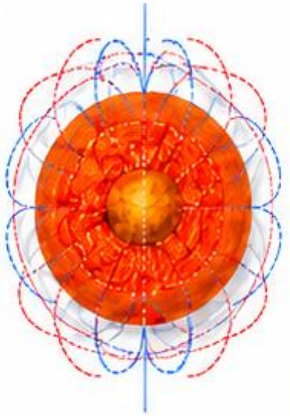
Magnetic activity cycles in the companion star drive internal angular momentum redistribution, changing its shape and gravitational quadrupole moment.

This **modulates the orbital period**, producing **quasi-sinusoidal** variations in the accumulated delay of  $T_{star}$ .

### THE APPLGATE-SHAHAM MECHANISM: FROM MAGNETIC CYCLE TO ORBITAL MODULATION

#### 1 Magnetic activity cycle

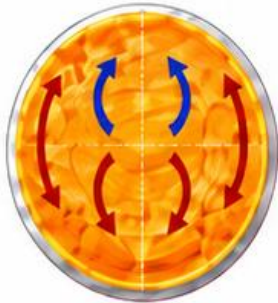
Dynamo action in the convective companion



Magnetic cycle drives changes in the internal structure.

#### 2 Angular momentum redistribution

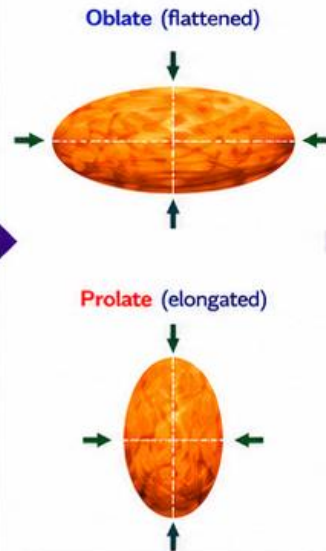
Magnetic stresses move angular momentum inside the star



Angular momentum is transported between different layers.

#### 3 Stellar deformation

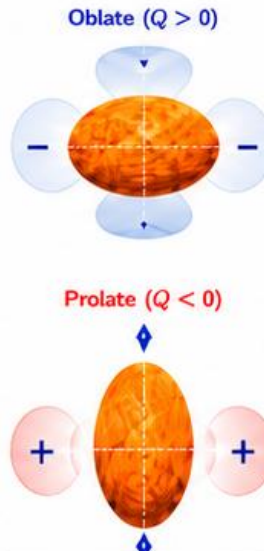
Star becomes more oblate (or more prolate)



The stellar shape changes with the activity cycle.

#### 4 Quadrupole moment change

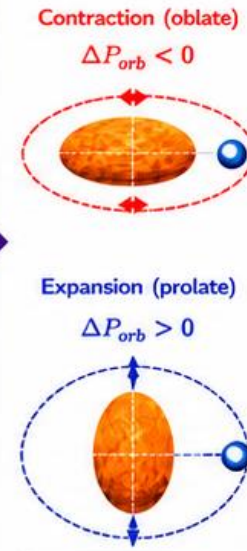
Gravitational quadrupole moment changes:  $\Delta Q$



The sign and amplitude of  $Q$  vary over the magnetic cycle.

#### 5 Orbital period modulation

Change in  $Q$  modulates the orbital period



$P_{orb}$  is periodically modulated: expansion (prolate) / contraction (oblate).



# SAX J1808.4-3658: APPELGATE-SHAHAM MODEL

## Periodic Orbital Modulations via Gravitational Quadrupole Changes (GQC)

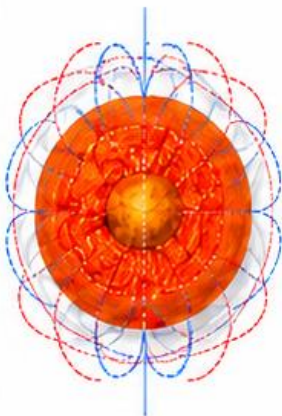
Magnetic activity cycles in the companion star drive internal angular momentum redistribution, changing its shape and gravitational quadrupole moment.

This **modulates the orbital period**, producing **quasi-sinusoidal** variations in the accumulated delay of  $T_{star}$ .

### THE APPELGATE-SHAHAM MECHANISM: FROM MAGNETIC CYCLE TO ORBITAL MODULATION

#### 1 Magnetic activity cycle

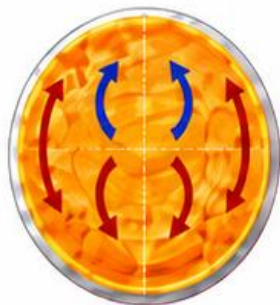
Dynamo action in the convective companion



Magnetic cycle drives changes in the internal structure.

#### 2 Angular momentum redistribution

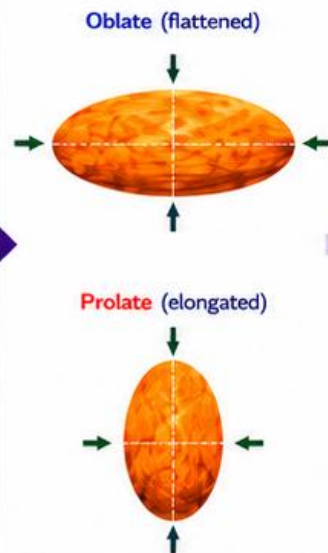
Magnetic stresses move angular momentum inside the star



Angular momentum is transported between different layers.

#### 3 Stellar deformation

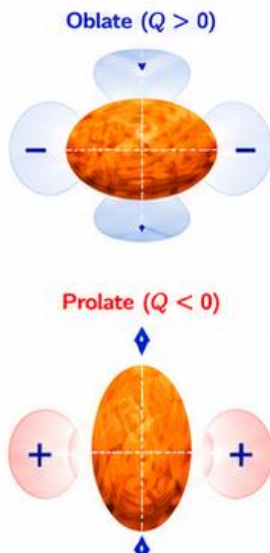
Star becomes more oblate (or more prolate)



The stellar shape changes with the activity cycle.

#### 4 Quadrupole moment change

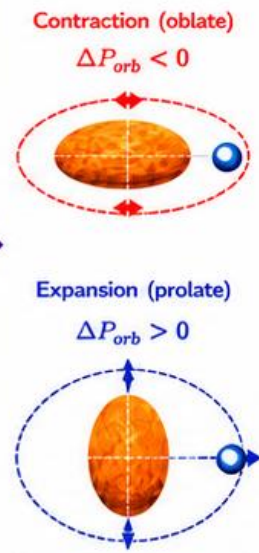
Gravitational quadrupole moment changes:  $\Delta Q$



The sign and amplitude of  $Q$  vary over the magnetic cycle.

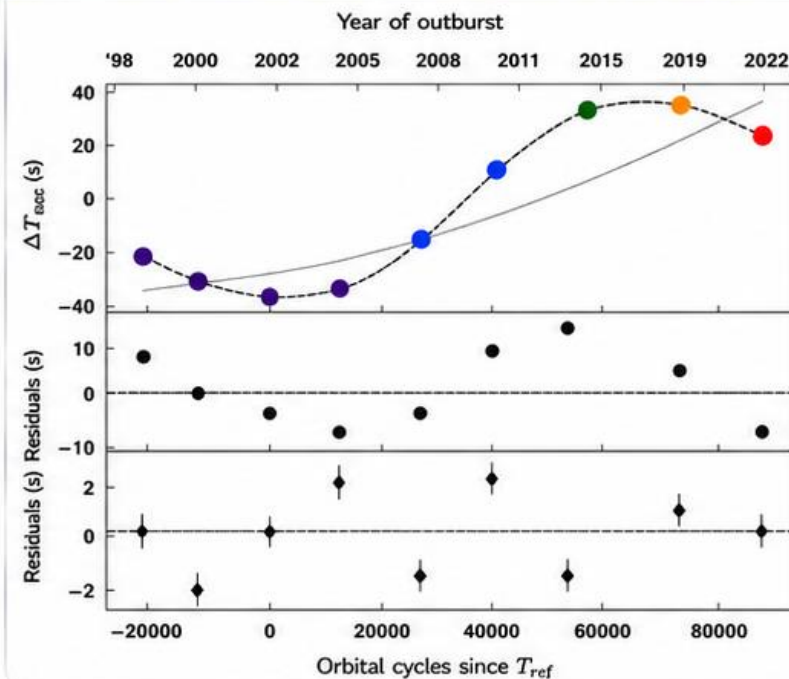
#### 5 Orbital period modulation

Change in  $Q$  modulates the orbital period



$P_{orb}$  is periodically modulated: expansion (prolate) / contraction (oblate).

### OBSERVED ACCUMULATED DELAY OF $T_{star}$



### BEST-FIT PARAMETERS (ILLIANO+23)

|                                                              |                               |
|--------------------------------------------------------------|-------------------------------|
| $\delta P_{ref} = 4.63(16) \times 10^{-4} \text{ s}$         | $A = 11.30(33) \text{ s}$     |
| $\dot{P}_{orb} = -2.82(69) \times 10^{-13} \text{ s s}^{-1}$ | $P = 20.7(0.6) \text{ years}$ |

$\delta P_{ref}$ : correction to reference spin period       $\dot{P}_{orb}$ : secular orbital period derivative  
 $A$ : semi-amplitude of the modulation       $P$ : modulation period