

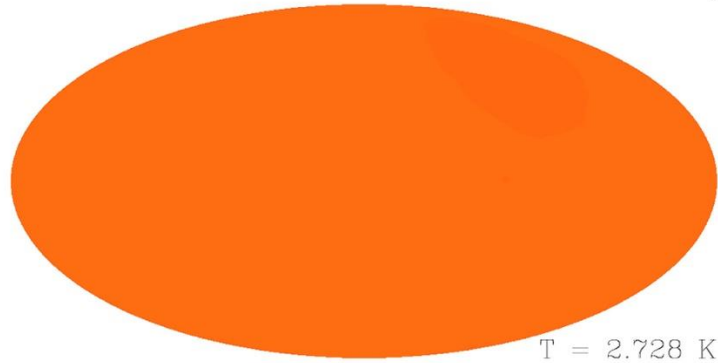
Dipole analyses of cosmic radio background with SKA

Tiziana Trombetti & Carlo Burigana

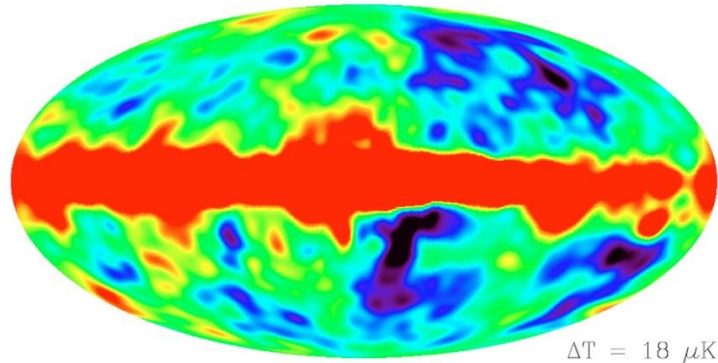
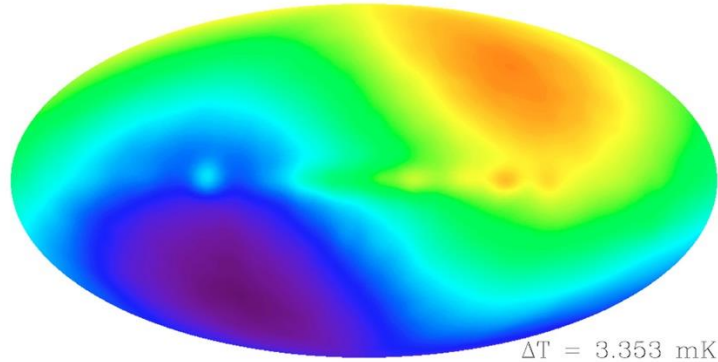
INAF-Istituto di Radioastronomia

CMB dipole

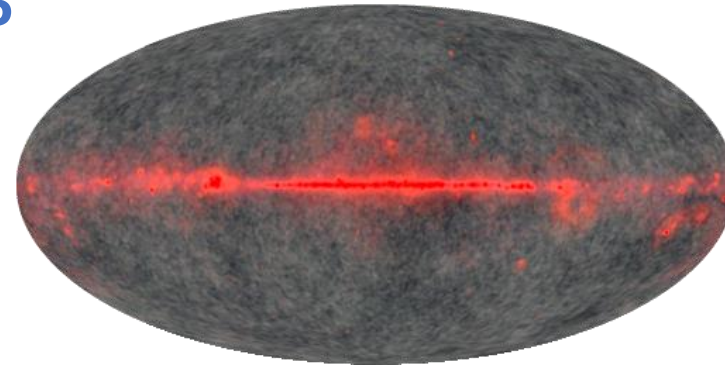
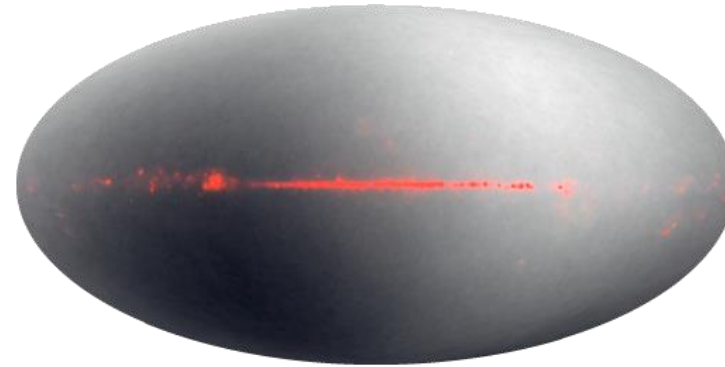
DMR 53 GHz Maps



COBE



WMAP



False color images. Q-band red, V-band green, W-band blue. A CMB therm spectrum grey.

Top: 3 color combination image from the Q-, V-, and W-band maps. Dipole and high Galactic latitude anisotropy are seen.

Bottom: similar but without dipole.

https://lambda.gsfc.nasa.gov/product/wmap/pub_papers/firstyear/basic/wmap_cb1_images.html

https://lambda.gsfc.nasa.gov/product/cobe/more_images/cobeslide29.jpg

CMB dipole: *Planck ... & beyond*

Dipole direction in Galactic coordinates

$l=264.021^\circ, b=48.253^\circ$ $v = (369.82 \pm 0.11) \text{ km/s}$

$\beta = v/c \simeq 1.2336 \times 10^{-3} \simeq A_{\text{dip}} / T_0$

velocity of the Solar System barycentre
with respect to the CMB

Planck Collaboration 2020, AA 641 A1

First confirmation of v with aberration & modulation
(Challinor & van Leeuwen 2002, Sollom 2010) of
CMB anisotropies

$v = 384 \text{ km/s} \pm 78 \text{ km/s (stat.)} \pm 115 \text{ km/s (syst.)}$

Planck Coll.
2014, A&A
571, A27,
Planck 2013
results.
XXVII.
Doppler
boosting
of the CMB:
Eppur
si muove

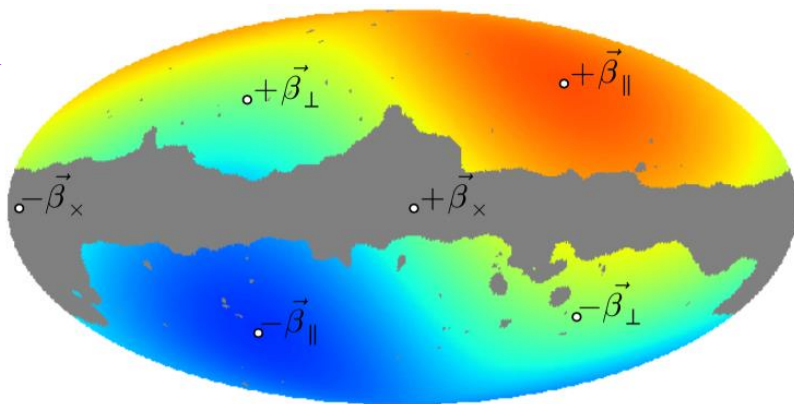


Fig. 2. Specific choice for the decomposition of the dipole vector β in Galactic coordinates. The CMB dipole direction $(l, b) = (263^\circ 99', 48^\circ 26')$ is given as β_{\parallel} , while two directions orthogonal to it (and each other) are denoted as β_{\perp} and β_{\times} . The vector β_{\times} lies within the Galactic plane.

❑ We observe the CMB dipole, and we now firmly know from *Planck* that a significant part of it is kinetic

But ... is it almost fully kinetic or there is also a non negligible intrinsic dipole?

For many standard models the anisotropy power of intrinsic dipole and quadrupole is expected to be similar ... but ...

- ✓ CMB space missions observed a relatively low quadrupole (and also other types of low multipole anomalies)
- ✓ But, in principle, anisotropy power of intrinsic dipole may be larger

❖ CMB space missions like CORE could study boosting effects to polarization and cross-correlations → more robust determination of purely velocity-driven effects that are not degenerate with the intrinsic CMB dipole: **overall S/N $\simeq 13$** (Burigana+ 2018)

→ **Essentially as an ideal cosmic-variance-limited experiment up to $\ell \simeq 2000$**

❖ Method based on the exploitation the leakage of the intrinsic dipole into the CMB monopole and quadrupole (Yasini & Pierpaoli 2017), e.g. with **CMB space missions like PIXIE** (Kogut+ 2016), **FOSSIL** (M8, Aghanim+ 2025) that recently passed ESA Phase 1 selection

CMB vs matter dipole

Many galaxy surveys indicates that matter dipole \neq CMB dipole

See e.g. N.J. Secrest + 2022, ApJL 937, L31 *A Challenge to the Standard Cosmological Model*

NRAO VLA Sky Survey
(NVSS; Condon et al. 1998)

Wide-field Infrared Survey Explorer
(WISE; Wright et al. 2010)

See also Böhme+ , PRL, 135, 201001 (2025) for
a recent analysis: source count dipole excess by
a factor of 3.67 ± 0.49 \rightarrow a 5.4σ discrepancy.

- ✓ The large dipoles seen in **radio galaxies** & **quasars** independently reject, at 2.6σ & 4.4σ , the null hypothesis that the dipoles arise from Doppler boosting and relativistic aberration with velocity 370 km/s in the CMB dipole direction
- ✓ Dipole amplitudes are about 3 and 2 times larger than the respective kinematic expectations and point 45° and 26° from CMB dipole ($l=264.021^\circ$, $b=48.253^\circ$)
- ✓ The joint significance of this rejection of the cosmological principle is 5.1σ
- ✓ These anomalously large dipoles are statistically consistent with a single, shared dipole of distant galaxies and quasars, with amplitude $\mathcal{D}=(1.40 \pm 0.13) \times 10^{-2}$ in the direction $(l, b)=(233^\circ \pm 6^\circ, 34^\circ \pm 5^\circ)$
- ✓ No evidence for a frequency dependence of the amplitude
- ✓ Agreement between radio galaxy & quasar dipoles improves by subtracting standard kinematic expectation: $\mathcal{D}=(0.86 \pm 0.14) \times 10^{-2}$; $(l, b)=(217^\circ \pm 10^\circ, 20^\circ \pm 7^\circ)$
- ✓ Intrinsic overdensity of galaxies and quasars on very large scales, in a direction 48° away from the CMB dipole

Observer motion → modification and transfer of the CB spectrum

$$T_{\text{th}}^{\text{BB/dist}}(\nu, \hat{n}, \boldsymbol{\beta}) = \frac{xT_0}{\ln(1 + 1/(\eta(\nu, \hat{n}, \boldsymbol{\beta}))^{\text{BB/dist}})} \quad \text{observed signal map} \quad (1)$$

where $\eta(\nu, \hat{n}, \boldsymbol{\beta}) = \eta(\nu')$ with $\nu' = \nu(1 - \hat{n} \cdot \boldsymbol{\beta})/(1 - \beta^2)^{1/2}$ (2)

Lorentz invariance of photon distribution function $\eta(\nu)$ sky direction unit vector associated to polar coordinates (colatitude) and (longitude)
 $\boldsymbol{\beta} = \mathbf{v}/c$

N.B.: monopole background is by definition the isotropic component – no aberration

Compton-Getting effect (Forman, M. A. 1970, Planet. Space Sci., 18, 25)

$$T_{\text{th}}^{\text{BB/dist}}(\nu, \theta, \phi, \beta) = \sum_{\ell=0}^{\ell_{\text{max}}} \sum_{m=-\ell}^{\ell} a_{\ell,m}(\nu, \beta) Y_{\ell,m}(\theta, \phi) \quad (3)$$

$Y_{\ell,m}(\theta, \phi)$ spherical harmonics, related to associated Legendre Polynomial $P_{\ell}^m(\cos \theta)$

$$Y_{\ell,m}(\theta, \phi) = \tilde{P}_{\ell}^m(\cos \theta) \quad \tilde{P}_{\ell}^m(\cos \theta) = \sqrt{\frac{2\ell+1}{4\pi} \frac{(\ell-m)!}{(\ell+m)!}} P_{\ell}^m(\cos \theta) \quad (4)$$

renormalized associated Legendre Polynomial

when $m=0$

✓ We adopt a **reference system with the z axis parallel to the observer velocity**

✓ Adopting a reference system with the z axis parallel (or antiparallel) to the observer velocity, **we are interested only in the non-vanishing coefficients with $m=0$**

✓ The publicly available tools (e.g. HEALPix, Górski et al. 2005) allow us to efficiently compute the $a_{\ell,m}$ coefficients passing from a reference system to another

✓ See Goldstein, J. D. 1984, J. Geophys. Res., 89, 4413 for transformations of spherical harmonics coefficients under rotation

Azimuthal symmetry simplification

Solution in terms of derivatives

T. Trombetti+ 2024

Let us assume that
 $T_{\text{th}}^{\text{BB/dist}}(w)$
 with $w = \cos \theta$
 can be expanded in
 Taylor's series
 around
 $w = \cos(\pi/2)=0$

i.e. the direction
 perpendicular to
 observer motion;

$T_{\text{th}}^{(0)}, T_{\text{th}}', \dots, T_{\text{th}}^{(6)}$
 derivatives
 with respect to w
 evaluated at $w = 0$

$$a_{0,0} = \sqrt{4\pi} \left[T_{\text{th}}^{(0)} + \frac{1}{6} T_{\text{th}}'' + \frac{1}{120} T_{\text{th}}^{(4)} + \frac{1}{5040} T_{\text{th}}^{(6)} \right]$$

monopole: observed \neq intrinsic

$$a_{1,0} = \sqrt{\frac{4\pi}{3}} \left[T_{\text{th}}' + \frac{1}{10} T_{\text{th}}''' + \frac{1}{280} T_{\text{th}}^{(5)} \right],$$

$$a_{2,0} = \frac{1}{3} \sqrt{\frac{4\pi}{5}} \left[T_{\text{th}}'' + \frac{1}{14} T_{\text{th}}^{(4)} + \frac{1}{504} T_{\text{th}}^{(6)} \right],$$

$$a_{3,0} = \frac{1}{15} \sqrt{\frac{4\pi}{7}} \left[T_{\text{th}}''' + \frac{1}{18} T_{\text{th}}^{(5)} \right],$$

Separation:
odd / even
 ℓ & derivatives

$$a_{4,0} = \frac{1}{105} \sqrt{\frac{4\pi}{9}} \left[T_{\text{th}}^{(4)} + \frac{1}{22} T_{\text{th}}^{(6)} \right],$$

$$a_{5,0} = \frac{1}{945} \sqrt{\frac{4\pi}{11}} T_{\text{th}}^{(5)},$$

Danese & De Zotti 1981
but there using
 $\theta=0$ and $\theta=\pi/2$

$$a_{6,0} = \frac{1}{10395} \sqrt{\frac{4\pi}{13}} T_{\text{th}}^{(6)},$$

$D_\ell = (2\ell - 1)D_{\ell-1}$, with $D_0 = 1$
denominator in front of square root

Signal given with respect to v
Link between

derivatives respect to w with
 derivatives with respect to v

$$v' = v(1 - \beta w)/(1 - \beta^2)^{1/2}$$

$$\frac{dT_{\text{th}}}{dw} = \frac{dT_{\text{th}}}{dv'} \frac{dv'}{dw} = \frac{dT_{\text{th}}}{dv'} \frac{-\beta v}{(1 - \beta^2)^{1/2}}$$

$-\beta v/(1 - \beta^2)^{1/2}$ does not contain w .

$$\frac{dT_{\text{th}}^n}{dw^n} = \frac{dT_{\text{th}}^n}{dv'^n} \left[\frac{-\beta v}{(1 - \beta^2)^{1/2}} \right]^n$$

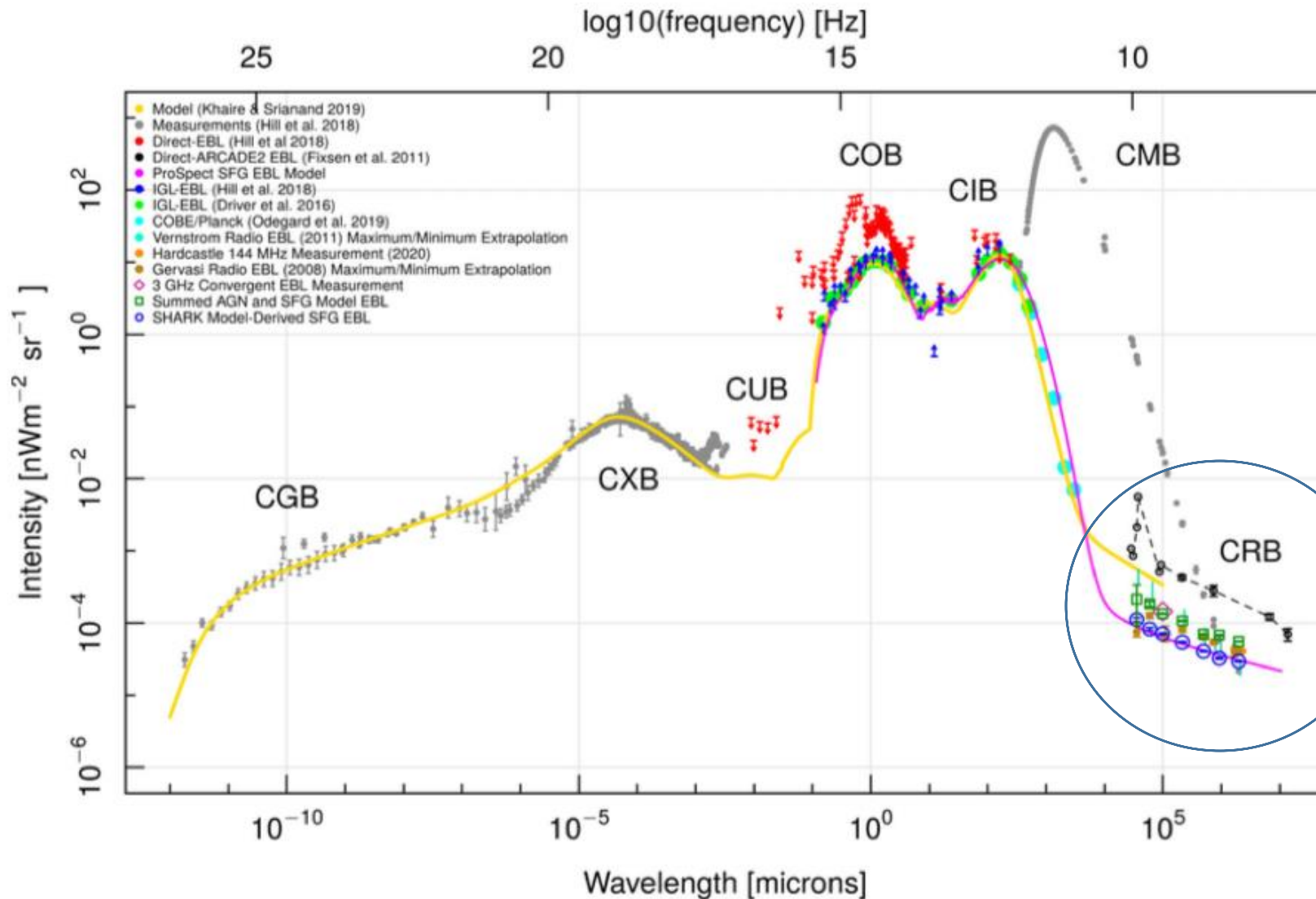
Approximate
 scaling as β^n

Changing β

For a speed $\beta_a \neq \beta$ (ex. $\beta_a > \beta$),
 defining $f_a = \beta_a/\beta$ (ex. $f_a > 1$),
 the ratio between the derivatives
 computed for these two speeds is:

$$\frac{T_{\text{th}}^{(n)}|_{\beta}}{T_{\text{th}}^{(n)}|_{\beta_a}} = f_a^{-n} \left(\frac{1 - \beta_a^2}{1 - \beta^2} \right)^{n/2} R_n$$

$$R_n = \left(\frac{dT_{\text{th}}^n}{dv'^n} \Big|_{v'_{\beta,\perp}} \right) \left(\frac{dT_{\text{th}}^n}{dv'^n} \Big|_{v'_{\beta_a,\perp}} \right)^{-1} \simeq 1$$



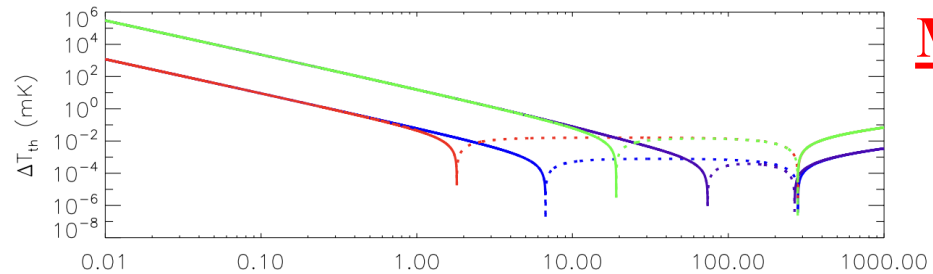
Cosmic Background Spectrum

Tompkins, S. A., et al. 2023, MNRAS, 521, 332

The cosmic radio background from 150 MHz to 8.4 GHz and its division into AGN and star-forming galaxy flux

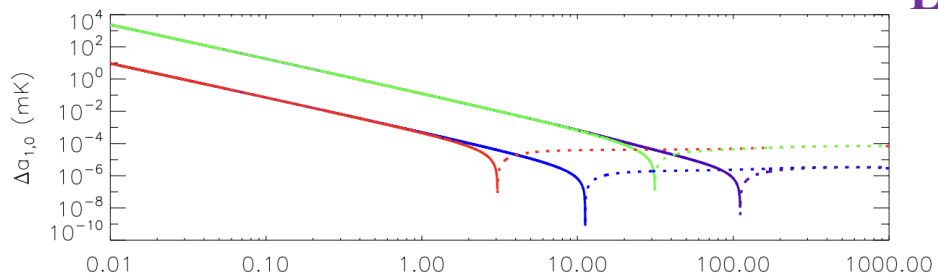
“We can rule out a significant missing discrete source radio population and suggest that the cause of the high ARCADE-2 radio-EBL values may need to be sought either in the foreground subtraction or as a yet unknown diffuse component in the radio sky.”

Figure 7. The complete EBL over the entire measured EM range, including our discrete radio source count measurements along with those from the literature (as indicated in the legend). Also shown is the CMB contribution which dominates at most radio wavelengths and the constraints on the total non-CMB radio EBL from ARCADE2 (black dotted line and open circles). Our model-derived (extrapolated) data points in the radio region are shown as green squares (AGN and SFG) and blue circles (SFG). The solid purple line is the best fitting (dotted) SFG only prediction from Fig. 6.

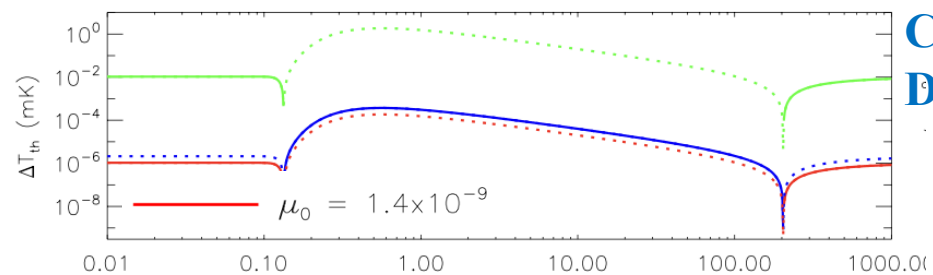


— $u = 2 \times 10^{-6}$ & G00 — $u = 10^{-7}$ & G00

Late

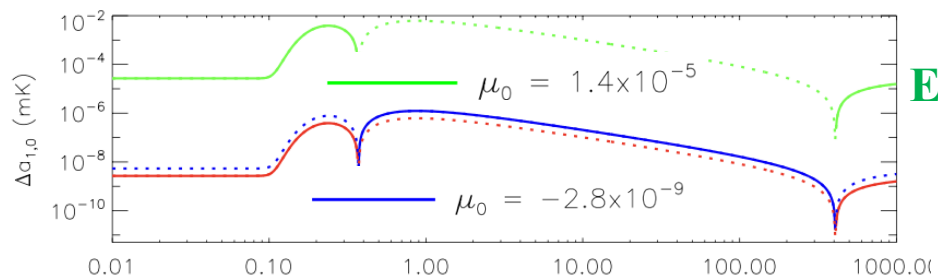


— $u = 10^{-7}$ & Oh — $u = 2 \times 10^{-6}$ & Oh



$\mu_0 = 1.4 \times 10^{-9}$

CMB
Distortions



$\mu_0 = 1.4 \times 10^{-5}$

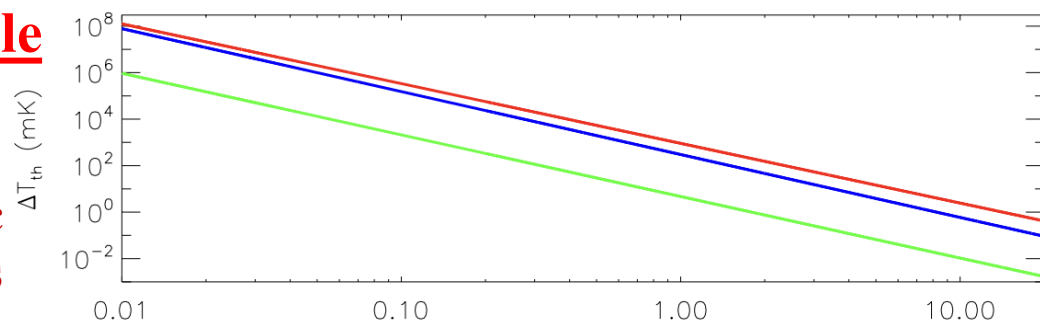
$\mu_0 = -2.8 \times 10^{-9}$

Early

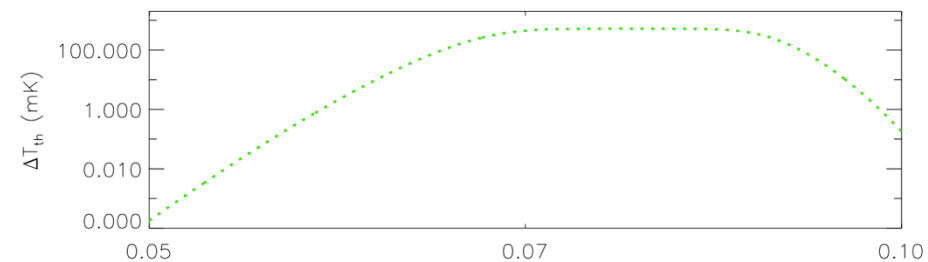
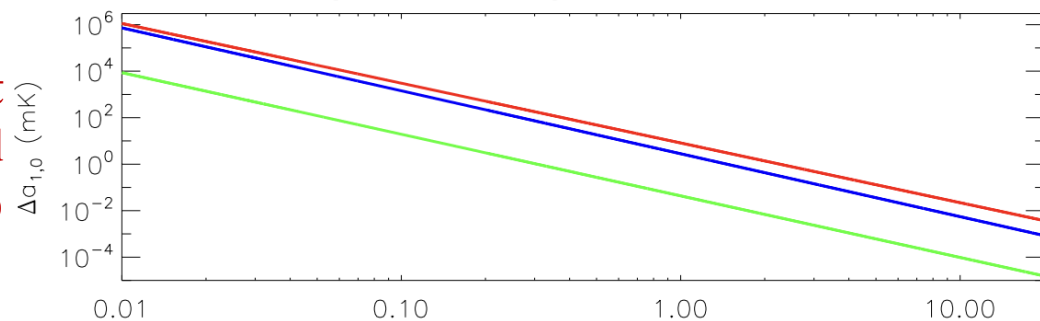
**Monopole & Dipole
Spectrum**

**Extragalactic
Sources
Radio
Background**

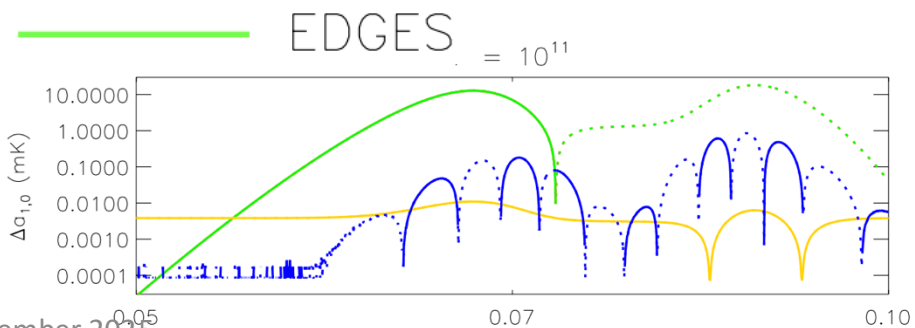
**Dominant
Background
In the Radio**



— Gervasi x 1.3 — ARCADE 2
— High radio background residual



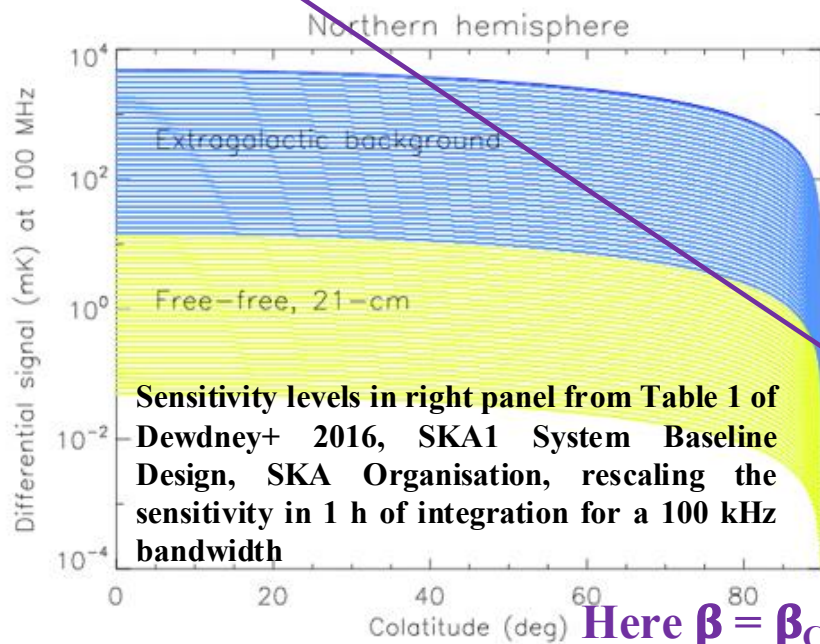
Redshifted
21 cm line



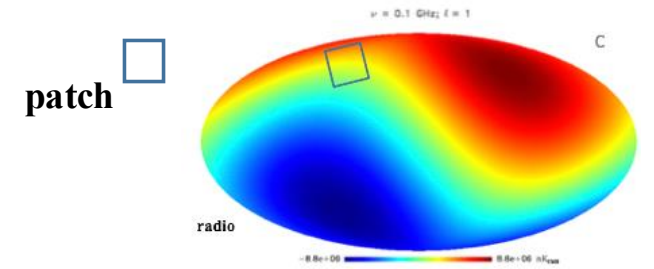
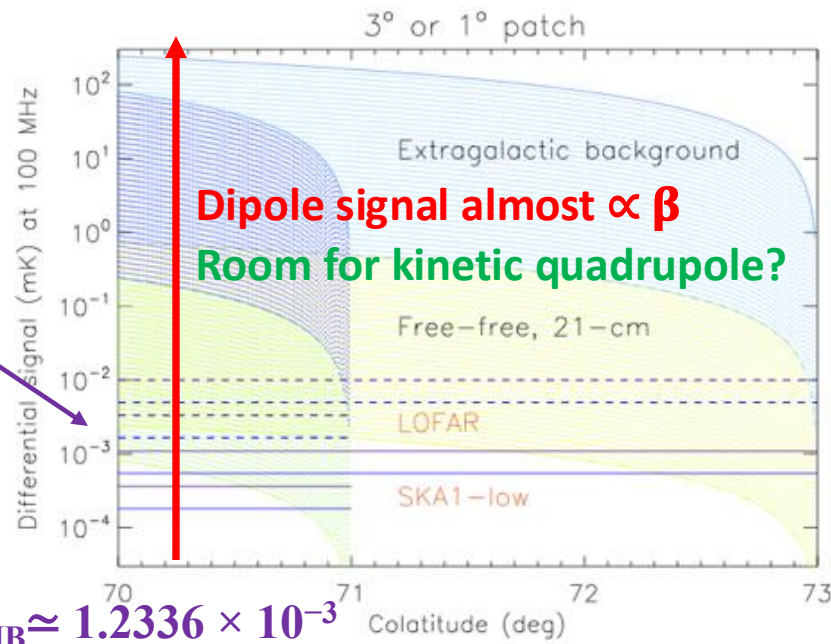
EDGES = 10^{11}

From Trombetti+
2021, AA 646, A75

Sensitivity on 2 arcmin pixel,
1 day of integration, 10 or 40 MHz band



Dipole sensitivity on patches



- ✓ Dealing with almost independently observed sky patches (e.g. interferometric techniques)
- ✓ In principle, for extreme sensitivities, dipole pattern reconstruction could be carried out not necessarily requiring a coherent sky mapping up to the largest scales [Trombetti & Burigana 2019]
- ✓ For example, considering ~50-100 MHz sensitivities to the diffuse signal with forthcoming and future projects
 - ~ several tens of mK could allow to identify the extragalactic background
 - from ~ a few μ K to ~ mK it could be possible to study the reionization imprints

Fig. 5: Range of predicted differential signal for the dipole, $\Delta T(\theta) = \Delta a_{\ell,0} [3/(4\pi)]^{1/2} \cos \theta$, where θ is the colatitude and $\Delta a_{\ell,0}$ refers to the dipole harmonic component $\ell=1$, $m=0$ in a frame with the z-axis parallel to the observer motion, after the subtraction of the standard CMB blackbody, in order to emphasize the interesting signal (here at 100 MHz and in equivalent thermodynamic temperature). The higher part of the blue areas refers to estimates of the signals for the diffuse background from extragalactic radiosources [see e.g. Trombetti+ 2021]; in the lower part it is assumed that sources above certain detection thresholds are subtracted. Yellow areas refer to estimates of the signals for the diffuse free-free distortion, from the minimal prediction accounting for the diffuse IGM contribution to the maximum level corresponding to the integrated contribution from ionized halos, and for various models of the IGM 21-cm redshifted HI line [e.g. Cohen+ 2017]. *Left panel*: the case of an all-sky survey, displayed for simplicity only for a hemisphere. *Right panel*: a zoom of left panel for a patch of 3° (1°); here we display $\Delta T(\theta) - \Delta T(\theta_*)$, with $\theta_* = 73^\circ$ (71°), i.e. the differential signal inside the patch, to be compared with typical sensitivity levels (see also text in Milestones) for LOFAR (dashed lines) and SKA1-low (solid lines) in a nominal pixel of 2 arcmin for one day of integration in the patch. Violet (blue) lines assumes a bandwidth of 10 (40) MHz to appreciate spectral shapes of the 21-cm redshifted HI line (the other types of signal).

Simple estimate: along a meridian in a reference frame with z-axis parallel to the dipole direction, the signal variation at colatitude θ from a dipole pattern with amplitude ΔT in a limited sky area of linear size $\Delta\theta$, has an amplitude $|\Delta T_{\Delta\theta}| \simeq \Delta T \cdot (\Delta\theta/90^\circ) \sin\theta$, with $\sin\theta \simeq 1$ at angles large enough from the poles

Frequency Range SKA-mid (GHz): 0.35 - 14

Sensitivity @ 100 kHz band

Rescaled to 4 GHz bandwidth @ 10GHz

Free-free

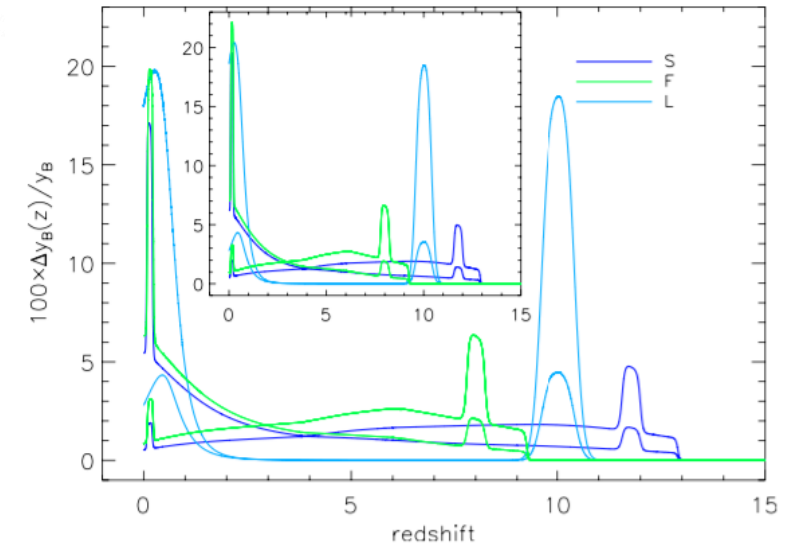
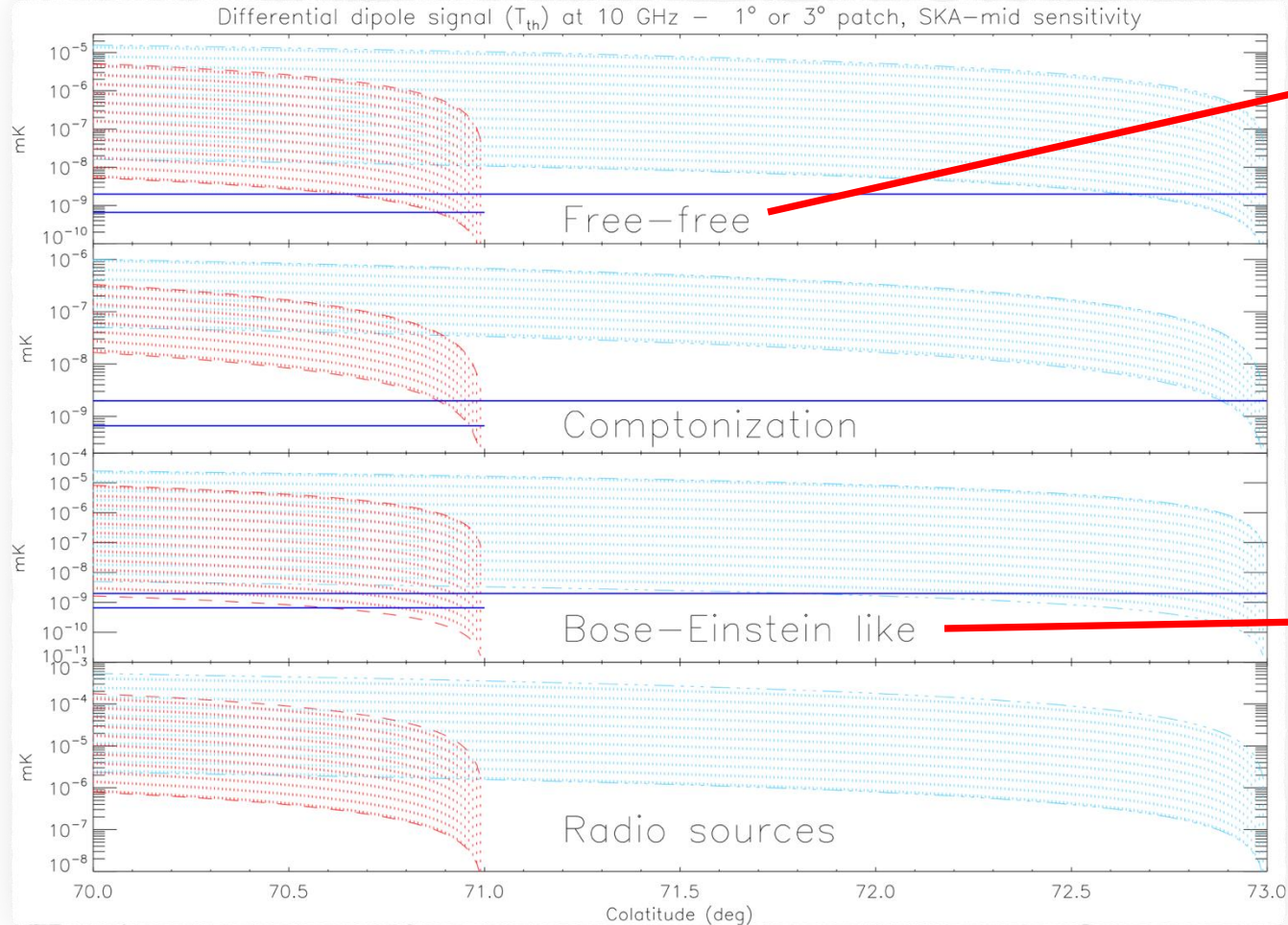


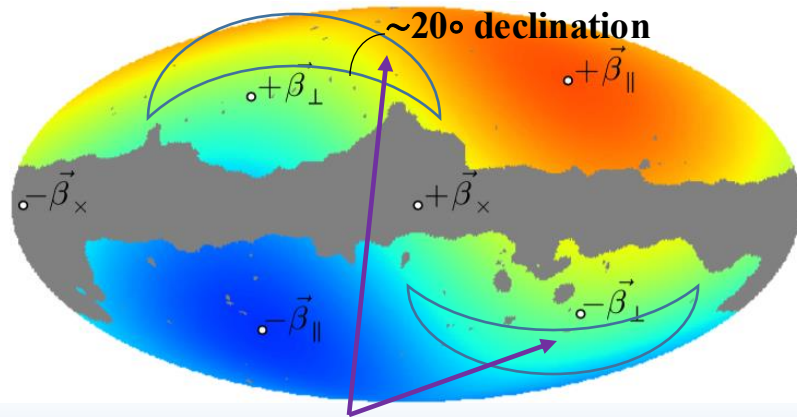
Figure 14. Redshift dependence of the partial contribution to the free-free parameter, evaluated per redshift bin $\Delta z = 0.2$ at each z for $k_{\max} = 100$ (and $k_{\max} = 500$ in the inset). Being normalized to the global value of y_B at each wavelength, $\Delta y_B(z)/y_B$ turns to be essentially independent of the wavelength, thus we present only the result at 10 cm. The dashed-dotted lines display the results found neglecting the clumping, for the corresponding histories reported in legend.

Trombetti & Burigana 2014

**BE: $z \sim 10^3$ recombination or
 $z > 10^5$ kinetic equilibrium era**

Observations & needs

- ✓ ensemble of independent patches, or
- ✓ sky areas from patch assembling with mosaicing techniques to increase differential signal
- ✓ multifrequency (SKA low & mid)
- keeping information on largest scales in the patch or patch assembling (short baselines)



**GOOD
SKY
REGIONS?**

Favourite regions **accessible to SKA** for patch selection should be **far enough from**:

- ✓ Galactic plane, to avoid large contamination
- ✓ maximum & minimum of dipole, because $|\Delta T_{\Delta\theta}| \simeq \Delta T \cdot (\Delta\theta/90^\circ) \sin\theta$
- ✓ bright sources, to avoid large contamination

- Above sensitivities are based on 1.6 (0.18) min of integration on 2 arcmin pixel of a 1deg (3 deg) side patch

- ✓ Likely instrument noise dominated
- ✓ ... but depending on sky area/direction check for source confusion noise

❑ Galactic signal subtraction

➤ Galactic modeling

- Component separation of diffuse signals using multifrequency data (various methods, blind and parametric, have been elaborated ...)

- Considering more patches to increase statistics and mitigate susceptibility to foreground Galactic modeling (... cosmological signal should come from the same dipole pattern in all patches)

➤ Simulations

CMB: nearly all-sky, moderate resolution

SKA: limited sky areas, very high resolution

Potential impact of Galactic diffuse foregrounds

Simulated sky in pixel (p) space

- ❖ **Theoretical model (T)** including boosting with monopole & dipole (& subdominant terms, quadrupole, ...) We consider the **Extragalactic Sources Radio Background** (adopting here the Gervasi+ 2008 model x 1.3)
+
- ❖ **Instrumental Noise (IN) + Source Confusion Noise (SCN)**
 - random Gaussian (RG), with zero mean & variance per pixel *from SKA specifications*/[sensitivity calculator](#)
- +
- ❖ **Potential Residuals from Galactic diffuse foreground (G)**, (parametrically, E_{for} & $E_{\text{for,syst}}$) modelled with two terms:
 - ✓ Stochastic, proportional to Galactic signal amplitude
 - ✓ Systematic, fully correlated with / proportional to Galactic signal

→

$$S(p) = T(p) + (IN(p) + SCN(p)) + E_{\text{for}} \cdot RG(p) \cdot |G(p)| + E_{\text{for,syst}} \cdot G(p)$$

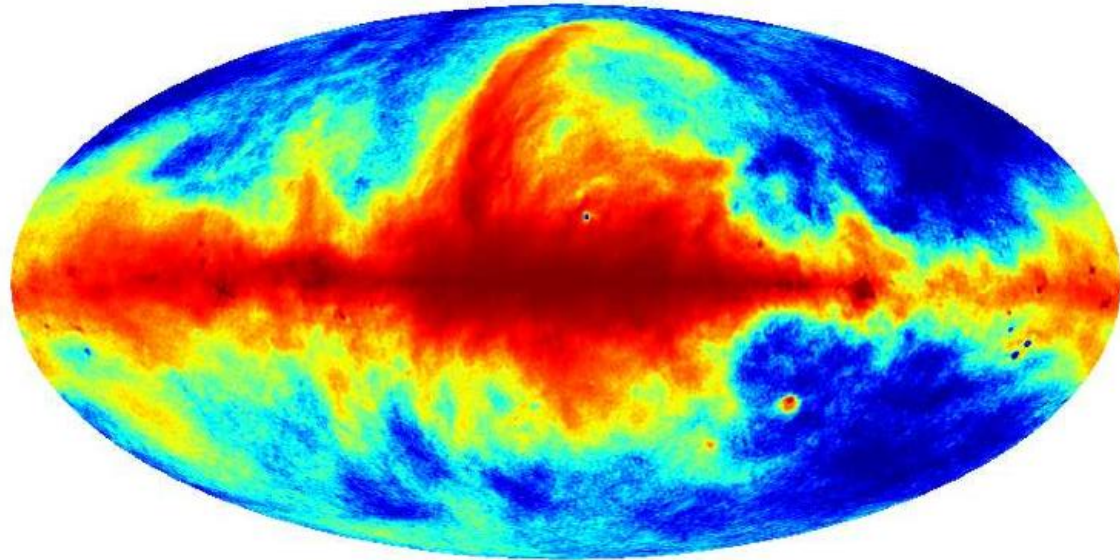
Not so critical

Critical term

Linear fitting on patches

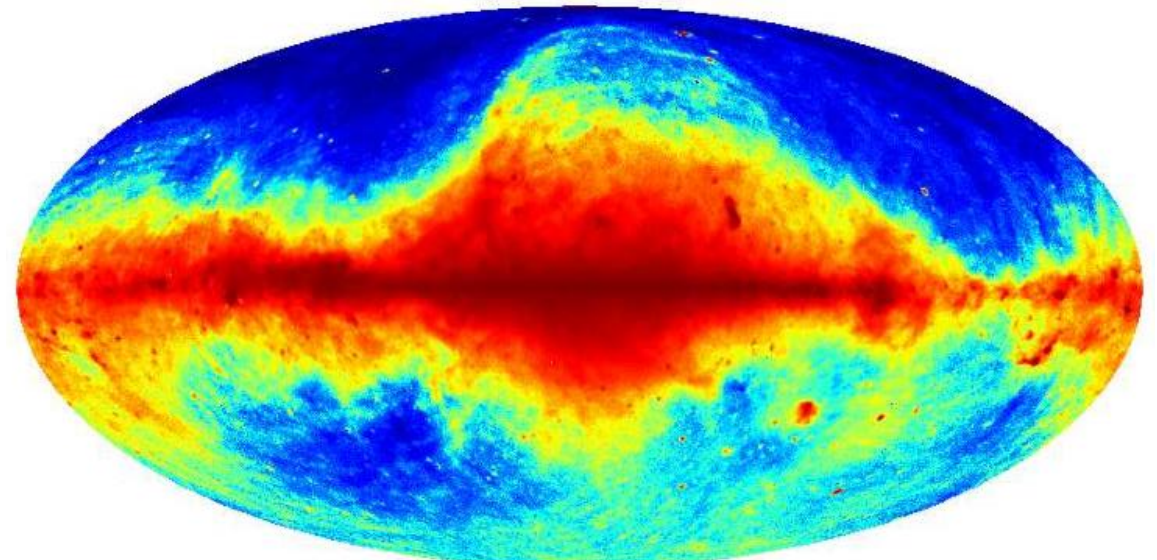
- ❖ Masking according to SKA Low and SKA Mid (band 2) typical Phase 1 cosmological surveys (D.J. Bacon +, Cosmology with Phase 1 of the Square Kilometre Array: Red Book 2018: Technical specifications and performance forecasts, PASA)
- ❖ Fitting just monopole & dipole: linear fit in $\cos(\text{colatitude})$ with z // motion →
intercept → Monopole ; slope → Dipole ; their ratio → v (@ first order)

Galaxy @ 100 MHz, GDSM16 model $n_{\text{side}} = 1024$ no CMB



-1.4 5.1 Log (K CMB)

Galaxy @ 1355 MHz, GDSM16 model $n_{\text{side}} = 1024$ no CMB



-0.92 2.1 Log (K CMB)

Diffuse Galactic emission model

@ SKA Low @ 100 MHz

and

SKA Mid band 2 @ 1.355 GHz from

“An improved model of diffuse galactic radio emission from 10 MHz to 5 THz”, H. Zheng +, 2016, MNRAS

maps @ $n_{\text{side}}=1024$, HEALPix, Gorski+ 2005, 3.4 arcmin

Simulation @ 100 MHz

Test with sensitivity corresponding an integration per FoV of 24h << t_{int} planned for Deep SKA1-LOW Survey

AA*

AA*

307

Degrees

Right Ascension *

51.6

deg

Declination *

-56.0

deg

Minimum Elevation *

20

Continuum

Integration Time *

2.8658951e-5

hours

Central Frequency *

100

MHz

Continuum Bandwidth *

40

MHz

Number of sub-bands *

4

Spectral Resolution

5.43 kHz (16.3 km/s)

Spectral Averaging *

1

Effective resolution

5.43 kHz (16.3 km/s)

Image Weighting *

Briggs

Robust Value

0

Results

Weighted continuum sensitivity

4.75 mJy/beam (1.31)†

Continuum confusion noise

62.49 uJy/beam

Total continuum sensitivity

4.75 mJy/beam

Continuum synthesized beam-size

18.1" x 14.8"

Continuum surface-brightness sensitivity

2160.16 K

Weighted sensitivity per sub-band

10.78 mJy/beam - 8.98 mJy/beam (1.31)†

Confusion noise per sub-band

95.20 uJy/beam - 43.23 uJy/beam

Total sensitivity per sub-band

10.78 mJy/beam - 8.98 mJy/beam

Synthesized beam-size per sub-band

21.3" x 17.4" - 15.7" x 12.9"

Surface-brightness sensitivity per sub-band

4906.14 K - 4085.64 K

Weighted spectral sensitivity

394.40 mJy/beam (1.36)‡

Spectral confusion noise

62.54 uJy/beam

Total spectral sensitivity

394.40 mJy/beam

Spectral synthesized beam-size

18.2" x 14.8"

Spectral surface-brightness sensitivity

179331.56 K

FWHM of the RMSF

0.4 rad/m²

Maximum Faraday depth extent

0.5 rad/m²

Maximum Faraday depth

909.4 rad/m²

AA* only 1.7 times less sensitive than AA4 → no problem!

Subarray Configuration *

AA4

Number of Stations

512

Degrees

Right Ascension *

51.6

deg

Declination *

-56.0

deg

Minimum Elevation *

20

Continuum

Integration Time *

2.8658951e-5

hours

Central Frequency *

100

MHz

Continuum Bandwidth *

40

MHz

Number of sub-bands *

4

Spectral Resolution

5.43 kHz (16.3 km/s)

Spectral Averaging *

1

Effective resolution

5.43 kHz (16.3 km/s)

Image Weighting *

Briggs

Robust Value

0

Results

Weighted continuum sensitivity

2.80 mJy/beam (1.29)†

Continuum confusion noise

63.39 uJy/beam

Total continuum sensitivity

2.80 mJy/beam

Continuum synthesized beam-size

18.8" x 14.5"

Continuum surface-brightness sensitivity

1255.51 K

Weighted sensitivity per sub-band

6.36 mJy/beam - 5.29 mJy/beam (1.29)†

Confusion noise per sub-band

96.55 uJy/beam - 43.87 uJy/beam

Total sensitivity per sub-band

6.36 mJy/beam - 5.29 mJy/beam

Synthesized beam-size per sub-band

22.1" x 17.1" - 16.3" x 12.6"

Surface-brightness sensitivity per sub-band

2851.24 K - 2374.28 K

Weighted spectral sensitivity

230.91 mJy/beam (1.33)‡

Spectral confusion noise

67.78 uJy/beam

Total spectral sensitivity

230.91 mJy/beam

Spectral synthesized beam-size

19.5" x 15.0"

Spectral surface-brightness sensitivity

96668.37 K

FWHM of the RMSF

0.4 rad/m²

Maximum Faraday depth extent

0.5 rad/m²

Maximum Faraday depth

909.4 rad/m²

for the same resolution element

← →

Subarray Configuration *

AA4 (core only)

Number of Stations

224

Degrees

Right Ascension *

51.6

deg

Declination *

-56.0

deg

Minimum Elevation *

20

Continuum

Integration Time *

2.8658951e-5

hours

Central Frequency *

100

MHz

Continuum Bandwidth *

40

MHz

Number of sub-bands *

4

Spectral Resolution

5.43 kHz (16.3 km/s)

Spectral Averaging *

1

Effective resolution

5.43 kHz (16.3 km/s)

Image Weighting *

Briggs

Robust Value

0

Results

Weighted continuum sensitivity

8.28 mJy/beam (1.67)†

Continuum confusion noise

58.69 mJy/beam

Total continuum sensitivity

59.27 mJy/beam

Continuum synthesized beam-size

490.4" x 406.5"

Continuum surface-brightness sensitivity

36.34 K

Weighted sensitivity per sub-band

18.81 mJy/beam - 15.66 mJy/beam (1.67)†

Confusion noise per sub-band

95.04 mJy/beam - 38.24 mJy/beam

Total sensitivity per sub-band

96.88 mJy/beam - 41.32 mJy/beam

Synthesized beam-size per sub-band

576.9" x 478.2" - 426.4" x 353.5"

Surface-brightness sensitivity per sub-band

59.40 K - 25.33 K

Weighted spectral sensitivity

614.04 mJy/beam (1.55)‡

Spectral confusion noise

63.67 mJy/beam

Total spectral sensitivity

617.33 mJy/beam

Spectral synthesized beam-size

508.3" x 420.2"

Spectral surface-brightness sensitivity

353.19 K

FWHM of the RMSF

0.4 rad/m²

Maximum Faraday depth extent

0.5 rad/m²

Maximum Faraday depth

909.4 rad/m²

AA4 (core only) about 80 times less sensitive than AA4 ... but confusion noise → about 600 times less sensitive than AA4

Warning: You are approaching the confusion limit given the synthesized beam-size and frequency.

Simulation @ 1.355 GHz Mid band 2

Test with sensitivity
corresponding
an integration of
10000 h on
5000 sq. deg
planned for
Medium-Deep
Band 2 Survey
Where? How?
N.B. integration time
of Wide Band 1 Survey
SKA1-Mid in Band 1
approximately
10000 hrs
on 20000 sq. deg.
i.e. about half sky

Bacon+2020

Observing Band *
Band 2 (0.95 - 1.76 GHz)

Weather (Precipitable Water Vapour) *
10

Subarray Configuration *
AA4

Number of 15-m antennas
133

Number of 13.5-m antennas
64

13.5-m antennas only cover 0.95-1.67 GHz

Degrees
☒

Right Ascension *
51.6 deg

Declination *
-56 deg

Elevation *
45 deg

Advanced ☐

Continuum

Supplied
Integration Time
2.1e-5 min

Central Frequency *
1.355 GHz

Continuum Bandwidth *
0.63 GHz

Number of sub-bands *
1

Spectral Resolution
13.44 kHz (3.0 km/s)

Spectral Averaging *
1

Effective Resolution
13.44 kHz (3.0 km/s)

Image Weighting *
Briggs

Robust *
0

Tapering *
No tapering

Results

Weighted continuum sensitivity
2.06 mJy/beam (1.35)†

Continuum confusion noise
0.00 Jy/beam

Total continuum sensitivity
2.06 mJy/beam

Continuum synthesized beam-size
0.75" x 0.67"

Continuum surface-brightness sensitivity
2713.53 K

Weighted spectral sensitivity
441.03 mJy/beam (1.33)‡

Spectral confusion noise
0.00 Jy/beam

Total spectral sensitivity
441.03 mJy/beam

Spectral synthesized beam-size
0.79" x 0.70"

Spectral surface-brightness sensitivity
533847.10 K

FWHM of the RMSF
68.10 rad/m²

Maximum Faraday Depth Extent
97.49 rad/m²

Maximum Faraday depth
806488.90 rad/m²

Activit

Observing Band *
Band 2 (0.95 - 1.76 GHz)

Weather (Precipitable Water Vapour) *
10

Subarray Configuration *
AA*

Number of 15-m antennas
80

Number of 13.5-m antennas
64

13.5-m antennas only cover 0.95-1.67 GHz

Degrees
☒

Right Ascension *
51.6 deg

Declination *
-56 deg

Elevation *
45 deg

Advanced ☐

Continuum

Supplied
Integration Time
2.1e-5 min

Central Frequency *
1.355 GHz

Continuum Bandwidth *
0.63 GHz

Number of sub-bands *
1

Spectral Resolution
13.44 kHz (3.0 km/s)

Spectral Averaging *
1

Effective Resolution
13.44 kHz (3.0 km/s)

Image Weighting *
Briggs

Robust *
0

Tapering *
No tapering

Results

Weighted continuum sensitivity
3.02 mJy/beam (1.40)†

Continuum confusion noise
41.59 nJy/beam

Total continuum sensitivity
3.02 mJy/beam

Continuum synthesized beam-size
1.98" x 1.72"

Continuum surface-brightness sensitivity
590.97 K

Weighted spectral sensitivity
656.12 mJy/beam (1.40)‡

Spectral confusion noise
54.66 nJy/beam

Total spectral sensitivity
656.12 mJy/beam

Spectral synthesized beam-size
2.12" x 1.87"

Spectral surface-brightness sensitivity
109766.16 K

FWHM of the RMSF
68.10 rad/m²

Maximum Faraday Depth Extent
97.49 rad/m²

Maximum Faraday depth
806488.90 rad/m²

† Weighting correction factor (30% bandwidth)

Observing Band *
Band 2 (0.95 - 1.76 GHz)

Weather (Precipitable Water Vapour) *
10

Subarray Configuration *
AA4 (MID_inner_r125m)

Number of 15-m antennas
22

Number of 13.5-m antennas
9

13.5-m antennas only cover 0.95-1.67 GHz
Covers inner radius of 125m

Degrees
☒

Right Ascension *
51.6 deg

Declination *
-56 deg

Elevation *
45 deg

Advanced ☐

Continuum

Supplied
Integration Time
2.1e-5 min

Central Frequency *
1.355 GHz

Continuum Bandwidth *
0.63 GHz

Number of sub-bands *
1

Spectral Resolution
13.44 kHz (3.0 km/s)

Spectral Averaging *
1

Effective Resolution
13.44 kHz (3.0 km/s)

Image Weighting *
Briggs

Robust *
0

Tapering *
No tapering

Results

Weighted continuum sensitivity
14.88 mJy/beam (1.52)†

Continuum confusion noise
536.01 µJy/beam

Total continuum sensitivity
14.89 mJy/beam

Continuum synthesized beam-size
151.48" x 115.79"

Continuum surface-brightness sensitivity
565.04 mK

Weighted spectral sensitivity
2.76 Jy/beam (1.30)‡

Spectral confusion noise
798.15 µJy/beam

Total spectral sensitivity
2.76 Jy/beam

Spectral synthesized beam-size
182.27" x 133.10"

Spectral surface-brightness sensitivity
75.68 K

FWHM of the RMSF
68.10 rad/m²

Maximum Faraday Depth Extent
97.49 rad/m²

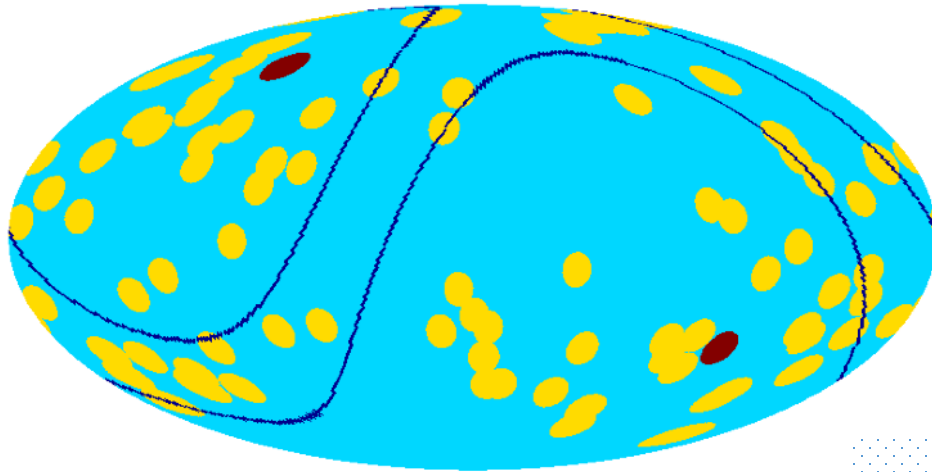
Maximum Faraday depth
806488.90 rad/m²

T. Trombetti & C. Burigana, Bologna, Italy, 24-28 November 2025

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“Good” sky regions - Results @ 100 MHz & 1.355 GHz

Stochastic residuals only: $\underline{E}_{\text{for}} = 0.05$



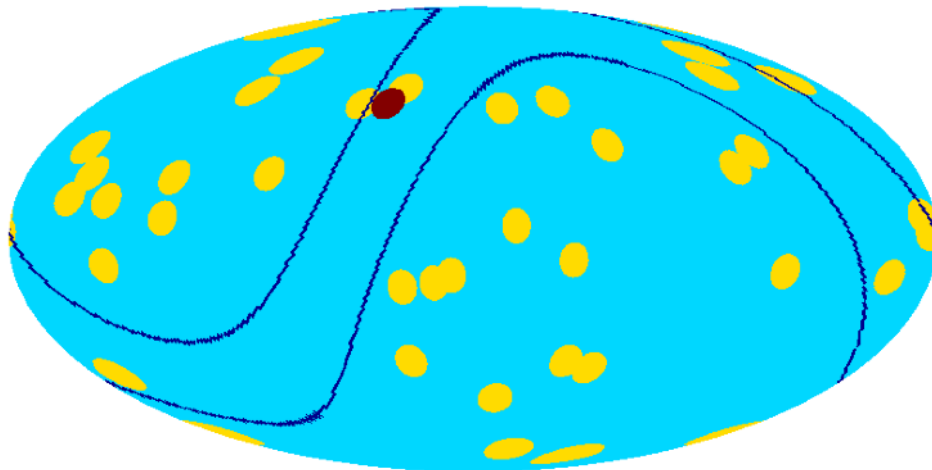
Blue lines corresponding to Dec of 30°, 0°
(Galactic coords, Mollweide projection)

Considering 49152
($n_{\text{side}}=64$, HEALPix, Gorski+ 2005)
centres of 100 sq deg circular patches

100 MHz - Rel Err on $\nu \leq 5\%$

60 and 30 patches

respectively for the two cuts in declinations,
with a retrieved relative error on β , on average,
of about 2.3%



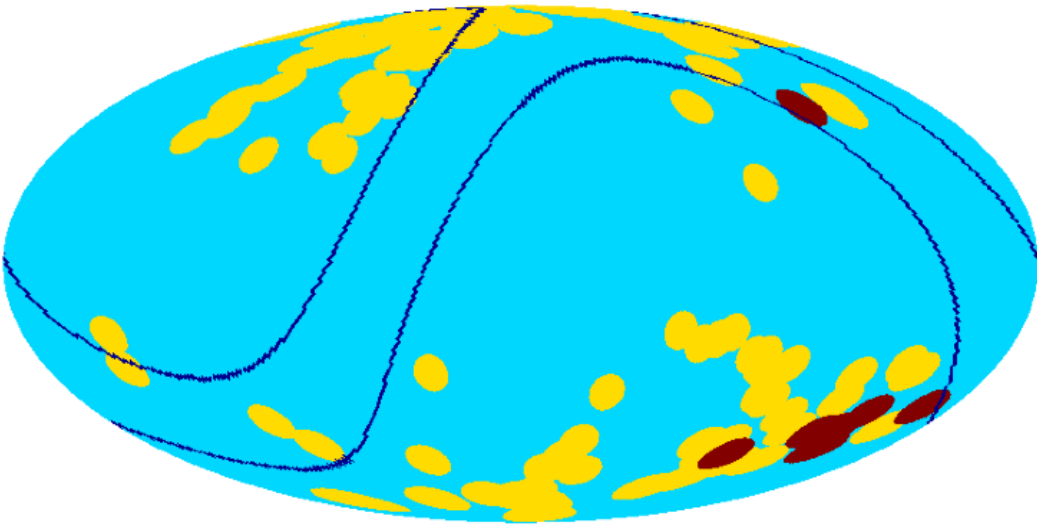
1.355 GHz - Rel Err on $\nu \leq 10\%$

26 and 18 patches

respectively for the two cuts in declinations,
with a retrieved relative error on β , on average,
of about 5.8%

“Good” sky regions - Results @ 100 MHz & 1.355 GHz

Systematic residuals only: $\underline{E_{\text{for,syst}} = 0.03}$

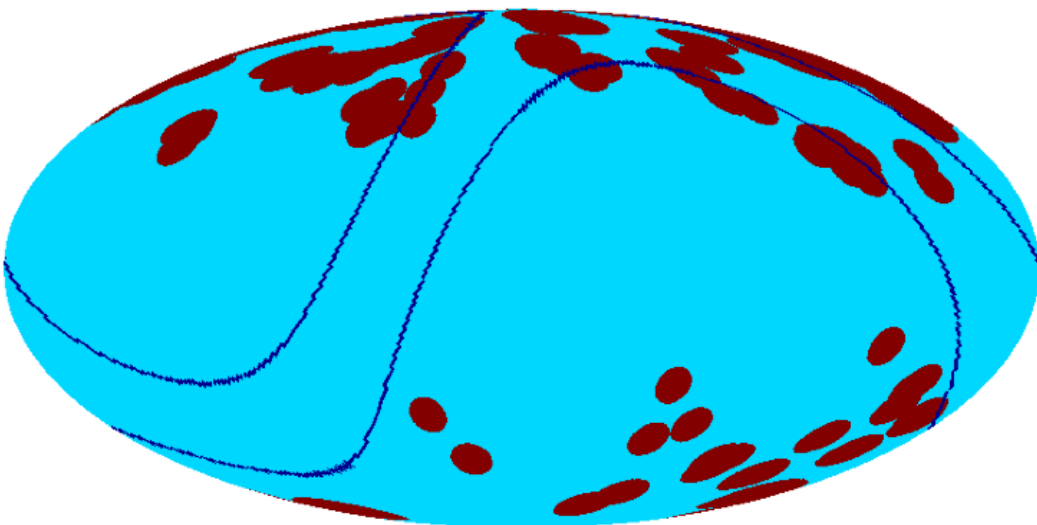


Blue lines corresponding to Dec of 30°, 0°
(Galactic coords, Mollweide projection)

100 MHz - Rel Err on $v \leq 20\%$

78 and 61 patches

respectively for the two cuts in declinations,
with a retrieved relative error on β , on average,
of about 15%



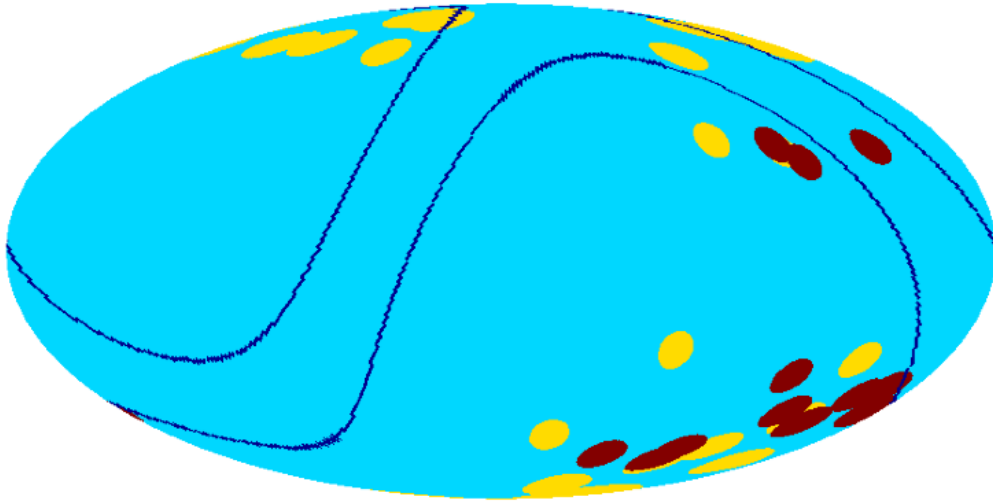
1.355 GHz - Rel Err on $v \leq 85\%$

60 and 40 patches

respectively for the two cuts in declinations,
with a retrieved relative error on β , on average,
of about 84%

“Good” sky regions - Results @ 100 MHz & 1.355 GHz

Combination of stochastic & systematic residuals: $\underline{E_{\text{for}} = 0.03}$ & $\underline{E_{\text{for,syst}} = 0.01}$



Blue lines corresponding to Dec of 30°, 0°
(Galactic coords, Mollweide projection)

100 MHz - Rel Err on $\nu \leq 5\%$

25 and 23 patches

respectively for the two cuts in declinations,
with a retrieved relative error on β , on average,
of about 4.2%

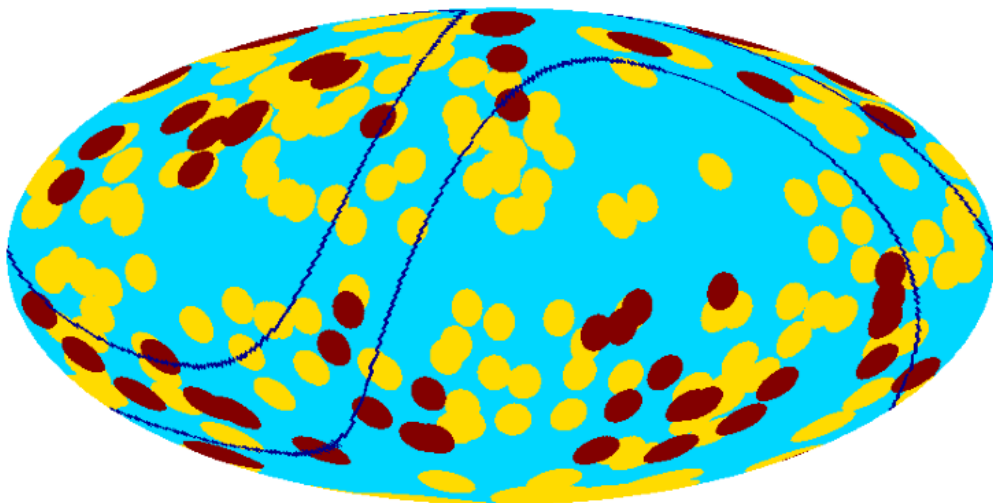
Red: most favourite patches, relative error less
than 1.2 x minimum relative error ($\approx 3.5\%$)

1.355 GHz - Rel Err on $\nu \leq 50\%$

146 and 96 patches

respectively for the two cuts in declinations,
with a retrieved relative error on β , on average,
of about 37%

Red: most favourite patches, relative error less
than 1.2 x minimum relative error ($\approx 26\%$)



Conclusions

- ❖ Differential methods relying on precise interfrequency calibration are promising
- ❖ For observations at extreme sensitivity/resolution, the differential method can be applied to sky patches or limited sky areas, as e.g. in the case SKA interferometric observation, for analyses on background spectra and tests on cosmic dipole
- ❖ The integrated signal from Extragalactic Sources (likely) gives the major contribution to the CRB dipole analyses compared with estimates for various high flux density limits will test consistency of dipole/monopole versus β from CMB
- ❖ Extracting dipole/monopole information from diffuse CRB on selected sky patches / areas:
 - testing v at few or some % accuracy level is feasible ...
 - provided that residuals of Galactic diffuse emission are within or below a few %
- ❖ Collecting many patches (or observing a large sky area) allows:
 - at least: improvement of S/N
 - furthermore: exploiting larger angular scales directly improves sensitivity on dipole
- ❖ Frequency modulations of CRB dipole spectrum are informative β for other types of signals, tomographic in nature (21cm) or mainly contributed at certain redshifts