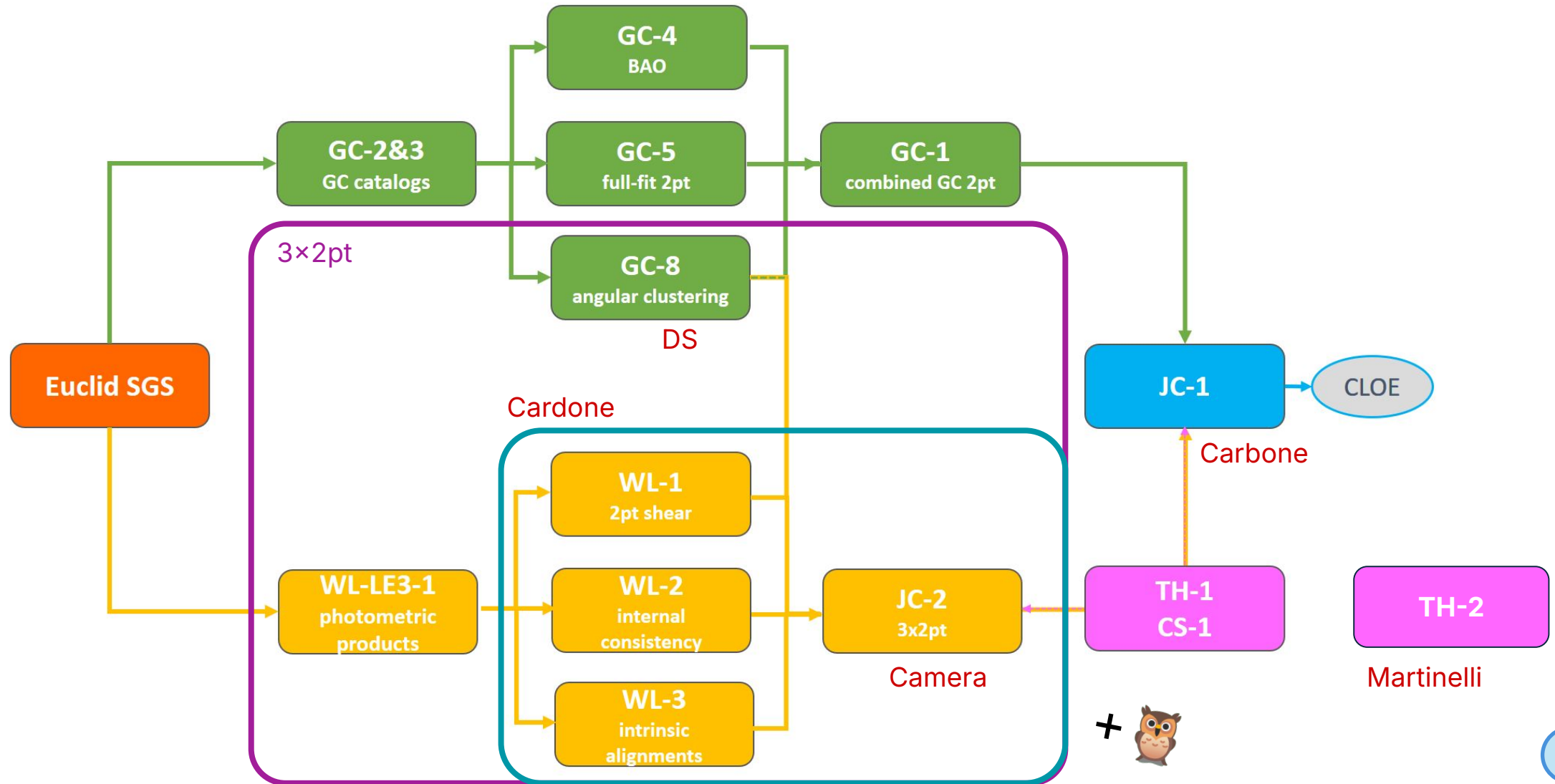


3x2pt (+HOWLS) science

Davide Sciotti (+ many others!)

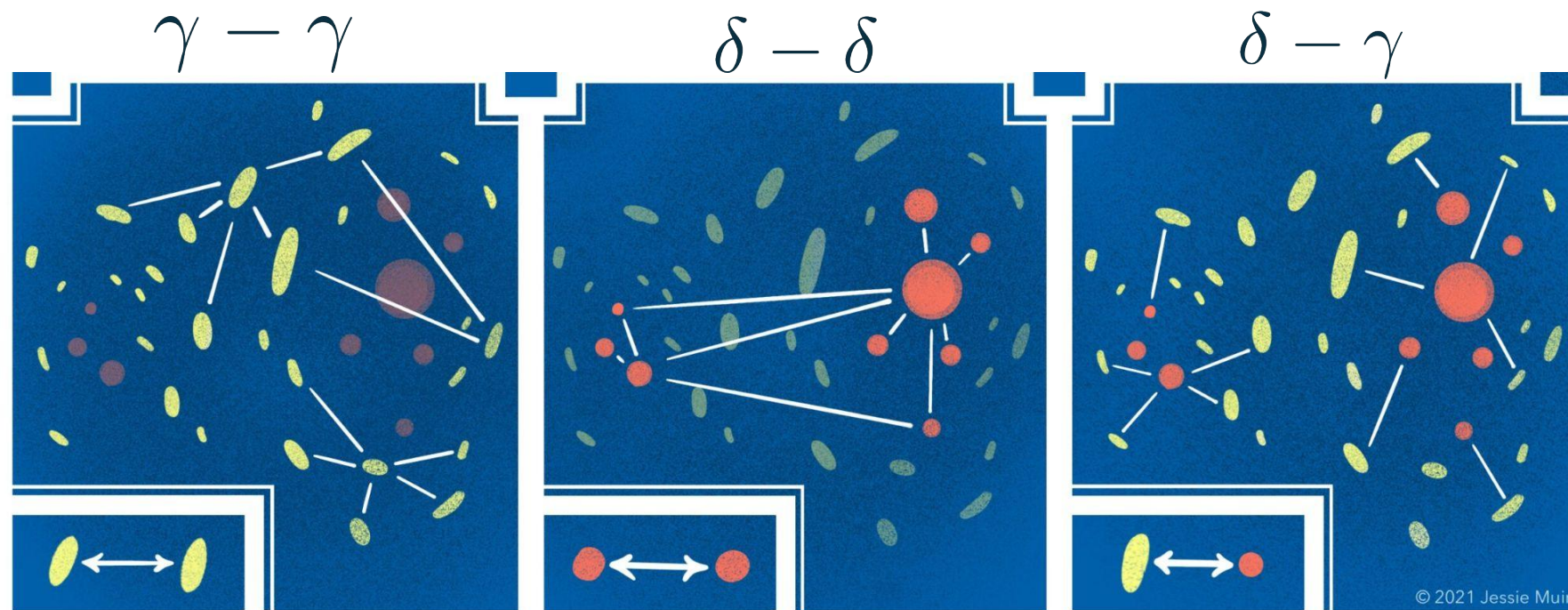
Euclid Italia 2025

KP structure and interactions



3x2pt photometric observables

- **3x** (WL, GCph, GGL) **2pt** *angular* CF/PS
- Fundamental quantities: **positions** (ra, dec, z) and **shapes** (e_1 , e_2)



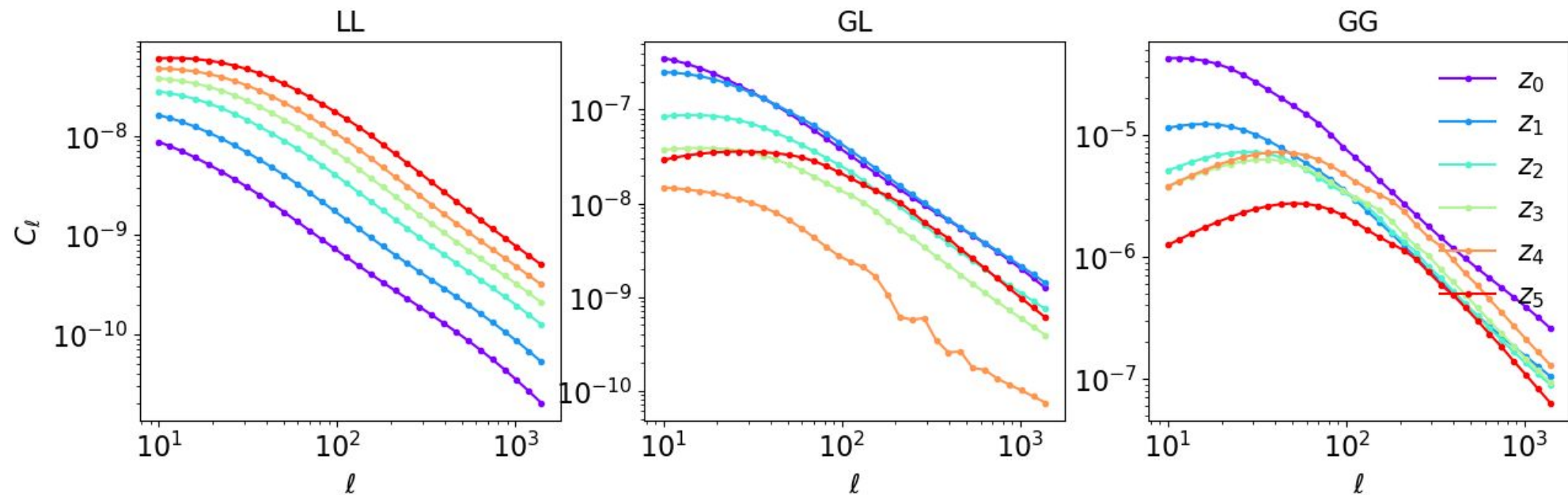
Theoretical modelling: HS

- Tracers of (density, shear) field $\rightarrow$ SHT $\rightarrow a_{\ell m} \rightarrow C_\ell$
- Complete summary if fields are Gaussian (they are not!)

$$C_{ij}^{AB}(\ell) = \int dz \frac{c W_i^A(z) W_j^B(z)}{H(z) f_K^2[r(z)]} P_{AB} \left[\frac{\ell + 1/2}{f_K[r(z)]}, z \right]$$

- Radial projection of the matter PS, weighted by probe-specific radial kernels
- Depend on geometry, expansion history, initial conditions...

Cl_s



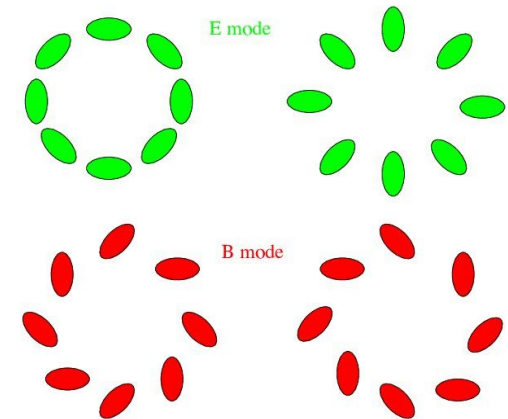
Theoretical modelling: CS

- HS: modelling
 - multipoles are uncorrelated
- CS: data
 - Mask effects (bright stars, PSF residuals, angular systematics) are local
 - We directly measure angles and physical separations
- Can map one into the other with a (numerically challenging) Hankel transform
- Additional 2pt statistics: COSEBIs, bandpowers, ...

$$\xi_{ij}^{\pm}(\theta) \simeq \frac{1}{2\pi} \int_{\ell_{\text{low}}}^{\ell_{\text{top}}} \ell J_{2\mp 2}(\ell\theta) C_{ij}^{\text{LL}}(\ell) d\ell$$

$$\xi_{ij}^{\text{GG}}(\theta) \simeq \frac{1}{2\pi} \int_{\ell_{\text{low}}}^{\ell_{\text{top}}} \ell C_{ij}^{\text{GG}}(\ell) J_0(\ell\theta) d\ell,$$

$$\xi_{ij}^{\text{GL}}(\theta) \simeq \frac{1}{2\pi} \int_{\ell_{\text{low}}}^{\ell_{\text{top}}} \ell C_{ij}^{\text{GL}}(\ell) J_2(\ell\theta) d\ell,$$



Systematics: WL

- **IA**
 - input: IA model, associated params
- **Multiplicative shear bias (residual):**
 - input: m-bias values
- **$\mathbf{dz}_i$: redshift distribution shifts**
 - input: dz (WL) values

$$e_{\text{obs}} = e_{\text{int}} + \gamma + e_{\text{IA}}$$

$$\hat{\gamma} = (1 + m) \gamma$$

$$\begin{cases} C_{ij}^{\text{LL}}(\ell) \rightarrow (1 + m_i)(1 + m_j) C_{ij}^{\text{LL}}(\ell), \\ C_{ij}^{\text{GL}}(\ell) \rightarrow (1 + m_j) C_{ij}^{\text{GL}}(\ell), \\ C_{ij}^{\text{GG}}(\ell) \rightarrow C_{ij}^{\text{GG}}(\ell), \end{cases}$$

$$n^i(z) = n_{pz}^i(z - \Delta z^i)$$

Systematics: GCph

- **Galaxy bias (linear and nonlinear)!**

- input: $b_i^{\text{photo}}(z)$

- **RSD**

- input: growth rate, galaxy bias

- **Magnification bias**

- input: luminosity function (log) slope (for a flux-limited sample)

- **dz_i** : redshift distribution shifts

- input: dz (GCph) values

- **σz_i** : redshift distribution stretch

- input: σz (GCph) values

$$P_{\text{gg}}^{\text{photo}}(k, z) = [b^{\text{photo}}(z)]^2 P_{\text{m}}(k, z)$$

$$W_i^{\text{RSD}}(\ell, z) = \sum_{m=-1}^{+1} \frac{L_m(\ell) H[z_m(\ell, z)] f_g[z_m(\ell, z)] n_i^L[z_m(\ell, z)]}{c b_g^{\text{photo}}[z_m(\ell, z)]}$$

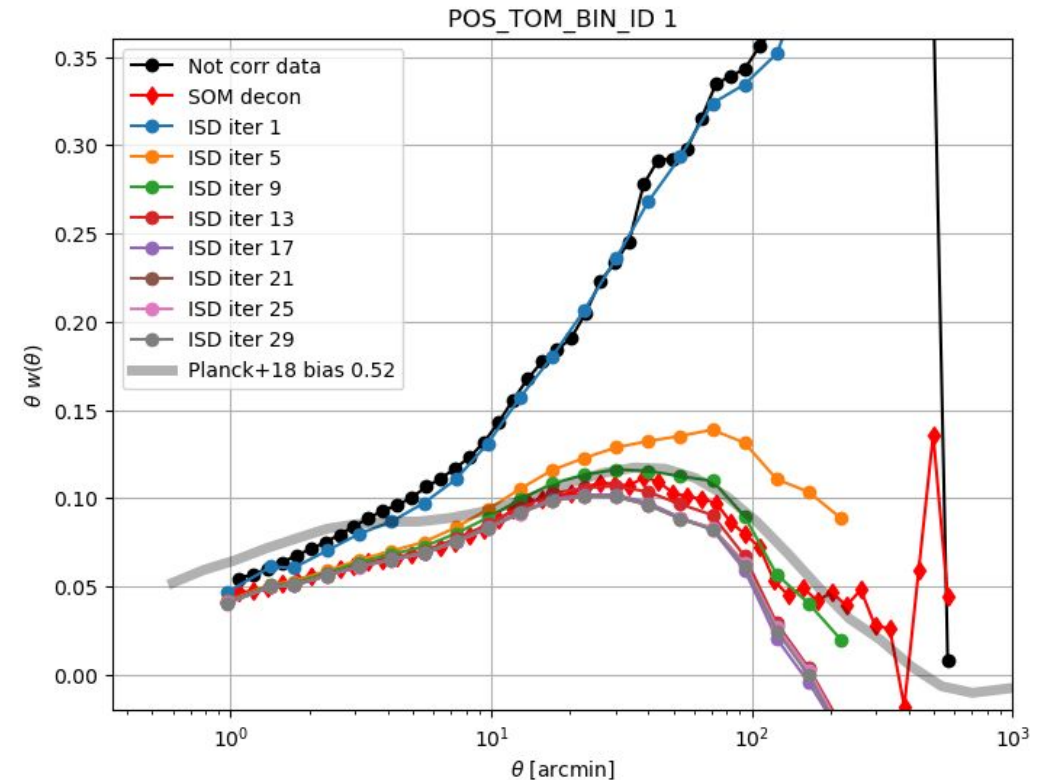
$$b_{\text{mag}}(z) = 5 s(z) - 2$$

$$n^i(z) = n_{pz}^i(z - \Delta z^i)$$

$$n^i(z) = \frac{1}{\sigma z^i} n_{pz}^i \left(\frac{z - \langle z \rangle}{\sigma z^i} + \langle z \rangle \right)$$

Other systematics

- **Spatially varying survey properties**
 - Non-uniform depth, reddening, extinction, stellar contamination...
 - Accounted for in the visibility map (e.g. ISD)
- **PSF**
 - Additive bias (c): leakage of PSF anisotropy → spurious B-modes
 - Multiplicative bias (m): misestimation of PSF size → biased shear amplitude



Credit: J. M. Perez, VMPZ-ID

Other systematics

- **Shot noise**
 - Due to discrete sampling of matter field
 - Accounted for in the analytical covariance
- **Shape noise**
 - Due to intrinsic ellipticity dispersion
 - Accounted for in the analytical covariance
- **Nonlinear clustering**
 - Marginalised over/mitigated with scale cuts
- **Baryonic effects**
 - Marginalised over/mitigated with scale cuts

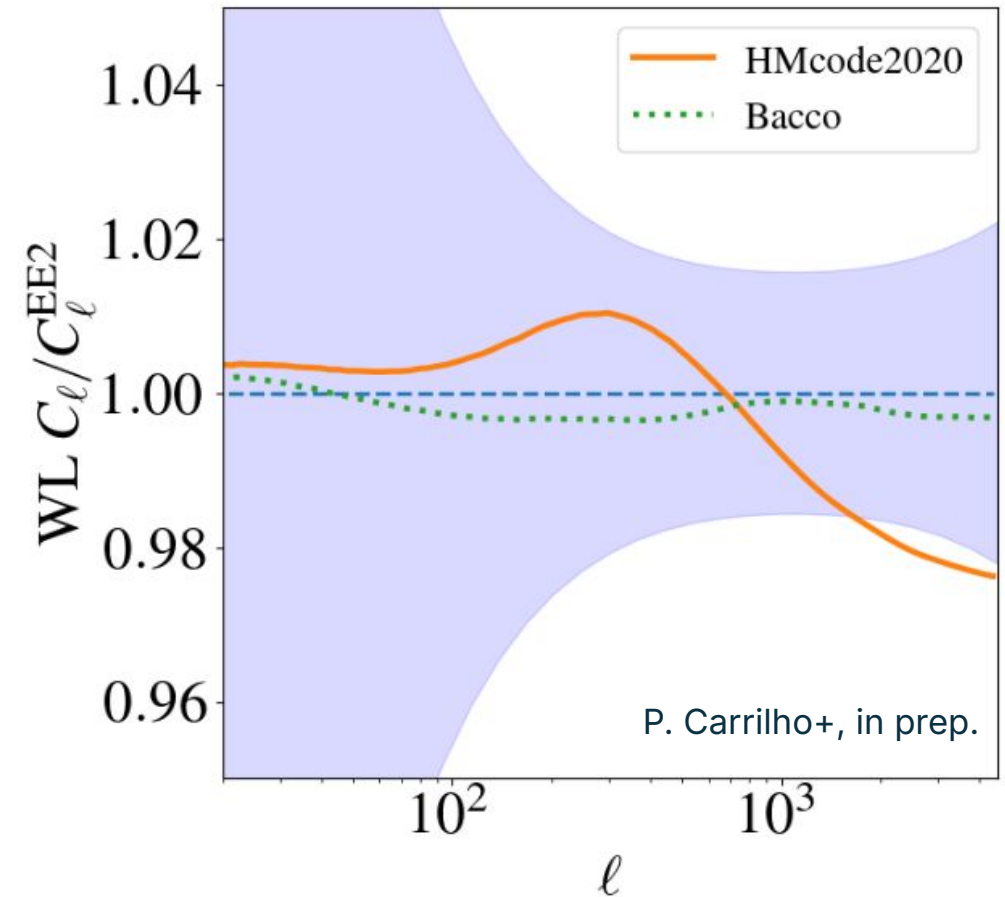
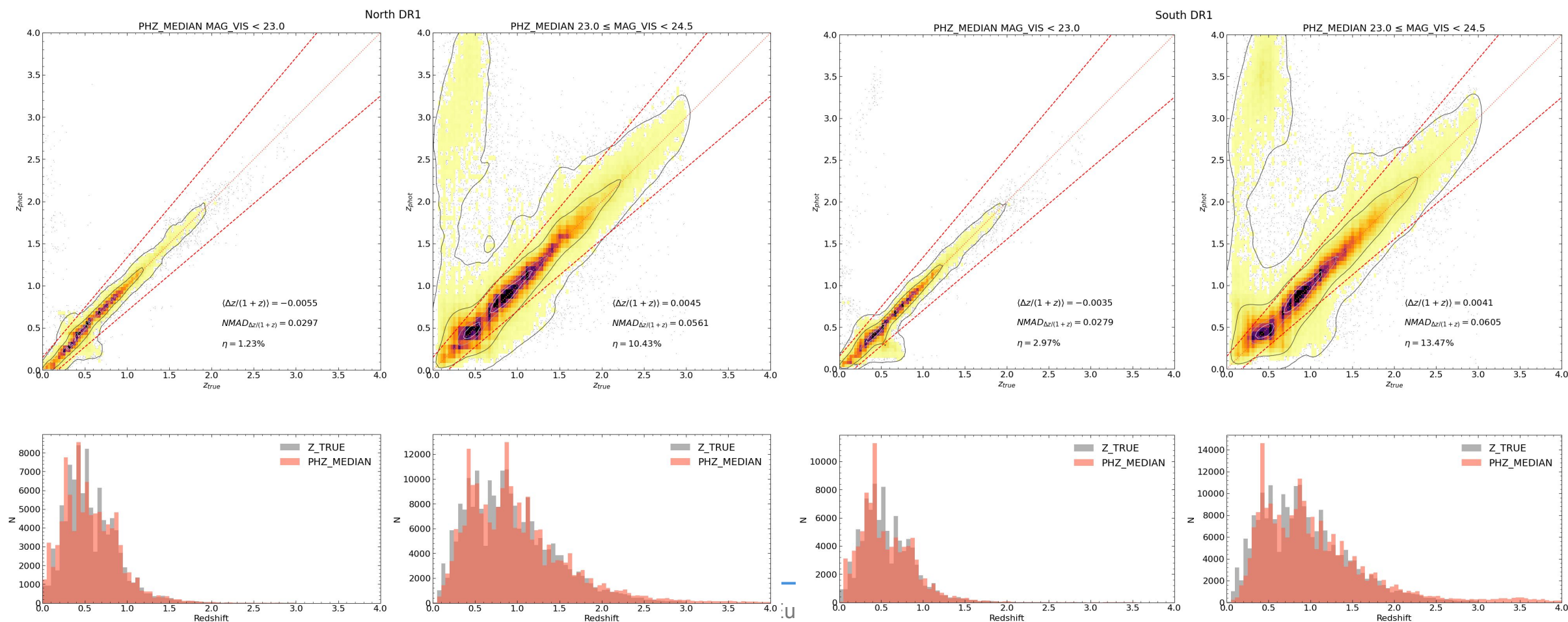


Photo-z

Template-fitting with Phosphoros

Credits:
M. Bolzonella,
C. Carbone



Towards DR1 analysis: tasks

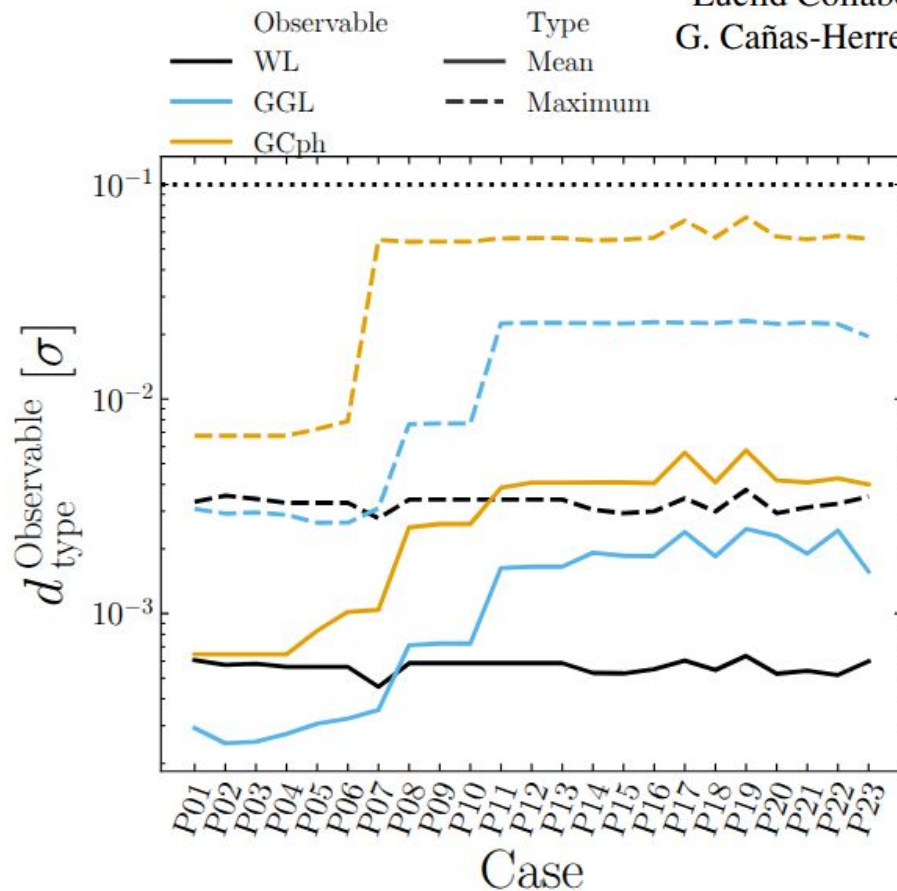
- Pipeline development
 - Observables & likelihood: cloelib + cloelike ✓ / ⚠
 - Covariance: Spaceborne ✓
 - Data IO: euclidlib ✓
- Pipeline validation:
 - Against independent codes ✓
 - Using simulations (FS2) ✓ / ⚠
 - Using (real!) data ⚠
- Analysis choices ⚠
 - Sample selection, nonlinear modelling, systematics, scale cuts, priors...
 - Optimize in terms of **bias** and **constraining** power (FoB and FoM)
- Data exploration (RR2) ⚠
 - Sources of spurious correlation
 - Star-galaxy separation
 - Impact of catalogue selection (depth, phz quality...)
 - Internal consistency (splits, N/S...)
 - ...

CLOE(lib) validation

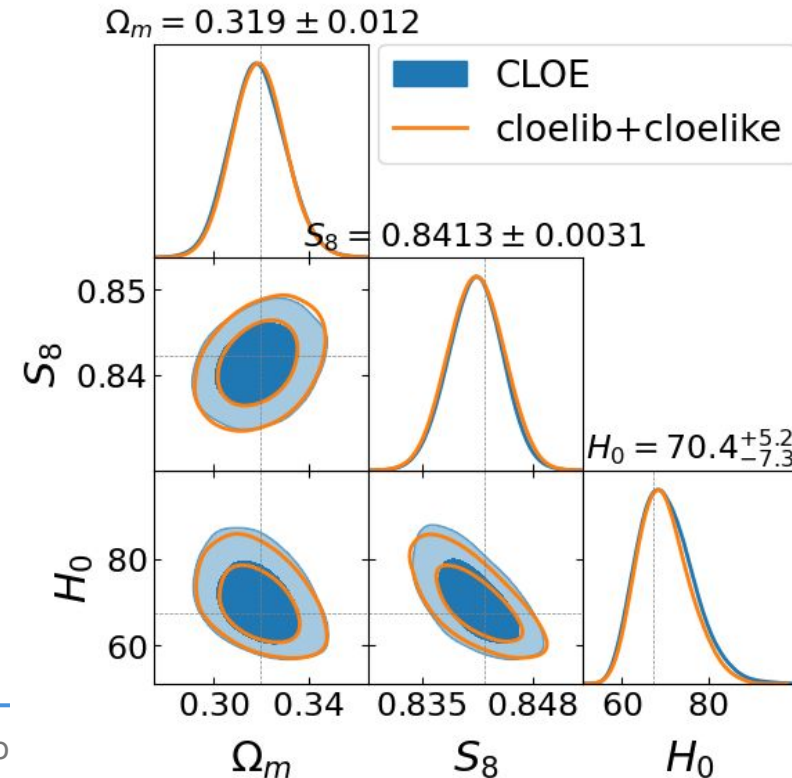
Euclid preparation

TBD. Cosmology Likelihood for Observables in Euclid (CLOE). 4: Validation and Performance

Euclid Collaboration: M. Martinelli^{1,2}, A. Pezzotta^{3,4}, D. Sciotti^{1,2}, L. Blot^{5,6}, M. Bonici^{7,8}, S. Camera^{9,10,11}, G. Cañas-Herrera^{12,13,14}, V. F. Cardone^{1,2}, P. Carrilho¹⁵, S. Casas¹⁶, S. Davini¹⁷, S. Di Domizio^{18,17}, S. Farrens¹⁹,

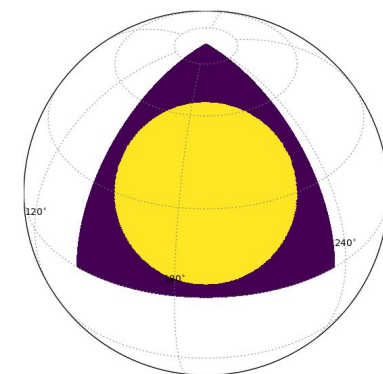
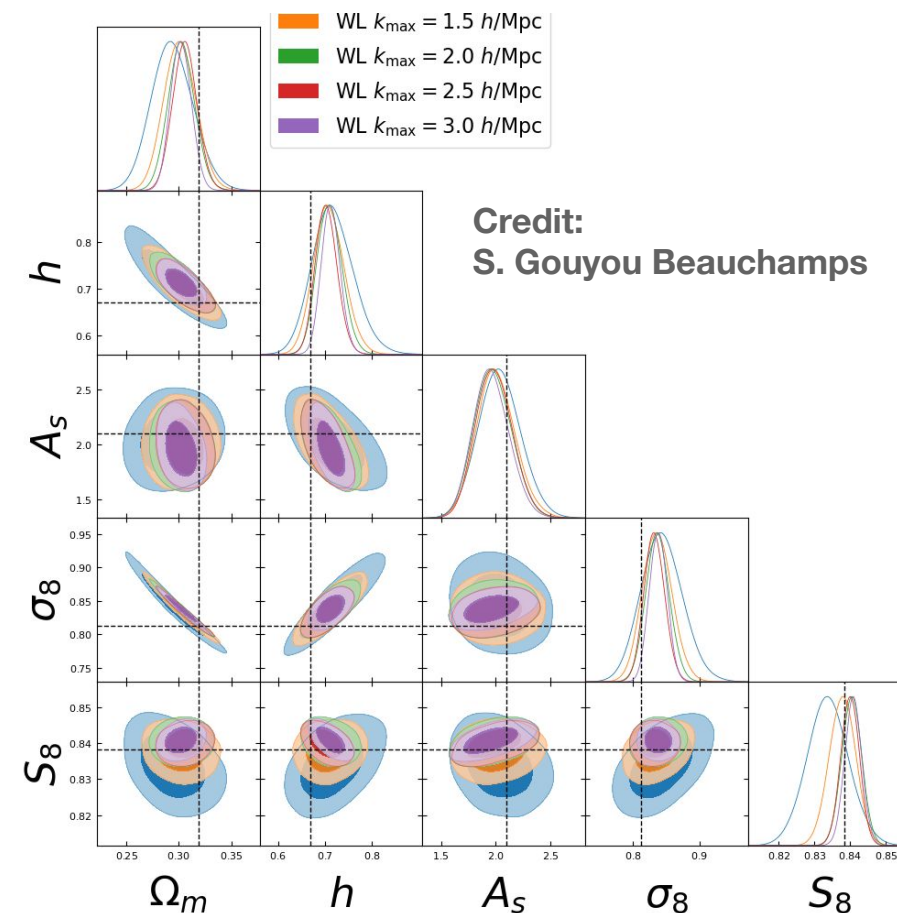
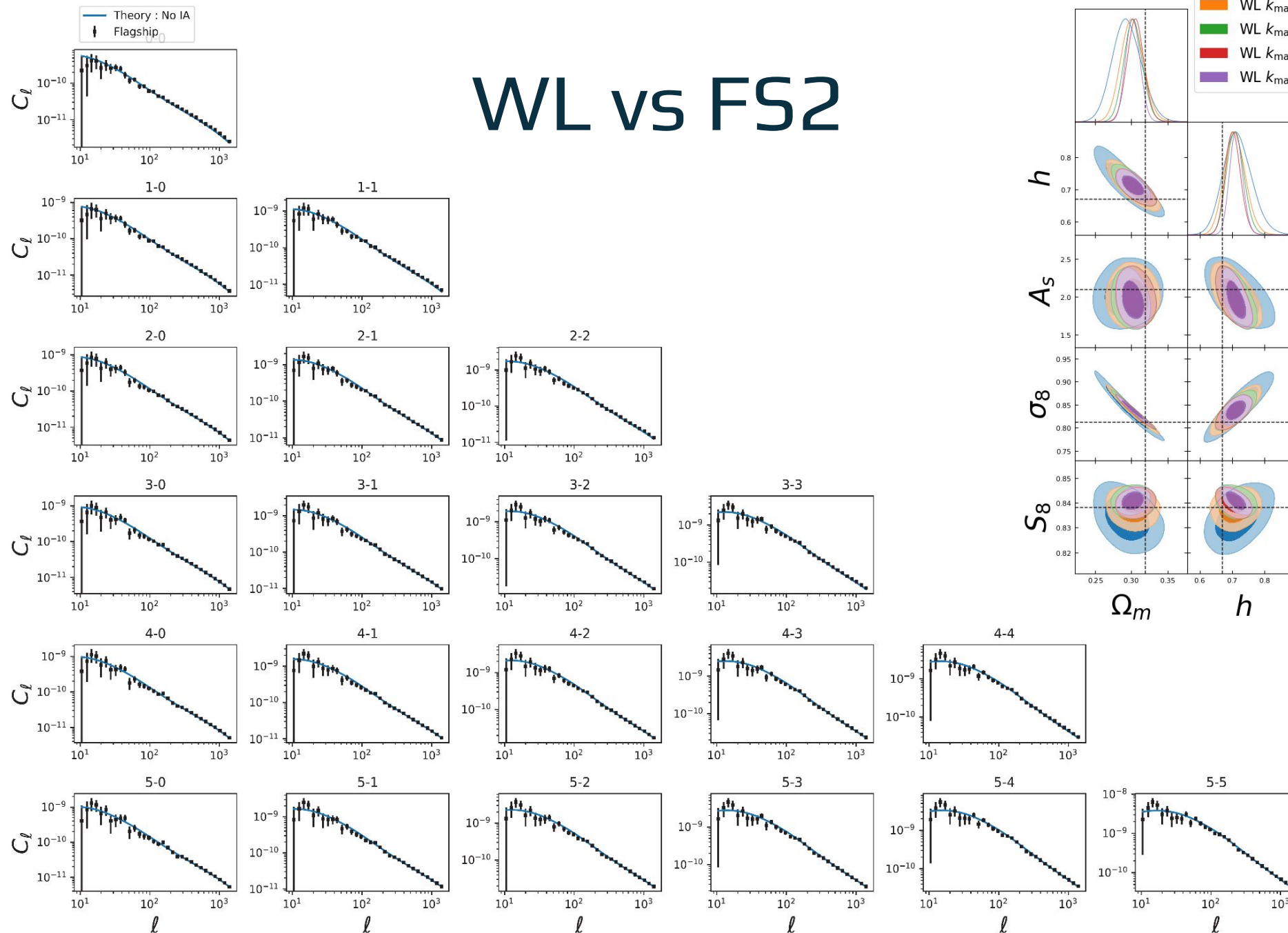


Credit:
M. Martinelli



Credit:
J. Coloma

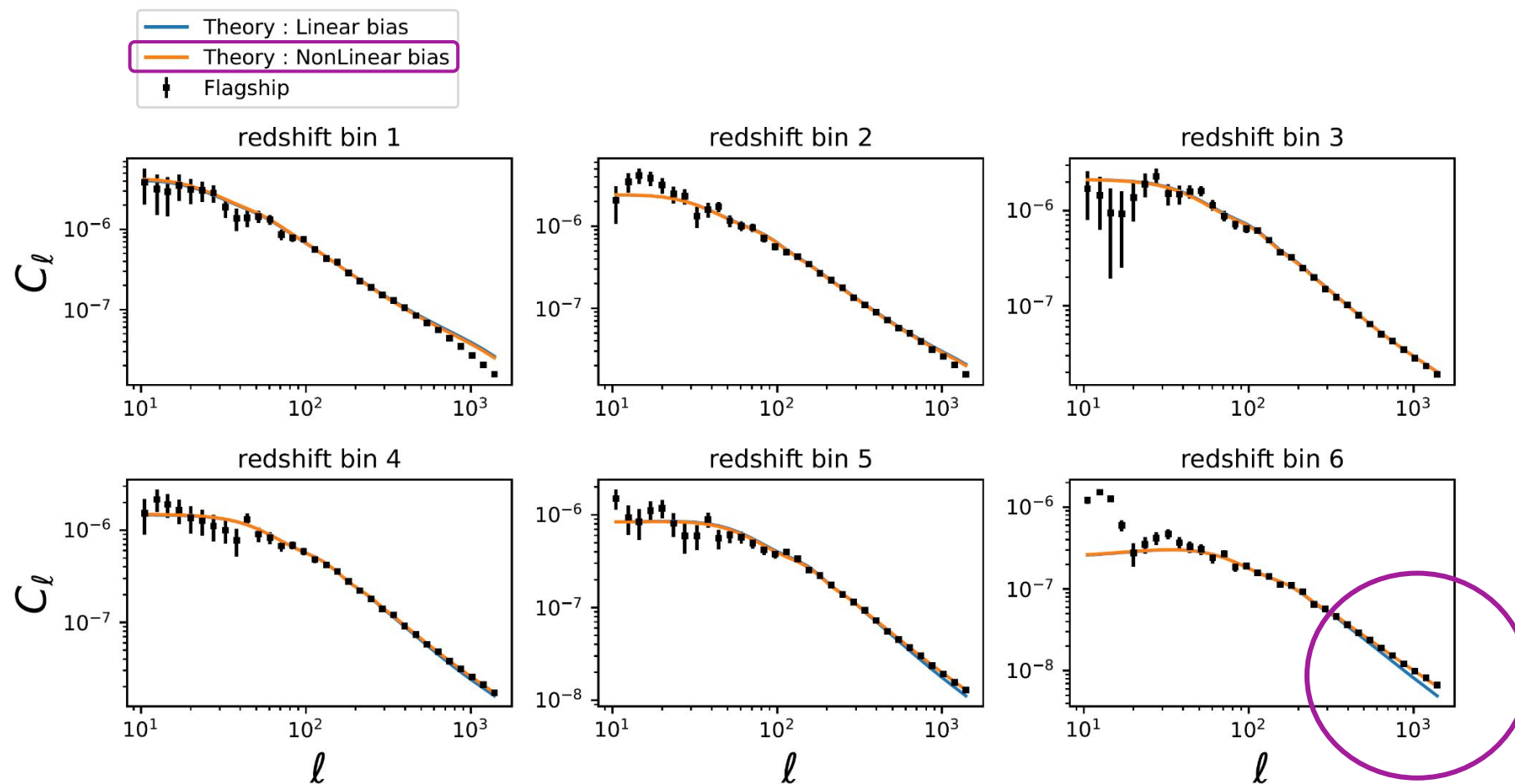
WL vs FS2



30deg-cone on FS2

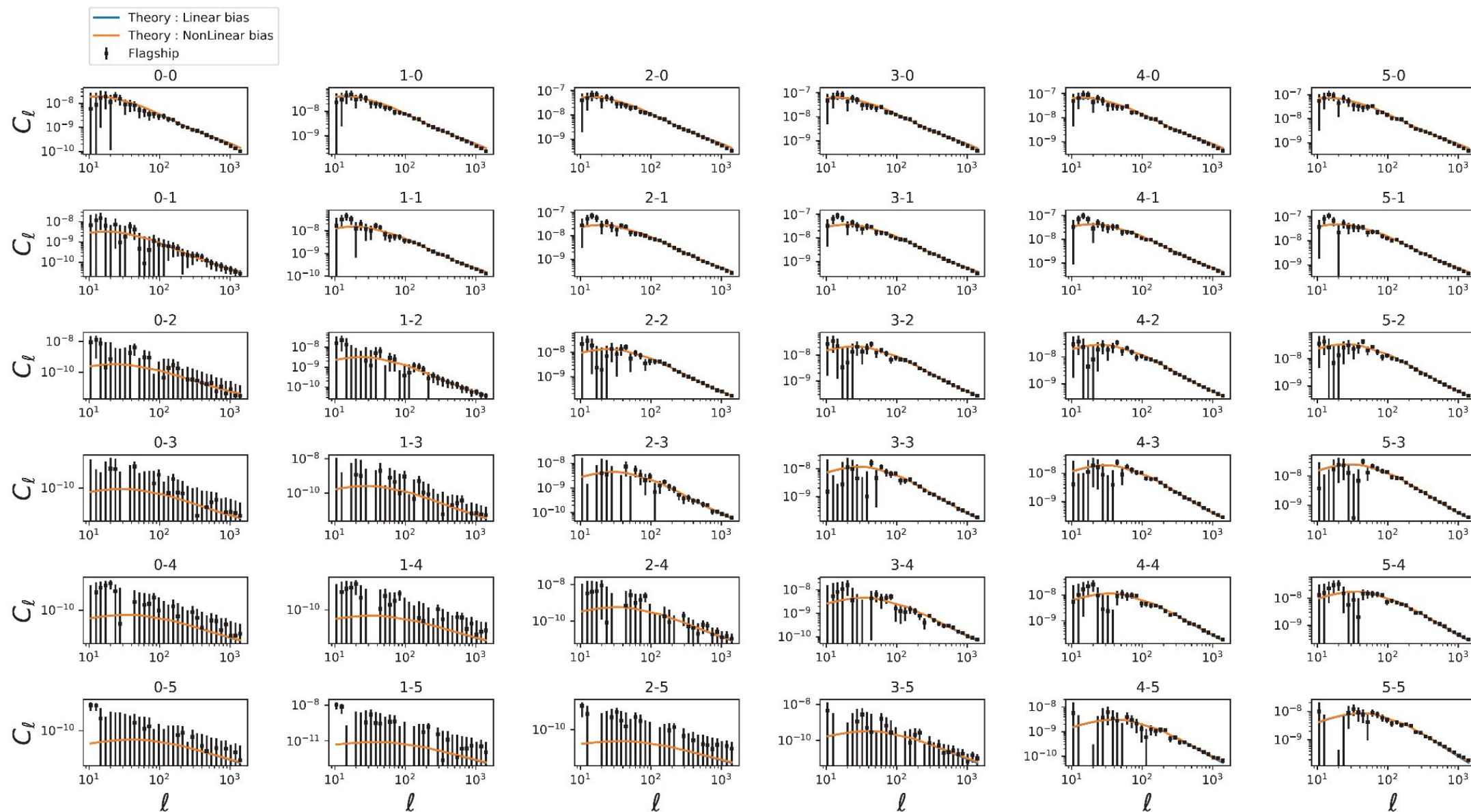
GCph vs FS2

Credit: S. Gouyou Beauchamps, C. Carbone



GGL vs FS2

Credit: S. Gouyou Beauchamps, C. Carbone



Covariance: Spaceborne

●● Main contributors

- **D. Sciotti:** main developer and maintainer
- **S. G. Beauchamps:** [SSC validation](#), partial-sky implementation
- **M. Bonici:** general structure, PyCCL interface, code optimization
- **R. Reischke:** NG cov, real-space validation
- **C. Garcia-Garcia:** partial-sky validation
- **J. R. Zapatero:** validation against jackknife

🌐 Coordinates (open repository)

- [GitHub](#)
- [Readthedocs](#)

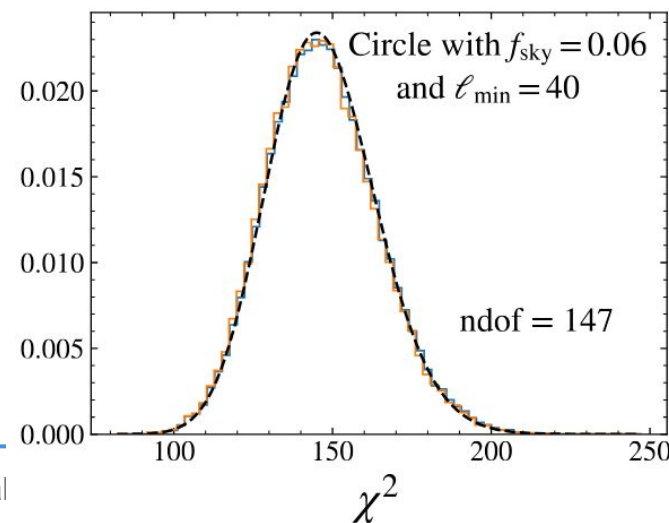
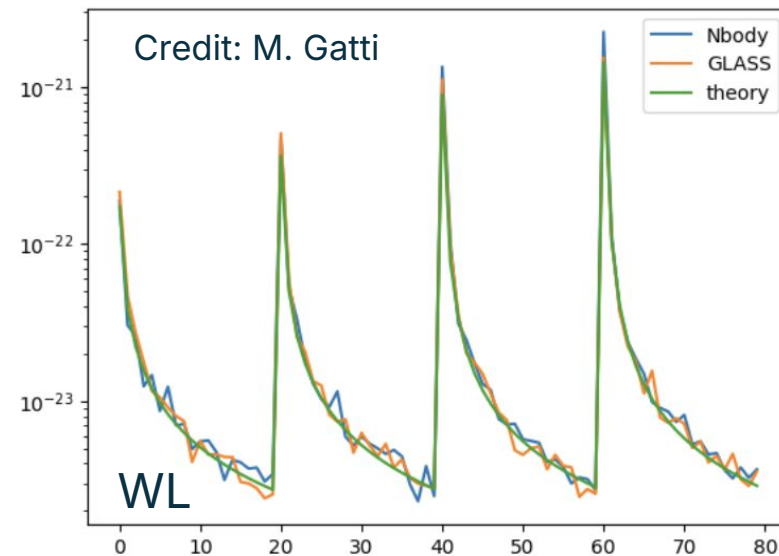
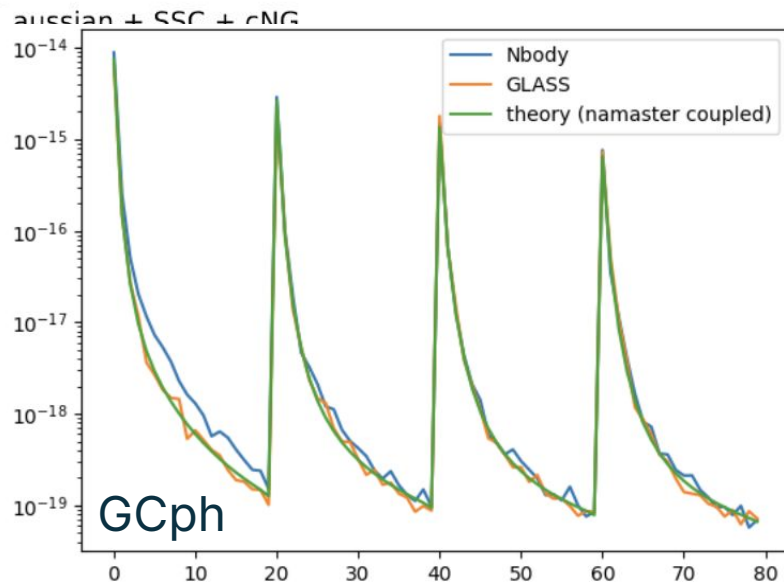
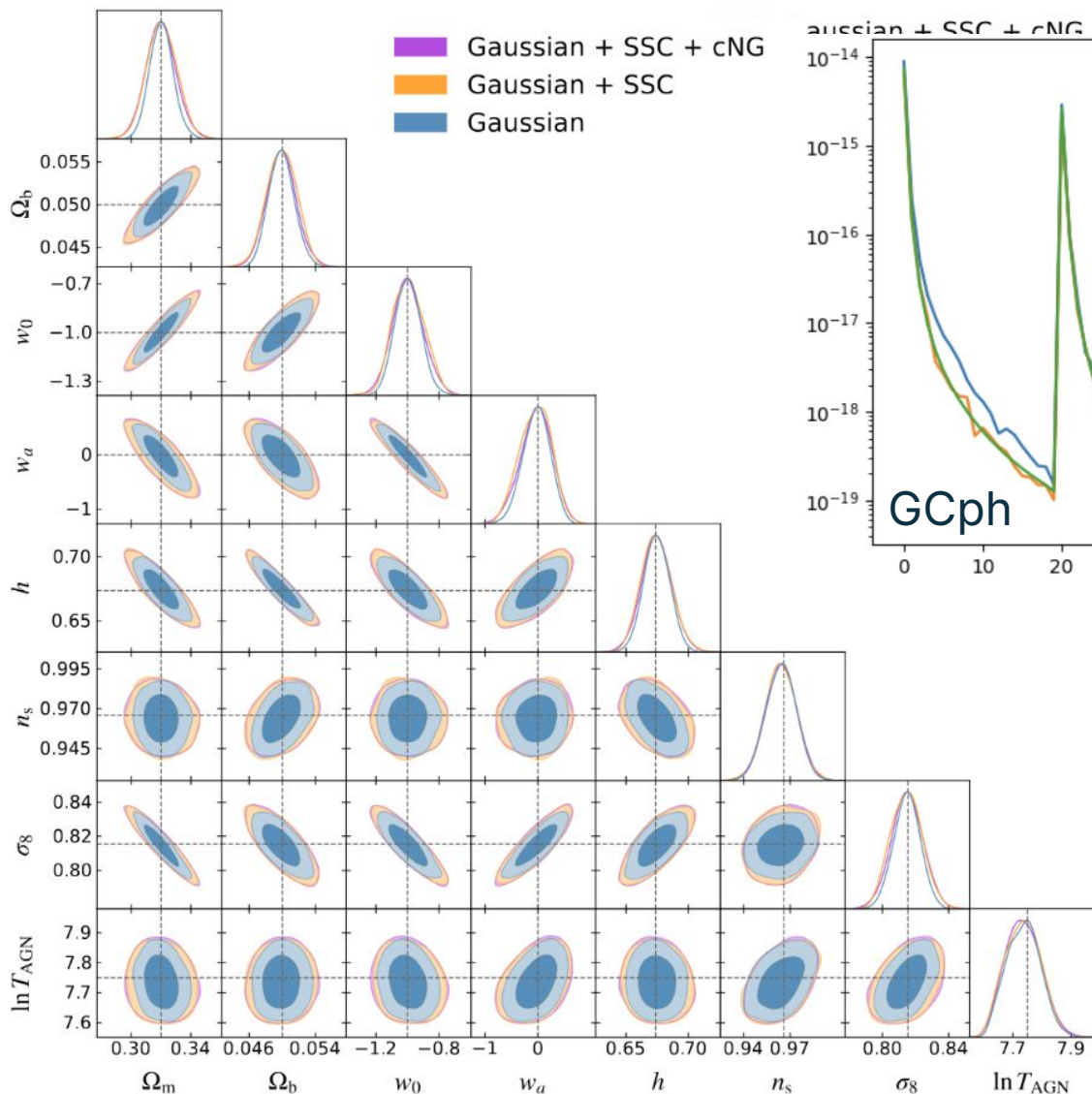
⚡ Key features

- Fast & parallel
- Interface with CCL (/cloelib)
- G, SSC, cNG
- Harmonic and real space
- Coupled/decoupled cov (int. with Namaster)
- and more!

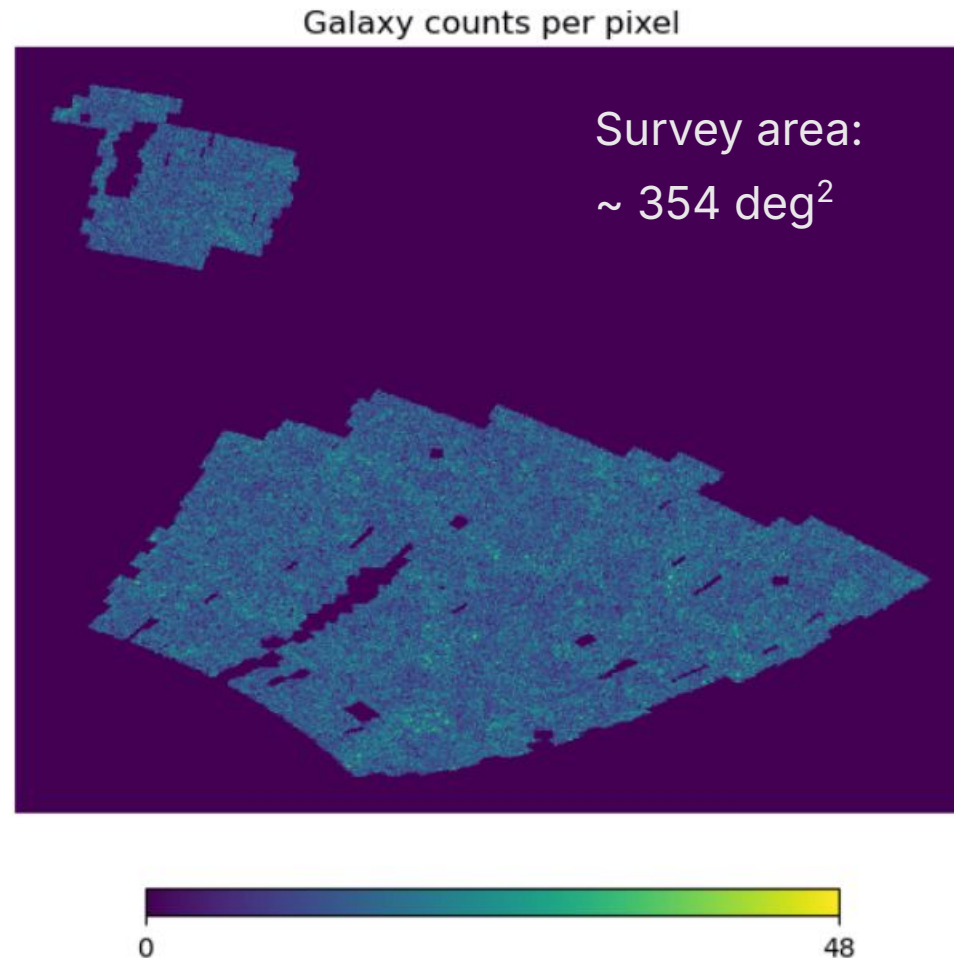
Validation

Euclid preparation. TBD. Theoretical modelling and numerical implementation of the harmonic-space 3x2pt covariance

Euclid Collaboration: D. Sciotti, M. Bonici, S. G. Beauchamps, G. Cañas-Herrera, R. Reischke, J. Coloma, M. Crocce, C. Giocoli, A. Pourtsidou, N. Tessore, M. Tsedrik, , et al.

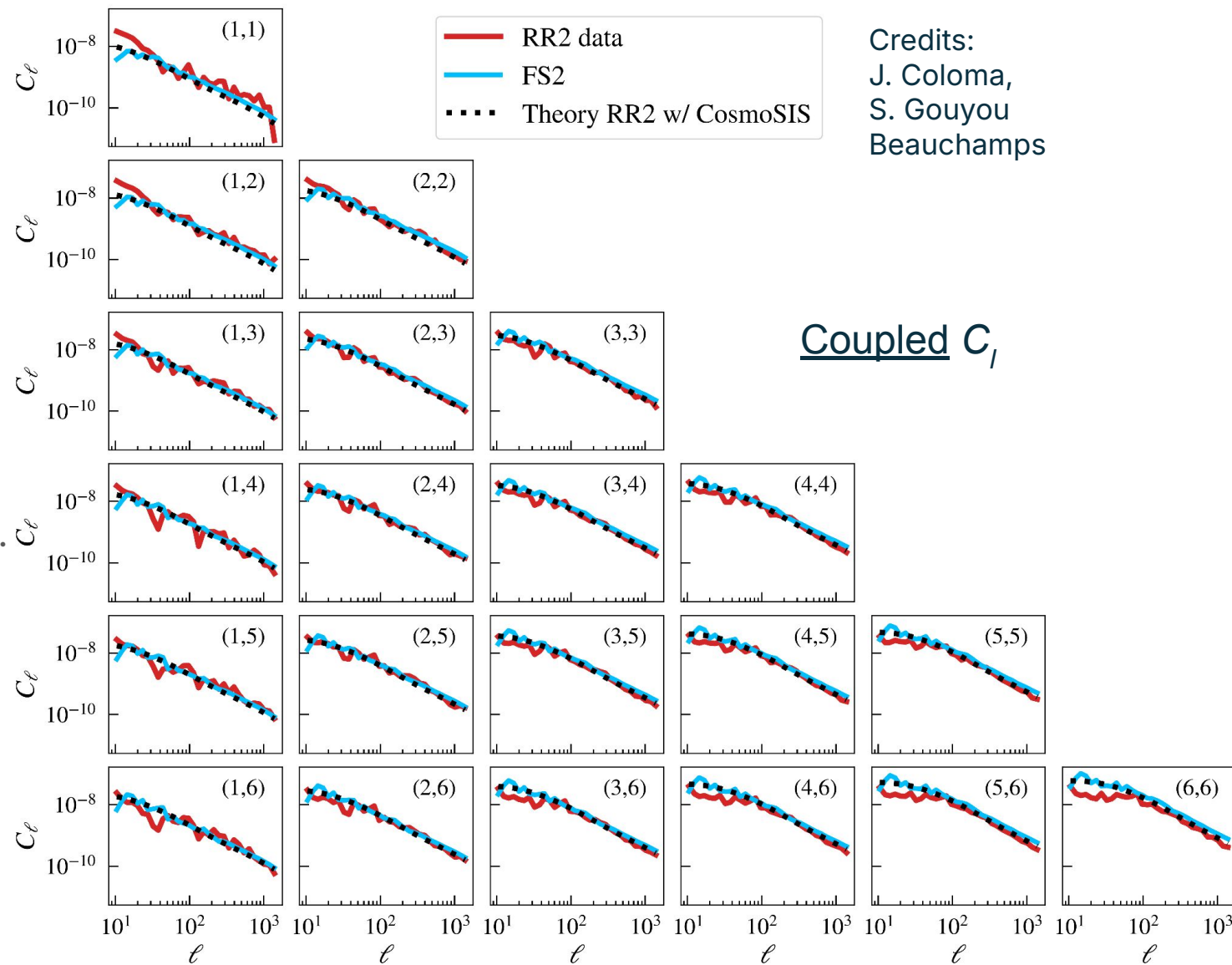
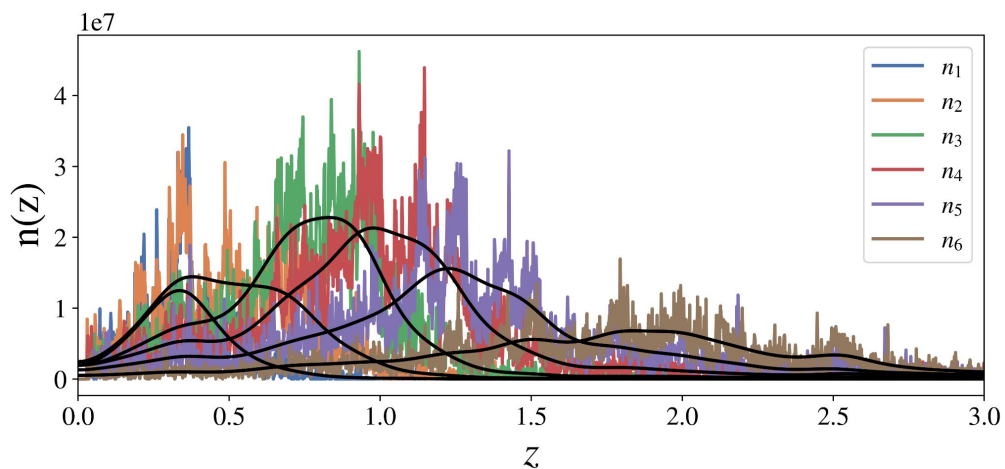


RR2 visibility mask & galaxy counts



First RR2 spectra

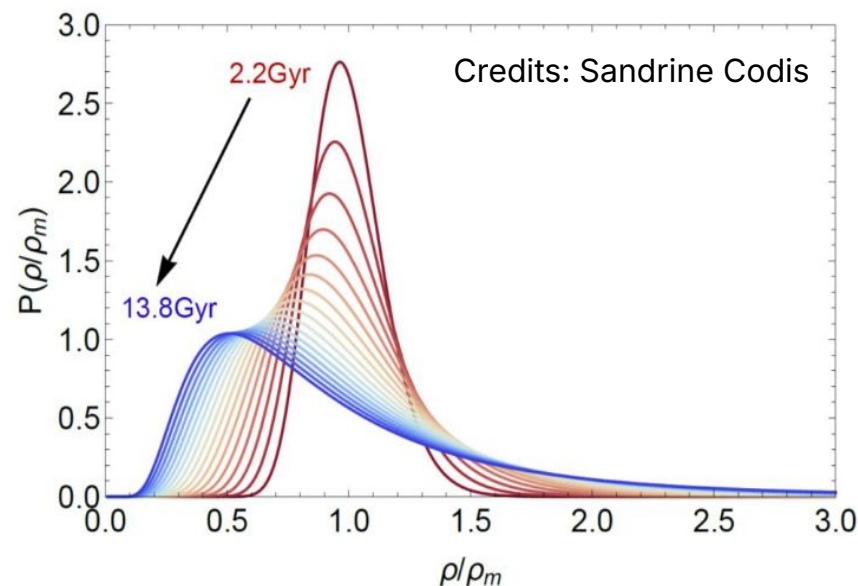
- **Data:**
 - Catalogue v1_1, w/o "bad tiles"
 - Unit weights, LensMC
 - Binary mask
- **Sim:**
 - FS2 30deg cone
 - Both sim and data rescaled to full-sky
- **Theory:**
 - CosmoSIS [pcl library](#)
 - RR2 smoothed $n(z)$'s
 - FS2 cosmology (no baryons/IA/mag.)



Credits:
J. Coloma,
S. Gouyou
Beauchamps

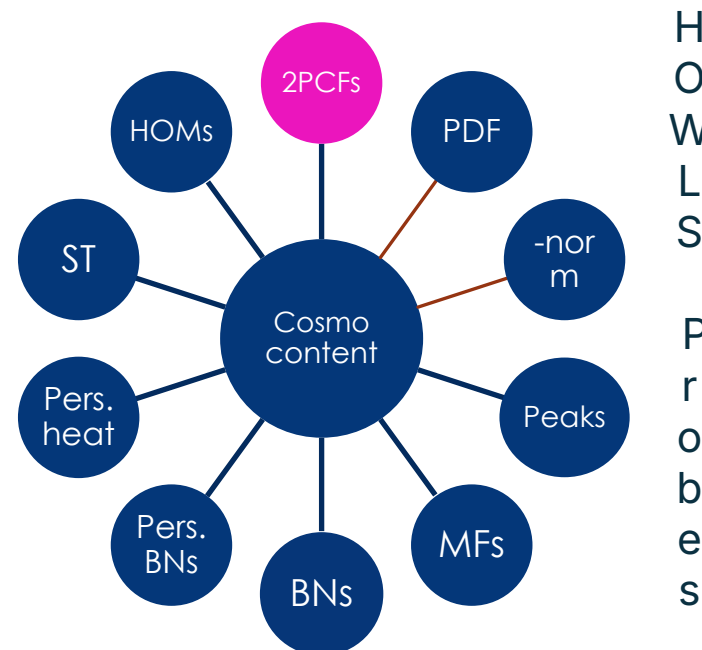
Higher-order statistics

Simulated Density Matter distribution



2-pt statistics (γ -2PCFs, κ -2PCF):

- ✓ Supported by solid theoretical models
- ✗ Only sensitive to the Gaussian information



Slide by Simone Vinciguerra

Higher Order Statistics (HOSs):

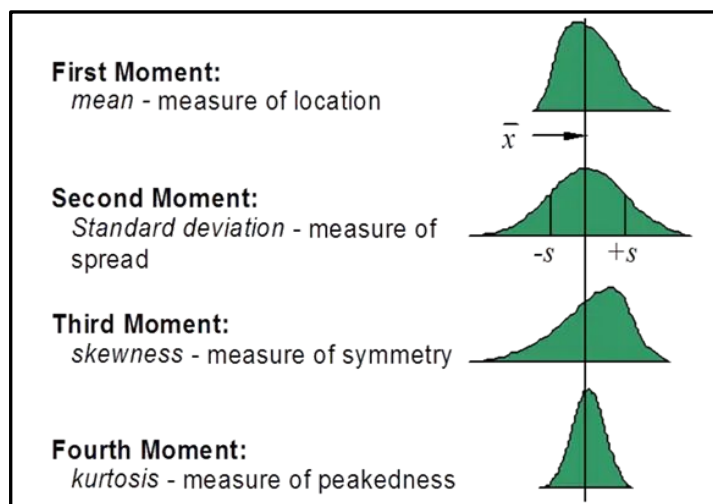
- ✓ Capture Gaussian & non-Gaussian content
- ✗ Mostly lacking of theoretical models

Higher-order statistics

1-point statistics

Moments, PDF, ...

- Probing the higher order cumulants of the field.



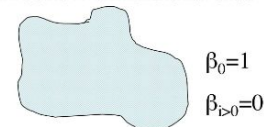
Fiveable. "3.5 Higher-order moments – Theoretical Statistics." Edited by Becky Bahr, Fiveable, 2024

Topological statistics

Peaks, MFs, BNs, ...

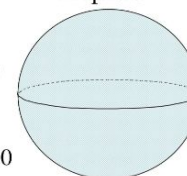
- Probing the distribution of maxima, minima, saddles and their connectivity.

A solid 2-dimensional blob

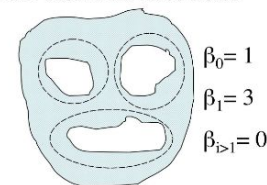


A sphere

$$\begin{aligned}\beta_0 &= 1 \\ \beta_1 &= 0 \\ \beta_2 &= 1 \\ \beta_{i>2} &= 0\end{aligned}$$

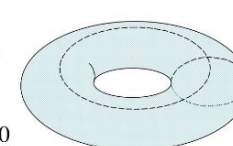


A 2D blob with three holes



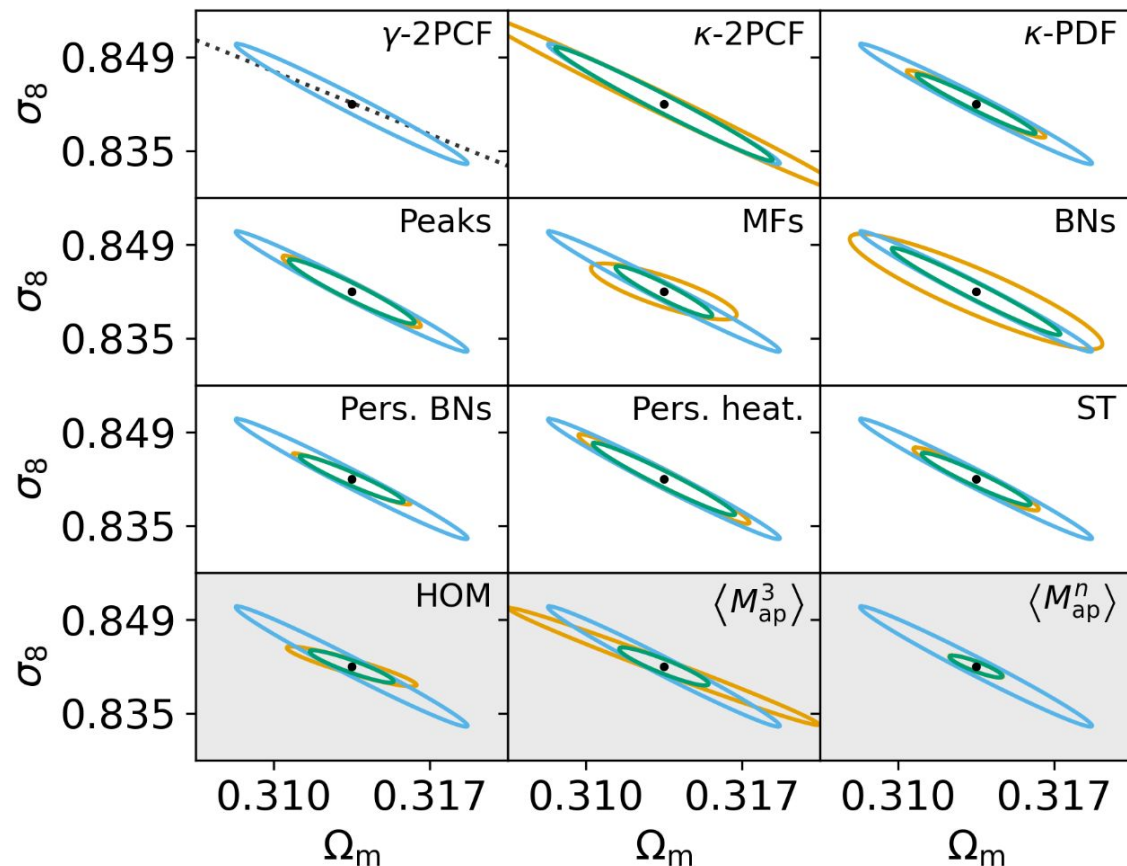
$$\begin{aligned}\beta_0 &= 1 \\ \beta_1 &= 2 \\ \beta_2 &= 1 \\ \beta_{i>2} &= 0\end{aligned}$$

A torus



B. Walker (2008)

Euclid Preparation. XXVIII. Ajani, HOWLS+



I. 7/10 HOSs compared against 2-pt,

- 7/10 HOSs compared against 2PCF (γ, κ)

II. Non-tomographic precision-forecasts on (Ω_m, σ_8) ,

- Non-tomographic precision-forecasts on (Ω_m, σ_8)

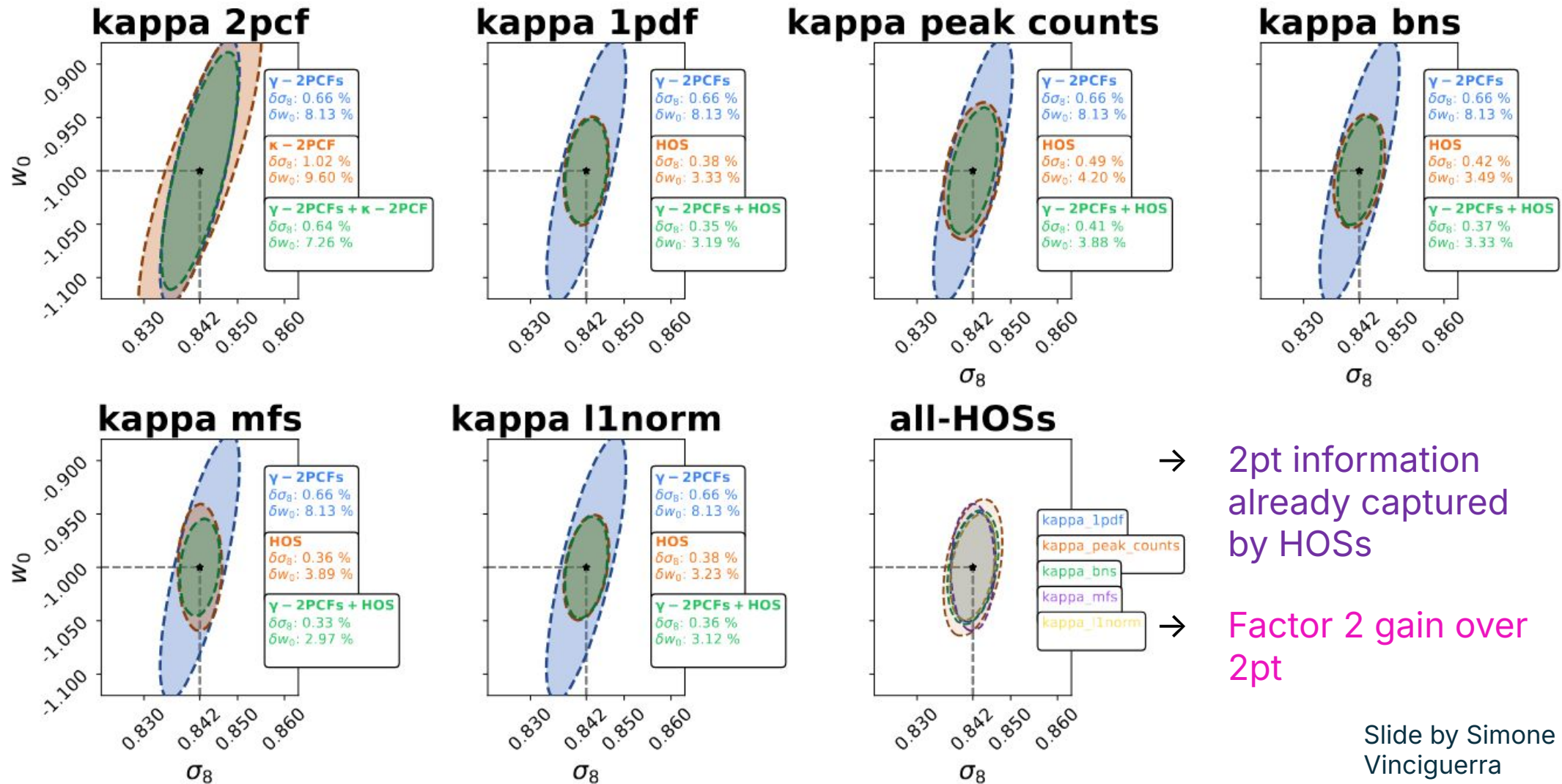
III. Individual constraining power improved up to a factor 2

- Individual constraining power improved up to a factor 2

IV. Joint constraining power boosted up to factor 5!

Slide by Simone Vinciguerra

HOSs comparison: Vinciguerra+, in prep



Conclusions

- 3×2 pt is a machine with **lots** of moving parts
- Analysis tools are being finalised and validated, with promising results (e.g., by recovering unbiased FS2 cosmology using different summary statistics)
- First application on RR2 data seems very good!
- The parameter space of analysis choice has many dimensions and is difficult to explore:
 - Sample selection (mostly dictated by **data quality**: photo-z and shape measurement quality, sample size, contamination, ability to run pipelines)
 - Scale cuts (mostly dictated by **modelling uncertainties**: NL bias, NL clustering, baryonic feedback...)
- HOS show the potential to boost constraining power without adding external information
- Timeline is extremely tight, but...

