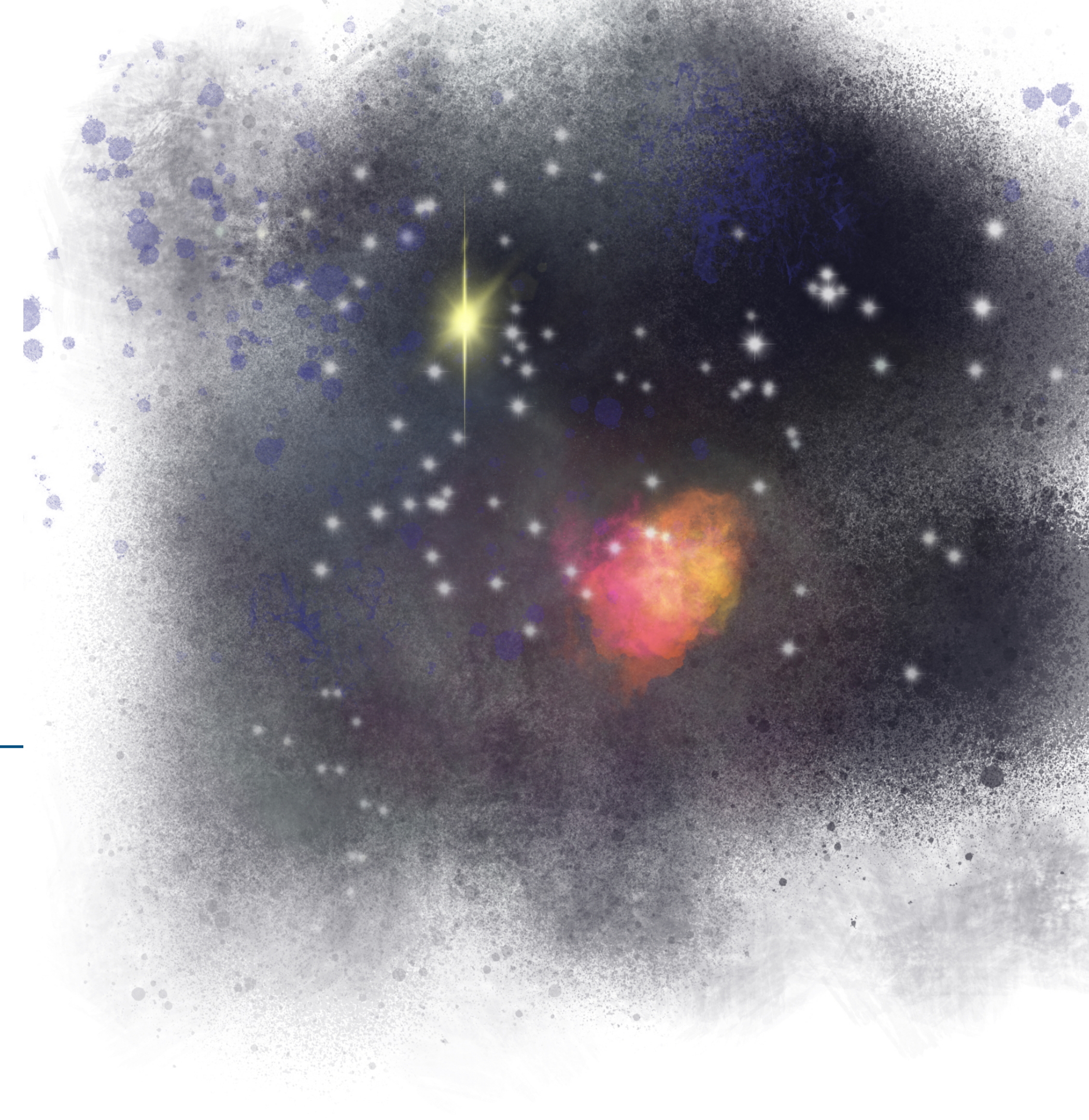


SKA Cosmology SWG meeting, Nov 4th, 2024
Observatoire de la Côte d'Azur

Testing the Cosmological Principle with the SKA

Sebastian von Hausegger
Oxford Physics



The Cosmological Principle and FLRW

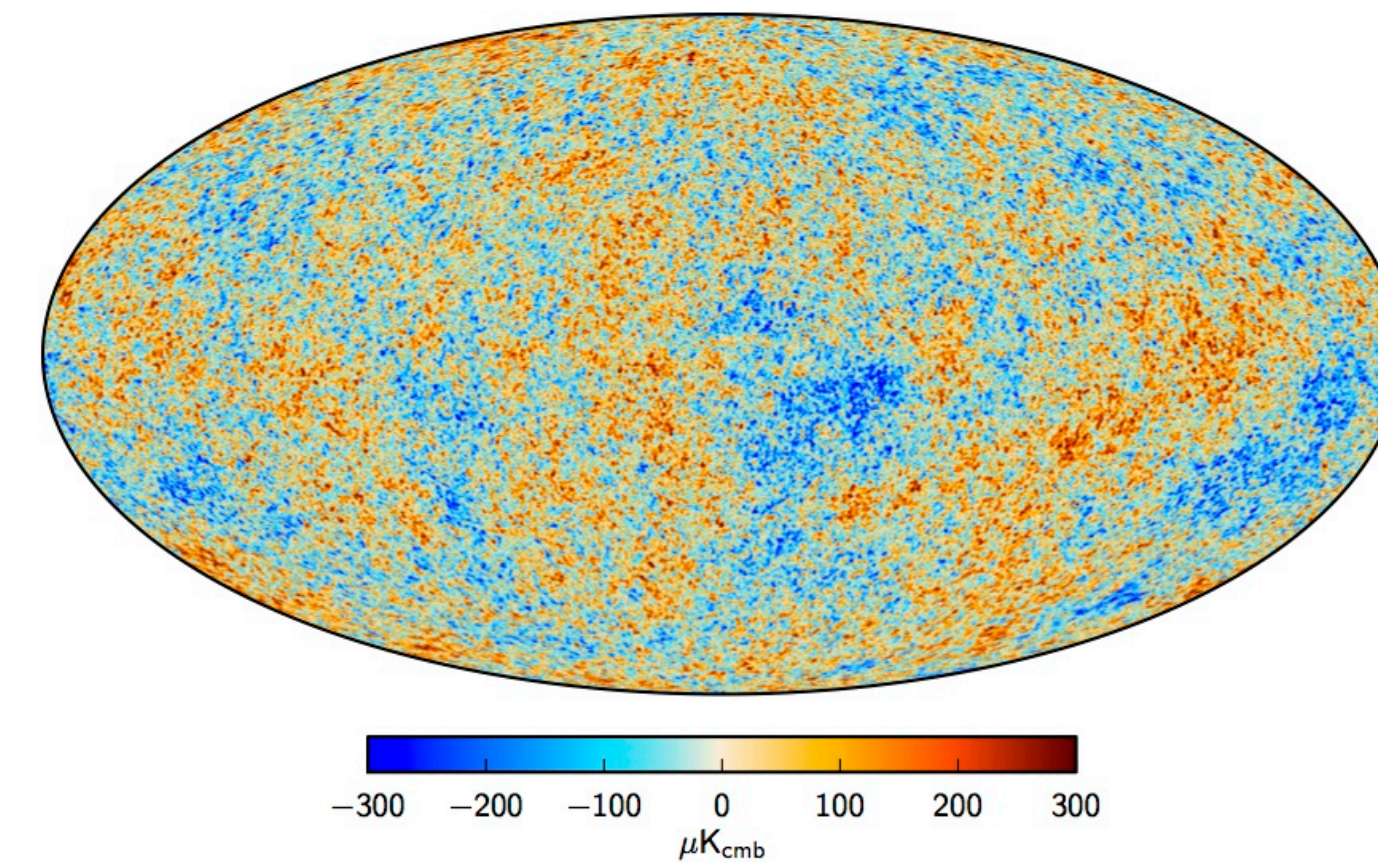
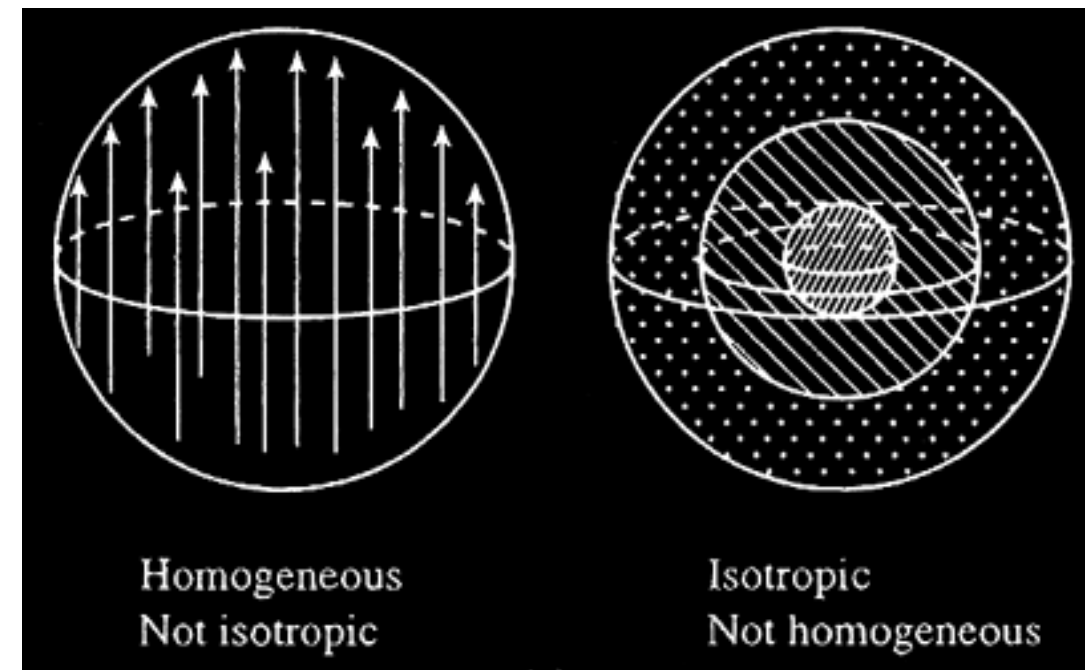
LCDM cosmological standard model based on **FLRW metric**

Relies on **Cosmological Principle**

Milne (1937)
deSitter (1934)

“All physical quantities measured by a **comoving** observer are spatially homogeneous and isotropic.”

Schwarz (2009)



If **all** comoving observers see an isotropic CMB then we must live in a Friedman Universe

Tauber&Weinberg (1961)
Ehlers et al. (1968)

The Cosmological Principle and FLRW

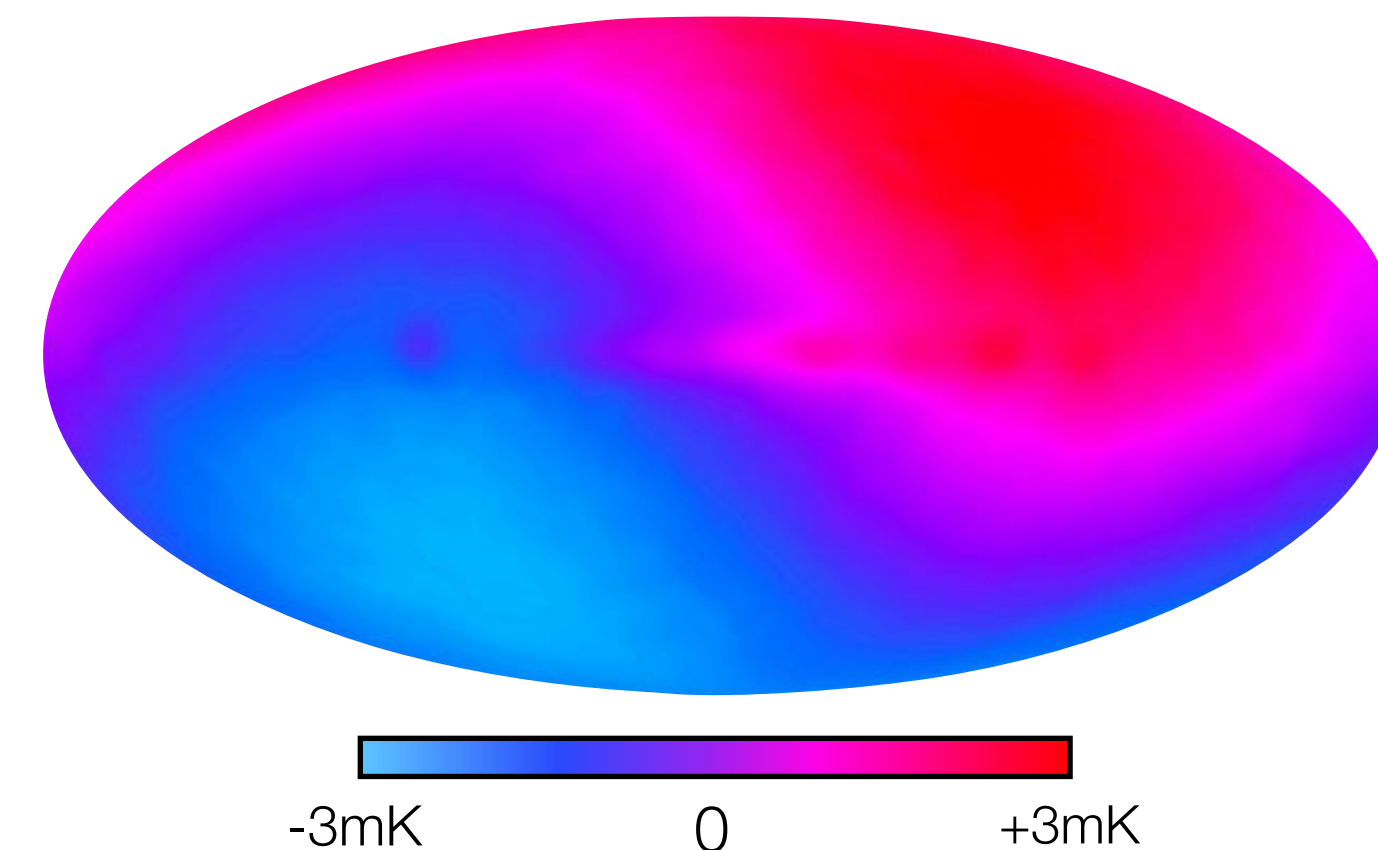
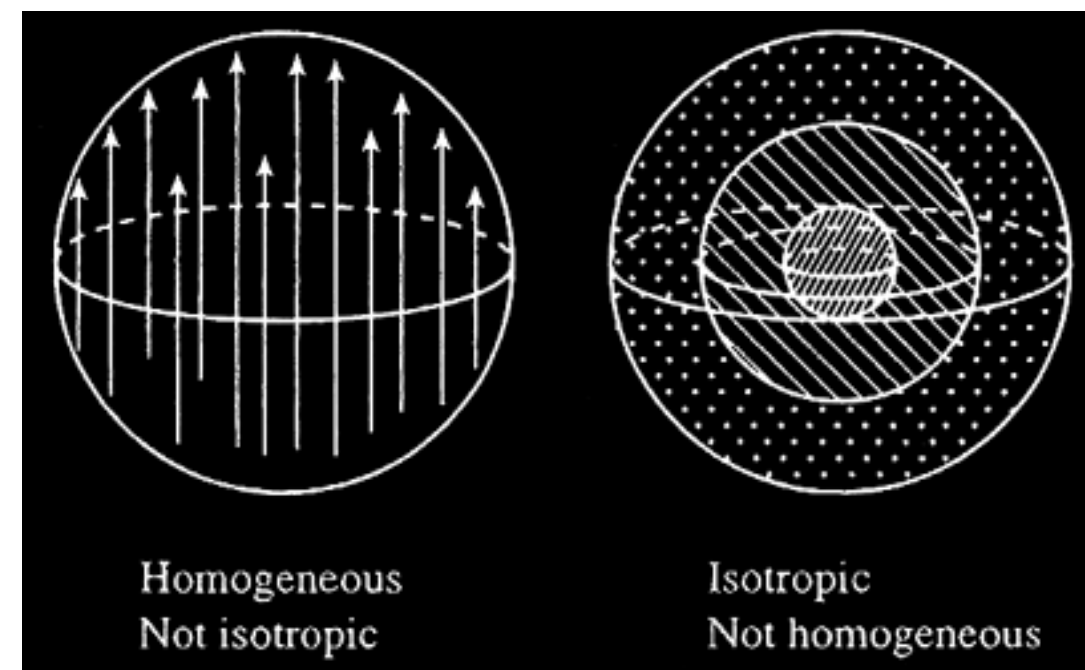
LCDM cosmological standard model based on **FLRW metric**

Relies on **Cosmological Principle**

Milne (1937)
deSitter (1934)

“All physical quantities measured by a **comoving** observer are spatially homogeneous and isotropic.”

Schwarz (2009)



We are **not** comoving observers:

At least check for consistency CMB rest frame and matter rest frame

The kinematic matter dipole anomaly

$$\mathcal{D} = [2 + x(1 + \alpha)] \cdot \beta$$

For radio sources we find $x \approx 1$ and $\alpha \approx 0.75$
&
Our (sun's) velocity wrt the CMB is 369km/s

$$\Rightarrow \mathcal{D} \approx 4.6 \times 10^{-3}$$

But Blake&Wall measure $\mathcal{D}_{BW} \approx 1.1 \times 10^{-2}$
(at $S > 25$ mJy, with \sim large uncertainties, and with $\sim 200,000$ sources)

letters to nature

A velocity dipole in the distribution of radio galaxies

Chris Blake & Jasper Wall

*Astrophysics, Nuclear and Astrophysics Laboratory, University of Oxford,
Keble Road, Oxford OX1 3RH, UK*

The motion of our Galaxy through the Universe is reflected in a systematic shift in the temperature of the cosmic microwave background¹—because of the Doppler effect, the temperature of the background is about 0.1 per cent higher in the direction of motion, with a correspondingly lower temperature in the opposite direction. This effect is known as dipole anisotropy. If our standard cosmological model is correct, a related dipole effect should also be present as an enhancement in the surface density of distant galaxies in the direction of motion². The main obstacle to finding this signal is the uneven distribution of galaxies in the local supercluster, which drowns out the small cosmological signal. Here we report a detection of the expected cosmological dipole anisotropy in the distribution of galaxies. We use a survey of radio galaxies that are mainly located at cosmological distances, so the contamination from nearby clusters is small. When local radio galaxies are removed from the sample, the resulting dipole is in the same direction as the temperature anisotropy of the microwave background, and close to the expected amplitude. The result therefore confirms the standard cosmological interpretation of the microwave background.

The kinematic matter dipole anomaly

THE ASTROPHYSICAL JOURNAL LETTERS, 742:L23 (4pp), 2011 December 1
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doi:10.1088/2041-8205/742/2/L23

LARGE PECULIAR MOTION OF THE SOLAR SYSTEM FROM THE DIPOLE ANISOTROPY IN SKY BRIGHTNESS DUE TO DISTANT RADIO SOURCES

ASHOK K. SINGAL

Astron

Astronomy & Astrophysics manuscript no. NVSS' dipole
January 16, 2018

© ESO 2018

Cosmic radio dipole from NVSS and WENSS

Matthias Rubart^{*}, Dominik J. Schwarz^{**}

THE ASTROPHYSICAL JOURNAL LETTERS, 908:L51 (6pp), 2021 February 20
© 2021. The Author(s). Published by the American Astronomical Society.

<https://doi.org/10.3847/2041-8213/abdd40>

OPEN ACCESS



A Test of the Cosmological Principle with Quasars

Nathan J. Secrest¹, Sebastian von Hausegger^{2,3,4}, Mohamed Rameez⁵, Roya Mohayaee³, Subir Sarkar⁴, and Jacques Colin³

THE ASTROPHYSICAL JOURNAL LETTERS, 937:L31 (9pp), 2022 October 1

<https://doi.org/10.3847/2041-8213/ac88c0>

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OPEN ACCESS



A Challenge to the Standard Cosmological Model

Nathan J. Secrest¹, Sebastian von Hausegger², Mohamed Rameez³, Roya Mohayaee^{2,4}, and Subir Sarkar²

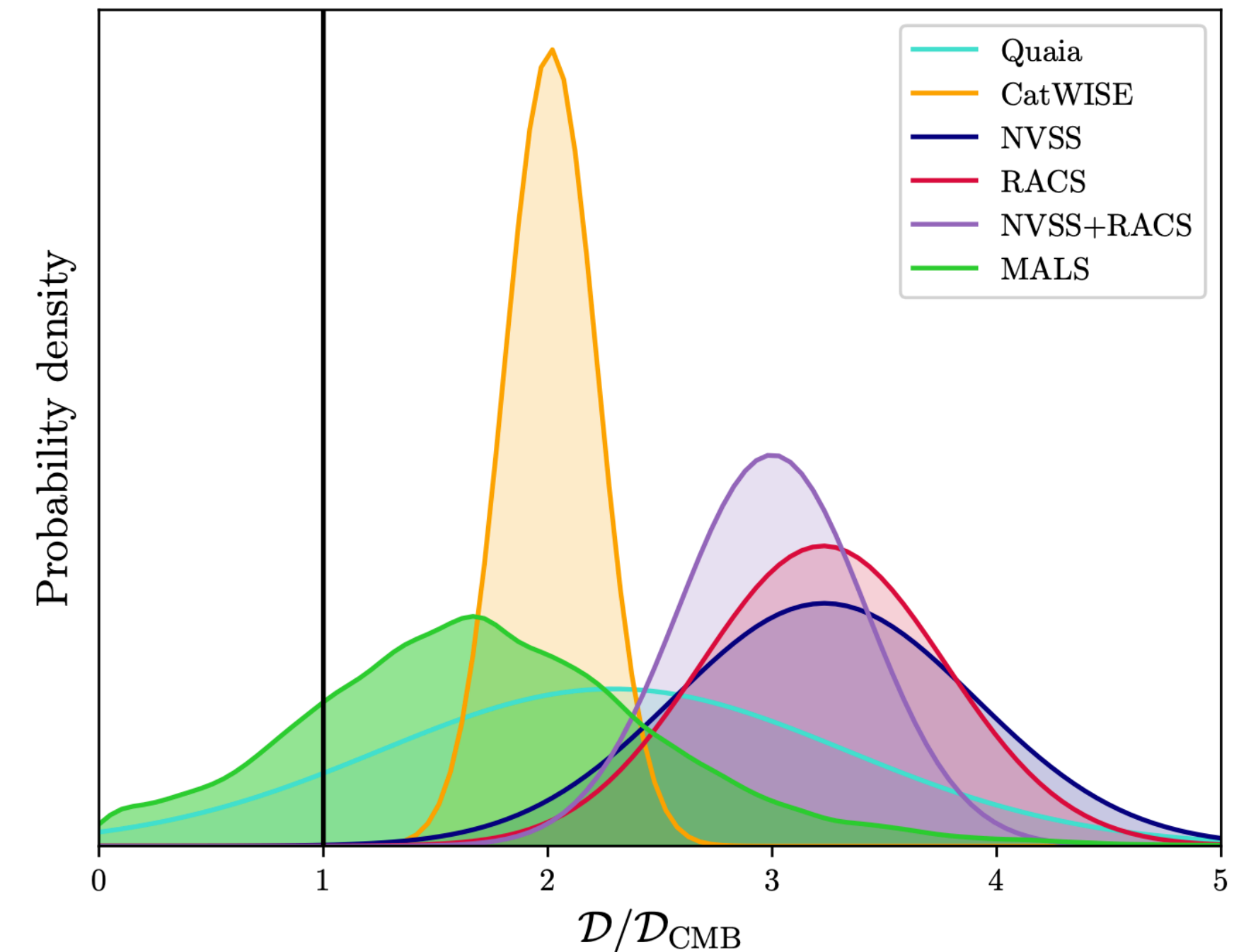
¹U.S. Naval Observatory, 3450 Massachusetts Ave. NW, Washington, DC 20392-5420, USA; nathan.j.secrest.civ@us.navy.mil

²Rudolf Peierls Centre for Theoretical Physics, University of Oxford, Parks Road, Oxford, OX1 3PU, UK

³Dept. of High Energy Physics, Tata Institute of Fundamental Research, Homi Bhabha Road, Mumbai 400005, India

⁴Sorbonne Université, CNRS, Institut d'Astrophysique de Paris, 98bis Bld Arago, Paris F-75014, France

Received 2022 June 10; revised 2022 August 9; accepted 2022 August 11; published 2022 September 28



Wagenveld et al. (2024)

The kinematic matter dipole

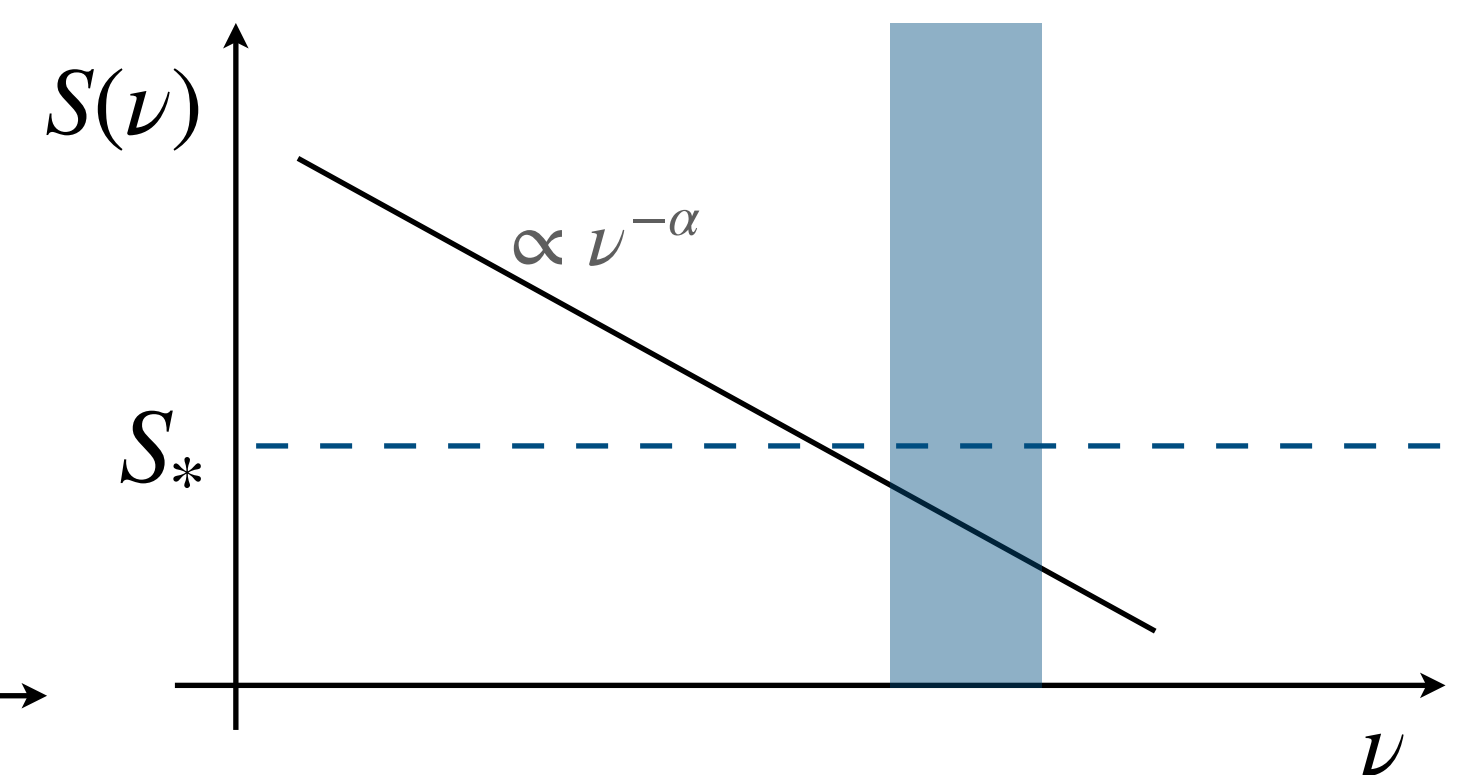
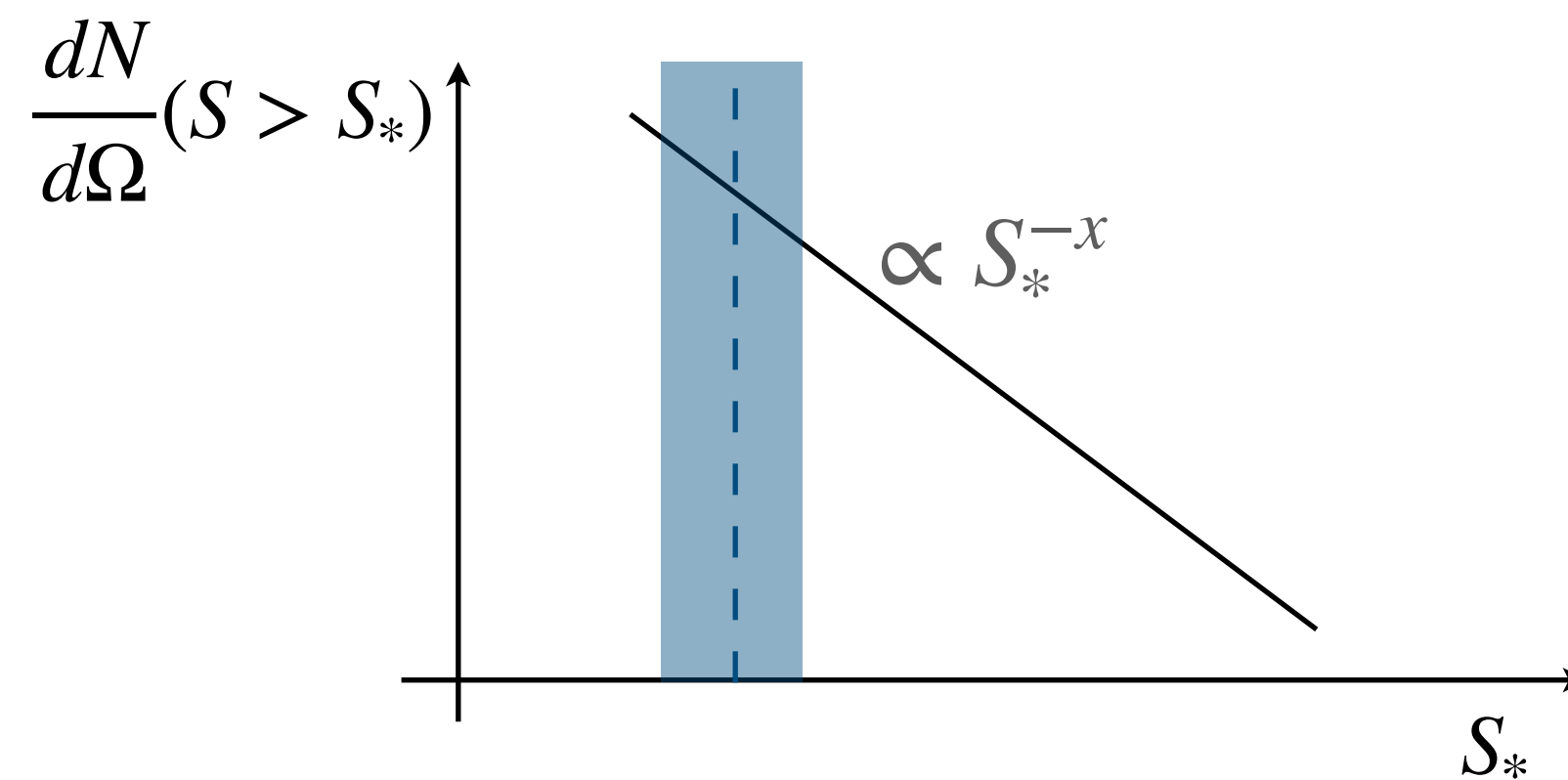
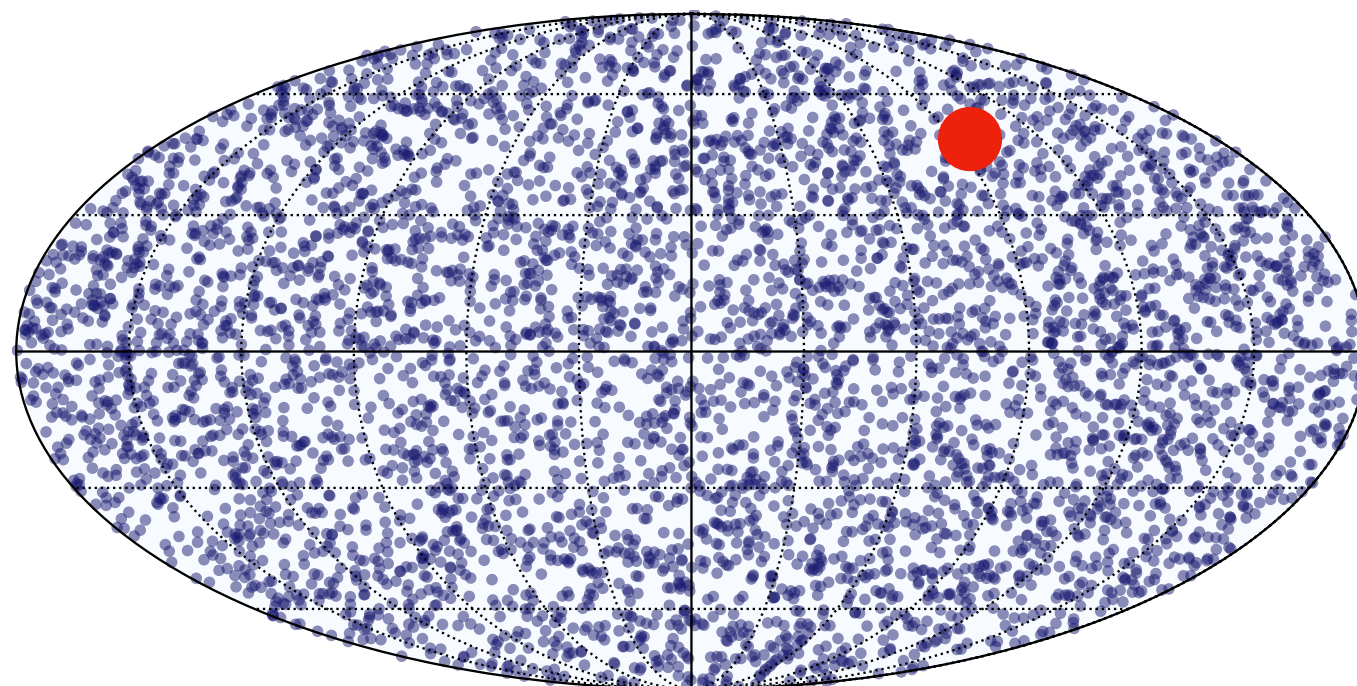
Ellis & Baldwin (1984)

Average spectral index
of source spectra

$$\tilde{\mathcal{D}} = [2 + \tilde{x}(1 + \tilde{\alpha})] \beta$$

Related to
magnification bias

“Tilde” quantities refer
to what we measure
(without redshifts!)



The kinematic matter dipole

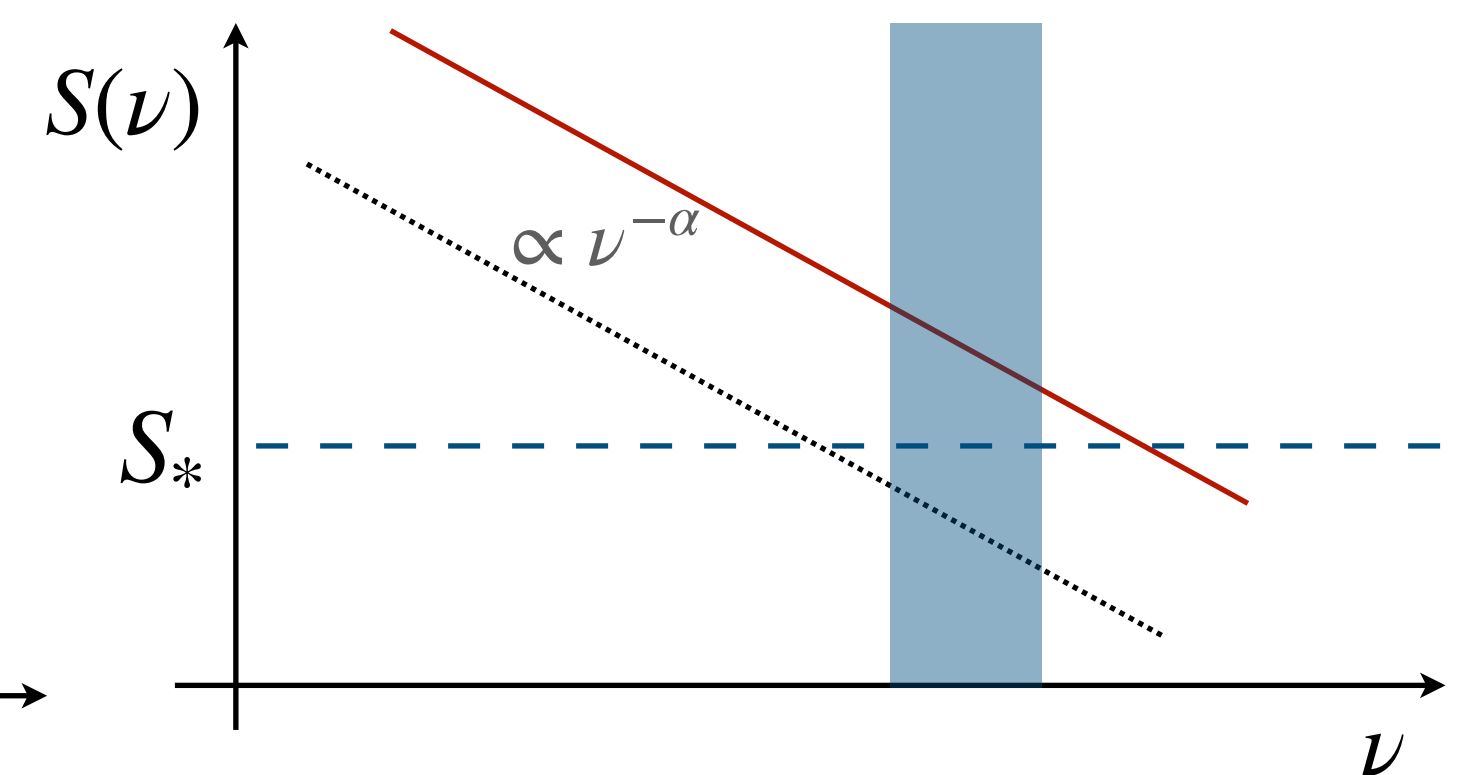
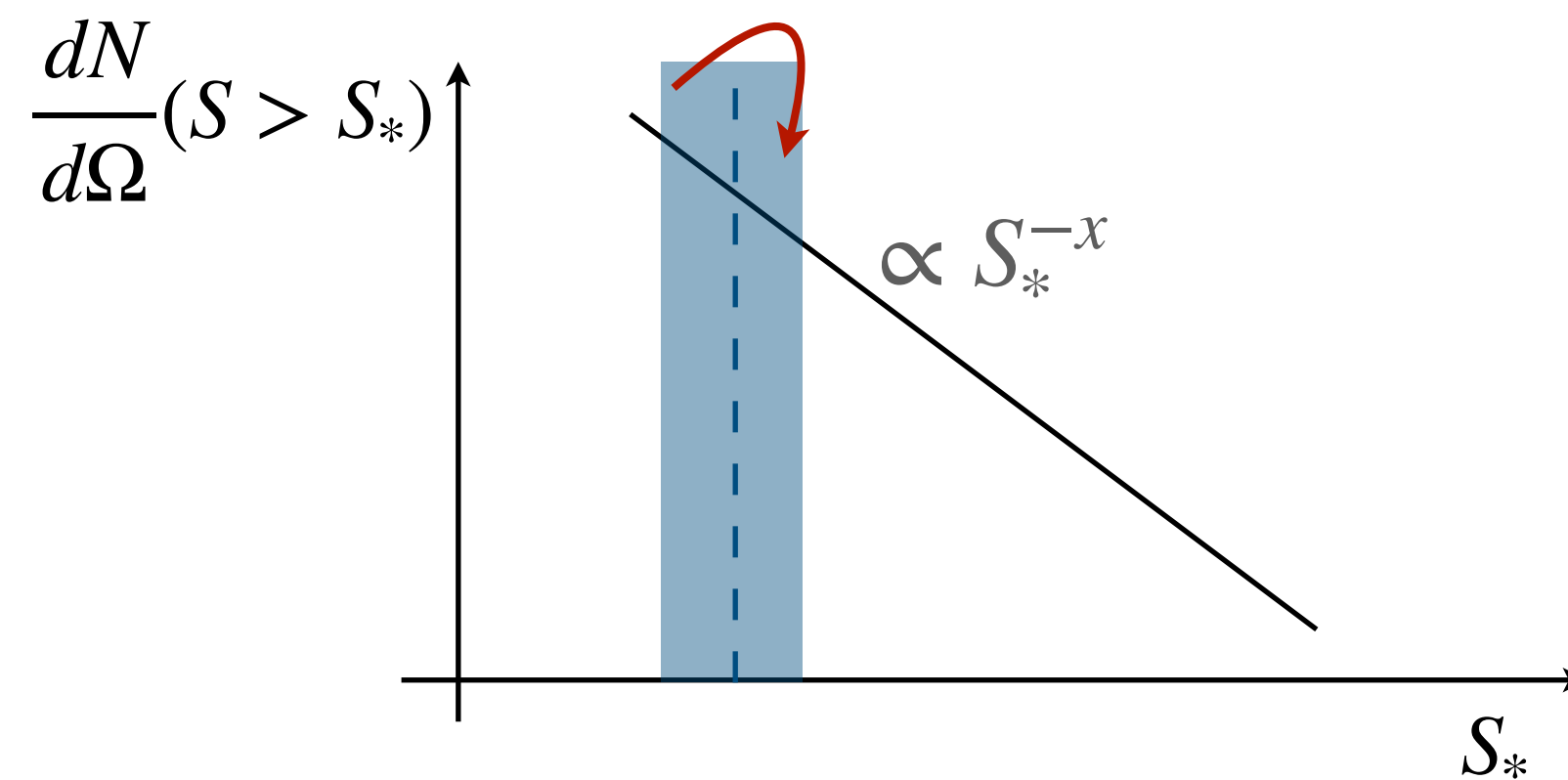
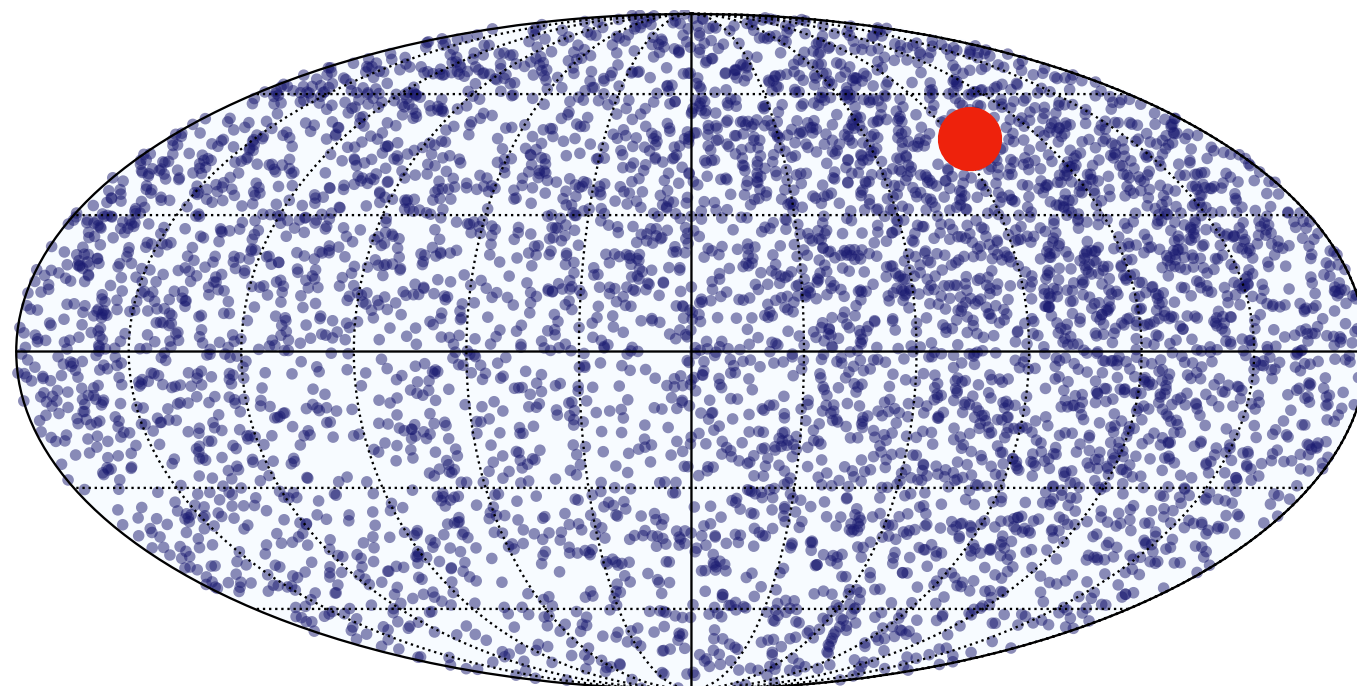
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Related to
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“Tilde” quantities refer
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(without redshifts!)



Redshift dependence

Ellis & Baldwin (1984)

Average spectral index
of source spectra

$$\tilde{\mathcal{D}} = [2 + \tilde{x}(1 + \tilde{\alpha})] \beta$$

Related to
magnification bias

“Tilde” quantities refer
to what we measure
(without redshifts!)

$$\mathcal{D} = \int_0^{\infty} dz f(z) \mathcal{D}(z)$$

Redshift dependence

Ellis & Baldwin (1984)

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of source spectra

$$\tilde{\mathcal{D}} = [2 + \tilde{x}(1 + \tilde{\alpha})] \beta$$

Related to
magnification bias

“Tilde” quantities refer
to what we measure
(without redshifts!)

(normalised)
redshift
distribution

$$\mathcal{D} = \int_0^{\infty} dz f(z) \mathcal{D}(z)$$

kinematic dipole
per redshift

Redshift dependence

Ellis & Baldwin (1984)

$$\tilde{\mathcal{D}} = [2 + \tilde{x}(1 + \tilde{\alpha})] \beta$$

Are the observed quantities enough to predict the dipole correctly?

Maartens et al. (2017)

$$\mathcal{D}(z) = \left[2 + \frac{\dot{\mathcal{H}}(z)}{\mathcal{H}^2(z)} + \frac{2(1 - x(z))}{r(z)\mathcal{H}(z)} - b_e(z) \right] \beta$$

See also, Dalang & Bonvin (2022)

(normalised)
redshift
distribution

$$\mathcal{D} = \int_0^{\infty} dz f(z) \mathcal{D}(z)$$

kinematic dipole
per redshift

Redshift dependence

Ellis & Baldwin (1984)

$$\tilde{\mathcal{D}} = [2 + \tilde{x}(1 + \tilde{\alpha})] \beta$$

**Are the observed quantities
enough to predict the dipole
correctly?**

Nadolny et al. (2021)

$$\mathcal{D}(z) = \left[3 + x(z)(1 + \alpha(z)) + \frac{d \log n(z)}{d \log(1 + z)} \right] \beta$$

See also, Dalang & Bonvin (2022)

**(normalised)
redshift
distribution**

$$\mathcal{D} = \int_0^{\infty} dz f(z) \mathcal{D}(z)$$

**kinematic dipole
per redshift**

Redshift dependence

Ellis & Baldwin (1984)

$$\tilde{\mathcal{D}} = [2 + \tilde{x}(1 + \tilde{\alpha})] \beta$$

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Monthly Notices
of the
ROYAL ASTRONOMICAL SOCIETY

MNRAS 535, L49–L53 (2024)
Advance Access publication 2024 September 26

<https://doi.org/10.1093/mnras/rlae092>

The expected kinematic matter dipole is robust against source evolution

Sebastian von Hausegger  

Department of Physics, University of Oxford, Parks Road, Oxford OX1 3PU, UK

Accepted 2024 September 23. Received 2024 September 2; in original form 2024 July 29

arXiv:2404.07929

Yes!

(normalised)
redshift
distribution

$$\mathcal{D} = \int_0^{\infty} dz f(z) \mathcal{D}(z)$$

kinematic dipole
per redshift

Redshift dependence

Ellis & Baldwin (1984)

$$\tilde{\mathcal{D}} = [2 + \tilde{x}(1 + \tilde{\alpha})] \beta$$


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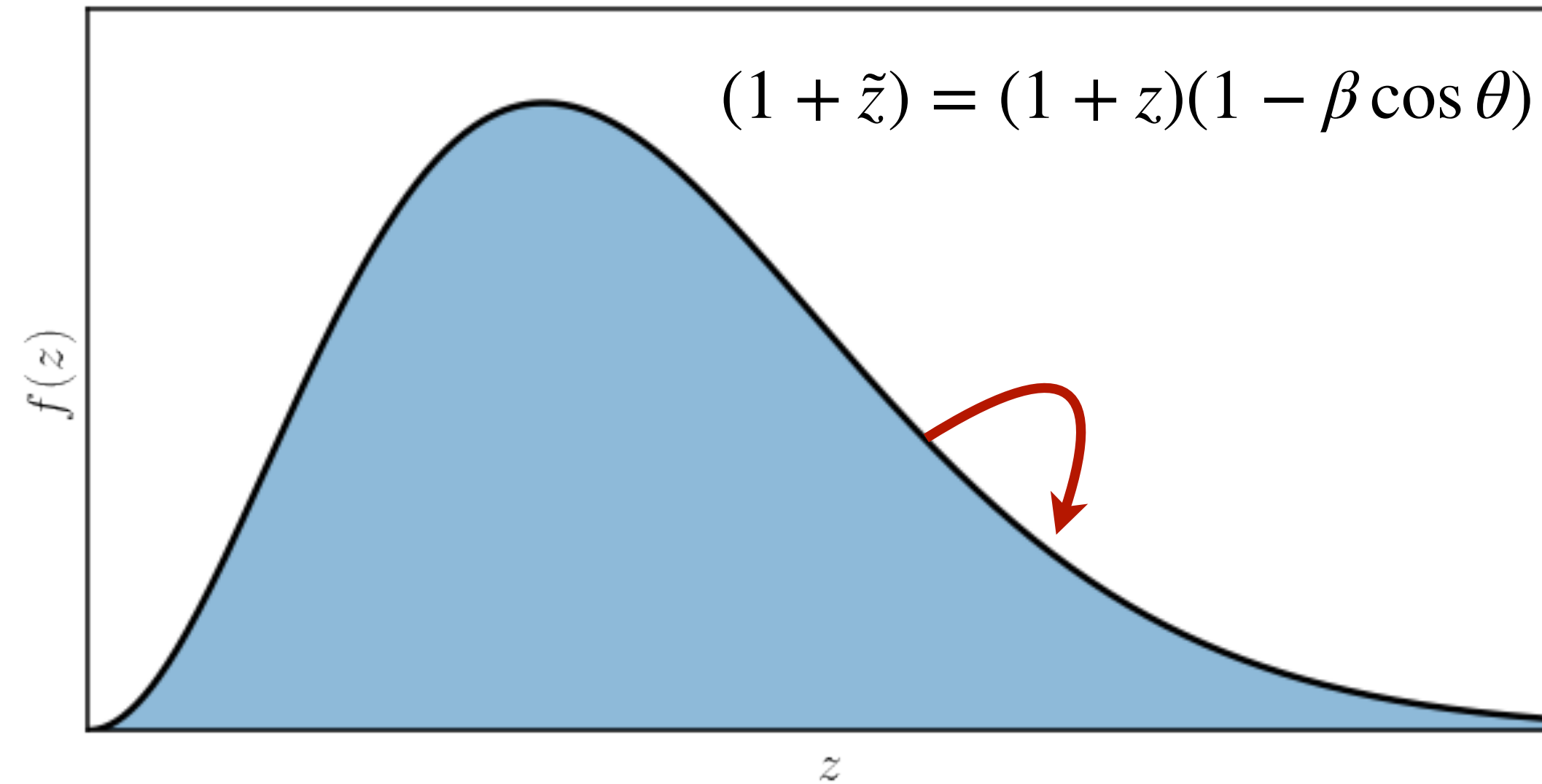
arXiv:2404.07929

(normalised)
redshift
distribution

$$\mathcal{D} = \int_0^{\infty} dz f(z) \mathcal{D}(z)$$

kinematic dipole
per redshift

Redshift dependence

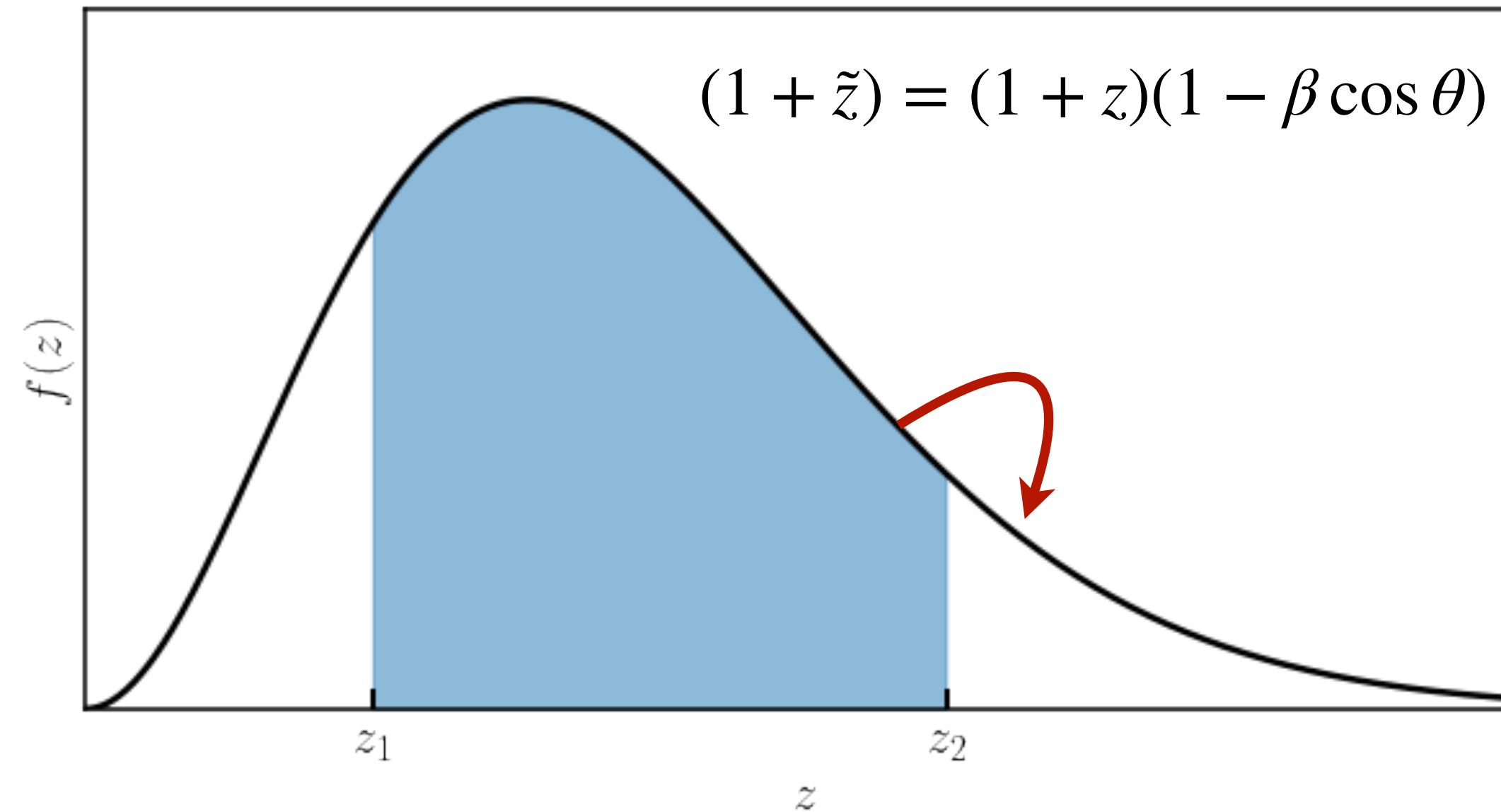


(normalised)
redshift
distribution

$$\mathcal{D} = \int_0^{\infty} dz f(z) \mathcal{D}(z)$$

kinematic dipole
per redshift

Redshift dependence

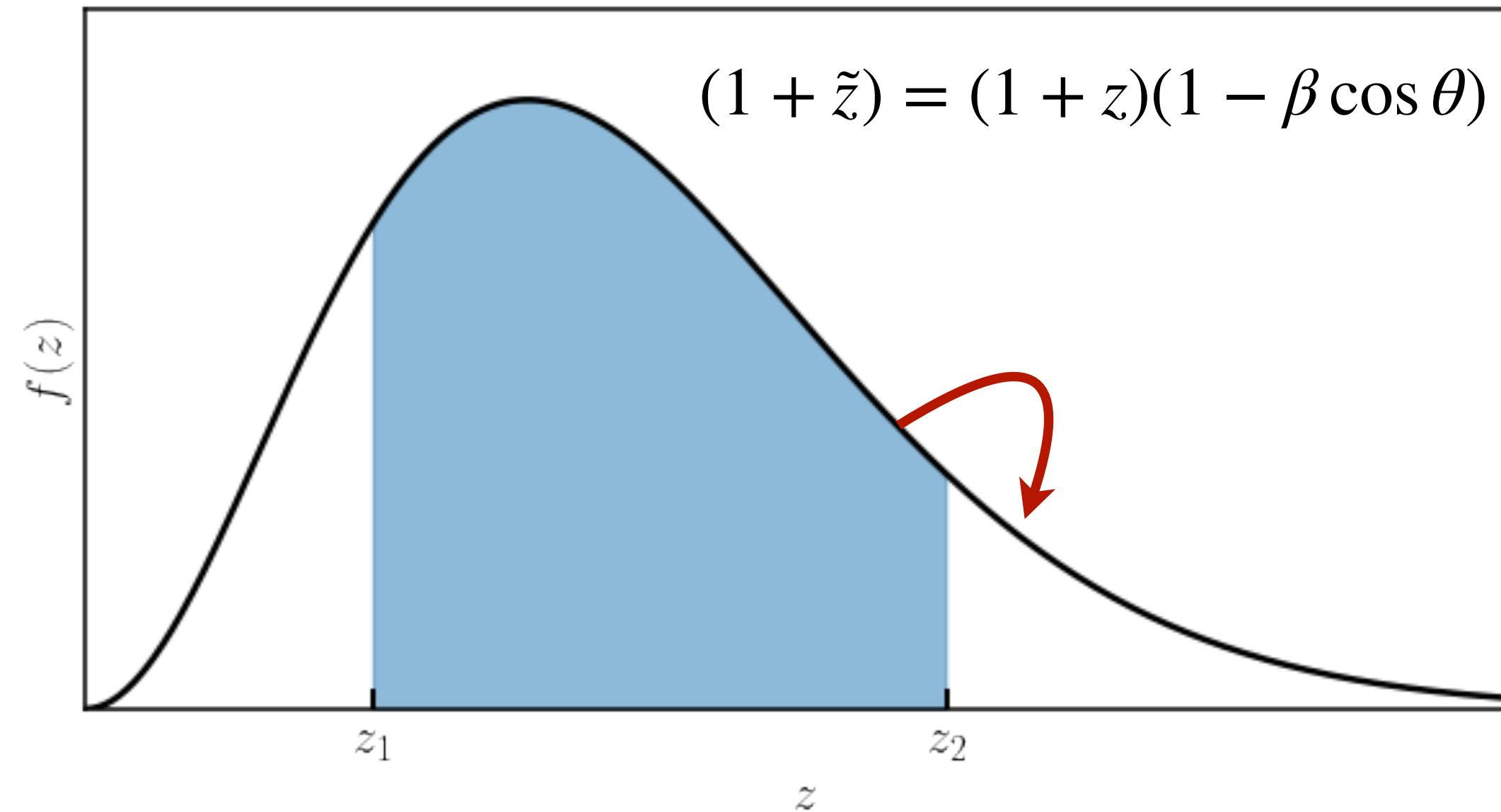


(normalised)
redshift
distribution

$$\mathcal{D} = \int_{z_1}^{z_2} dz f_b(z) \mathcal{D}(z)$$

kinematic dipole
per redshift

Redshift dependence

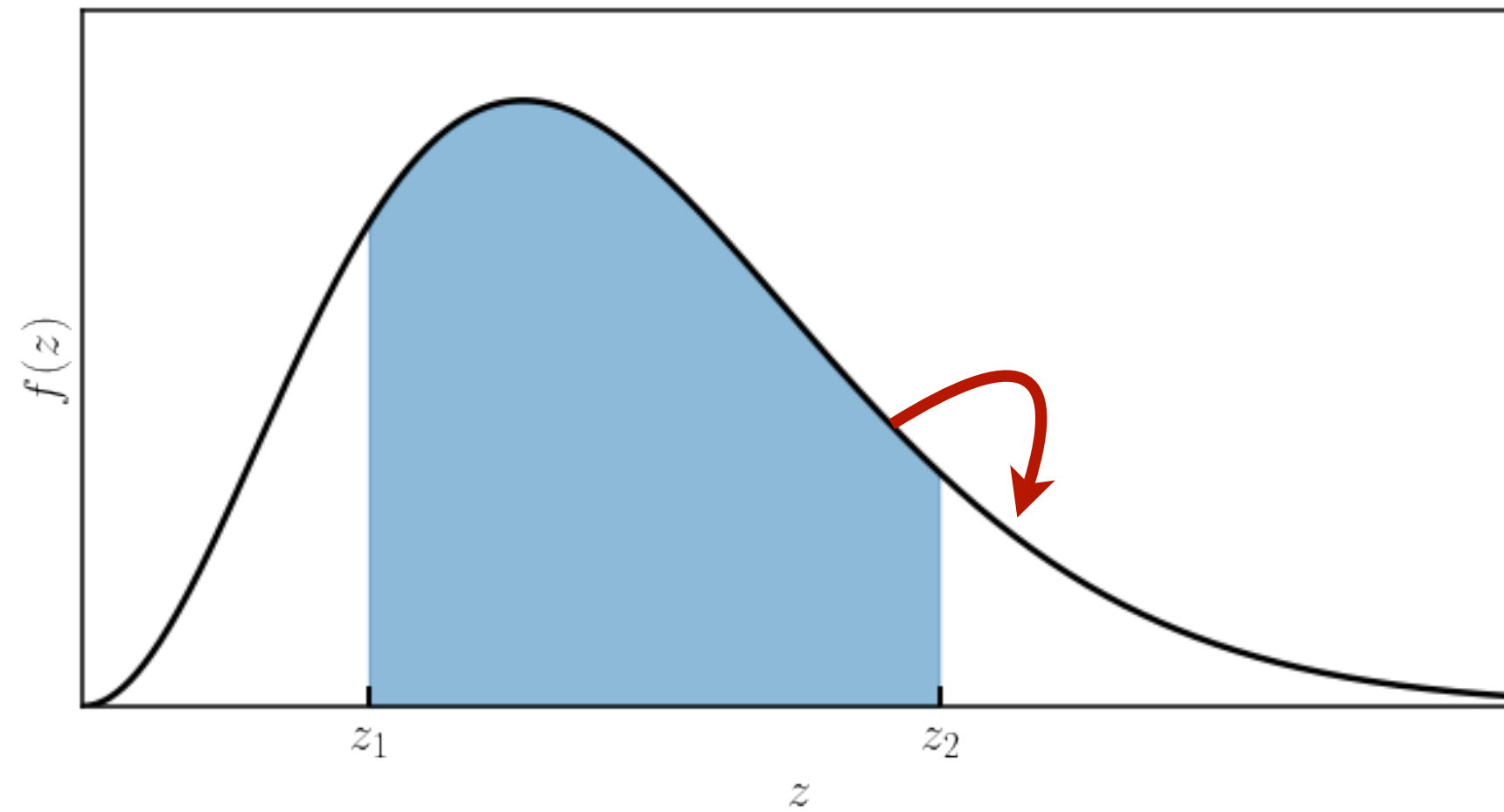


(normalised)
redshift
distribution

$$\mathcal{D} = \int_{z_1}^{z_2} dz f_b(z) \mathcal{D}(z)$$

kinematic dipole
per redshift

Redshift tomography



Redshift tomography of the kinematic matter dipole

Sebastian von Hausegger^{1,*} and Charles Dalang^{2,3,†}

¹Department of Physics, University of Oxford, Parks Road, Oxford OX1 3PU, United Kingdom

²School of Mathematical Sciences, Queen Mary University of London,
Mile End Road, London E1 4NS, United Kingdom

³Institute of Cosmology and Gravitation, University of Portsmouth,
Burnaby Road, Portsmouth PO1 3FX, United Kingdom

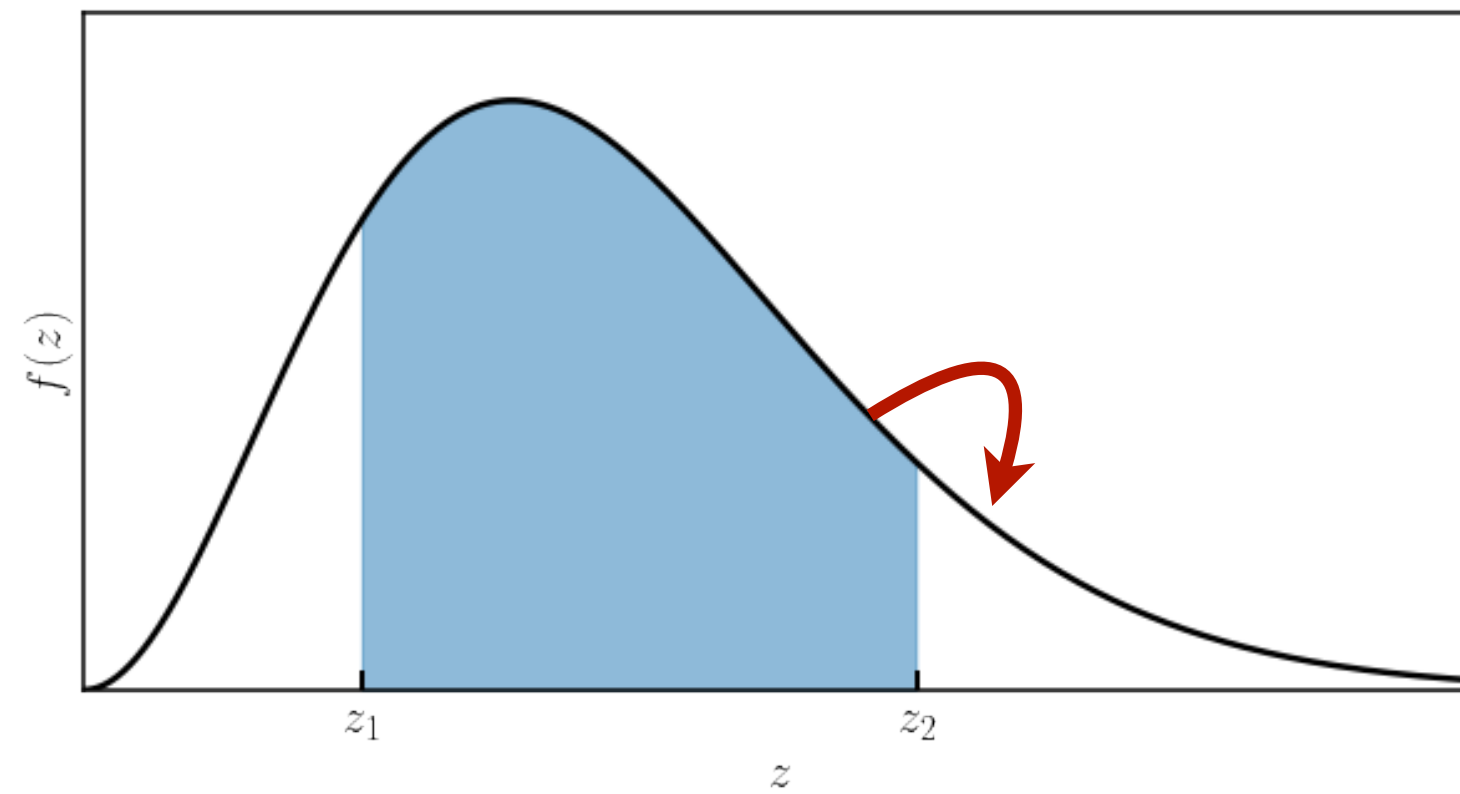
arXiv:2411.xxxx

(normalised)
redshift
distribution

$$\mathcal{D} = \int_{z_1}^{z_2} dz f_b(z) \mathcal{D}(z)$$

kinematic dipole
per redshift

Redshift tomography



Additional
"boundary term"

$$\mathcal{D} = \left[2 + \tilde{x}(1 + \tilde{\alpha}) + (1 + z)f_b(z) \right]_{z_1}^{z_2} \beta$$

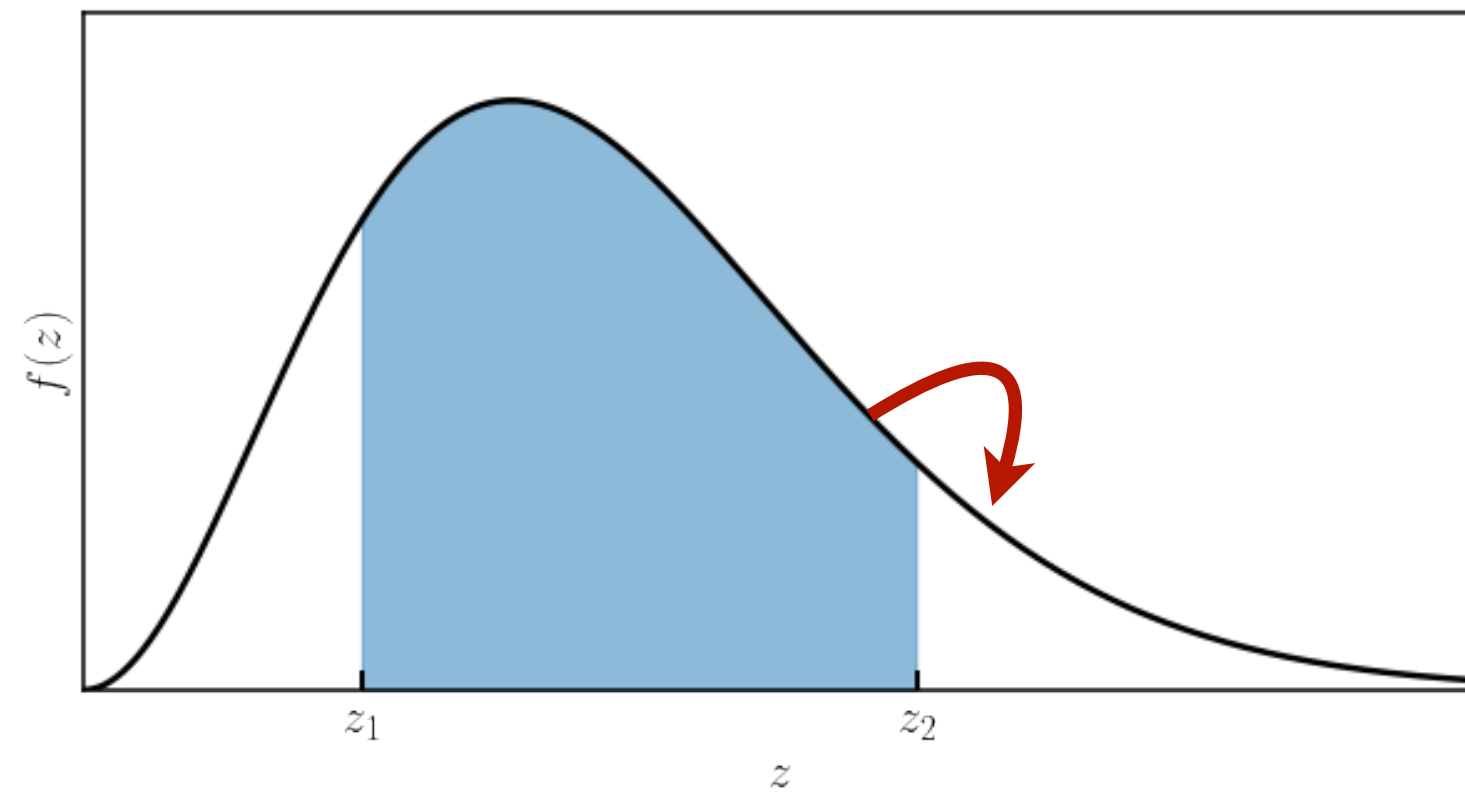
$$\equiv B(z_1, z_2)$$

(normalised)
redshift
distribution

$$\mathcal{D} = \int_{z_1}^{z_2} dz f_b(z) \mathcal{D}(z)$$

kinematic dipole
per redshift

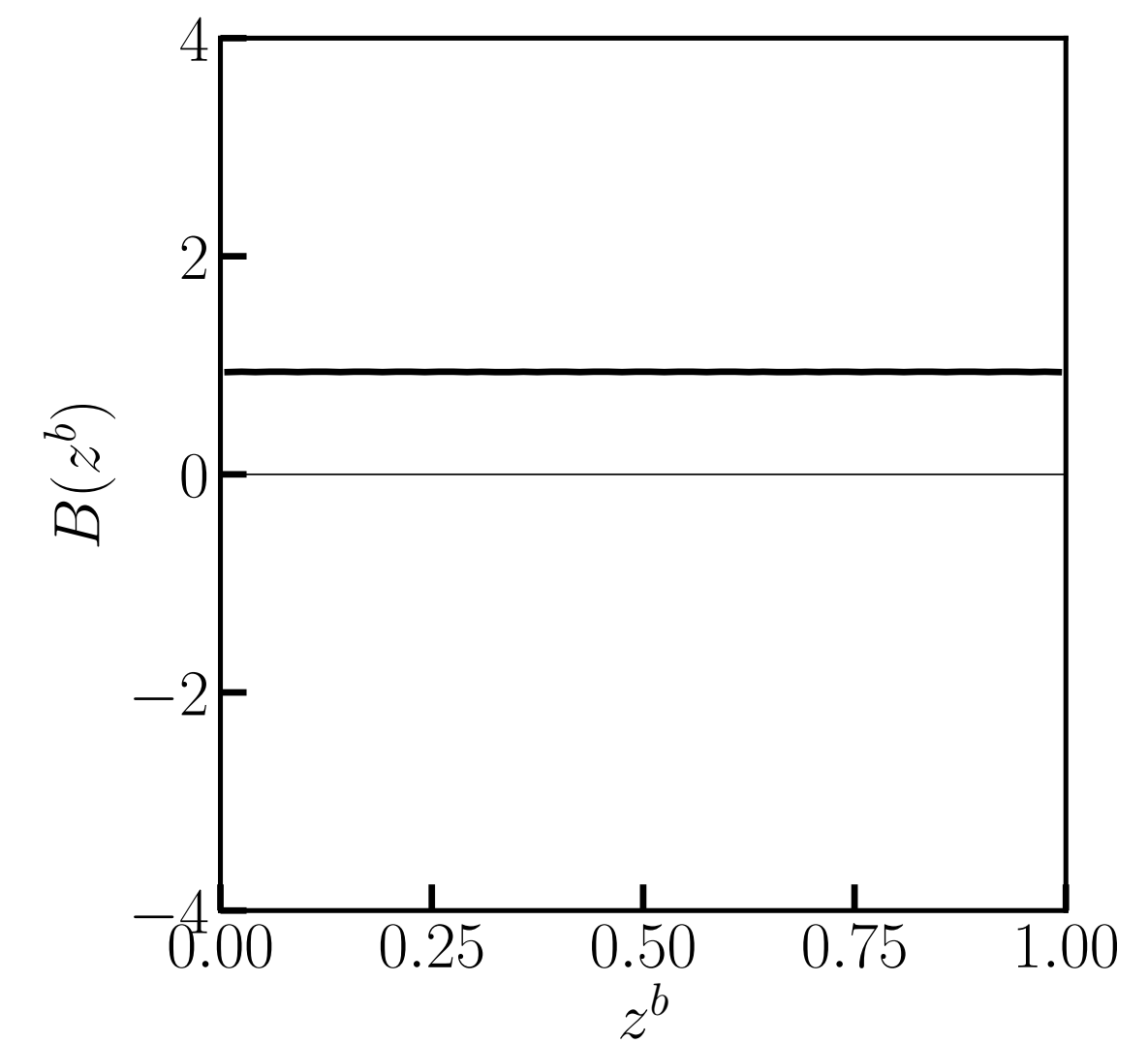
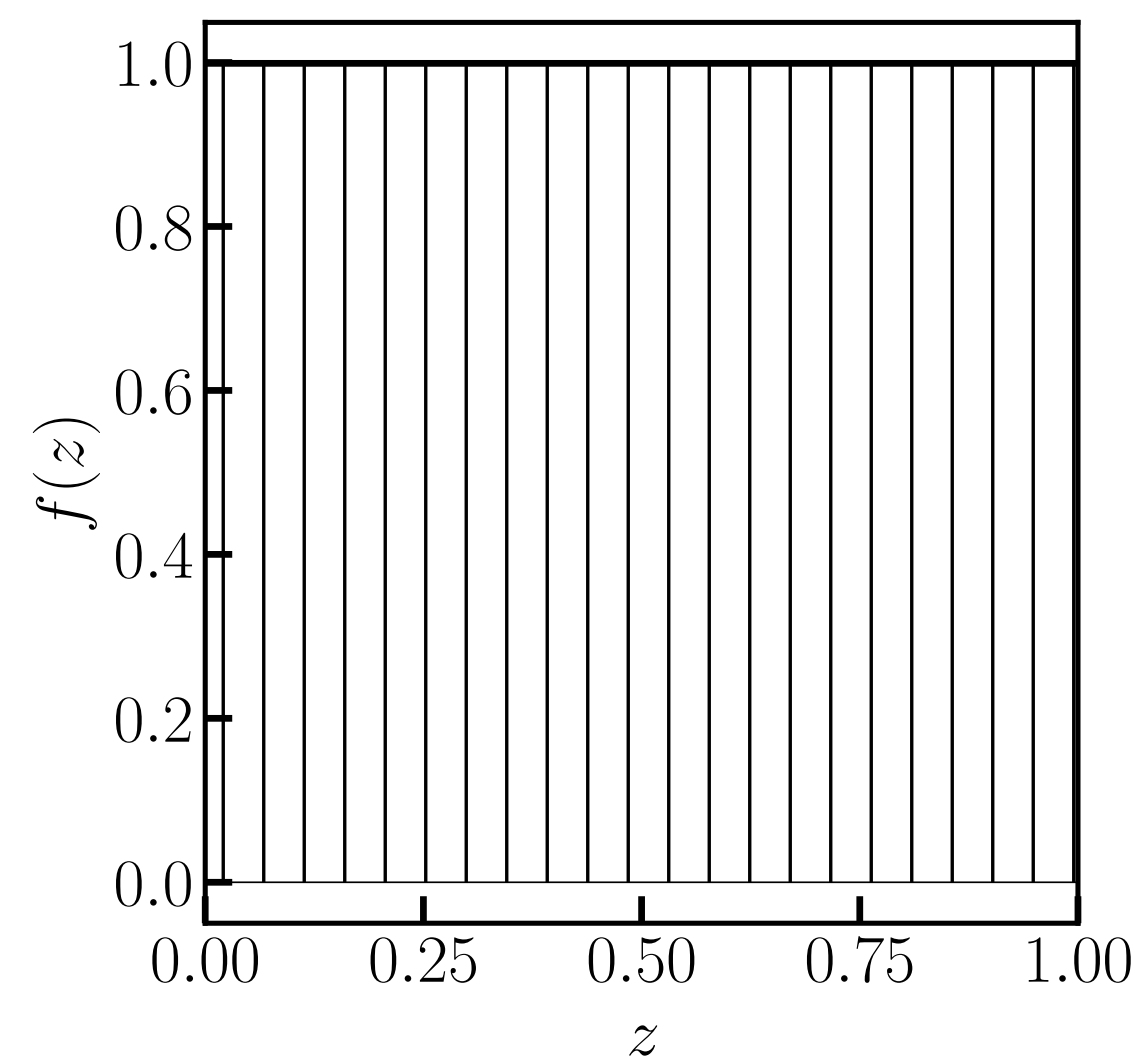
Redshift tomography



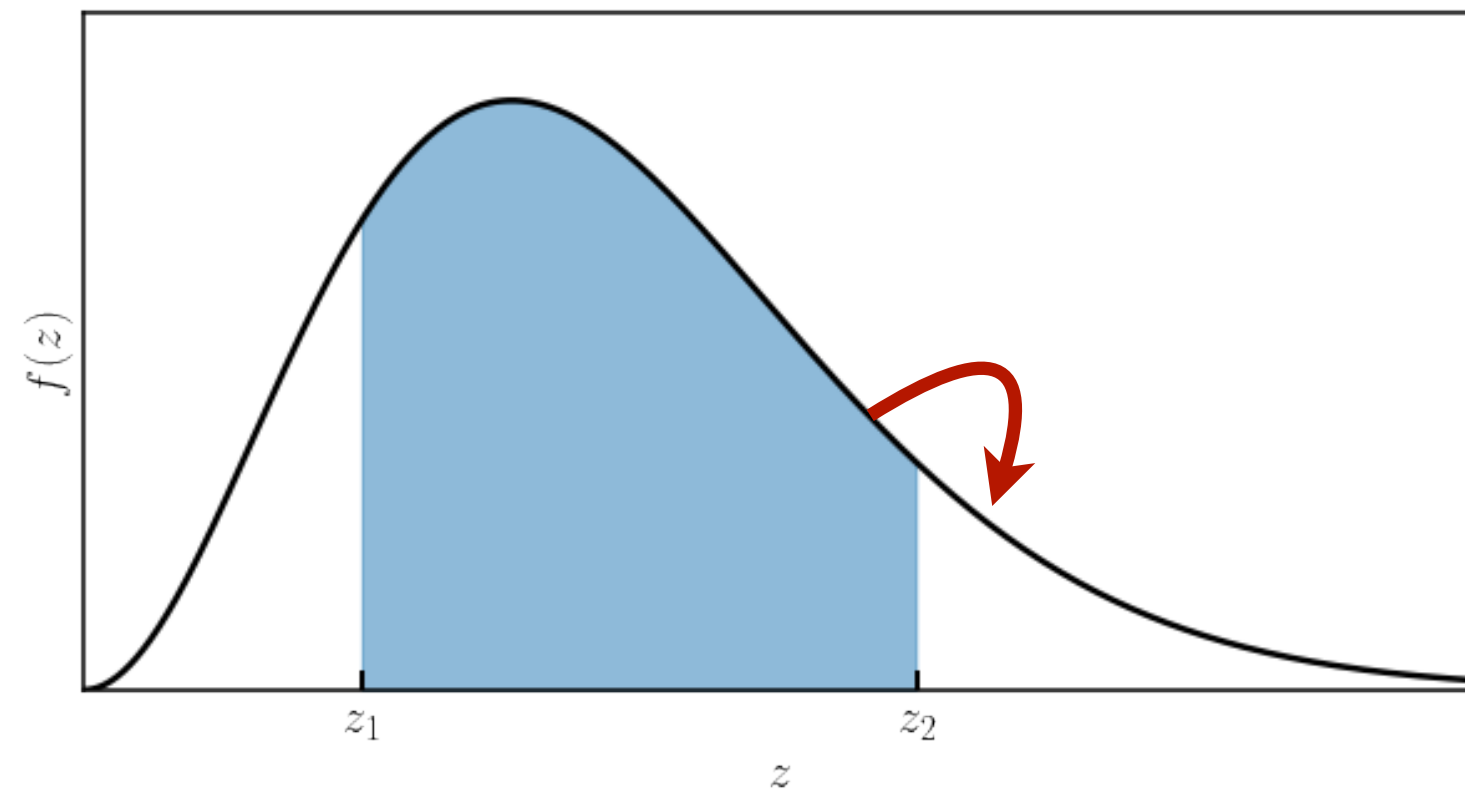
Additional
"boundary term"

$$\mathcal{D} = \left[2 + \tilde{x}(1 + \tilde{\alpha}) + (1 + z)f_b(z) \right] \Big|_{z_1}^{z_2} \beta$$

Constant redshift
distribution



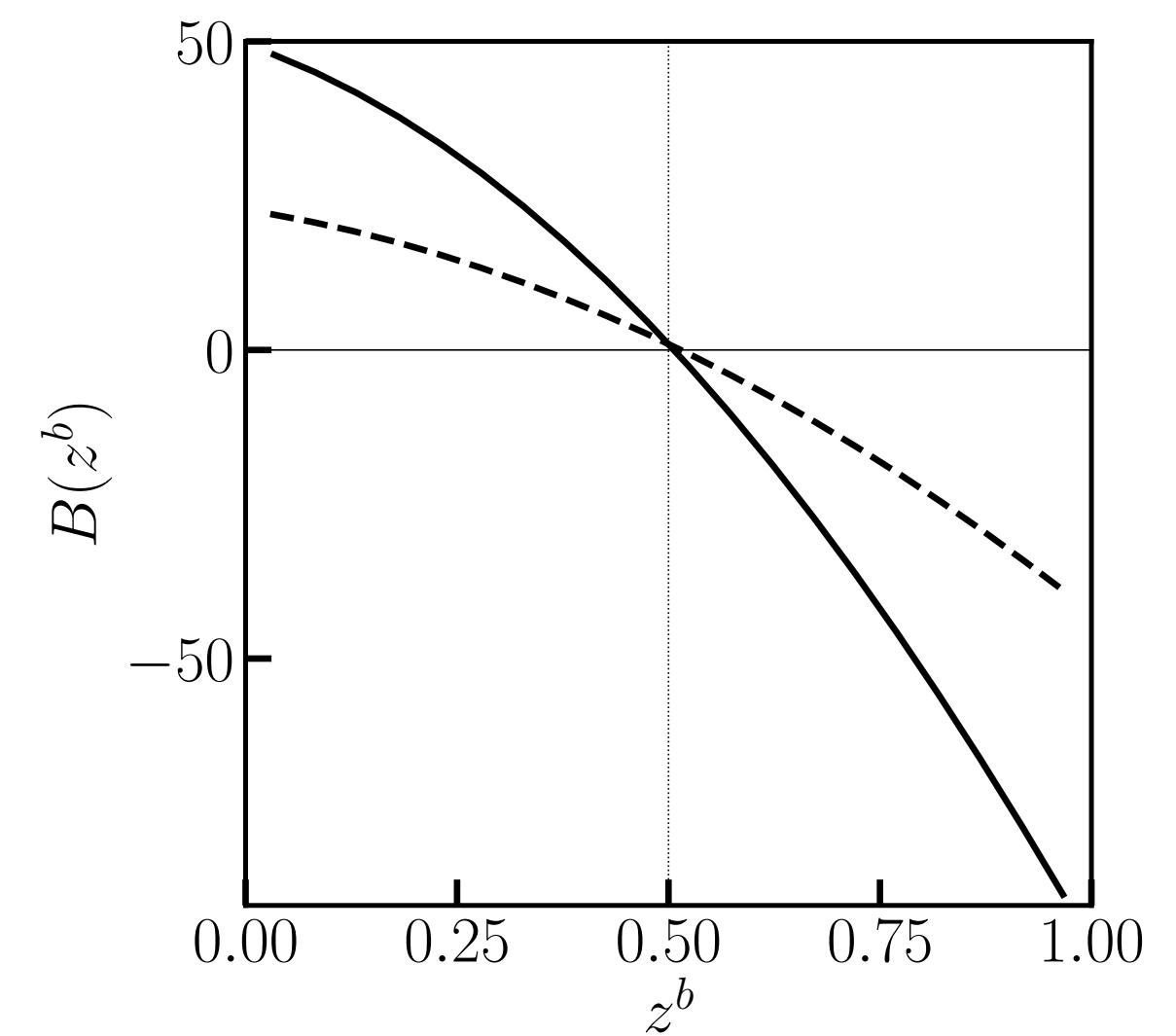
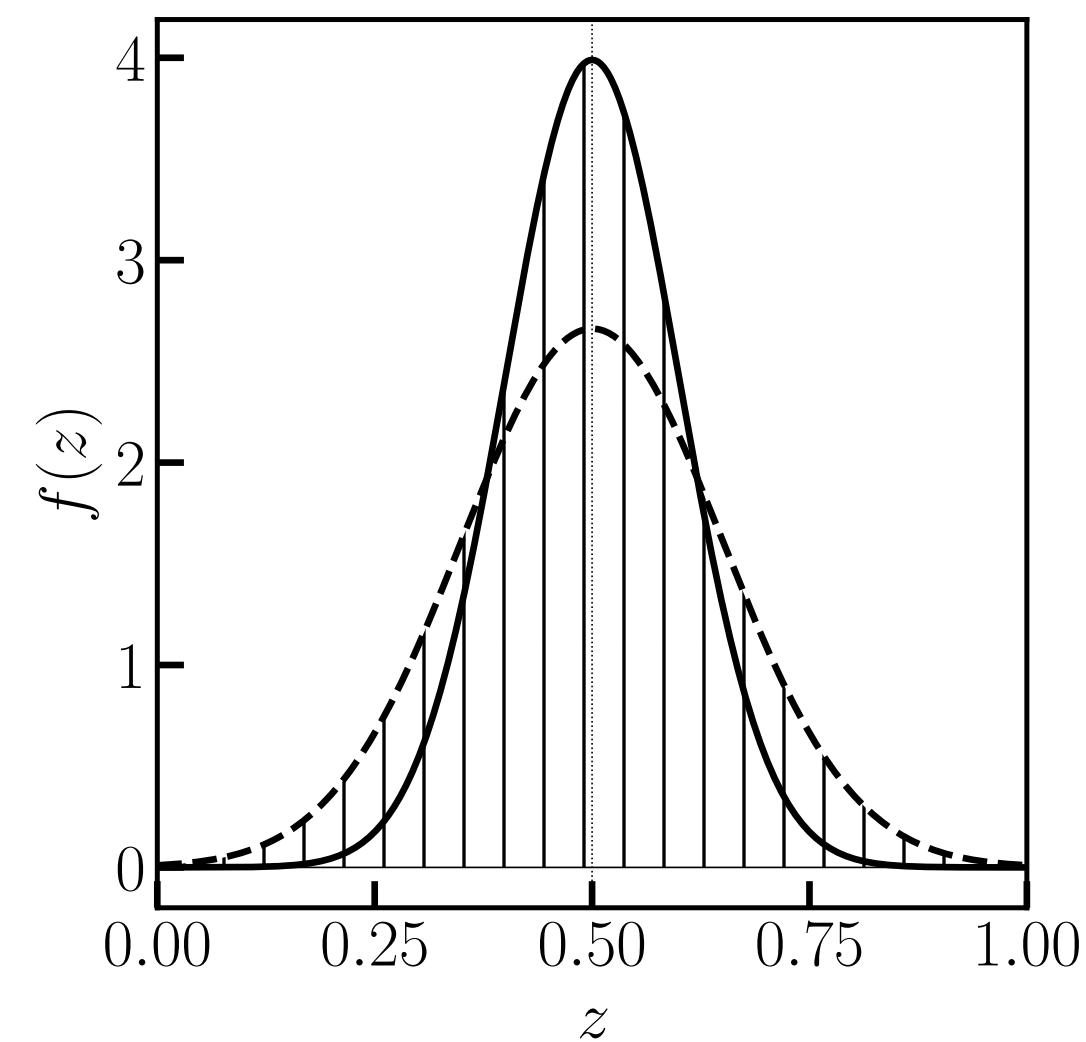
Redshift tomography



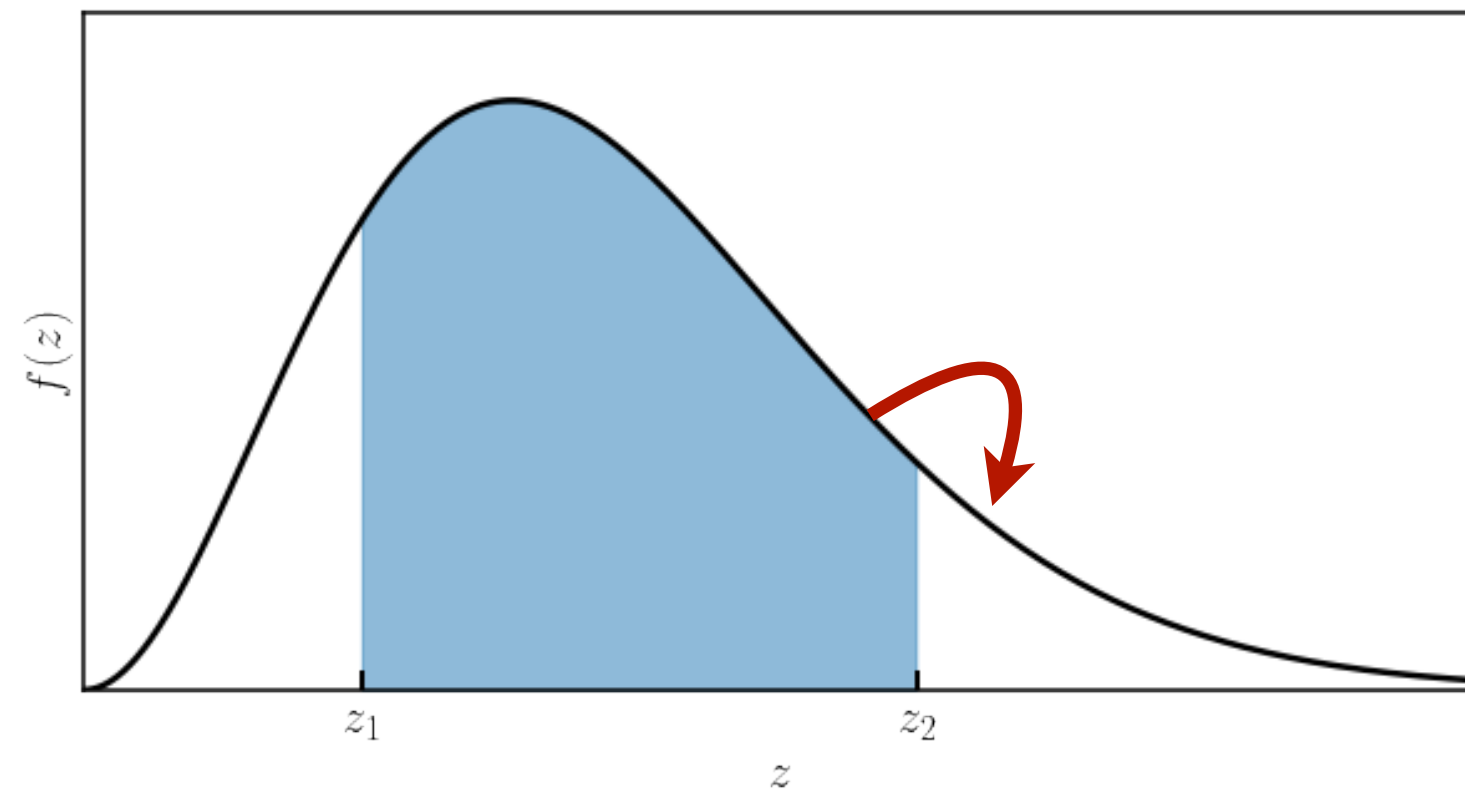
Additional
"boundary term"

$$\mathcal{D} = \left[2 + \tilde{x}(1 + \tilde{\alpha}) + (1 + z)f_b(z) \right] \Big|_{z_1}^{z_2} \beta$$

Gaussian redshift
distributions



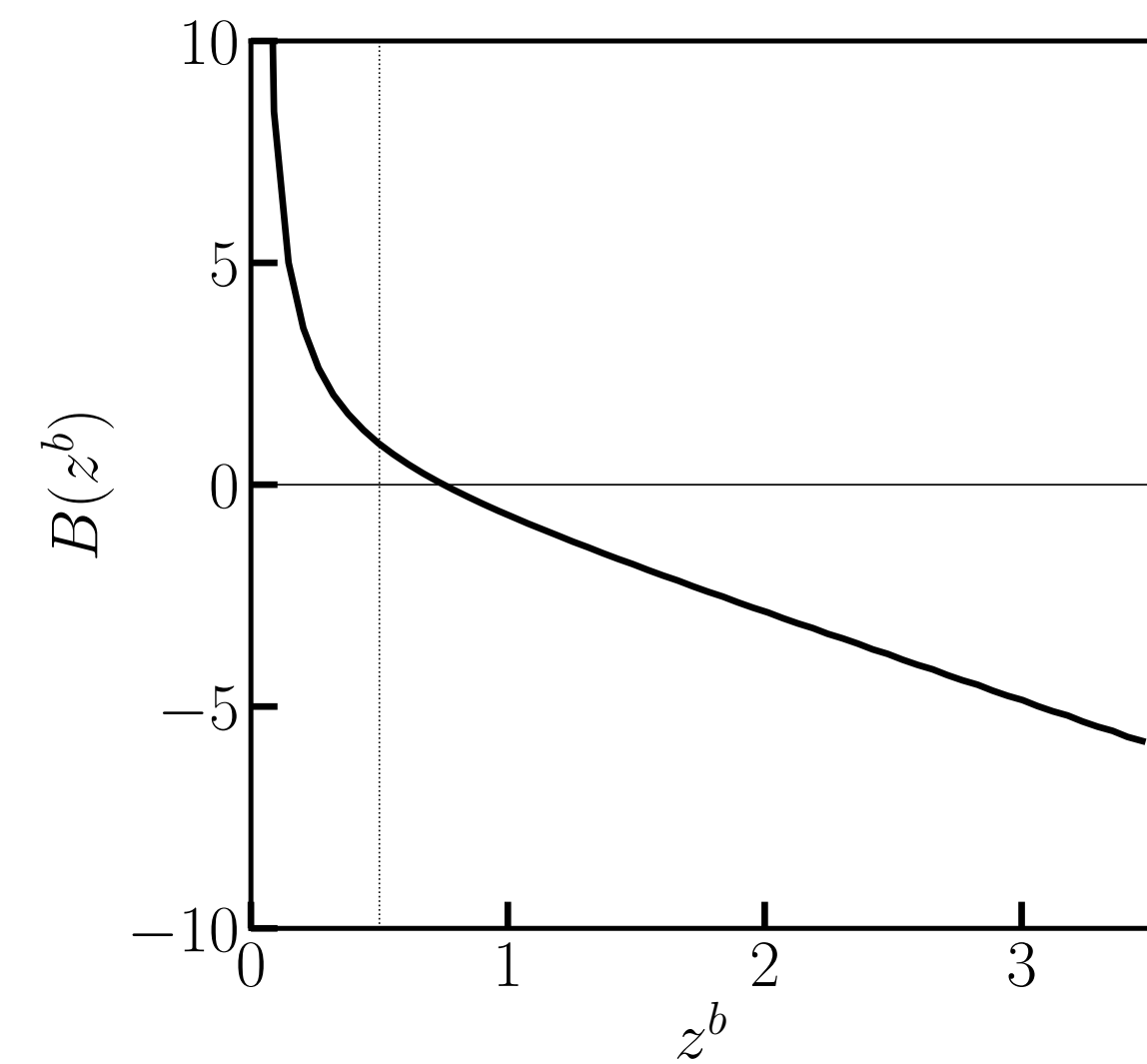
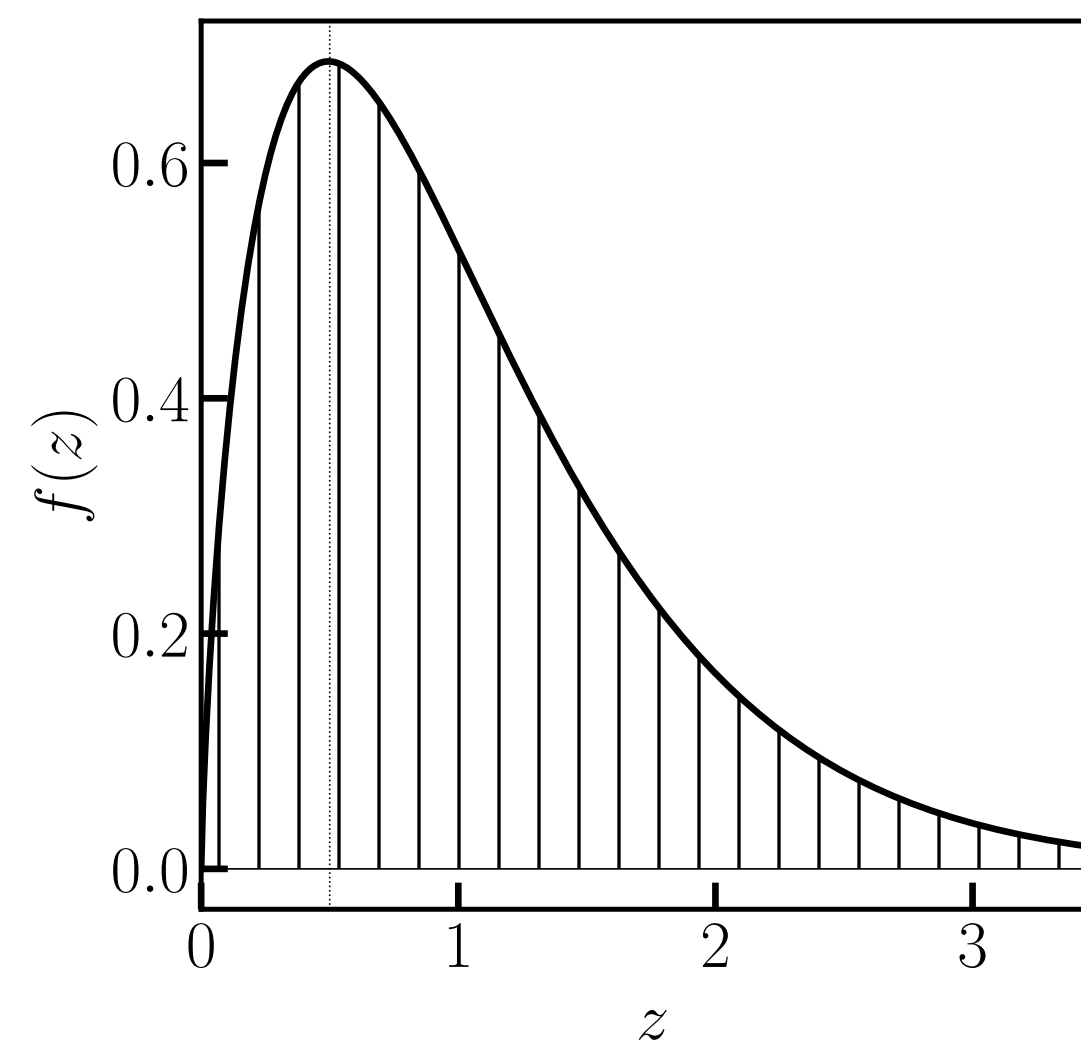
Redshift tomography



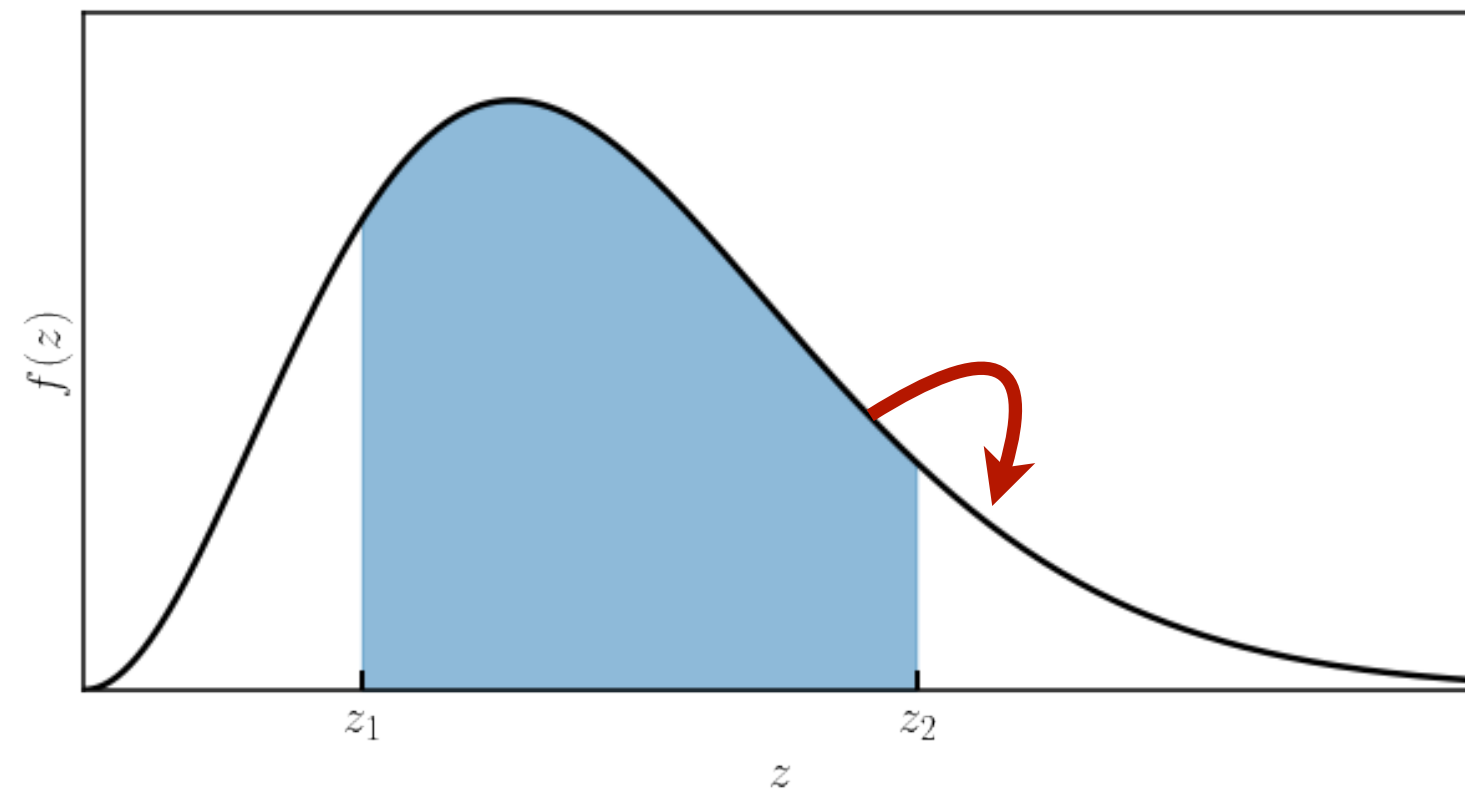
Additional
“boundary term”

$$\mathcal{D} = \left[2 + \tilde{x}(1 + \tilde{\alpha}) + (1 + z)f_b(z) \right] \Big|_{z_1}^{z_2} \beta$$

**NVSS redshift
distribution**



Redshift tomography – Selection functions



$$W_b(z) = \int_{z_1}^{z_2} dz' P(z', z)$$

**Top-hat in phot- z
gives selection
 W_b in spec- z**

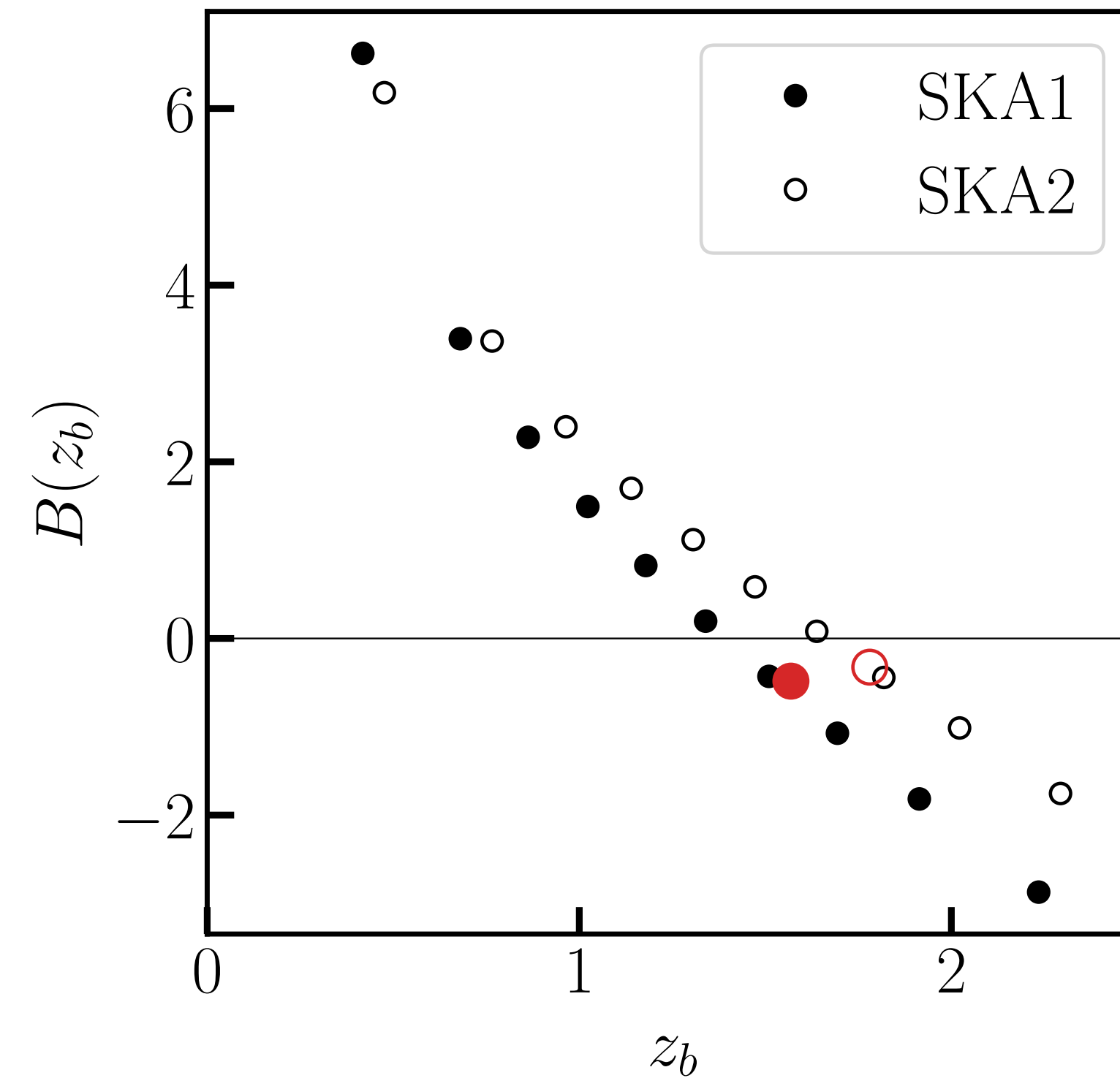
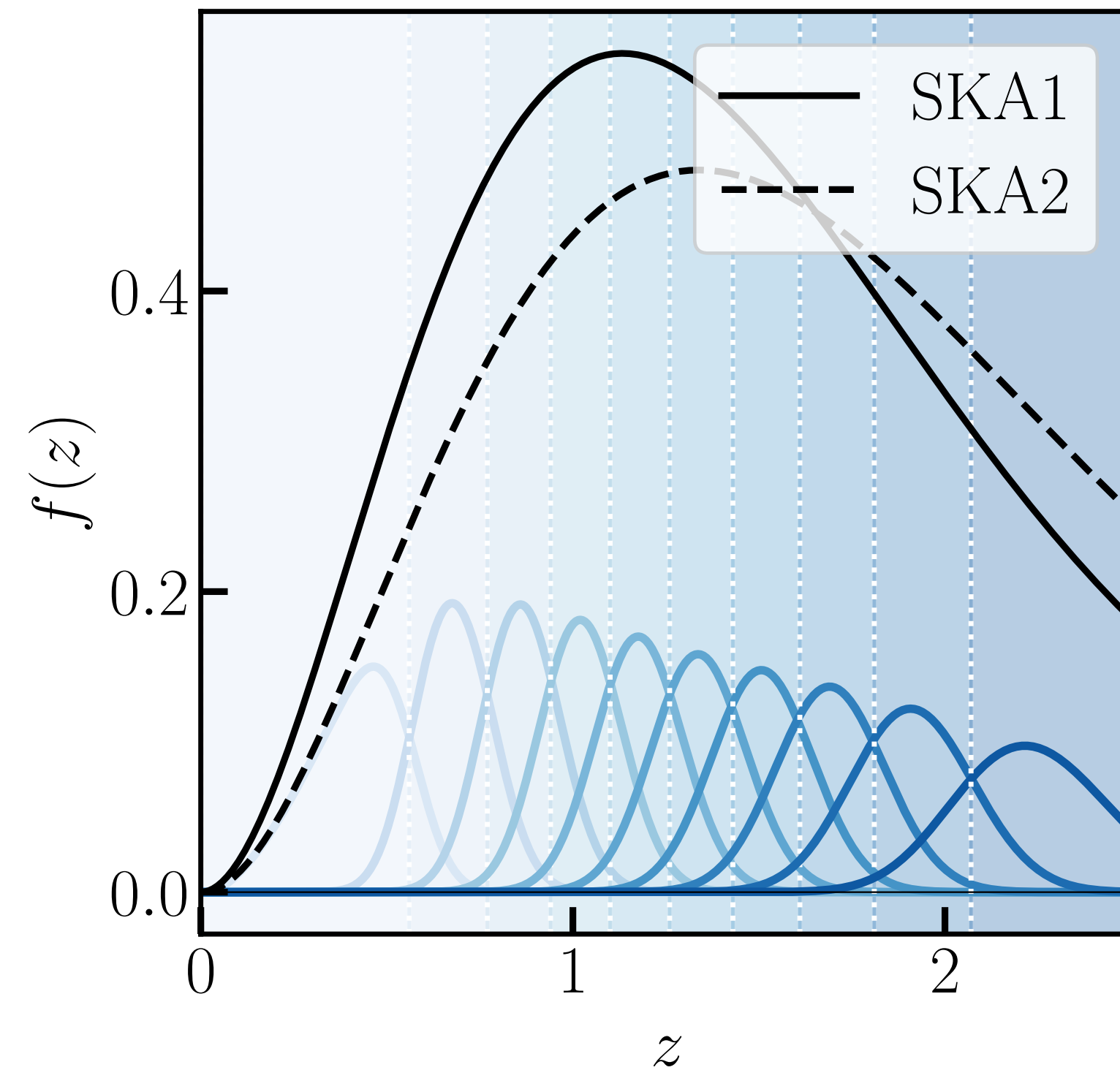
**Redshift
distribution**

$$n_b(z) = n(z) W_b(z)$$

$$\mathcal{D} = \left[2 + \tilde{x}(1 + \tilde{\alpha}) - \int_0^{\infty} dz f_b(z) \frac{d \log W(z)}{d \log(1+z)} \right] \beta$$

**General
“boundary term”**

Redshift tomography with SKA



Redshift distributions from Harrison et al. (2016)

Boundary terms' size comparable to Ellis&Baldwin signal

Redshift cuts to remove contamination adds boundary terms

Some requirements for Science Book Chapter

***Number counts* – Which number densities can AA4 provide?**

**(Shot noise, sky coverage,
contaminants/systematics...)**

***Redshift tomography* – Which accuracy for redshift distributions?**

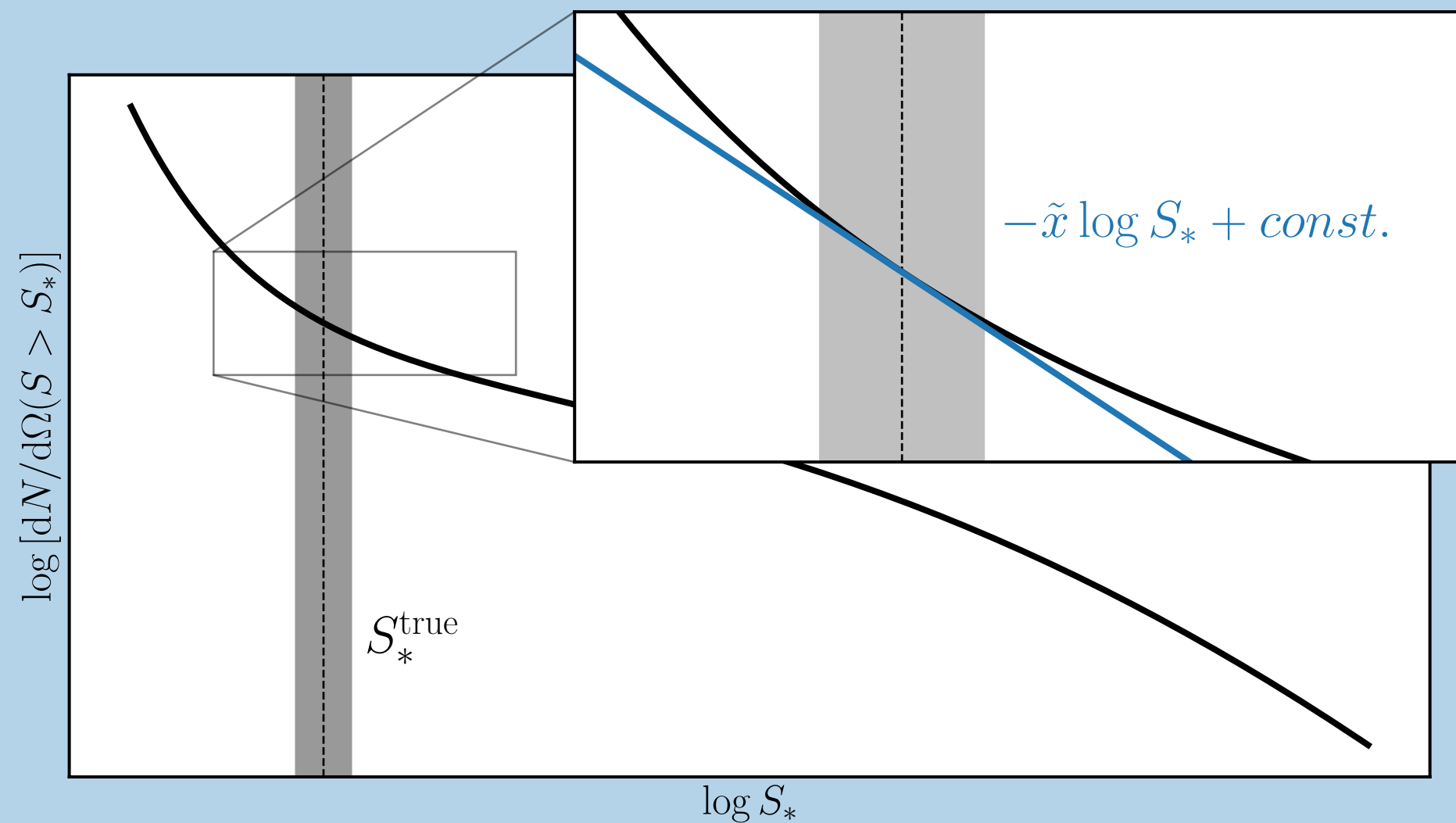
**(cross-matched spec-z sample,
estimate biases...)**

Future directions (also for Science Book Chapter)

Flux cut dependence of the kinematic matter dipole

$$\mathcal{D}(S_*) = [2 + \tilde{x}(S_*)(1 + \tilde{\alpha}(S_*))] \beta$$

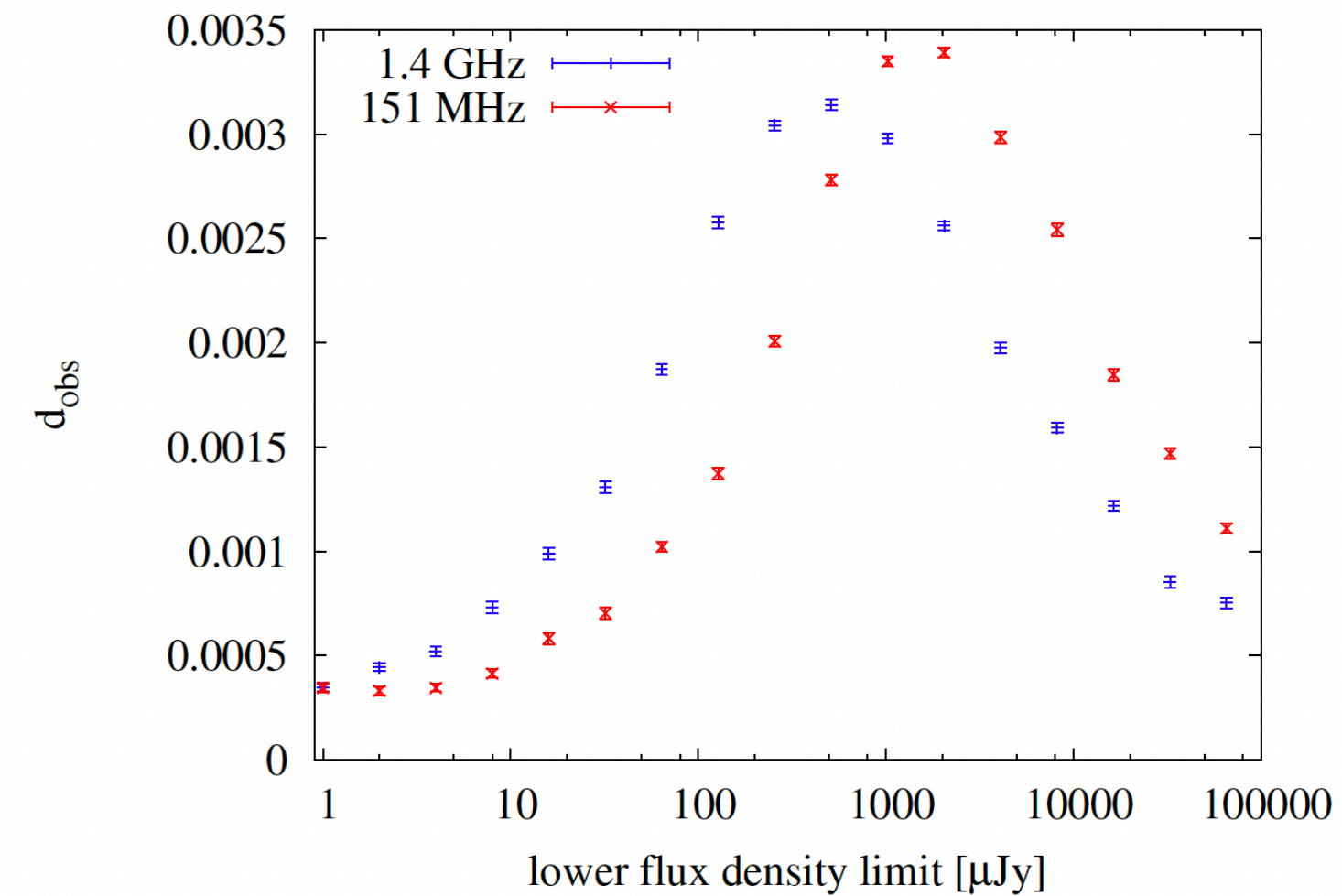
Also dependent on
luminosity function
– **but projected
counts sufficient**



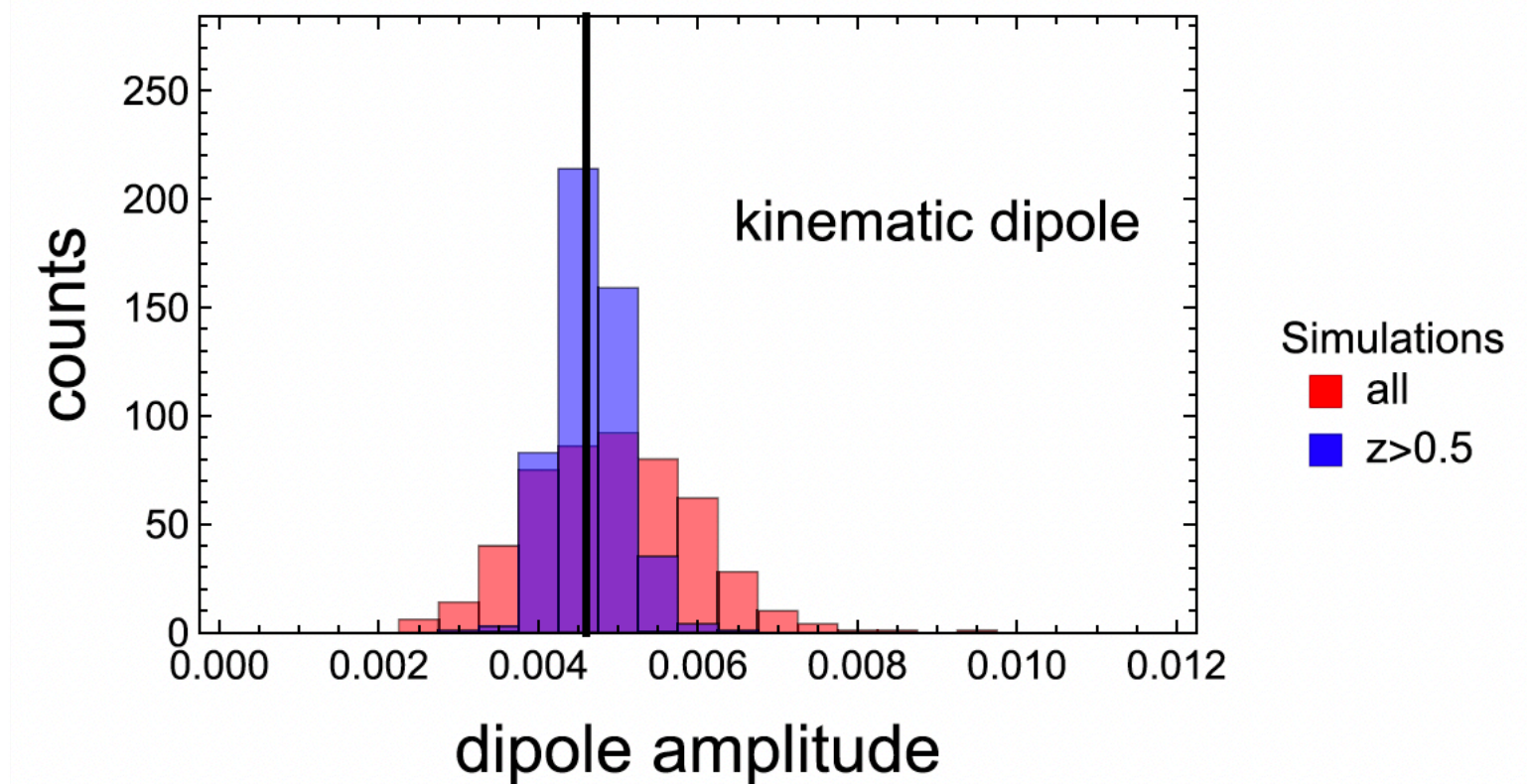
SvH (2024) [arXiv:2404.07929]

Future directions (also for Science Book Chapter)

Flux cut dependence of the kinematic matter dipole



Redshift cut dependence of the kinematic matter dipole



from Science Book and Red Book

Future directions (also for Science Book Chapter)

Kinematic matter dipole in HI

Dependent on
luminosity function



$$\mathcal{D}_{IM} = \left[3 + \frac{\dot{H}}{H} - b_e \right] \beta$$

Maartens et al. (2017)

Specific take aways

SvH & Dalang (2024) [[arXiv:2411.xxxx](#)]

The matter dipole in redshift bins is not the same as expected from Ellis&Baldwin alone

Strong dependency on redshift distribution (at edges of bins)

Photometric measurements require modelling of $W(z)$

SKA but also Euclid, SPHEREx, and LSST will leverage this