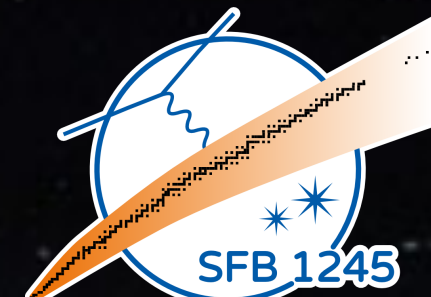




TECHNISCHE
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DARMSTADT



INAF
ISTITUTO NAZIONALE
DI ASTROFISICA

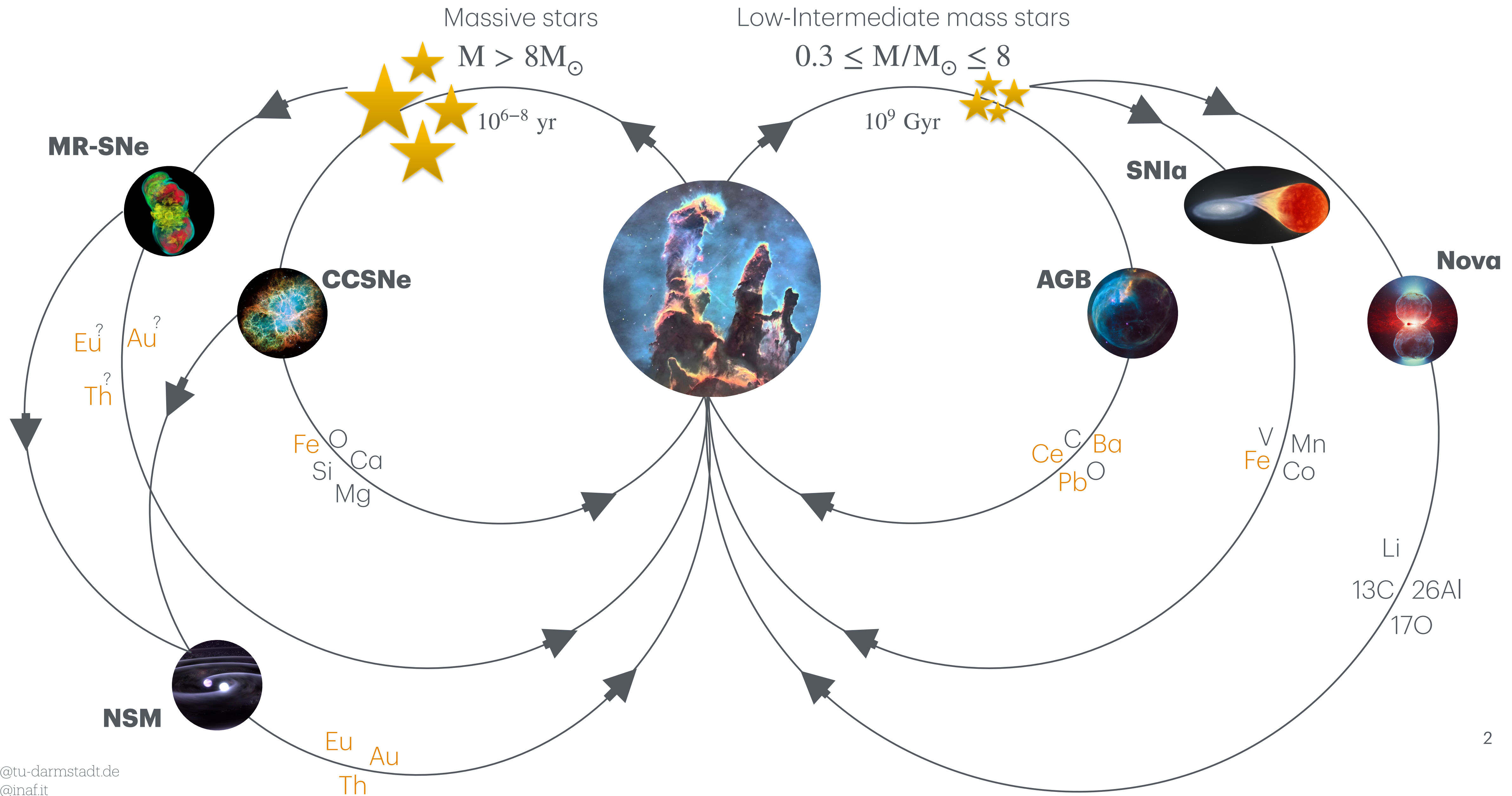
Chemical evolution of NC-elements



Marta Molero

s, i, & r Element Nucleosynthesis (sirEN) Conference

Introduction: chemical evolution



Introduction: chemical evolution

- The evolution of the mass of gas in the form of the chemical element i

$$\dot{M}_{\text{gas},i}(R, \theta, t) = -\psi(R, \theta, t)X_i(R, \theta, t) + X_{i,A}A(R, \theta, t) - X_i(R, \theta, t)W(R, \theta, t) - X_i(R, \theta, t)\dot{M}_{BH}(R, \theta, t) + \dot{R}_i(R, \theta, t)$$

Emanuele's talk for 2D (Spitoni et al. 2019,2023; Vasini et al. 2025)
Benjamin's talk for 3D (Wehmeyer et al. 2023)

Introduction: chemical evolution

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$$\dot{M}_{\text{gas},i}(R, \theta, t) = -\psi(R, \theta, t)X_i(R, \theta, t) + \underbrace{X_{i,A}A(R, \theta, t)}_{\text{accretion of gas through infall}} - \underbrace{X_i(R, \theta, t)W(R, \theta, t)}_{\text{lost of gas galactic winds}} - X_i(R, \theta, t)\dot{M}_{BH}(R, \theta, t) + \dot{R}_i(R, \theta, t)$$

accretion of
gas through
infall

lost of gas galactic
winds

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accretion of
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Introduction: chemical evolution

- The evolution of the mass of gas in the form of the chemical element i

$$\dot{M}_{\text{gas},i}(R, \theta, t) = \underbrace{-\psi(R, \theta, t)X_i(R, \theta, t)}_{\text{lost of gas because of SF processes}} + \underbrace{X_{i,A}A(R, \theta, t)}_{\text{accretion of gas through infall}} - \underbrace{X_i(R, \theta, t)W(R, \theta, t)}_{\text{lost of gas galactic winds}} - \underbrace{X_i(R, \theta, t)\dot{M}_{BH}(R, \theta, t)}_{\text{lost of gas by feeding the central BH}} + \dot{R}_i(R, \theta, t)$$

lost of gas because of
SF processes

accretion of
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Introduction: chemical evolution

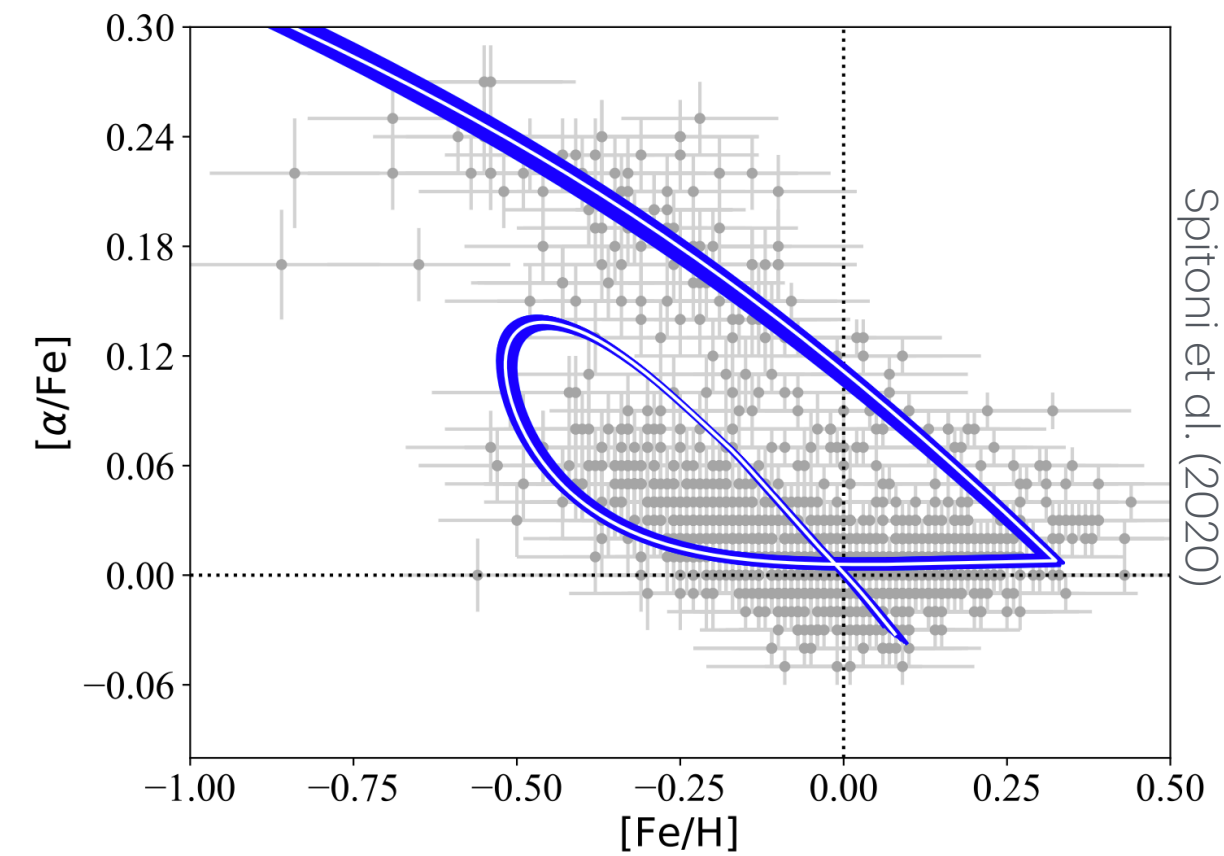
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Emanuele's talk for 2D (Spitoni et al. 2019,2023; Vasini et al. 2025)
Benjamin's talk for 3D (Wehmeyer et al. 2023)

Homogeneous models:

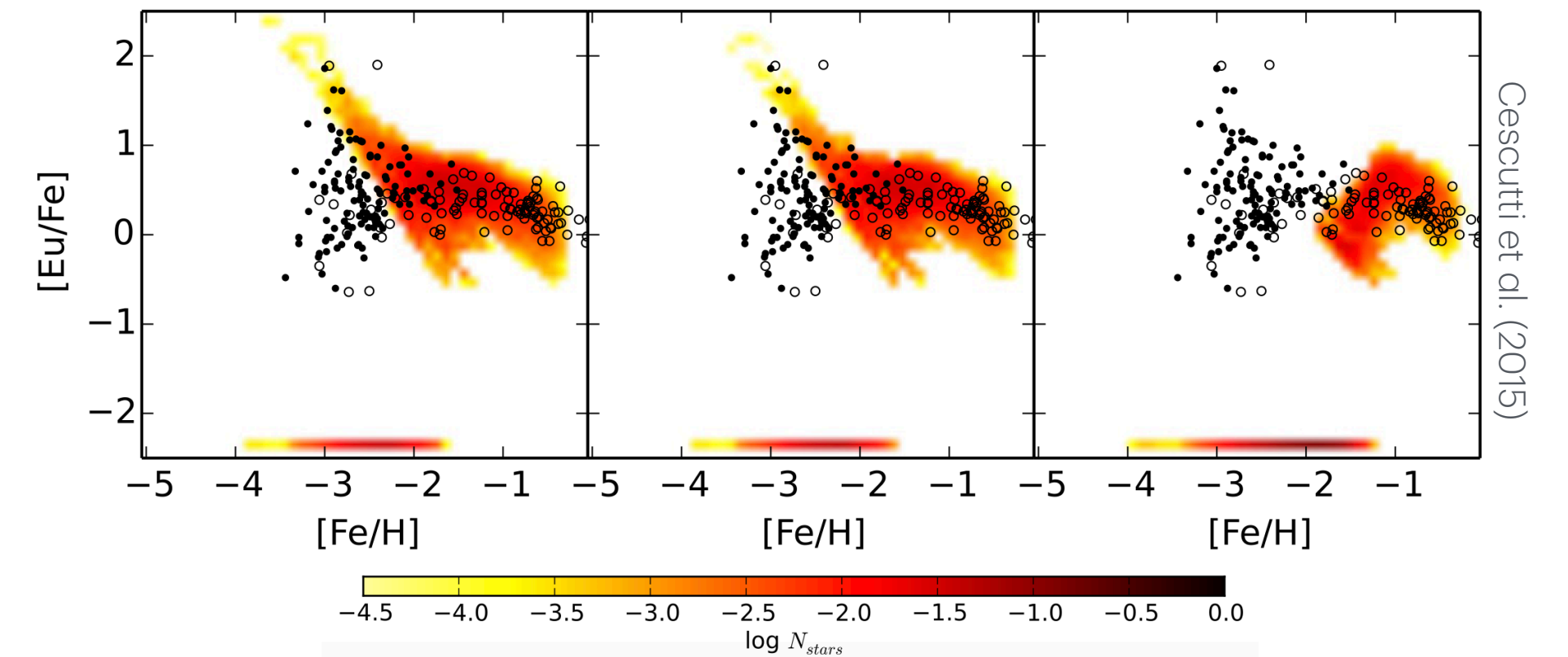
- One or multi-Zone system treated as a single homogeneous zone



Matteucci&Greggio 1986; Chiappini+97; Mollà+15; Côté+17; Spitoni+23;...

Stochastic models:

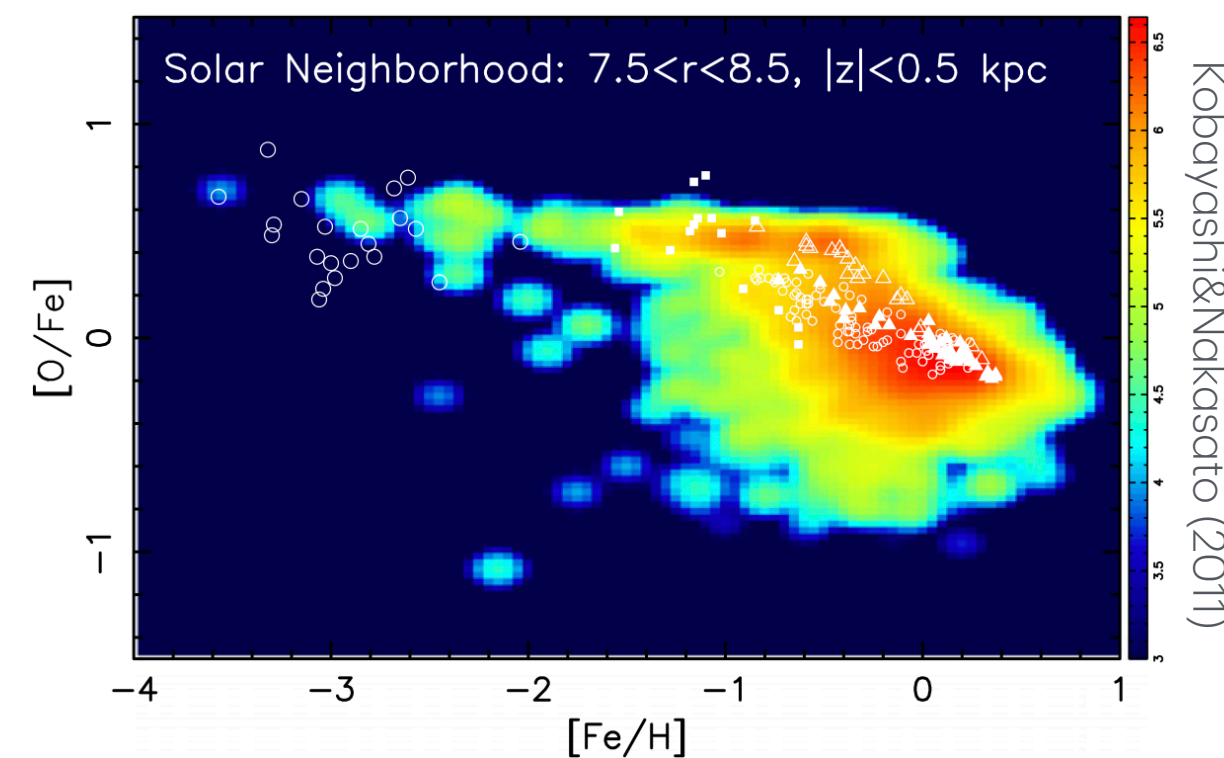
- System divided into multiple zones: each evolves independently with stochastic sampling of stellar mass distribution



Argast+00; Cescutti 2008; Hishimaru+15;...

Chemodynamical simulations:

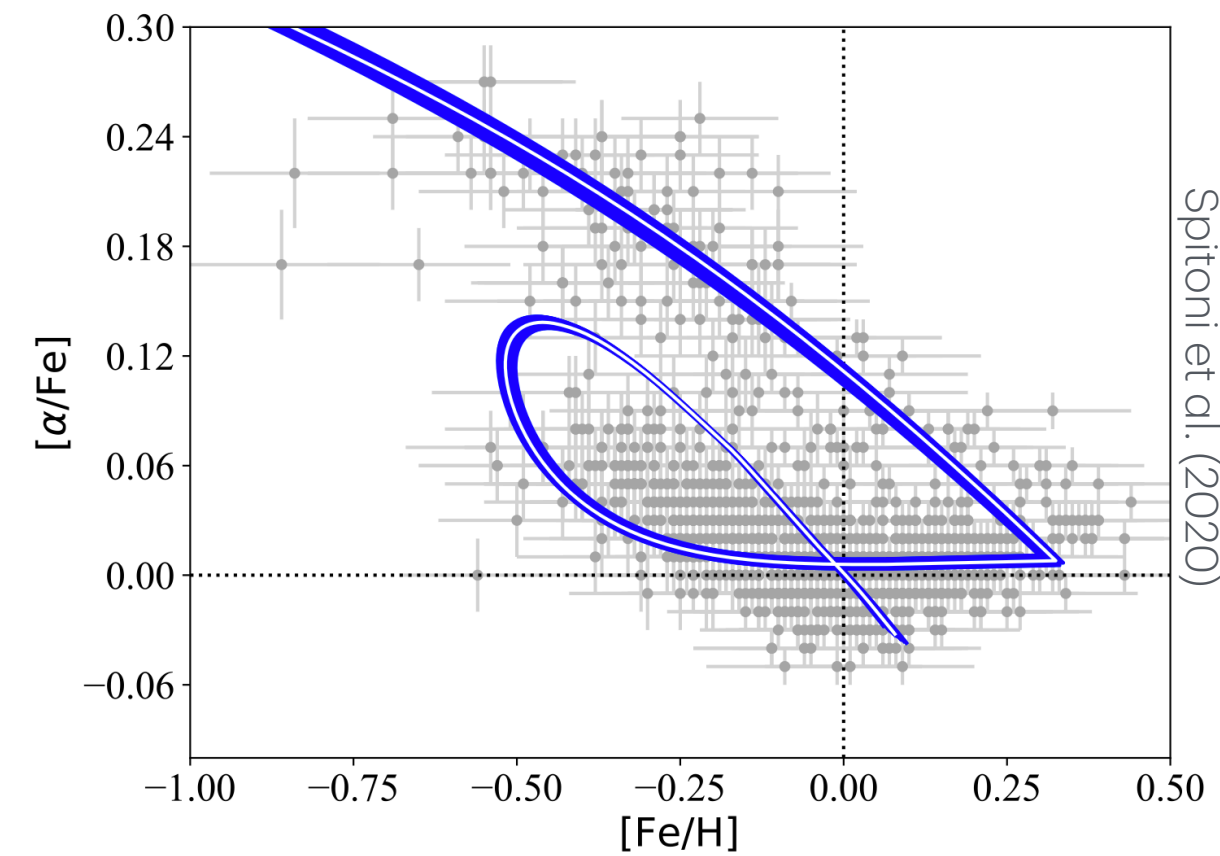
- Integrate chemical evolution + dynamical processes in a cosmological framework



Kobayashi 2004; Scannapieco+22

Homogeneous models:

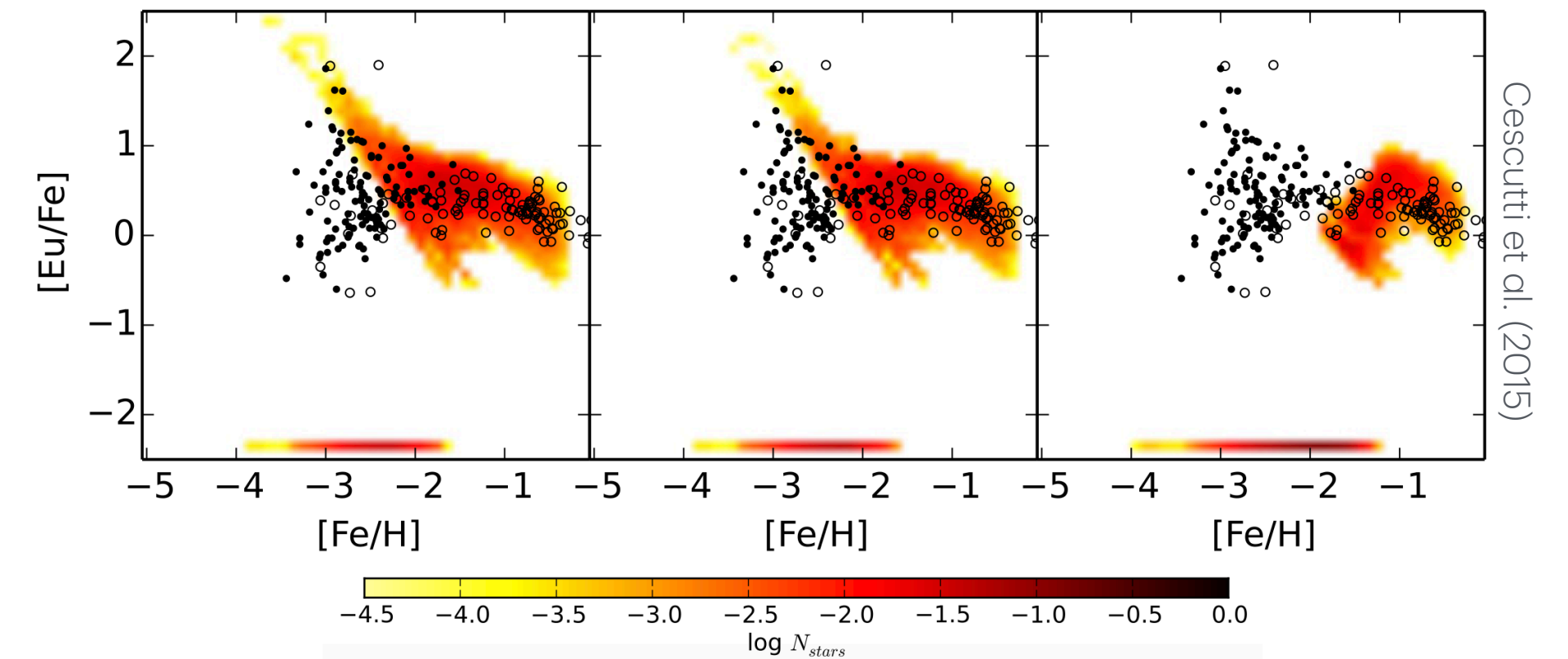
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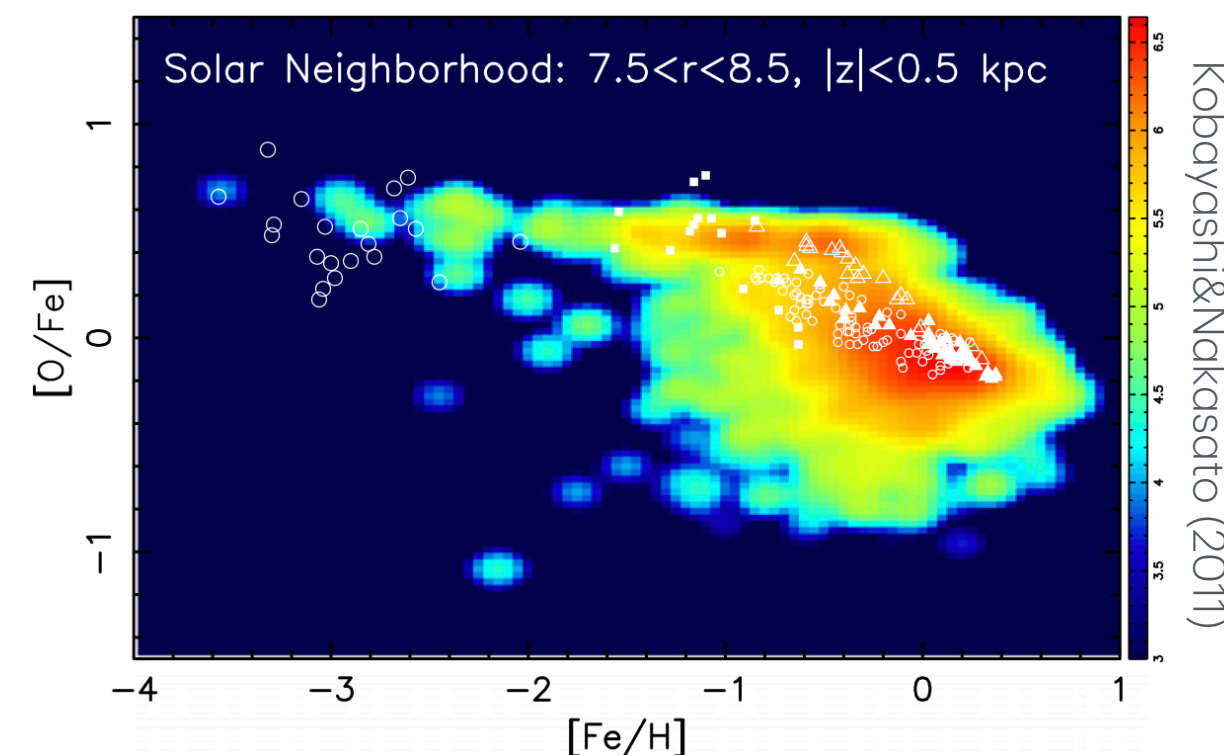
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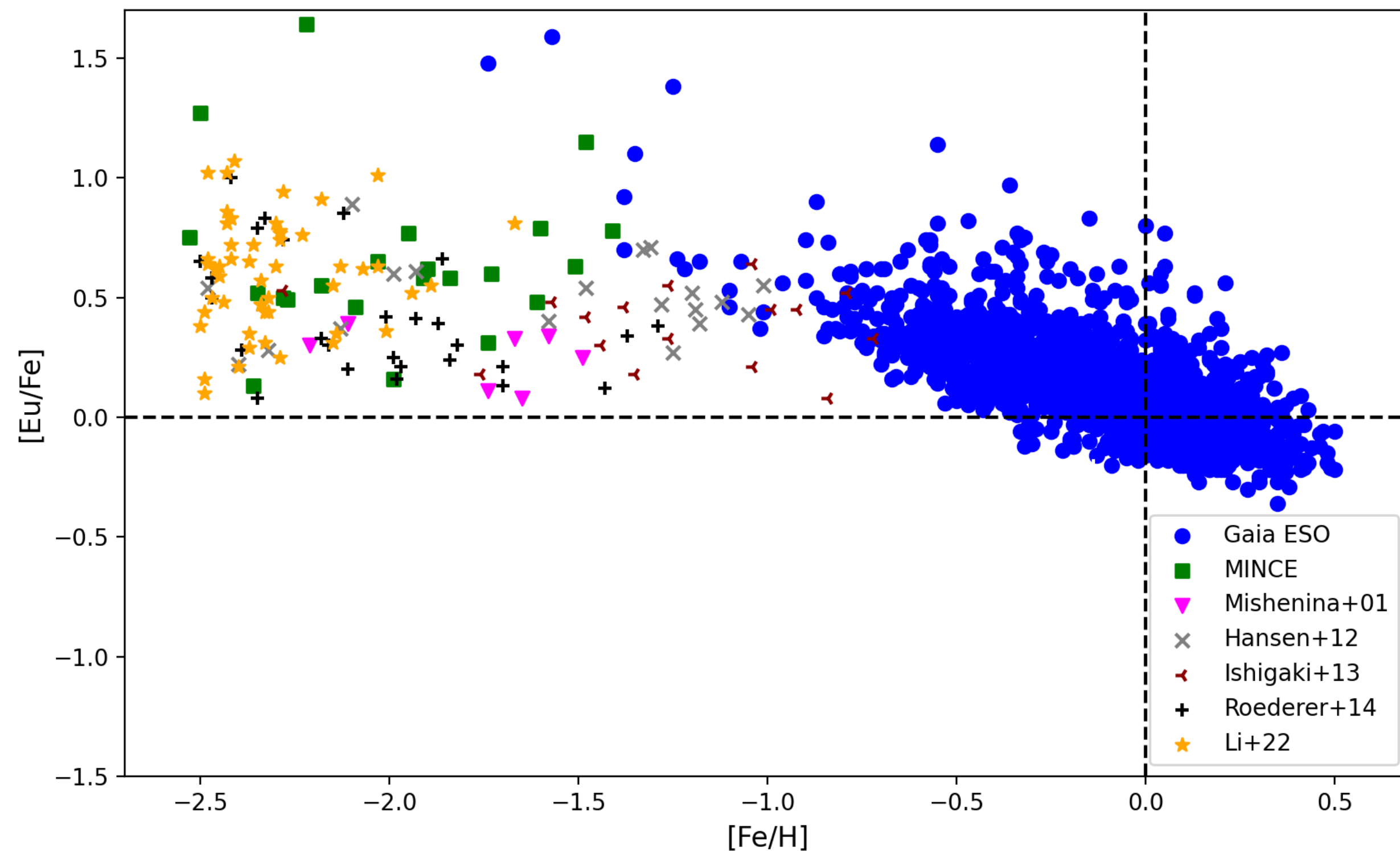
- Integrate chemical evolution + dynamical processes in a cosmological framework



Kobayashi 2004; Scannapieco+22

The [Eu/Fe] vs. [Fe/H]

$$[\text{Eu}/\text{Fe}] = \log(\text{Eu}/\text{Fe}) - \log(\text{Eu}/\text{Fe})_{\odot}$$



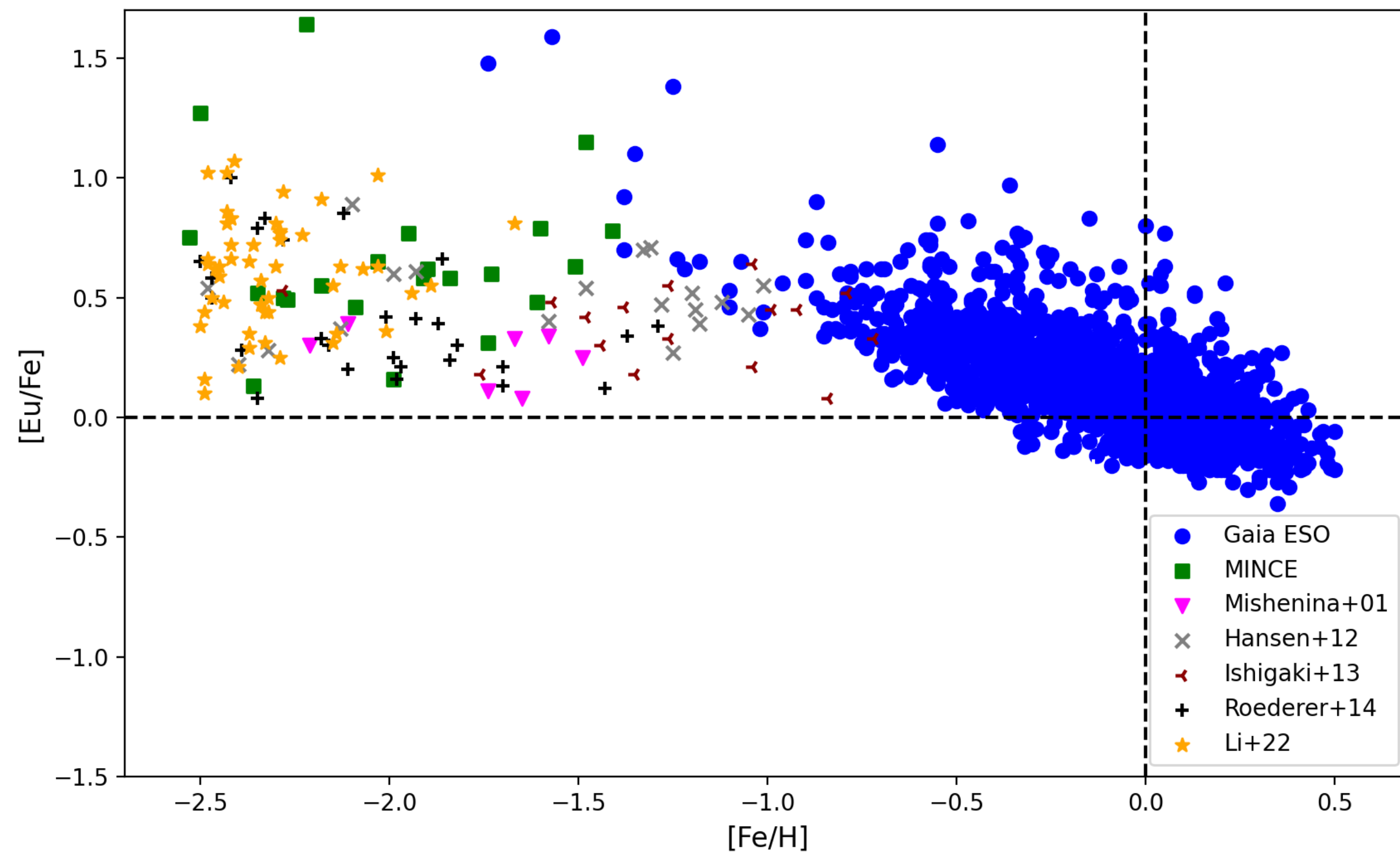
the observed metal abundances of stars today measures the composition of the ISM when the star was formed

Stars are the *fossil records* of past events:

Galactic Archeology

The [Eu/Fe] vs. [Fe/H]

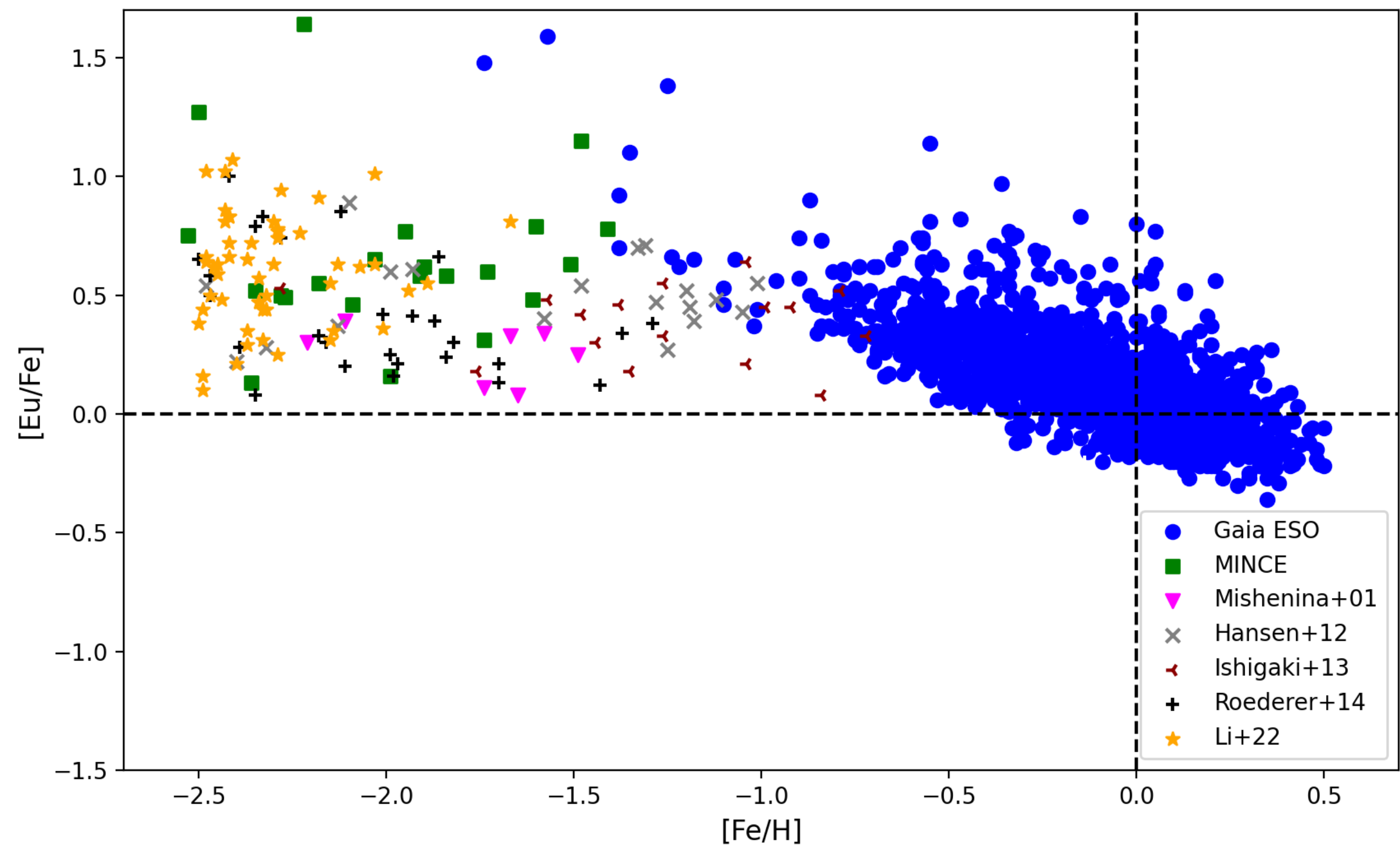
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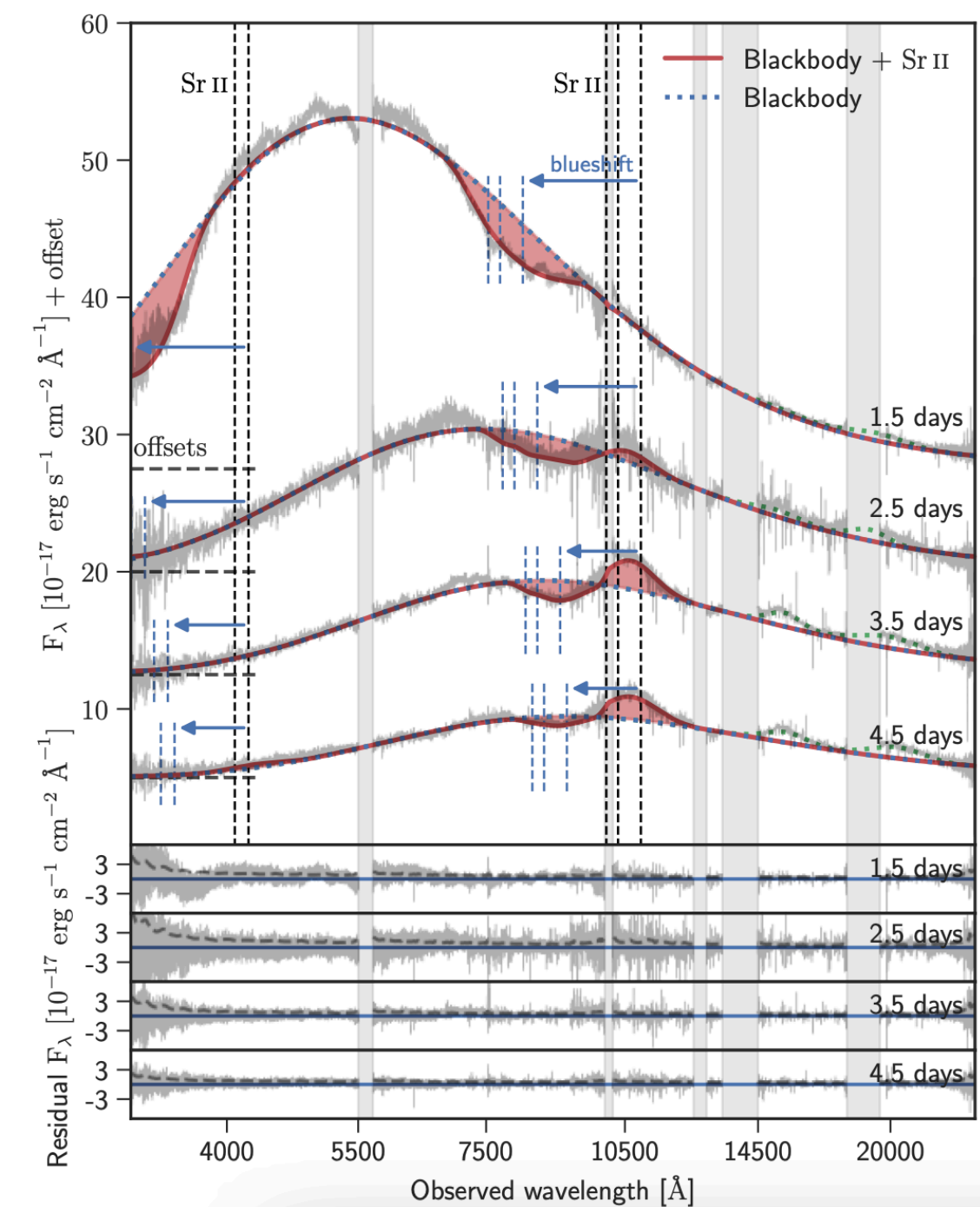
Type Ia SNe
long lifetimes main Fe producers

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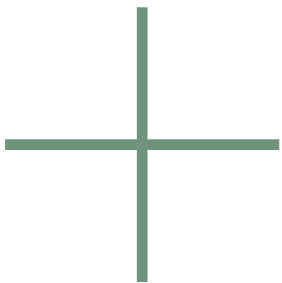


$$Y_{\text{Sr}} \propto 10^{-5} M_{\odot}$$
$$Y_{\text{Eu}} \propto 10^{-6} M_{\odot}$$



Watson et al. (2019)

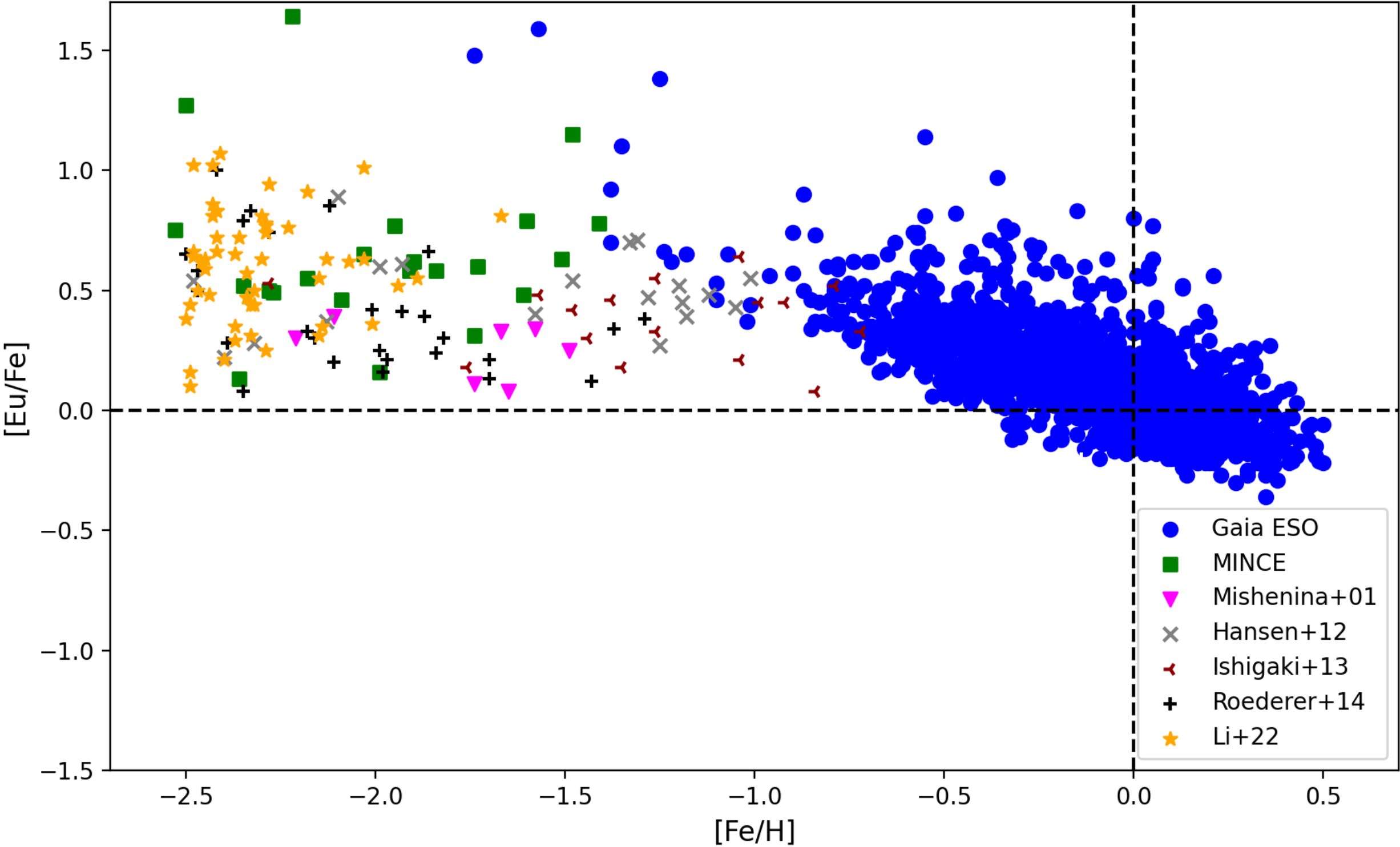
Type Ia SNe
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Neutron star mergers

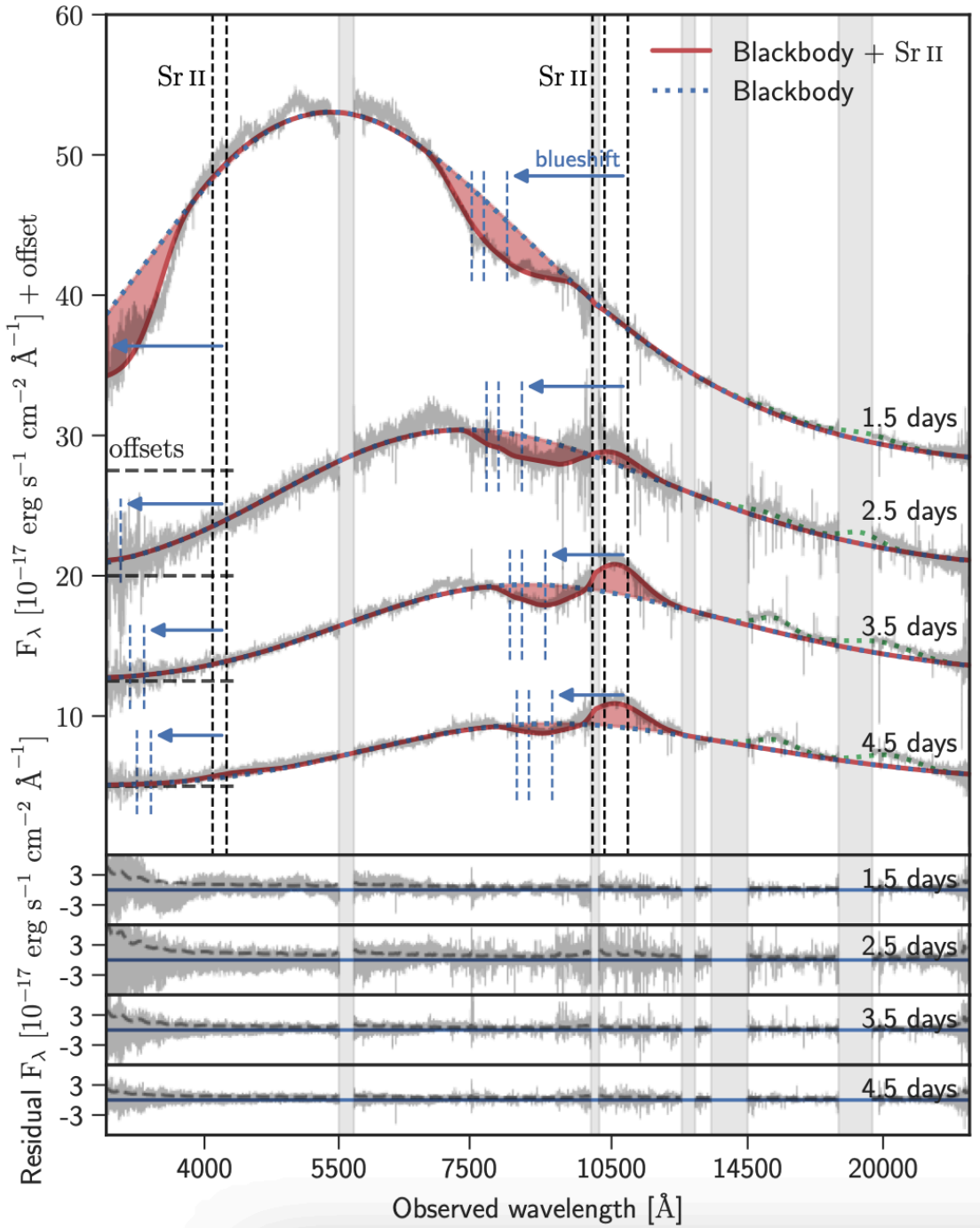
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$$Y_{\text{Sr}} \propto 10^{-5} M_{\odot}$$

$$Y_{\text{Eu}} \propto 10^{-6} M_{\odot}$$



Watson et al. (2019)

lifetime of secondary component

$$\text{Delay time for MNS: } \tau = \tau_s + \tau_{gw}$$

gravitational radiation delay

$$\tau_{gw} = \tau_{gw}(m_1, m_2, A, e)$$

The rate of neutron star mergers

Fong et al. (2017)
 Chruslinska et al. (2018)
 Cotè et al. (2019)
 Greggio et al. (2021)

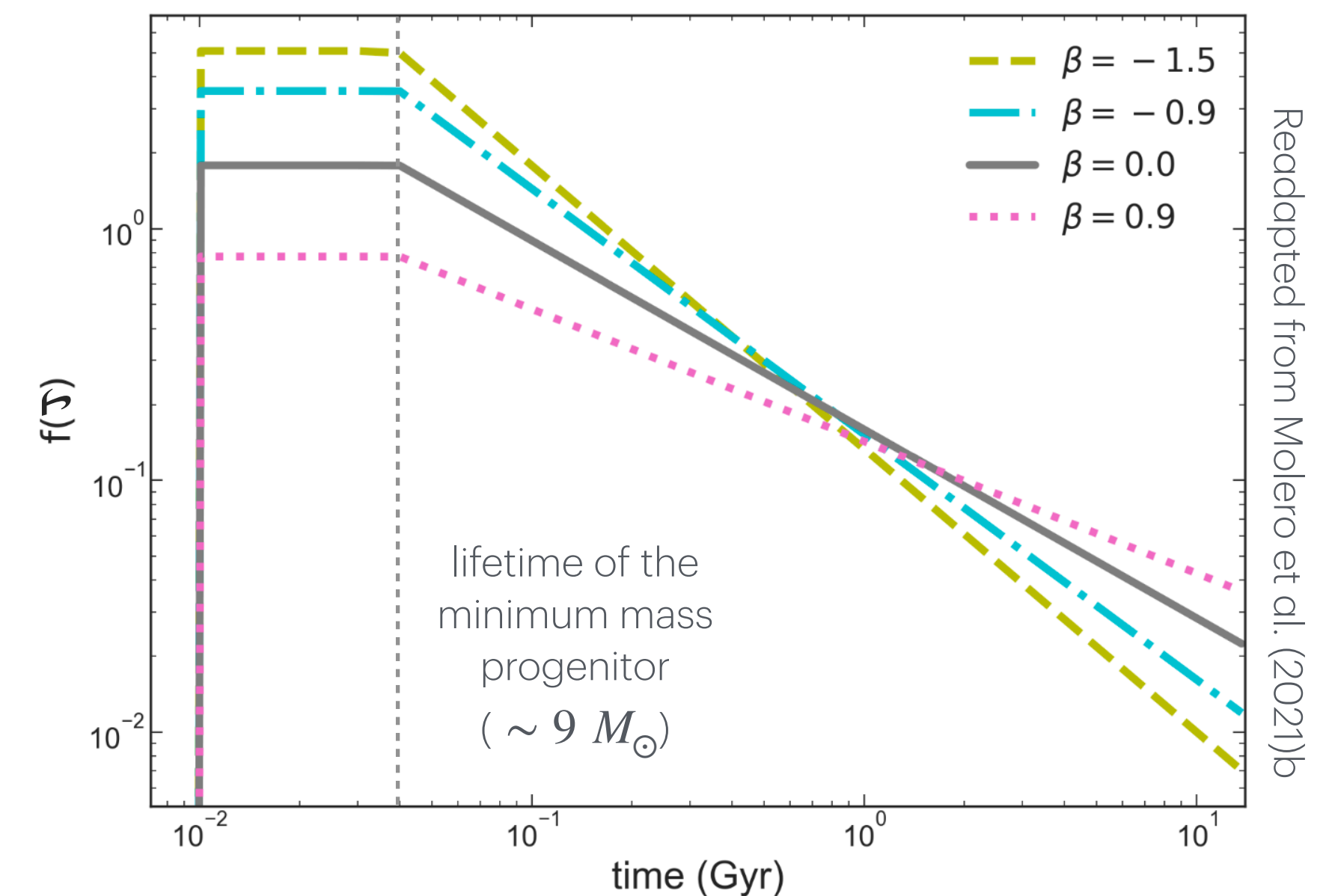
More DTDs

When? + How much? + How many?

$$R_{MNS}(t) = k_{\alpha} \int_{\tau_i}^{\min(t, \tau_x)} \alpha_{MNS}(\tau) \psi(t - \tau) f_{MNS}(\tau) d\tau$$

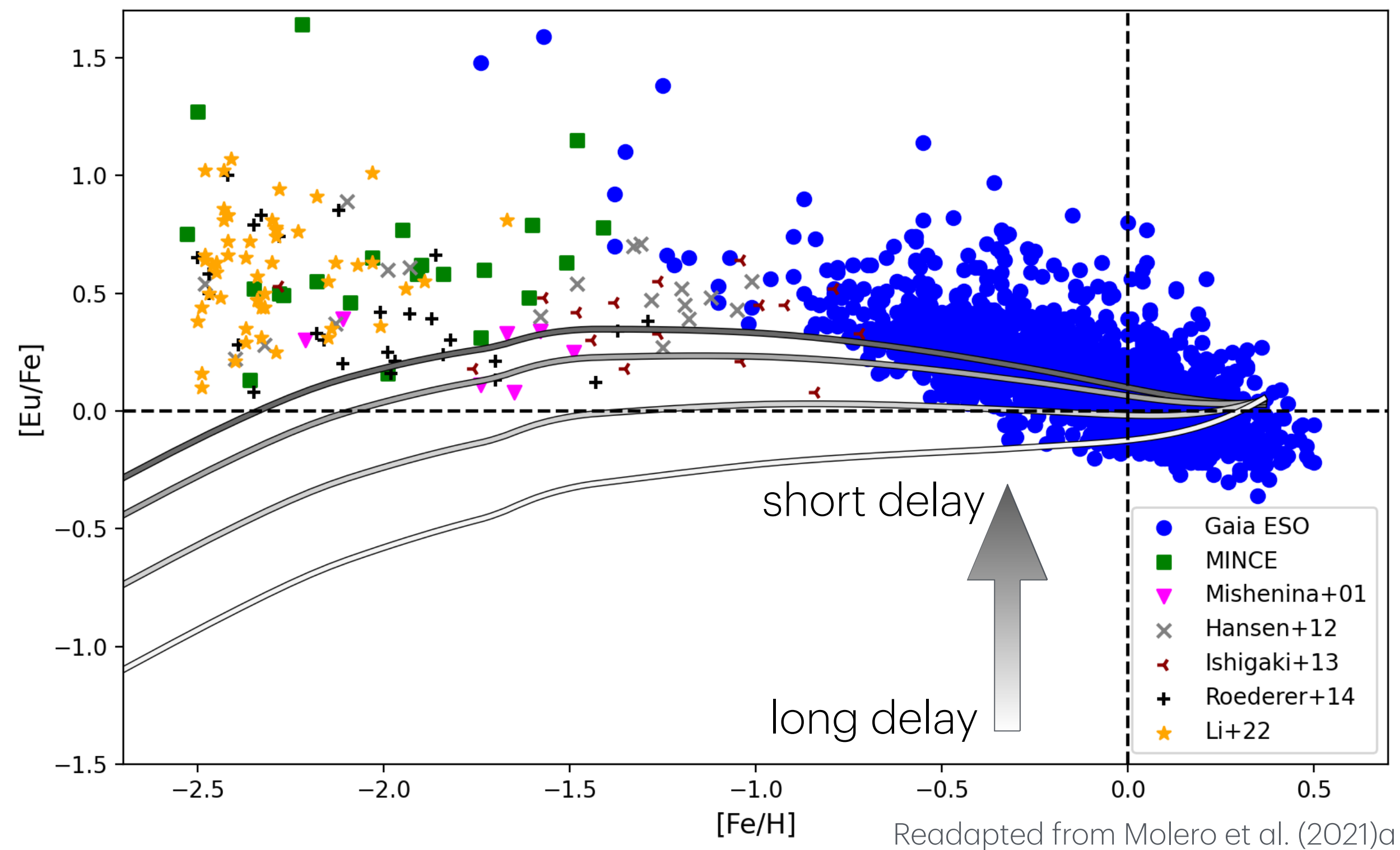
Initial Mass Function
Star Formation
Delay Time Distribution

Simonetti et al. (2019)



The [Eu/Fe] vs. [Fe/H]

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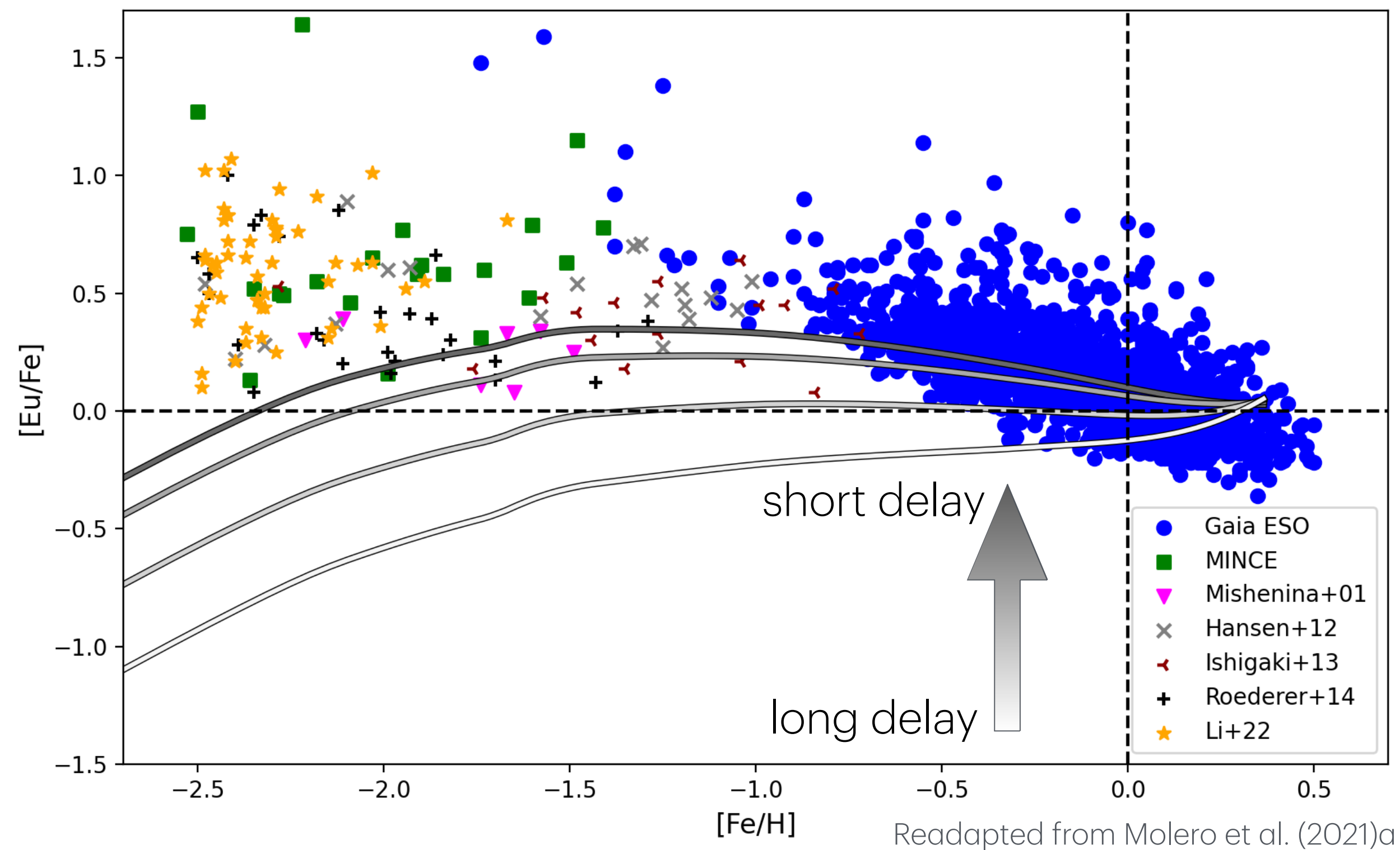


Either NS all merge on short timescales or they cannot be the major producers of Eu

Argast+04, Matteucci+14, Cescutti+15, Wehmeyer+15, Cotè+19, Simonetti+19, Kobayashi+20, Cavallo+21, Molero+21a,b, Van der Swaelmen+23, ...

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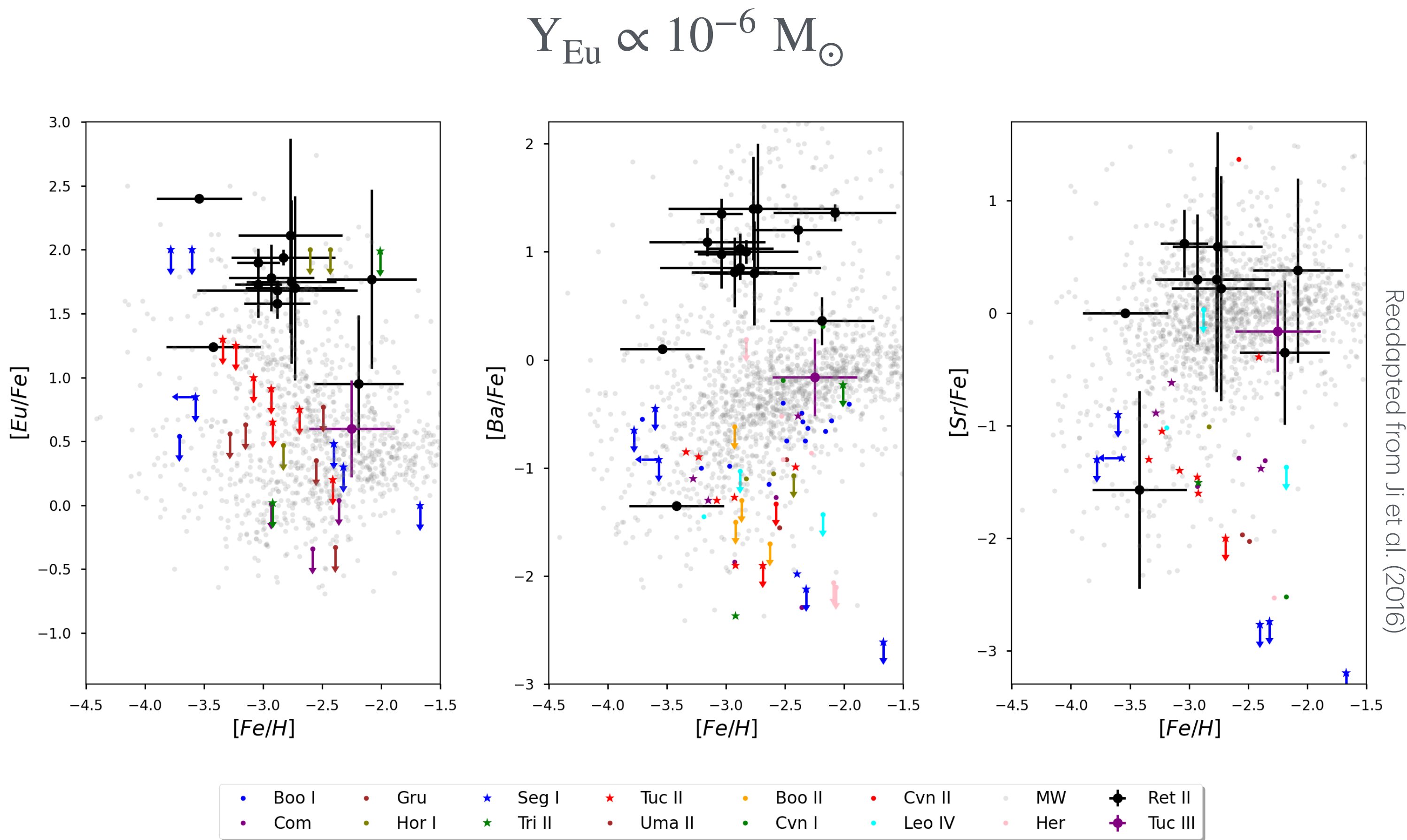
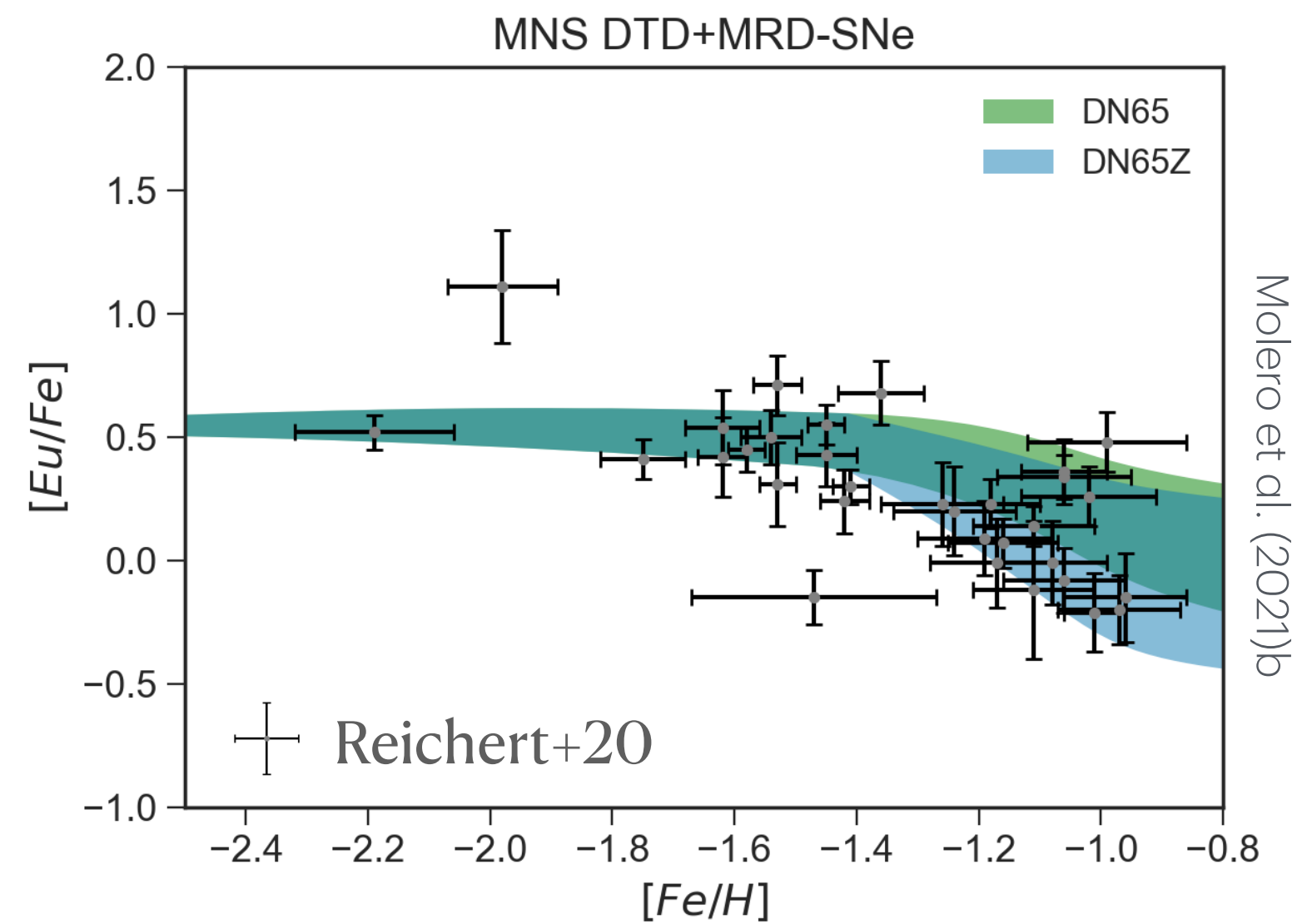
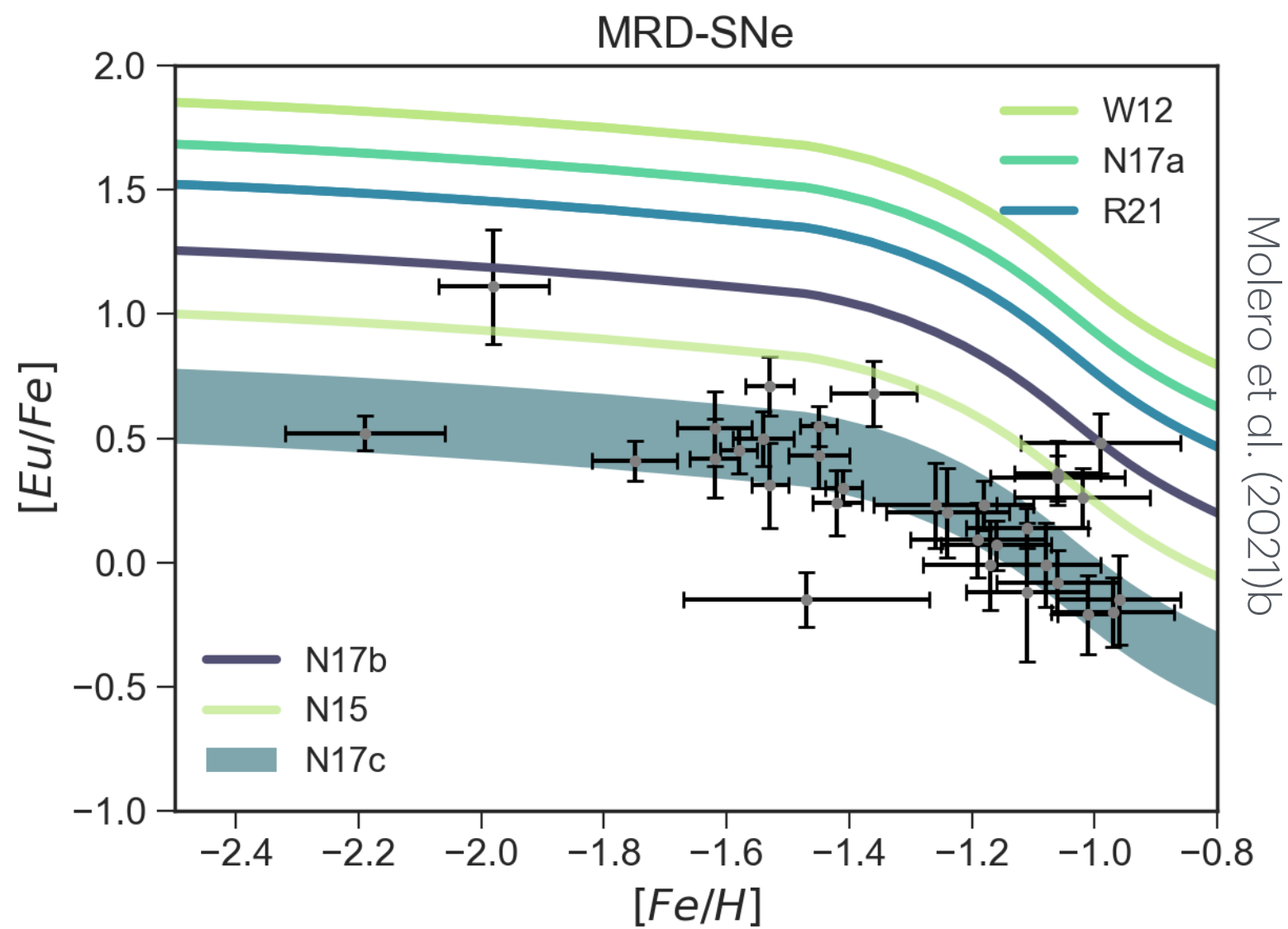


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Massive stars... MR-SNe, collapsars... something quick

The [Eu/Fe] vs. [Fe/H] - Local Group galaxies



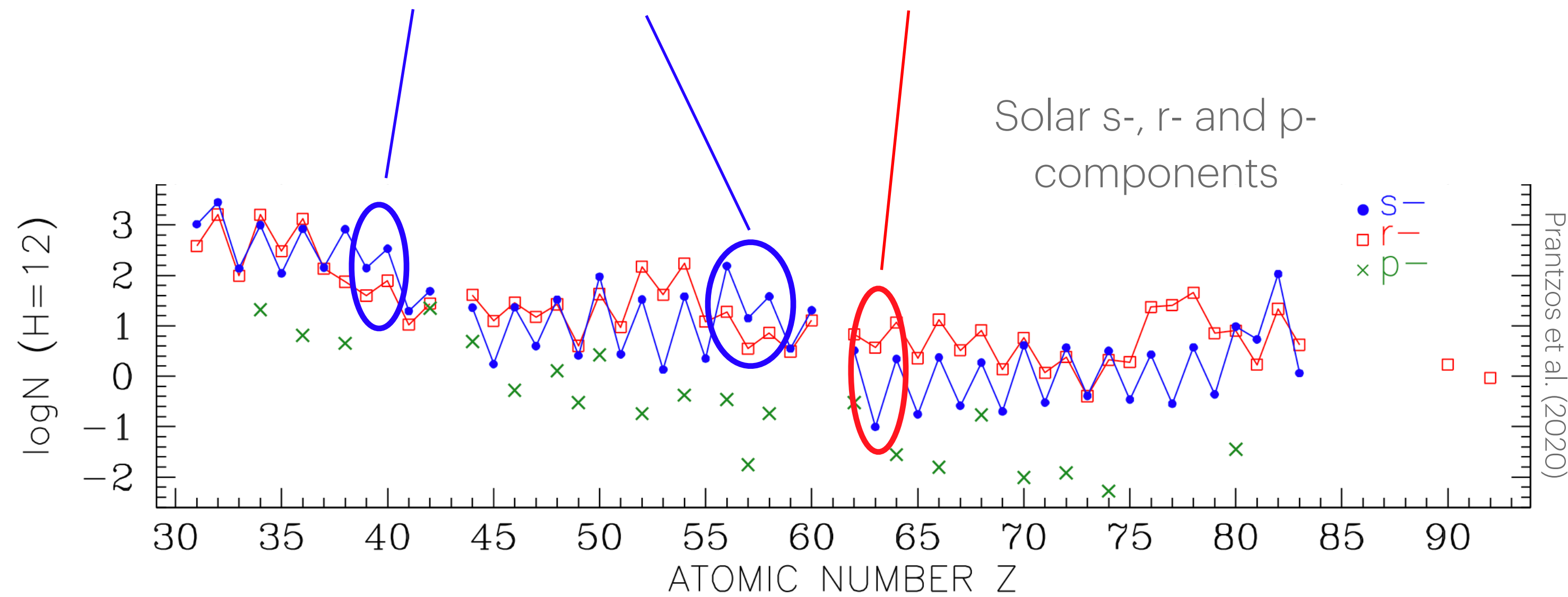
Cescutti&Chiappini (2014)
for MR-SNe in GCE

For more dwarf galaxies model of nc-elements: Lanfranchi et al. (2008)
Hirai et al. (2015)
Vincenzo et al. (2015)
Palla, Molero, et al. (2025)

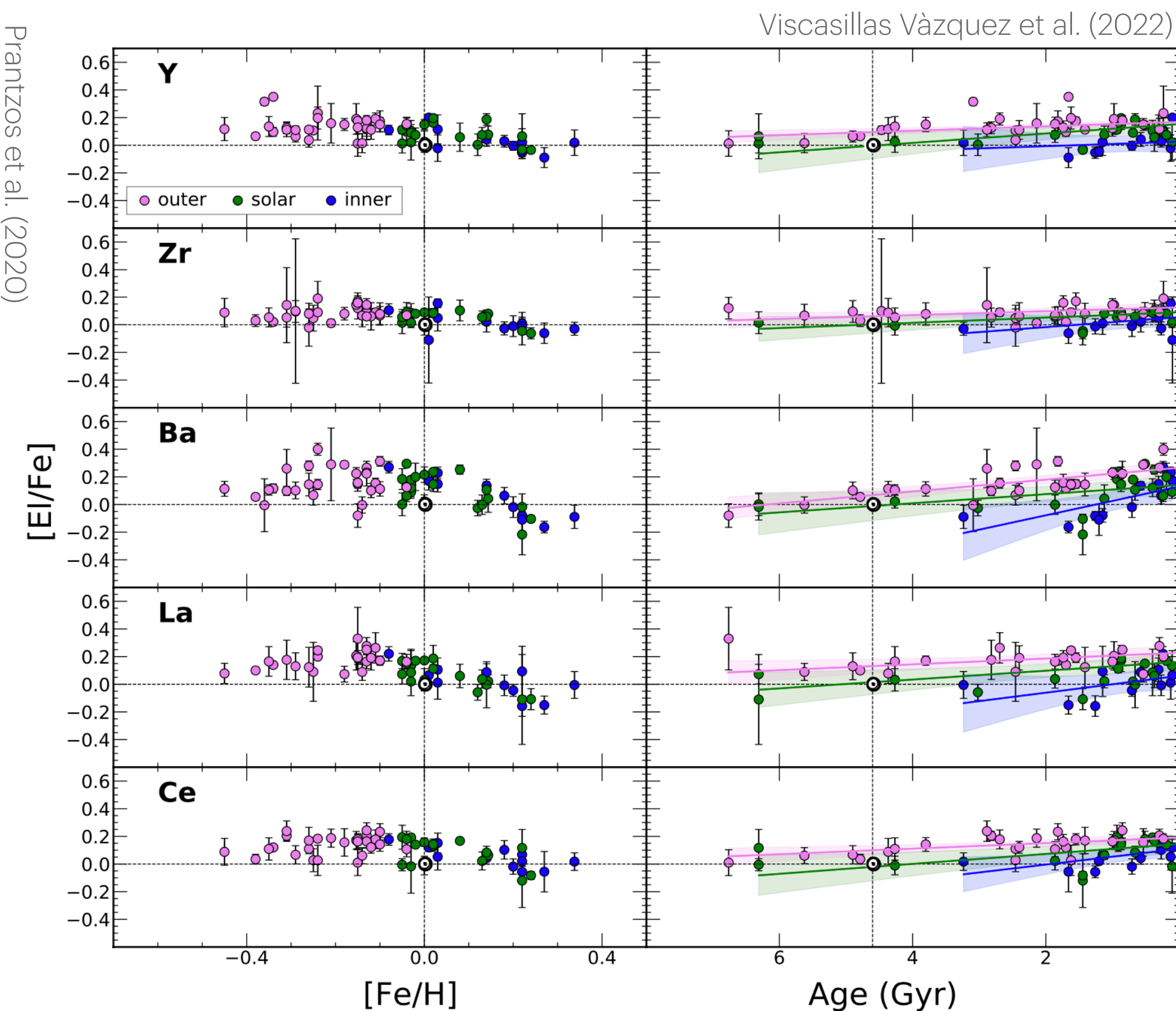
see also Skúladóttir & Salvadori (2020)

Homogeneous model for the disk

- NC elements: Y, Zr, Mo, Ba, La, Ce, Pr, Nd, Eu



- Gaia-ESO survey data from the 6th data release:
 1. field stars (3975)
 2. Open clusters (OCs, 62)



Abundance patterns

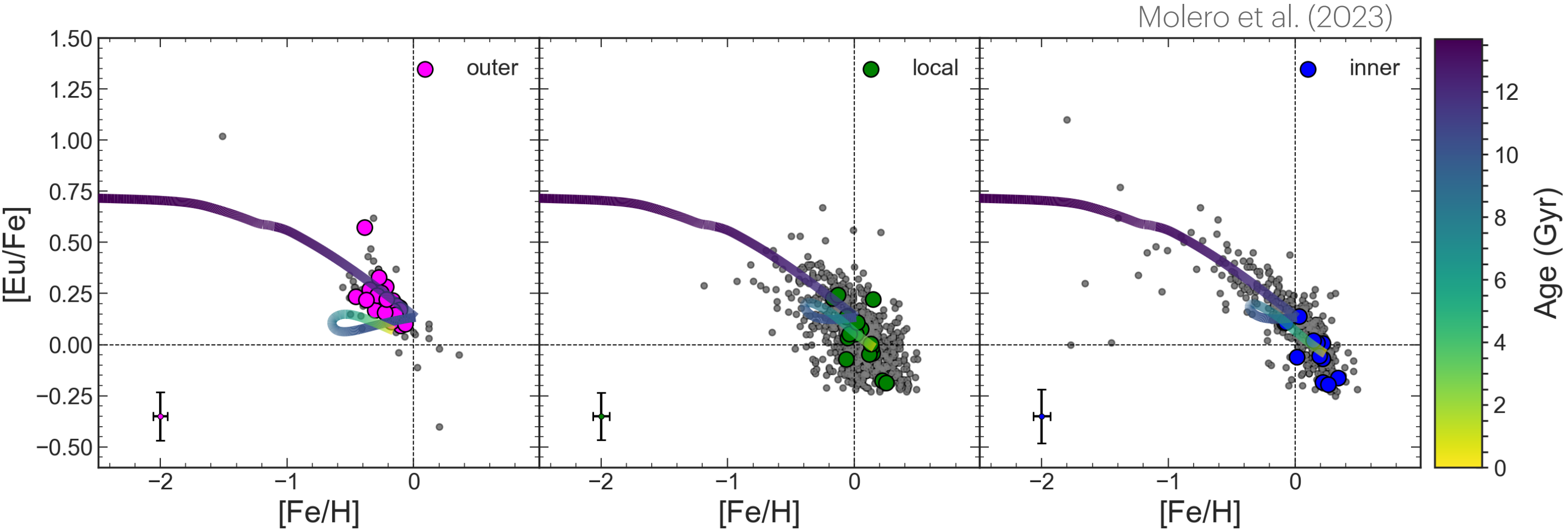
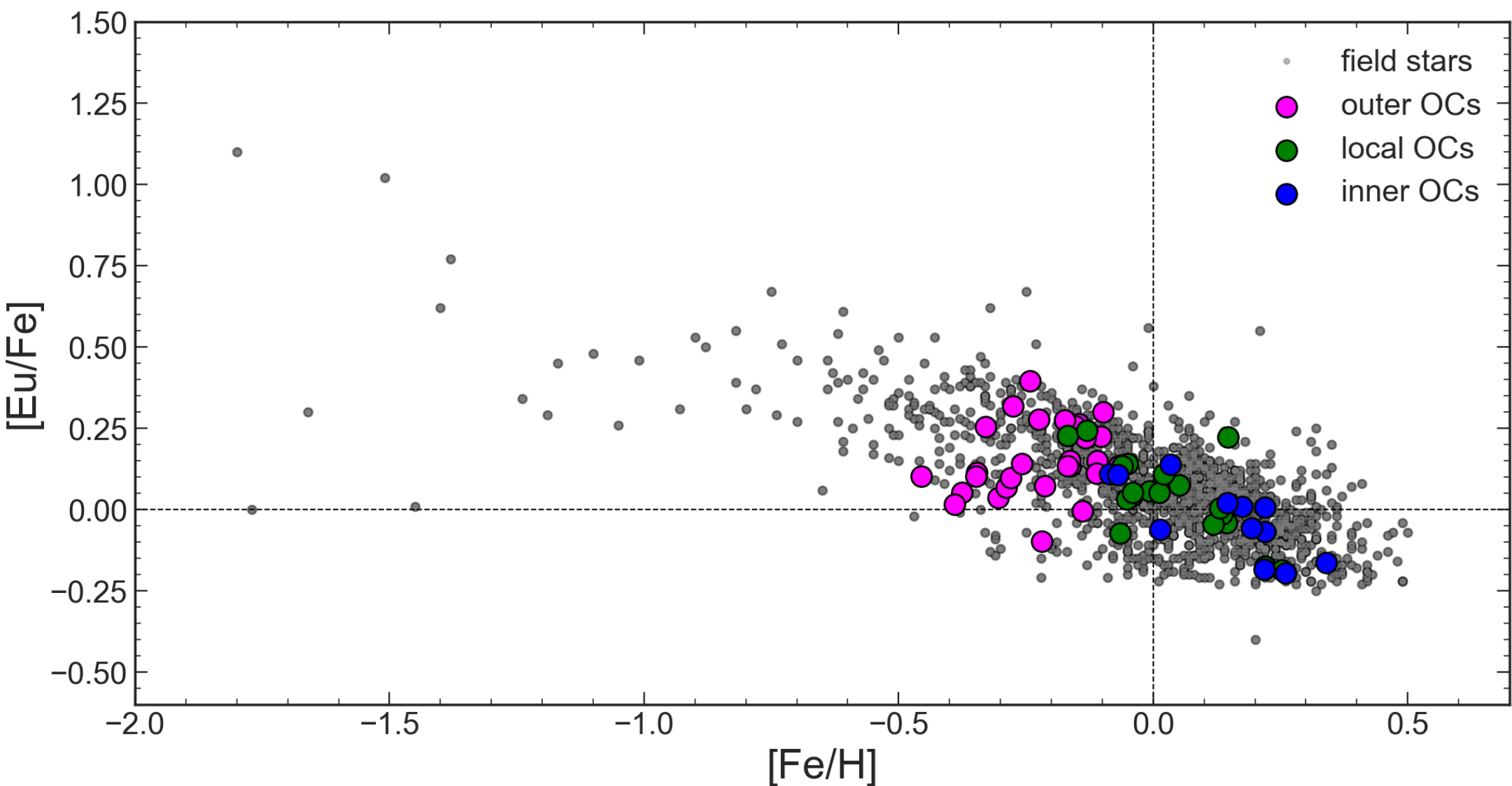
R-process

QUICK

- MR-SNe : i) with yield from Nishimura et al. (2017)
ii) low fraction of normal CC-SNe

DELAYED

- NSM : i) yield $Y_{\text{Eu}} \propto 10^{-6} M_{\odot}$
ii) rate from LIGO/Virgo



Abundance patterns

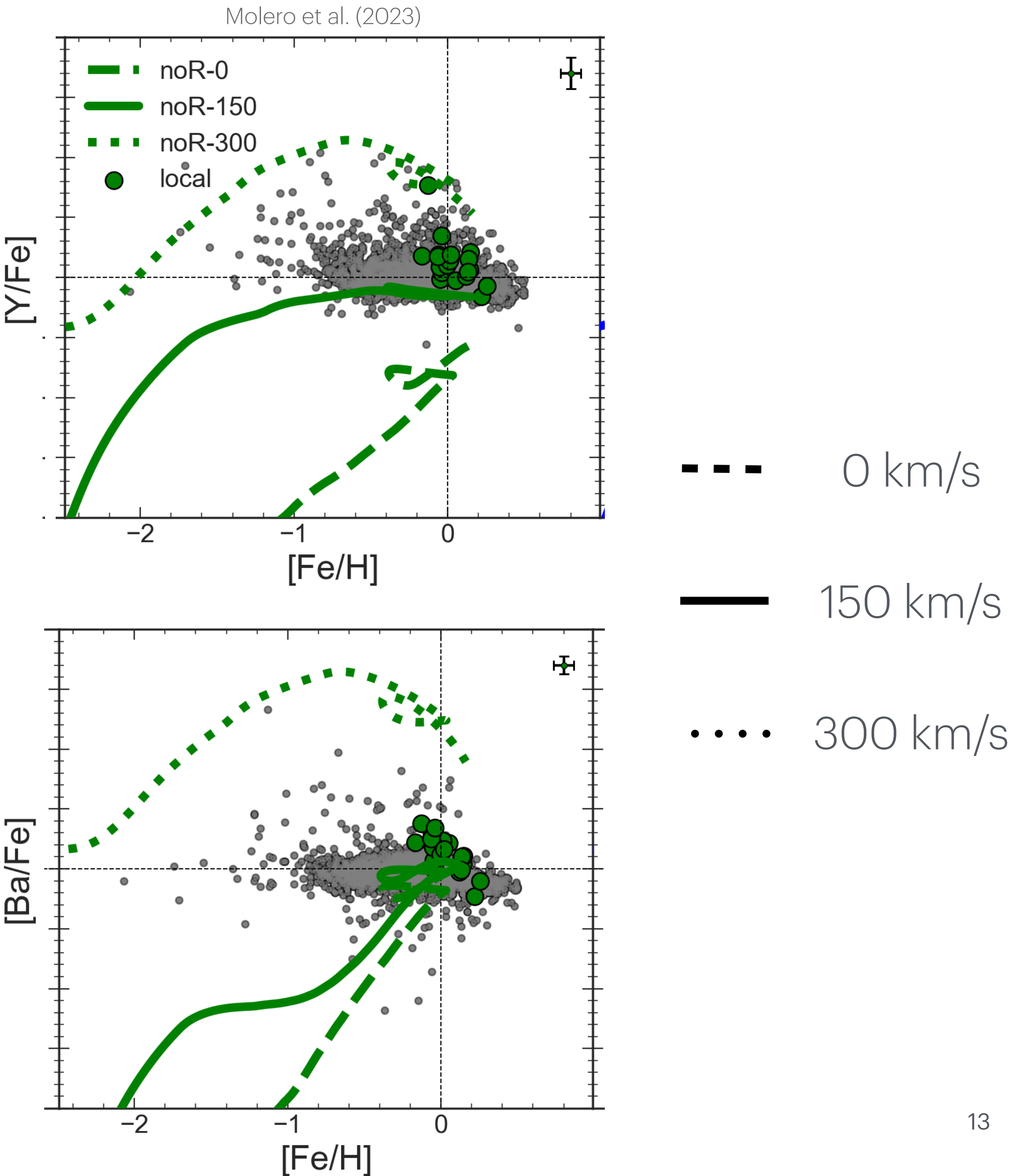
S-process

QUICK

- Rotating massive stars : i) 36 progenitors (x3) yield grid (Limongi&Chieffi 2018)
ii) rate fine-tuned with observations

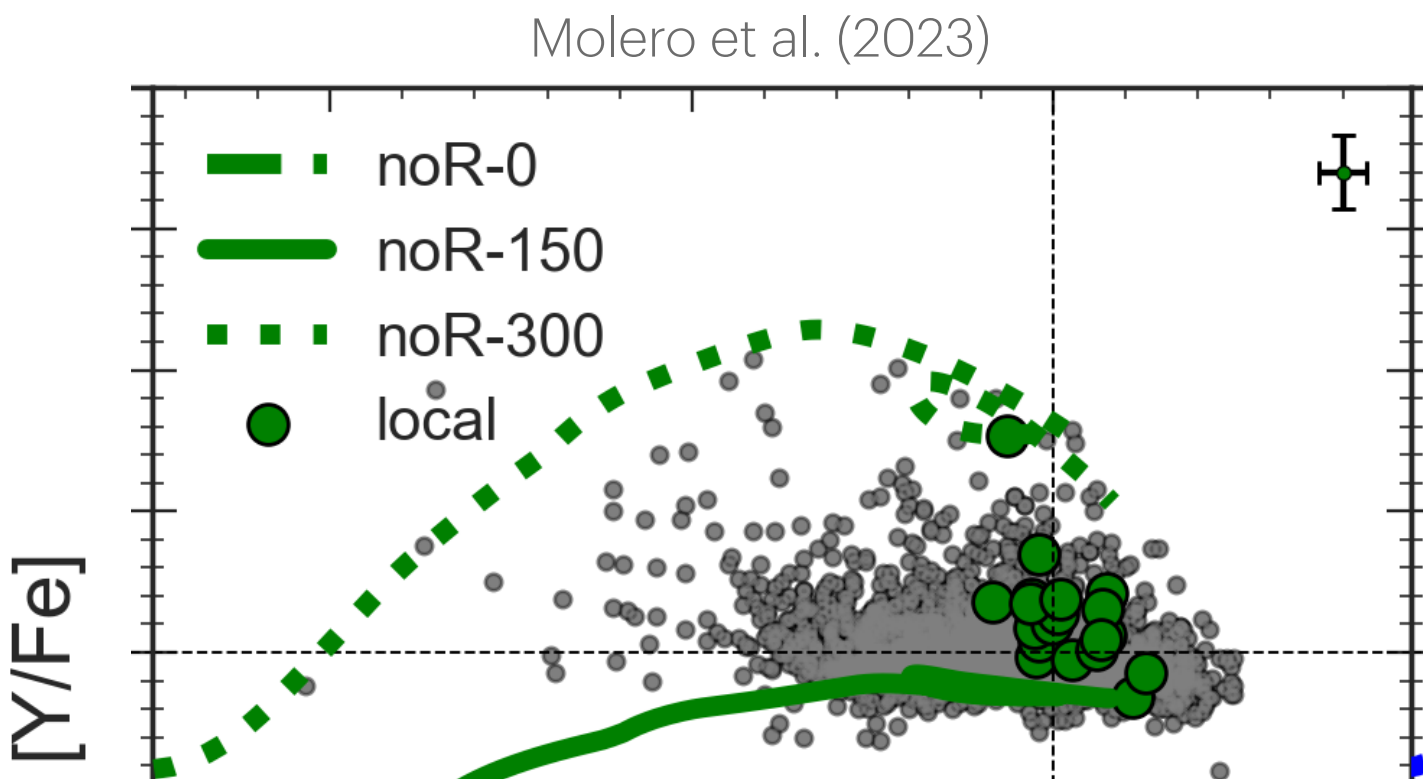
DELAYED

- AGB stars : i) large (108 progenitors) yield grid from FRUITY

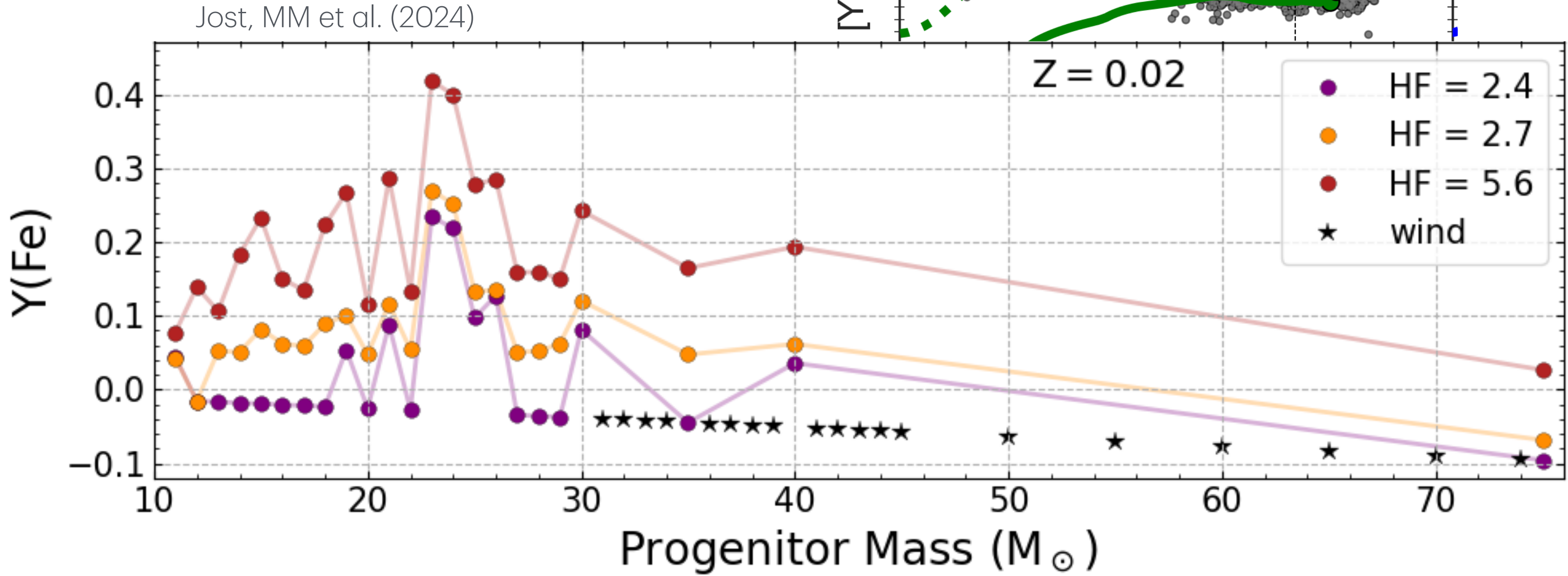
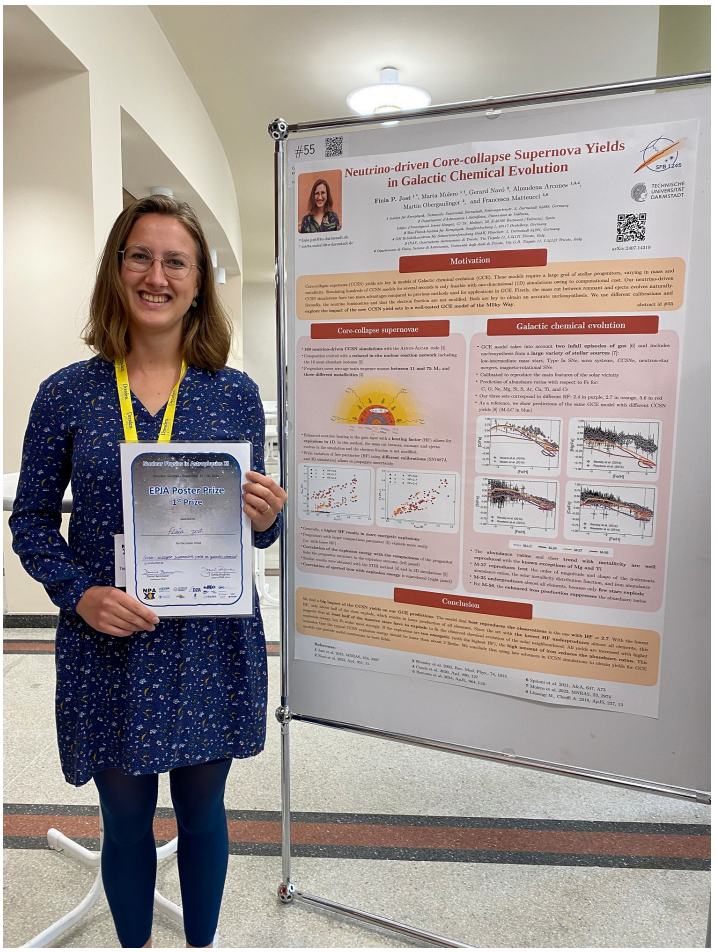


Abundance patterns

S-process



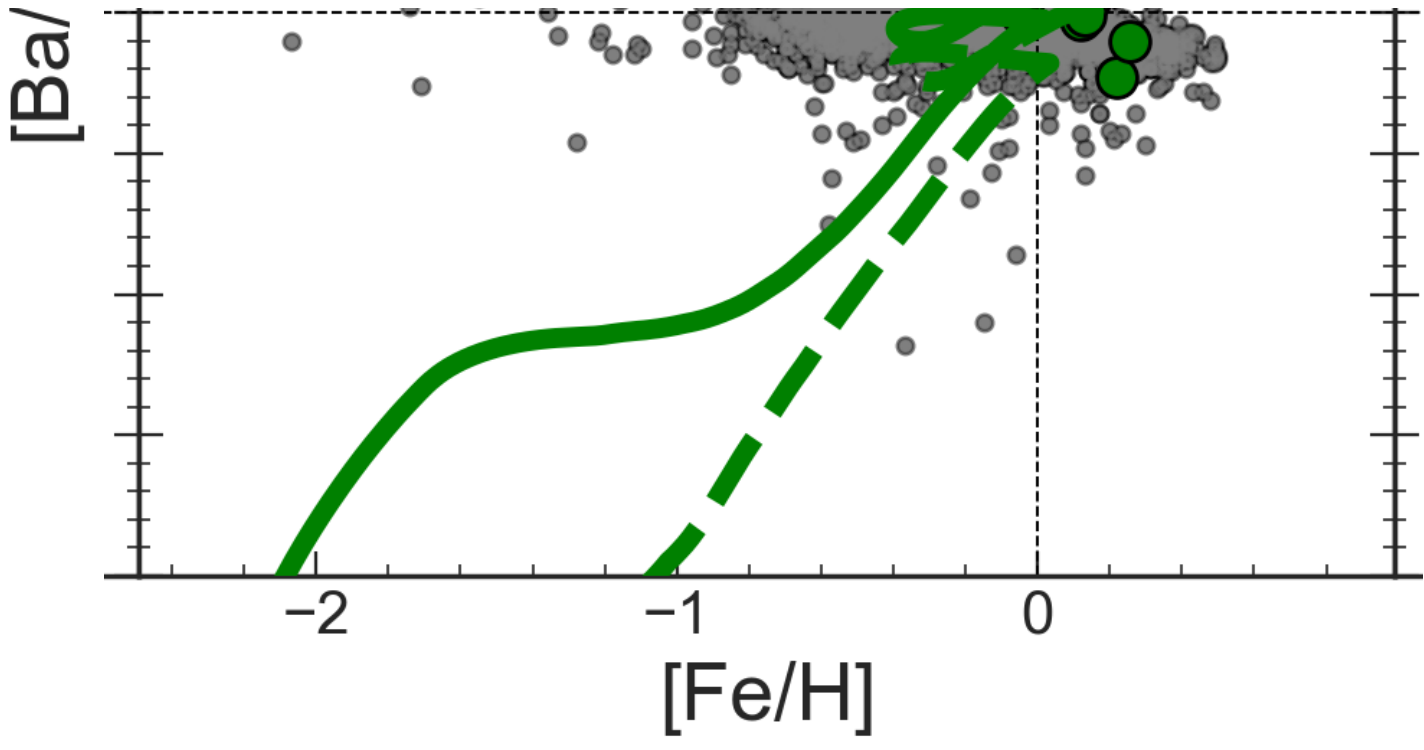
NPA 2024



0 km/s

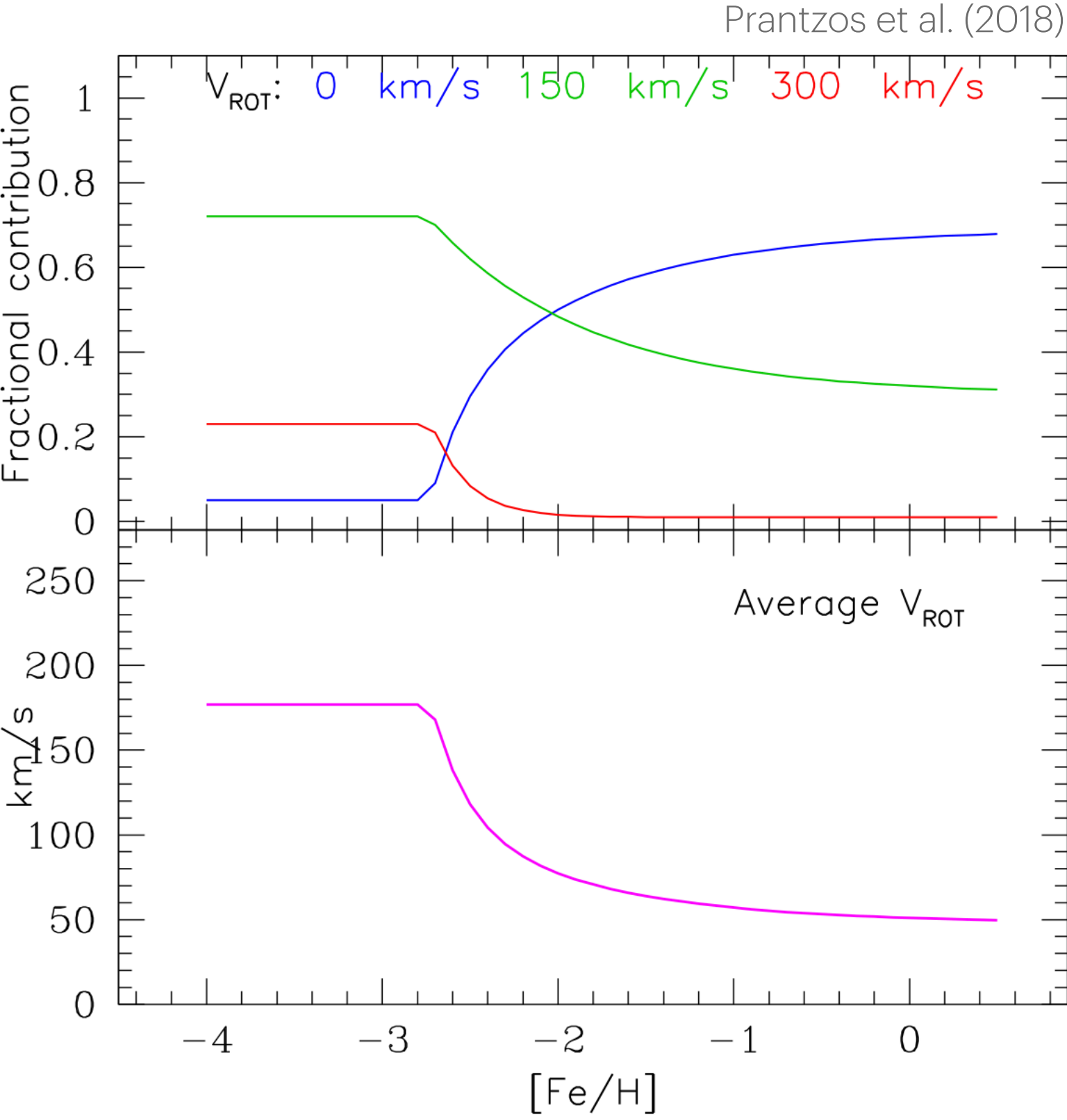
150 km/s

300 km/s



- Rotating massive stars
- AGB stars : i) large

Abundance patterns



s- + r-
s-

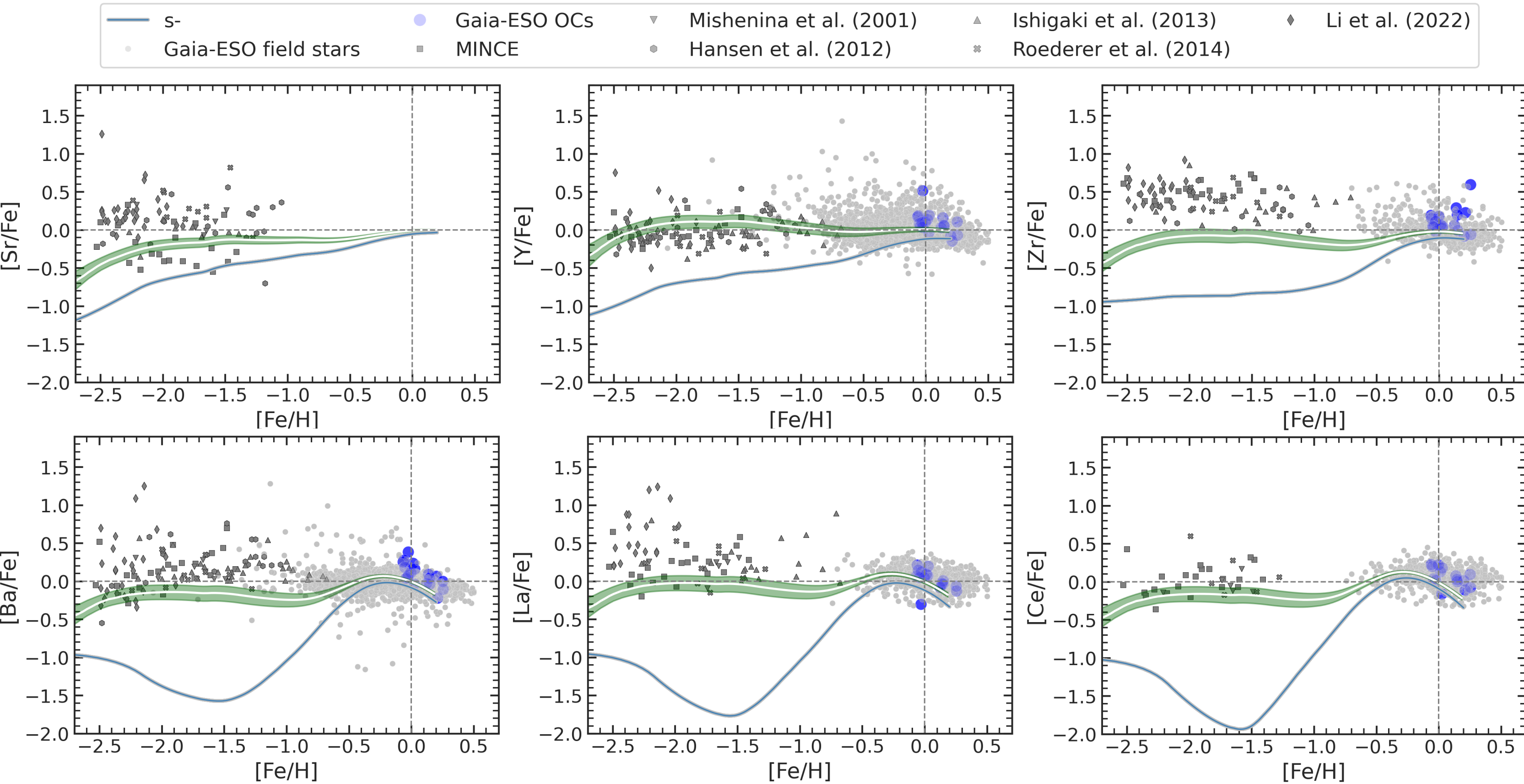
S-process
nucleosynthesis

MDF of the bulge

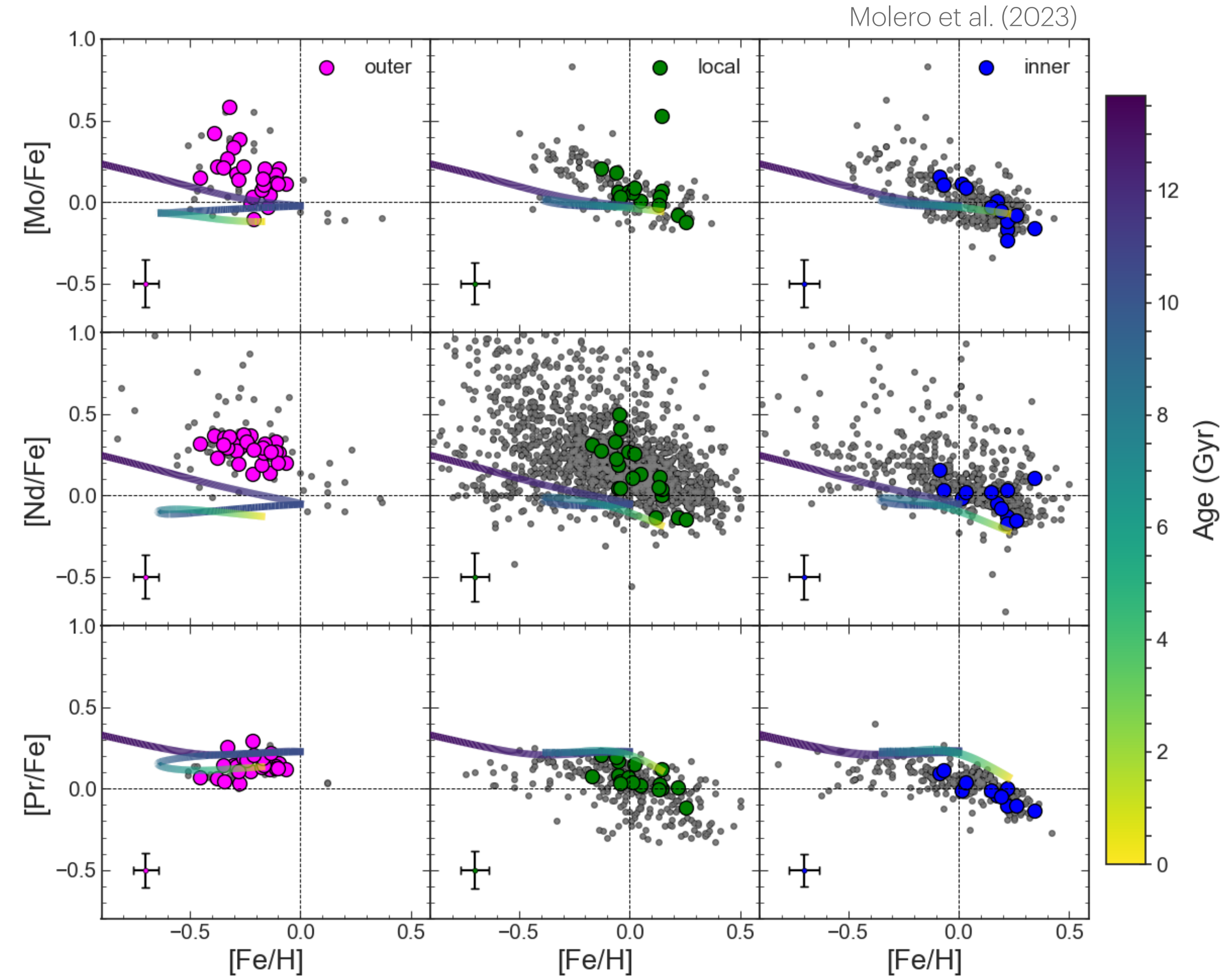
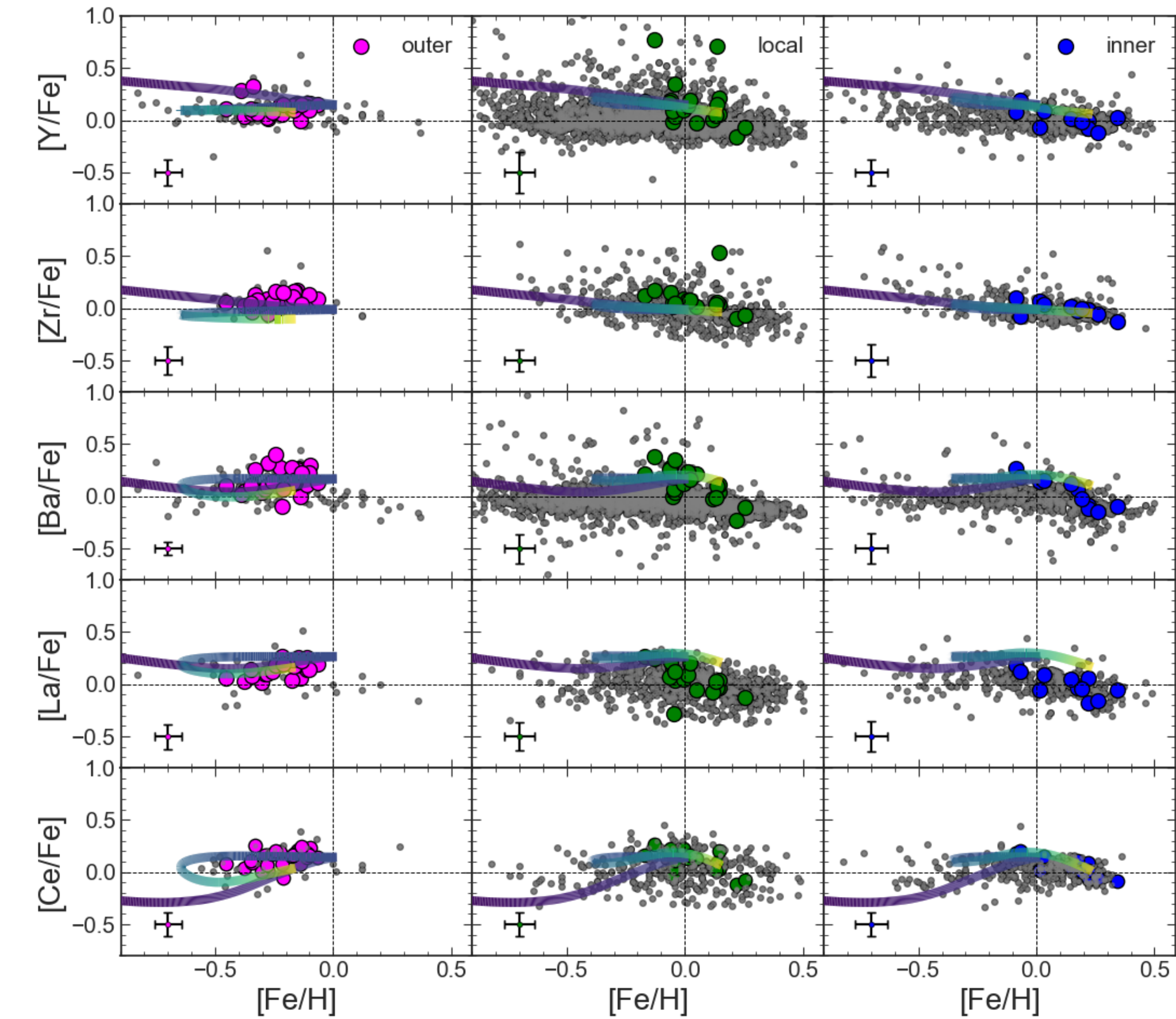
Rizzuti et al. (2021), Romano et al. (2019), Molero et al. (2024,2025)

CNO isotopes

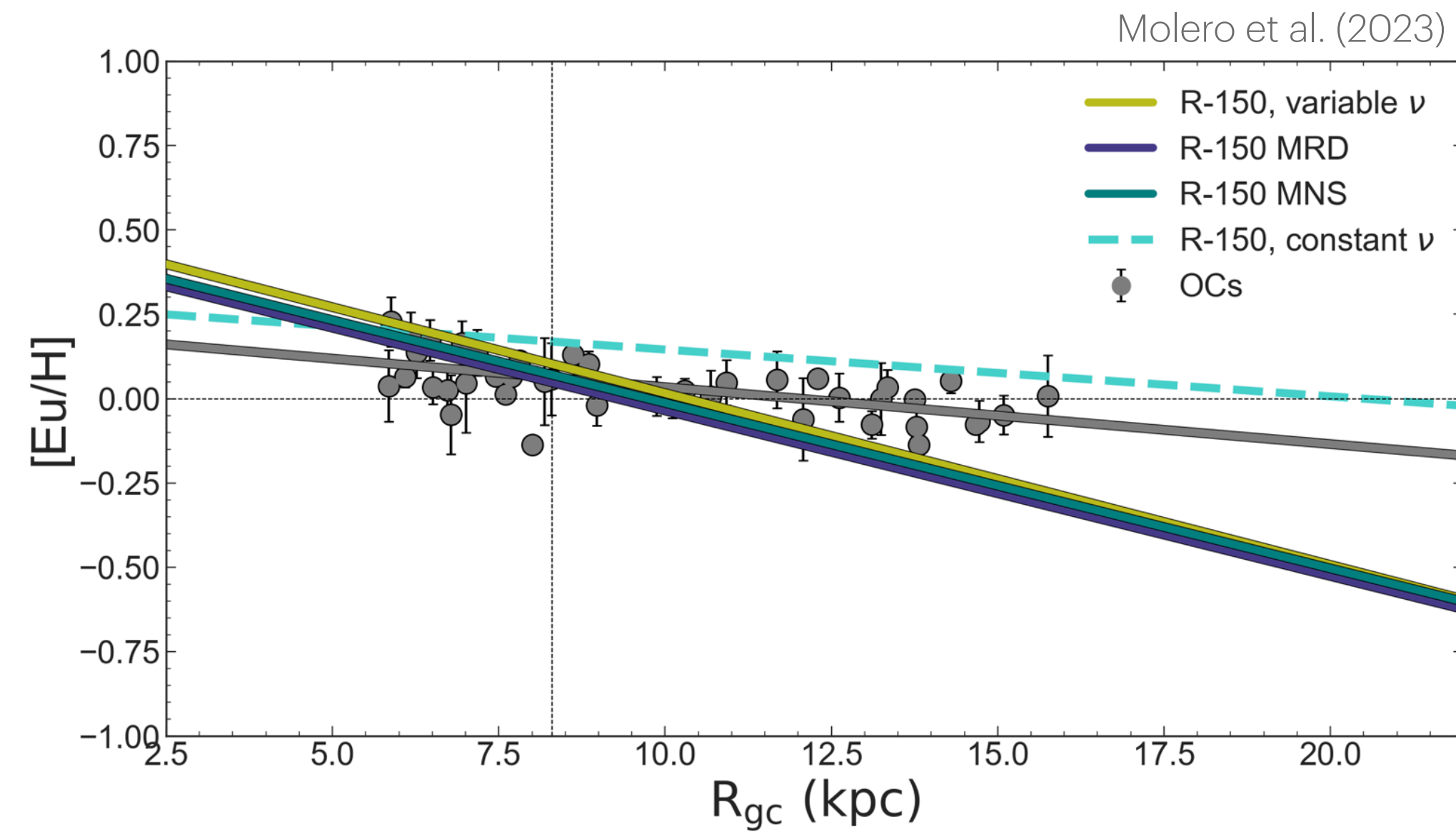
Chemical clocks



Abundance patterns



Abundance gradients

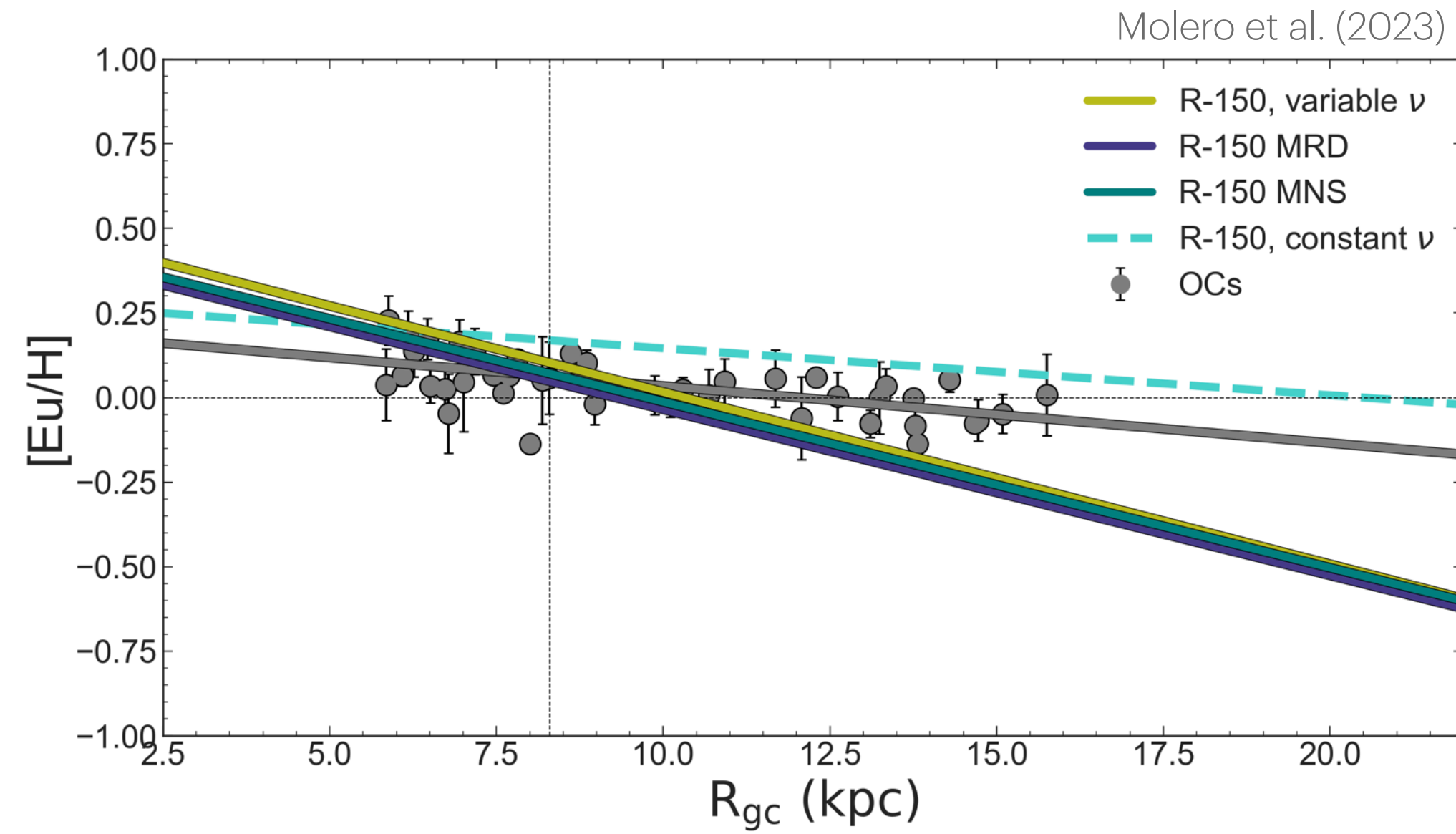


Observed: $[\text{Eu}/\text{H}] = -0.019(\pm 0.003) \times R_{\text{GC}} + 0.245(\pm 0.030)$

Model:

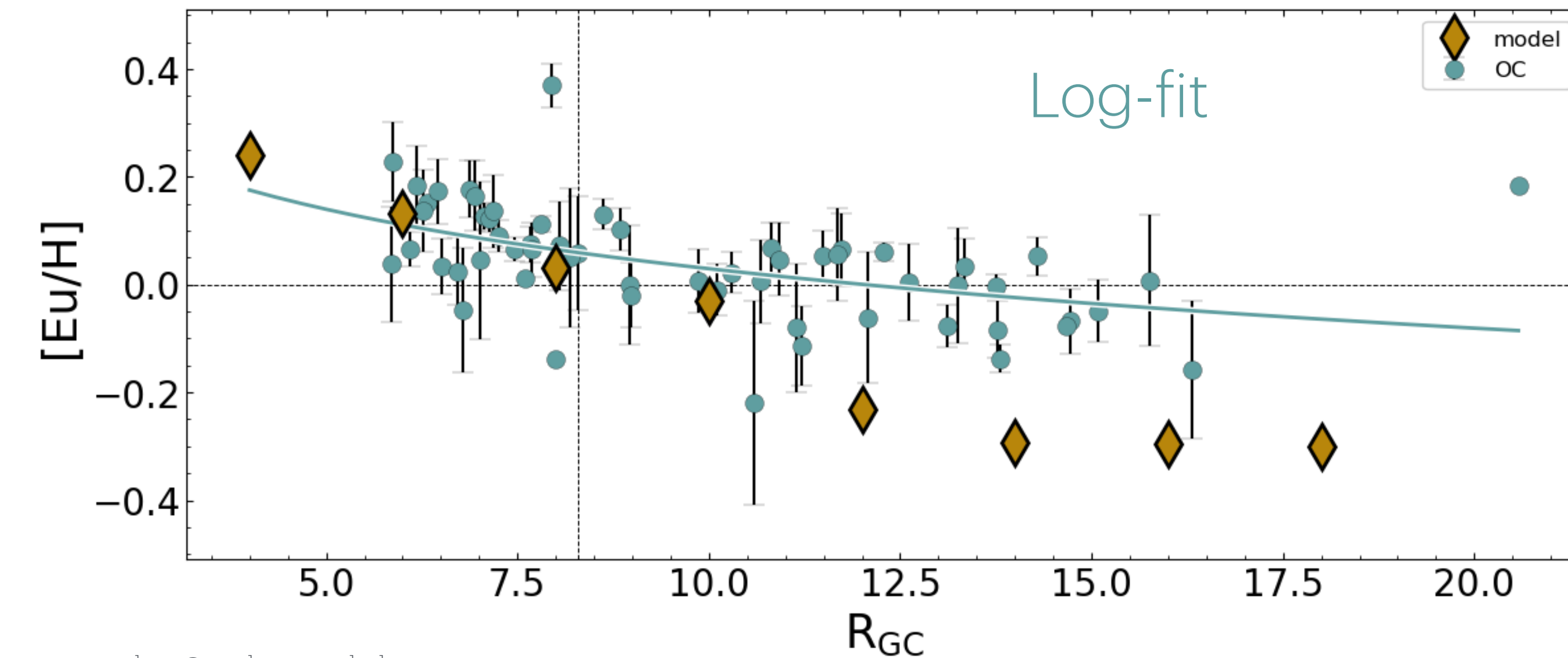
$-0.050(\pm 0.003) \text{ dex kpc}^{-1}$

Abundance gradients

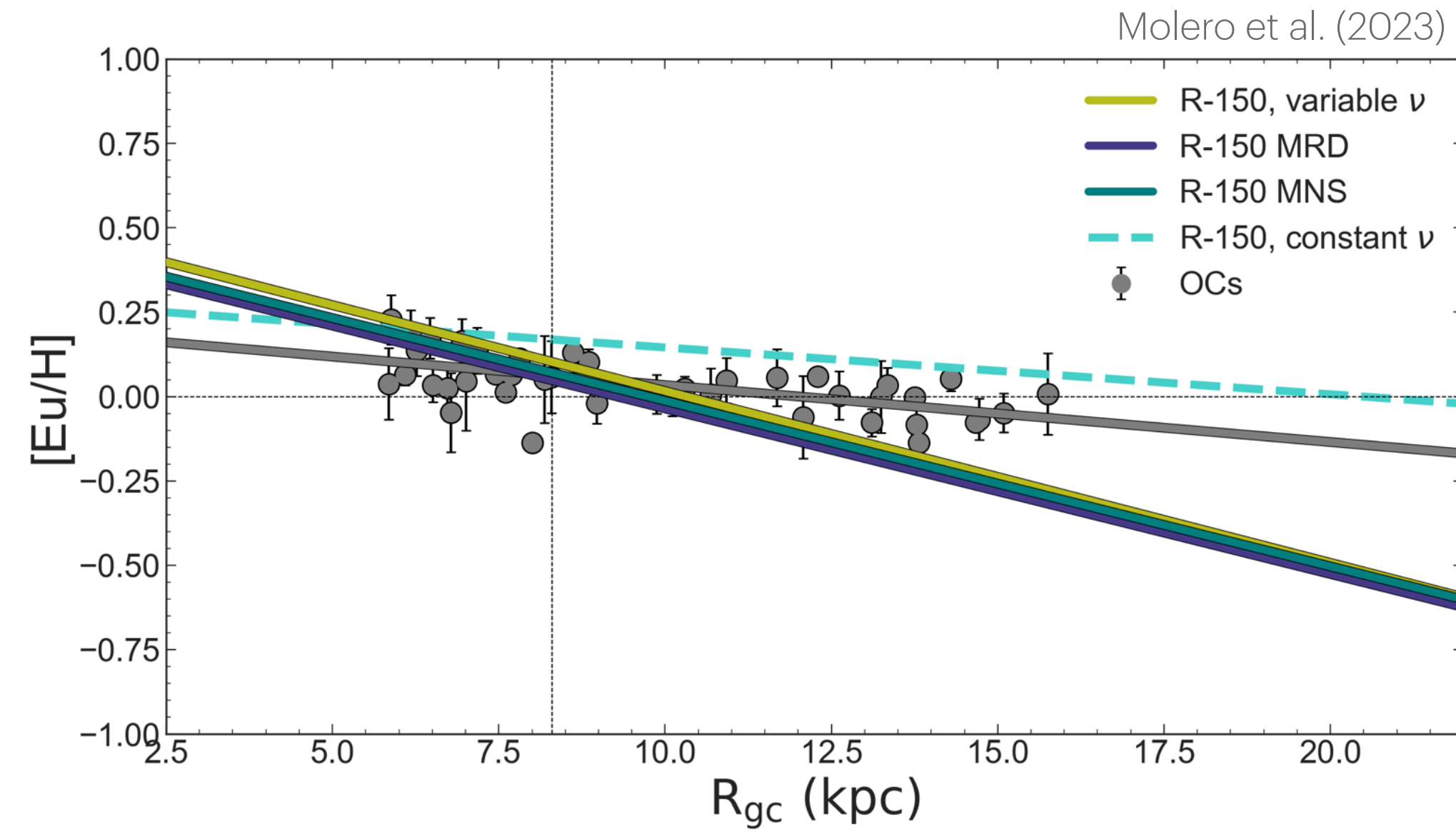


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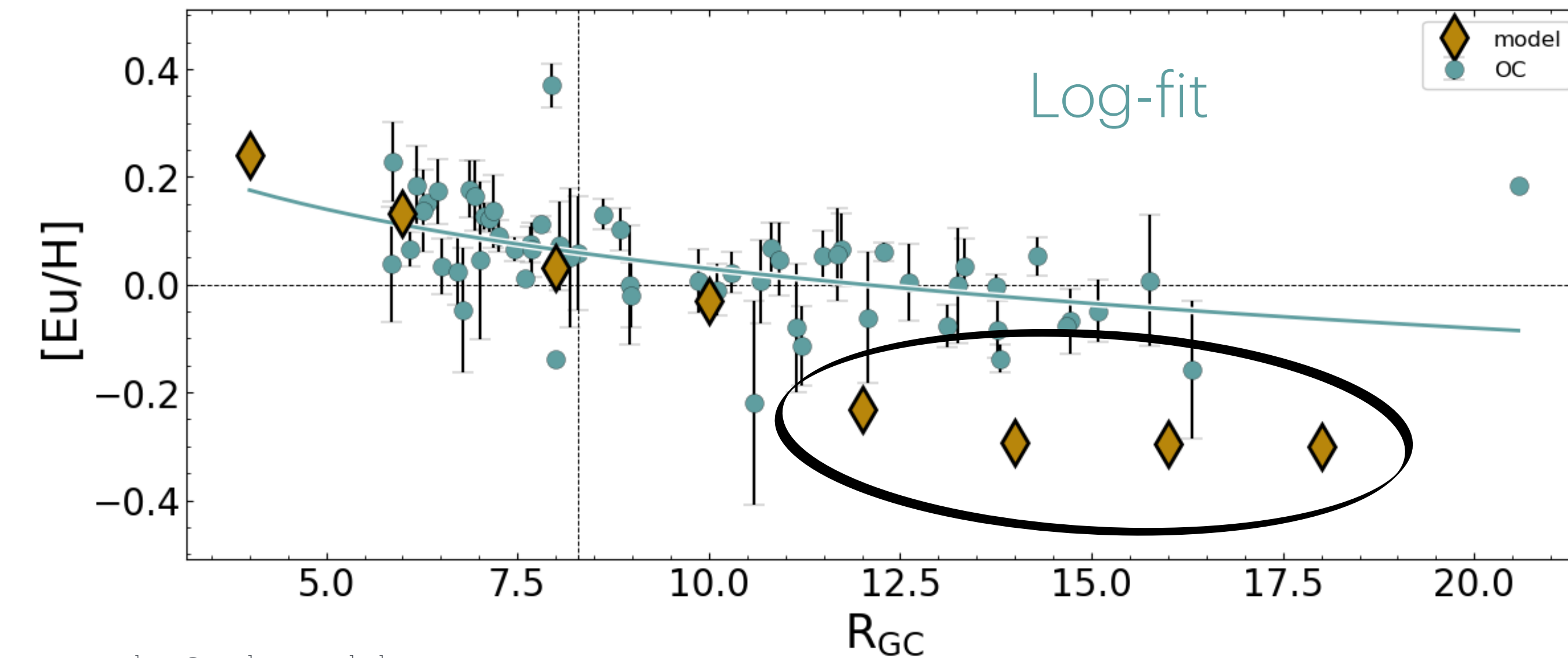


Abundance gradients

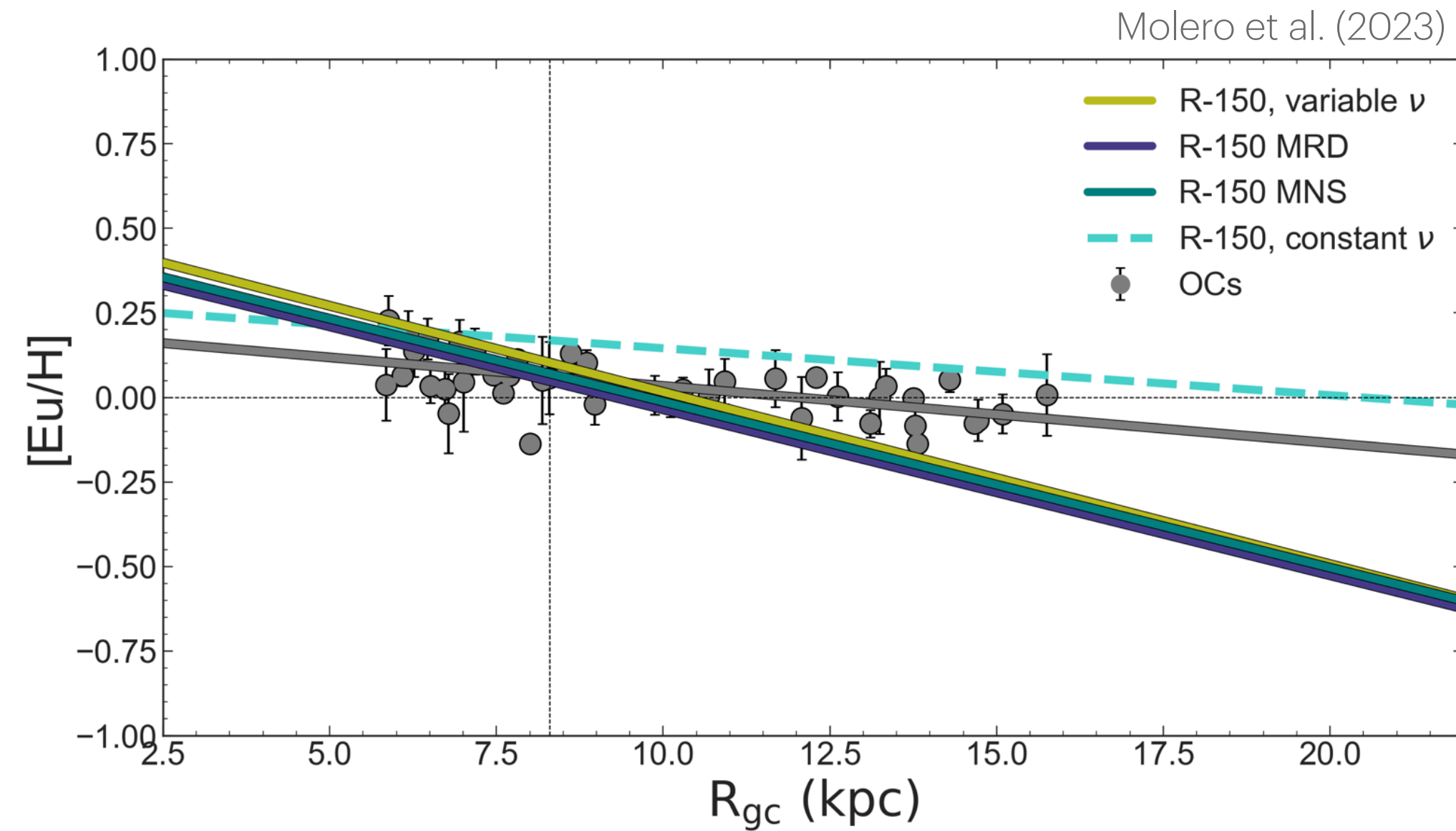


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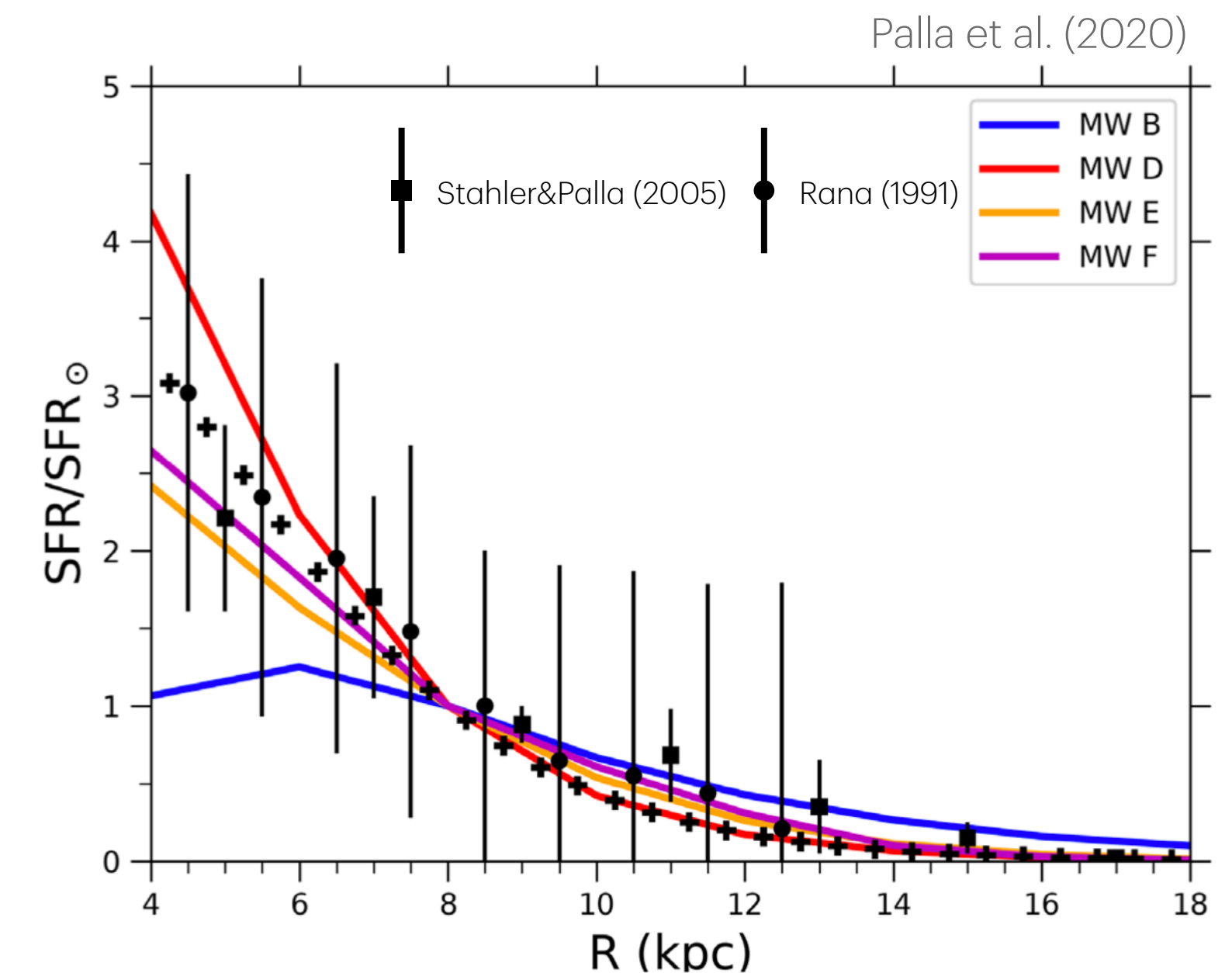
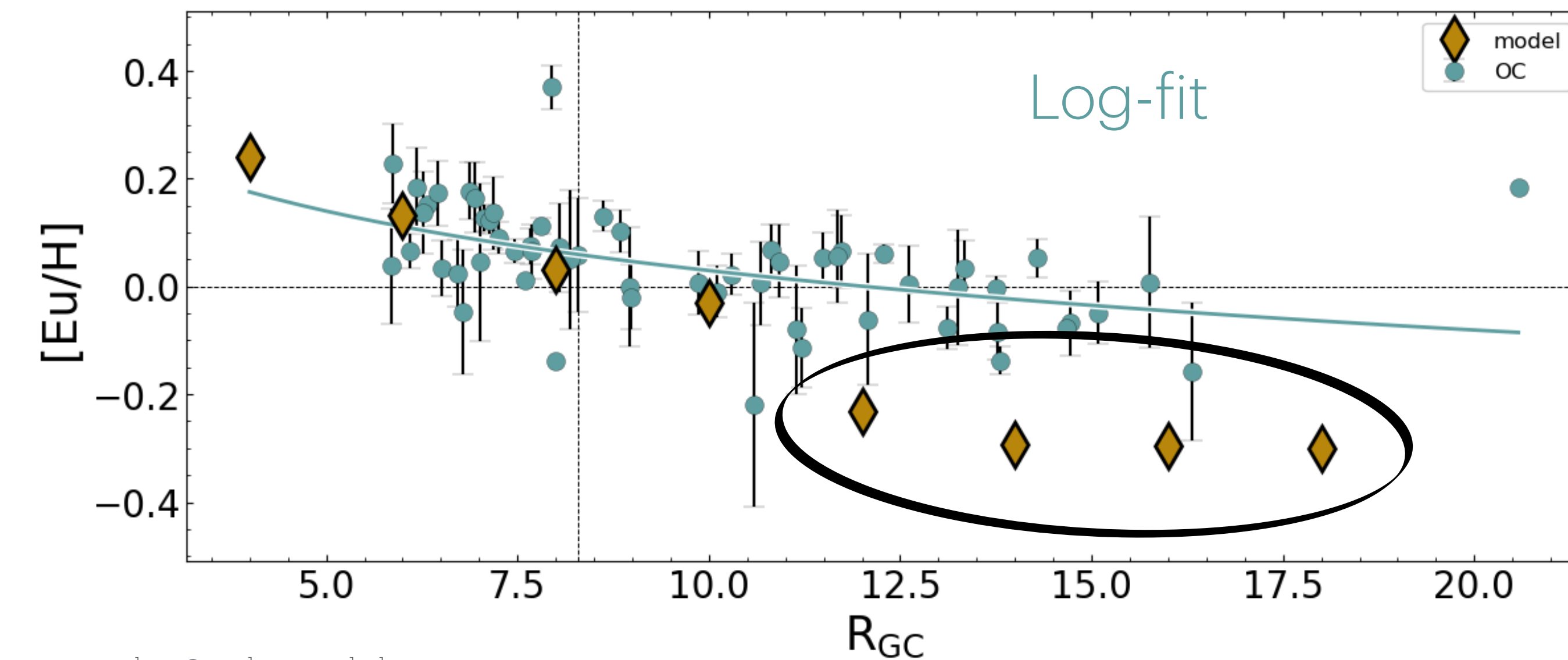
Abundance gradients



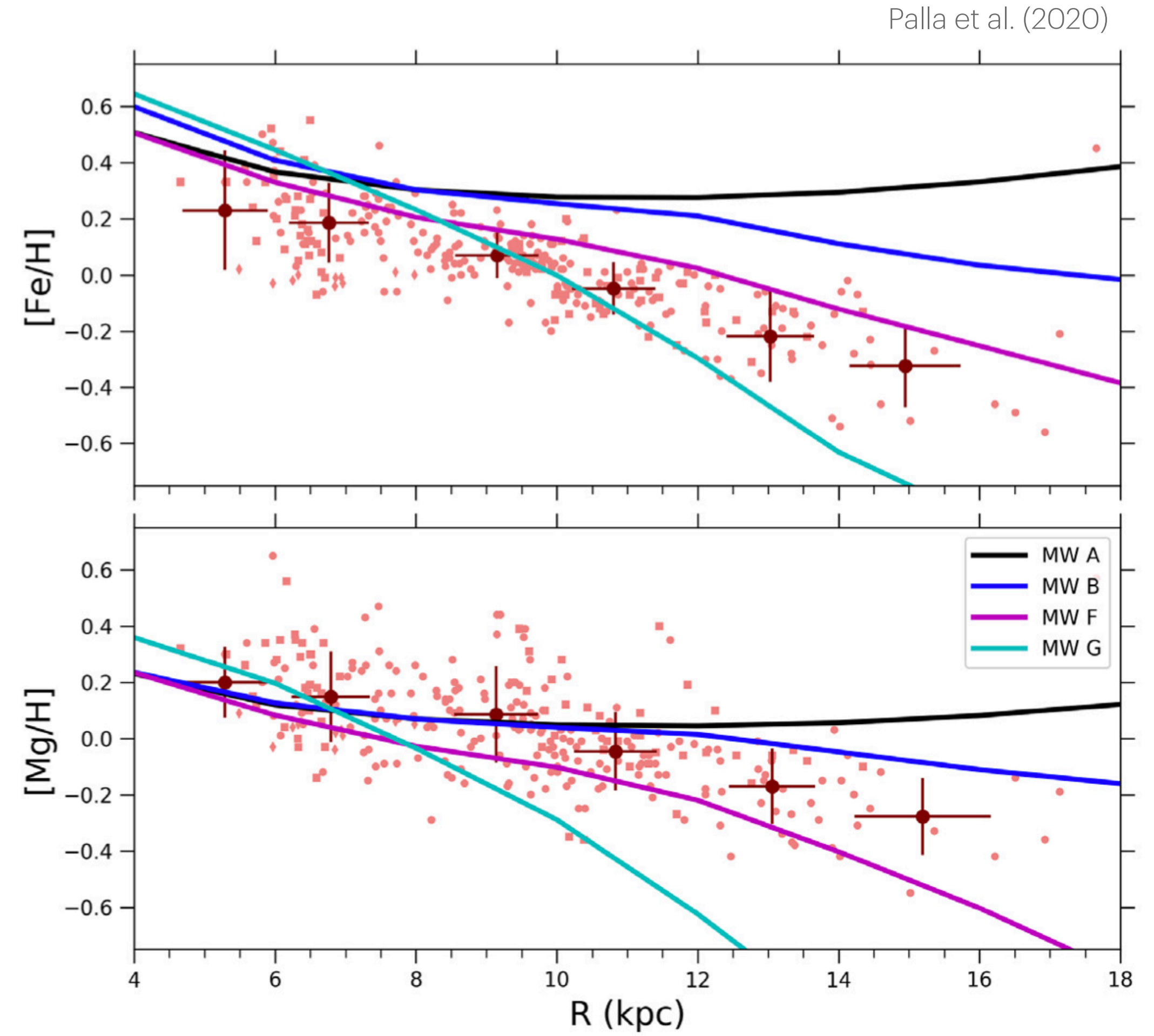
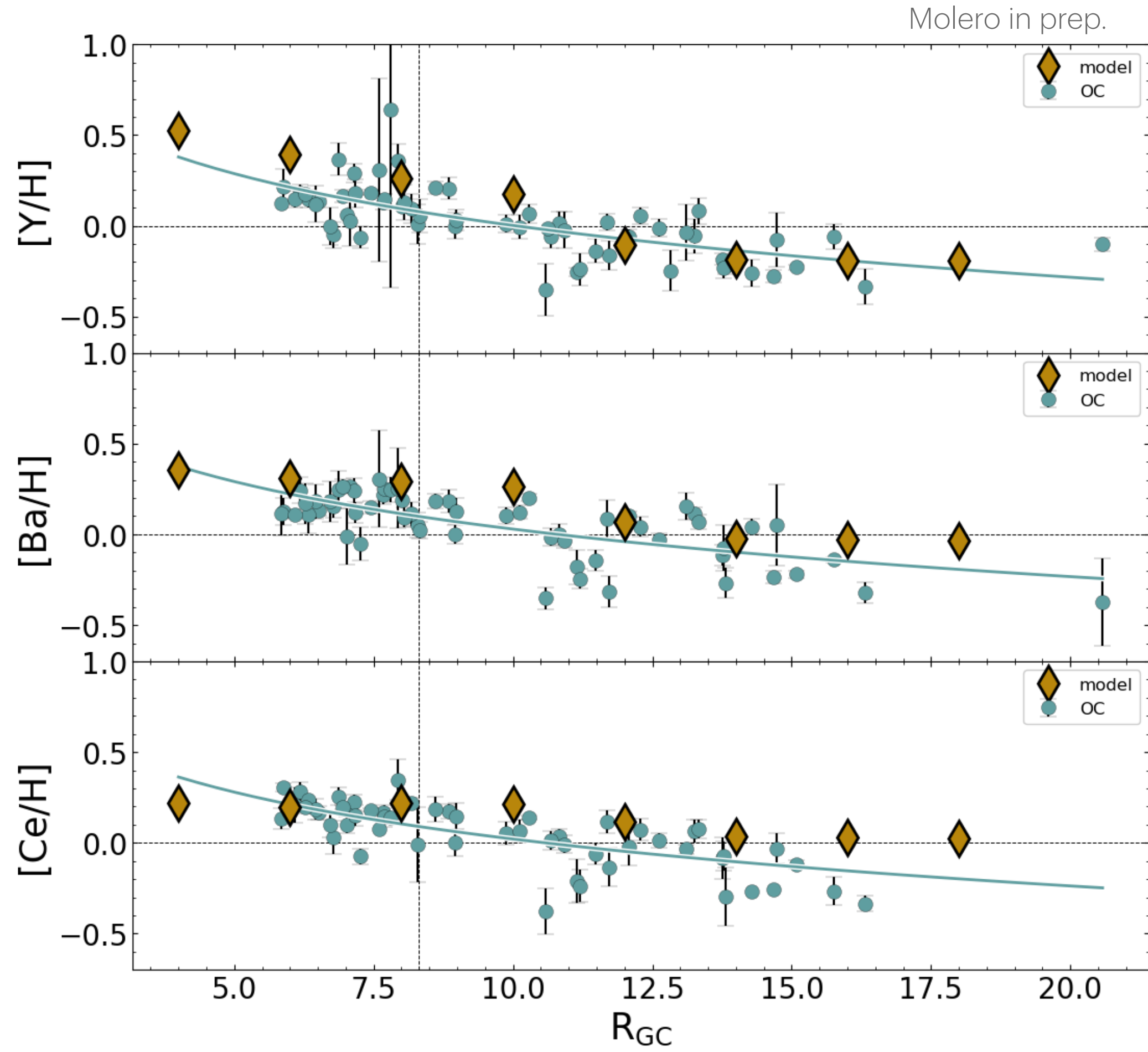
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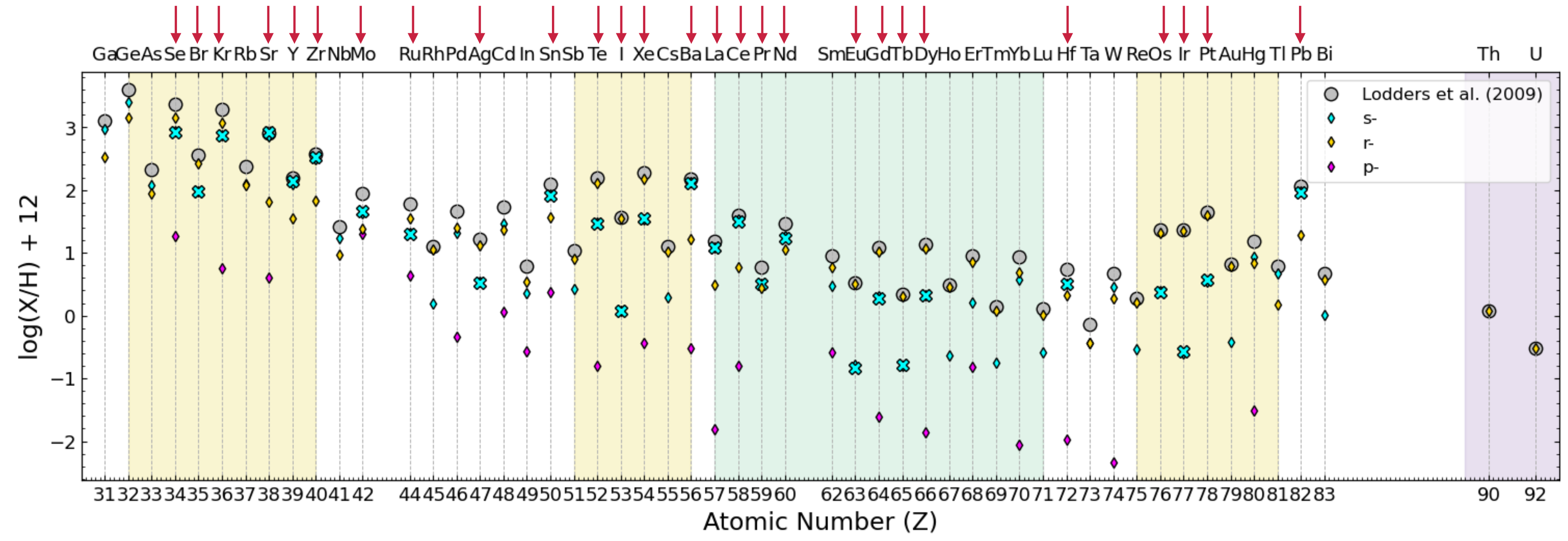
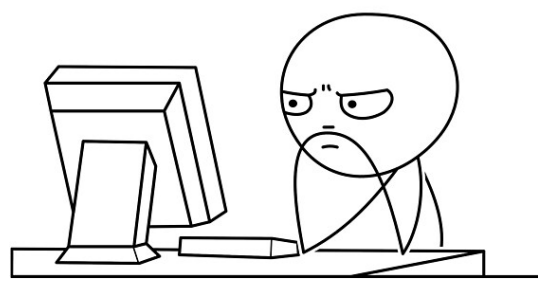
Inside out Galaxy formation



Abundance gradients



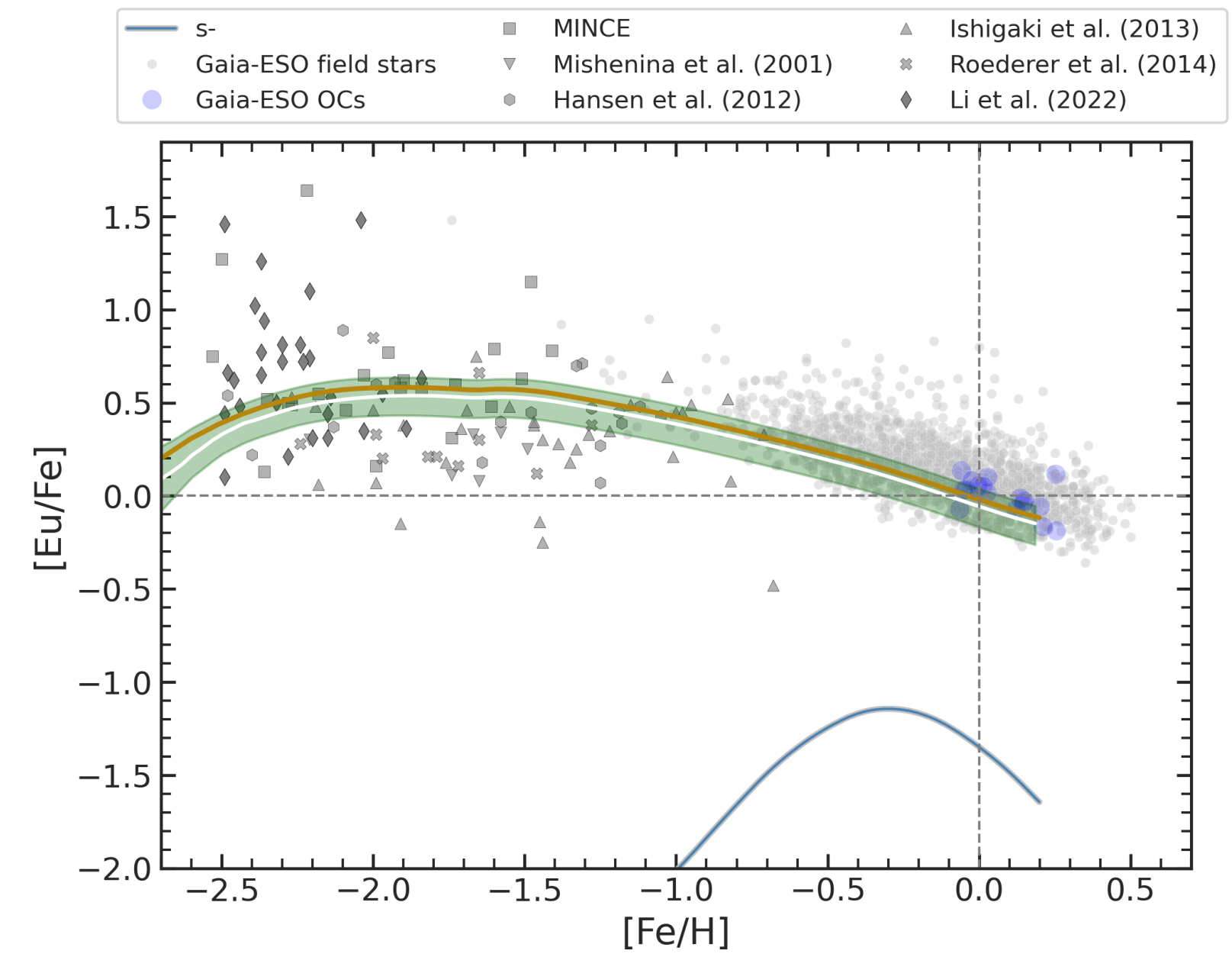
Parameter space exploration



e.g., Matteucci et al. (2014)

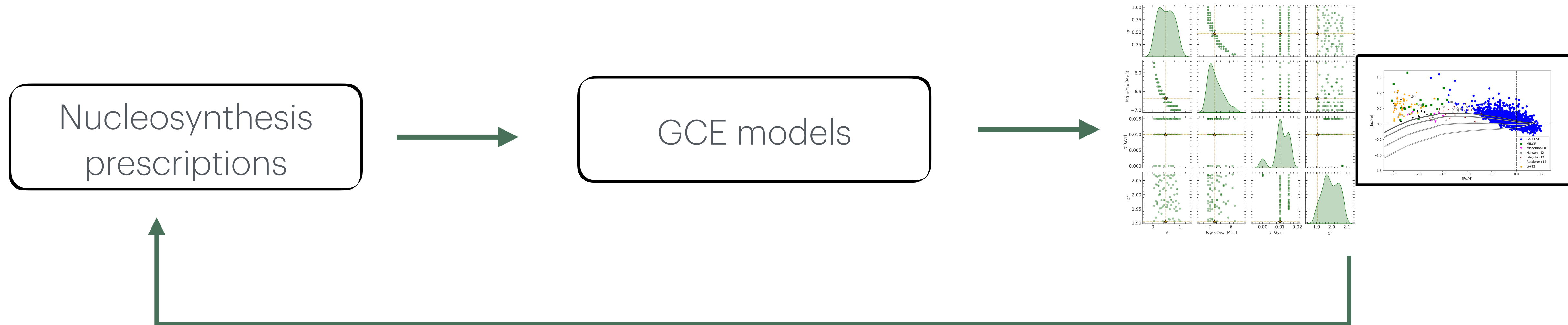
$$Y_{Eu} \times \alpha \int_{M_{min}}^{M_{max}} \psi(t - \tau_m - \tau) \phi(m) dm$$

$\sim 1 \times 10^5 \text{ runs}$



Conclusions

- GCE models are powerful tools to understand the formation and distribution of chemical species
- Homogenous models are useful for parameter exploration (**nucleosynthesis**) and sensitivity analysis

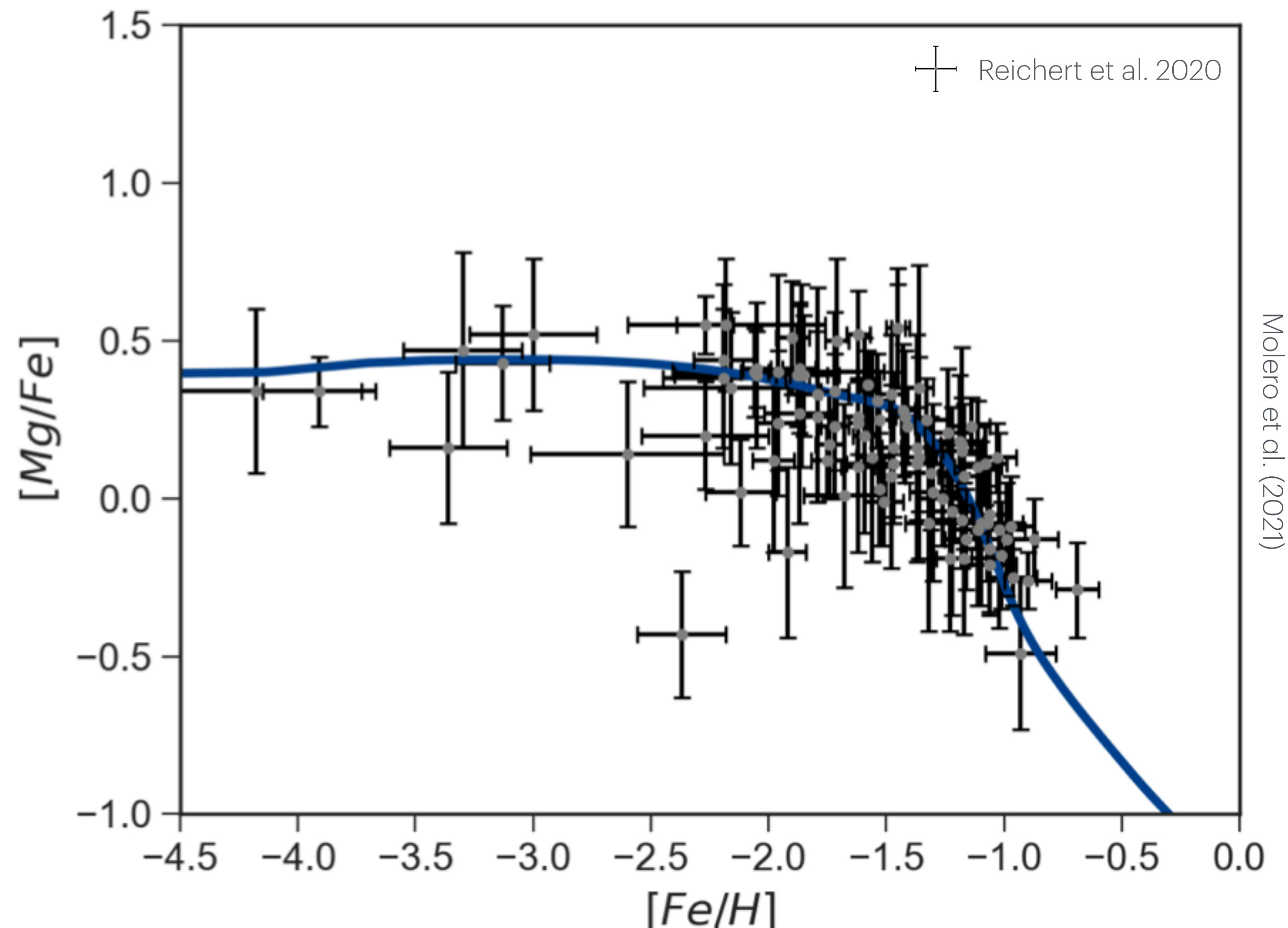


- Are NSM the dominant source of r-process in the Galaxy? Frequency? Delay?
- Do we need a second source? How can we calibrate it? Is the r-process still robust?
- Homogenous models can explain the average trend neutron-capture elements? Gradients?
- Open questions still remain...

Backup slides

Introduction: chemical evolution

$$[\text{Mg}/\text{Fe}] = \log(\text{Mg}/\text{Fe}) - \log(\text{Mg}/\text{Fe})_{\odot}$$



the observed metal abundances of stars today measures the composition of the ISM when the star was formed

Stars are the *fossil records* of past events:
Galactic Archeology

DTD for neutron star mergers

Delay time for MNS: $\tau = \tau_s + \tau_{gw}$

 lifetime of the secondary component
  gravitational radiation delay

$$\tau_{gw} = \frac{5c^5 A^4}{156G^3 m_1 m_2 (m_1 + m_2)} \text{Gyr}$$

Landau&Lifshitz (1966)

$$\tau_{gw} \propto \frac{0.15A^4}{m_1 m_2 (m_1 + m_2)} \text{Gyr}$$

Simonetti et al. (2019)

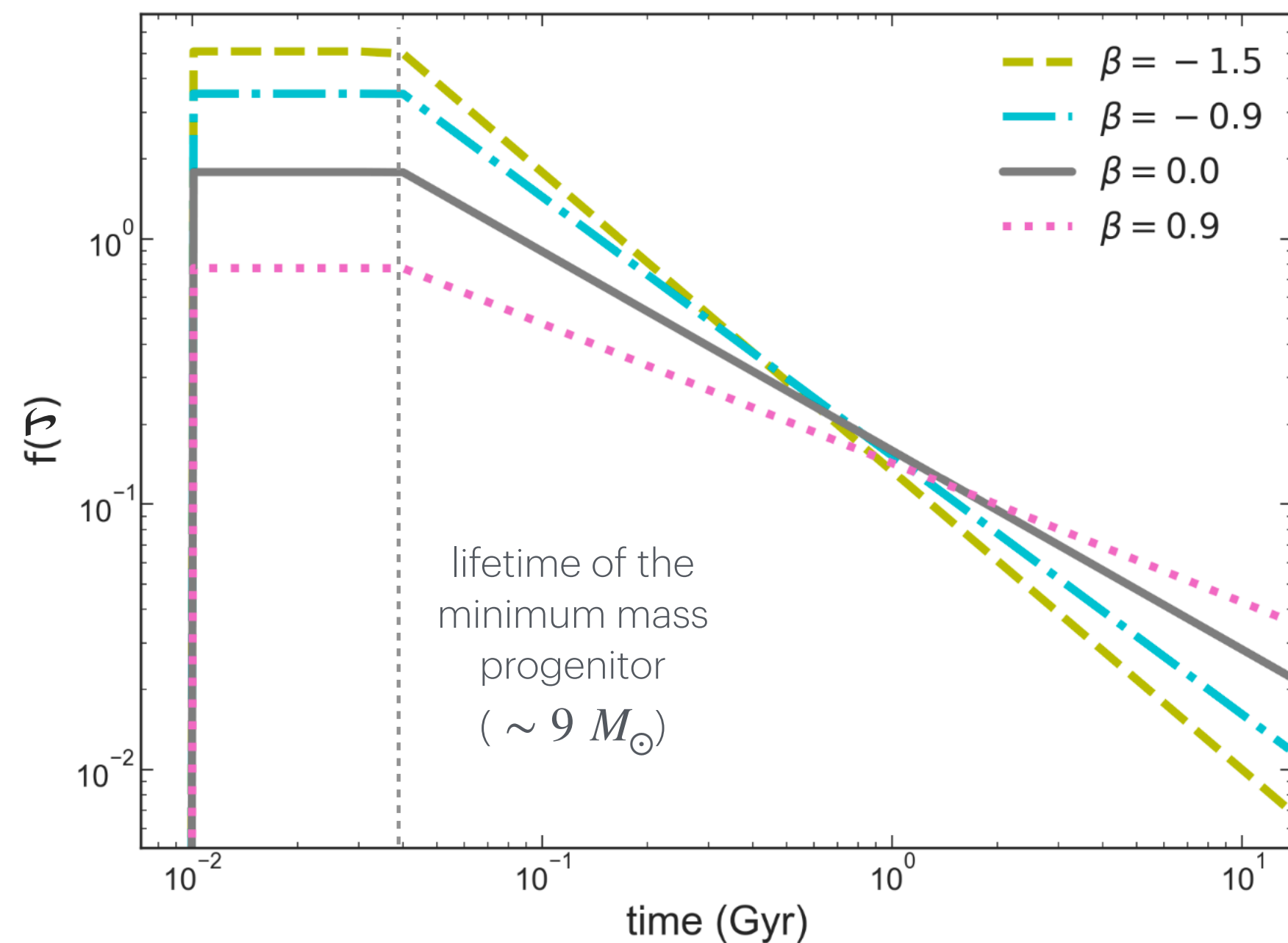
$$\tau_{gw} \propto \frac{0.6A^4}{M^3} \text{Gyr}$$

$$df(\tau_{gw}) = df(A, M) = g(A)h(M)dAdM$$

$$\begin{cases} g(A) \propto A^\beta \\ h(M) \propto \text{const.} \end{cases}$$

DTD for neutron star mergers

$$f(\tau) \propto \begin{cases} 0 & \text{if } \tau < 10 \text{ Myr} \\ p_1 & \text{if } 10 < \tau < 40 \text{ Myr} \\ p_2 \tau^{0.25\beta-0.75} (M_s^{0.75(\beta+2.33)} - M_l^{0.75(\beta+2.33)}) & \text{if } 40 \text{ Myr} < \tau < 13.7 \text{ Gyr} \end{cases}$$



- First portion: formation of the first DNS system.
- Second portion: systems which merge soon after formation of DNS system.
- Third portion: distribution of gravitational delay times.

Rate of neutron star mergers

When? + How much? + How many?

→ The rate, $R_{event}(t)$

$$R_{MNS}(t) = k_{\alpha} \int_{\tau_i}^{\min(t, \tau_x)} \alpha_{MNS}(\tau) \psi(t - \tau) f_{MNS}(\tau) d\tau$$

Initial Mass Function

Star Formation

Delay Time Distribution

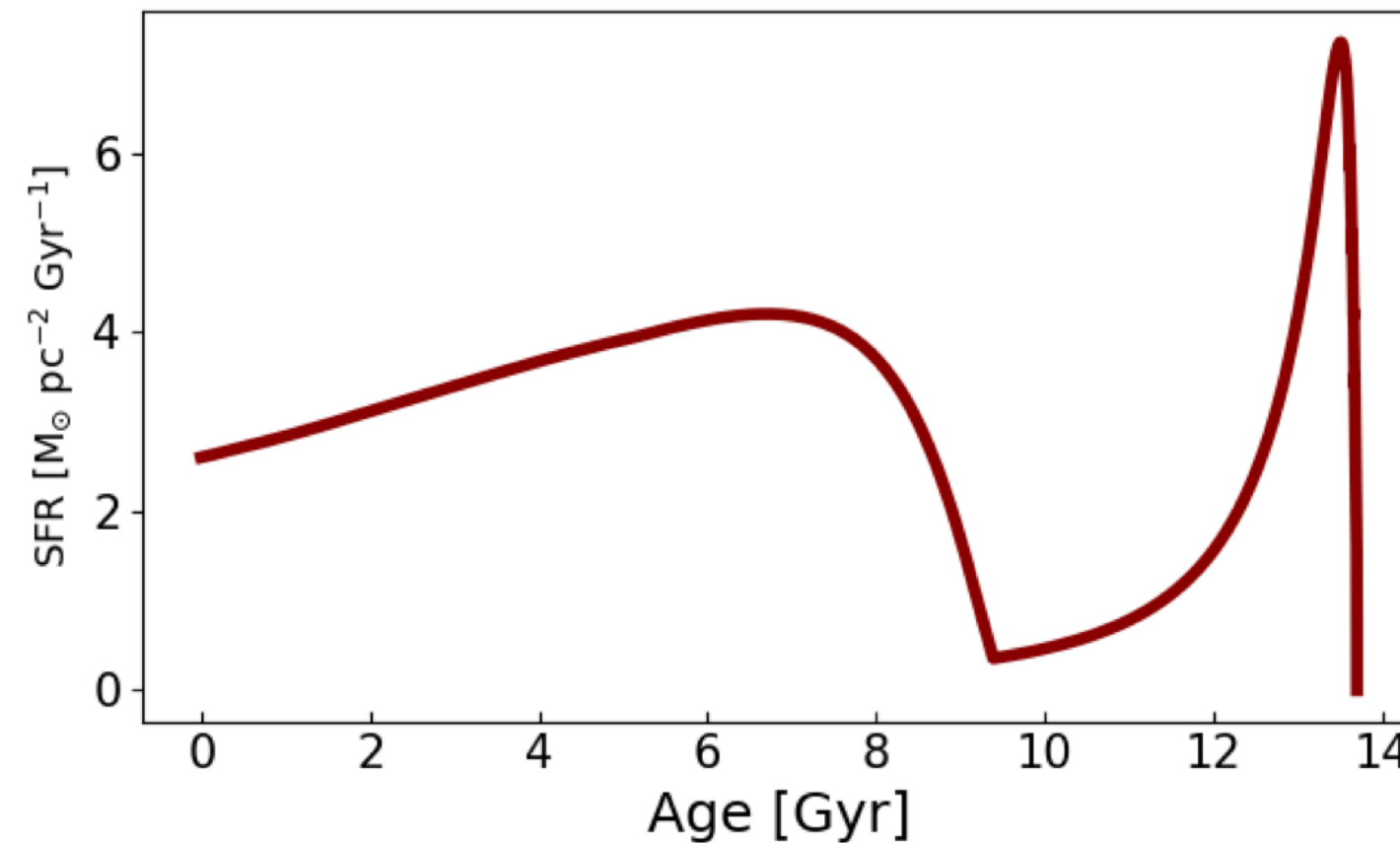
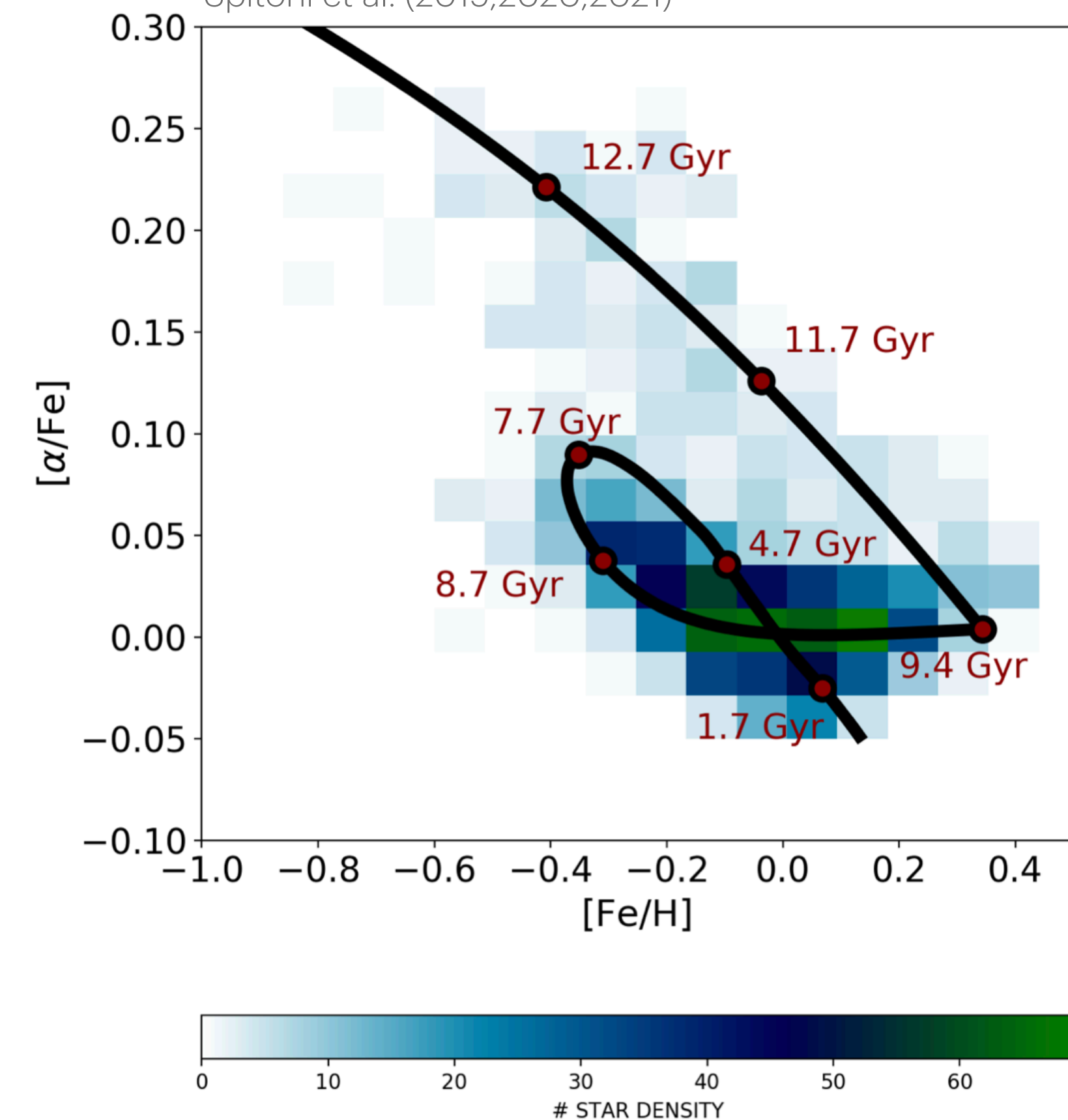
Two-infall model for the disk

$$\dot{M}_{\text{gas},i}(t, R) = -\psi(t, R)X_i(t, R) + X_{i,A}A(t, R) + \dot{R}_i(t, R)$$

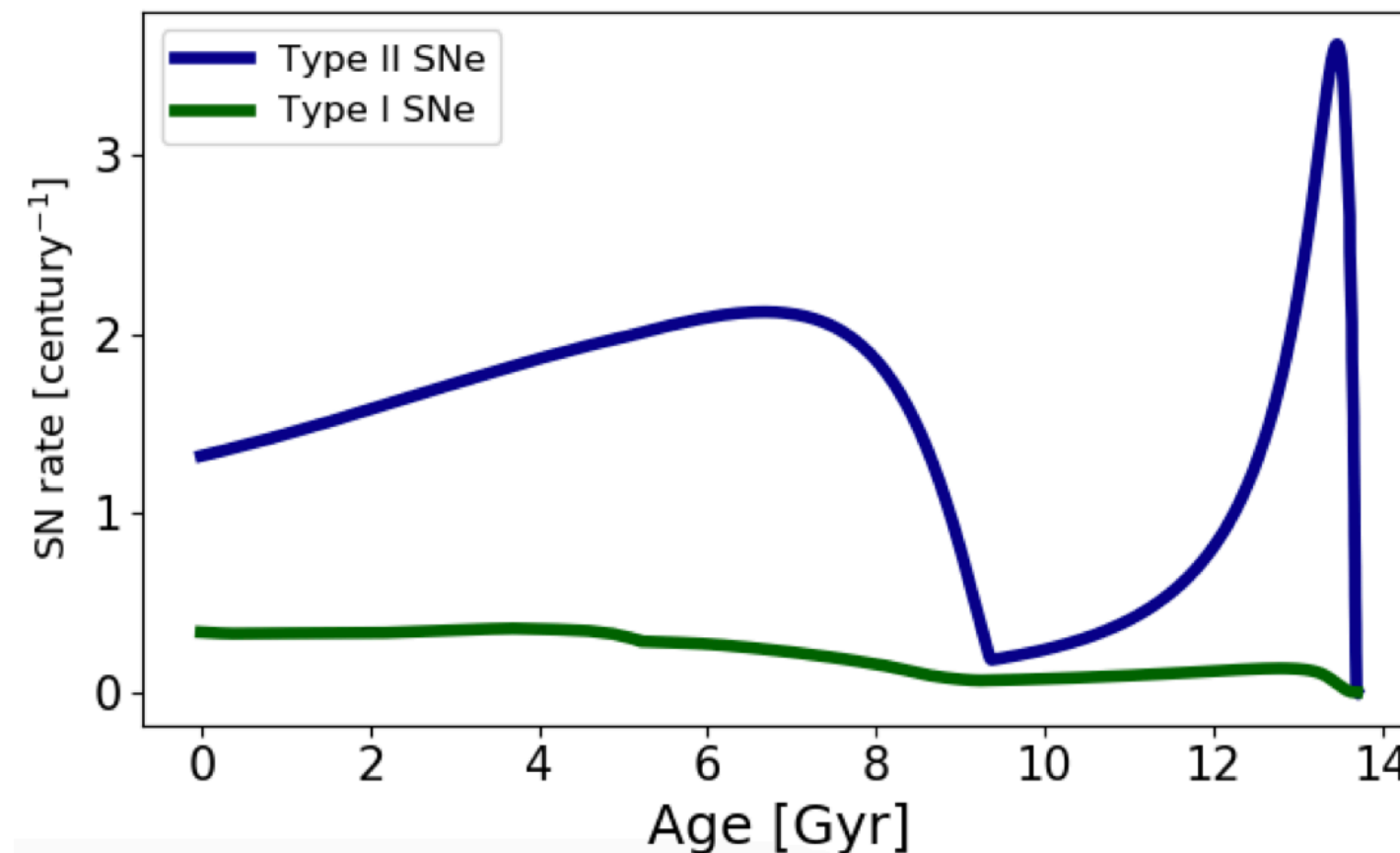


$$A(t, R) = c_1 e^{-t/\tau_{D1}} + \theta(t - t_{\text{max}})c_2 e^{-(t-t_{\text{max}})/\tau_{D2}}, \quad t_{\text{max}} = 3.25 \text{ Gyr} \quad \text{Palla et al. (2020)}$$

Spitoni et al. (2019;2020;2021)



- The late accretion of pristine gas has the effect of decreasing the metallicity of each stellar population born immediately after the infall event while it has little effect on the $[\alpha/\text{Fe}]$ ratio



- When the SF resumes, Type II SNe produce a rise in the $[\alpha/\text{Fe}]$ ratio, which is then decreased and shifted towards higher metallicities due to pollution from Type Ia SNe

The effect of rotation

1. ^{12}C synthesized in the He core diffuses up to the base of the H-burning shell
2. ^{12}C is converted into CNO nuclei, enhancing their abundance (^{14}N in particular)
3. CNO and some He are brought back to the centre
4. ^{14}N in the centre is converted into ^{22}Ne first and then into $^{25,26}\text{Mg}$

primary neutron source

