



# Atomic data requirements for Non-LTE modelling of Kilonovae

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(sirEN) Conference

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ULisboa



# ATOMIC DATA NEEDS

## LTE modelling (first few days):

→ **energy levels** and **E1 radiative transitions** required:

Saha & Boltzmann equations

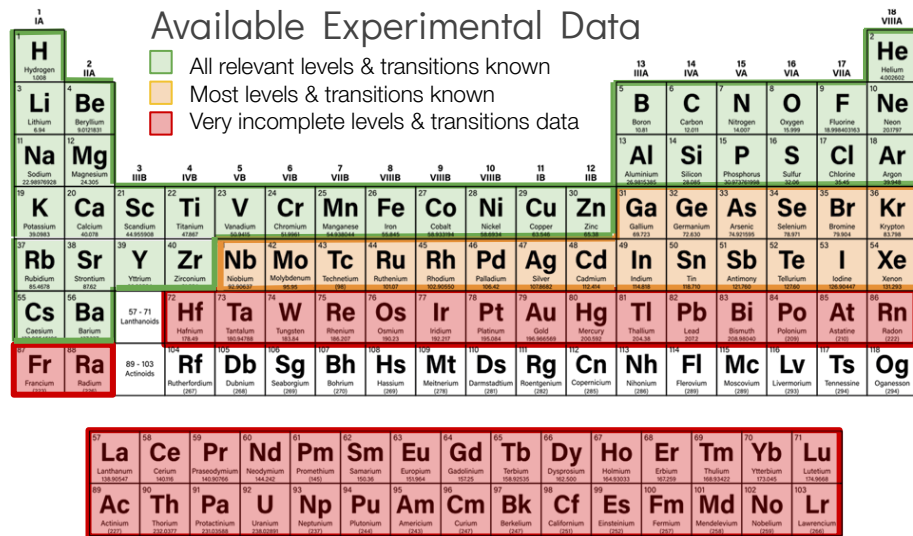
→ bolometric light curves: grey opacities from uncalibrated data good enough

→ spectral models: use of calibrated atomic data essential for line identification and obtaining the relevant spectral features

## NLTE modelling (after a few days):

→ requires additional atomic data: **electron-ion impact cross sections, photoionisation & recombination cross sections, forbidden (M1 and E2) transitions**

→ due to lack of atomic data only possible using approximations



Credit: A. Flörs

# ATOMIC DATA NEEDS

Energy levels

Recombination  
rates

(Optimal)  
Wavefunctions

Calibration

Radiative rates  
(M1, E2 transitions)

Radiative rates  
(E1 transitions)

Electron-impact  
excitation rates

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Detail in the modelling

# ATOMIC CODES

## General use codes - multiple atomic processes

- Usually user-input dependent **parameters**
- Able to calculate a large number of processes
- **Limited accuracy**
- **Fast and efficient**
  - 100 000+ levels and transitions in hours/days
- E.g. - **FAC**, Hullac, **Autostructure**, Los Alamos Suite, JAC ...

## High accuracy structure codes

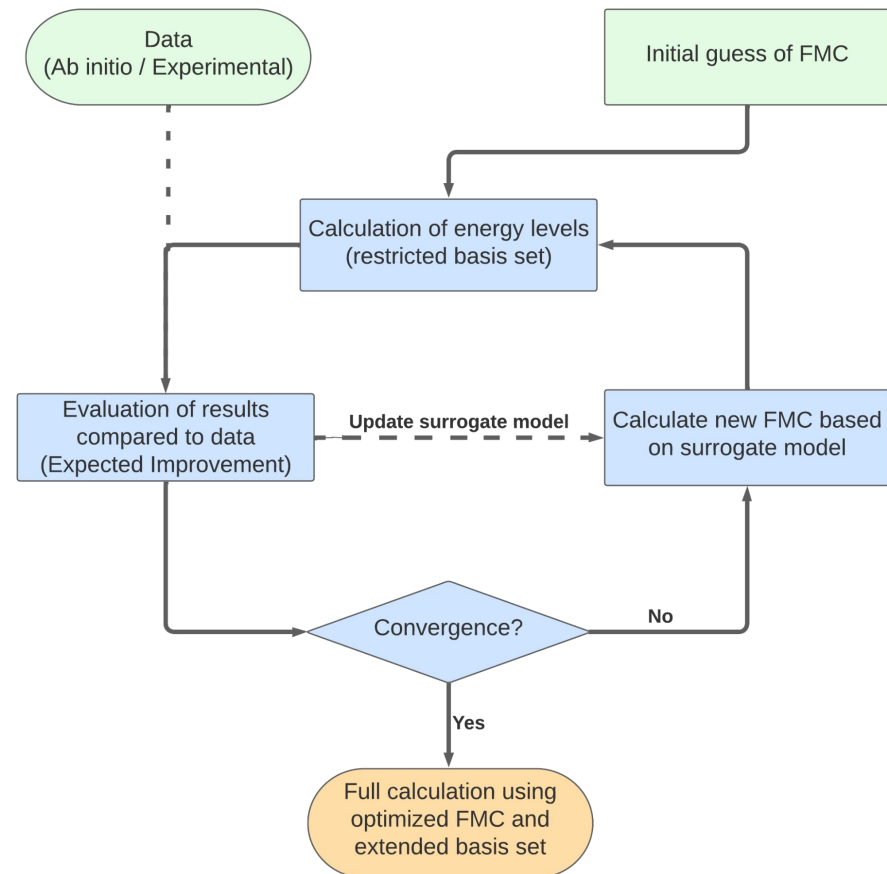
- Fully *ab-initio* using MC(D)HF or MBPT approaches
- Focused on structure and some radiative properties
- **High accuracy**
- **Computationally demanding**
  - Can take months for large scale calculations depending on the ion
- E.g. - GRASP\*, ATSP\*, MCDFGME\*, AMBiT, CI-MBPT...

\*Can be (usually) coupled to R-matrix codes for computation of other properties

# POTENTIAL OPTIMIZATION WORKFLOW

- **General** optimization procedure can be applied to multiple codes requiring direct user input for determining local central potential
  - **Sequential Model-Based Optimization (SMBO)** procedure applied to **FAC**- RFS+ 25 (10.48550/ARXIV.2502.13250)
  - Similar application done already in **AUTOSTRUCTURE** (M. Mendez PhD Thesis (2021); RFS (in prep.))
- **Flexible** loss function - can be adapted to optimized for different needs
  - Energy levels, transition rates, cross sections...

Open source code will be up on GitHub soon



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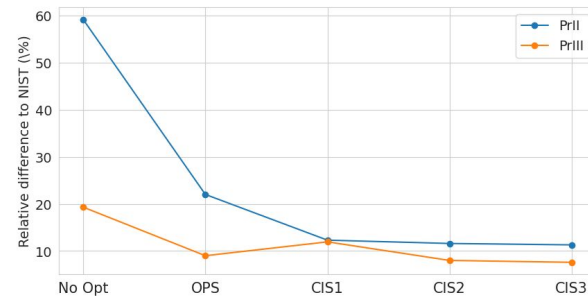
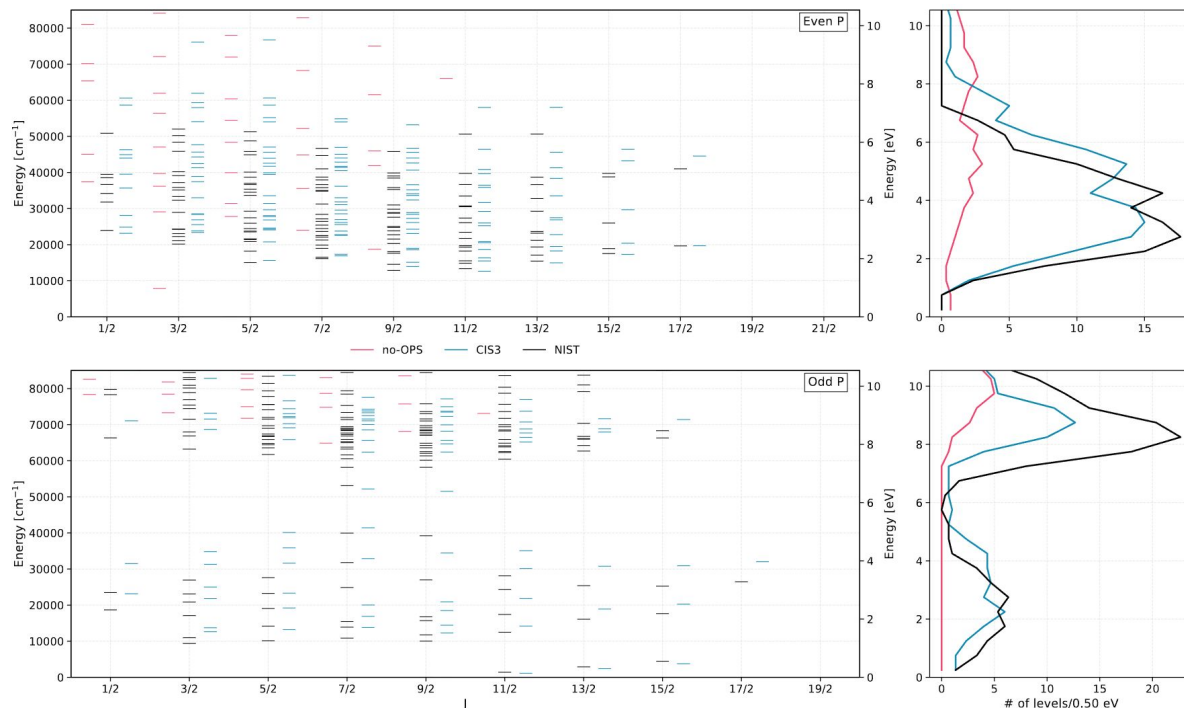
Radiative rates  
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Detail in the modelling

# ENERGY LEVELS – LANTHANIDES



- Optimization has the biggest impact in the accuracy of energy levels
- Further calibration (using Term Matching) is then achieved

Calculations for all singly and doubly ionized lanthanides have been achieved

# ENERGY LEVELS OF ACTINIDES

[R. F. Silva, in prep.]

$$\alpha_{GdII} = 4f^{6.3}5d^{2.08}6s^{0.54}6p^{0.08}$$



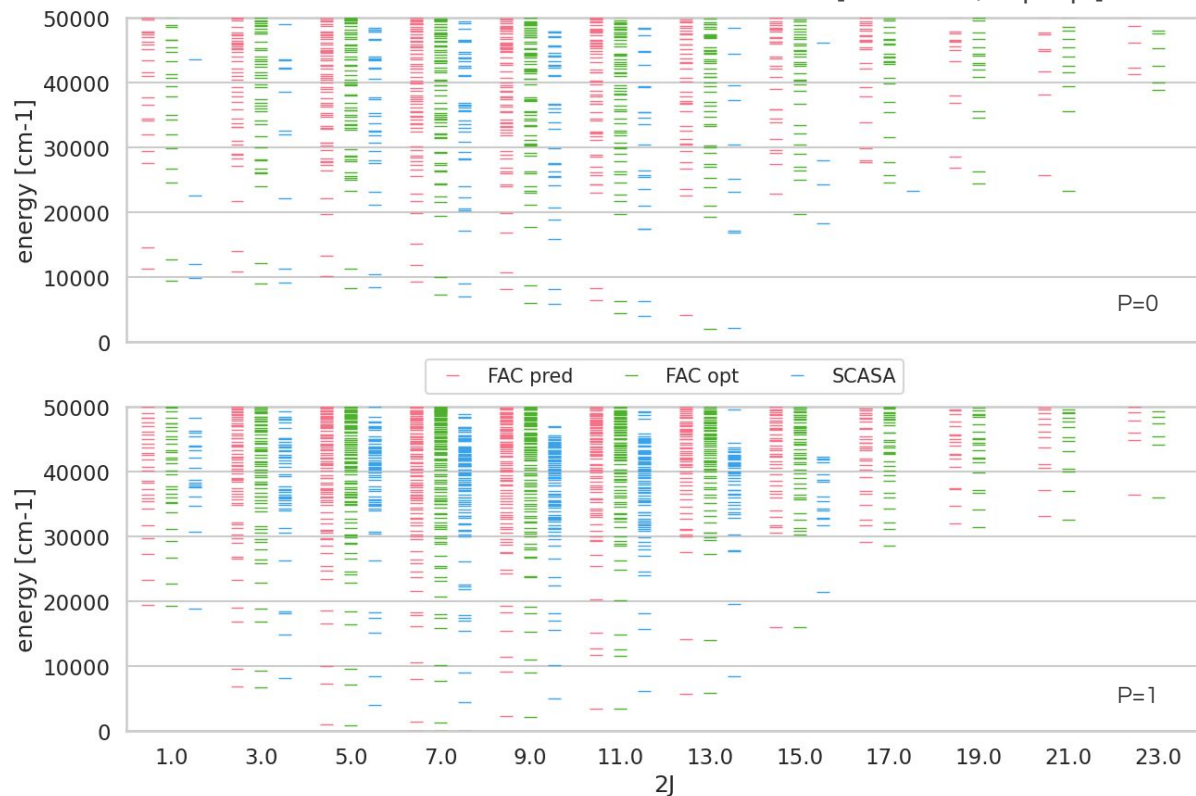
$$\alpha_{CmII}^{pred} = 5f^{6.3}6d^{2.08}7s^{0.54}7p^{0.08}$$

( $\Delta_{Exp} = 8.4\%$ )

$$\alpha_{CmII}^{opt} = 5f^{6.88}6d^{2.12}7s^07p^0$$

( $\Delta_{Exp} = 7.8\%$ )

- Ability to provide improved data for where no experimental data is available



SCASA - Selected constants, energy levels and atomic spectra of actinides (Blaise and Wyart 1983)



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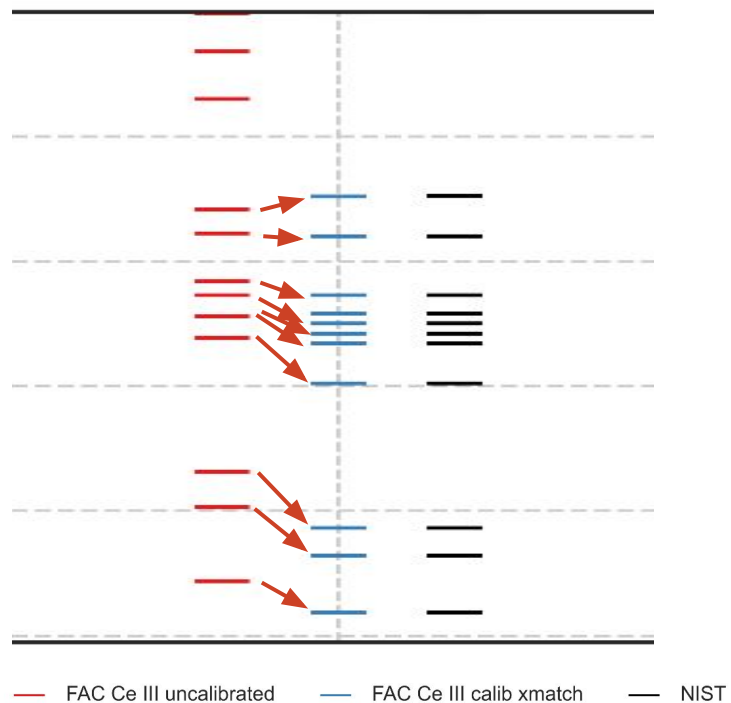
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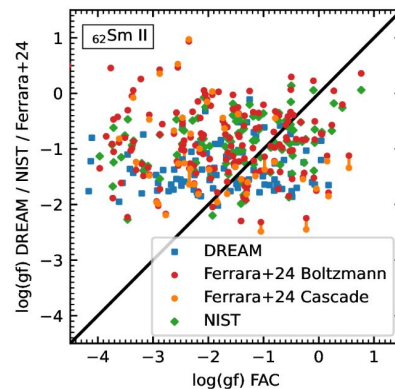
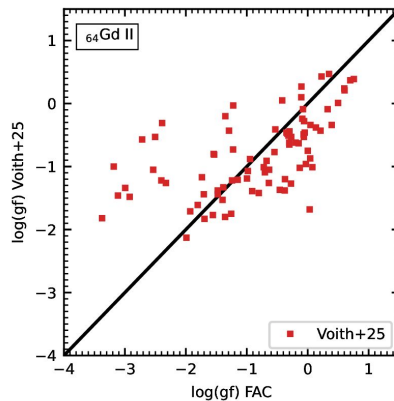
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Detail in the modelling

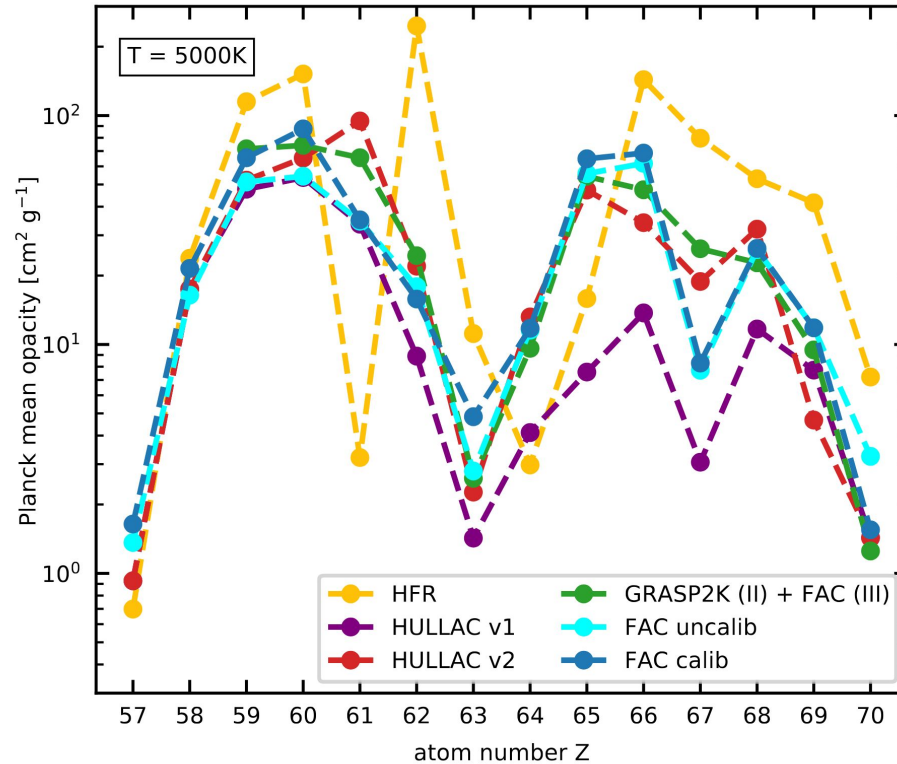
# CALIBRATION



- All levels are calibrated, either by matching directly to NIST or by using an empirical shift based on the corrections applied on other levels of same P, J and config
- Line strengths in agreement between calculations, but **less** so with available **experimental data** - especially for stronger lines



# ATOMIC DATA FOR LTE MODELLING



# ATOMIC DATA NEEDS

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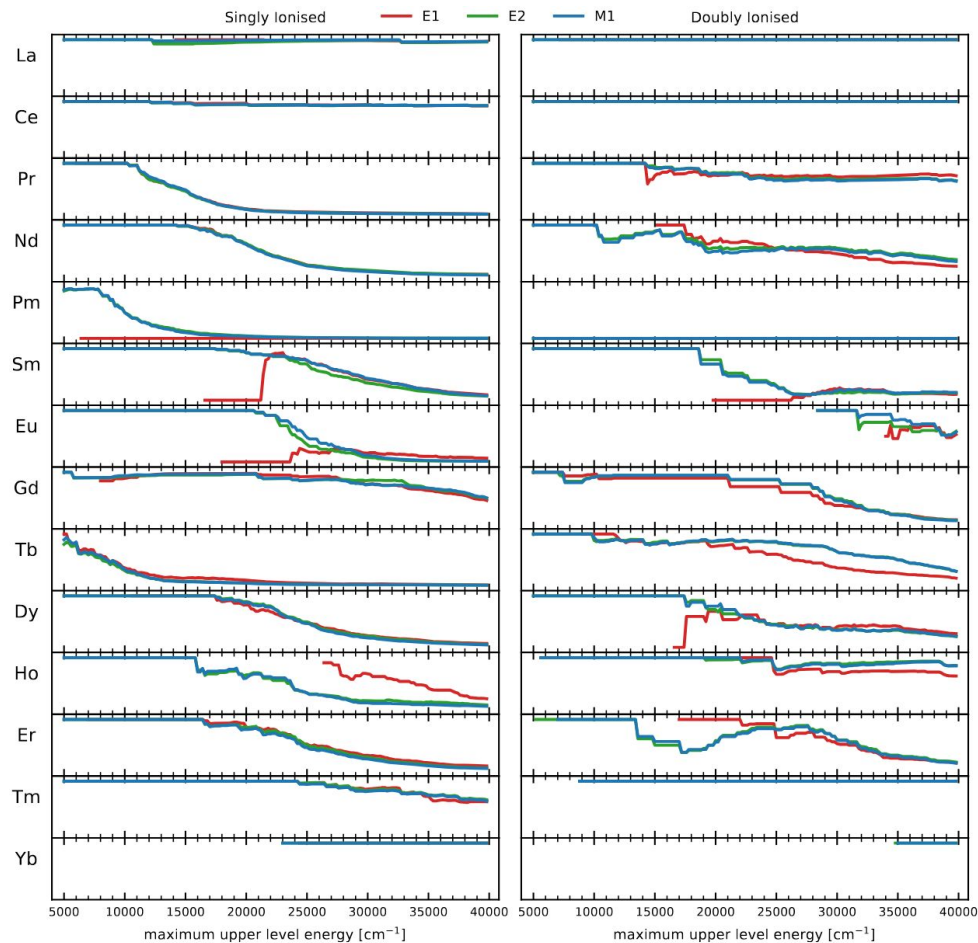
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Detail in the modelling

# FORBIDDEN LINES

- Doubly ionised lanthanides sufficiently well studied experimentally (exception: Pm III)
- Most permitted & forbidden transitions up to 20 000 - 30 000  $\text{cm}^{-1}$  energy calibrated
- Higher number of transitions for singly ionized ions makes the fraction of levels calibrated lower



Flörs et al. (in prep.)

# FORBIDDEN LINES

Flörs et al. (in prep.)

Ion	FAC calib. below $E_{\text{ion}}$		# E1 lines	# lines E1 calib.	# E2 lines	# lines E2 calib.	# M1 lines	# lines M1 calib.
	# config	# levels						
La II	44	472	17 743	1 239	17 277	1 335	16 551	1 286
La III	23	41	219	219	232	232	125	125
Ce II	40	2 829	408 639	14 592	387 677	20 456	499 746	15 873
Ce III	24	295	7 083	3 680	8 140	4 638	5 736	3 182
Pr II	18	3 689	571 453	881	687 044	1 012	708 795	848
Pr III	15	1 105	63 935	9 436	77 435	12 855	54 138	8 389
Nd II	27	9 994	3 336 077	5 434	3 284 715	6 512	4 100 622	5 215
Nd III	21	4 580	667 955	3675	720 857	4 718	848 074	4 228
Pm II	7	4 990	913 018	0	1 355 037	93	1 303 516	66
Pm III	14	5 526	797 829 s	0	1 046 057	0	1 267 671	0
Sm II	6	6 145	1 111 875	1 106	1 776 621	1 038	1 767 334	1 033
Sm III	16	11 177	1 911 972	95	2 189 469	237	2 835 854	206
Eu II	10	6 781	888 646	224	2 281 580	271	2 430 630	198
Eu III	11	8 470	1 308 810	893	2 218 726	934	2 640 346	821
Gd II	8	12 394	3 070 318	2 909	5 926 233	4 333	6 533 689	3 295
Gd III	10	6 298	814 002	85	1 665 995	94	1 844 924	64
Tb II	8	16 092	5 245 495	445	9 641 783	526	1 0486 628	433
Tb III	9	8 385	1 335 501	928	1 886 633	1071	2 546 384	806
Dy II	9	12 493	3 580 925	4 617	7 062 482	5 456	7 117 517	4 836
Dy III	6	3 910	355 148	1 246	863 920	1 223	747 452	960
Ho II	8	1 517	86 064	101	141 936	107	125 433	104
Ho III	14	4 658	462 551	1 162	601 531	1 617	696 321	1 149
Er II	16	5 072	838 067	983	1 153 835	1 272	1 416 125	1 016
Er III	18	2 837	195 156	216	234 072	238	238 953	163
Tm II	17	1 517	114 318	7 307	172 834	6 911	152 396	7 406
Tm III	11	650	16 361	1 200	24 834	1 792	18 229	1 461
Yb II	34	348	8 849	3 711	11 223	3 963	11 052	4 414
Yb III	14	916	1 585	202	2 457	347	1 987	264
total		143 181	28 129 594	66 586	45 440 635	83 281	50 416 228	67 841

# ATOMIC DATA NEEDS

Energy levels

Recombination  
rates

Hotokezaka et al., MNRAS, 506, 5863 (2021)

Banerjee et al., submitted to ApJ (2025)

(Optimal)  
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Detail in the modelling

# ATOMIC PROCESSES WITH THE CONTINUUM

Ideally, all processes should be computed using the same wave function expansion for the bound (N) and continuum (N+1) states

$$\Psi(N+1) = \mathcal{A} \sum_i^{n_f} \Psi_i(N) \theta_i$$

Two main methods:

- Distorted Wave (DW)
  - Neglects interaction between channels (resonances)
  - Fast and efficient
  - FAC, AUTOSTRUCTURE, HULLAC
- Coupled-Cluster (aka R-matrix)
  - Resonances are treated consistently
  - Very computationally demanding
  - GRASP<sup>0</sup>+DARC

(Pradhan and Nahar, "Atomic Astrophysics and Spectroscopy", Cambridge 2011)

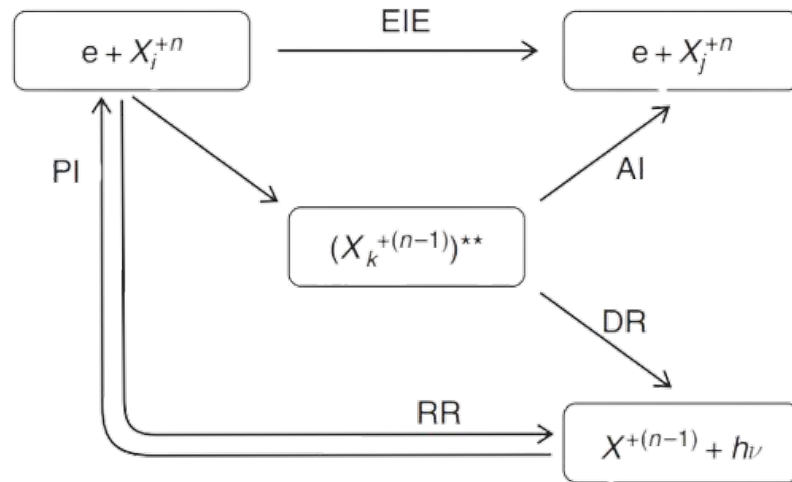
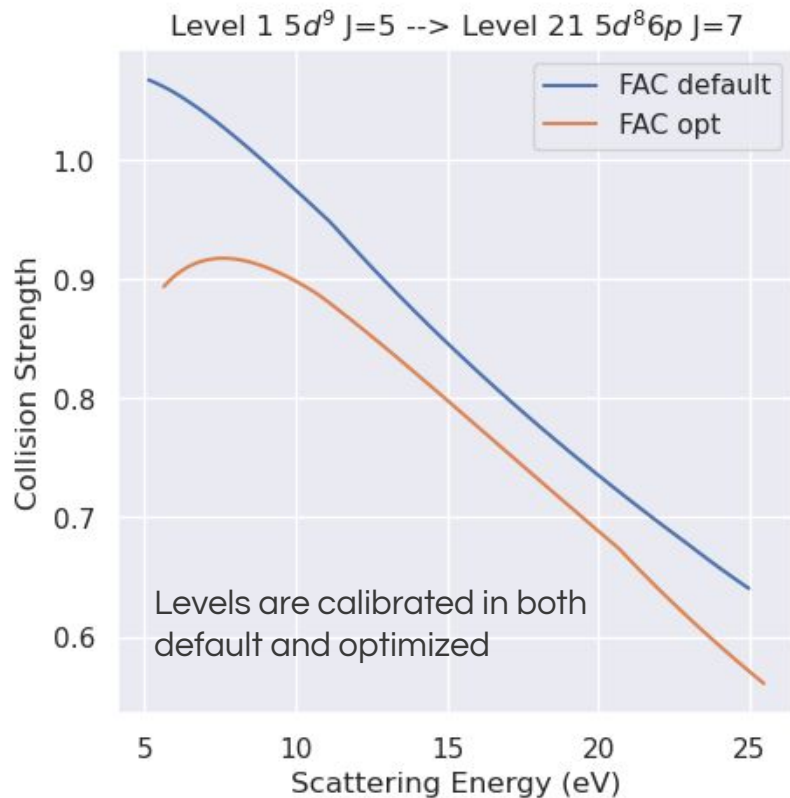


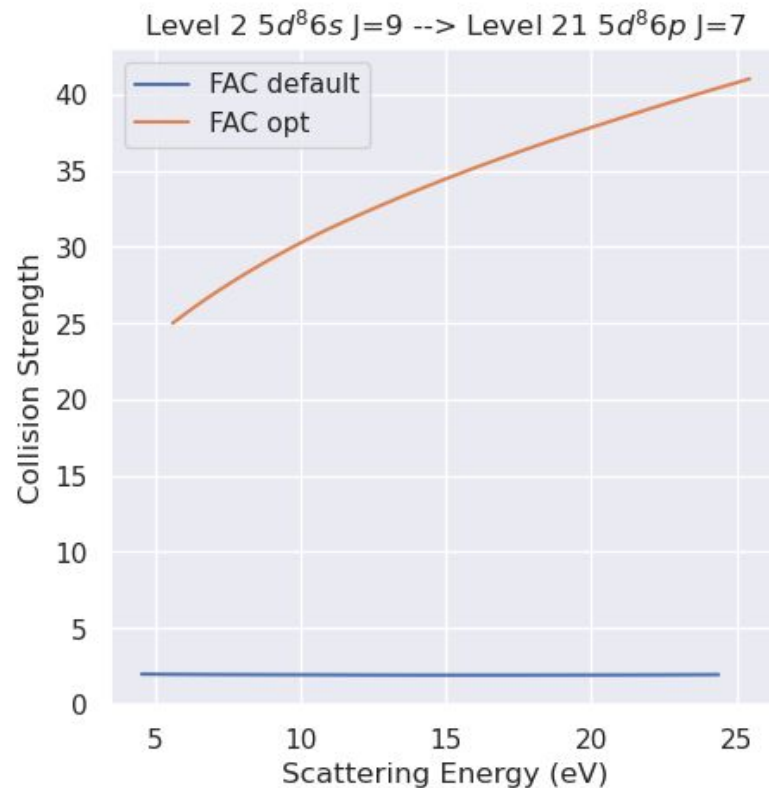
FIGURE 3.5 Unified picture of dominant atomic processes in plasmas: electron impact excitation (EIE), photoionization (PI), autoionization (AI), dielectronic recombination (DR) and radiative recombination (RR). Note the often important role of resonance states in the centre, mediating atomic processes.



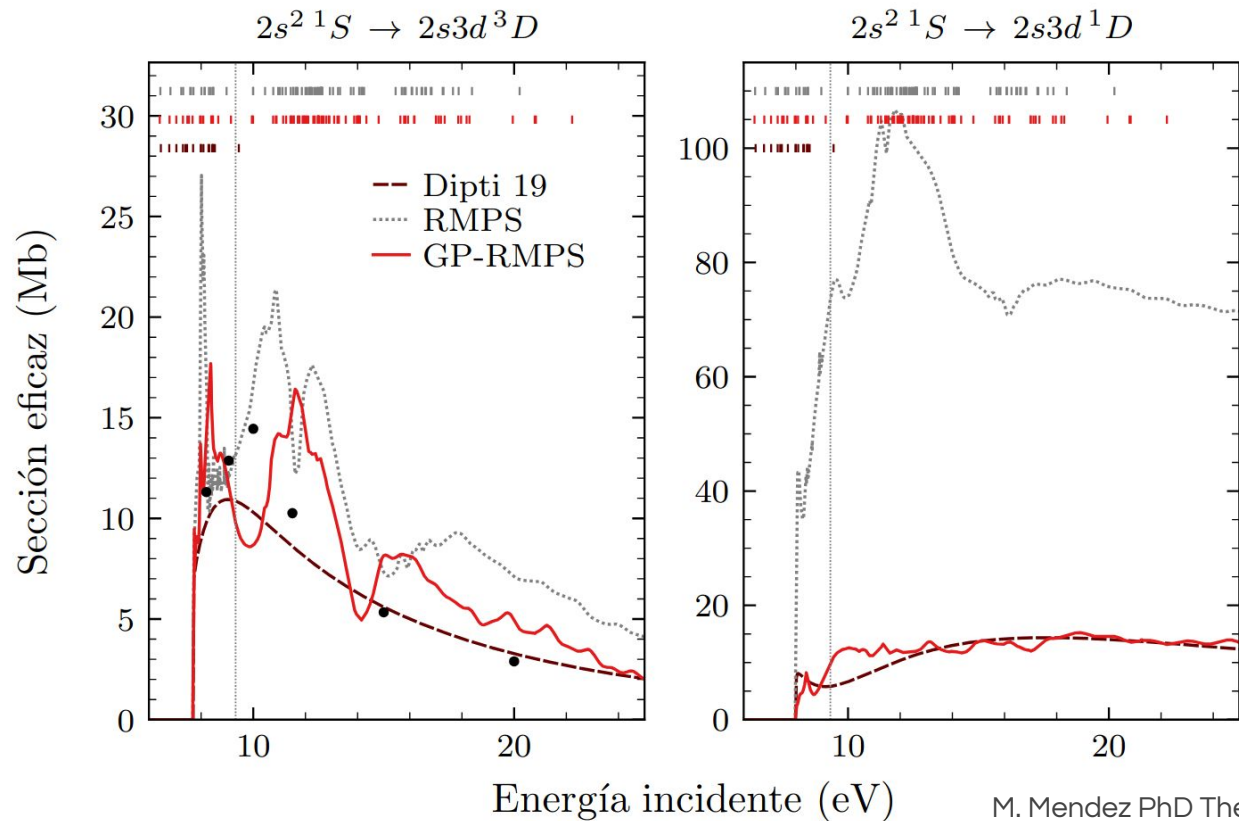
# IMPACT OF OPTIMIZATION ON EIE



Pt II



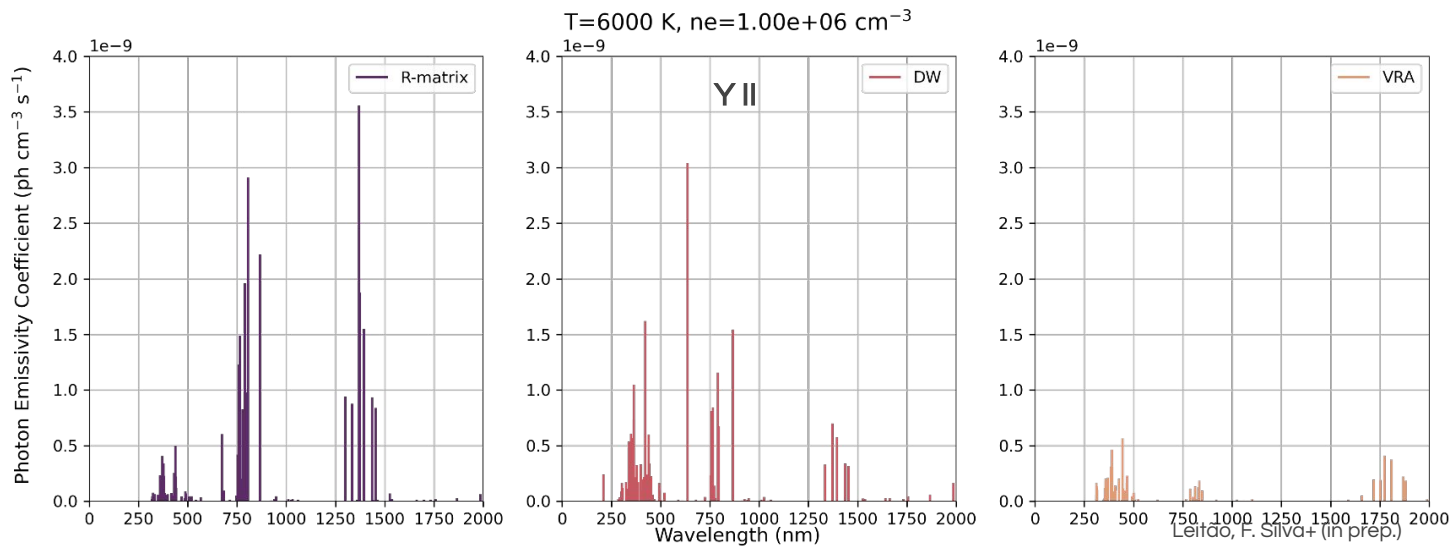
# IMPACT OF OPTIMIZATION ON EIE



M. Mendez PhD Thesis (2021)

- Similar optimization procedure for improved wavefunctions have shown similar effects on collisions strengths

# IMPROVING EIE COLLISION RATES



DW seems to provide significant improvements to the current status, based on empirical formulas (VRA):

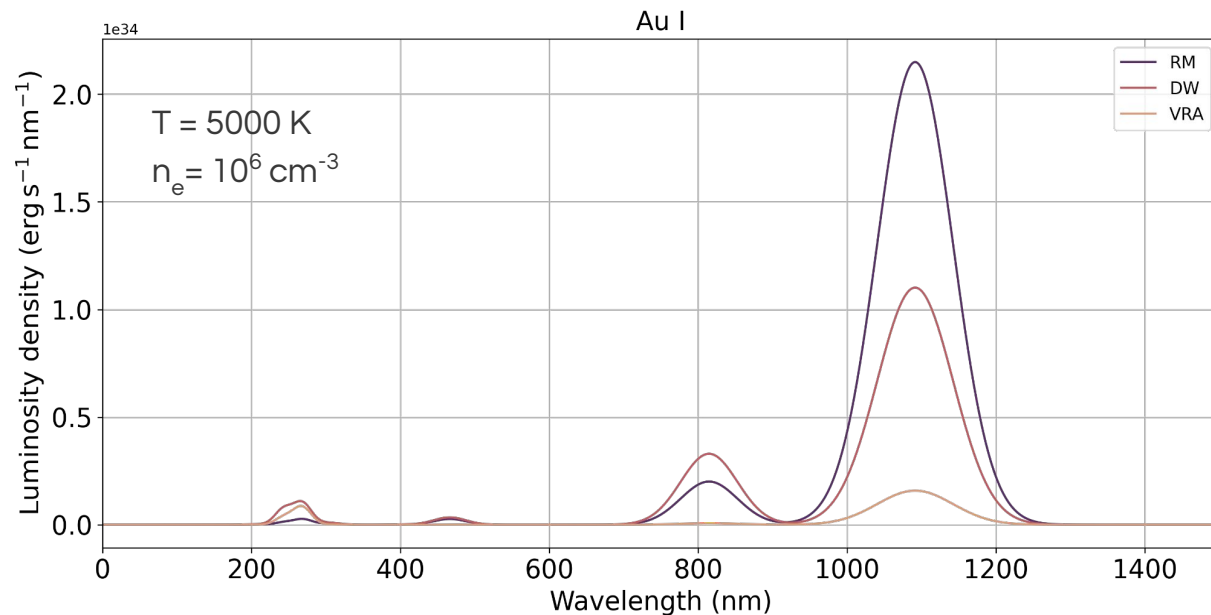
→ Van Regemorter for allowed,  $f_{\text{osc}} \geq 10^{-3}$

→ Axelrod 1980 for forbidden,  $f_{\text{osc}} < 10^{-3}$

Empirical approximations produce PECs ("line intensities") much lower than current calculations

DW provide a much better estimate at a very low computational cost

# IMPROVING EIE COLLISION RATES

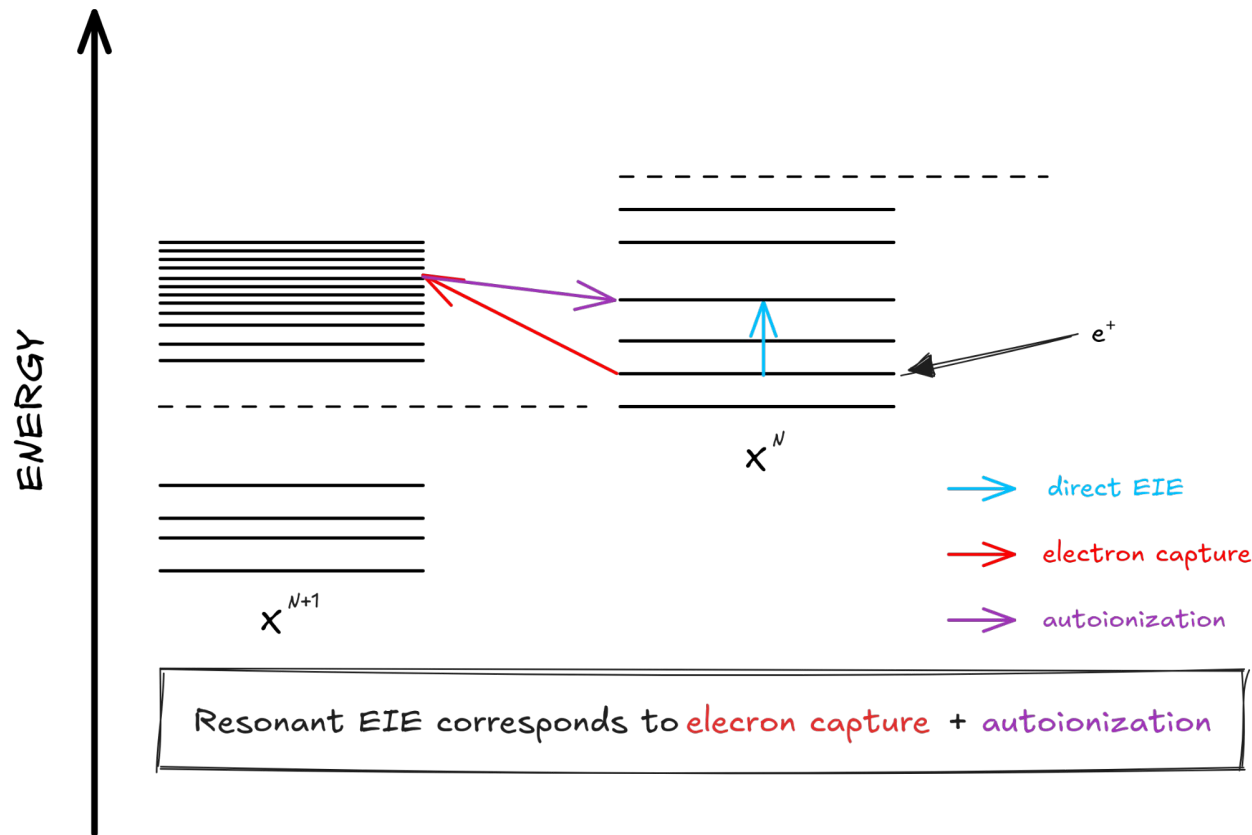


R-matrix calculation: McCann+ (2021)

- DW shows an improvement when compared to just using the VRA approximations -even without the inclusion of resonances.
- “Comparable” to R-Matrix - but at a much lower computational cost
- Calculations for multiple lanthanides have been achieved

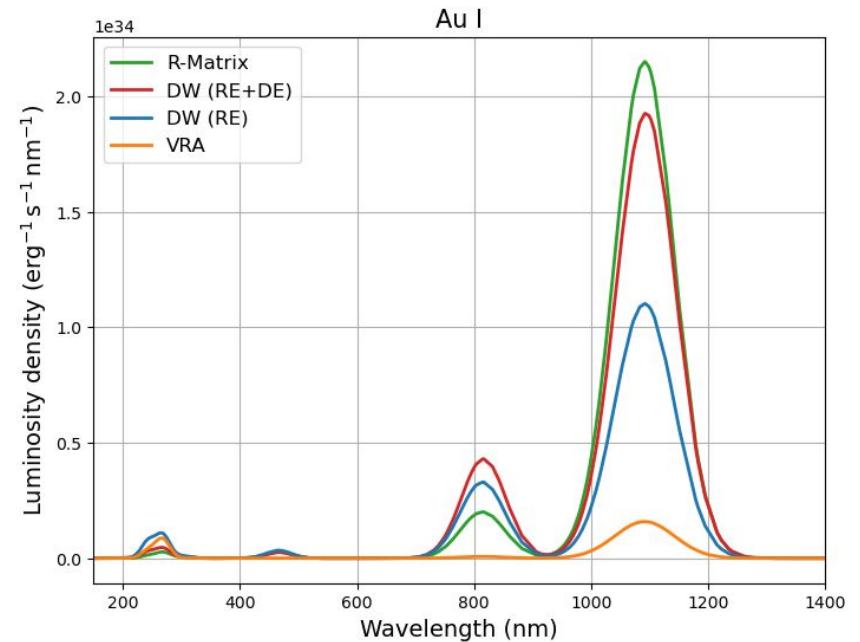
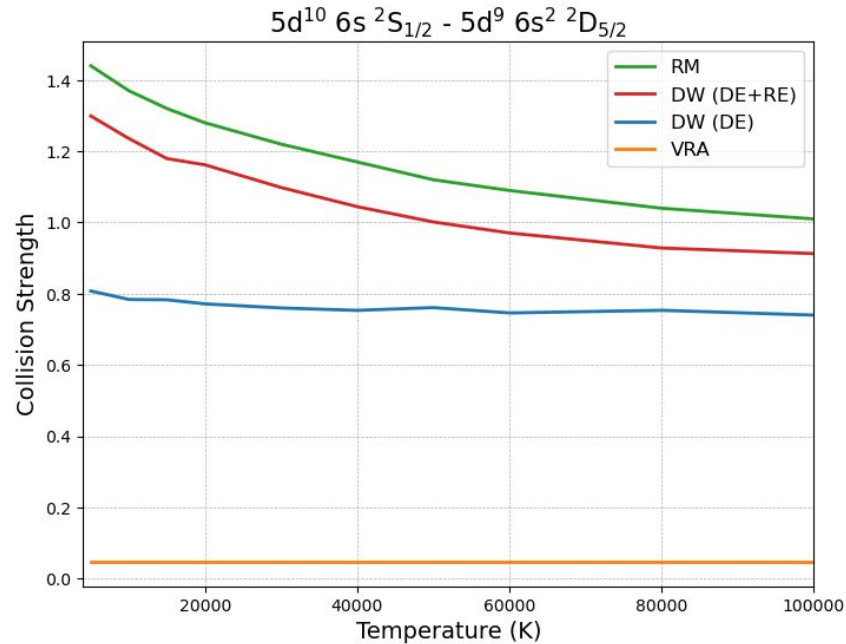
Check out Jorge Sampaio Poster!

# INCLUDING RESONANCES



- Resonances can be accounted for in the Independent-Process, Isolated-Resonance Distorted-Wave (IPIRDW) Method (see. e.g. L.Xia et al., 2017)
- While not as accurate is much more computationally efficient
  - Autoionization and EIE can be computed in parallel

# INCLUDING RESONANCES (PRELIMINARY)



- Calculation of Resonant EIE for multiple lanthanides ongoing

# CONCLUSIONS

- We computed the atomic structure of all **singly and doubly ionised lanthanide ions**
  - total of 28 ions (27 of them calibrated to experimental data)
  - 120 million (E1 + E2 + M1) transitions, of which 220 000 have calibrated wavelengths
- Inaccurate wavefunctions can have major effects in all atomic data parameters computed
  - Large configurations sets and optimization to available data (when possible) is essential when *ab-initio* calculations are not feasible
- Ongoing calculations of EIE under the DW approximation (DE and RE) for all singly and doubly ionized lanthanides
  - Accuracy of wavefunctions can have a strong impact in collision strengths

# COLLABORATION

Luis Leitão  
Daniel Garcia  
Tomás Campante  
Jorge Miguel Sampaio  
José Pires Marques

Gabriel Martínez-Pinedo  
Andreas Flörs  
Gerrit Leck  
Luke Shingles



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DARMSTADT

## ACKNOWLEDGEMENTS:

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PhD research grant: 2022.10009.BD





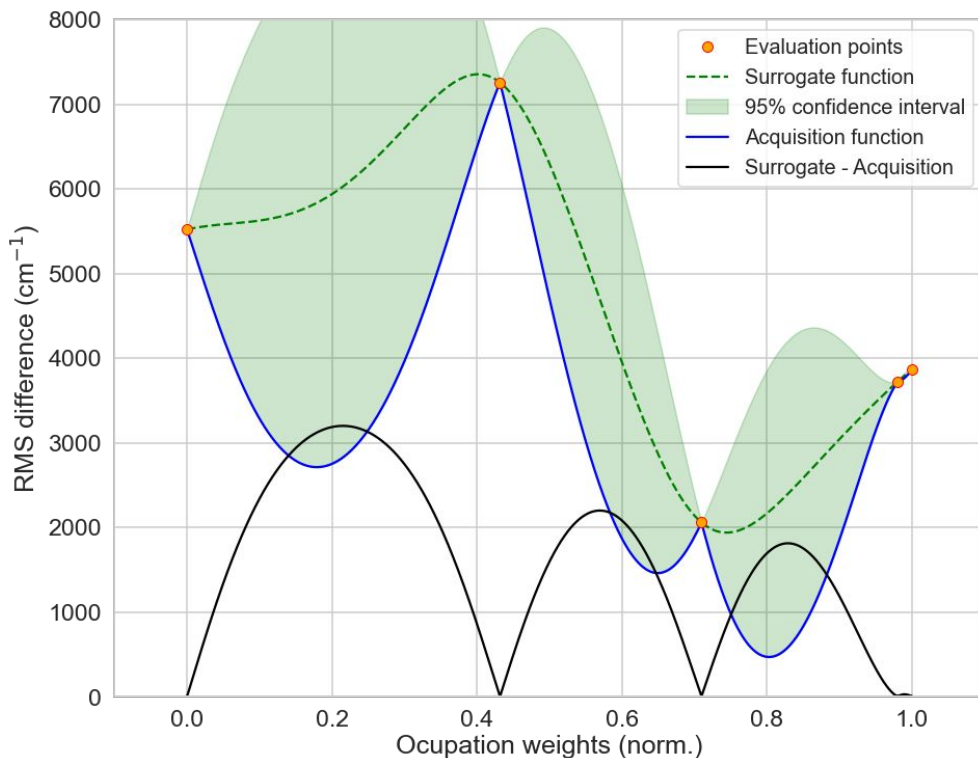
THANK YOU FOR YOUR  
ATTENTION!

# OPTIMIZATION PROCEDURE

1. Get a set of initial points
2. **Fit** a surrogate model for a specific loss function
3. Compute **acquisition function** - dynamically chosen between EI, PI and GP-UCB
4. Evaluate new point
5. Repeat 2. - 4. until convergence of loss function evaluation (exploitation) or chosen number of iterations (exploration)
6. **Make recommendation**



Sequential Model-Based Optimization  
(SMBO)



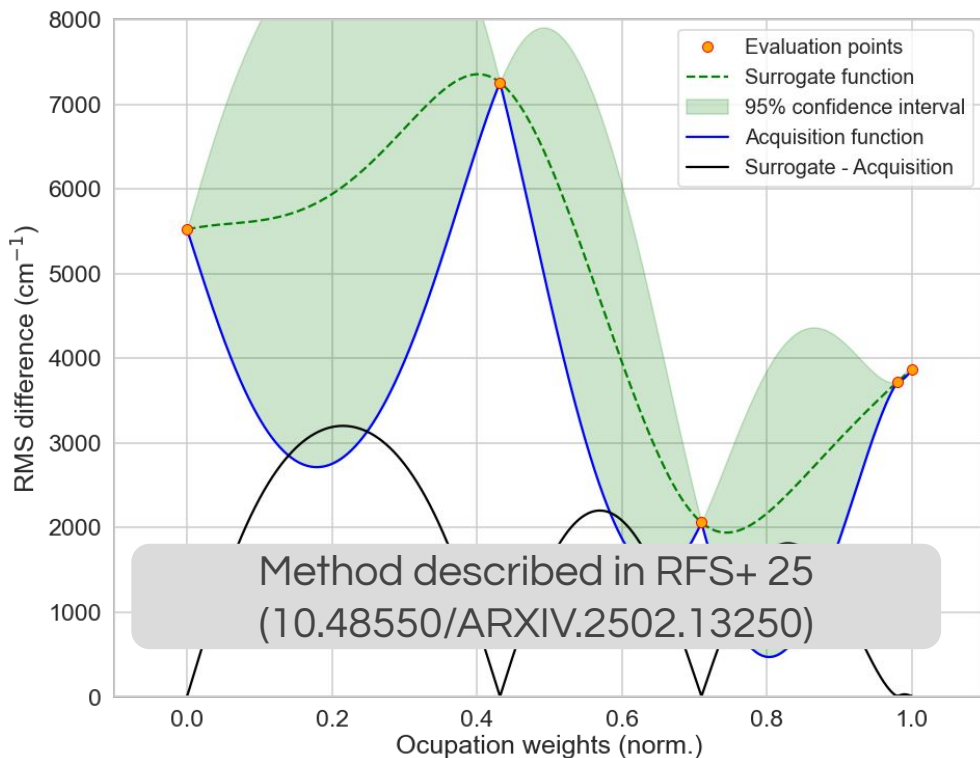
Example optimization for 1 parameter (4f)  
(5d, 6s, 6p) fixed at (0.357, 0.0714, 0.0714)

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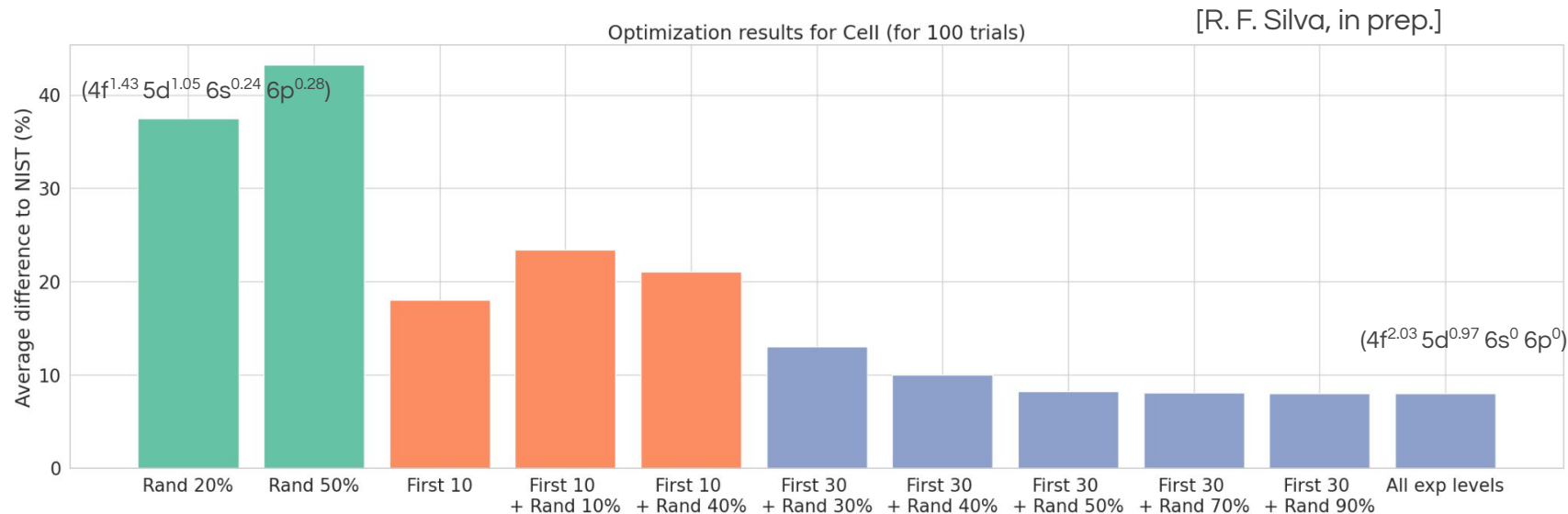
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Method described in RFS+ 25  
(10.48550/ARXIV.2502.13250)

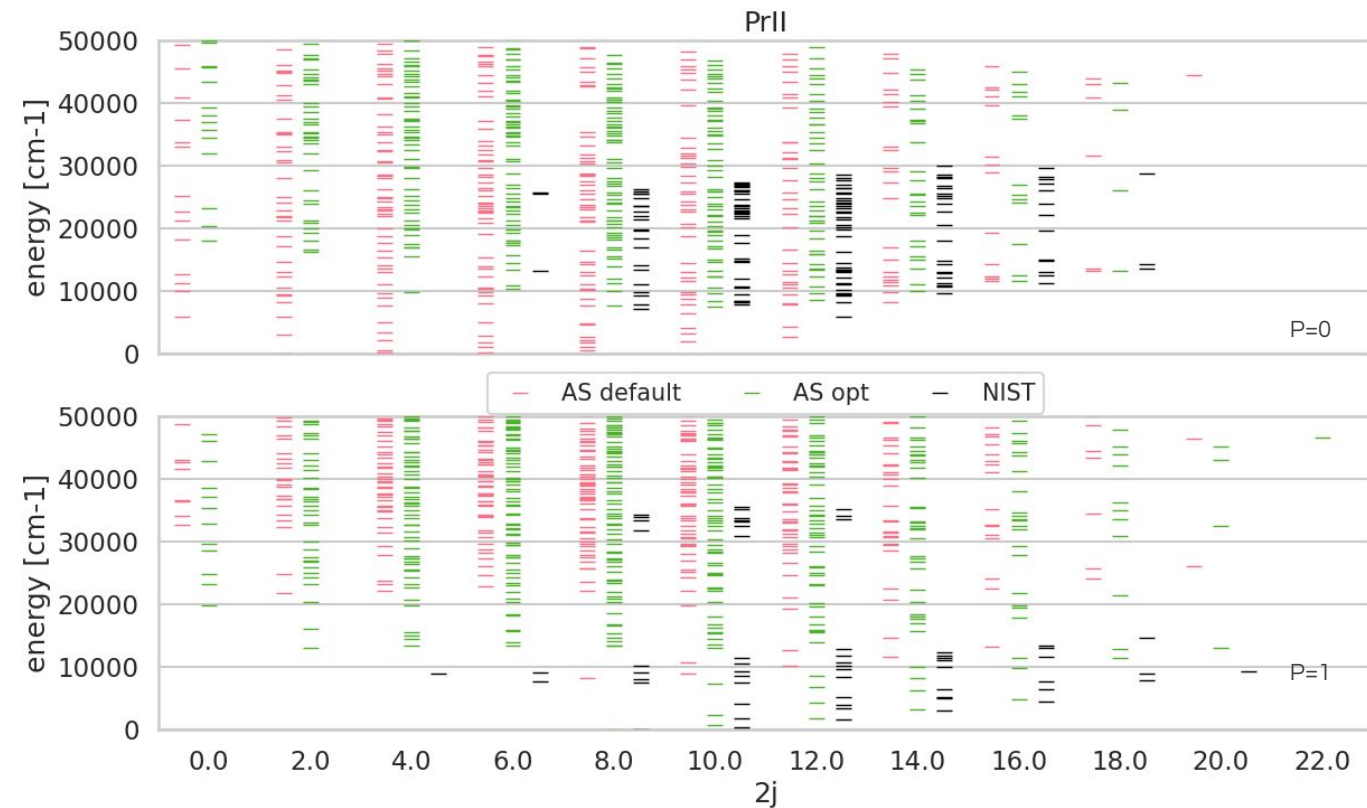
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# SENSITIVITY OF THE OPTIMIZATION



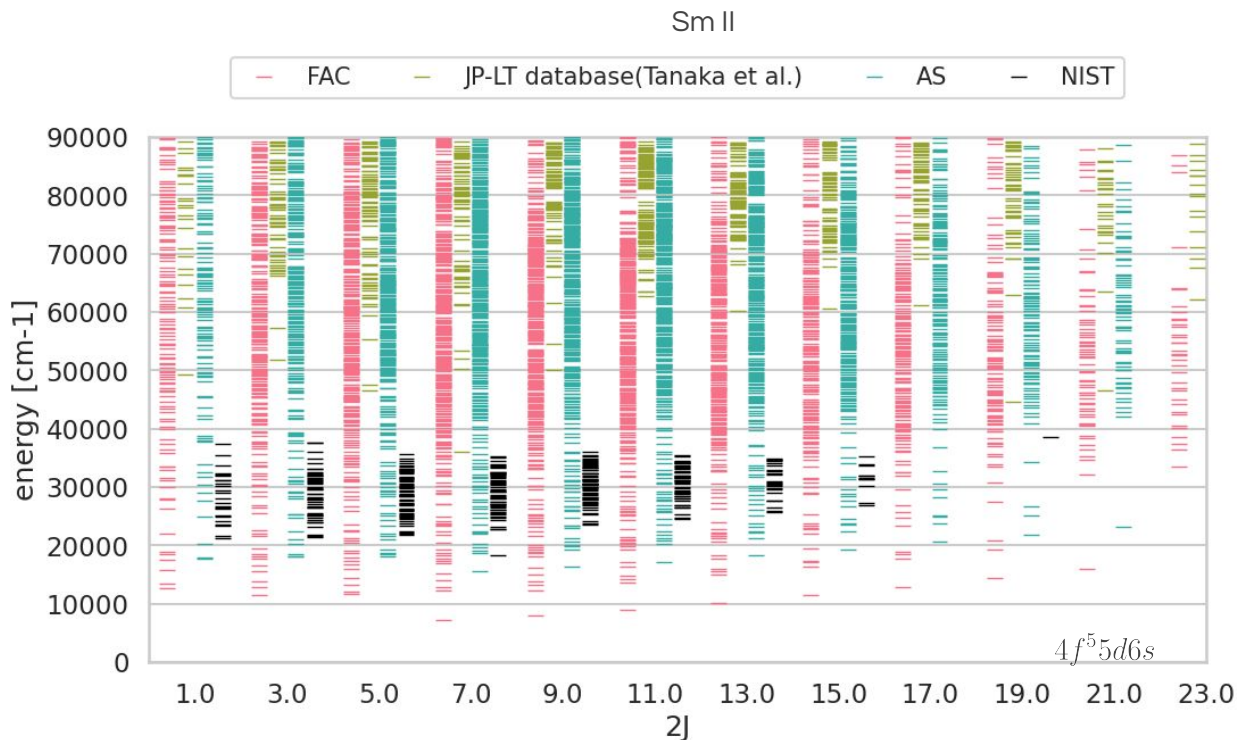
- Only very small changes to FMC after including more than 50% of the available data for Ce II - maintaining a relative accuracy of ~8%
- Close to ground state levels have the most impact (~10-30 levels)
- Provides confidence on it's predictive value for non-measured levels and robust to low amounts of data

# OPTIMIZATION IN AUTOSTRUCTURE

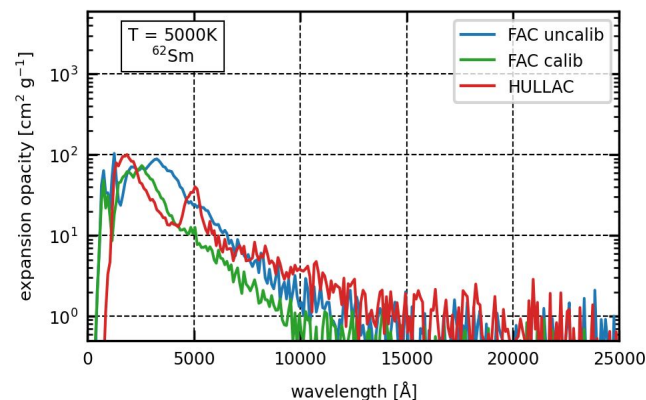


- Faster and better memory handling than FAC
- Not fully relativistic
- “AS default” uses one of multiple built in ways to optimize the potential - possible better result if tweaked
- **No extra input** needed in “AS opt” - optimization in this work

# ASSESSMENT OF ATOMIC DATA – ENERGY LEVELS

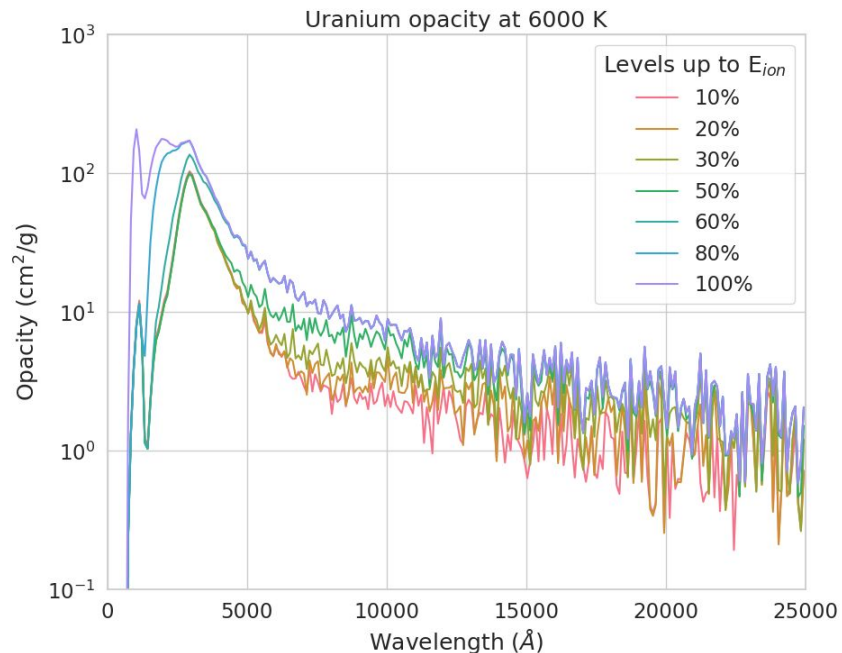


- Systematic discrepancy in  $4f^n5d6s$  configuration
- Consequence of local potential model(?)

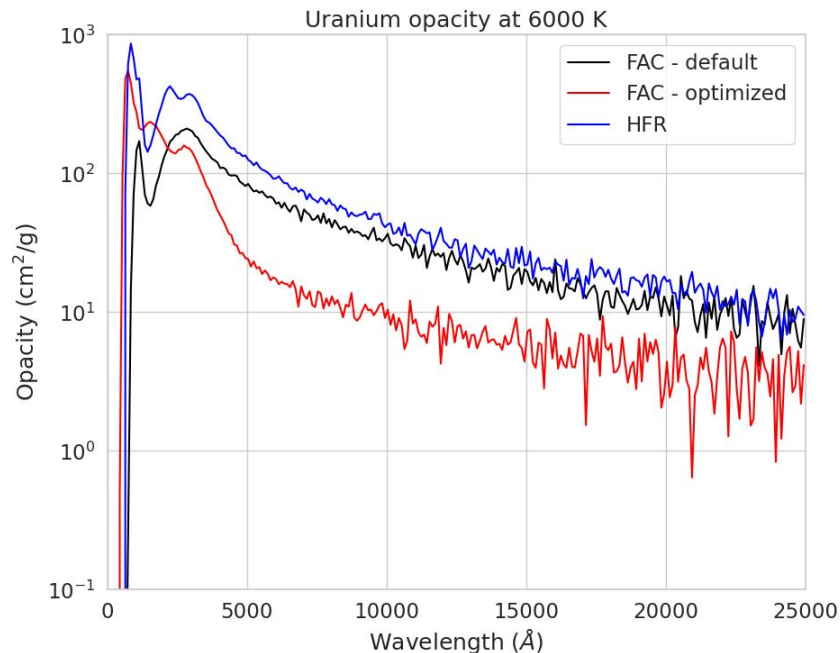


- Calibration to experimental data helps but is not sufficient
  - Lack of experimental data
  - Possibly inaccurate wavefunctions

# COMPLETENESS/ACCURACY DUALITY

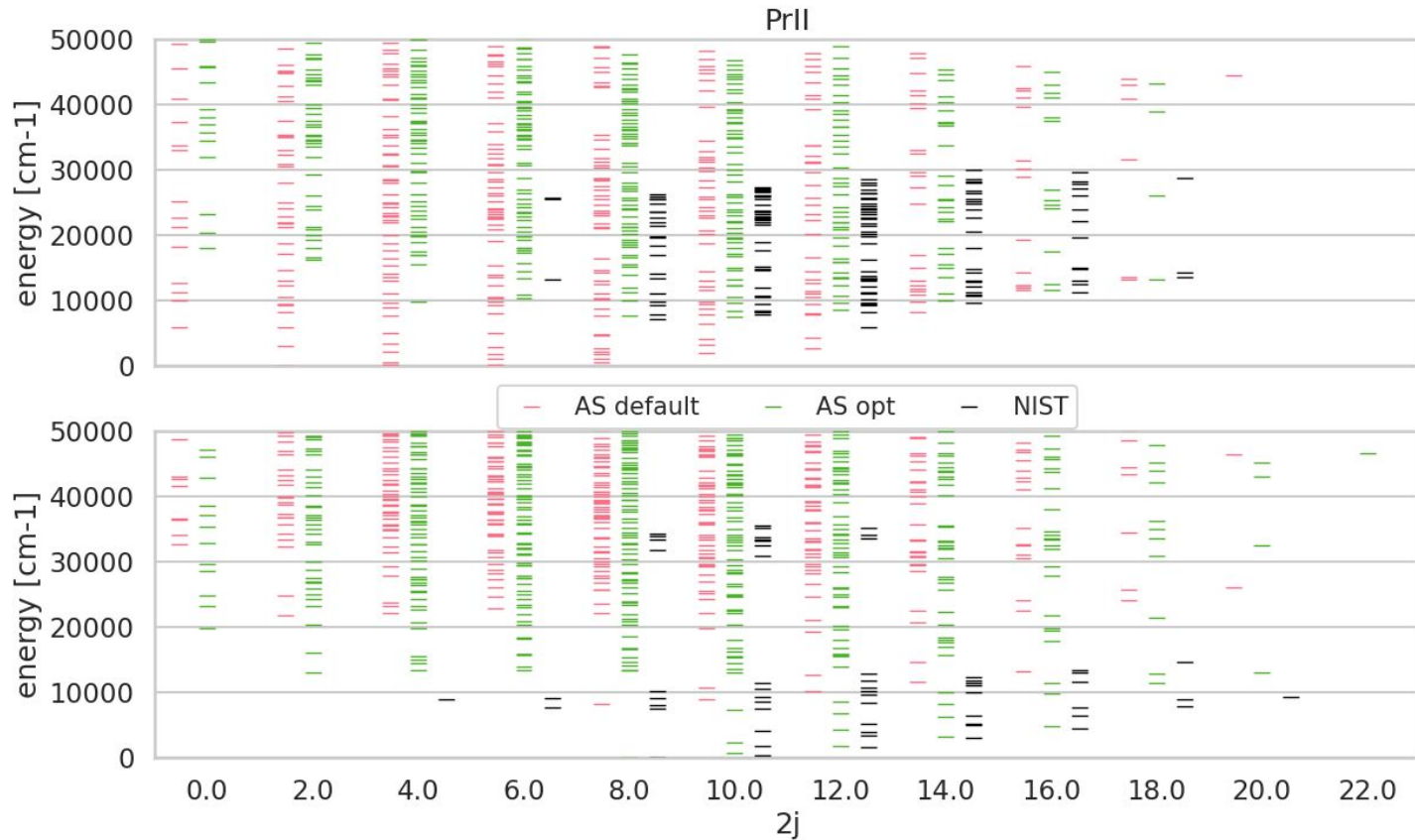


- Necessary to ensure convergence



- Differences in atomic data can have significant effect in opacity

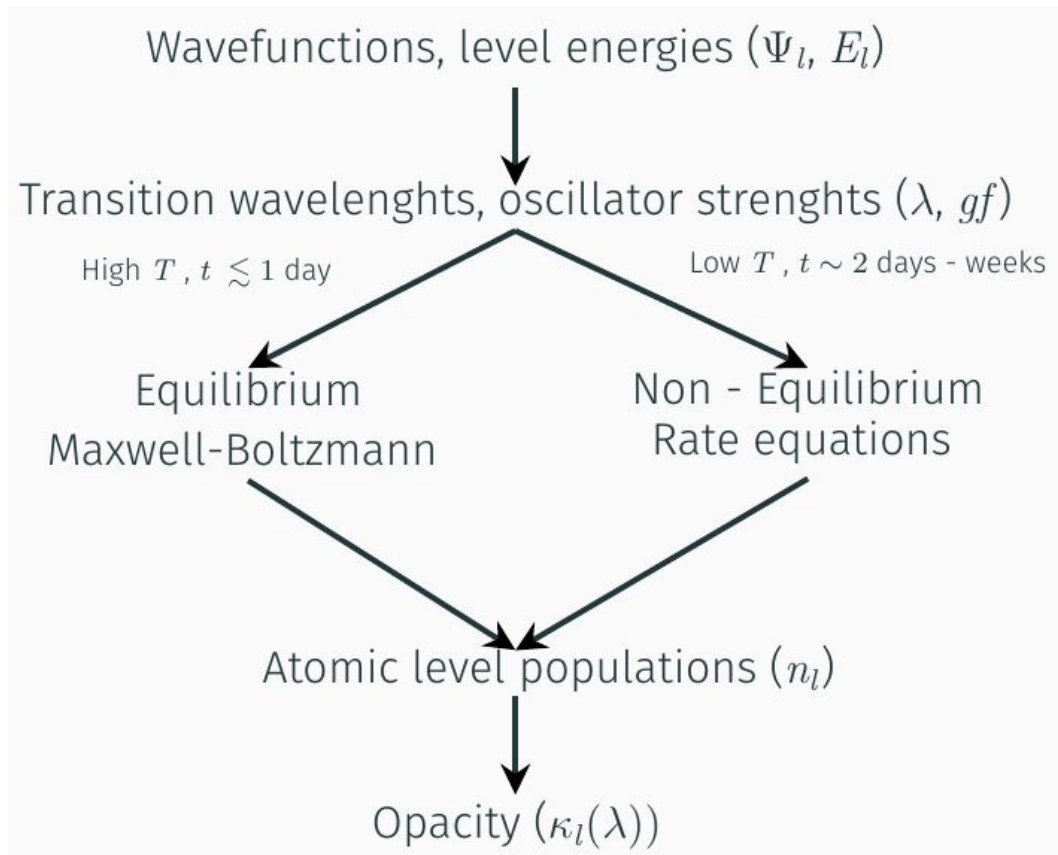
# OPTIMIZATION IN AUTOSTRUCTURE



- Faster and better memory handling than FAC - allows for larger computations, essential for CIE, PI and DR (active development by Prof. Nigel Badnel)
- Not fully relativistic
- “AS default” uses one of multiple built in ways to optimized the potential - possible better result if tweaked
- No extra input needed in “AS opt” - optimization in this work



# ROADMAP TO OPACITY



# ASSESSMENT OF ATOMIC DATA – TRANSITION RATES

