



UNIVERSITÀ  
DI TRENTO



# Neutrino reaction rates in BNS mergers

BNS\_NURATES: AN OPEN-SOURCE PERFORMANT LIBRARY

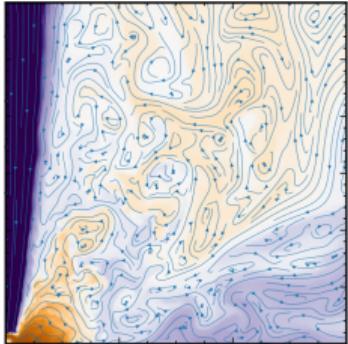
L. Chiesa, M. Bhattacharyya, F. Mazzini

**Federico Maria Guercilena**

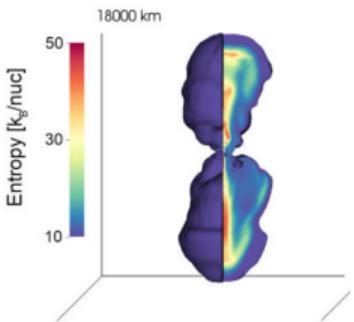
A. Perego, D. Radice

Phys. Rev. D 111, 063053 (2025)

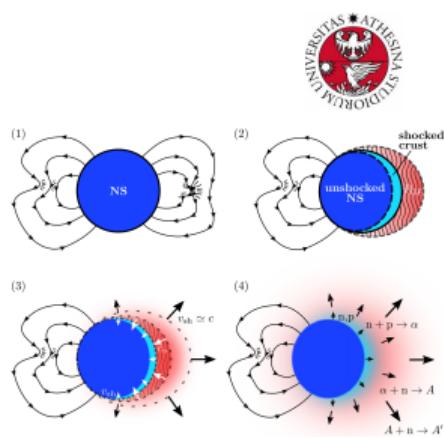
# R-PROCESS SITES AND ROLE OF NEUTRINOS



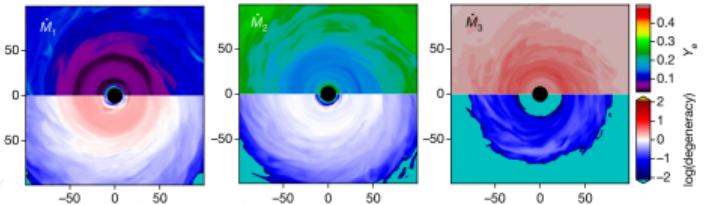
Accretion-induced collapse  
of WD [Cheong et al., 2025]



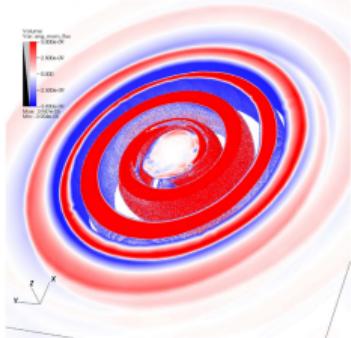
Magneto-rotational CCSne  
[Reichert et al., 2022]



Magnetar Giant Flares  
[Cehula et al., 2024]

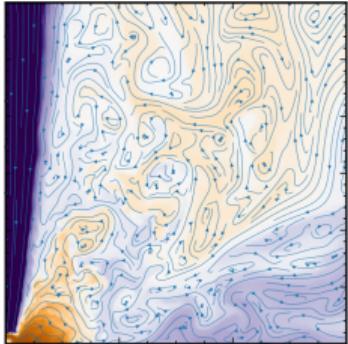


Collapsars [Siegel et al., 2019]

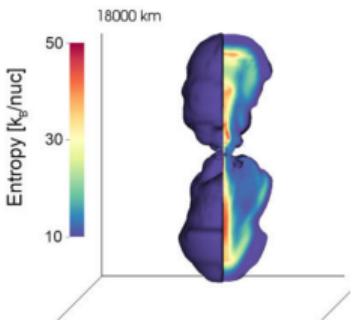


BNS mergers  
[Nedora et al., 2019]

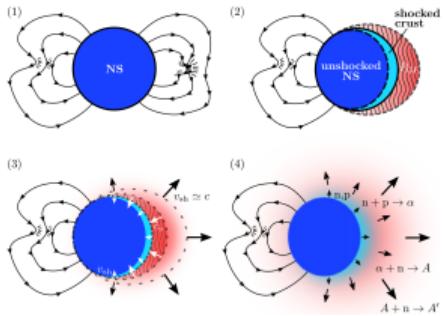
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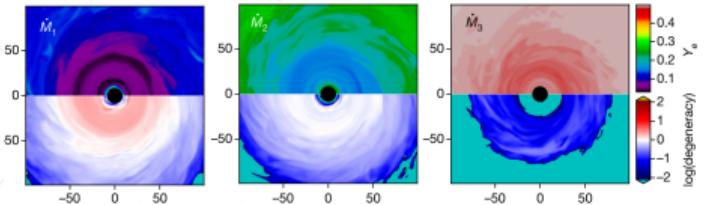
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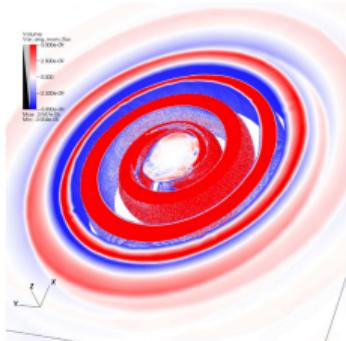


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$$\frac{\partial f}{\partial t} + \frac{\mathbf{p}}{m} \cdot \nabla f + \mathbf{F} \cdot \frac{\partial f}{\partial \mathbf{p}} = \left( \frac{\partial f}{\partial t} \right)_{\text{coll}}$$

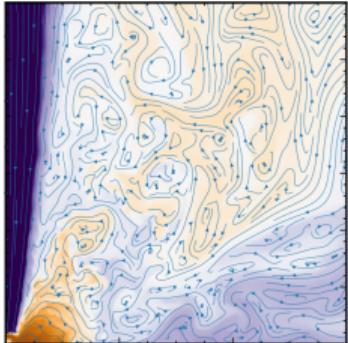
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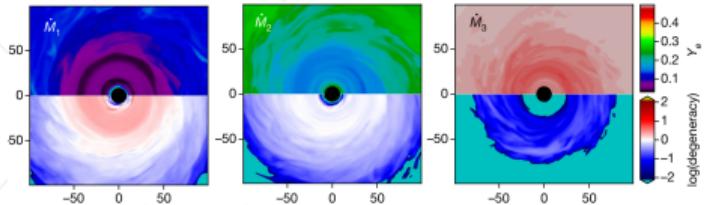
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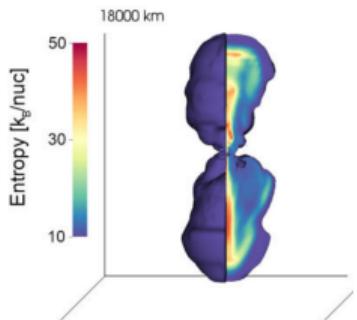
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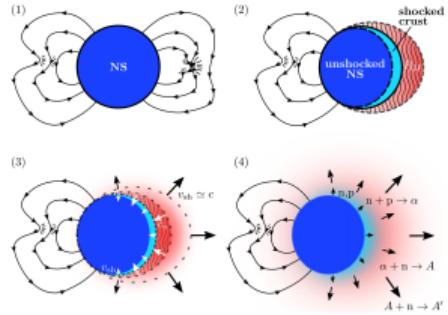
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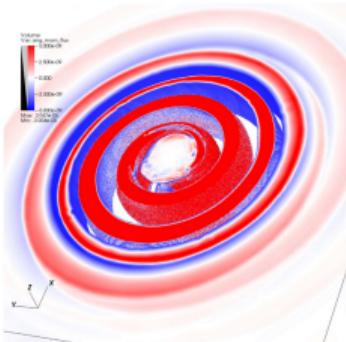


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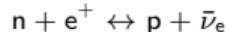
BNS mergers

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# THE BNS\_NURATES LIBRARY

## Monopole term of energy-dependent kernels

$\beta$  processes [Bruenn, 1985]



► weak-magnetism

[Horowitz, 2002]

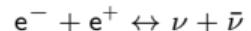
► in-medium effects

[Oertel et al., 2020]

► (inverse) nucleon decay

Electron/positron annihilation

[Pons et al., 1998]



Nucleon-nucleon Bremsstrahlung

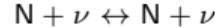
[Hannestad and Raffelt, 1998]



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[Fischer, 2016]

Elastic scattering on nucleons [Bruenn, 1985]

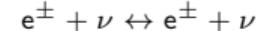


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Inelastic scattering on (anti-)electrons

[Mezzacappa and Bruenn, 1993]



### Gray emissivities/opacities

Integration of kernels with a highly tuned 1- and 2-dimensional custom Gauss-Legendre quadrature rule on a **generic neutrino distribution function**.

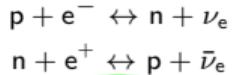
### Reconstruction of neutrino distribution

$f(\omega) = w_{\text{thick}} f_{\text{thick}}(\omega; a, b) + w_{\text{thin}} f_{\text{thin}}(\omega; c, d)$   
 with parameters and weights retrieved from neutrino number/energy densities and Eddington factors.

# THE BNS\_NURATES LIBRARY

## Monopole term of energy-dependent kernels

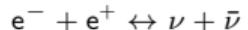
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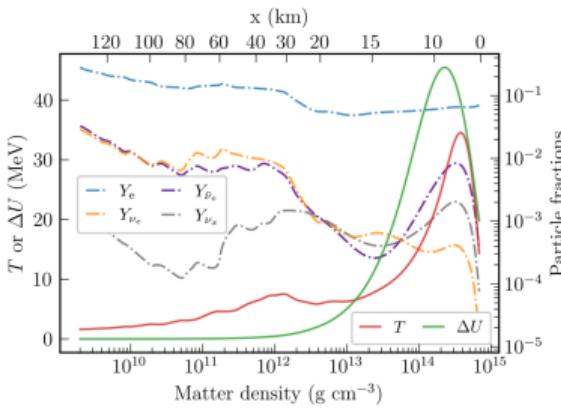
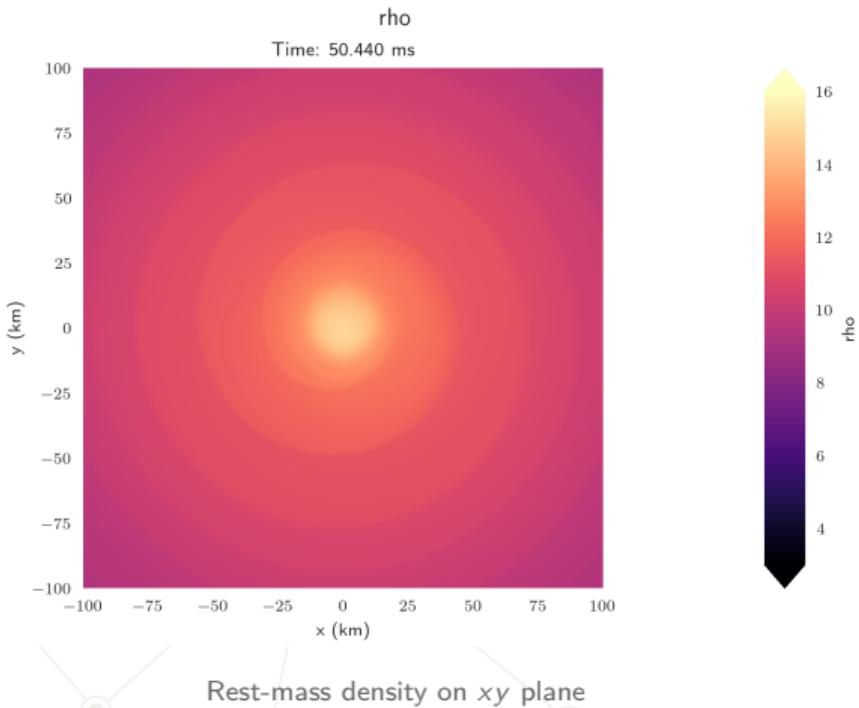
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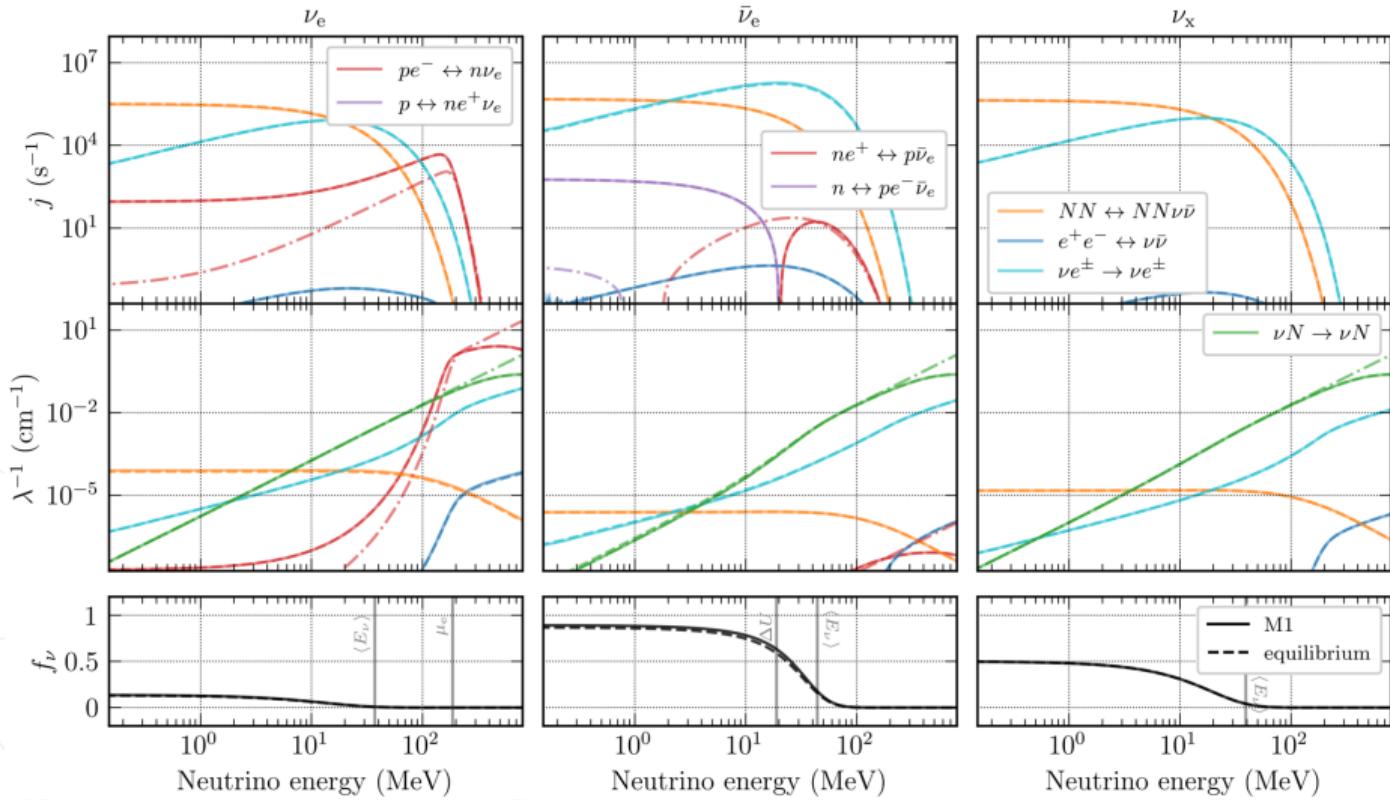
# REFERENCE SIMULATION

Equal-mass,  $M_{\text{NS}}=1.298 M_{\odot}$ , DD2 EOS

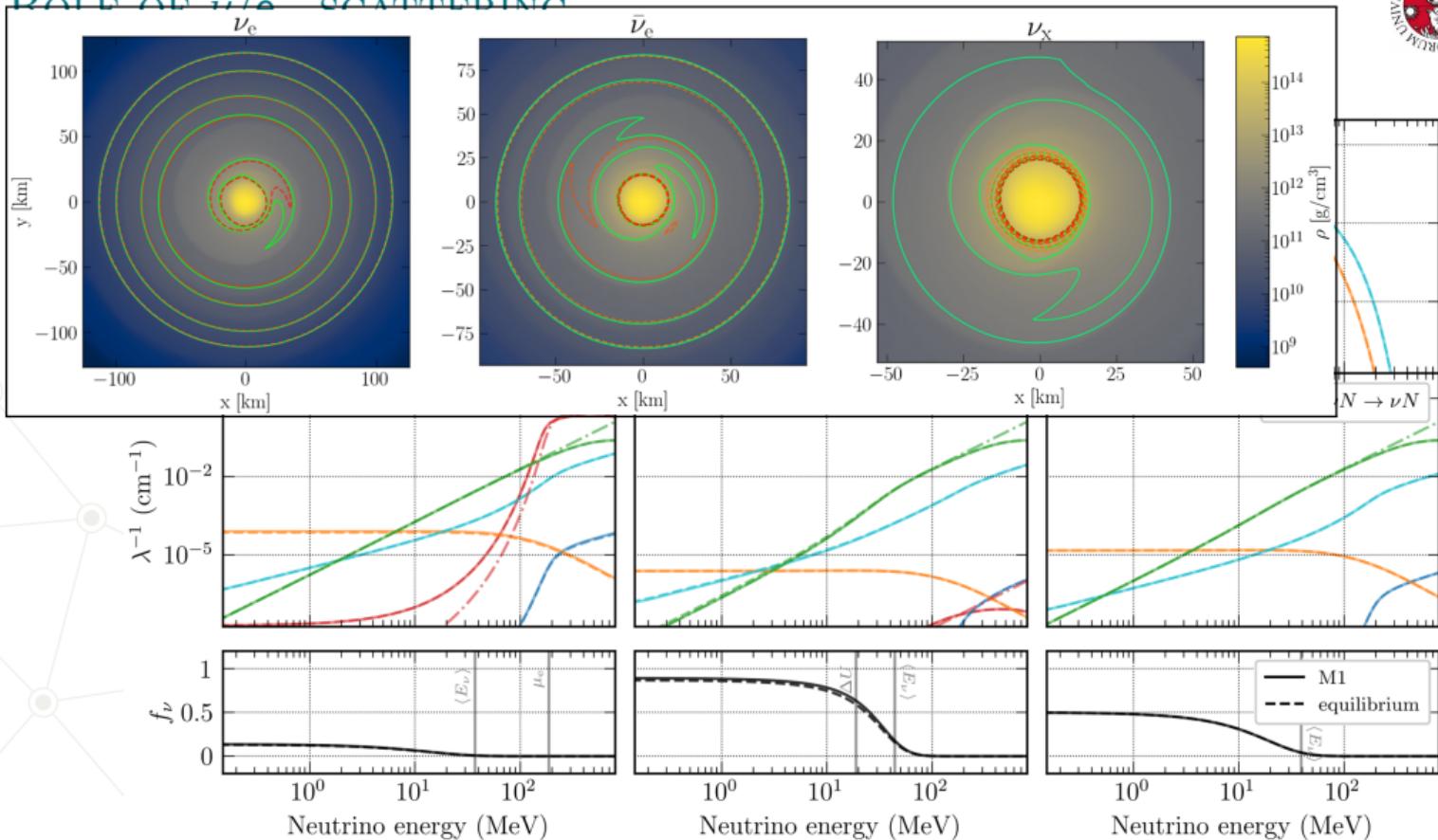


#	$\rho$ ( $\text{g}/\text{cm}^3$ )	$T$ (MeV)	$Y_e$
A	$6.90 \cdot 10^{14}$	12.39	0.07
B	$9.81 \cdot 10^{13}$	16.63	0.06
F	$1.01 \cdot 10^{10}$	2.17	0.19

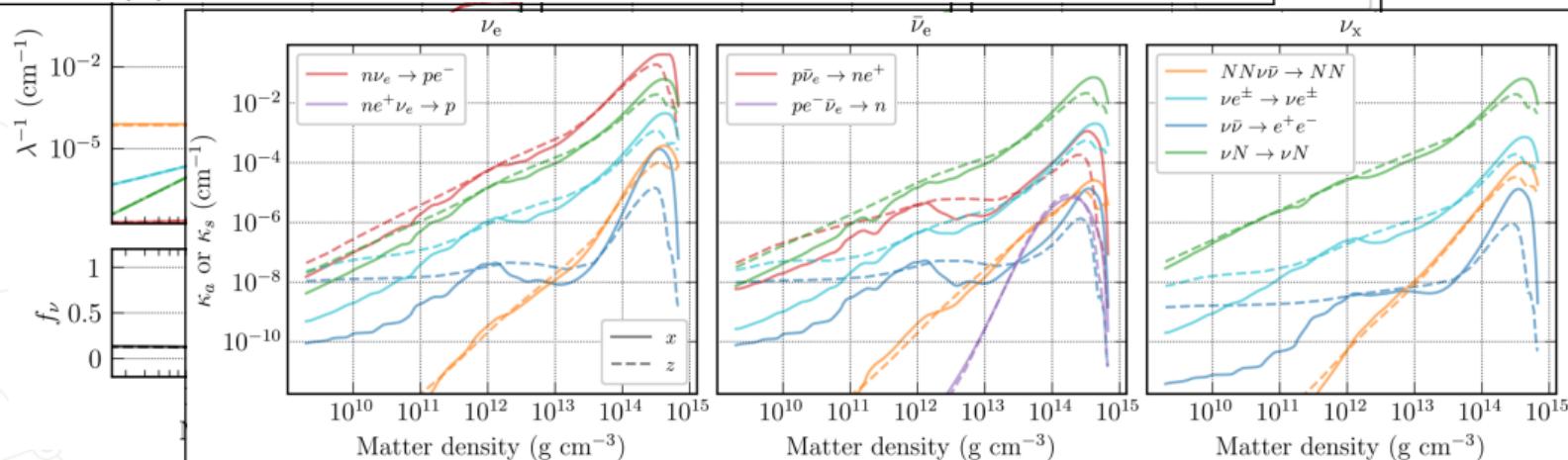
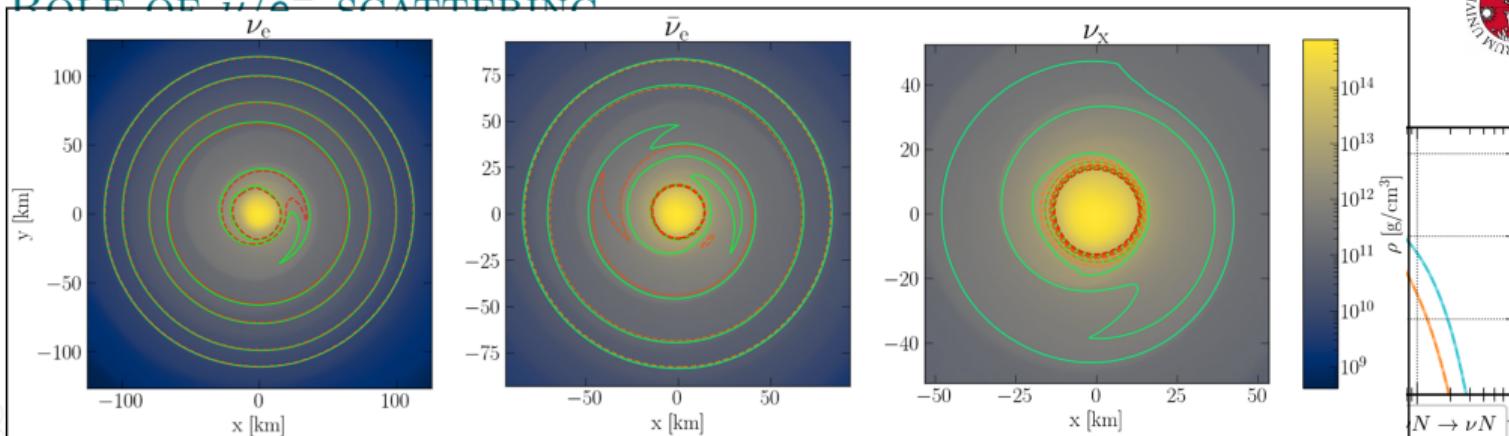
# ROLE OF $\nu/e^-$ SCATTERING



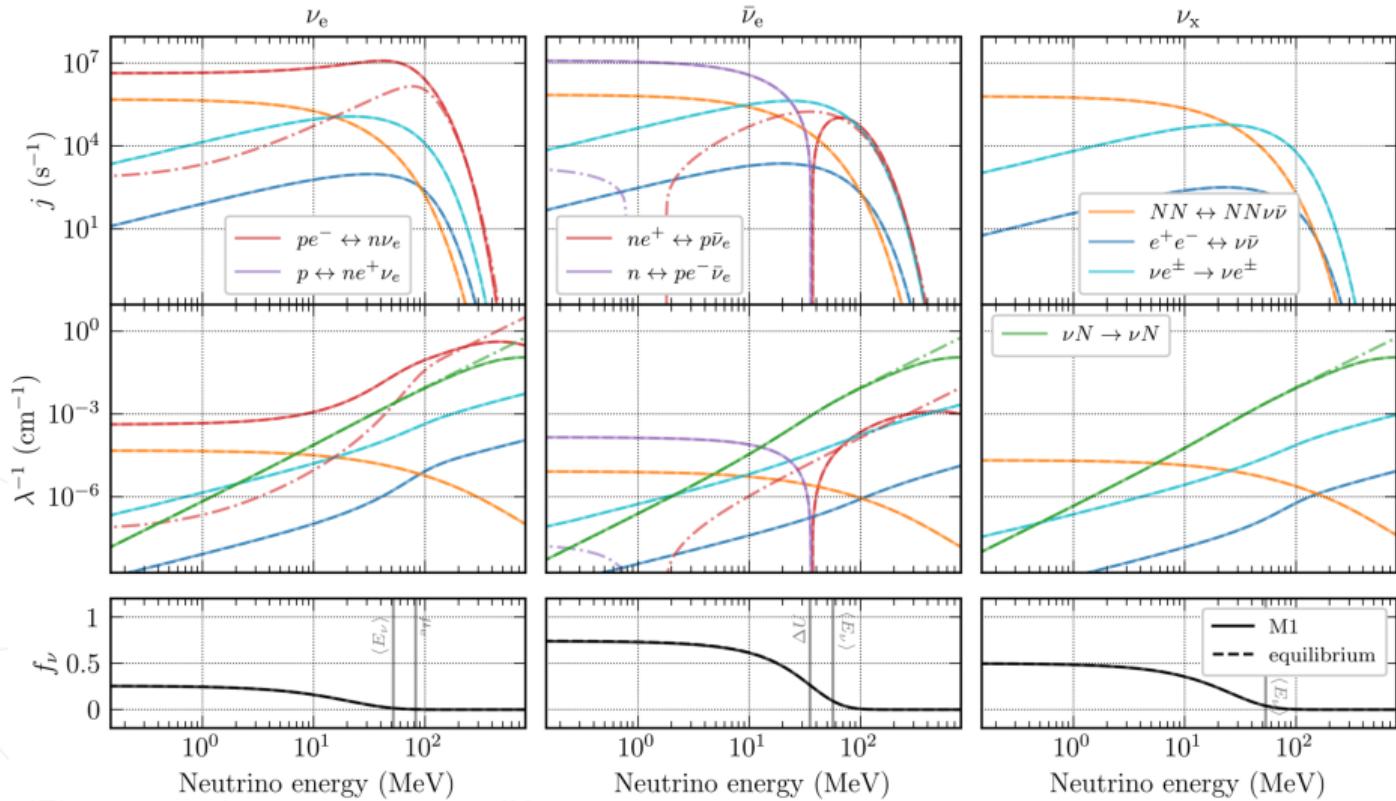
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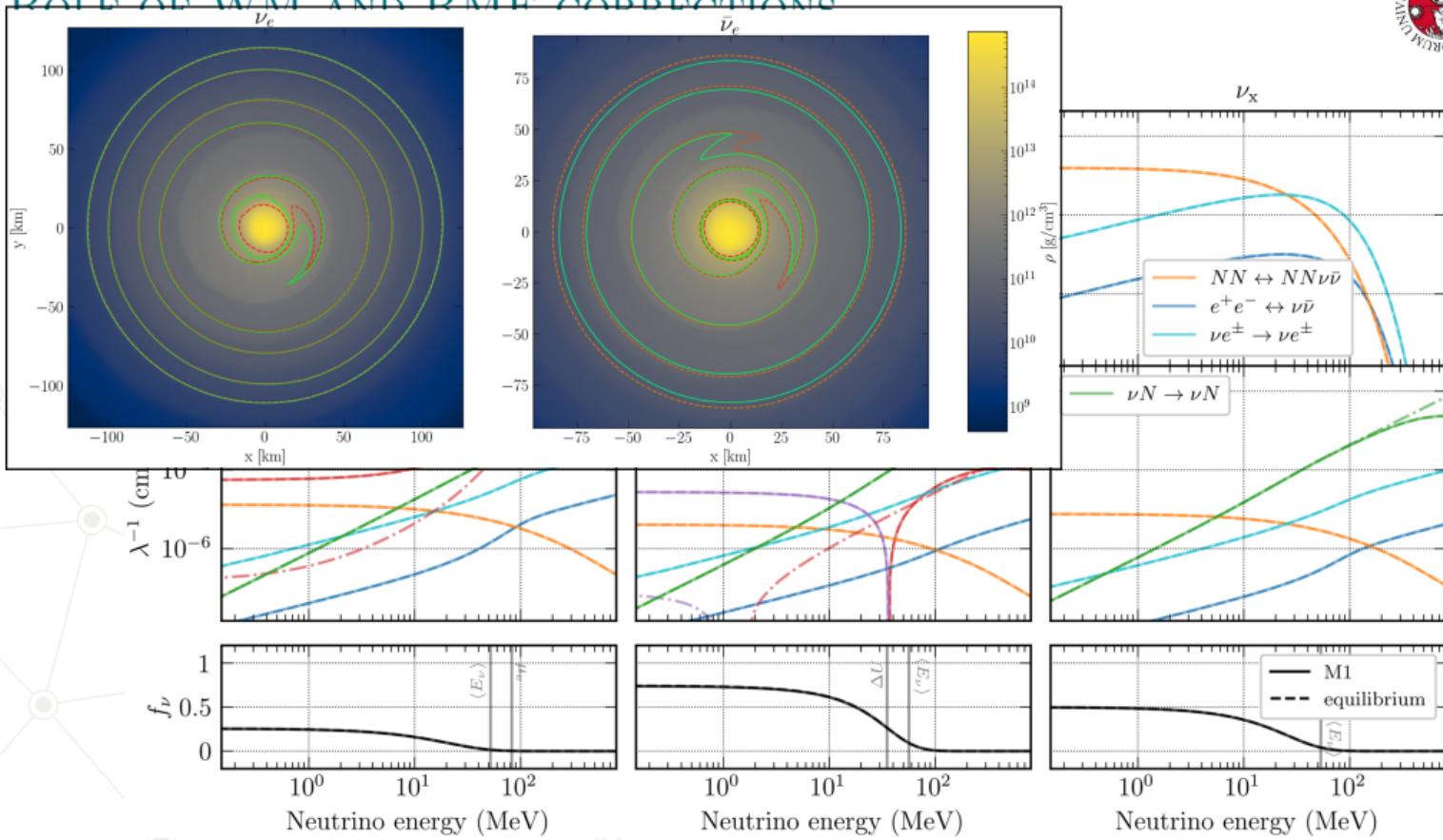
## ROLE OF $\nu/\bar{\nu}$ - SCATTERING



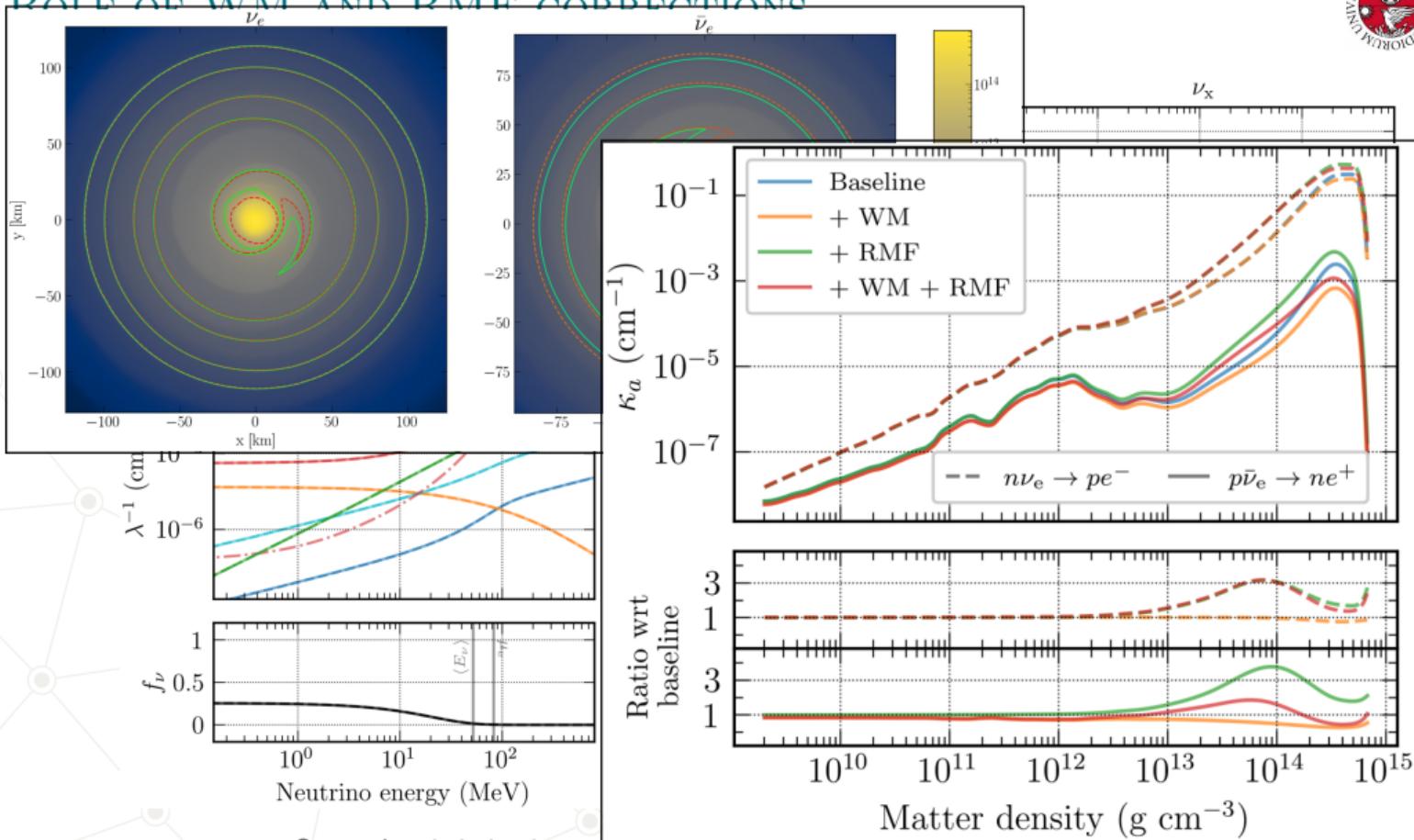
# ROLE OF WM AND RMF CORRECTIONS



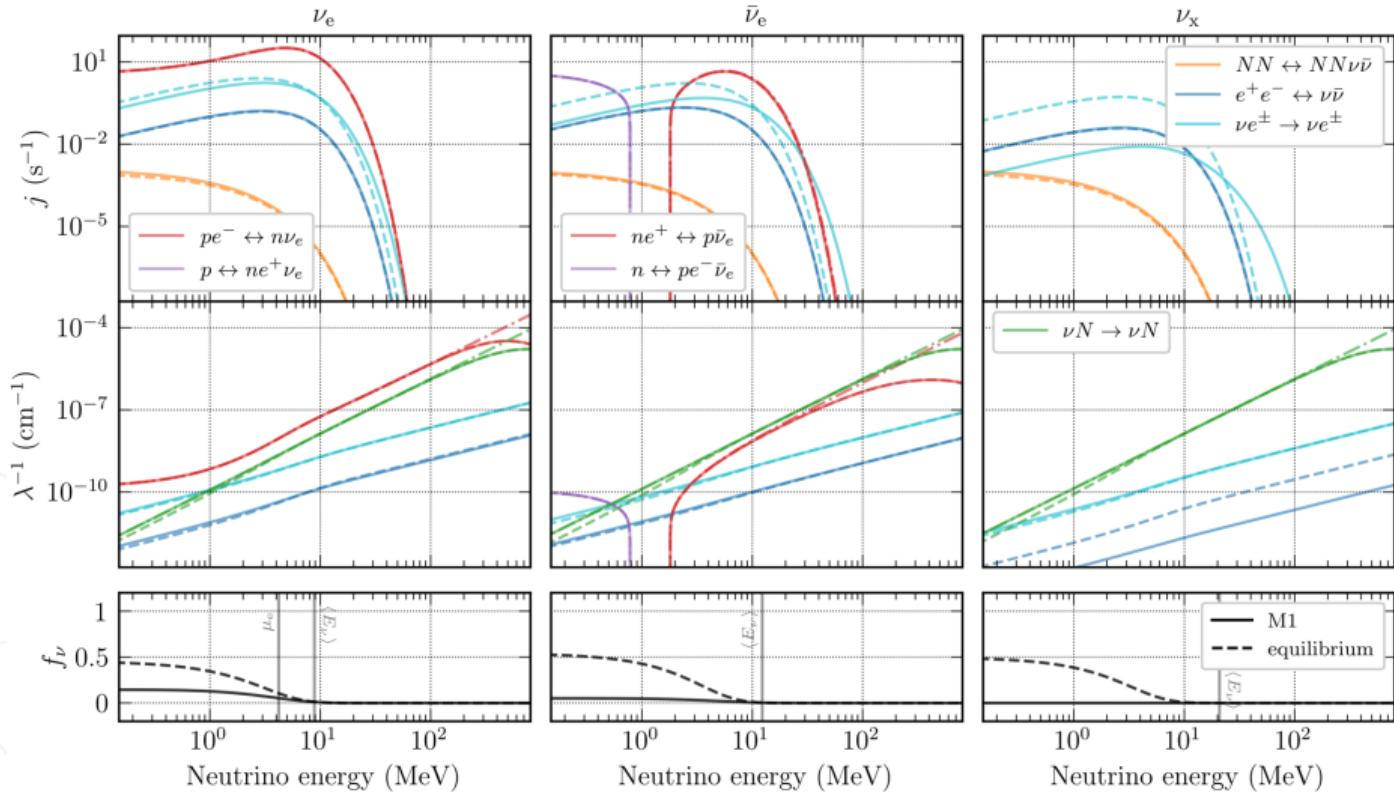
## ROLE OF WM AND RME CORRECTIONS



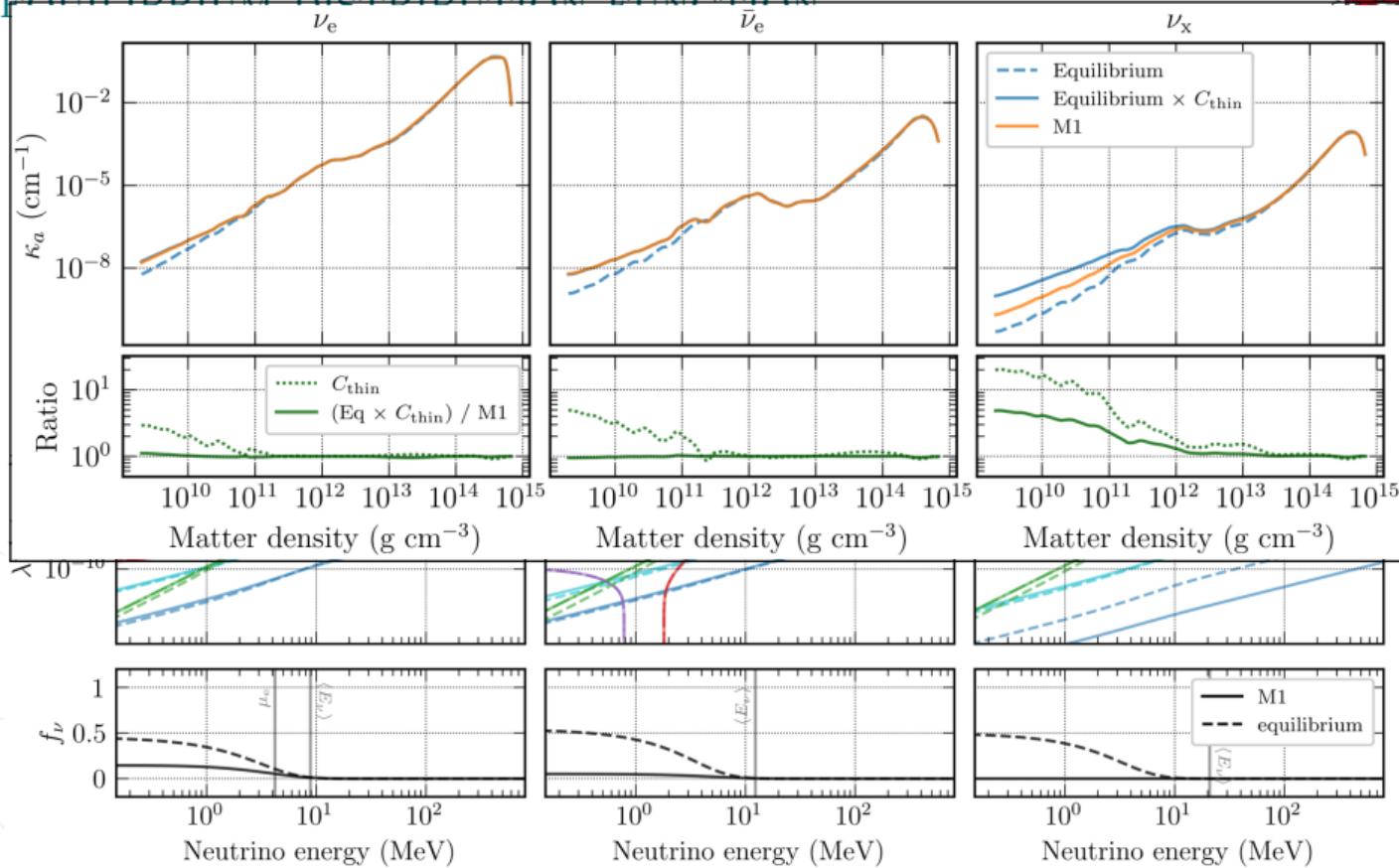
## ROLE OF WM AND RMF CORRECTIONS



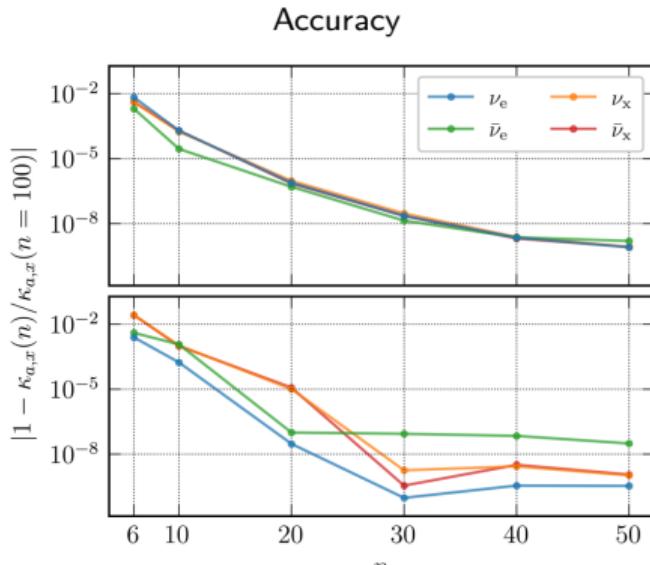
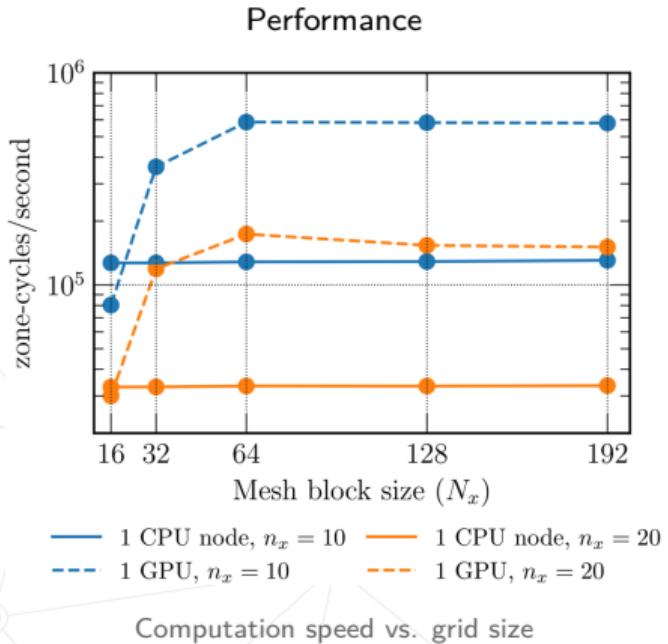
# NON-EQUILIBRIUM DISTRIBUTION FUNCTION



# NON-EQUILIBRIUM DISTRIBUTION FUNCTION



# NUMERICAL/COMPUTATIONAL CONSIDERATIONS

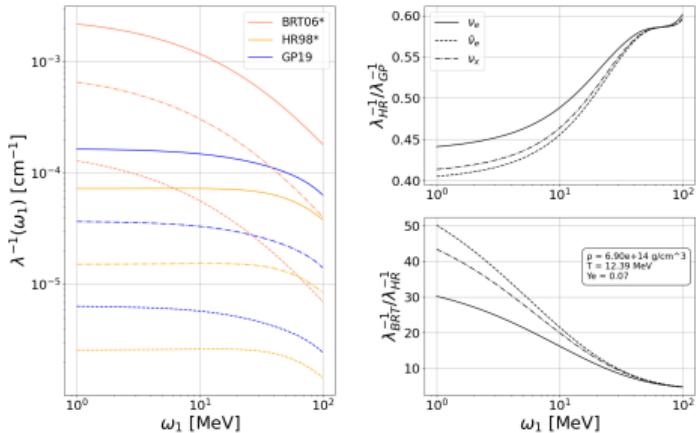


Accuracy vs. number of integration nodes.

Integration efforts into BNS evolution codes (WhiskyTHC, GR-Athena++, AthenaK) is ongoing and almost complete.

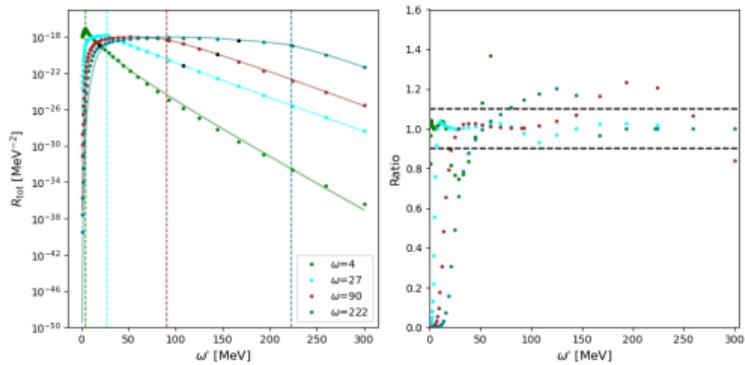
# ONGOING DEVELOPMENTS

Better nucleon-nucleon Bremsstrahlung via the T-matrix formalism [Guo and Martínez-Pinedo, 2019]



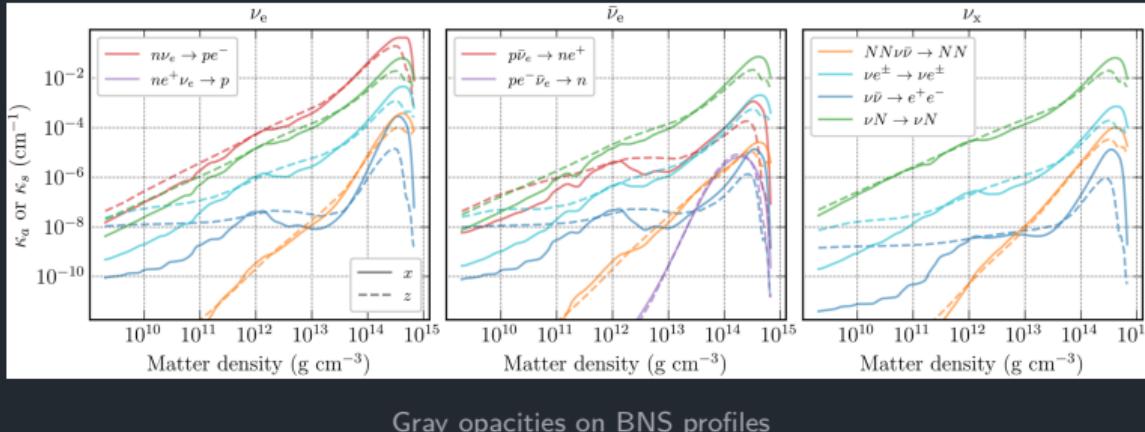
NN Bremsstrahlung opacity at point A (courtesy of Stefano Caldini).

Extension to scattering on *massive* leptons (muons)



$\mu/\nu$  scattering kernel at  $T = 11$  MeV and  $\mu_\mu = 157$  MeV as function of outgoing neutrino energy (courtesy of Raffaele Ferrari).

# CONCLUSIONS

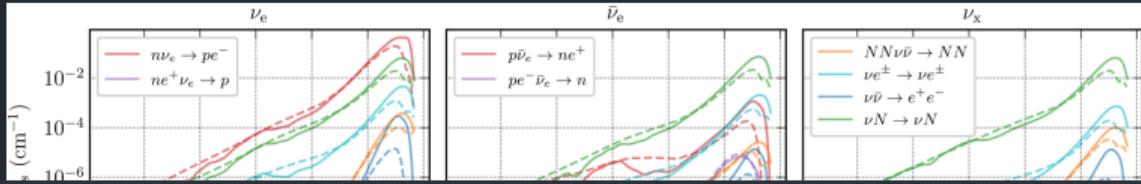


Reliable modelling of neutrino dynamics in BNS mergers requires a realistic yet performing treatment of their reactions. BNS\_NURATES offers:

- ▶ Representative and growing set of  $\nu$  reactions
- ▶ State of the art correction terms
- ▶ Reconstruction of the  $\nu$  distribution
- ▶ Clean, well tested and preforming implementation

First simulations exploiting it are coming soon, so ...

# CONCLUSIONS



## References

L. Chiesa, M. Bhattacharyya, F. Mazzini, F. M. Guercilena, A. Perego, D. Radice, Phys. Rev. D 111, 063053 (March 2025)

[https://github.com/RelNucAs/bns\\_nurates](https://github.com/RelNucAs/bns_nurates)

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## REFERENCES

# REFERENCES I

- [Bruenn, 1985] Bruenn, S. W. (1985).  
Stellar core collapse - Numerical model and infall epoch.  
*ApJS*, 58:771.
- [Cehula et al., 2024] Cehula, J., Thompson, T. A., and Metzger, B. D. (2024).  
Dynamics of baryon ejection in magnetar giant flares: implications for radio afterglows,  $r$ -process nucleosynthesis, and fast radio bursts.  
*Monthly Notices of the Royal Astronomical Society*, 528(3):5323–5345.
- [Cheong et al., 2025] Cheong, P. C.-K., Pitik, T., Longo Micchi, L. F., and Radice, D. (2025).  
Gamma-Ray Bursts and Kilonovae from the Accretion-induced Collapse of White Dwarfs.  
*ApJL*, 978(2):L38.
- [Fischer, 2016] Fischer, T. (2016).  
The role of medium modifications for neutrino-pair processes from nucleon-nucleon bremsstrahlung: Impact on the protoneutron star deleptonization.  
*A&A*, 593:A103.

## REFERENCES II

- [Guo and Martínez-Pinedo, 2019] Guo, G. and Martínez-Pinedo, G. (2019).  
Chiral Effective Field Theory Description of Neutrino Nucleon–Nucleon Bremsstrahlung in Supernova Matter.  
*ApJ*, 887(1):58.
- [Hannestad and Raffelt, 1998] Hannestad, S. and Raffelt, G. (1998).  
Supernova Neutrino Opacity from Nucleon-Nucleon Bremsstrahlung and Related Processes.  
*ApJ*, 507(1):339–352.
- [Horowitz, 2002] Horowitz, C. J. (2002).  
Weak magnetism for antineutrinos in supernovae.  
*Phys. Rev. D*, 65(4):043001.
- [Mezzacappa and Bruenn, 1993] Mezzacappa, A. and Bruenn, S. W. (1993).  
Stellar core collapse - A Boltzmann treatment of neutrino-electron scattering.  
*ApJ*, 410:740.
- [Nedora et al., 2019] Nedora, V., Bernuzzi, S., Radice, D., Perego, A., Endrizzi, A., and Ortiz, N. (2019).  
Spiral-wave Wind for the Blue Kilonova.  
*ApJL*, 886(2):L30.

## REFERENCES III

- [Oertel et al., 2020] Oertel, M., Pascal, A., Mancini, M., and Novak, J. (2020).  
Improved neutrino-nucleon interactions in dense and hot matter for numerical simulations.  
*Phys. Rev. C*, 102(3):035802.
- [Pons et al., 1998] Pons, J. A., Miralles, J. A., and Ma Ibáñez, J. (1998).  
Legendre expansion of the  $\vec{\nu}$  kernel: Influence of high order terms.  
*Astron. Astrophys. Suppl. Ser.*, 129(2):343–351.
- [Reichert et al., 2022] Reichert, M., Obergaulinger, M., Aloy, M. A., Gabler, M., Arcones, A., and Thielemann, F. K. (2022).  
Magnetorotational supernovae: a nucleosynthetic analysis of sophisticated 3D models.  
*Monthly Notices of the Royal Astronomical Society*, 518(1):1557–1583.
- [Siegel et al., 2019] Siegel, D. M., Barnes, J., and Metzger, B. D. (2019).  
Collapsars as a major source of r-process elements.  
*Nature*, 569(7755):241–244.