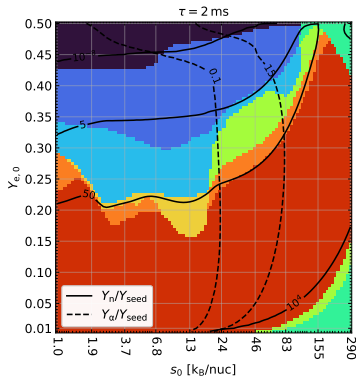


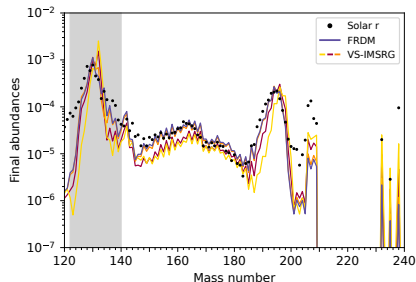
ASTROPHYSICAL AND NUCLEAR UNCERTAINTIES OF THE R-PROCESS



June 13th, 2025

Jan Kuske
(TU Darmstadt)

with:
Almudena Arcones
Takayuki Miyagi
Moritz Reichert
Achim Schwenk

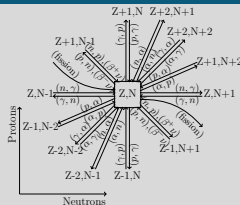


Ingredients

$$\frac{dY_i(t)}{dt} = \sum_j N_j^i \lambda_j Y_j \quad (\text{one-body})$$

$$+ \sum_{j,k} \frac{N_{j,k}^j}{1 + \delta_{jk}} \rho N_A \langle \sigma v \rangle_{j,k} Y_j Y_k \quad (\text{two-body})$$

$$+ \sum_{j,k,l} \frac{N_{j,k,l}^j}{1 + \Delta_{jkl}} \rho^2 N_A^2 \langle \sigma v \rangle_{j,k,l} Y_j Y_k Y_l \quad (\text{three-body})$$



r-Process Calculations

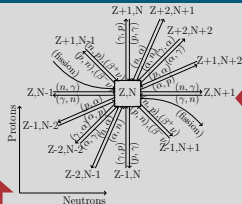
Ingredients

Reaction network code (WINNET)

$$\frac{dY_i(t)}{dt} = \sum_j N_j^i \lambda_j Y_j \quad (\text{one-body})$$

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Nuclear inputs

- masses
- reaction rates
- β -decays
- fission
- ...

Astrophysical inputs

- $\rho(t)$, $T(t)$, $Y_e(t)$, $s(t)$, ... $\rightarrow$ Lagrangian tracers from hydrodynamical simulations or **parametric models**
- + most realistic
 - extremely computationally expensive
 - important physics still unclear: nuclear EOS, neutrino interactions, progenitors, ...
- not only realistic conditions
- + computationally cheap
- + systematic variation of conditions possible
 - $\Rightarrow$ nuclear sensitivity studies

r-Process Calculations

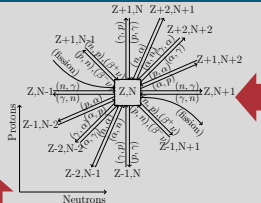
Ingredients

Reaction network code (WINNET)

$$\frac{dY_i(t)}{dt} = \sum_j N_j^i \lambda_j Y_j \quad (\text{one-body})$$

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$$+ \sum_{j,k,l} \frac{N_{j,k,l}^i}{1 + \Delta_{jkl}} \rho^2 N_A^2 \langle \sigma v \rangle_{j,k,l} Y_j Y_k Y_l \quad (\text{three-body})$$



Nuclear inputs

Part II

- masses
- reaction rates
- β -decays
- fission
- ...

Astrophysical inputs

Part I

- $\rho(t), T(t), Y_e(t), s(t), \dots \rightarrow$ Lagrangian tracers from hydrodynamical simulations or **parametric models**
- + most realistic
 - extremely computationally expensive
 - important physics still unclear: nuclear EOS, neutrino interactions, progenitors, ...
- not only realistic conditions
- + computationally cheap
- + systematic variation of conditions possible $\Rightarrow$ nuclear sensitivity studies

Part I - Astrophysical Uncertainties

**Complete survey of r-process
conditions**

Model for Astrophysical Conditions

based on J. Lippuner & L. Roberts, ApJ 815 82 (2015)

see also: R. Hoffman, S. Woosley & Y.-Z. Qian, ApJ 482 951 (1997)

B. S. Meyer & J. S. Brown, ApJS 112 199 (1997)

C. Freiburghaus, J. Rembges, T. Rauscher et al., ApJ, 516 381 (1999)

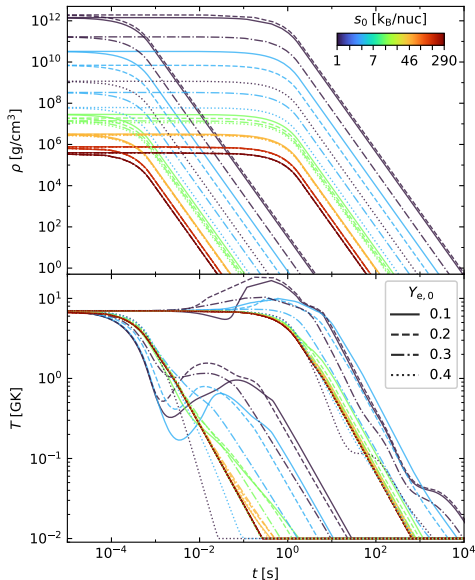
- 3 parameters: $\left. \begin{matrix} Y_{e,0} \\ s_0 \\ \tau \end{matrix} \right\} T_0 = 7 \text{ GK} \Rightarrow \rho_0$

- density evolution:

$$\rho(t) = \rho_0 \begin{cases} \exp\left(-\frac{t}{\tau}\right) & \text{if } t \leq 3\tau \\ \left(\frac{3\tau}{et}\right)^3 & \text{if } t \geq 3\tau \end{cases}$$

- adiabatic expansion + nuclear energy generation
- parameter space: $100 \times Y_{e,0}, 100 \times s_0, 12 \times \tau$

$\Rightarrow$ **120 000 total conditions**



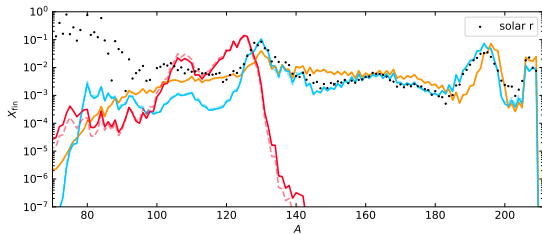
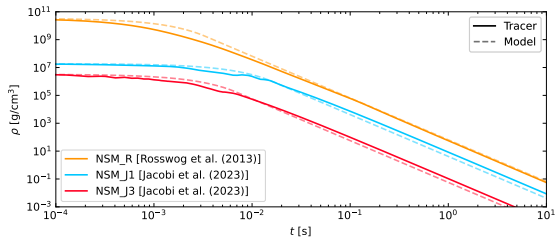
Comparison to Trajectories

From Hydrodynamical Simulations

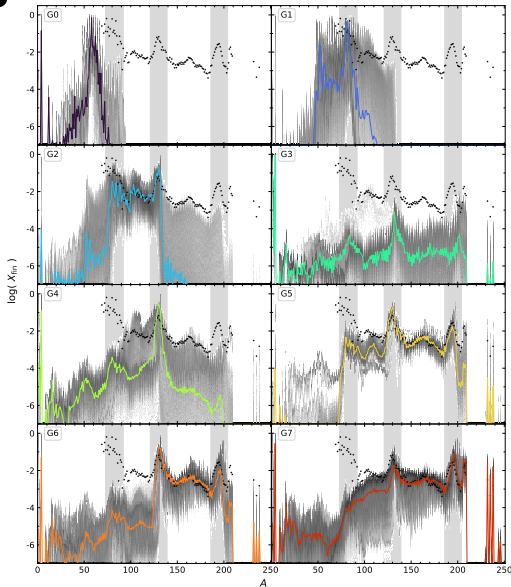
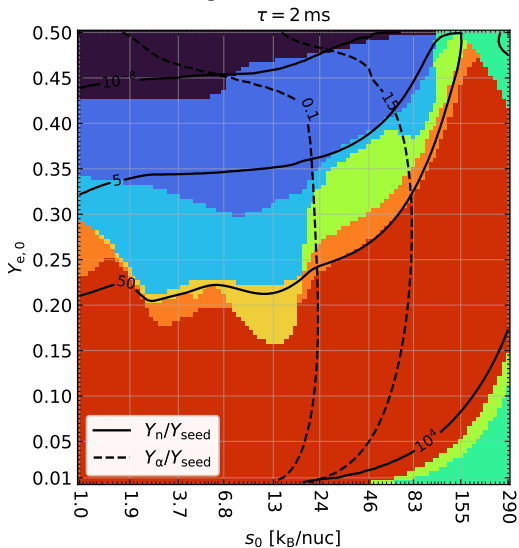
- 22 models of different astrophysical sites with up to 100 trajectories each
- map trajectories to parameter space:

$$\left. \begin{array}{l} Y_{e,0} \\ s_0 \end{array} \right\} \Rightarrow \text{from interpolation to 7 GK}$$
$$\tau \Rightarrow \text{from fit to density profile}$$

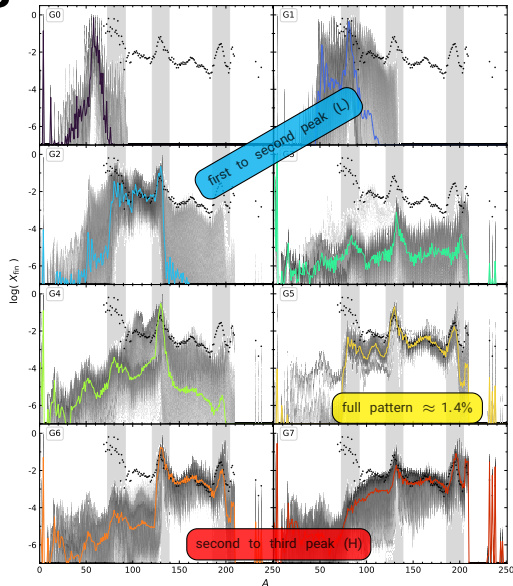
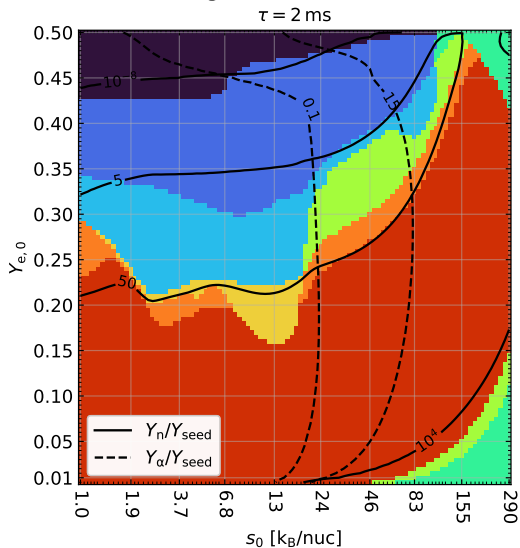
- good agreement** for $\approx 98\%$ of trajectories



Nucleosynthesis Groups

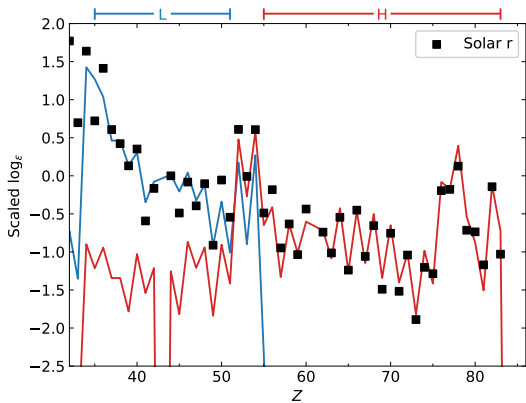


Nucleosynthesis Groups



Comparison to Solar

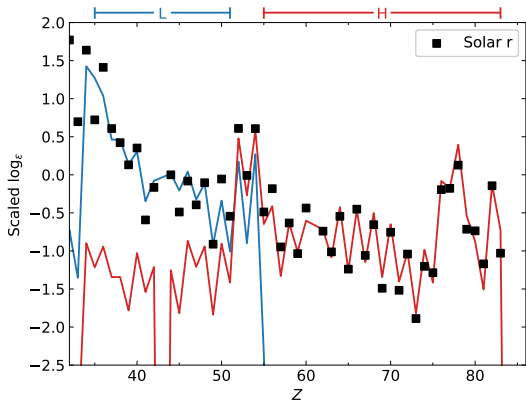
2 Component Model: L + H



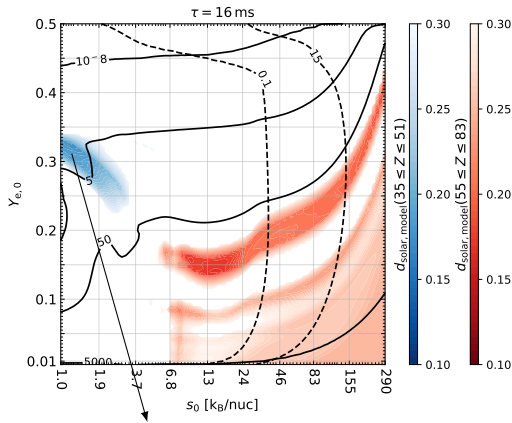
$$d = \frac{1}{\Delta Z} \sum_Z |\log(X_{\text{solar}}(Z)) - \log(X_{\text{model}}(Z))|$$

Comparison to Solar

2 Component Model: L + H



$$d = \frac{1}{\Delta Z} \sum_Z |\log(X_{\text{solar}}(Z)) - \log(X_{\text{model}}(Z))|$$

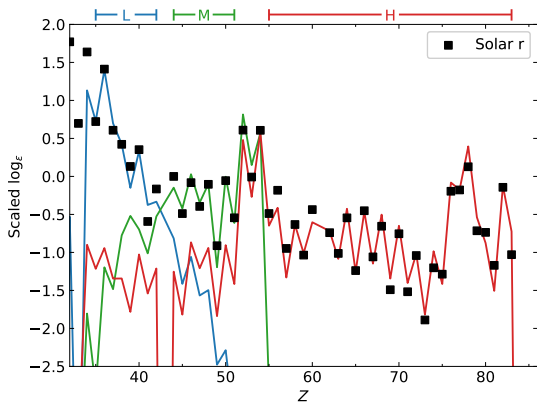


L-component
not produced
in simulations!

add additional
M-component

Comparison to Solar

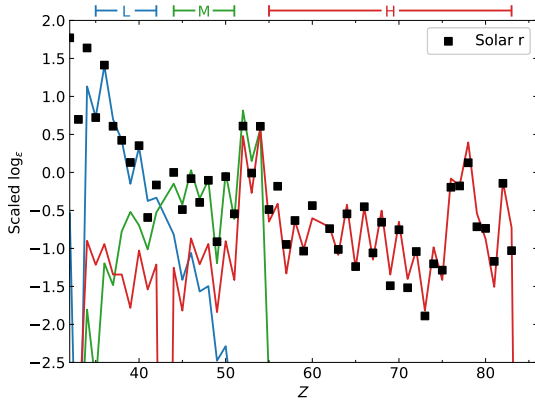
3 Component Model: L + M + H



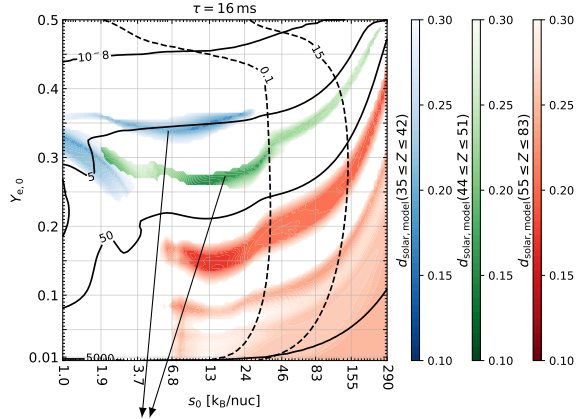
see also: Y.-Z. Qian & G. J. Wasserburg, ApJ 559 925 (2001)
C. J. Hansen, F. Montes & A. Arcones, ApJ 797 123 (2014)

Comparison to Solar

3 Component Model: L + M + H



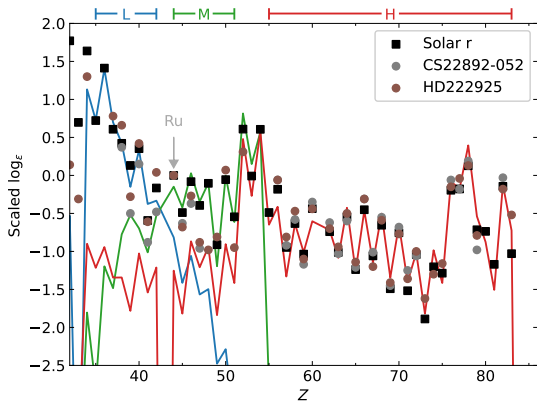
see also: Y.-Z. Qian & G. J. Wasserburg, ApJ 559 925 (2001)
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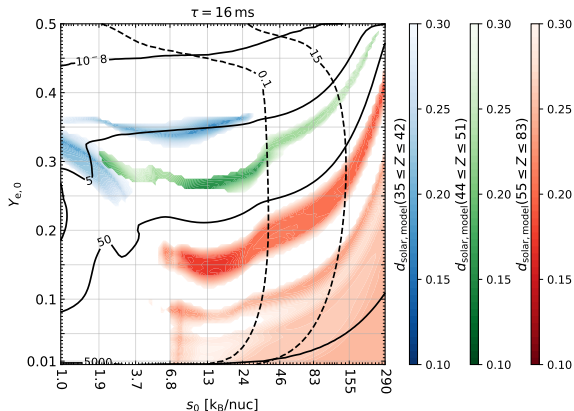
✓ conditions produced
in simulations

Comparison to Metal-Poor Stars

3 Component Model: L + M + H



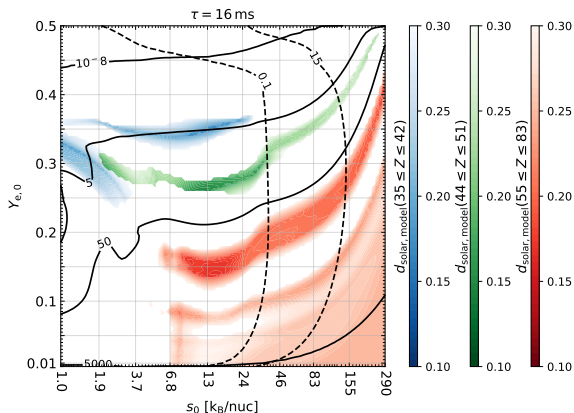
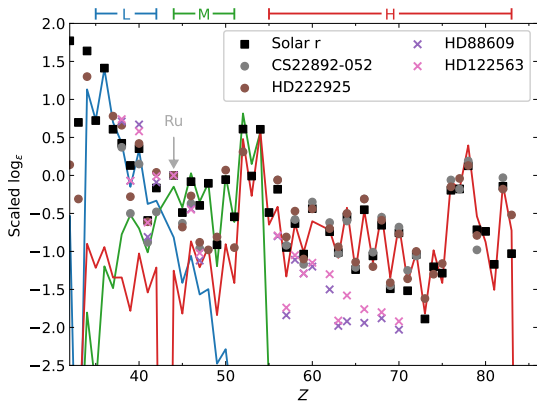
- very similar for main r-process stars
- ⇒ **robust** mass ratios of L/M/H: 50%/25%/25%



Solar r: C. Sneden, J. J. Cowan & R. Gallino, *AnnuRevAstro* 46:241-288 (2008)
 CS22892-052: C. Sneden, J. J. Cowan, J. E. Lawler et al., *ApJ* 591 936 (2003)
 HD222925: I. U. Roederer, J. E. Lawler, E. A. Den Hartog et al., *ApJS* 260 27 (2022)

Comparison to Metal-Poor Stars

3 Component Model: L + M + H

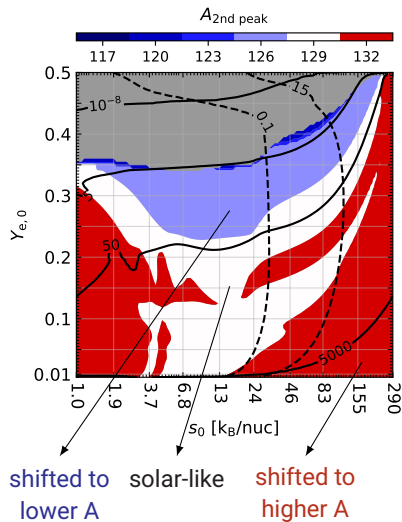


- very similar for main r-process stars
- ⇒ **robust** mass ratios of L/M/H: 50%/25%/25%
- H-component 1 dex lower for **Honda stars**

Solar r: C. Sneden, J. J. Cowan & R. Gallino, AnnuRevAstro 46:241-288 (2008)
 CS22892-052: C. Sneden, J. J. Cowan, J. E. Lawler et al., ApJ 591 936 (2003)
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 HD88609 & HD122563: S. Honda, W. Aoki, Y. Ishimaru et al., ApJ 666 1189 (2007)

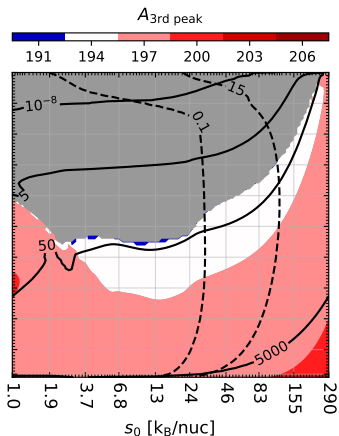
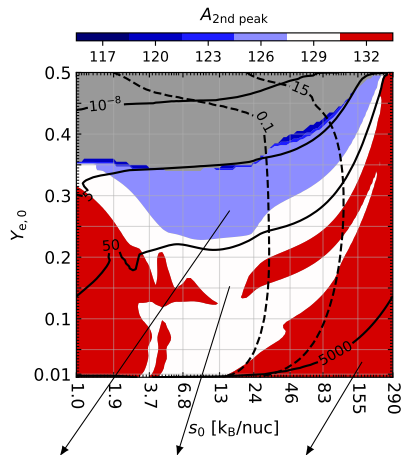
r-Process Peaks

see also: B. S. Meyer & J. S. Brown, ApJS 112 199 (1997)



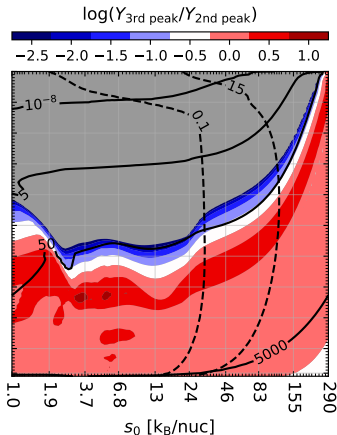
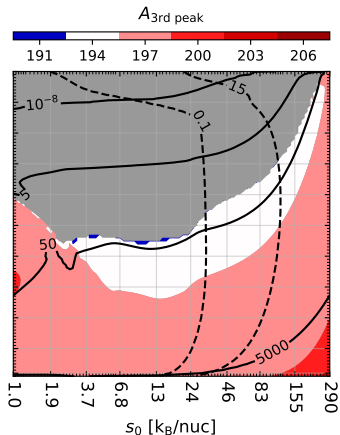
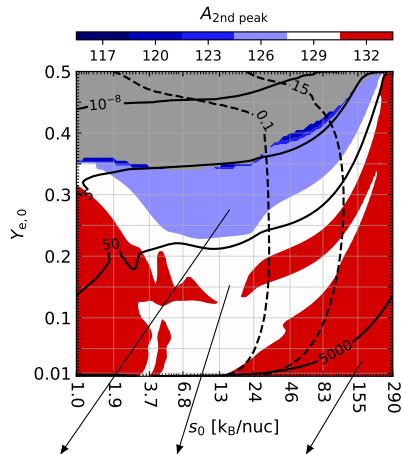
r-Process Peaks

see also: B. S. Meyer & J. S. Brown, ApJS 112 199 (1997)



r-Process Peaks

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- ✓ good agreement with solar when $Y_n/Y_{seed} \approx 50$
- ✗ strong dependency on nuclear physics

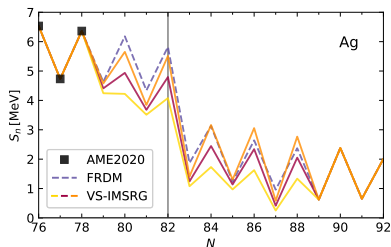


Part II - Nuclear Uncertainties

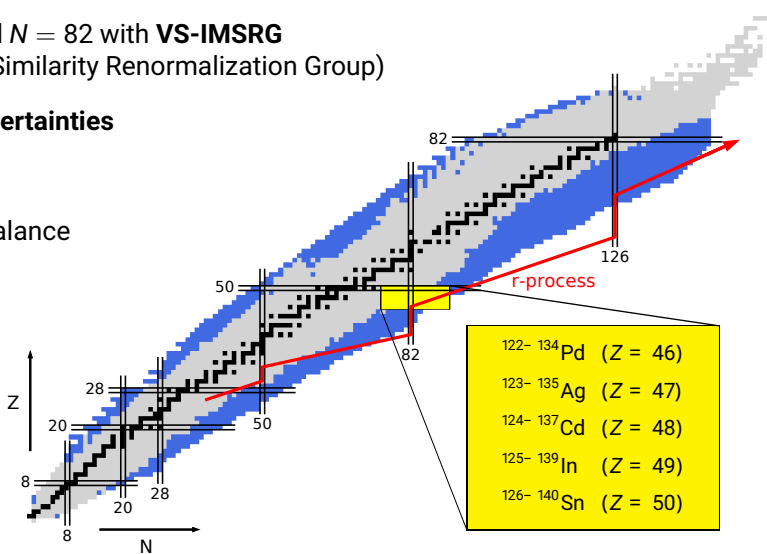
Ab-initio masses from VS-IMSRG

Ab-Initio Masses

- masses for 70 nuclei around $N = 82$ with **VS-IMSRG** (Valence Space In-Medium Similarity Renormalization Group)
- including valence space **uncertainties**
- (n, γ) -rates from *TALYS*
- (γ, n) -rates from detailed balance



sirEN 2025 (Giulianova)



Jan Kuske

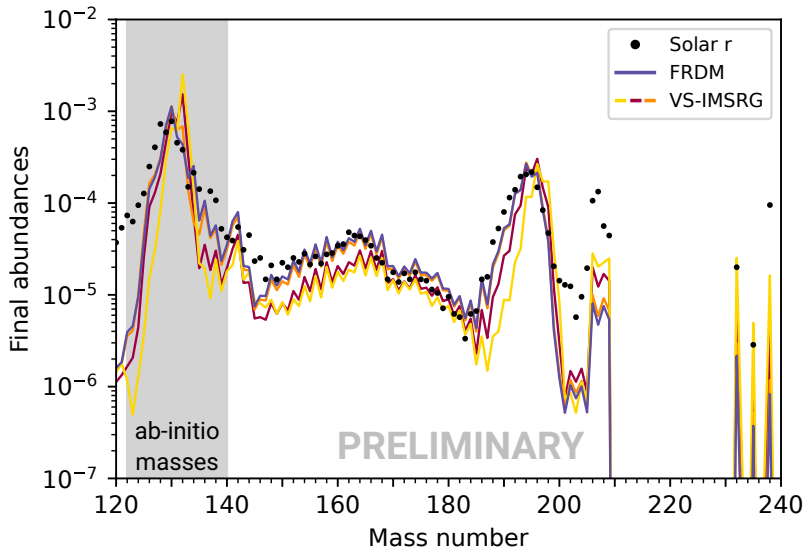
VS-IMSRG: T. Miyagi et al., Phys. Rev. C 105, 014302 (2022)
Fig. (mod.): A. Arcones & F. Thielemann, Astron Astrophys Rev 31, 1 (2023)

Nucleosynthesis Results

VS-IMSRG vs. FRDM2012

- ↘ lower S_n
- ↘ lower (n, γ) -rates
- ⇒ **stronger waiting point**
- ↘ lower abundances beyond second peak
- ↗ higher $Y_n/Y_{\text{seed}}(A > 140)$
- ⇒ **more Pb and actinides**

*J. Kuske, T. Miyagi,
A. Arcones, A. Schwenk
(in prep.)*



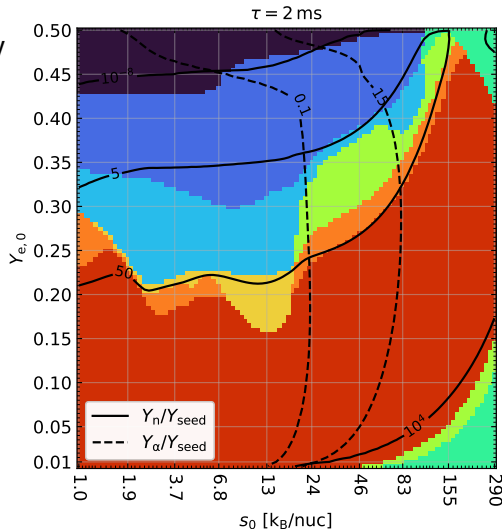
Summary & Outlook

Part I - Complete r-process study

- second-to-third peak produced **robustly** for many conditions
 - full r-process pattern requires **superposition** of at least 2–3 different conditions
- ⇒ more details: *J. Kuske, A. Arcones, M. Reichert (submitted to ApJ), arXiv:2506.00092*

Part II - Ab-initio masses from VS-IMSRG

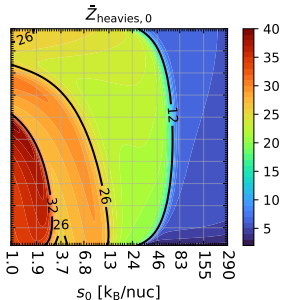
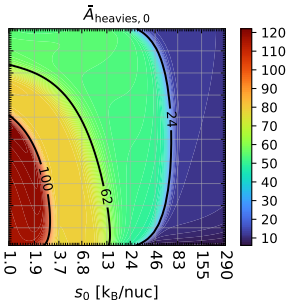
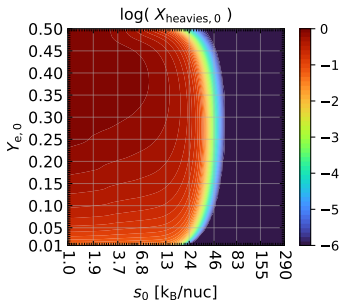
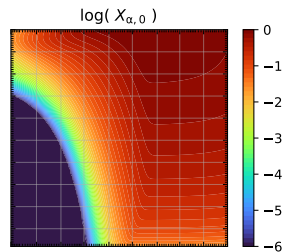
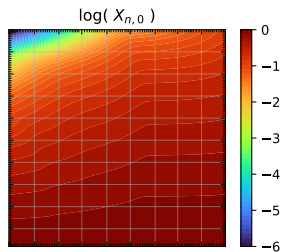
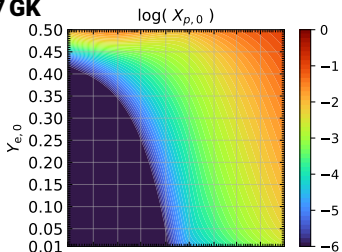
- first application in r-process calculations
- ⇒ coming soon: *J. Kuske, T. Miyagi, A. Arcones, A. Schwenk (in prep.)*





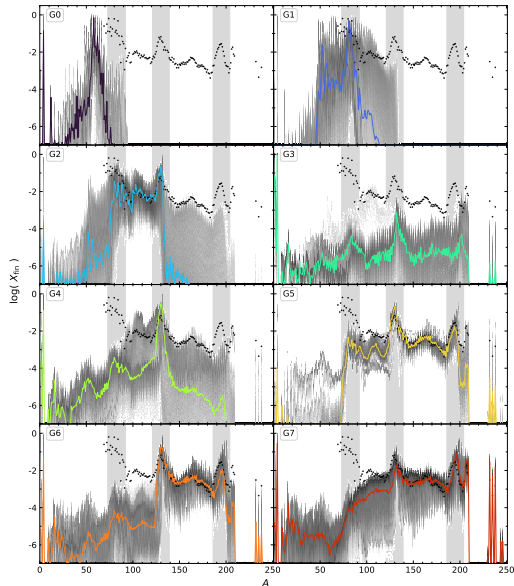
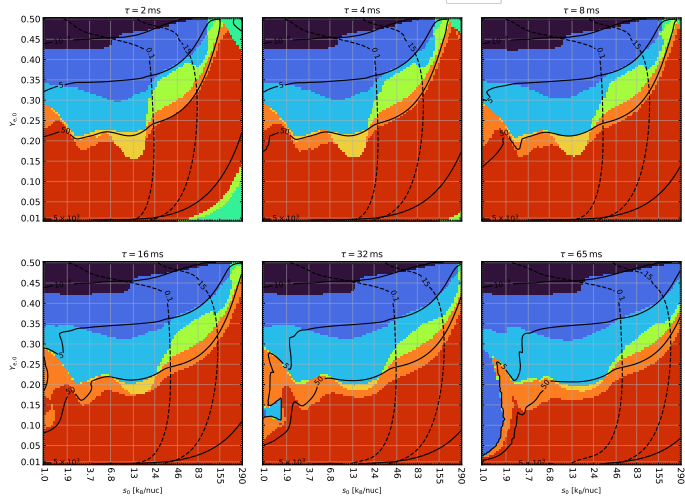
Initial Conditions

NSE at 7 GK



Nucleosynthesis Groups

For Different Expansion Timescales



$$\bar{A}_{fin} \approx \bar{A}_{seed} + \frac{Y_n}{Y_{seed}}$$

Comparison to Trajectories

From Hydrodynamical Simulations

- map trajectory to $Y_{e,0}-s_0-\tau$ -space:

$$\left. \begin{matrix} Y_{e,0} \\ s_0 \end{matrix} \right\} \Rightarrow \text{from interpolation to 7 GK}$$

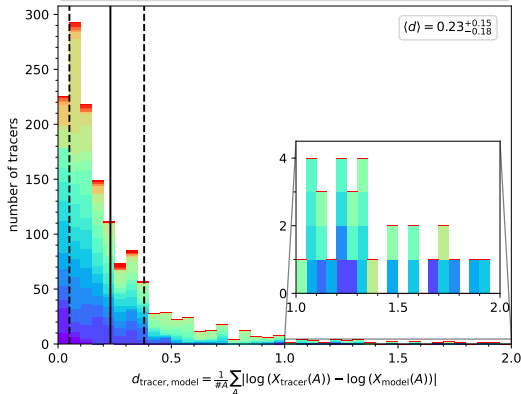
$$\tau \Rightarrow \text{from fit to density profile}$$

- metric for comparing final mass fractions:

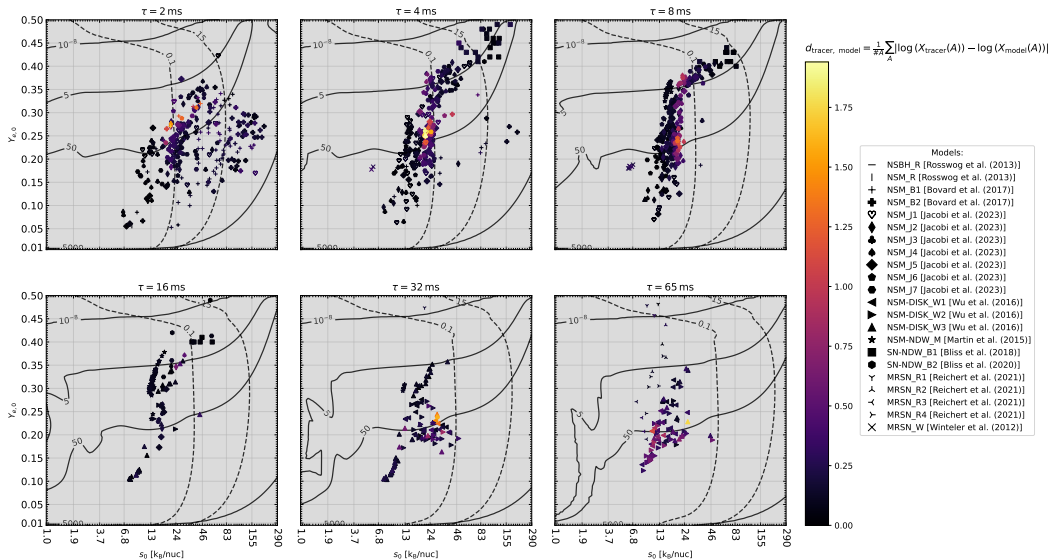
$$d_{\text{tracer,model}} = \frac{1}{\#A} \sum_A |\log(X_{\text{tracer}}(A)) - \log(X_{\text{model}}(A))|$$

- 22 models of different astrophysical sites with up to 100 trajectories each

NSBH_R [Rosswog et al. (2013)]	NSM-DISK_W1 [Wu et al. (2016)]
NSM_R [Rosswog et al. (2013)]	NSM-DISK_W2 [Wu et al. (2016)]
NSM_B1 [Bovard et al. (2017)]	NSM-DISK_W3 [Wu et al. (2016)]
NSM_B2 [Bovard et al. (2017)]	NSM-NDW_M [Martin et al. (2015)]
NSM_J1 [Jacobi et al. (2023)]	SN-NDW_B1 [Bliss et al. (2018)]
NSM_J2 [Jacobi et al. (2023)]	SN-NDW_B2 [Bliss et al. (2020)]
NSM_J3 [Jacobi et al. (2023)]	MRSN_R1 [Reichert et al. (2021)]
NSM_J4 [Jacobi et al. (2023)]	MRSN_R2 [Reichert et al. (2021)]
NSM_J5 [Jacobi et al. (2023)]	MRSN_R3 [Reichert et al. (2021)]
NSM_J6 [Jacobi et al. (2023)]	MRSN_R4 [Reichert et al. (2021)]
NSM_J7 [Jacobi et al. (2023)]	MRSN_W [Winteler et al. (2012)]



Comparison to Trajectories



Comparison to Trajectories

From Hydrodynamical Simulations

- **good agreement** for $\approx 98\%$ of trajectories
- large discrepancies for some trajectories due to:
 - 1) non-monotonic density evolution: **hydrodynamical shocks**
 - 2) **sensitive conditions**: between two nucleosynthesis groups

