

# Double white dwarf populations in the era of GW astronomy

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**Observatories  
& experiments**

Ground-based  
experiment



Space-based observatory



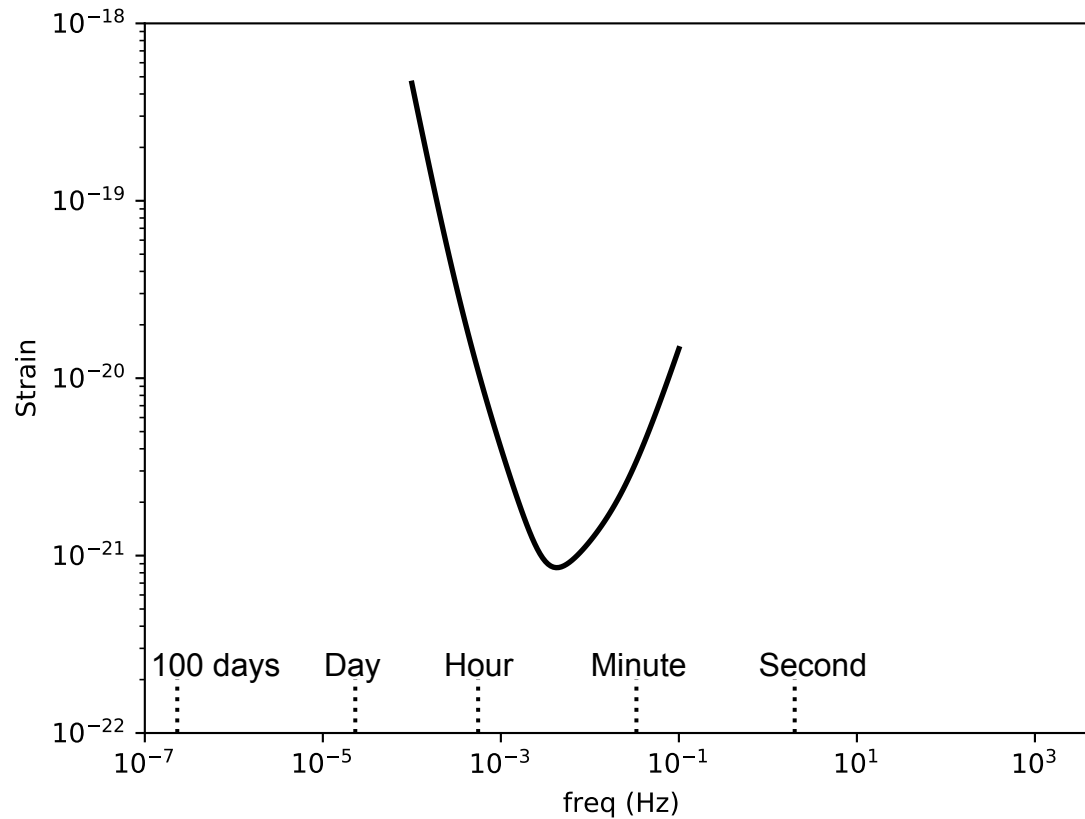
Pulsar timing array



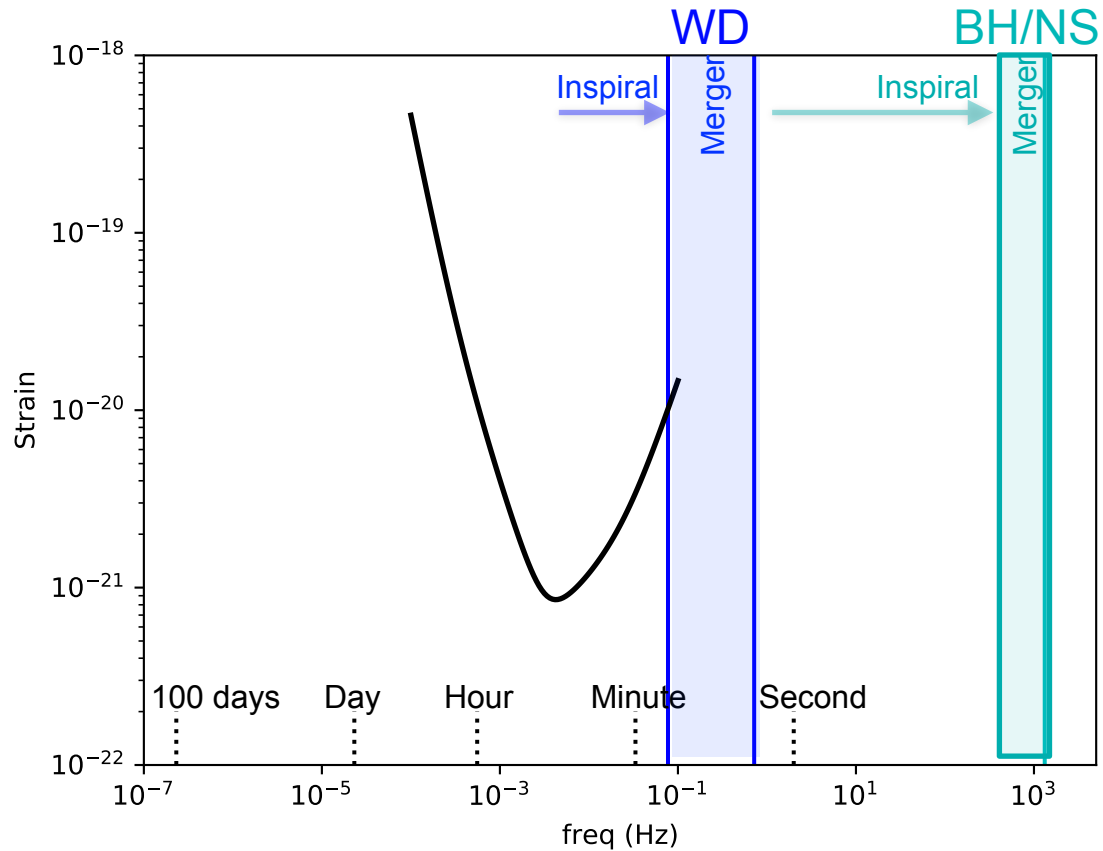
Cosmic microwave  
background polarisation



# Galactic compact binaries: from micro- to deci-Hz

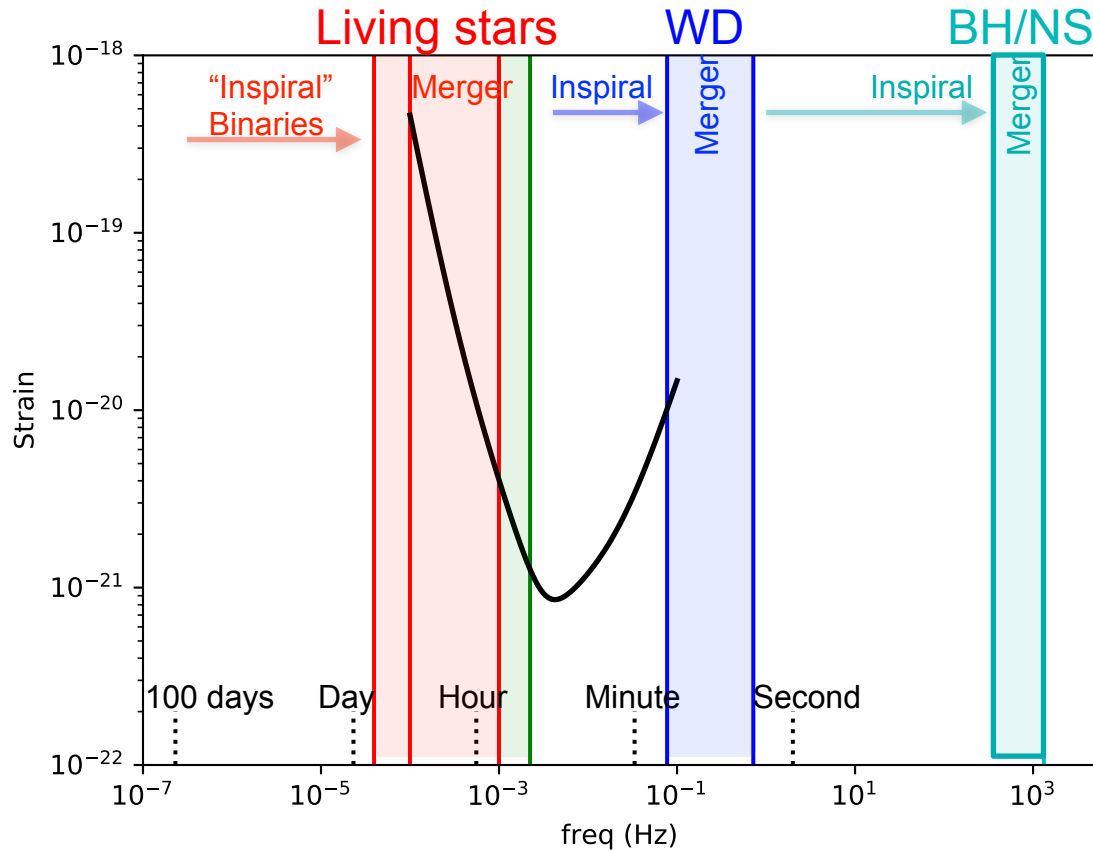


# Galactic compact binaries: from micro- to deci-Hz



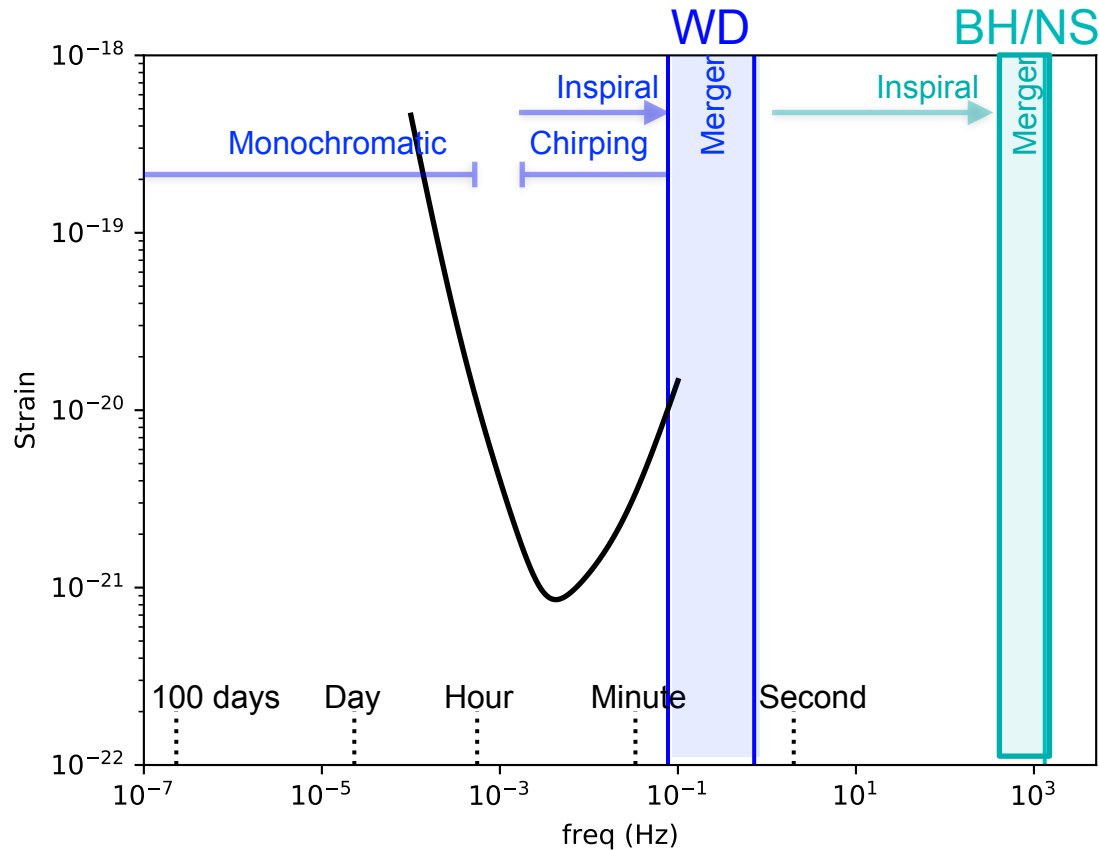
# Galactic compact binaries: from micro- to deci-Hz

- “living” stars:
- ‘Main-sequence stars’ Normal hydrogen-burning
  - ‘Stripped stars’ Helium rich, SdB



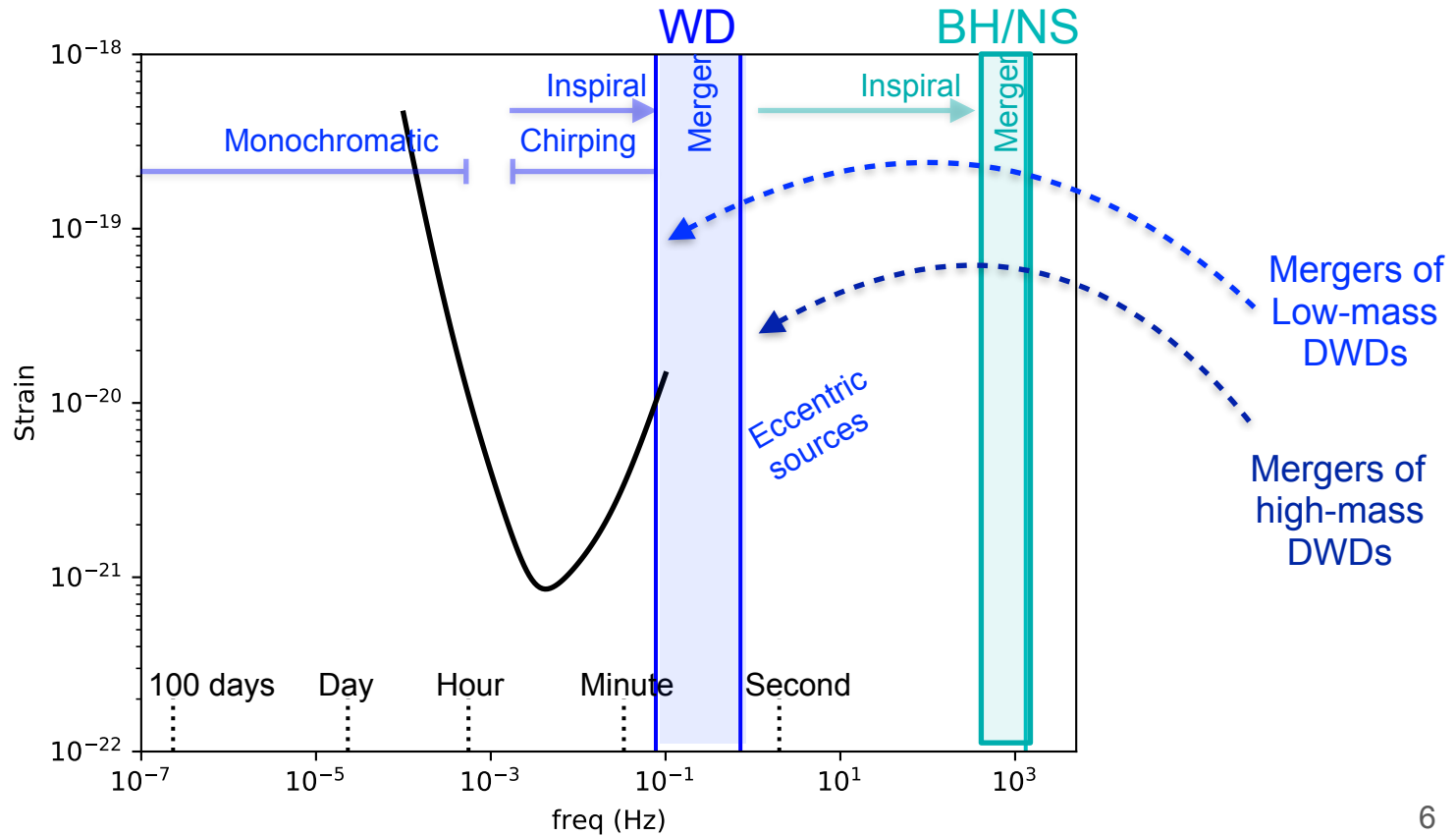


# Galactic compact binaries: from micro- to deci-Hz



"Chirping" sources with a measurable  $df/dt$  (possible  $d^2f/dt^2$ )  
Break the degeneracy between distance and chirp mass

# Galactic compact binaries: from micro- to deci-Hz



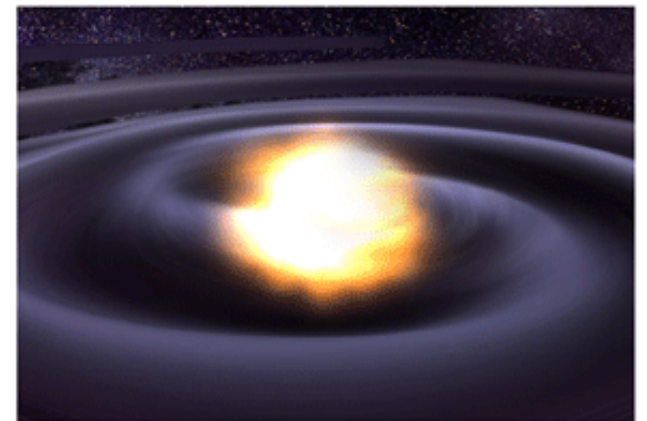
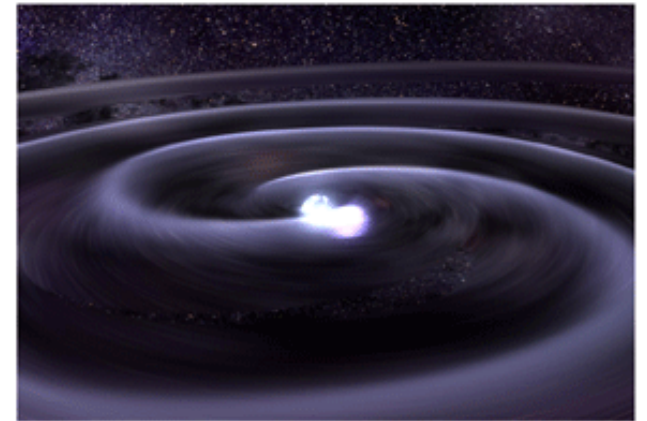
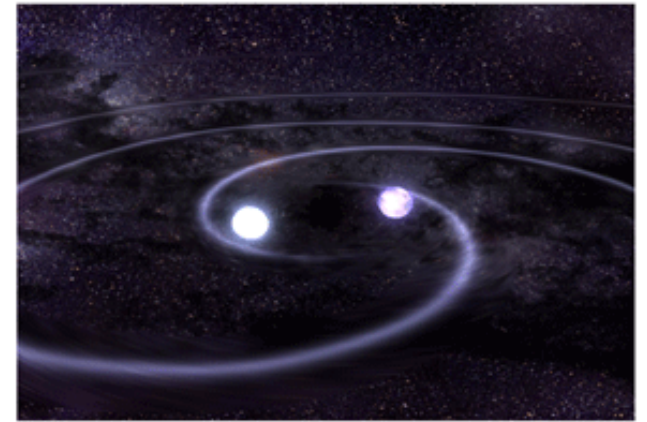
# Mergers with WDs

Transient events:

- Supernova type Ia
- Calcium-rich transients
- & other thermonuclear transients

Major quests for the origins of these transients

- Simultaneous GW observations would be ground-breaking, but distance horizon problematic



# Why study double white dwarfs?

Largest population of ultracompact binaries in the Milky Way

## **Gravitational waves:**

Dominant sources at milli- and decihertz frequencies, leading to GW foreground

## **Progenitors of supernova Type Ia:**

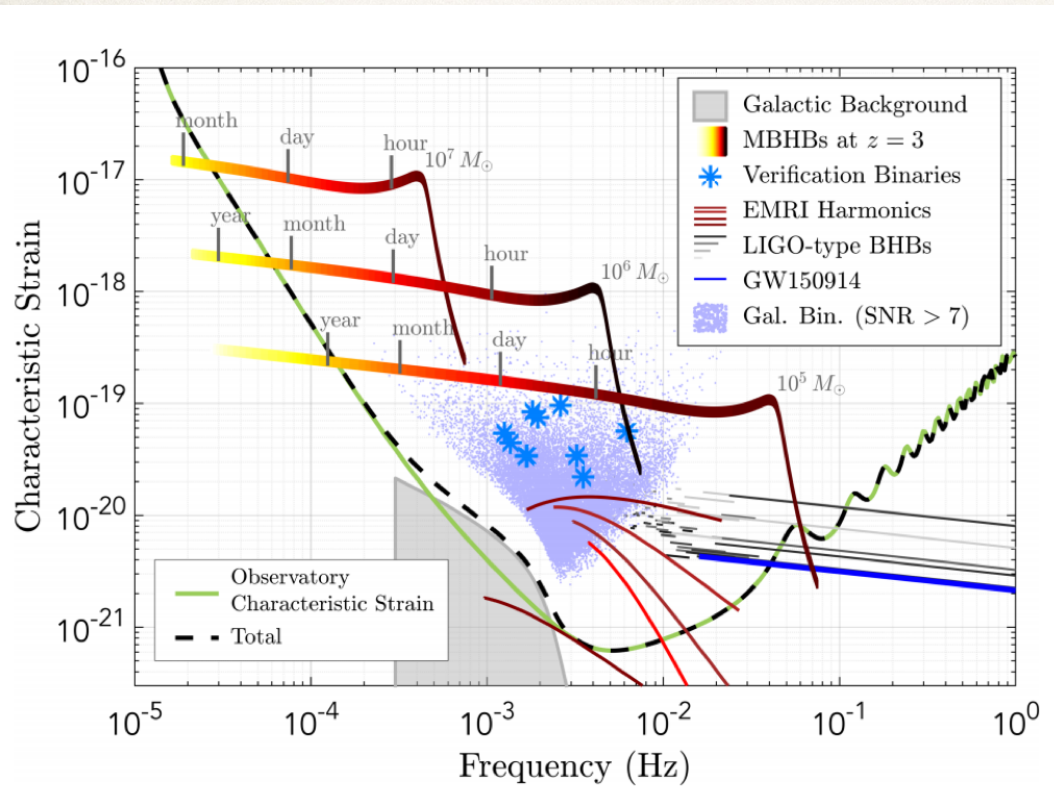
Expansion of universe, dark energy

## **Stellar interaction:**

Stellar and binary evolution  
Mass transfer



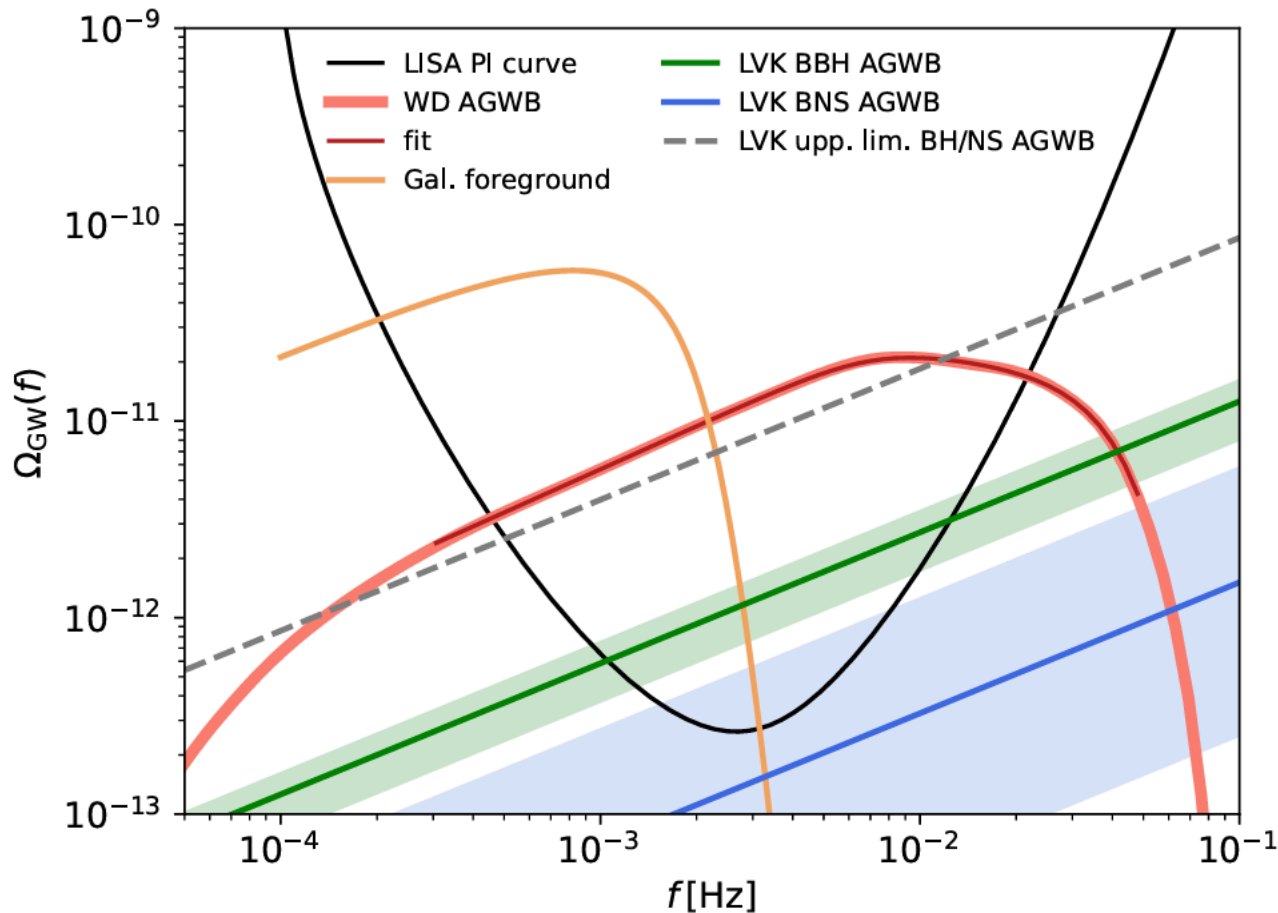
# GW foreground



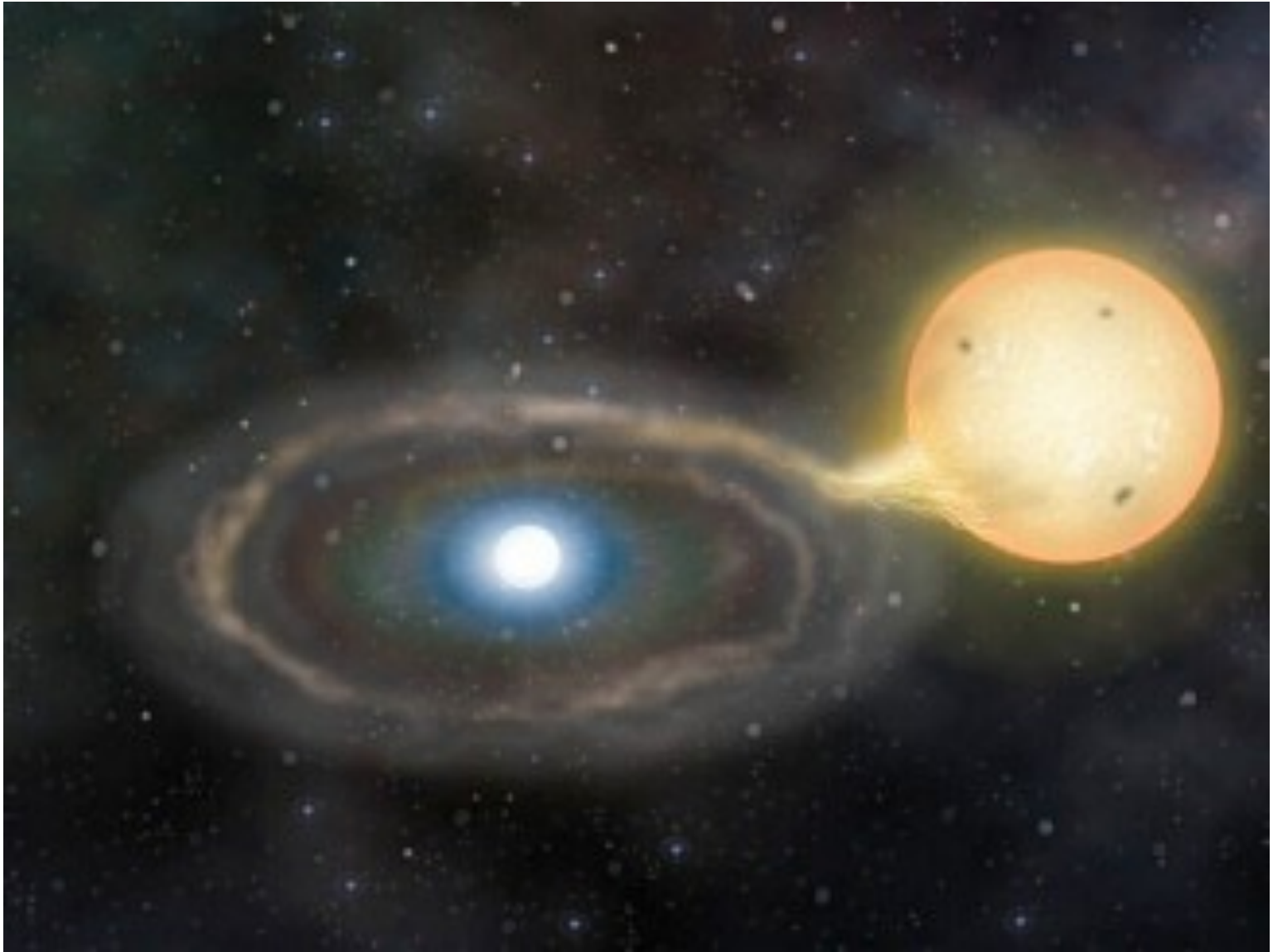
- Resolved vs unresolved
- $\Delta f_{\text{lisa}} = 1 / T_{\text{obs}} \sim 8e-9 \text{ Hz}$



# GW background from extragalactic sources



- ❖ Farmer & Phinney 03, Schneider 01, Staelens & Nelemans 24
- ❖ DWDs dominating the deciHz regime



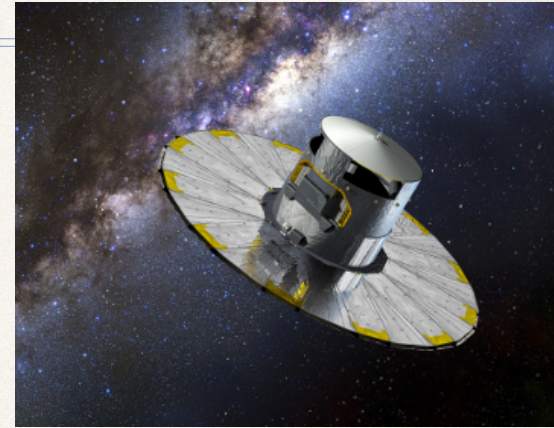
**EM observations of double WDs**



# Observations so far

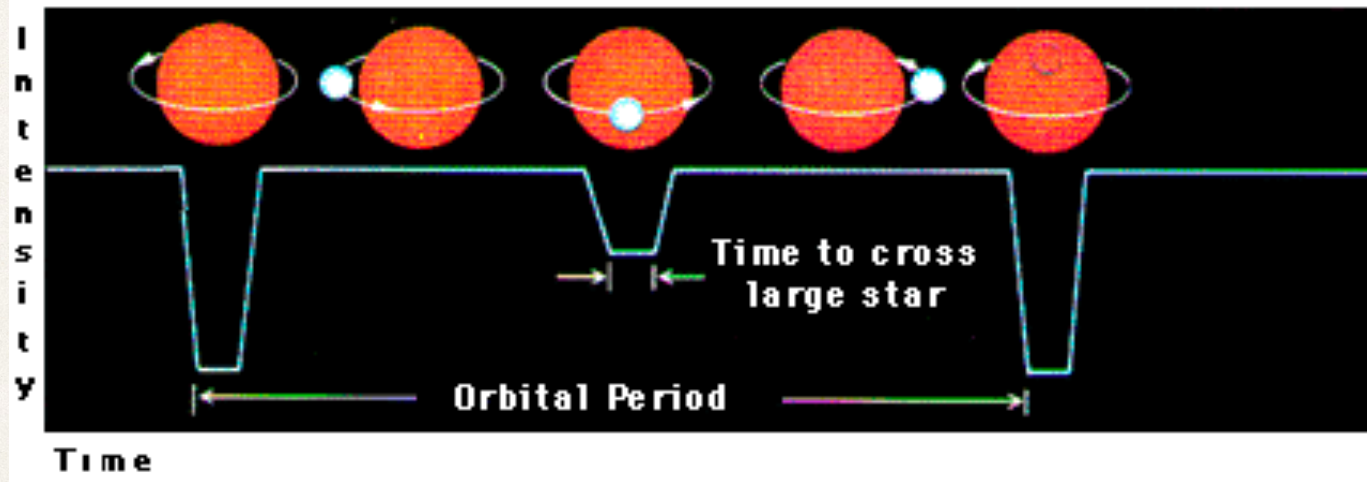
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- ❖ ~10 yrs ago : ~50 double WDs known
  - ❖ detected with variety of methods
- ❖ Now: ~150 double WDs
  - ❖ SDSS ELM survey: Extremely-Low Mass WDs
  - ❖ ZTF: ~30 eclipsing double WDs (also mostly low mass)
- ❖ Next few years:
  - ❖ Gaia: 5-10% double WDs in several 100,000 WDs...  
needs follow-up for confirmation of binarity





# Eclipsing binaries



## ❖ Expectations:

- ❖ ZTF: ~30 DWDS
- ❖ Vera Rubin Observatory: ~1000 DWDS
- ❖ Gaia satellite: ~200 DWDS

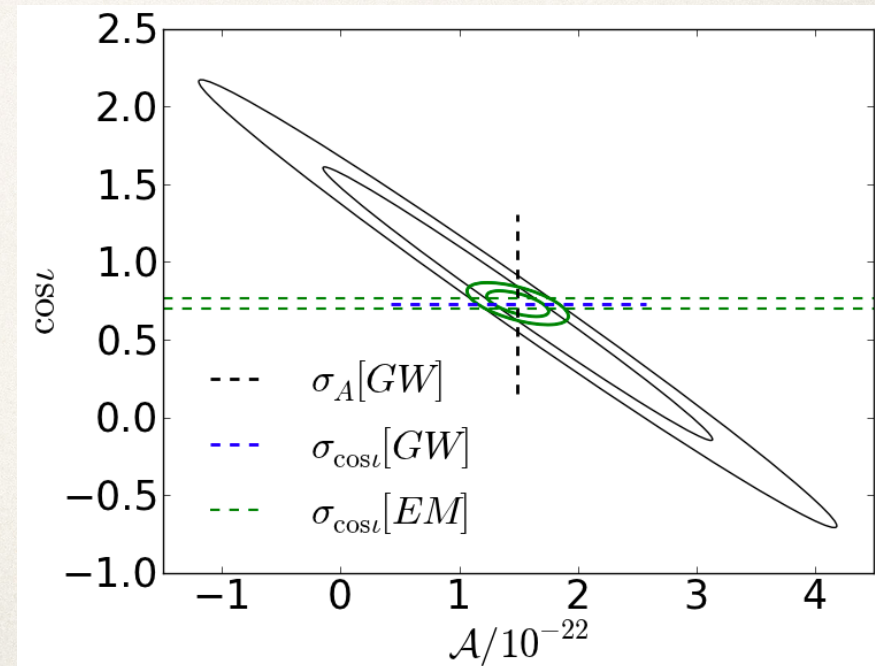
Van Roestel in  
prep.

Korol+ 17



# Multimessenger binaries

- ❖ EM can provide: inclination, sky position, distance
- ❖ Combining GW & EM observations can improve parameter estimations
- ❖ Apriori knowledge of sky position and inclination can improve GW amplitude measurement up to a factor of 60 (Shah+ 13).
- ❖ Errors in the GW inclination may indicate an eclipsing system, that can be followed by EM (Shah+ 12)





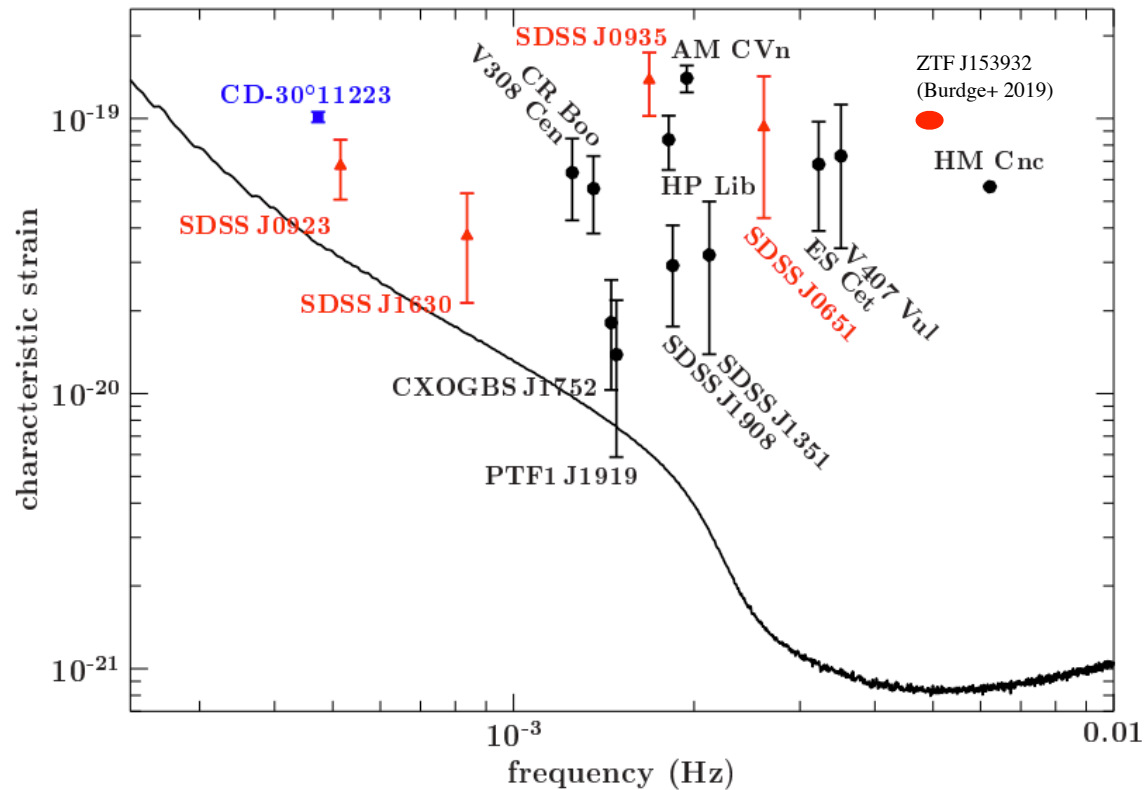
# Verification binaries

## Detached DWDs

DWDs undergoing mass transfer (AM CVn)

WD + stripped-envelope star

- ❖ 'Easily detectable in GWs'
- ❖ 18 sources after 3 months, +22 sources after 48 months (Kupfer+ 24)
- ❖ Crucial for testing of space-based GW interferometers (but see Littenberg & Lali '24)



Kupfer+ 15, 24 -> See Thomas Kupfer's talk later today



# Optical observations

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- ❖ WDs are dim objects (<300 pc)
- ❖ Sensitive to cooling physics & dust extinction
- ❖ Selection effects hard to model

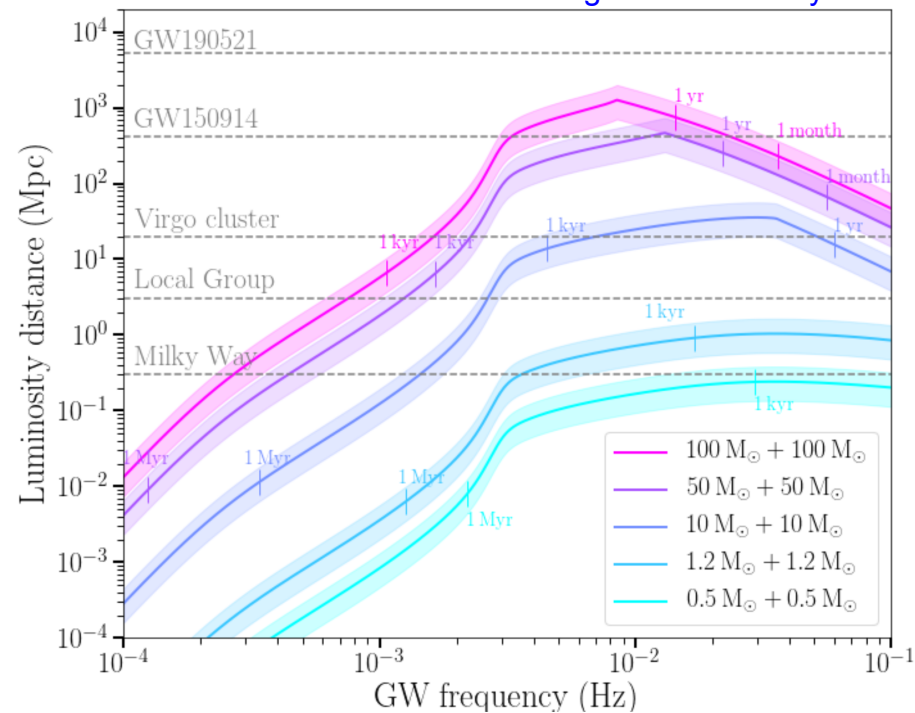
**Gravitational waves can be a game changer!**



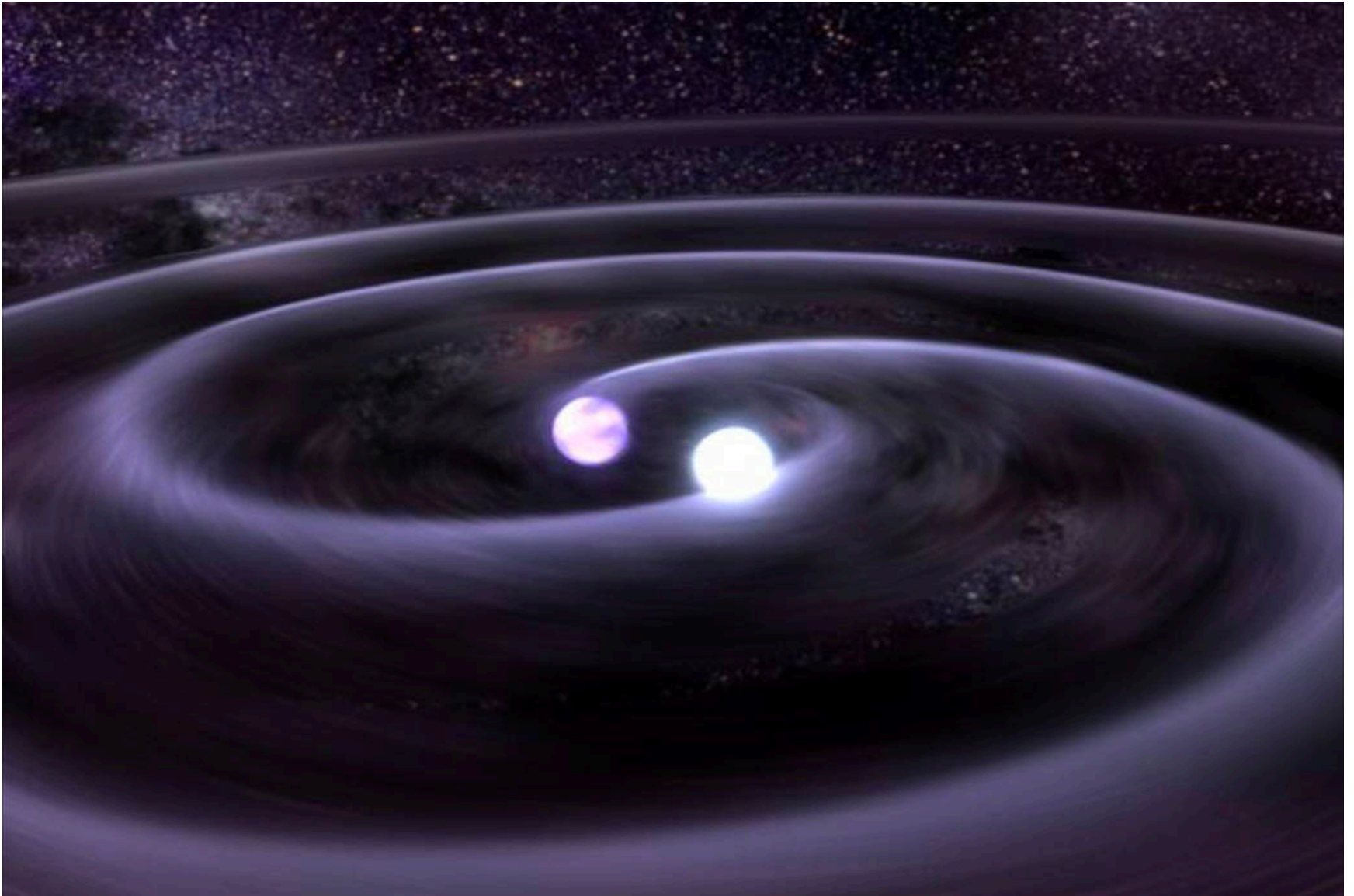
# Max distance to observe Expected GW sources

- WD+WD binaries
- NS+WD binaries  
evidence: millisecond radio pulsars
- BH+WD binaries  
selection effects against detection  
expected from population synthesis
- NS+NS binaries  
evidence: radio pulsar binaries: 10 out of  $\sim 20$  known NS+NS will merge
- BH+NS and BH+BH binaries  
selection effects against detection - expected from population synthesis  
We also anticipate detection of **extragalactic** BH+BH binaries  $\sim$  few to 10 yr before merger (Sesana 2016)

Figure credit: Antoine Klein & Valeriya Korol  
Assuming SNR>7 & T=4yr







**Double white dwarfs as GW sources: numbers**

# Expected number of sources

## Population synthesis studies

## Empirical rate estimates from observed populations

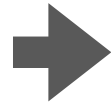
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| BH+BH  | $\sim 10^6$           | 0–70                     | up to ~50                | (Sesana '16)          |
|        | Total # in the Galaxy | Total # expected by LISA | Total # expected by LISA |                       |

- Several thousand WD binaries
- A few hundred with NS / BH companions
- Lots of potential to combine data from different resources

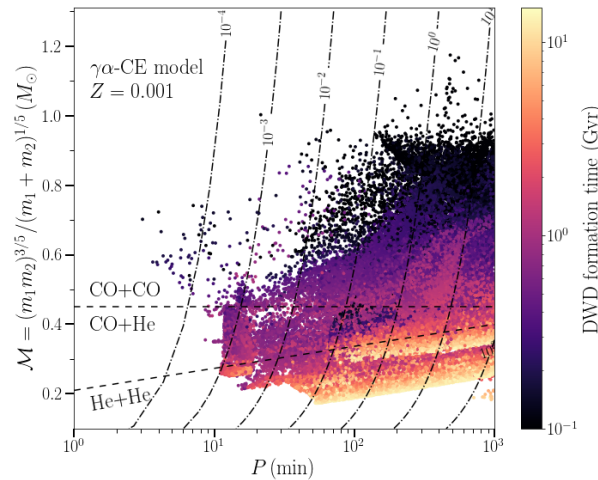
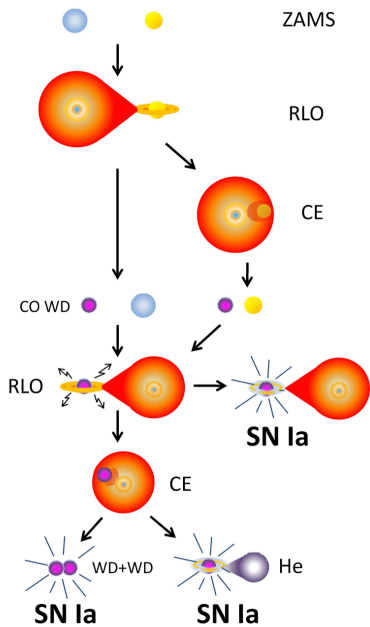
# Assembling a mock population with Binary Population Synthesis

Step 1

Model Binary evolution



Binary population



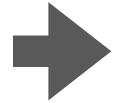
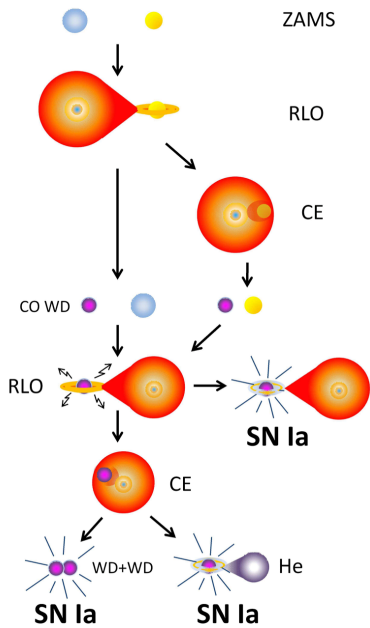
Toonen et al. 2012, 2017, 2018, based on the SeBa code See also: Nelemans et al. (2001), Ruiters et al. (2010), Yu & Jaffery (2010), Lamberts et al. (2018), Breivik et al. (2020), Li et al. (2020) and others



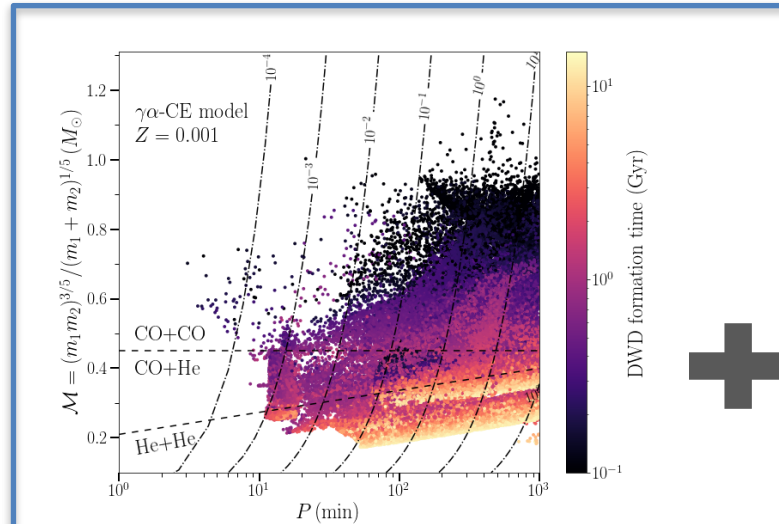
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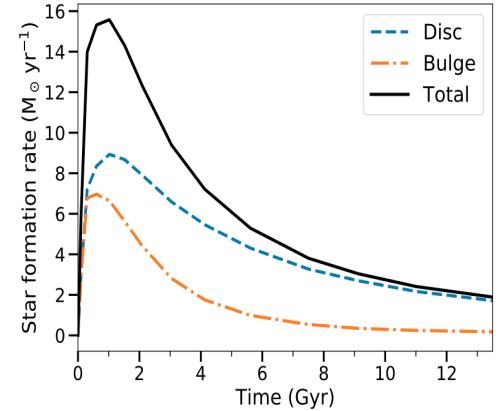


Step 2

Milky Way population

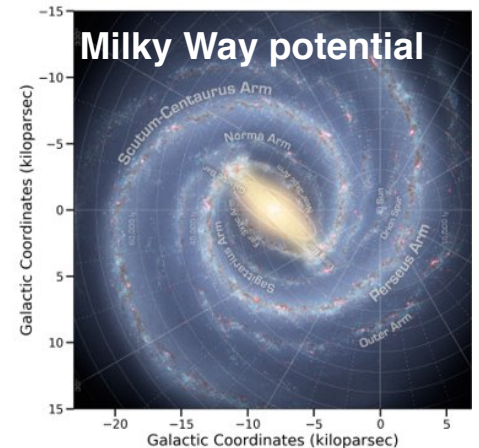


Star formation history



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Milky Way potential

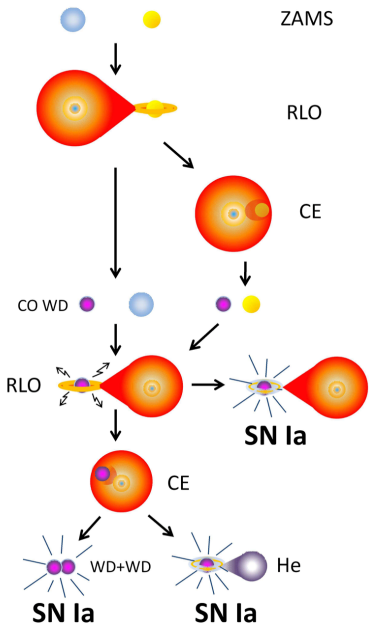


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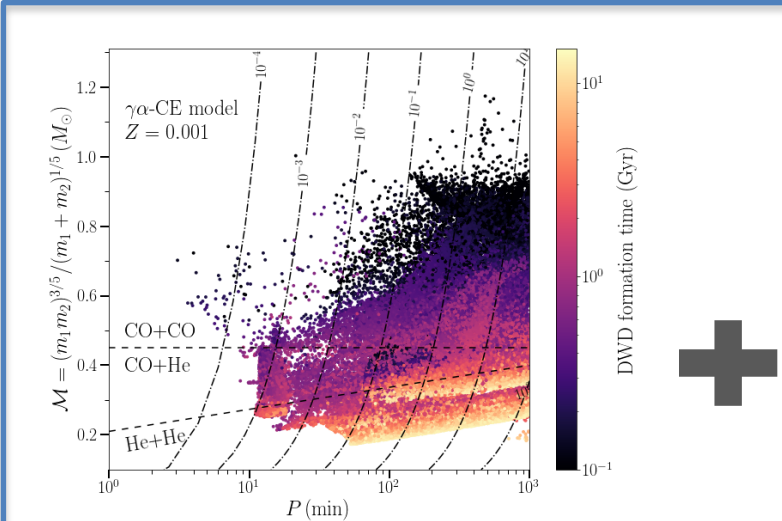
How (un)certain are step 1 & 2?

Step 1

Model Binary evolution



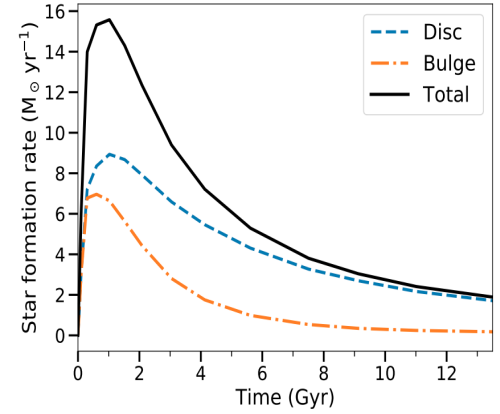
Binary population



Step 2

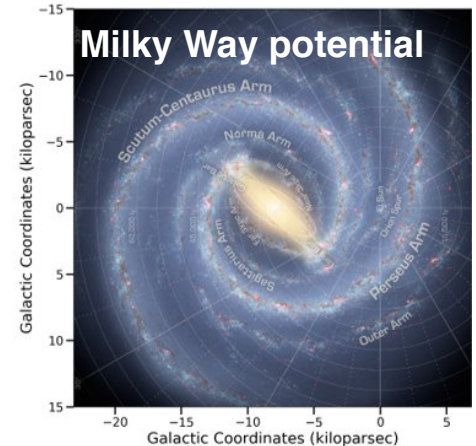
Milky Way population

Star formation history



+

Milky Way potential



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# Assembling a mock population with Binary Population Synthesis

## How (un)certain are step 1 & 2?

- PopCORN project: when we make the same assumptions, we get the same binary populations (Toonen+ 14)
- Currently on the way: Compact binary collab, lead by Alexey Bobrick & Katie Breivik

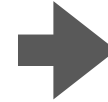
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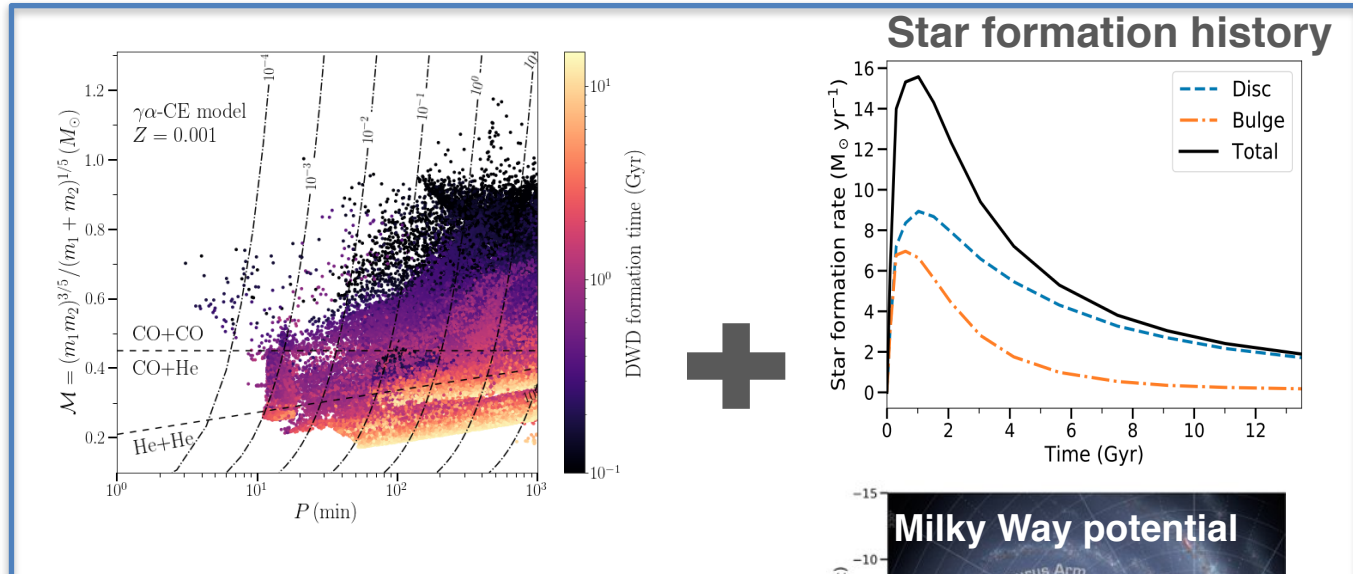
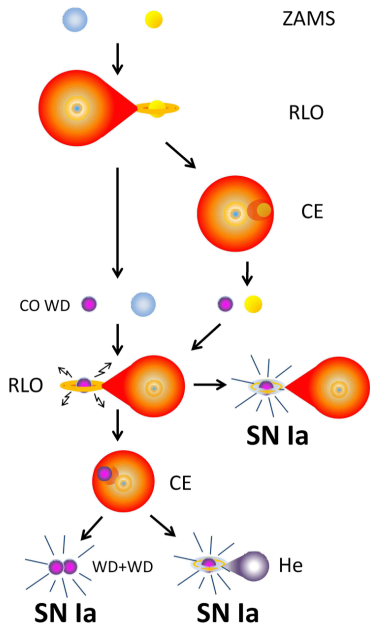


Binary population

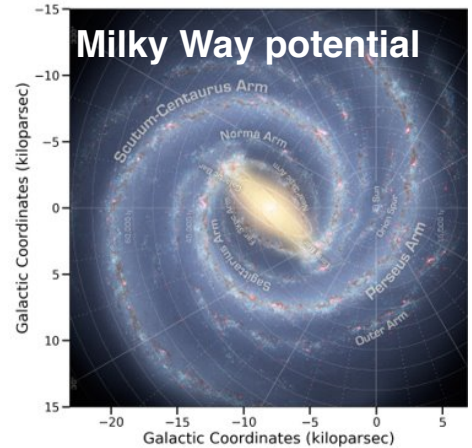
Step 2



Milky Way population



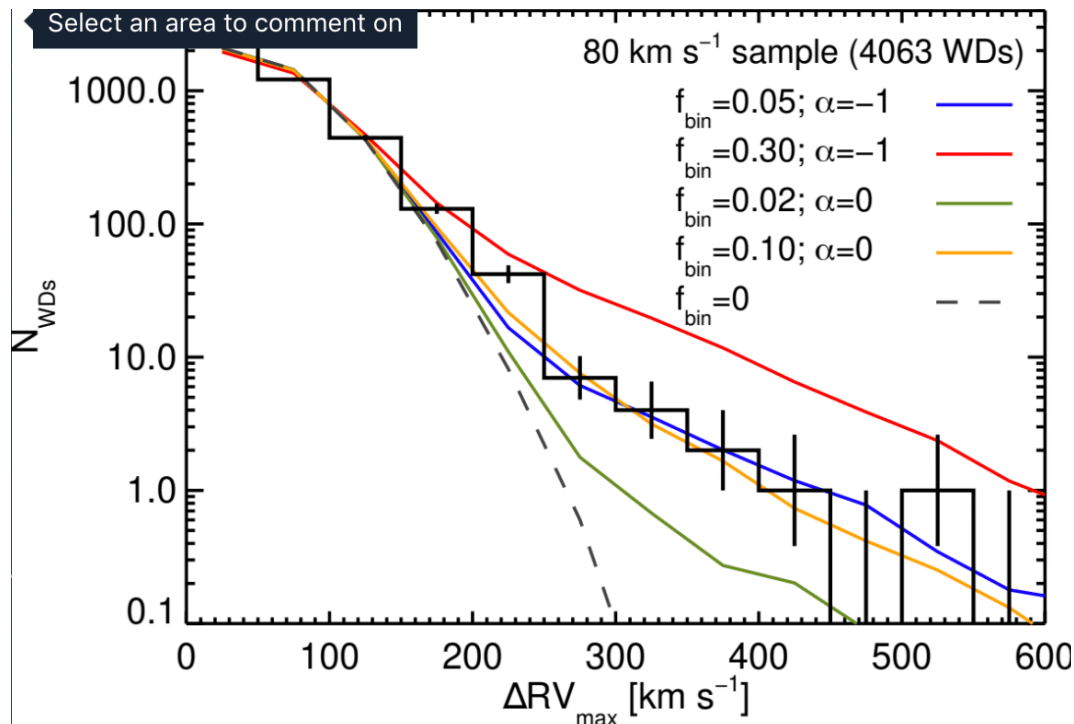
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# Expected number of sources

## Empirical studies

- For example WD+WD (Korol, Hallakoun, Toonen, Karnesis 2022)
  - Using radial velocities from the SDSS & SPY surveys (Maoz, Hallakoun, Badenes 2012,2017,2018)



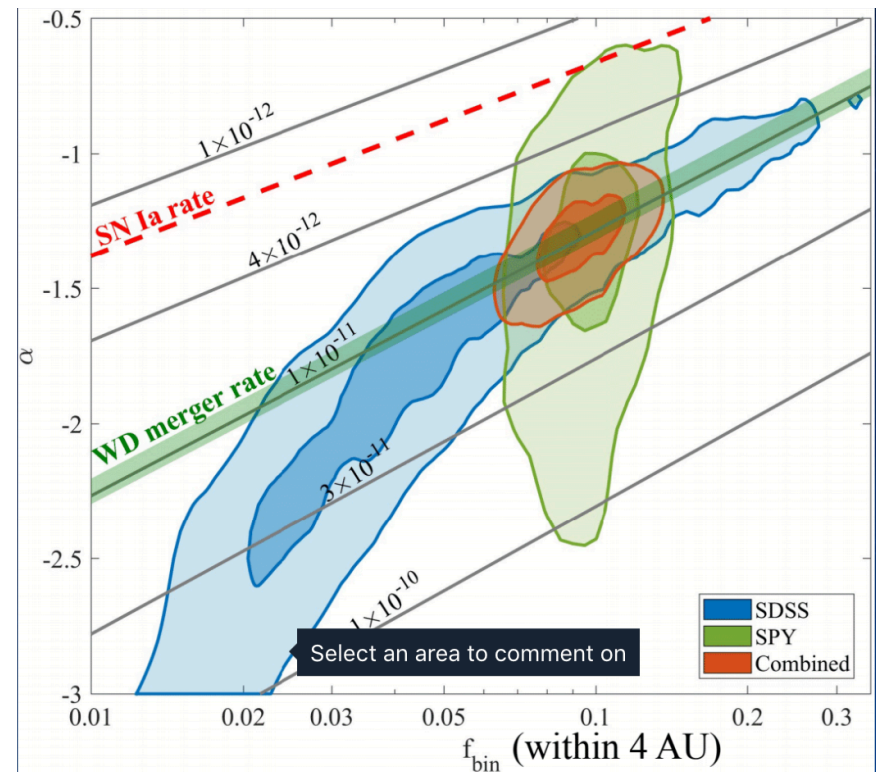
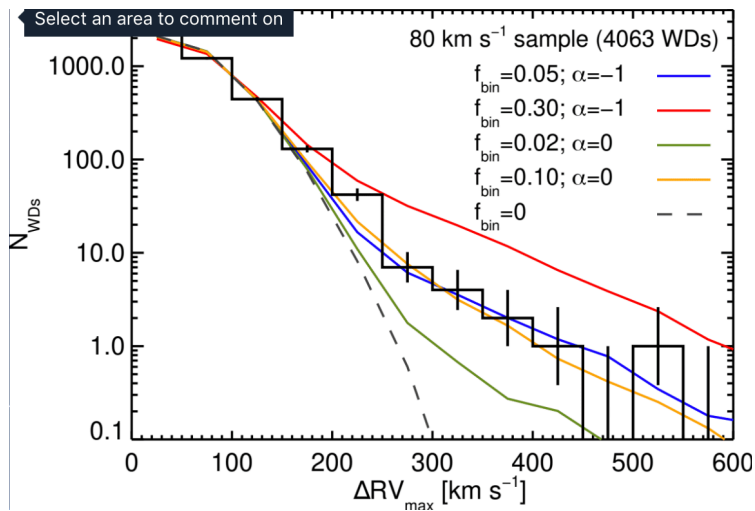
Depends mostly on:

- Binary fraction  $f_{\text{bin}}$  & power ( $\alpha$ ) of separation distribution ( $a^\alpha$ )

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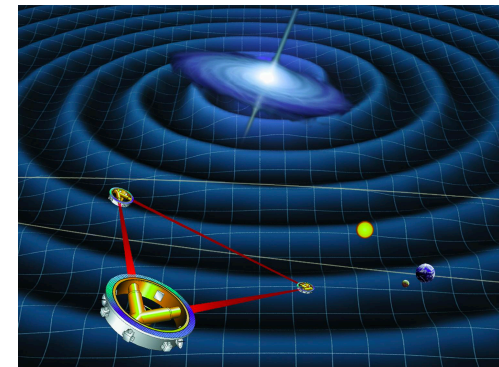
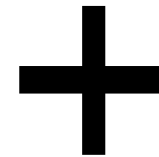
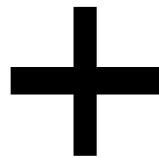
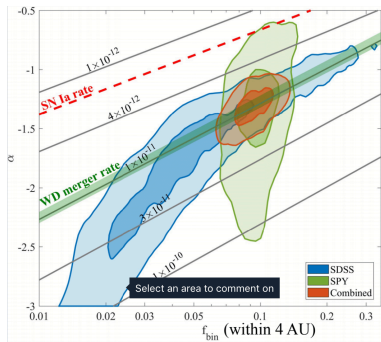
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  - Using radial velocities from the SDSS & SPY surveys (Maoz, Hallakoun, Badenes 2012,2017,2018)
- ➔ Observations suggest larger DWD space density (Toonen+ '18)
- ➔ Effect for LISA (Korol, Hallakoun, Toonen & Karnesis 2022)



Observationally based model  
of DWD population

Distances as our previous  
BPS studies  
(Toonen & Nelemans 2013,  
Korol+ '2017)

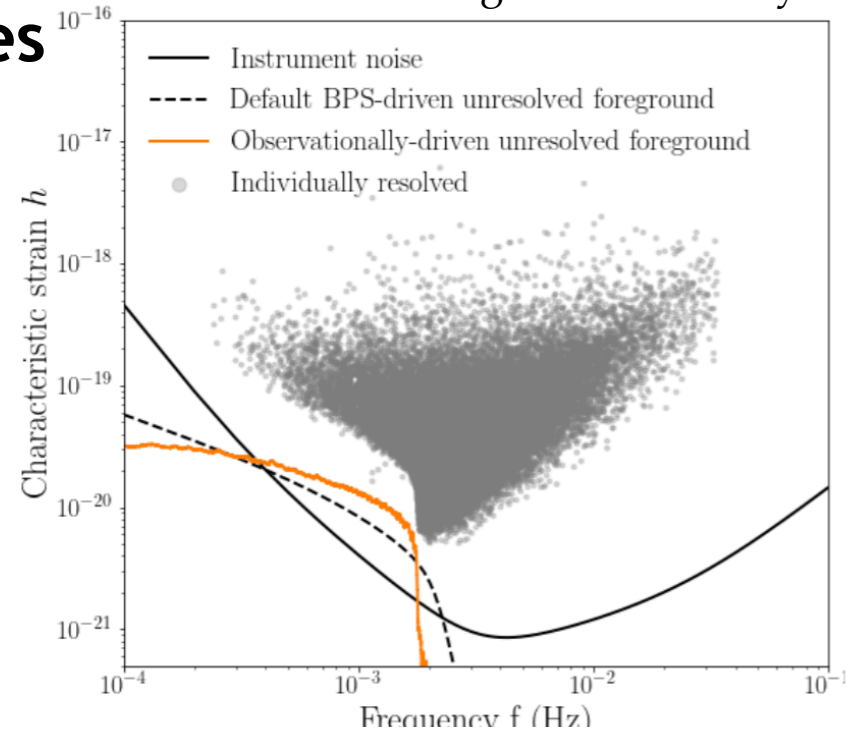
What can LISA see:  
following Karnesis+ 21

Assuming SNR>7 & T=4yr

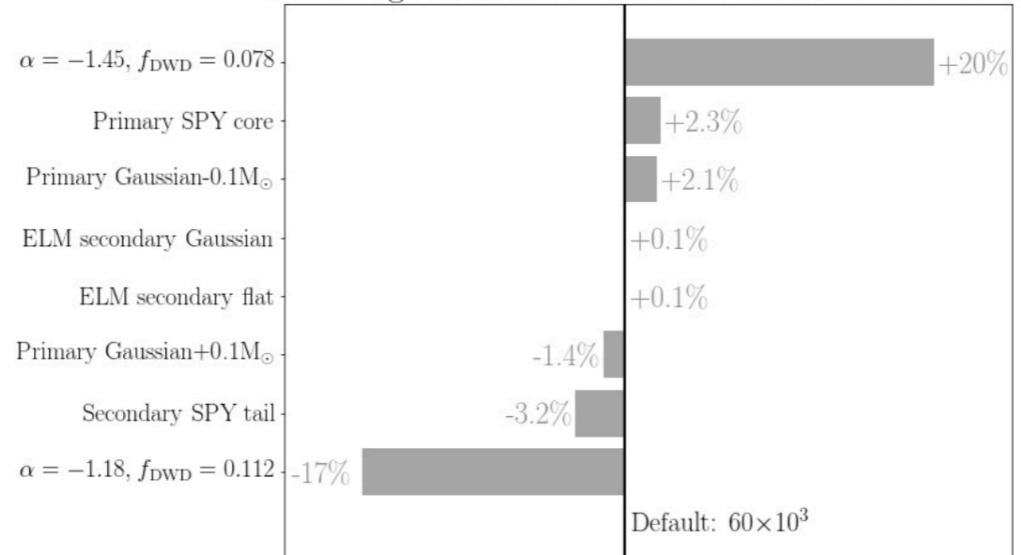
# Expected number of sources

## Empirical studies

- ❖ ~60,000 resolved sources
  - ❖ 2-5x more compared to BPS studies (Korol+ '17, Lamberts+ '19, Breivik+ '20, Wilhelm+ '21)
- ❖ a significantly different shape of the DWD confusion foreground.



Percentage difference in the total number of detections



# Expected number of sources

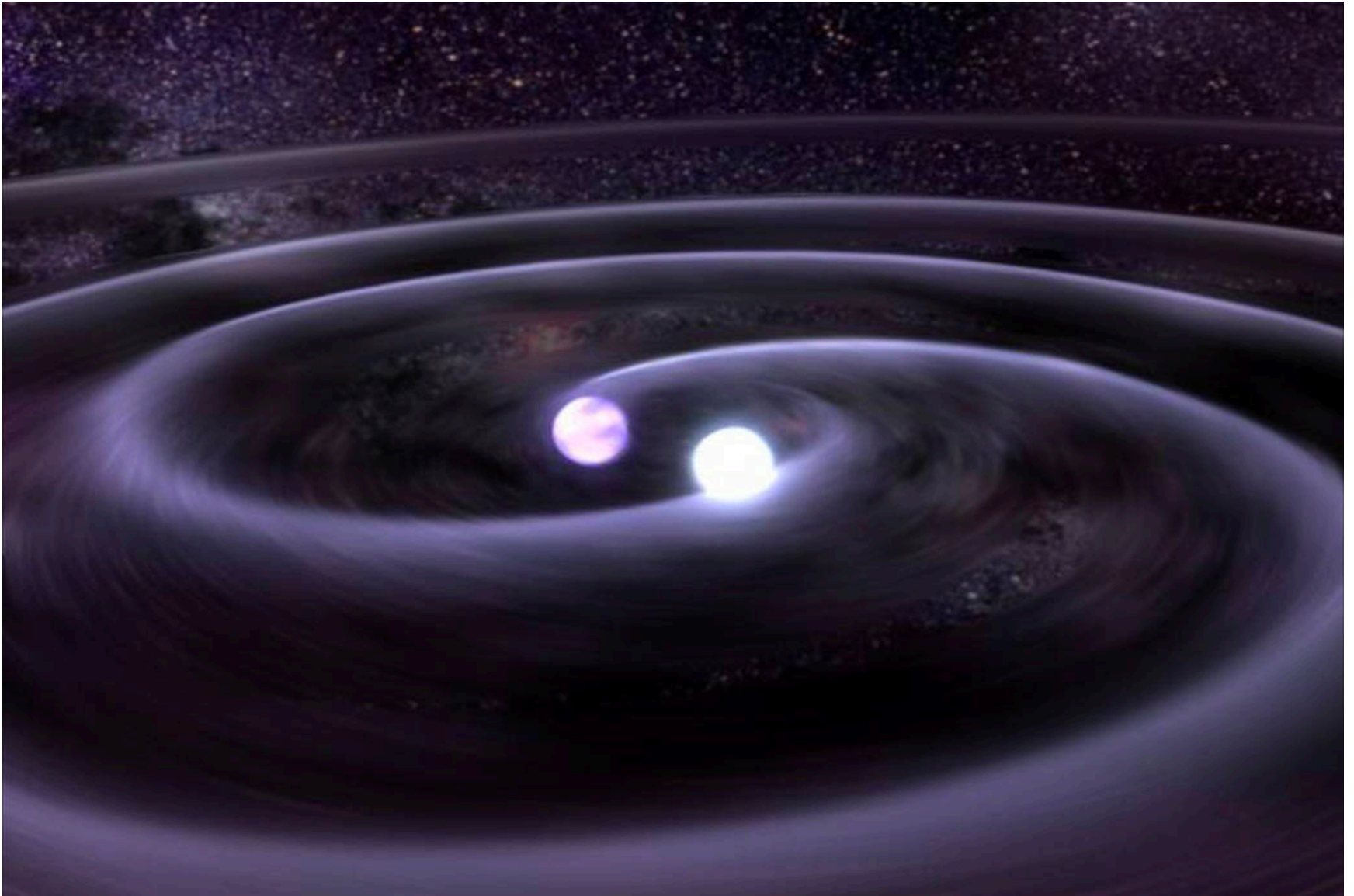
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|        | Total # in the Galaxy | Total # expected by LISA | Total # expected by LISA |                       |

- EM DWD observations help to constrain both methods
- Currently most systems at orbits outside the milliHz & deciHz regime.





**Double white dwarfs as GW sources: constraints**

# Expected number of sources

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# GW observations

- ❖ New era for double WDs:

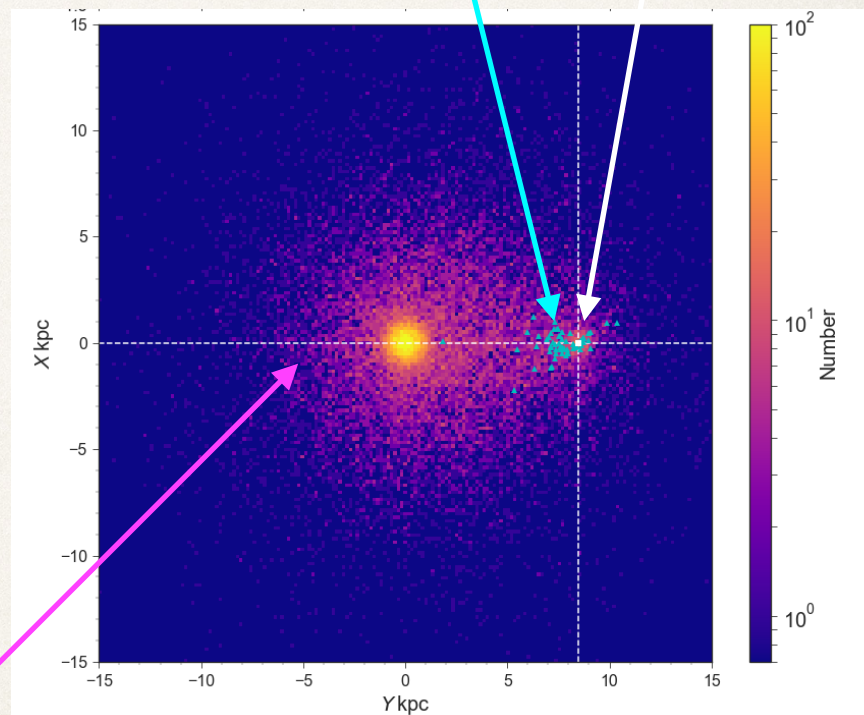
- ❖ LISA: ~6k-30k DWDs

- ❖ Tracer of Galactic structure (Korol +18, Wilhelm+ 21)

- ❖ Even the Local group (Korol +18, Keim+ 23, van Zeist+ 24)

Opposite side of  
Milky Way!

Optical  
Dwds      Sun



Korol+ 19



# LISA sources as Galactic probes

**LISA**: several 1000s DWD with sky position & distance to map



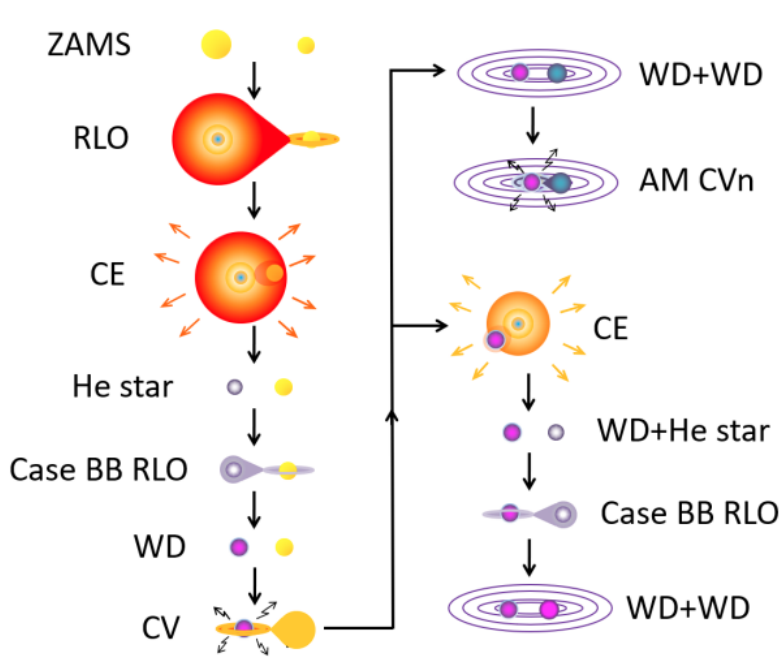
- Scale length of disk, bulge (halo) to few 10% accuracy (Adams+ '12, Korol+ '19, Wilhelm+ '20). Crude ( $\sim 300$  pc) but independent measurement from foreground (Benacquista+ '06, Breivik+ '20)
- Disk density profile & bar' axis length ratio & orientation angle. Spiral arms remain elusive (Wilhelm+ '20)

- Universal IMF? (Rebassa-Mansergas '19, Korol+ '20)
- (Local) star formation histories (Yu+ '10, Lamberts+ '19, Korol+ '20)
- (Satellite) Masses (Korol+ '21) from # of WD+WD
- Galactic mass from rotation curve with EM proper motion (Korol+ '17, Breivik+ '18, Korol+ '19)



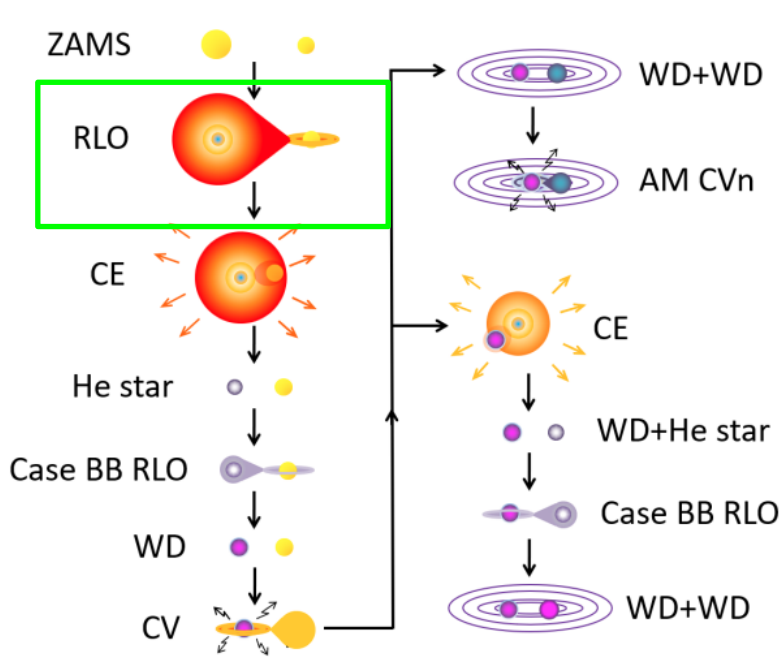
# Evolution in characteristic strain-frequency parameter space

An example of the evolutionary process leading to the formation of the most common double compact objects in the Milky Way: **detached double white dwarfs** (WD+WD) and **interacting double white dwarfs** (AM CVns).



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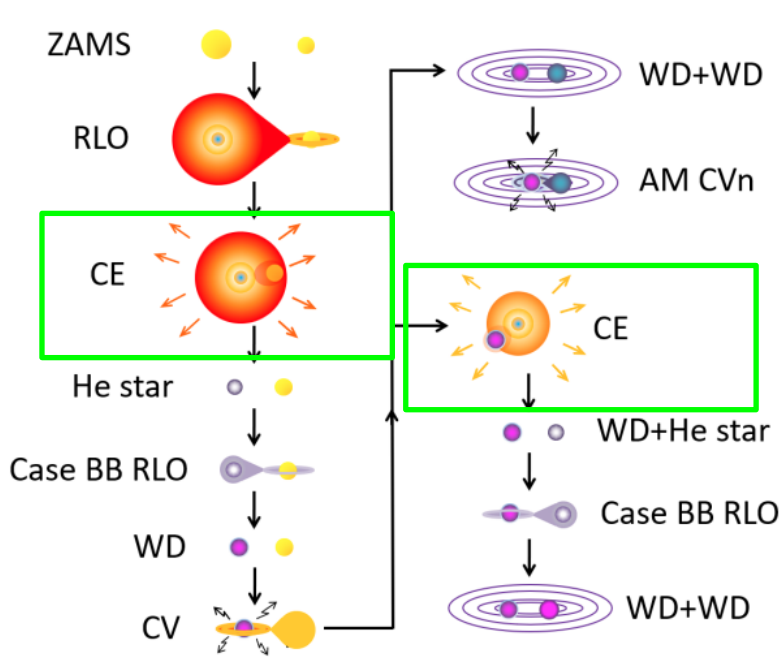
Tauris and van den Heuvel (2022), Amaro-Seoane et al. (2023)

- Stability of mass transfer, accretion efficiency during mass transfer
- Determines DWD mass ratios & chirp masses
- Recent work favours stable mass transfer (RLO) (Nelemans+ 01, Woods+ 12, Passy+ 12, Ge+ 15, Temmink+ 23, Li+ 23)

# Evolution in characteristic strain-frequency parameter space

Common envelope ejection (major uncertainty; Which systems eject the CE? What is the final orbital separation?)

- Indirect information from the LISA population
- Binaries 'born' in the LISA band
- Direct observations related to CE interaction



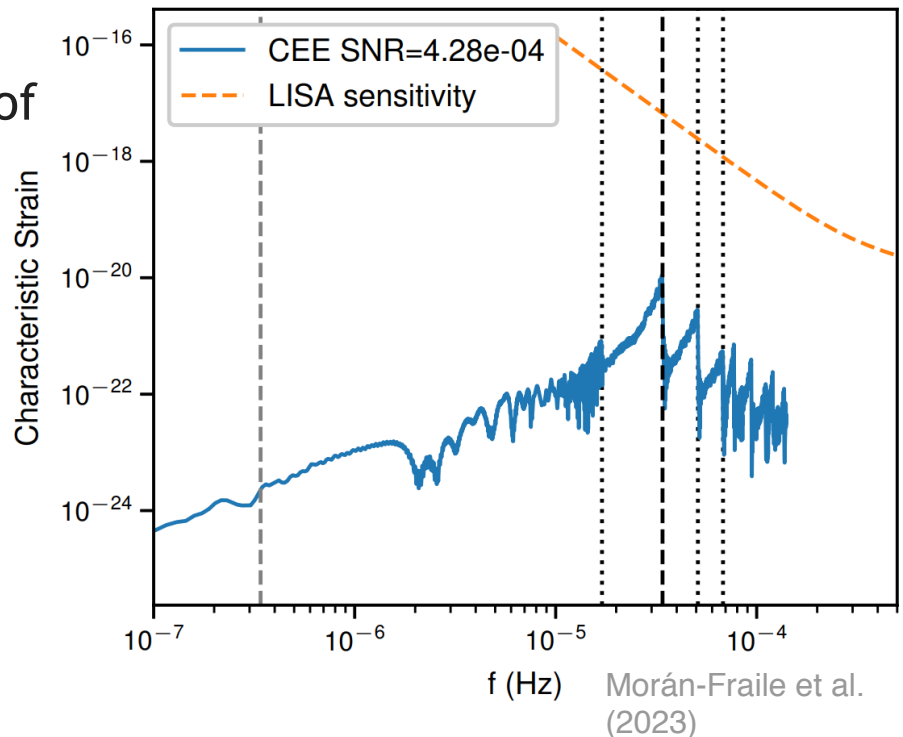


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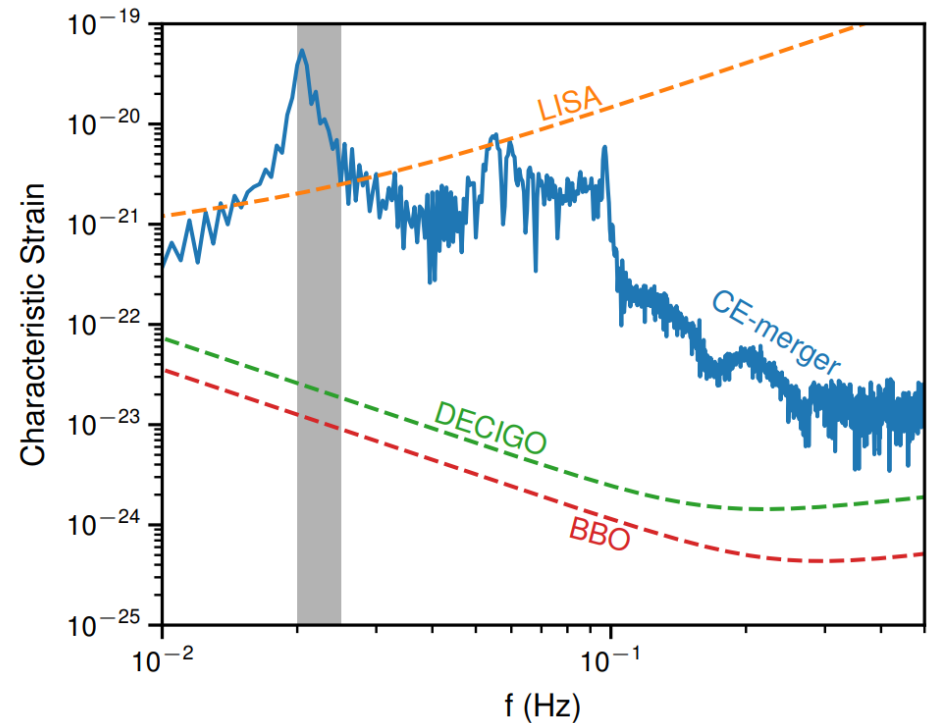
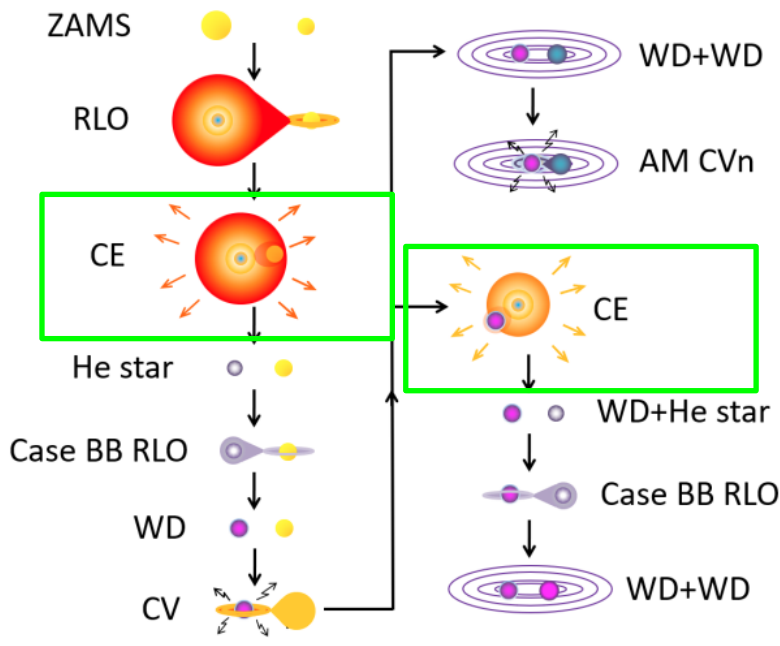
- Indirect information from the LISA population
- Binaries ‘born’ in the LISA band
- Direct observations related to CE interaction

- Typically: compact object spiralling in deeply in envelope of giant with compact core
- Unlikely to see initial plunge-in, at most 1 per few centuries (Ohlmann+ '16, Ginat+ '20)
- Better chances for the slow thermal phase:  $\sim 0.1$ -100 in MW during LISA mission (Renzo+ '21)



# Evolution in characteristic strain-frequency parameter space

A non-successful common-envelope ejection leads to a merger in the deci-Hz band

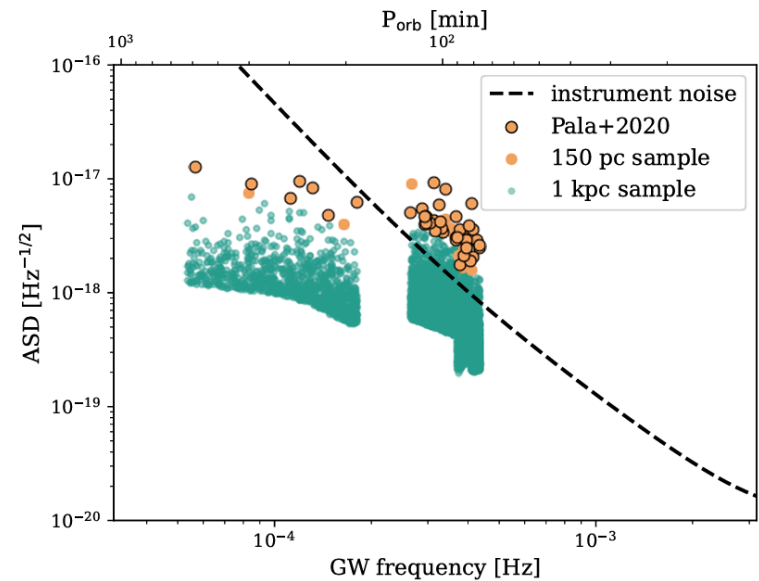
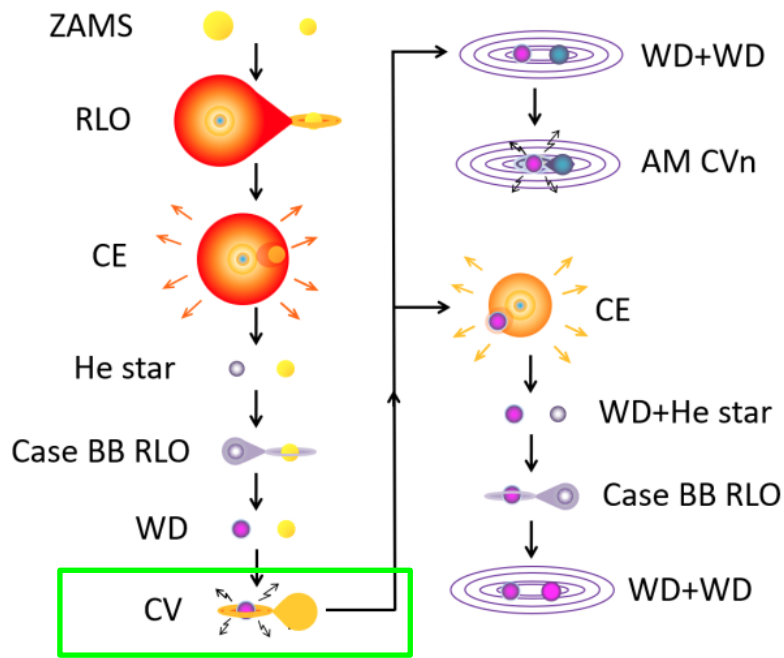


Tauris and van den Heuvel (2022), Amaro-Seoane et al. (2022)

Morán-Fraile et al. (2023)  
Signal last  $\sim$  few 1000s sec

# Evolution in characteristic strain-frequency parameter space

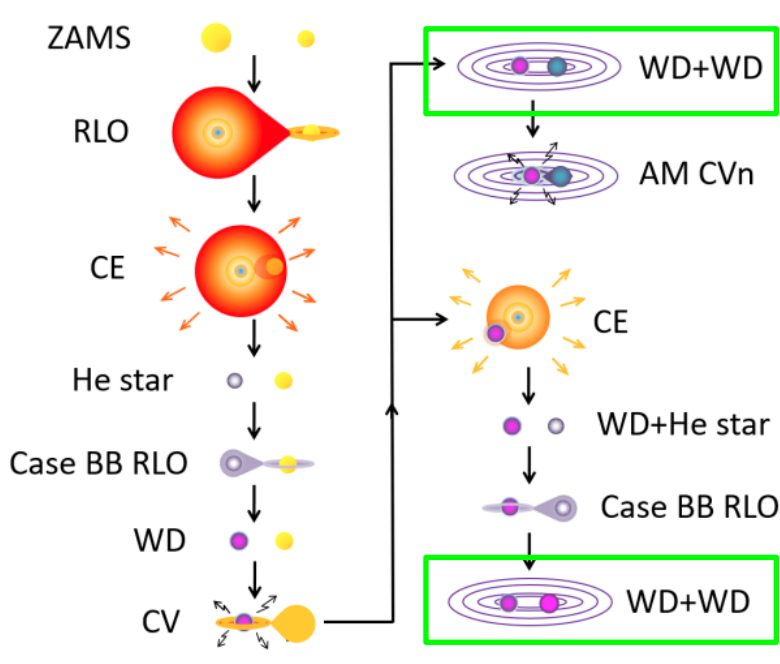
Scaringi et al. (2023) have recently shown that known Cataclysmic Variables (CVs) may be detectable by LISA. CVs pile up at  $\sim 0.3$  milli-Hz (reaching their orbital period minimum) to produce a spike in the Galactic foreground.



Tauris and van den Heuvel (2022), Amaro-Seoane et al. (2023)

# Evolution in characteristic strain-frequency parameter space

- WD+WDs are the predominant GW emitters in the milli-Hertz regime. Other phases capable of producing detectable GW signals, such as CE, CV, etc., are significantly rarer, by orders of magnitude.
- In fact, according to our current understanding of WD+WDs, evolution through a common envelope phase—bypassing the cataclysmic variable stage—is more likely.

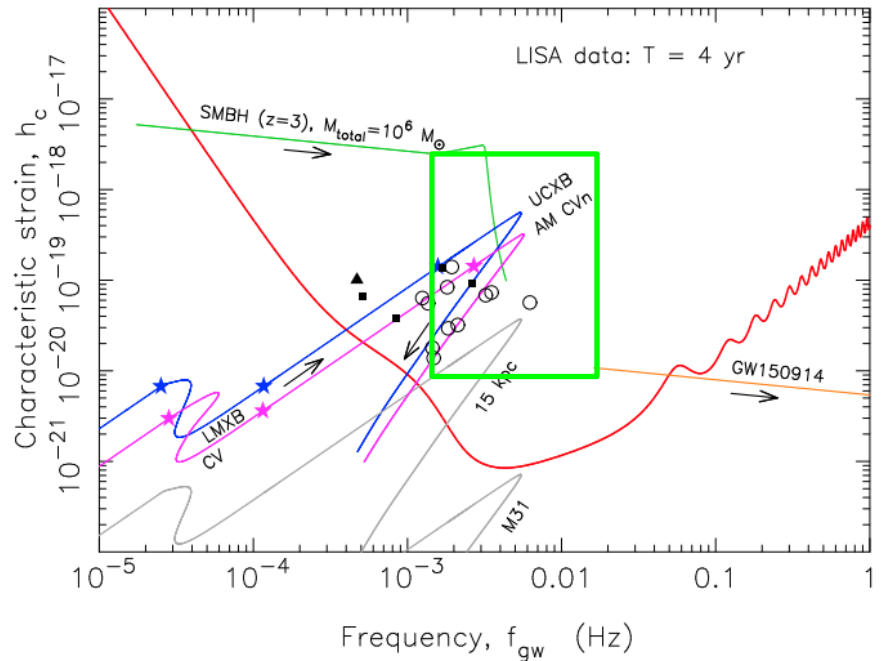
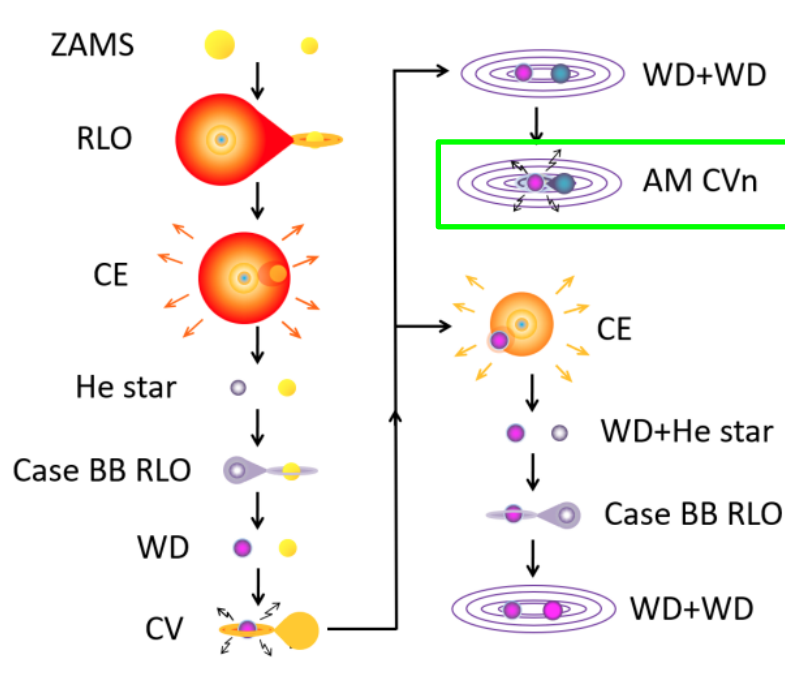


Tauris and van den Heuvel (2022), Amaro-Seoane et al. (2023)



# Evolution in characteristic strain-frequency parameter space

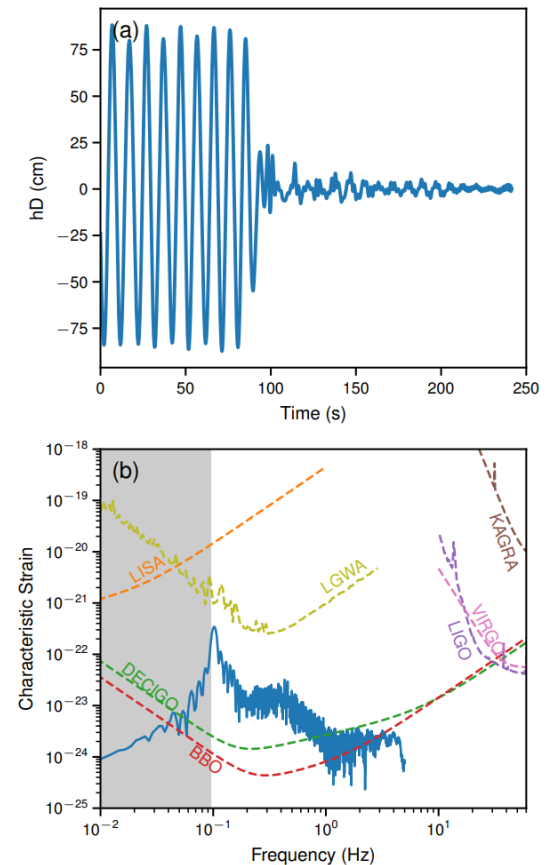
AM CVns are amongst the shortest period binaries that we know of from electromagnetic observations. Can be distinguished from detached (non-interacting) WD+WD because of the negative chirp.



Tauris and van den Heuvel (2022), Amaro-Seoane et al. (2023)

# Evolution in characteristic strain-frequency parameter space

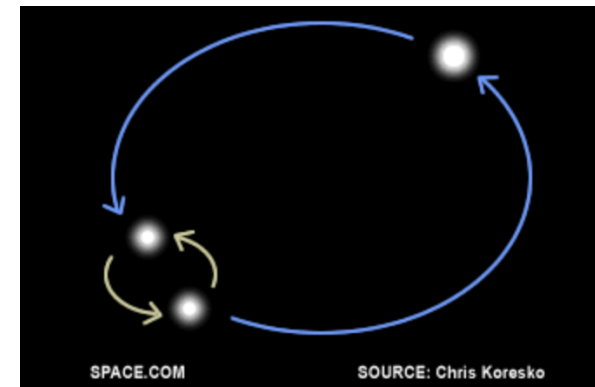
- Binaries without extreme mass ratios fail to establish stable accretion, resulting in mergers
- Mergers of WD+WD may result in thermonuclear transients, and mergers of massive WD+WD may result in bright Type Ia supernovae
- Indirect GW constraints on Galactic merger rates
  - ~500 compact superchandraskhar DWDs (Ruiter+ '10, Rebaasa-Mansergas+ '19)



An example of a NS + WD merger from Morán-Fraile et al. (2023)

# Triples and other multiples

- Common: For every 3 binaries, there is at least 1 triple (Tokovinin+ '08, Moe+ '17)



Visible in LISA through:

- Eccentricity variations from three-body dynamics (Hoang+ '19)
- Doppler frequency modulation (Robson+ '18, Tamanini & Danielski '19, Tamanini+ '20)
- ➔ The sensitivity of LISA will be able to detect DWDs companions with masses down to  $\sim M_J$  (Danielski+ '19)
- Detectable out to LMC! (Danielski & Tamanini '20)
- Early estimates: 3-83 circumbinary exoplanets, and 14-2218 circumbinary brown dwarfs (Danielski+ '19)
- Preliminary results with full triple calculations with TRES (Toonen+ 16, 20),  $\sim 20\%$  of DWDs manage to retain their planets (Columba, Danielski, Toonen, Dorozsmai in prep. )

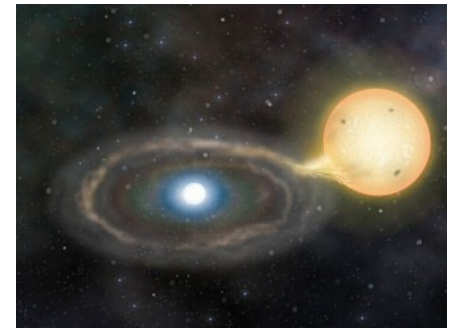
# Detecting stellar binaries and multiples with GWs

A key science objective and most abundant observable sources for current & planned GW detectors. The only guaranteed sources!

- Primary population: Galactic compact binaries with  $P_{\text{orb}} \lesssim 60$  mins

Not all of them will be resolved.

- Rich physics constraints to Stellar & binary evolution theories



- Strong synergies with: -> See Thomas Kupfer's talk
  - Electromagnetic observatories to enhance measurement precision
  - Among GW detectors for multiband observations (primarily binary black holes)



# Scientific return is immense

## **Unprecedented Survey of Galactic Stellar Content**

- Nearly half of all stars in the Milky Way are in binaries. GWs offer a unique, independent messenger to explore the Milky Way's stellar content.

## **Direct Access to Electromagnetically Dark Companions**

- GWs grant direct insight into binaries consisting of electromagnetically dark companions, such as white dwarfs, neutron stars, and black holes, which are often challenging to detect through traditional electromagnetic methods.

## **Enhancing Understanding of Binary Evolution**

- Significantly advances in our knowledge of binary evolution are anticipated from GW astronomy, shedding light on critical processes such as mass transfer, loss of mass and angular momentum, and the outcomes of mergers.

## **A Guaranteed Multi-Messenger Link**

- Inspiralling and merging Galactic compact binaries guarantee a multi-messenger connection from micro-Hz to deci-Hz frequencies, bridging the gap between mergers and their progenitors.