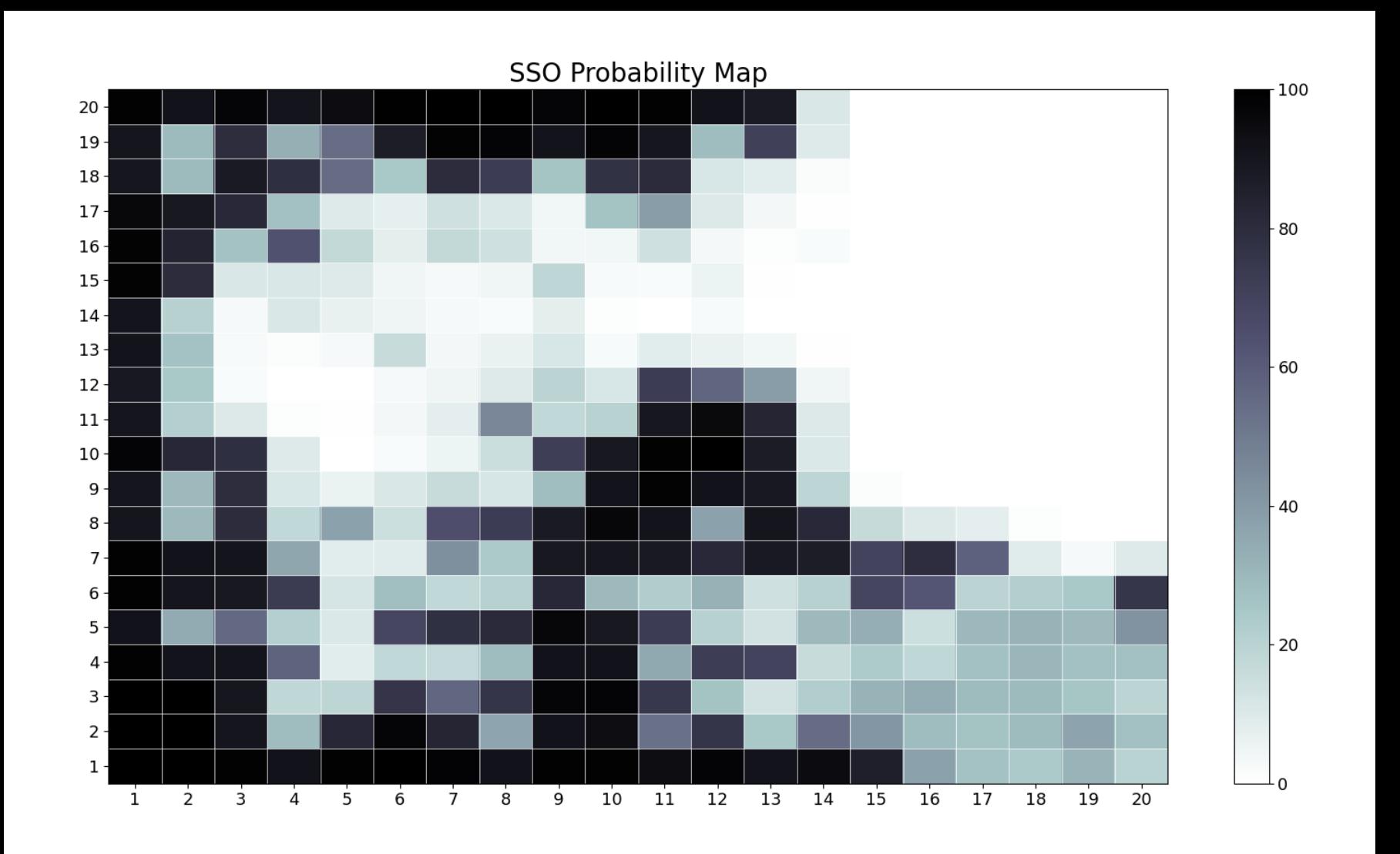


Early-stopping SOMs as a tool to classify SSOs in space surveys

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SOM: How Does It Work

- $Q = N M$ neurons organized in a rectangular lattice, with coordinates (i, j) with $(i = 0, \dots, N - 1, j = 0, \dots, M - 1)$
- Each neuron associated to a reference vector r_k with K values and is exposed to an input vector w_k coming from a training dataset with L inputs
- How does a neuron win? By minimizing the Euclidean distance:

$$D_{\min}^l = \min_{i,j} \left(\sqrt{\sum_{k=0}^{K-1} m_k^l (r_k^{i,j} - w_k^l)^2} \right)$$

- After a full epoch, iterative process by updating neuron components:

$$r_k'^{i,j} = r_k^{i,j} + \alpha \left(\frac{t}{N_e} \right) H \left(\frac{t}{N_e}, d_{win} - d \right) (w_k^l - r_k^{i,j})$$

- The parameters $\alpha(t)$ and $\sigma(t)$ can either be linearly or exponentially decreasing with the passing epochs.

Early stopping

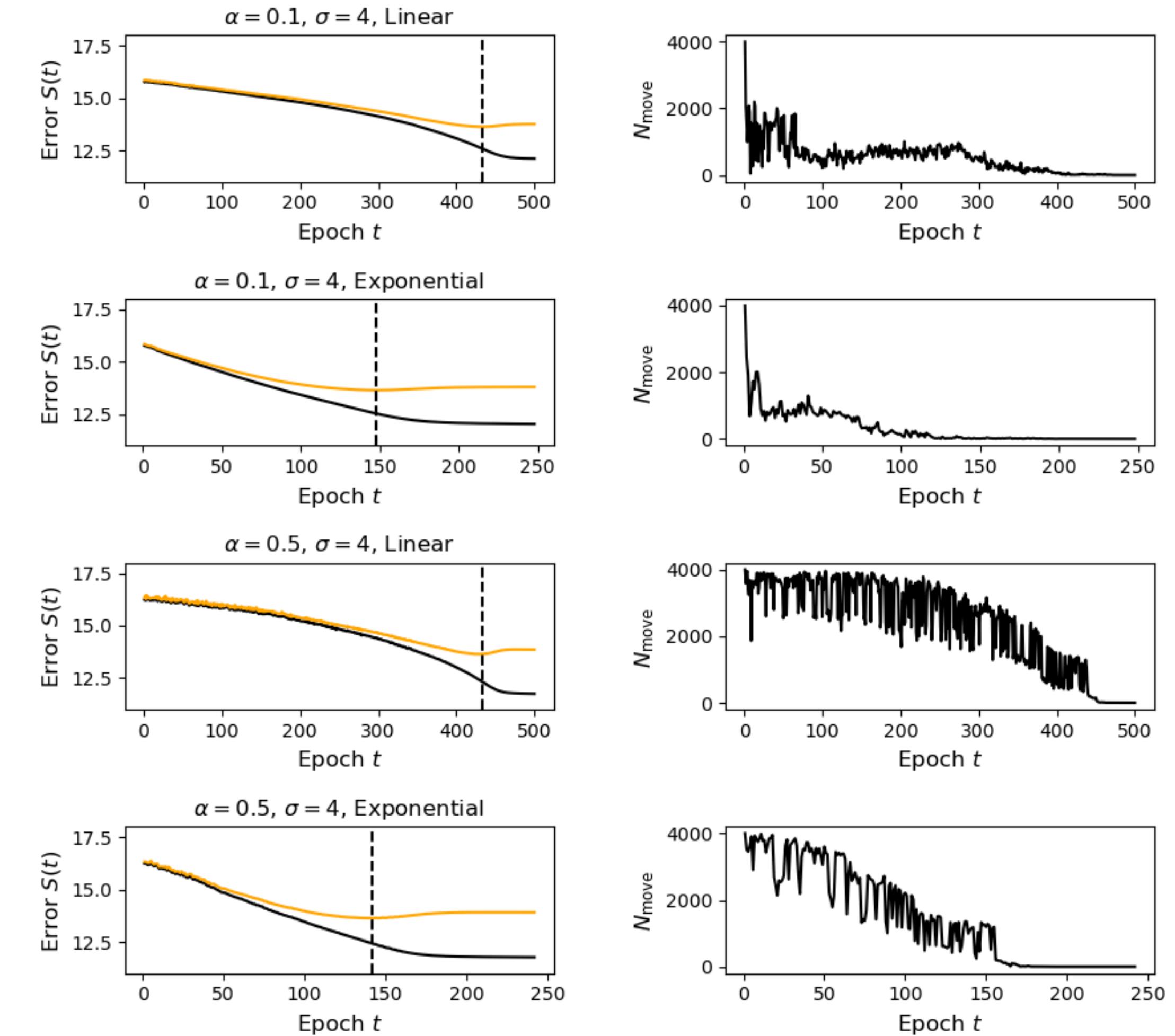
- Using N_e , process can be long and time (and memory!) consuming, and eventually produce over-fitting
- Solution: check performance of the SOM on an independent, randomly chosen validation dataset
- Metric:

$$S(t) = \frac{\sum_{l=0}^{L-1} D_{\min}^l}{L}$$

- Expected behavior: $S(t)$ will continuously decrease, $S_{val}(t)$ will reach a minimum and trend upward (overfitting!)
- By stopping the learning process before the overfitting stage, the SOM will maintain its capability to classify new data.

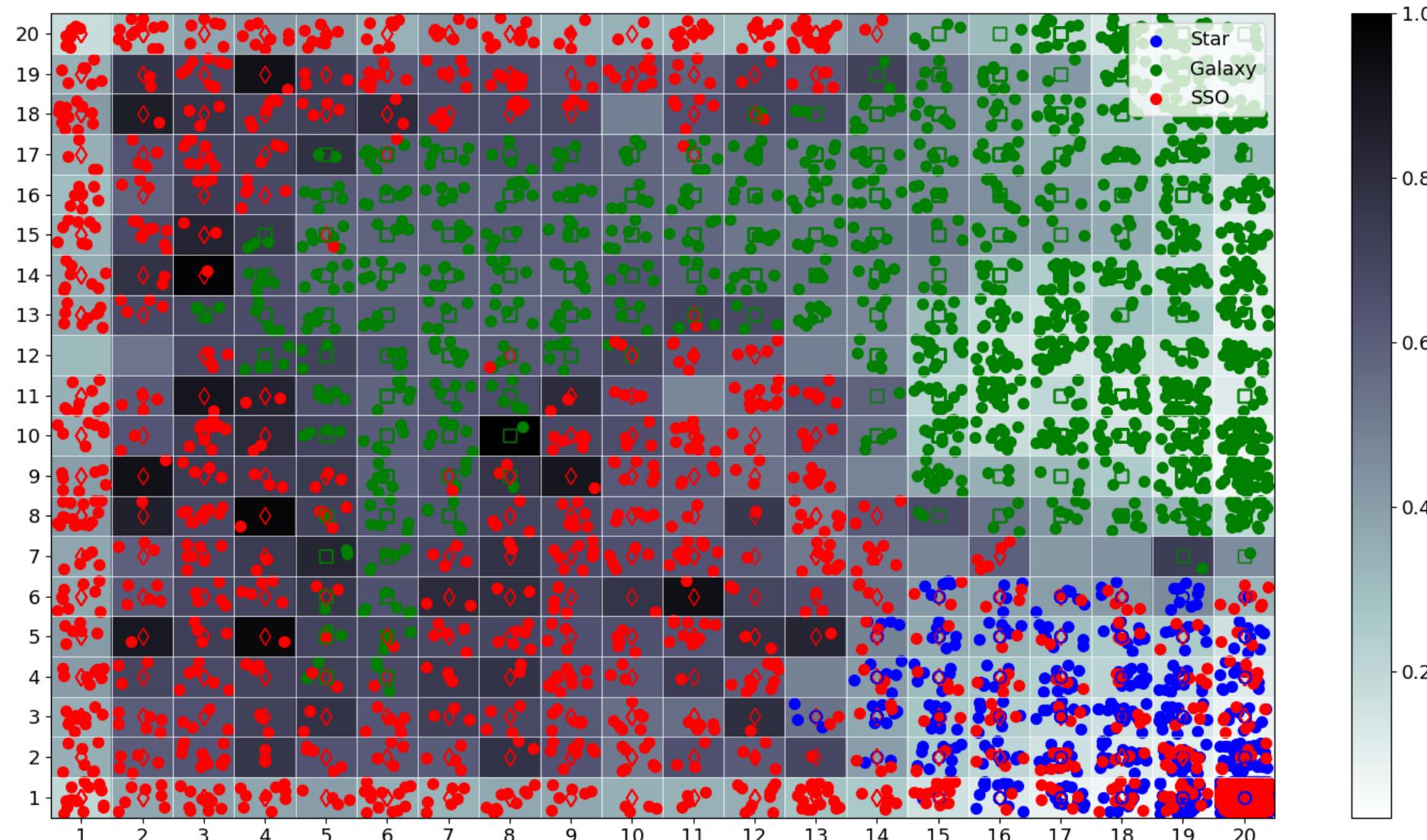
Training the SOM

- 4000 random 101x101 images → 20x20 neurons
- Comparing errors and numbers of movements for different models and parameters:
- Results: exponential, $\alpha = 0.5$, $\sigma = 4$

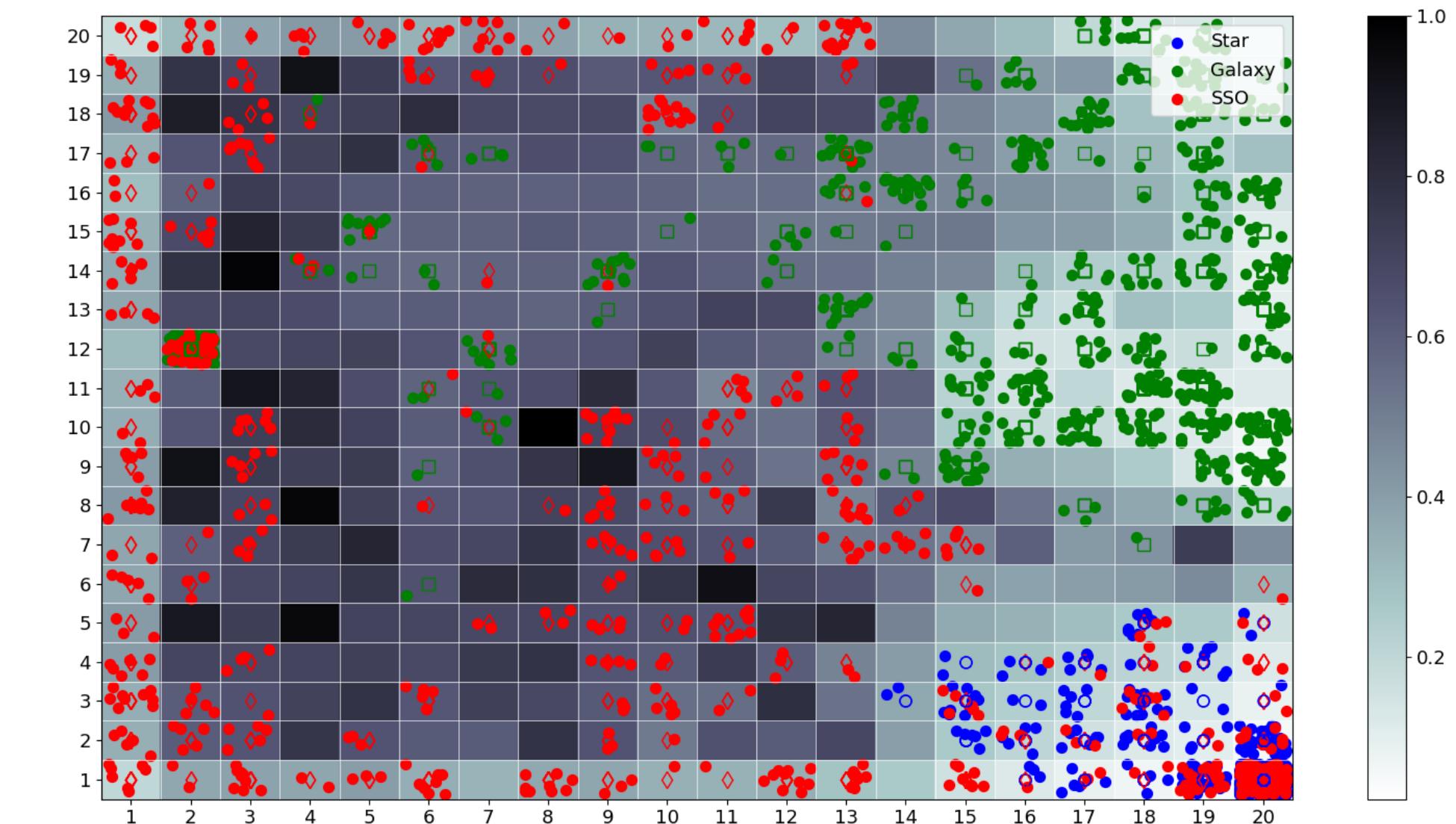


Training the SOM

- U-matrix generated from SOM training:

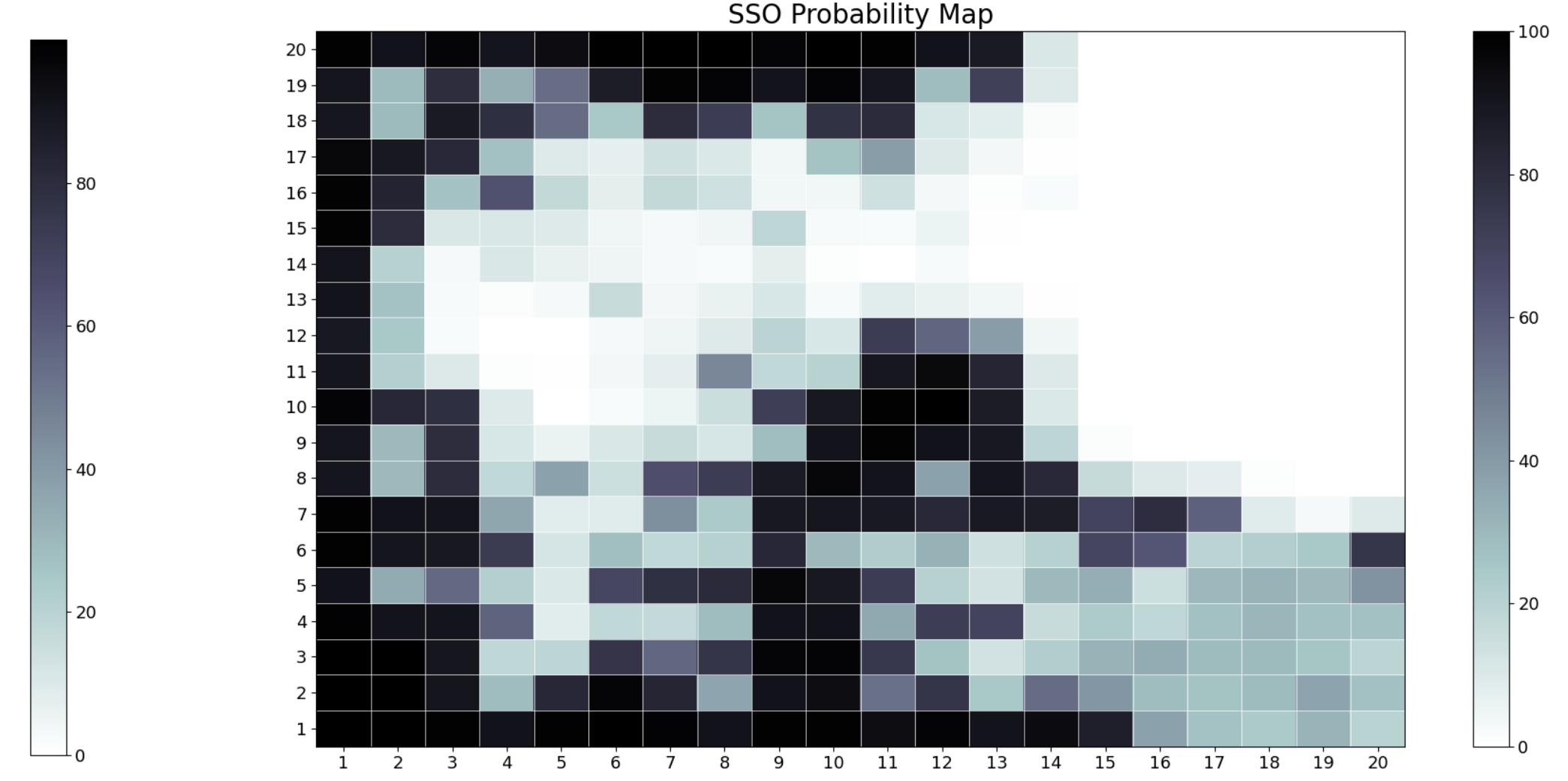
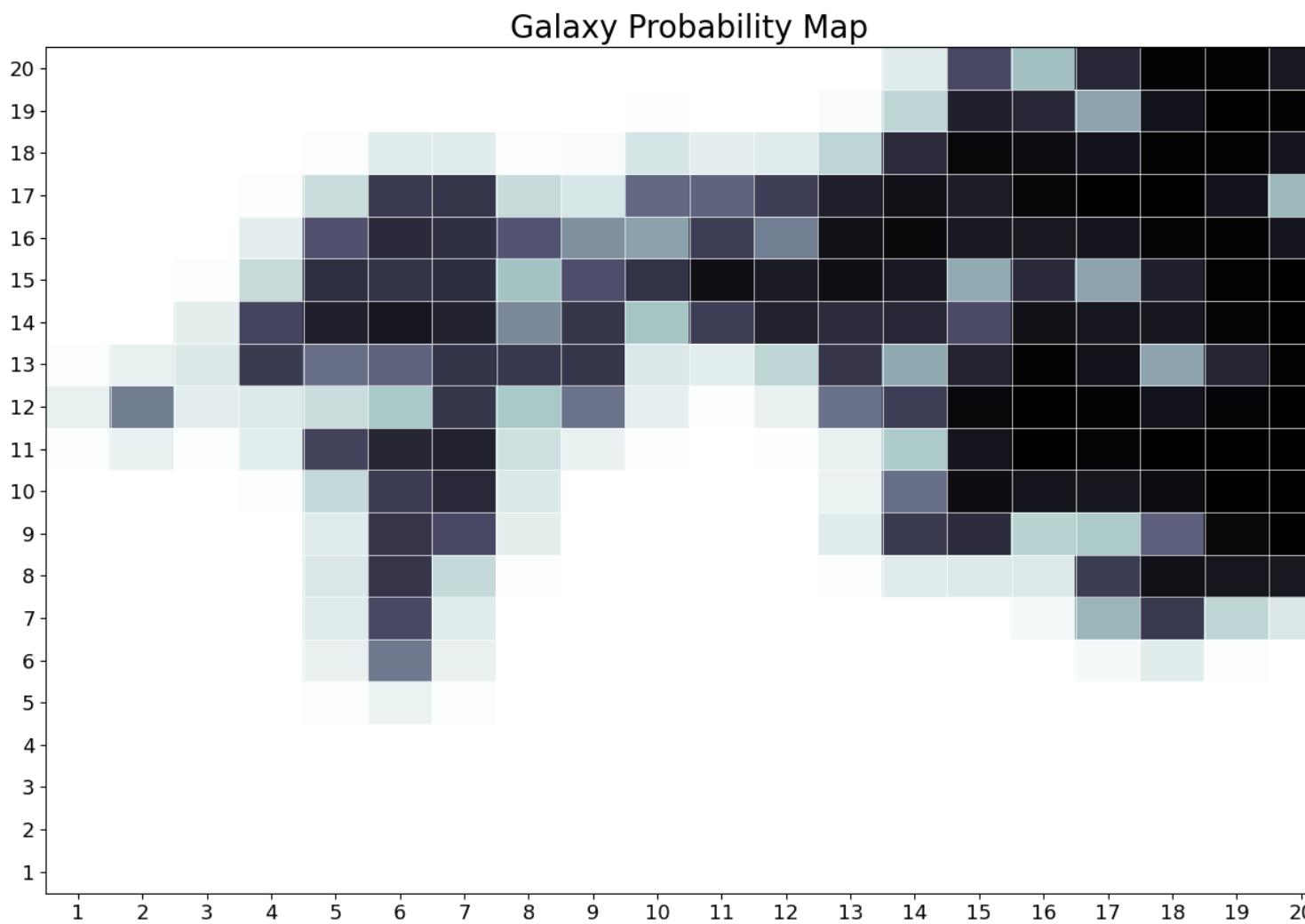
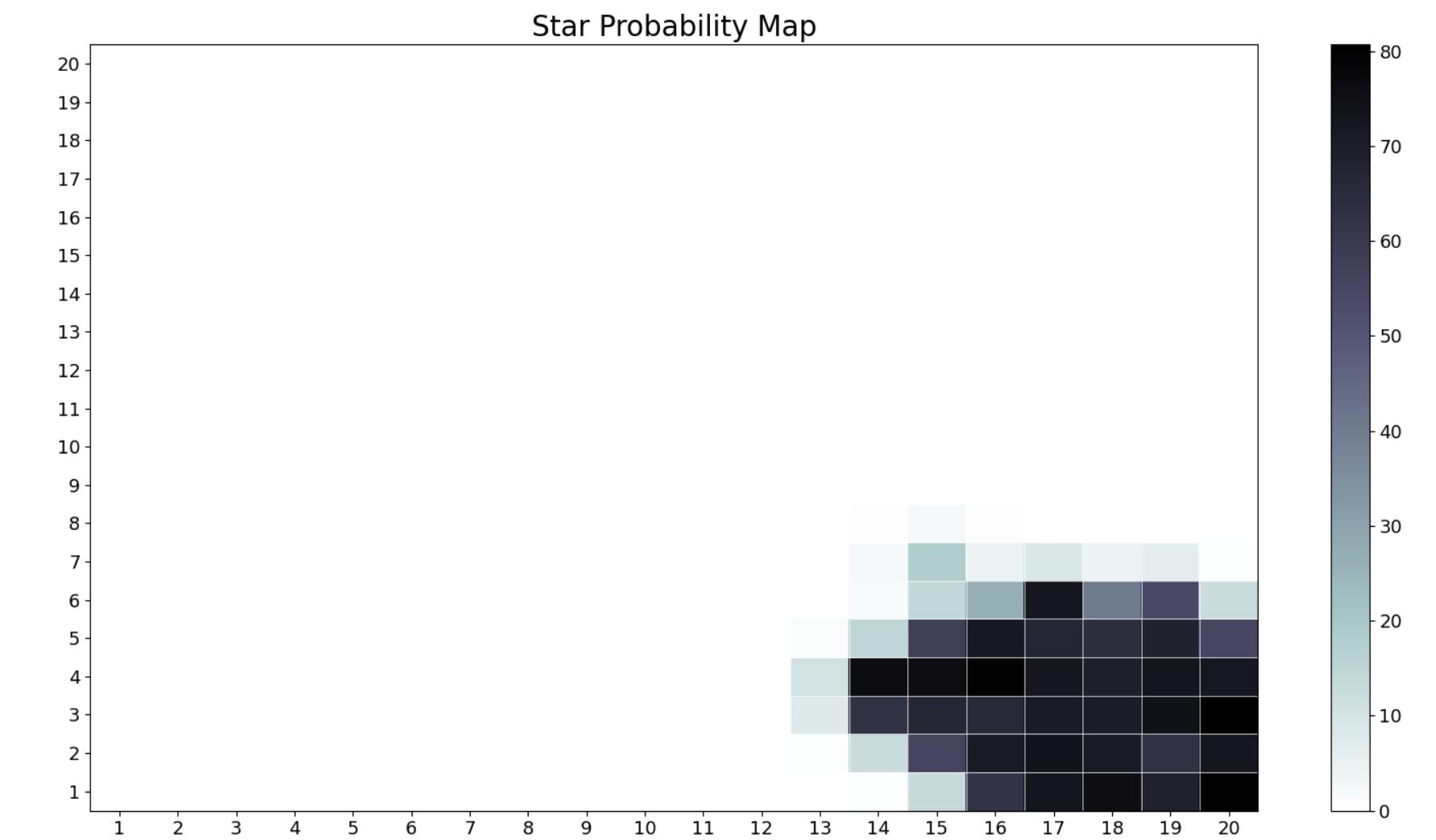


- U-matrix with 2000 images from test dataset:



Results

- Quality assessment with 10^4 images, bins
0-3''/h, 3-6''/h, 6-10''/h
- Purity: 11%, 100%, 100%
- Completeness: 51%, 48%, 60%



Conclusions

- Early-stopping is a powerful technique to improve SOMs
- With proper parameters, stopping time is more than halved
- Relatively high accuracy above $1''/\text{h}$ (slow moving SSOs are undistinguishable from stars!)
- Difference between simulated and authentic images: more training is needed for real survey data