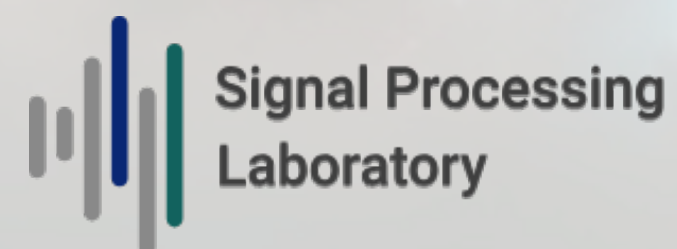


# Self-supervised deep learning for component separation in the submillimeter sky

Victor Bonjean

with Nabila Aghanim, Marian Douspis, Tony Bonnaire, and Hideki Tanimura

ML4ASTRO2 - Catania - 11/07/2024



Funded by  
the European Union

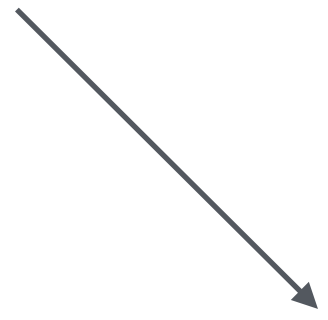
What is component separation?

What is component separation?

$$X = S_0 + S_1 + S_2$$

What is component separation?

Observation



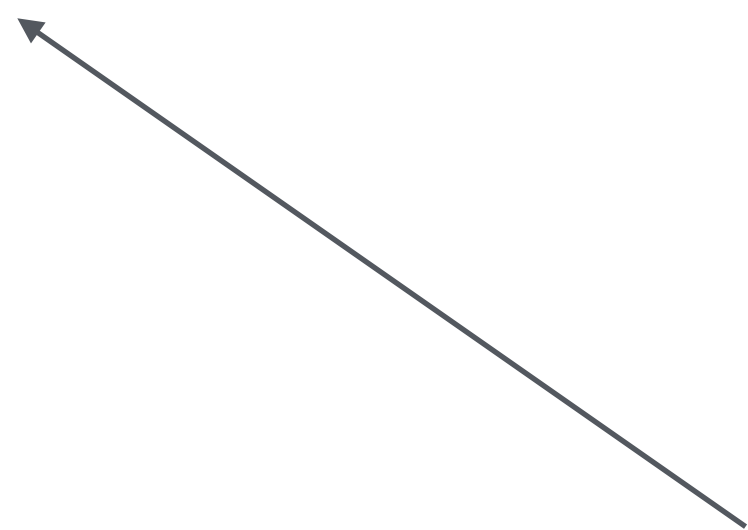
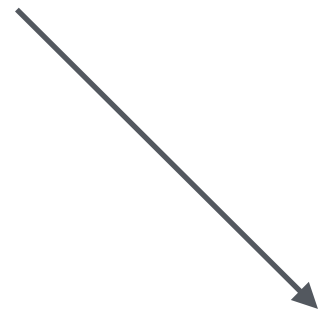
$$X = S_0 + S_1 + S_2$$

What is component separation?

Observation

$$X = S_0 + S_1 + S_2$$

3 components



What is component separation?

Observation

Multiple frequencies

$$X_i = a_i.S_0 + b_i.S_1 + c_i.S_2$$

3 components

What is component separation?

$$\begin{pmatrix} X_0 \\ X_1 \\ \dots \\ X_n \end{pmatrix} = \begin{pmatrix} a_0 & b_0 & c_0 \\ a_1 & b_1 & c_1 \\ \dots & \dots & \dots \\ a_n & b_n & c_n \end{pmatrix} \cdot \begin{matrix} S_0 \\ S_1 \\ S_2 \end{matrix}$$

n frequencies

What is component separation?

$n \times 3$ : « **Mixing matrix** »

$$\begin{pmatrix} X_0 \\ X_1 \\ \dots \\ X_n \end{pmatrix} = \begin{pmatrix} a_0 & b_0 & c_0 \\ a_1 & b_1 & c_1 \\ \dots & \dots & \dots \\ a_n & b_n & c_n \end{pmatrix} \cdot \begin{pmatrix} S_0 \\ S_1 \\ S_2 \end{pmatrix}$$

$n$  frequencies



What is component separation?

$$\mathbf{X} = \mathbf{A} \cdot \mathbf{S}$$

What is component separation?

$$\mathbf{X} = \mathbf{A} \cdot \mathbf{S}$$

1. We know  $\mathbf{A}$

« No problem »

$$\mathbf{S} = \mathbf{A}^{-1} \cdot \mathbf{X}$$

- Never the case

# What is component separation?

$$\mathbf{X} = \mathbf{A} \cdot \mathbf{S} + \mathbf{N}$$

Blind Source Separation (BSS)

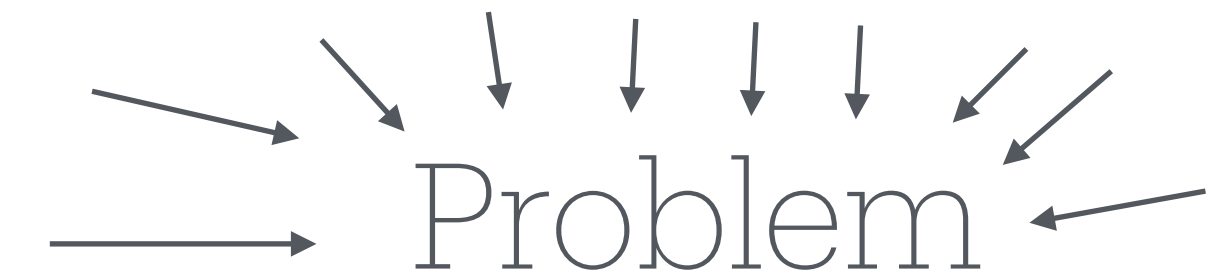
1. We know  $\mathbf{A}$

« No problem »

$$\mathbf{S} = \mathbf{A}^{-1} \cdot \mathbf{X}$$

- Never the case

2. We don't know  $\mathbf{A}$



- FastICA → Prior on S
- GMCA
- Unsupervised Learning

# What is component separation?

$$\mathbf{X} = \mathbf{A}\mathbf{S} + \mathbf{N}$$

Blind Source Separation (BSS)

1. We know  $\mathbf{A}$

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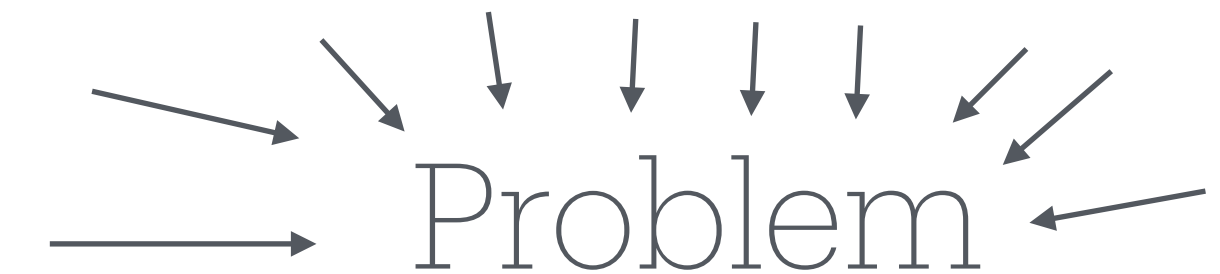
- Never the case

1.5. We know a bit of  $\mathbf{A}$

Problem

- ILC
- GMCA
- Self-supervised Learning
- Template based fitting  
→ Prior on  $\mathbf{A}$

2. We don't know  $\mathbf{A}$



- FastICA → Prior on  $\mathbf{S}$
- GMCA
- Unsupervised Learning

# What is component separation?

$$\mathbf{X} = \mathbf{A}\mathbf{S} + \mathbf{N}$$

Blind Source Separation (BSS)

## 1. We know $\mathbf{A}$

« No problem »

$$\mathbf{S} = \mathbf{A}^{-1}\mathbf{X}$$

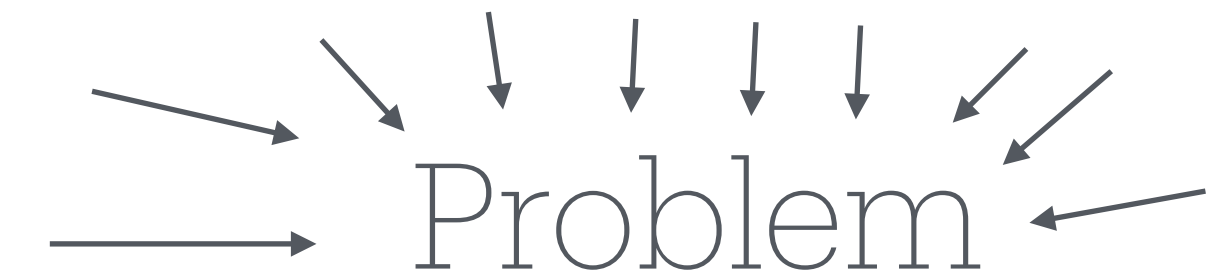
- Never the case

## 1.5. We know a bit of $\mathbf{A}$

Problem

- ILC
- GMCA
- **Self-supervised Learning** ✓
- Template based fitting  
→ Prior on  $\mathbf{A}$

## 2. We don't know $\mathbf{A}$



- FastICA → Prior on  $\mathbf{S}$
- GMCA
- **Unsupervised Learning** ✓

# What is component separation?

$$\mathbf{X} = \mathbf{A} \cdot \mathbf{S} + \mathbf{N}$$

Blind Source Separation (BSS)

1. We know **A**

« No problem »

$$\mathbf{S} = \mathbf{A}^{-1} \cdot \mathbf{X}$$

- Never the case

1.5. We know a bit of **A**

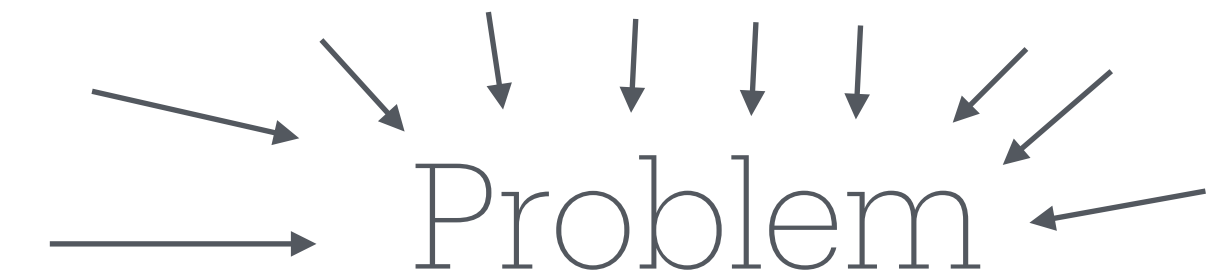
Problem

- ILC
- GMCA
- **Self-supervised Learning**
- Template based fitting

→ Prior on A

1.75 My work

2. We don't know **A**



- FastICA
  - GMCA
- Prior on S

**Unsupervised Learning**



# Component separation with deep learning

# Component separation with deep learning

## Deep Image Prior (DIP) and « Double-DIP »

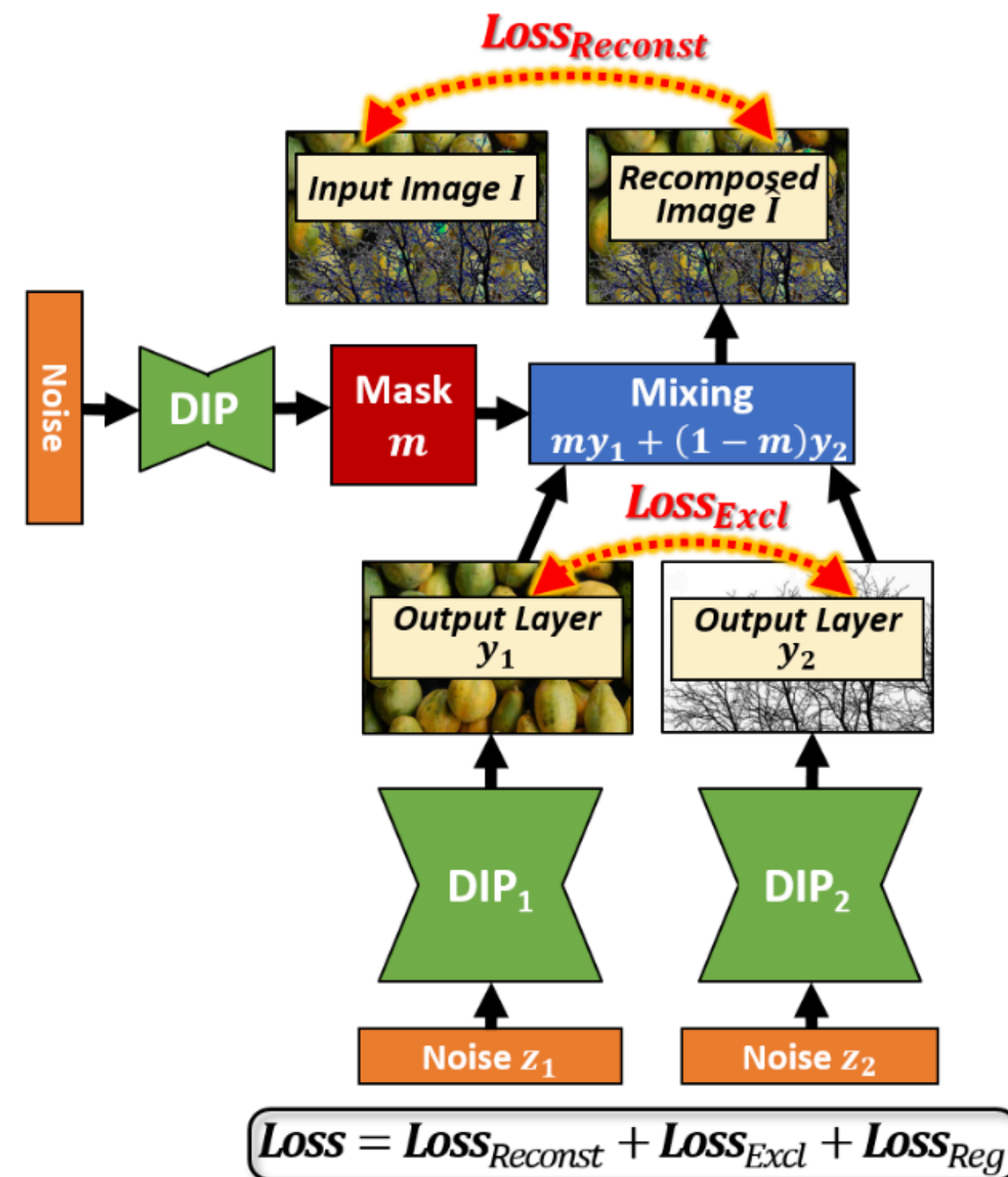


Figure 2: **Double-DIP Framework.** Two Deep-Image-Prior networks ( $DIP_1$  &  $DIP_2$ ) jointly decompose an input image  $I$  into its layers ( $y_1$  &  $y_2$ ). Mixing those layers back according to a learned mask  $m$ , reconstructs an image  $\hat{I} \approx I$ .



# Component separation with deep learning

## Deep Image Prior (DIP) and « Double-DIP »

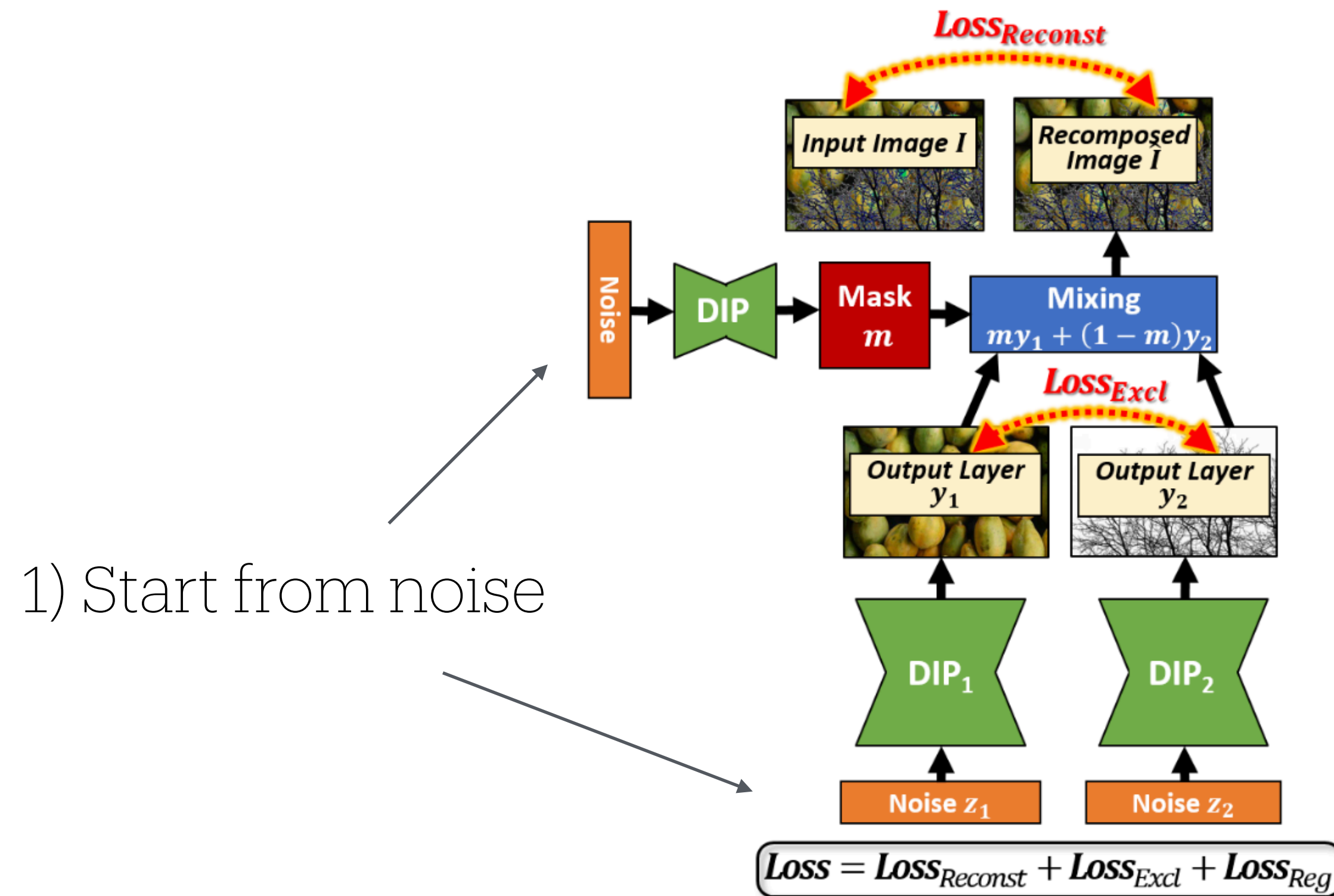


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# Component separation with deep learning

## Deep Image Prior (DIP) and « Double-DIP »

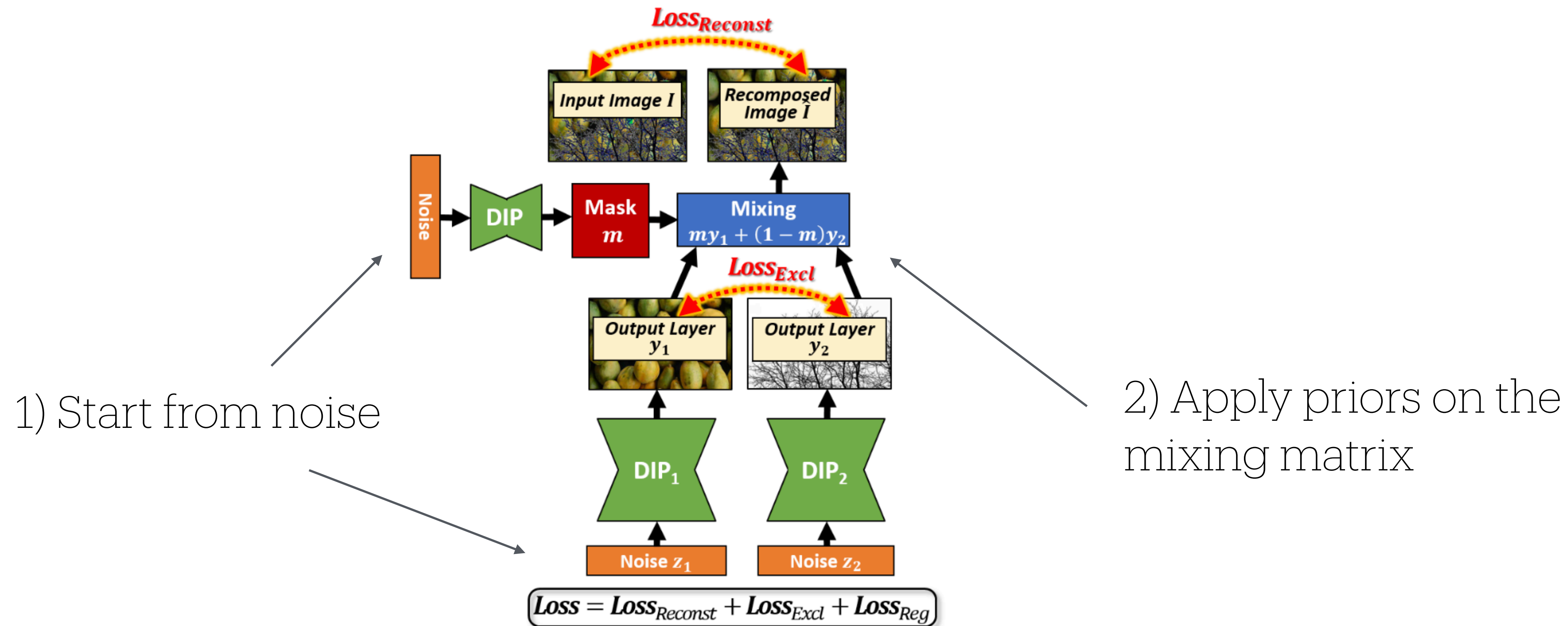


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# Component separation with deep learning

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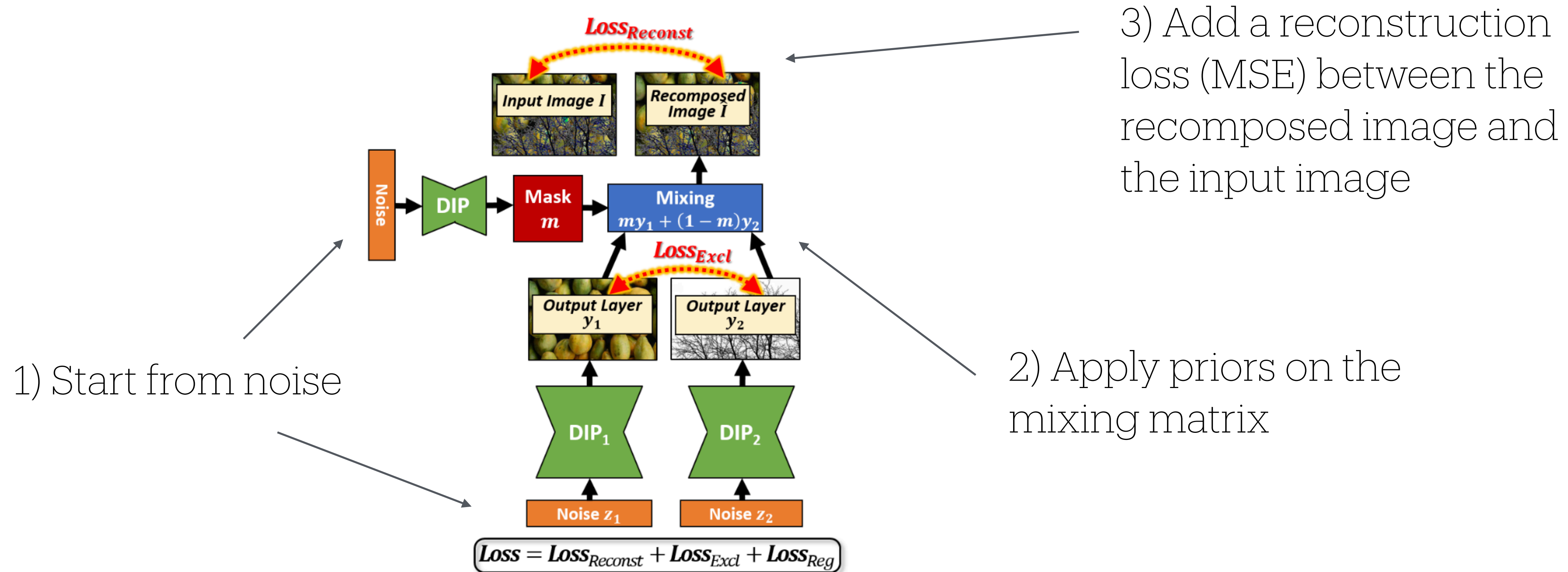


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# Component separation with deep learning

« Double-DIP »

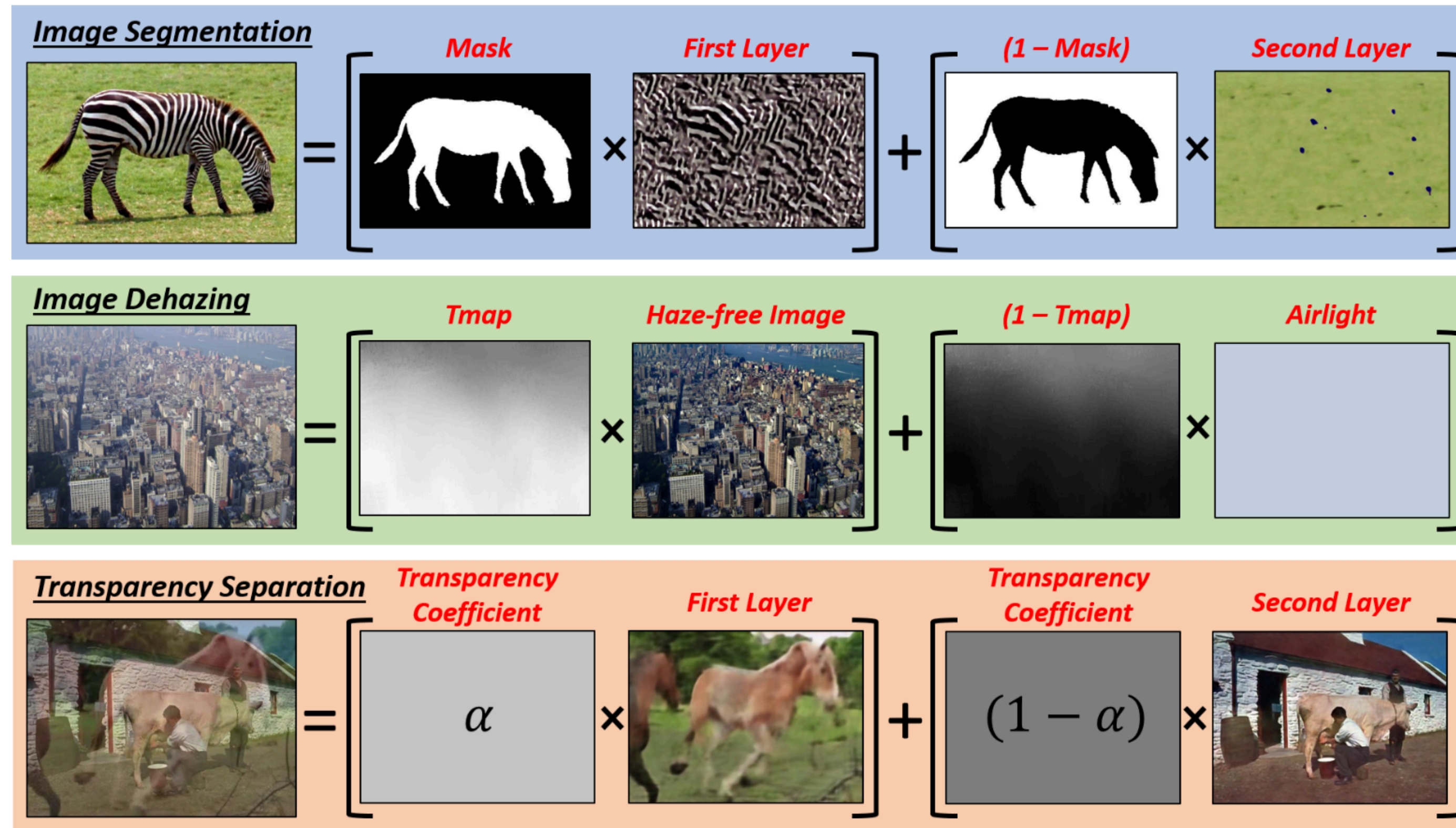
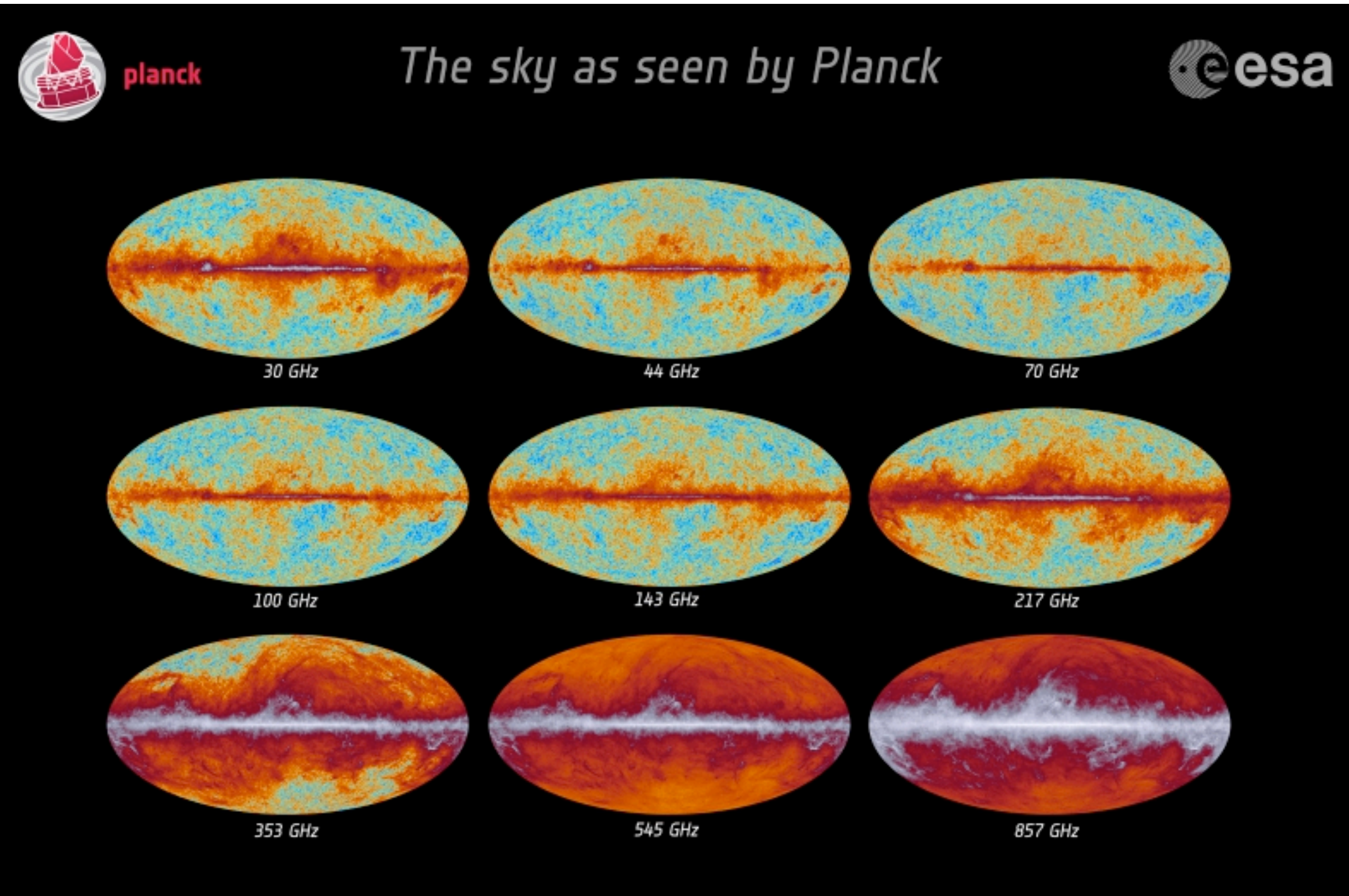
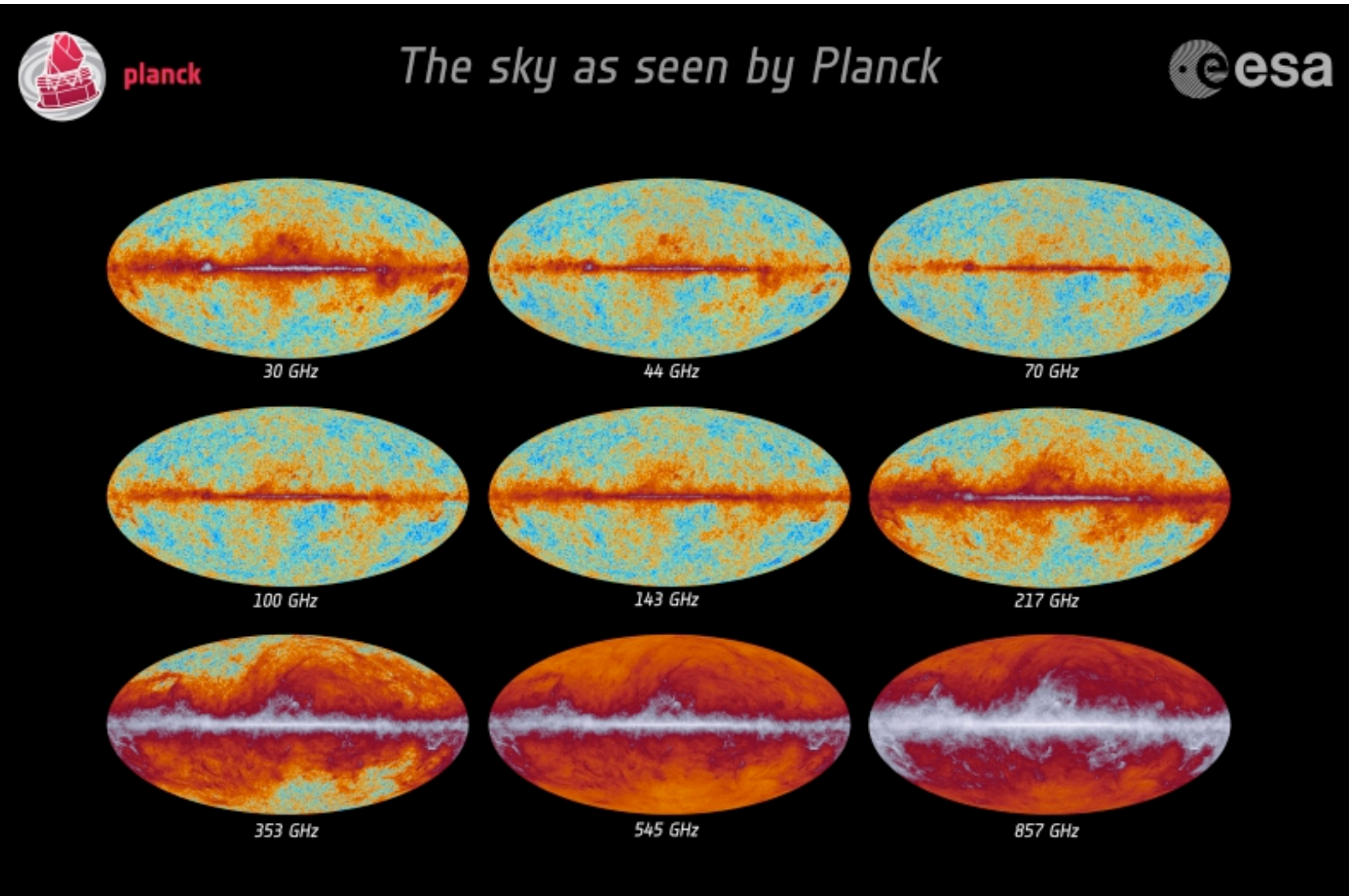


Figure 1: **A unified framework for image decomposition.** An image can be viewed as a mixture of “simpler” layers. Decomposing an image into such layers provides a unified framework for many seemingly unrelated vision tasks (e.g., segmentation, dehazing, transparency separation). Such a decomposition can be achieved using “Double-DIP”.

# An application to CMB data - CIB removal - SZ extraction

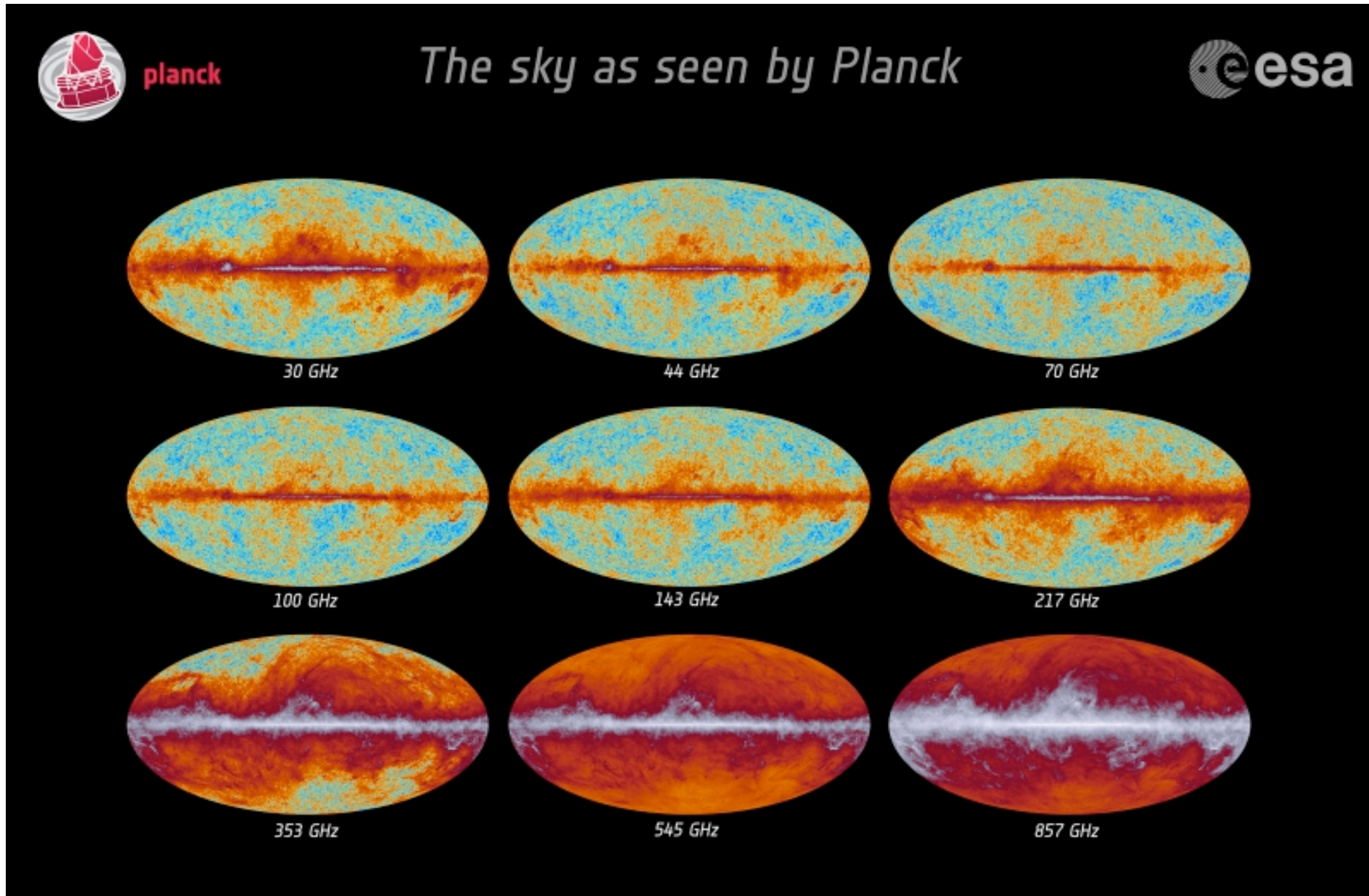


# An application to CMB data - CIB removal - SZ extraction

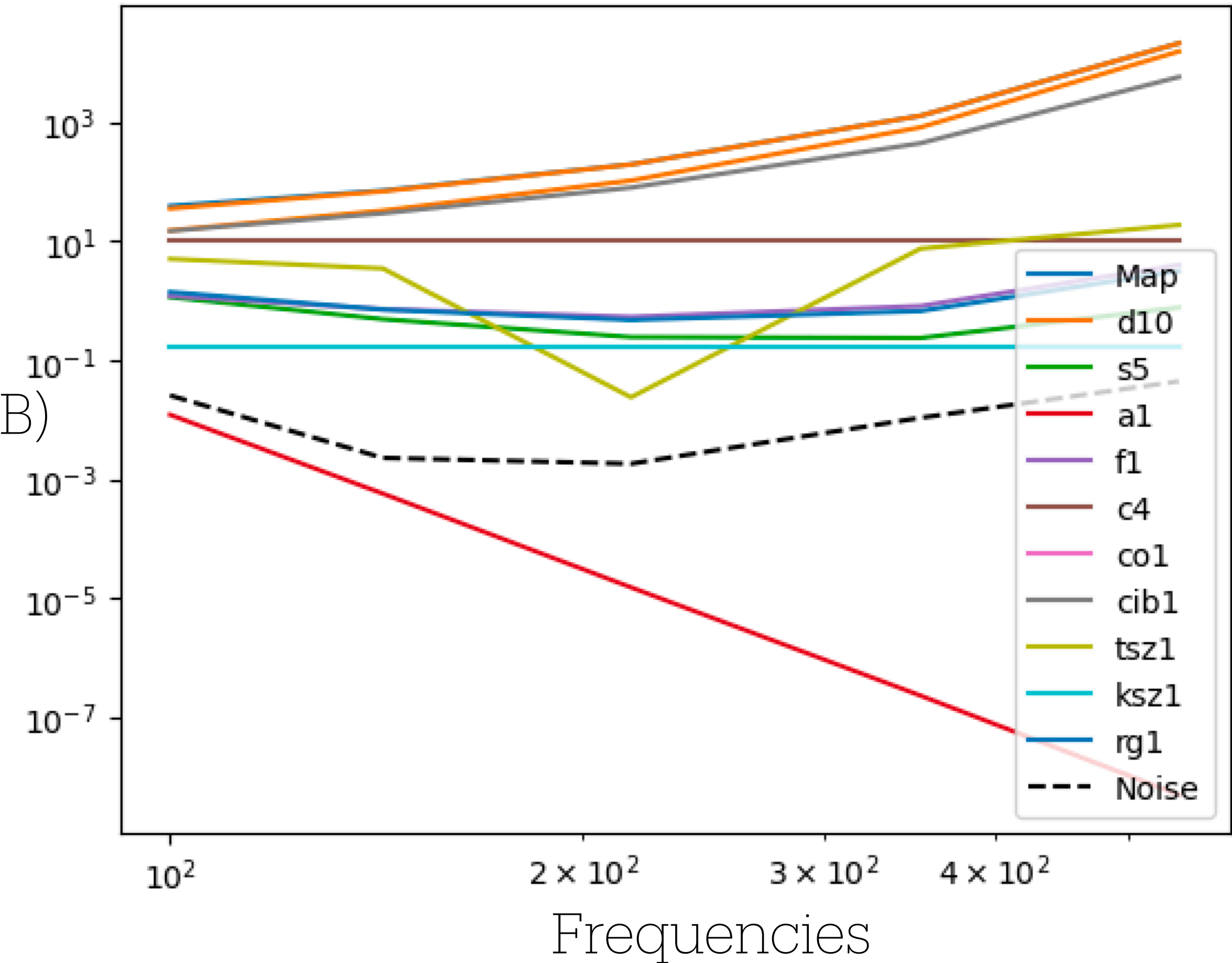


CMB, tSZ, kSZ, CIB, Radio sources, CO,  
Free-free, Synchrotron and Galactic dust

# An application to CMB data - CIB removal - SZ extraction

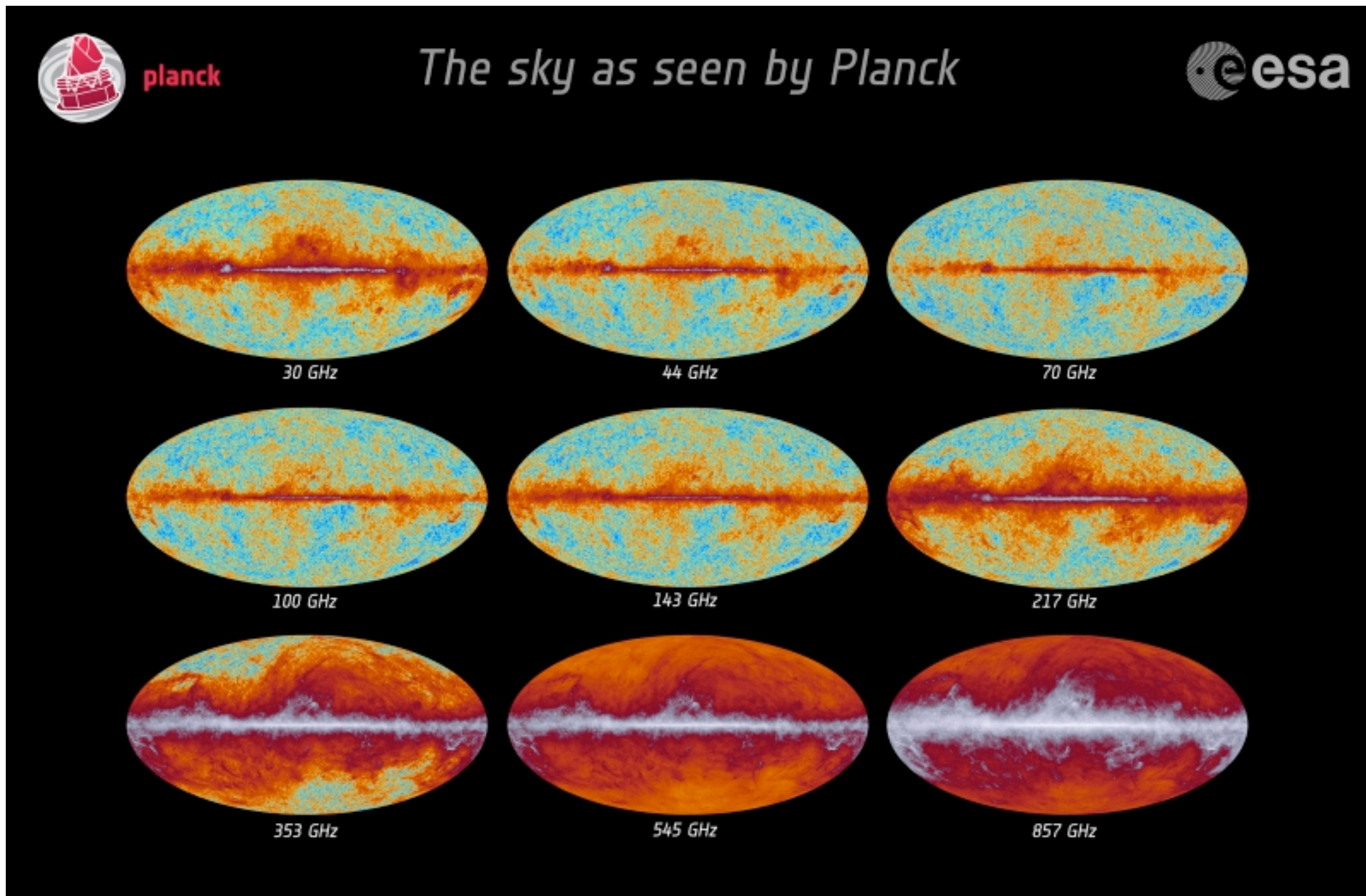


Means  
( $\mu\text{K}_{\text{CMB}}$ )

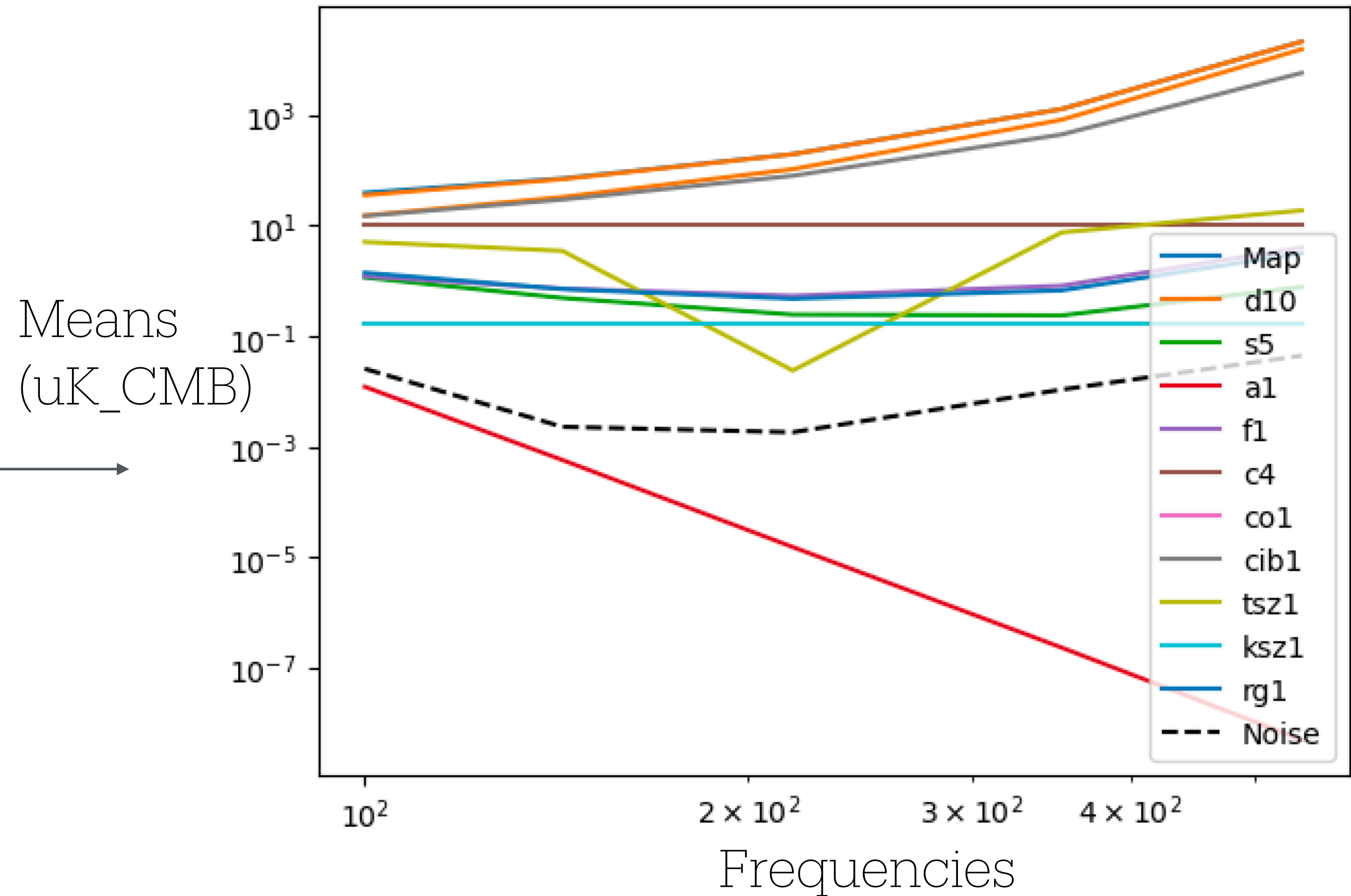


CMB, tSZ, kSZ, CIB, Radio sources, CO,  
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# An application to CMB data - CIB removal - SZ extraction



CMB, tSZ, kSZ, CIB, Radio sources, CO, Free-free, Synchrotron and Galactic dust



Means  
(uK\_CMB)  
→

Non linear

$$\{C_i\} = B_i o (1^*(\text{CMB} + \text{kSZ}) + f_i^* \text{SZ} + \text{CIB}_i) + N_i$$

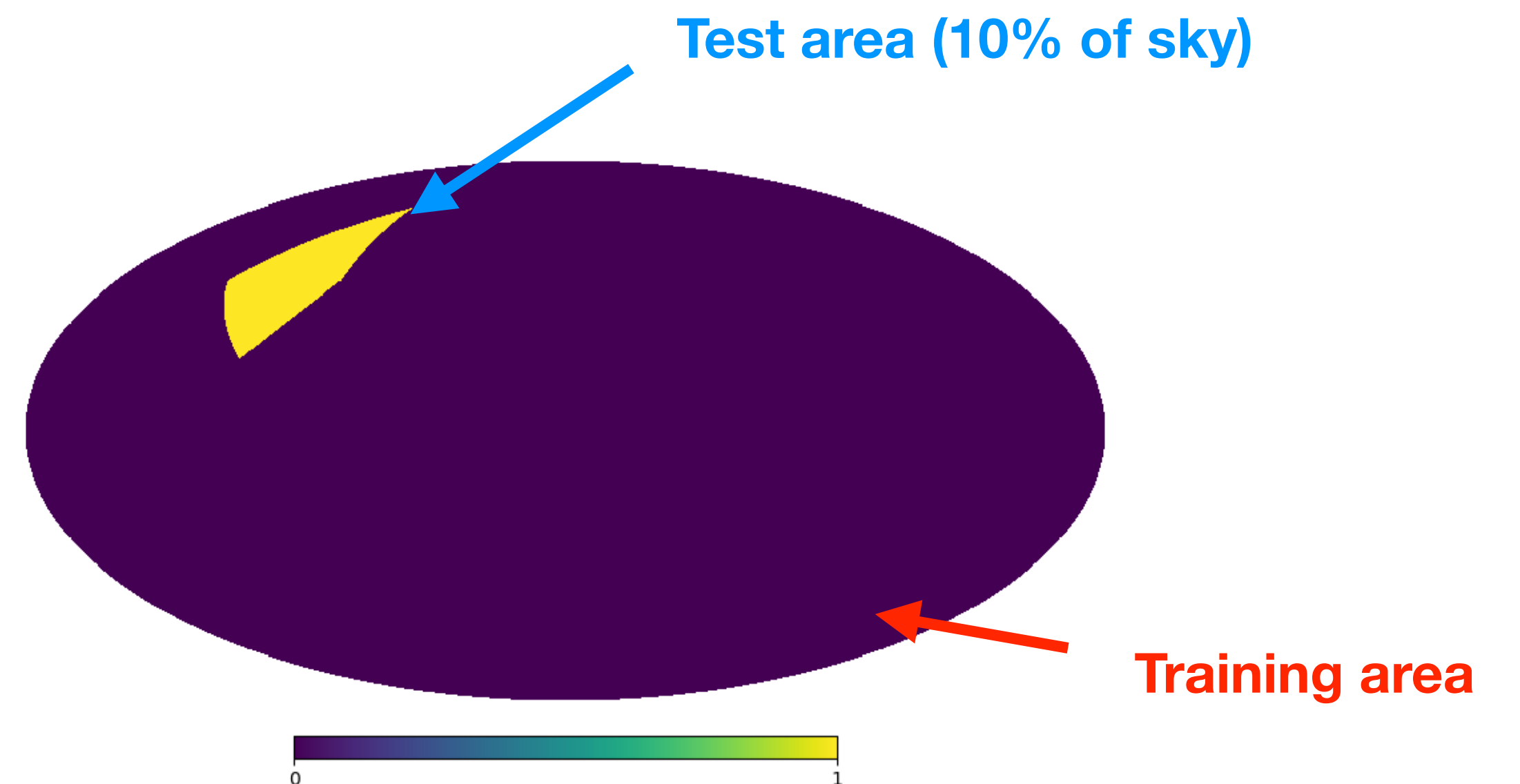
Non independent



# Data

First study on **WebSky** numerical simulations (Stein et al, 2020):

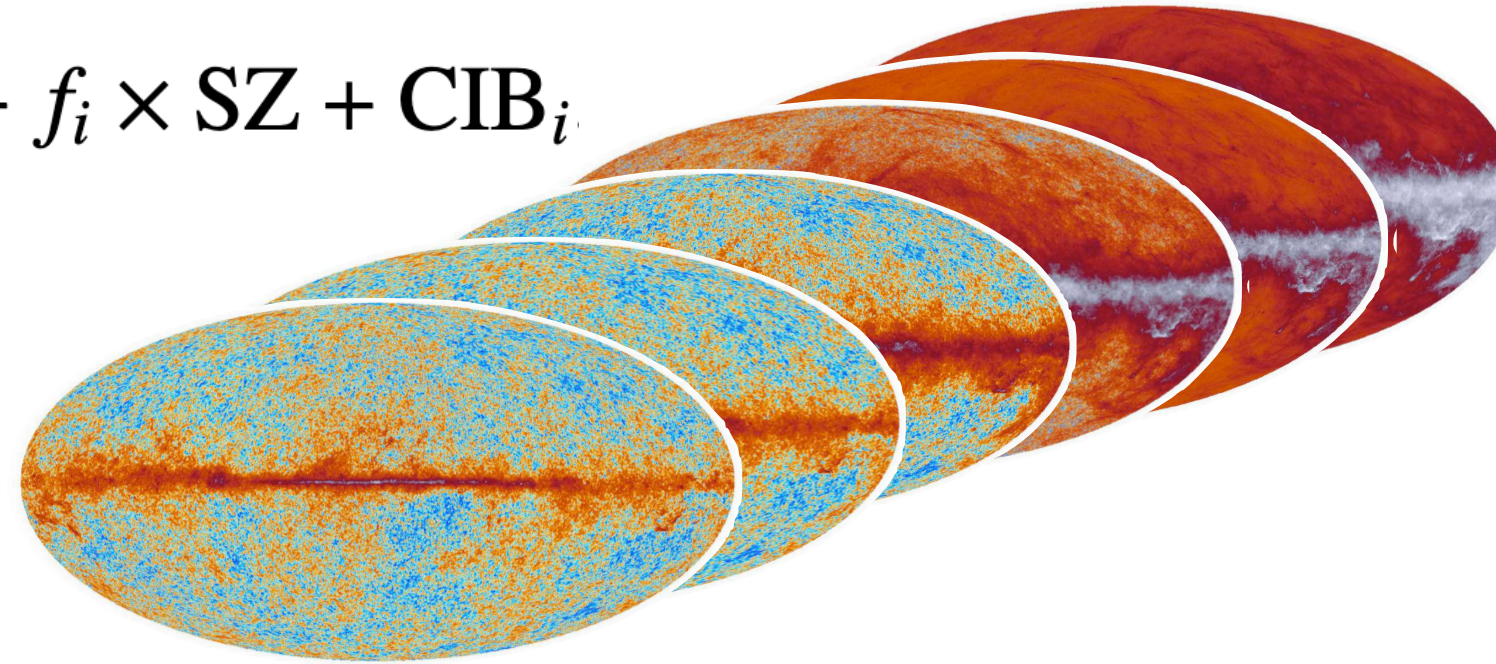
- 90, 100, 143, 145, 217, 225, 280, 353, 545 GHz (Planck and SO)
- Healpix nside=4096
- CMB, CIB, SZ
- No noise, no beams



# Method

$$C_i = 1 \times \text{CMB} + f_i \times \text{SZ} + \text{CIB}_i$$

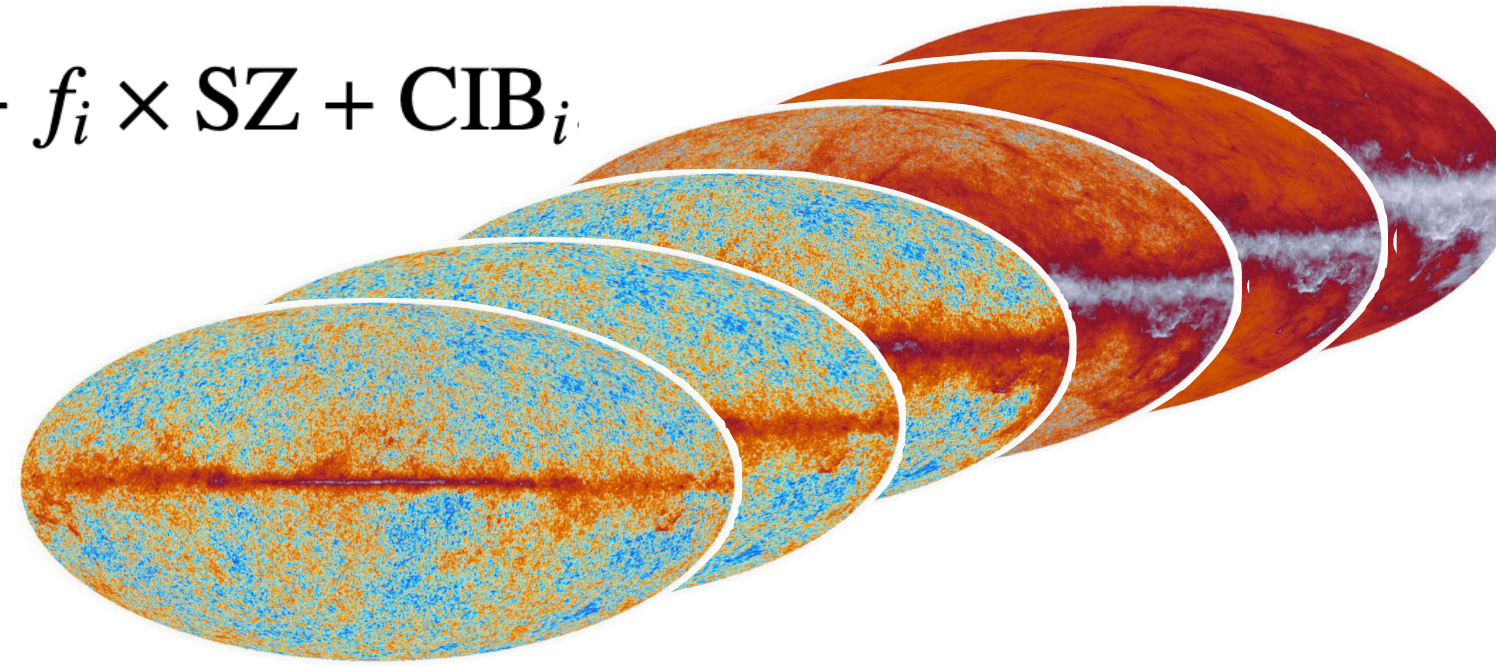
1) Project HEALPIX  
nside=4096 in patches



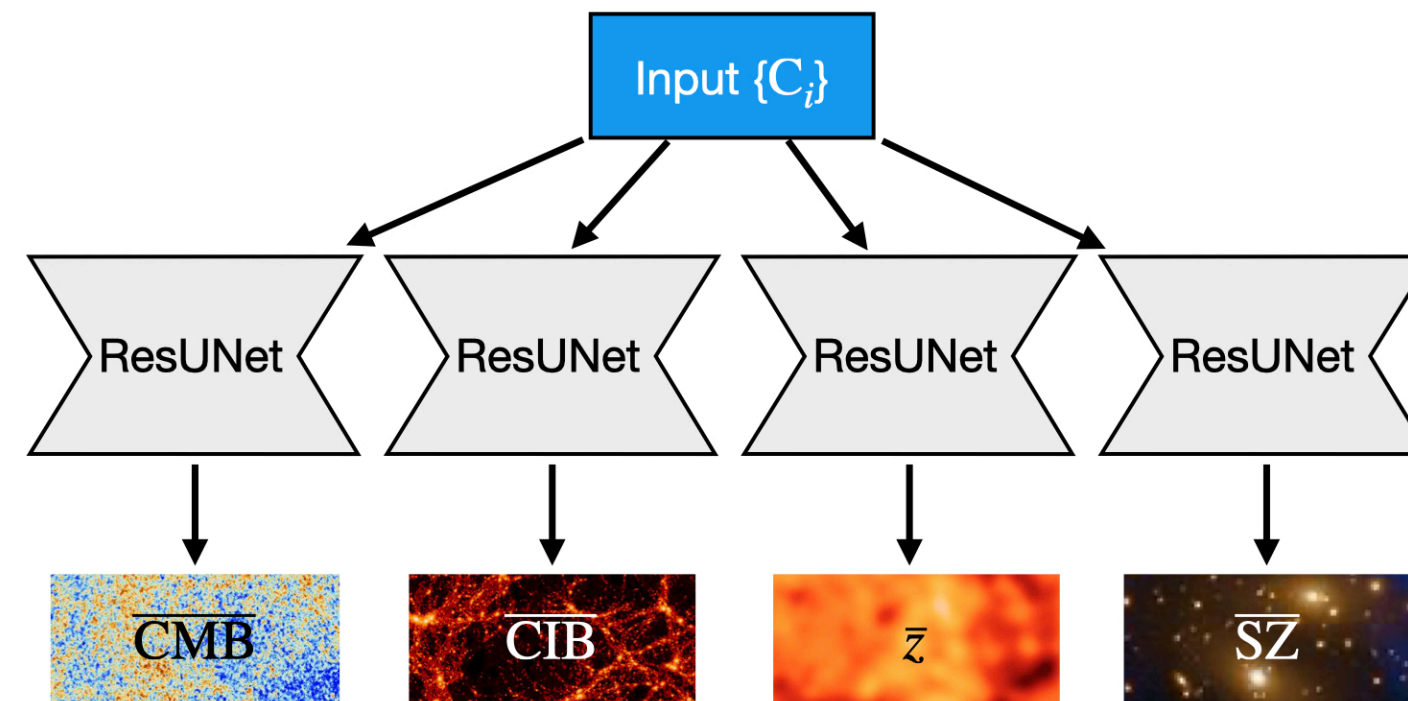
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nside=4096 in patches



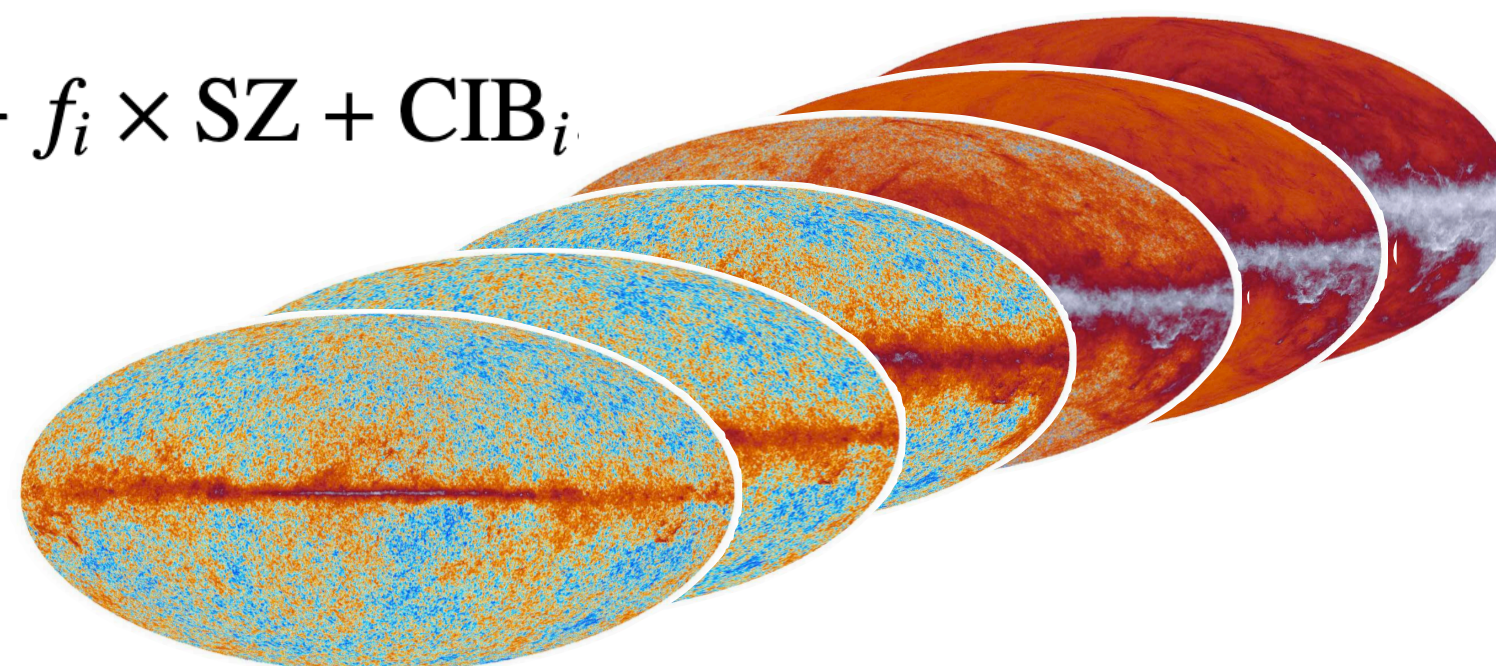
2) Network with n DIP for  
n components



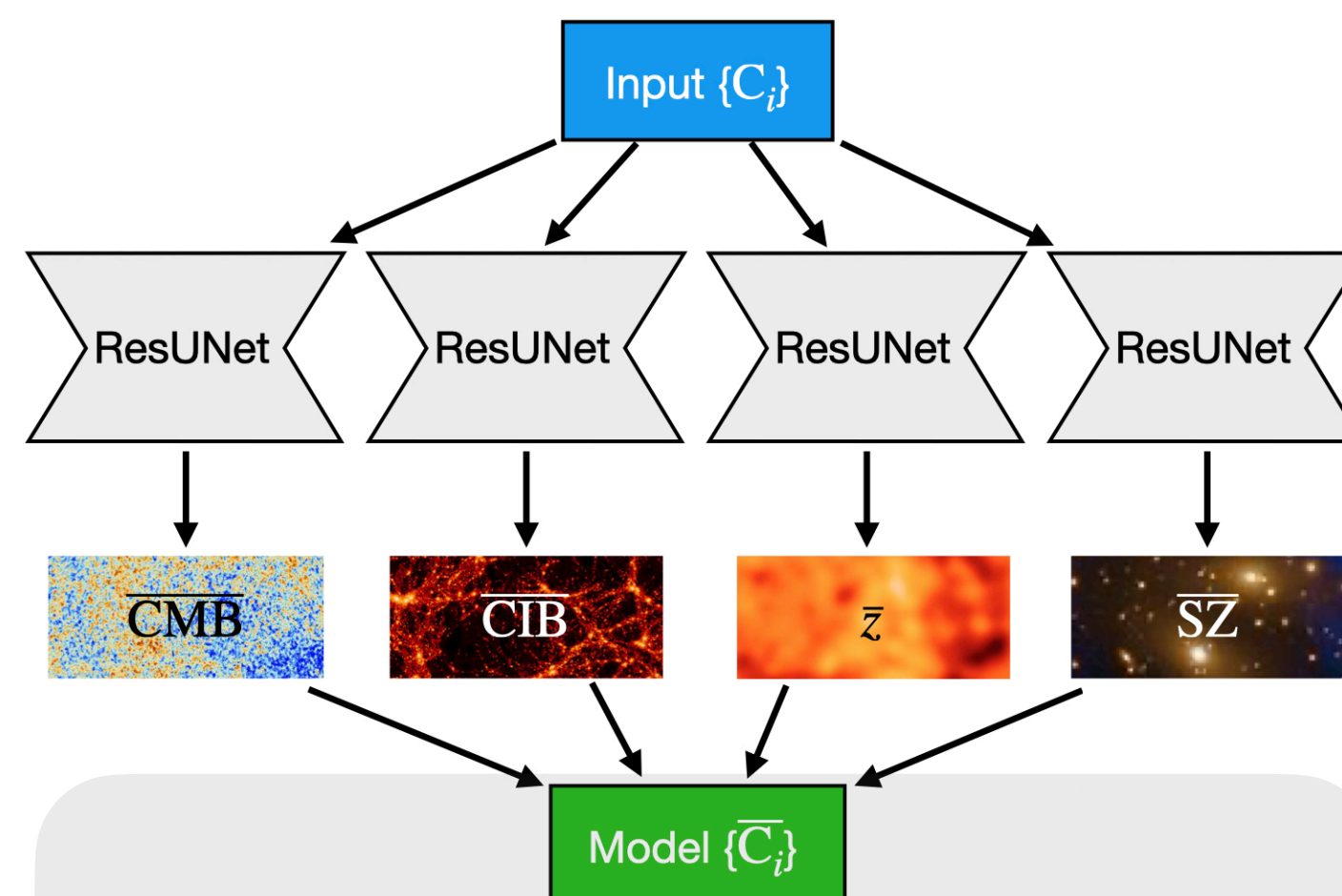
# Method

$$C_i = 1 \times \text{CMB} + f_i \times \text{SZ} + \text{CIB}_i$$

1) Project HEALPIX  
nside=4096 in patches



2) Network with n DIP for  
n components



3) Reconstruct the maps with  
the approximated mixing  
matrix

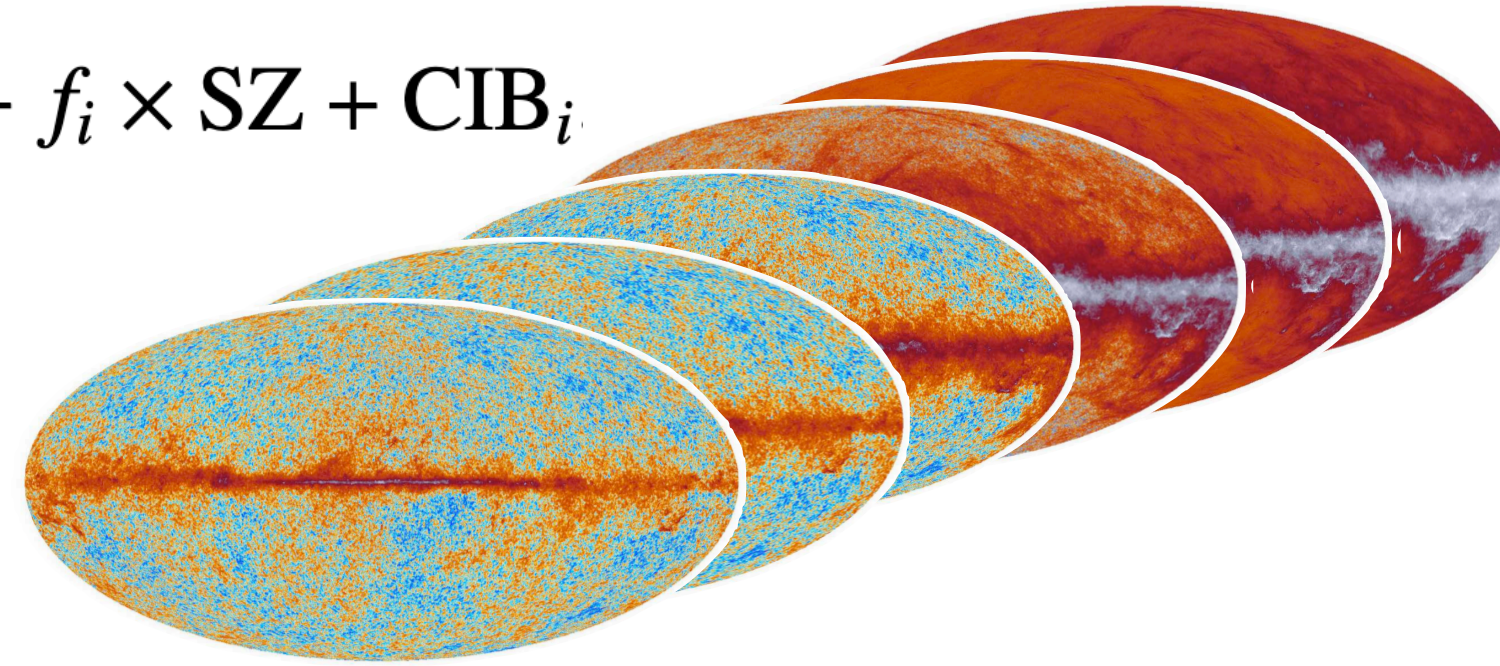
$$\bar{C}_i = 1 \times \bar{\text{CMB}} + f_i \times \bar{\text{SZ}} + \psi_i(\bar{z}) \bar{\text{CIB}}$$

$$\psi_i(\bar{z}) = \left(\frac{i}{545}\right)^{\beta+3} \times \frac{\exp\left(\frac{h \times 545 \times 10^9 (1+\bar{z})}{k_B T_0 (1+\bar{z})^\alpha}\right) - 1}{\exp\left(\frac{h \times i \times 10^9 (1+\bar{z})}{k_B T_0 (1+\bar{z})^\alpha}\right) - 1}$$

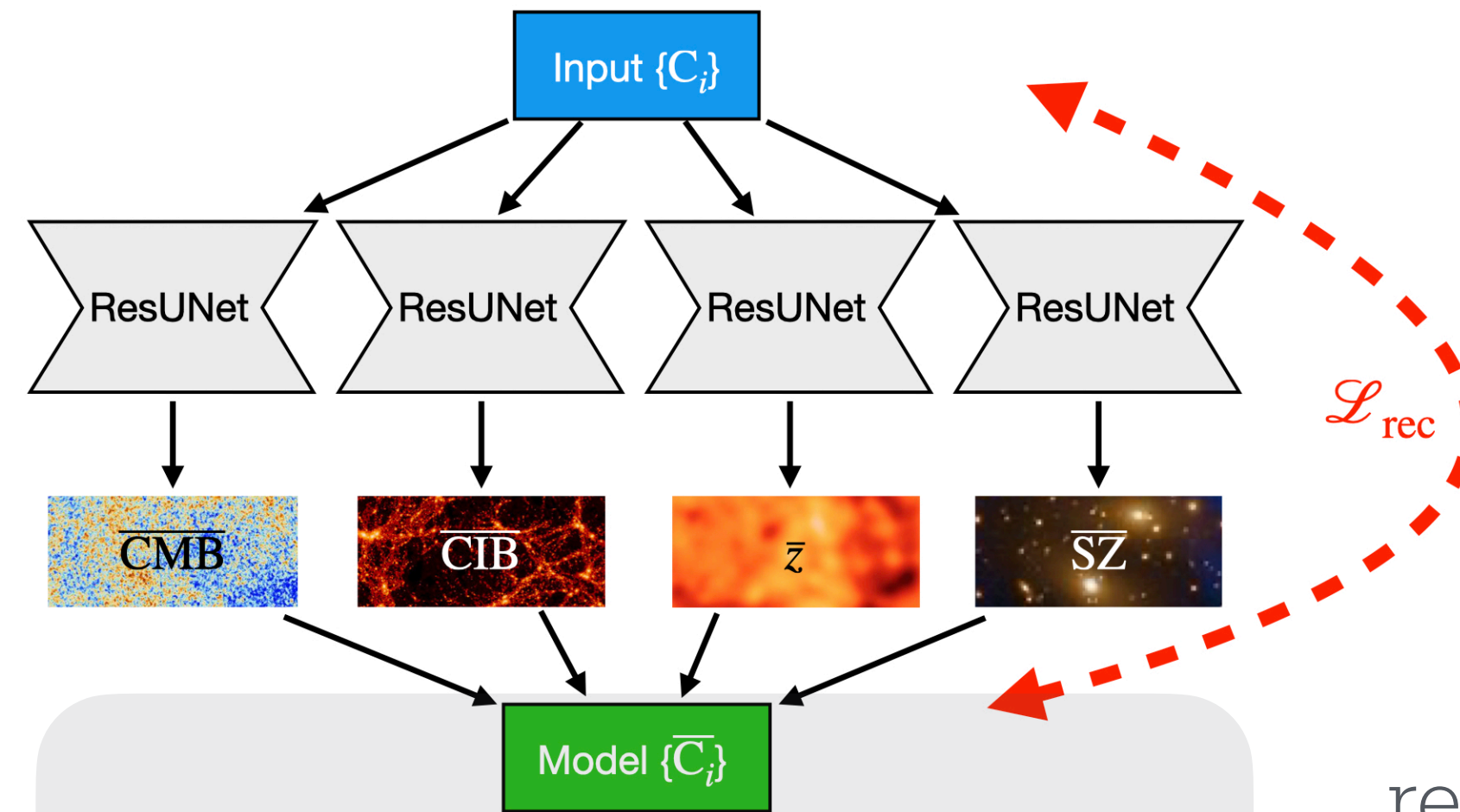
# Method

$$C_i = 1 \times \text{CMB} + f_i \times \text{SZ} + \text{CIB}_i$$

1) Project HEALPIX  
nside=4096 in patches



2) Network with n DIP for  
n components



3) Reconstruct the maps with  
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matrix

$$\bar{C}_i = 1 \times \bar{\text{CMB}} + f_i \times \bar{\text{SZ}} + \psi_i(\bar{z}) \bar{\text{CIB}}$$

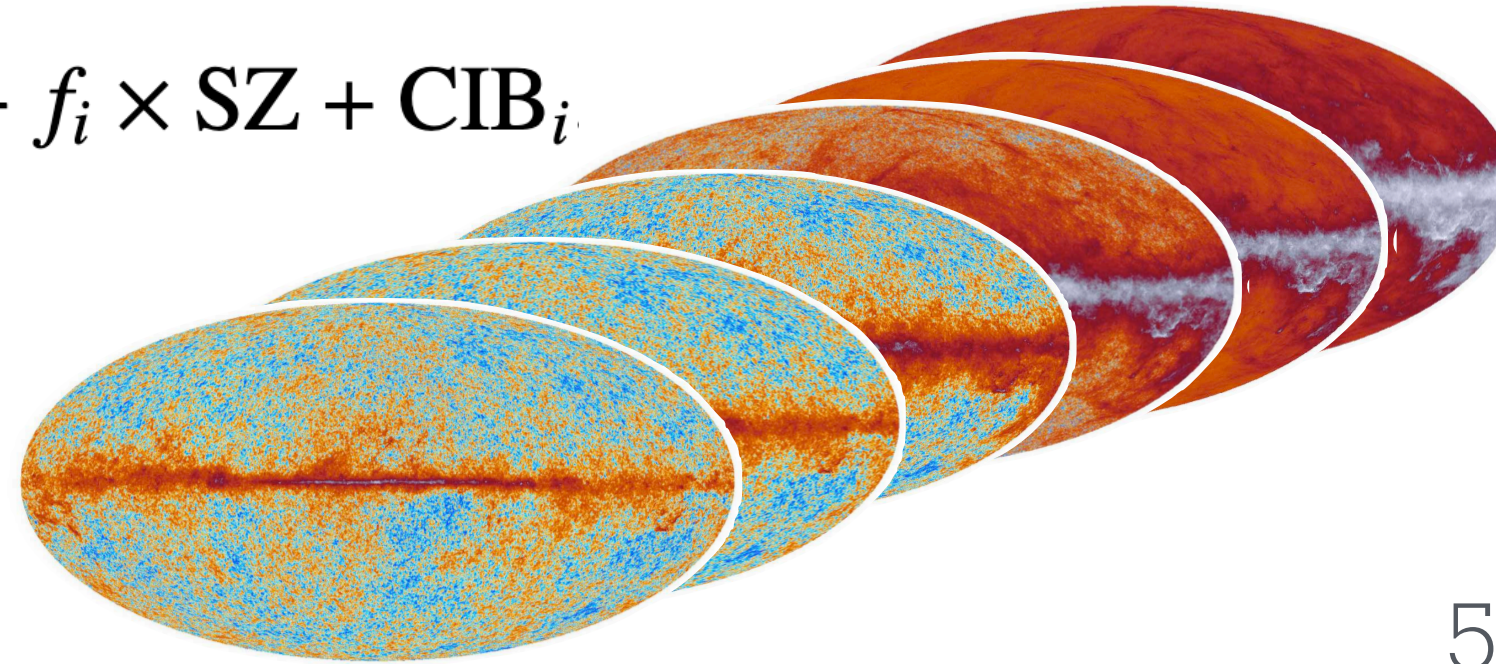
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4) Reconstruction loss between  
reconstructed maps and input maps

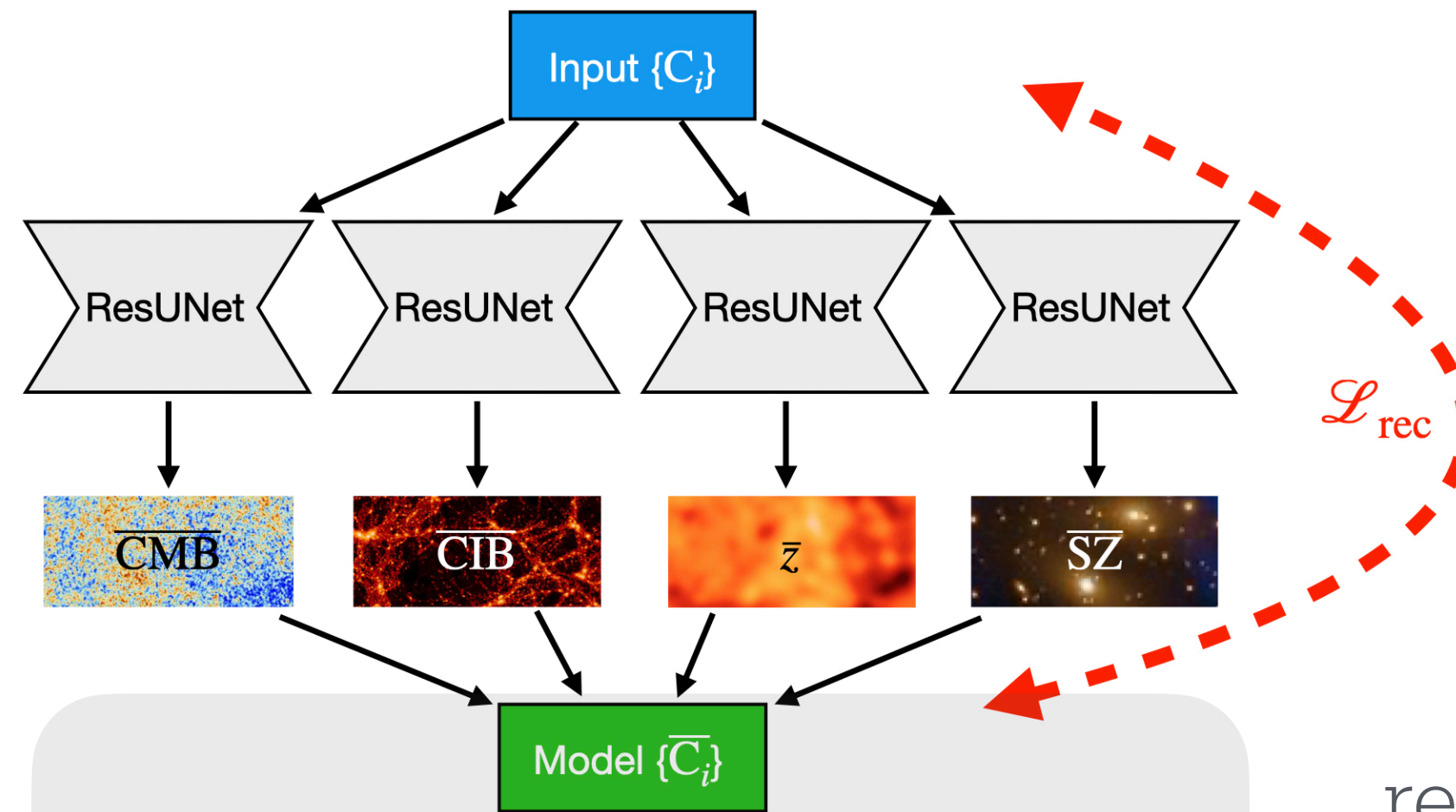
# Method

$$C_i = 1 \times \text{CMB} + f_i \times \text{SZ} + \text{CIB}_i$$

1) Project HEALPIX  
nside=4096 in patches



2) Network with n DIP for  
n components



5) Reconstruct HEALPIX maps with the  
extracted components

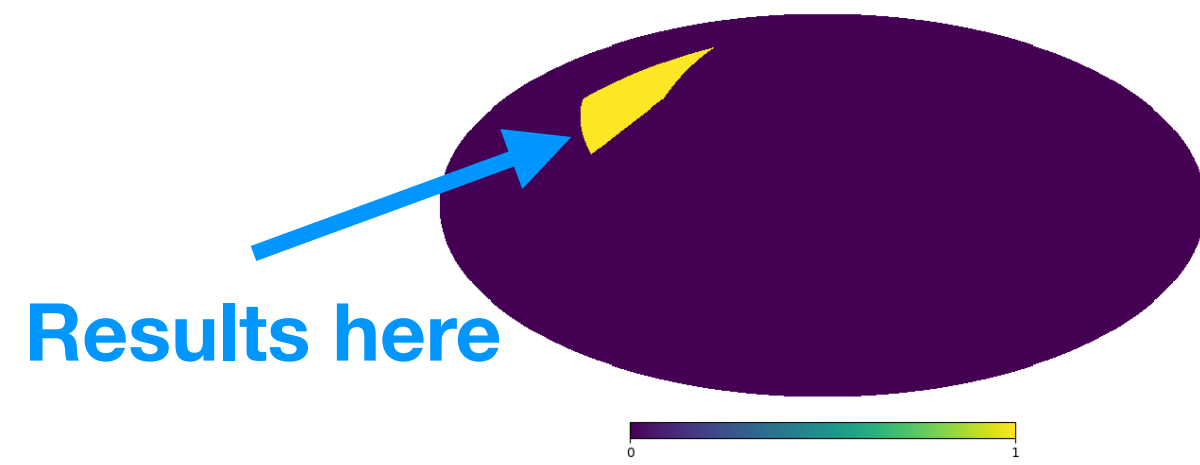
3) Reconstruct the maps with  
the approximated mixing  
matrix

$$\bar{C}_i = 1 \times \bar{\text{CMB}} + f_i \times \bar{\text{SZ}} + \psi_i(\bar{z}) \bar{\text{CIB}}$$

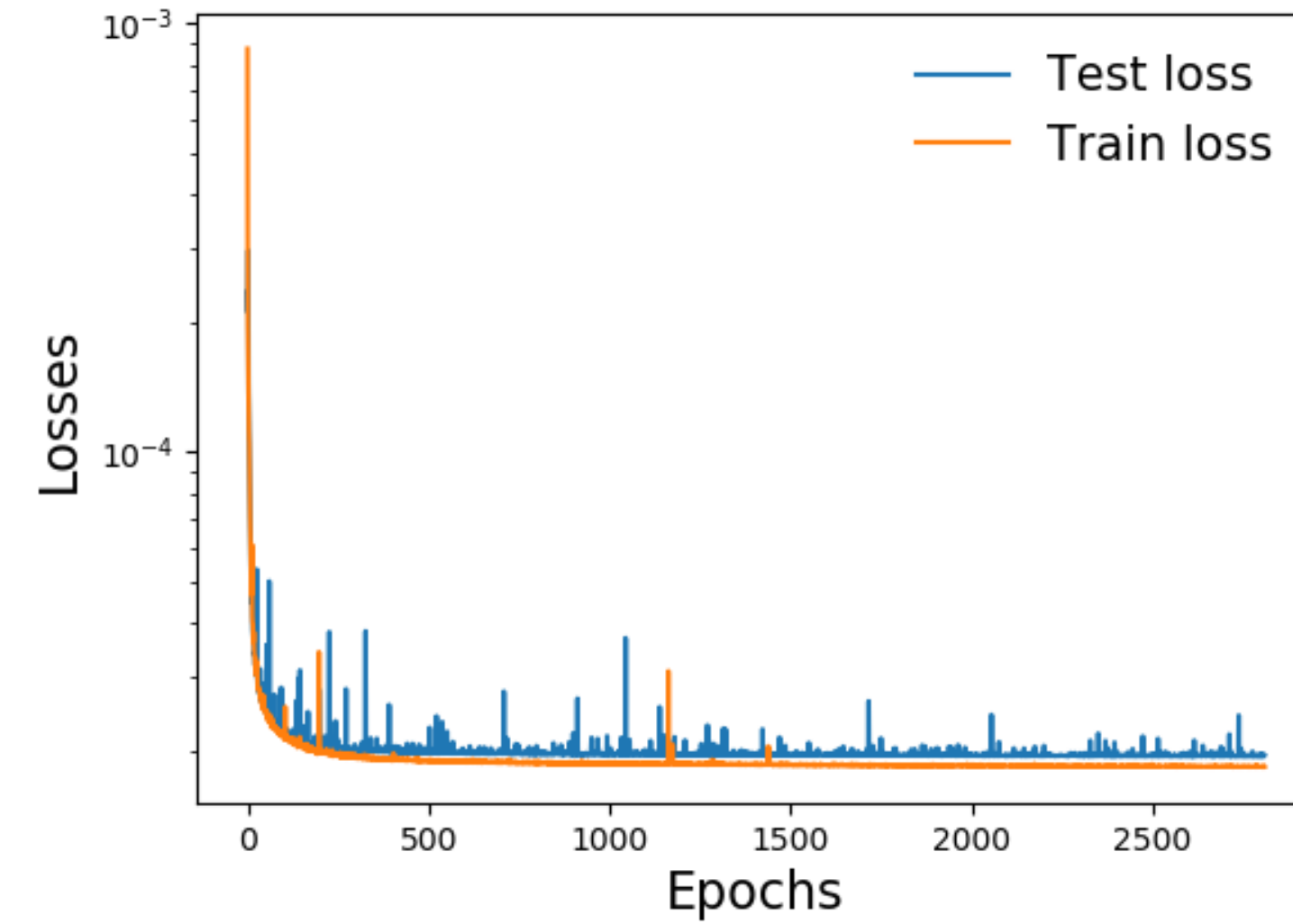
$$\psi_i(\bar{z}) = \left(\frac{i}{545}\right)^{\beta+3} \times \frac{\exp\left(\frac{h \times 545 \times 10^9 (1+\bar{z})}{k_B T_0 (1+\bar{z})^\alpha}\right) - 1}{\exp\left(\frac{h \times i \times 10^9 (1+\bar{z})}{k_B T_0 (1+\bar{z})^\alpha}\right) - 1}$$

4) Reconstruction loss between  
reconstructed maps and input maps

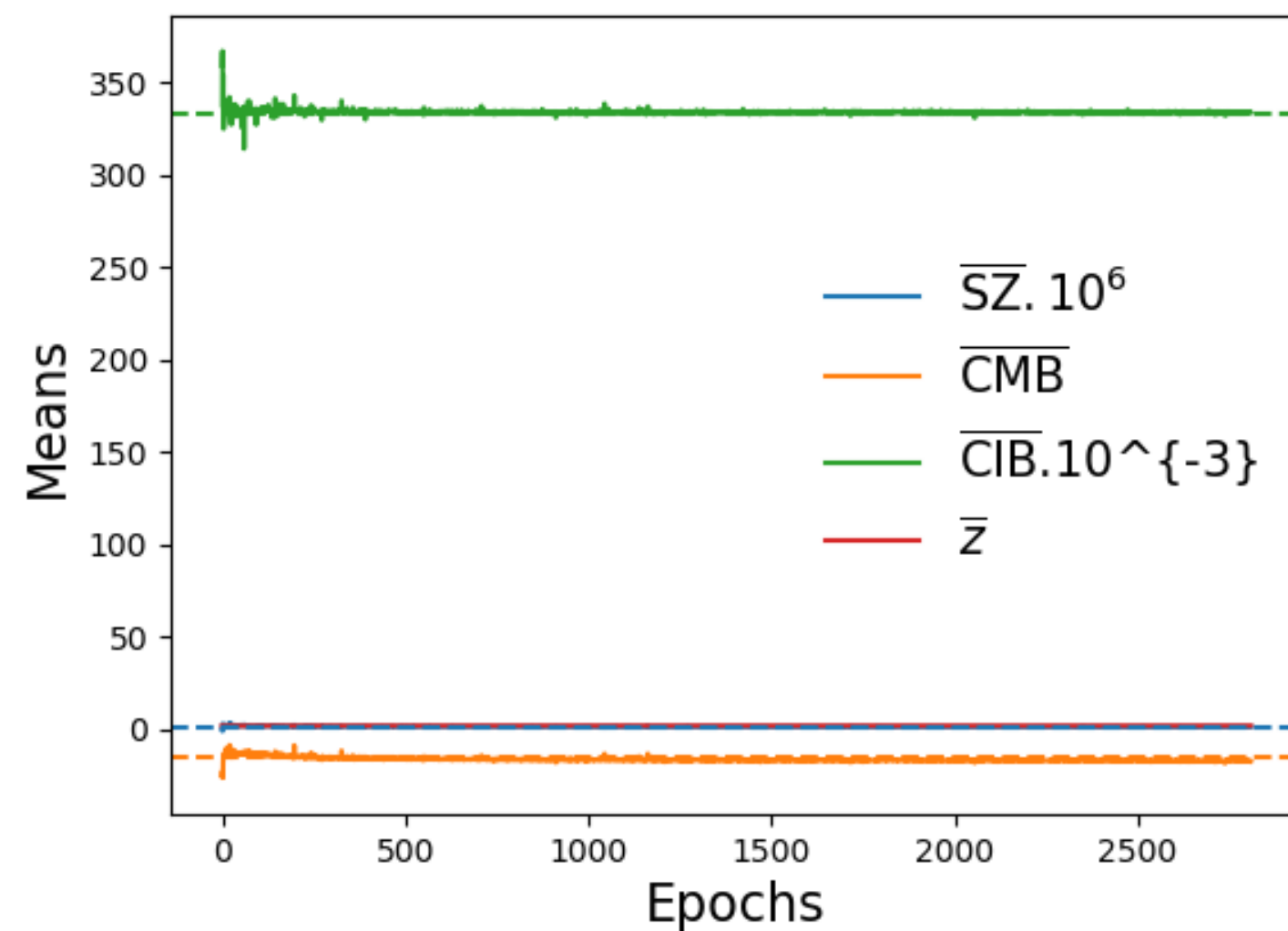
# Optimization process



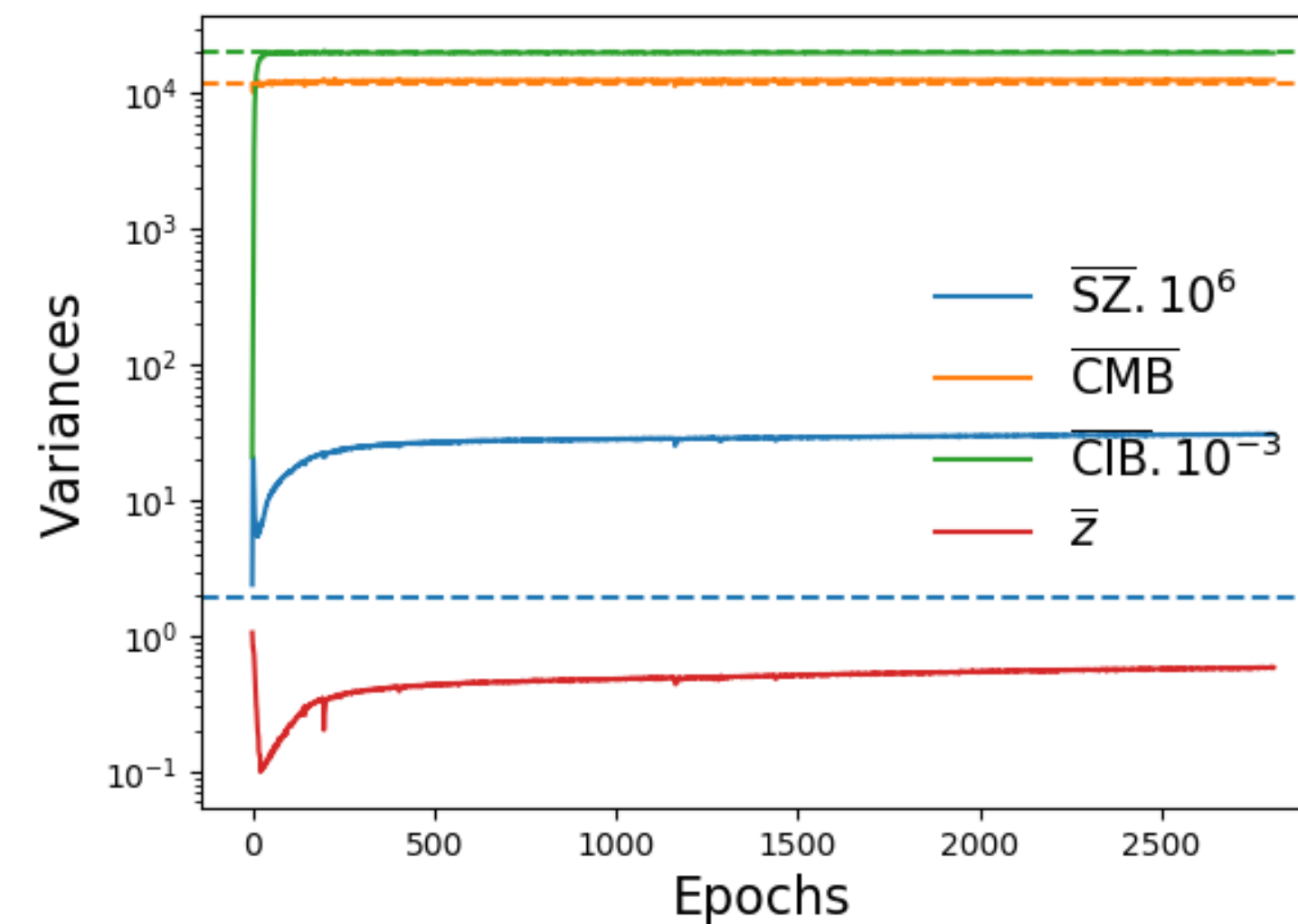
Components are converging into the expected solution during the optimization



Means:



Variances:

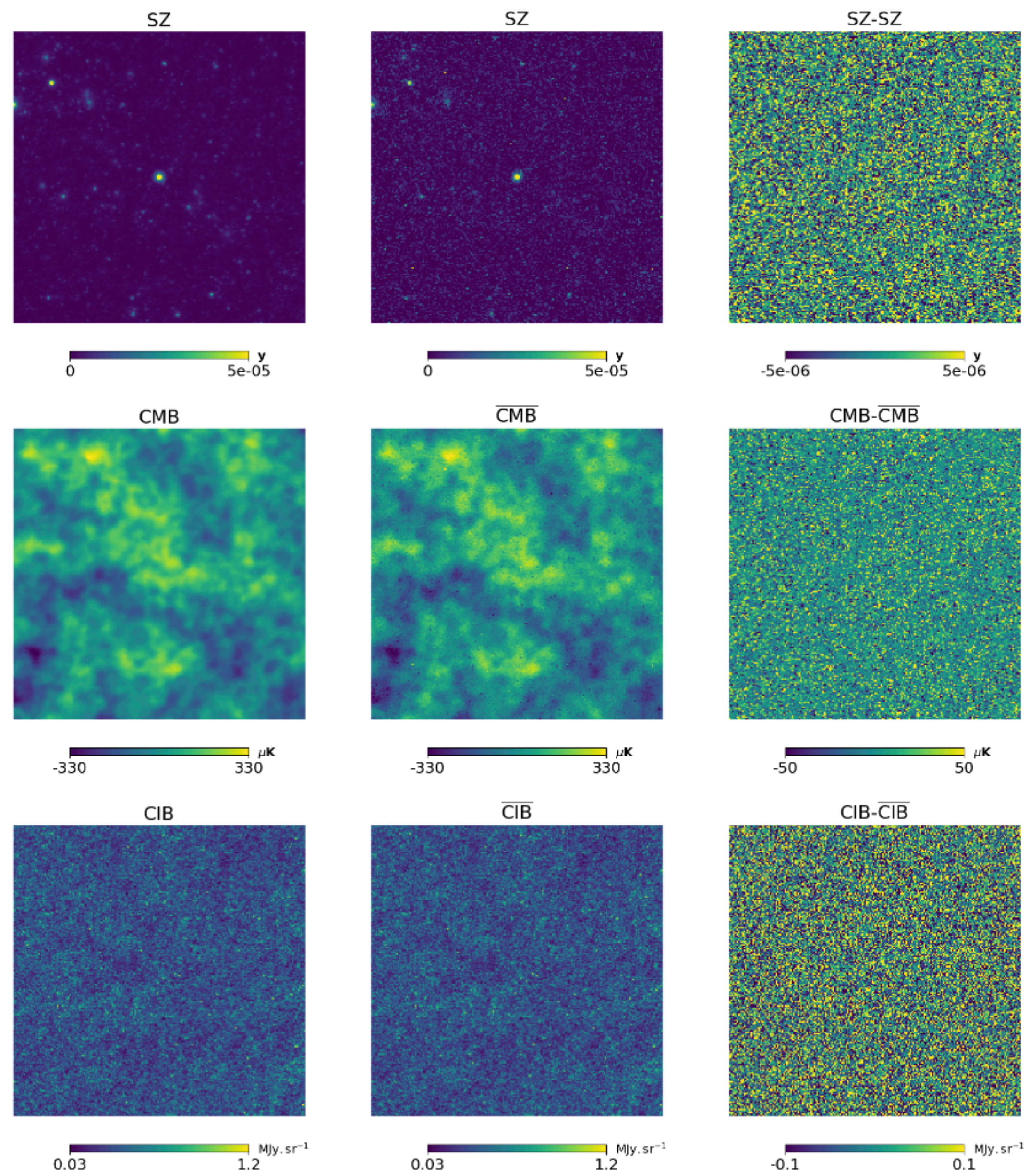


# Results



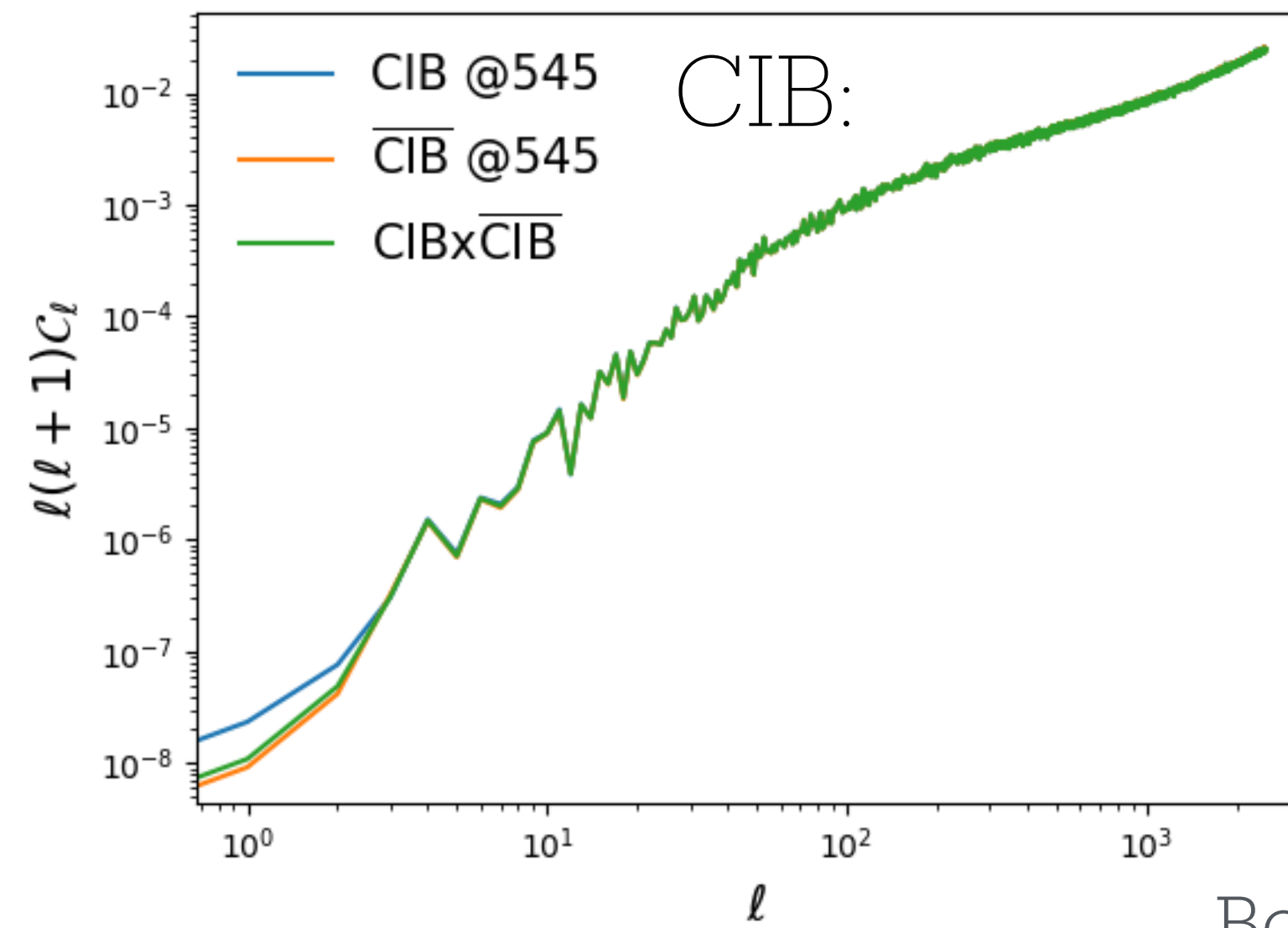
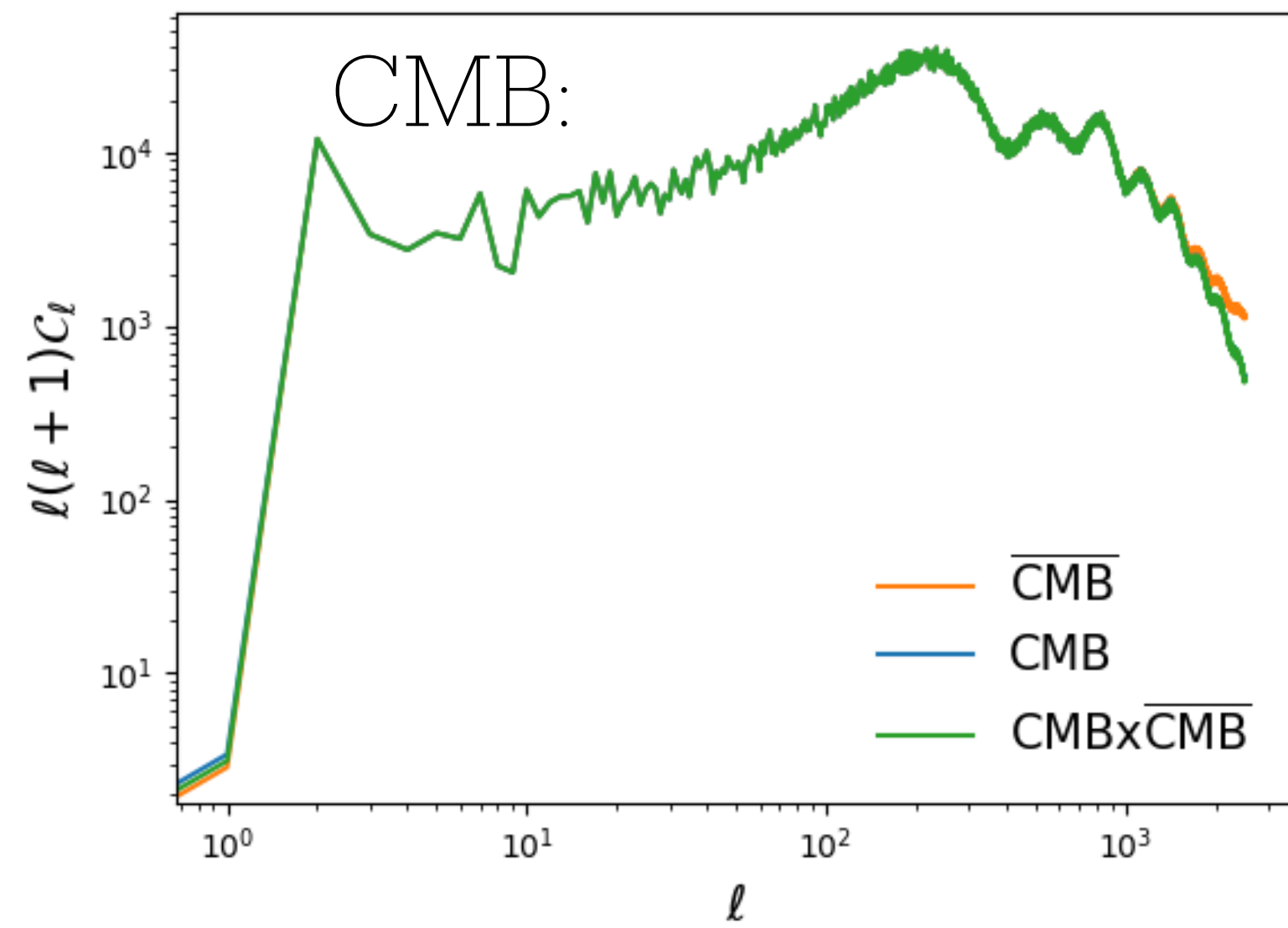
# Results

Quick look:



# Results

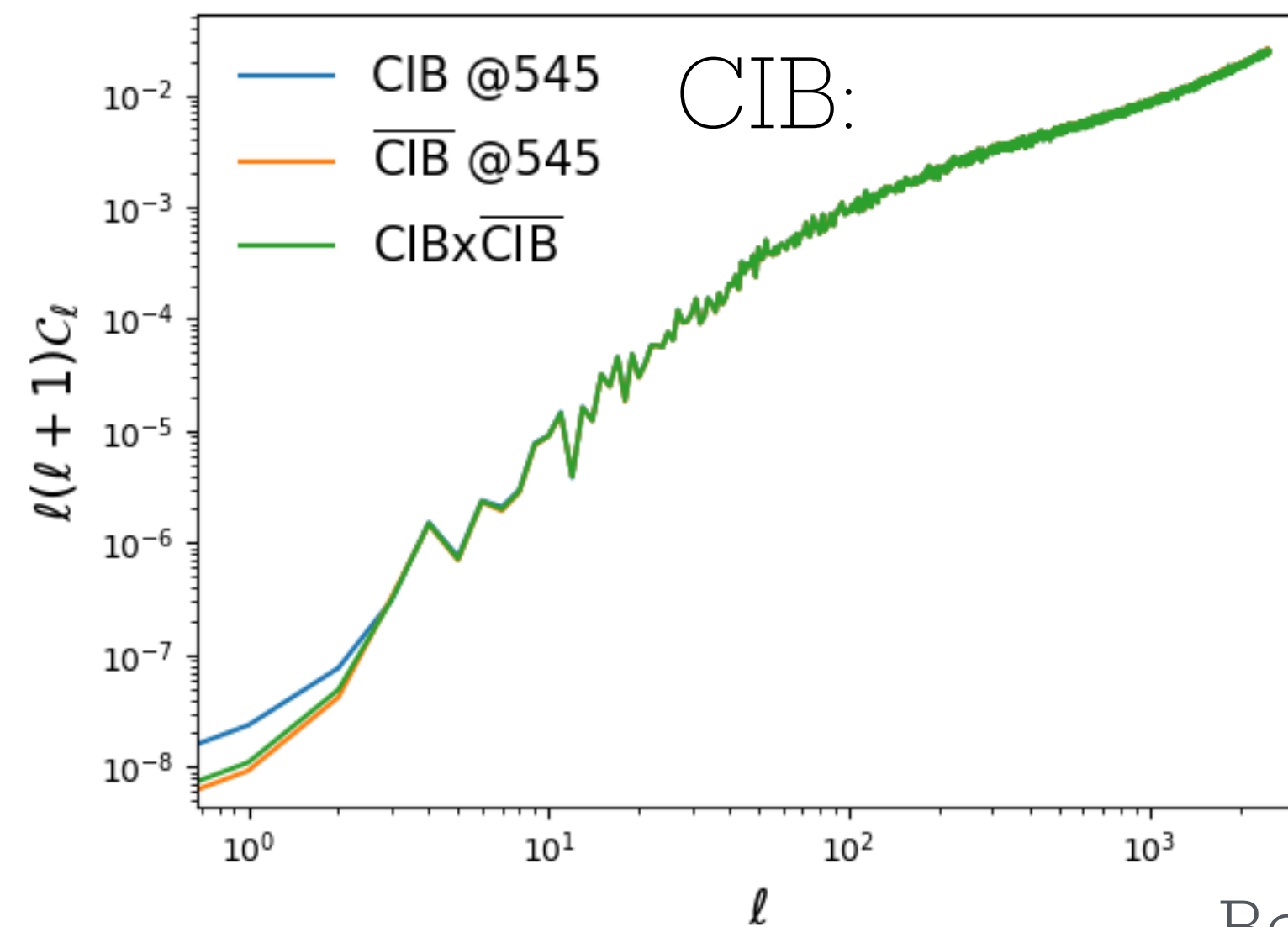
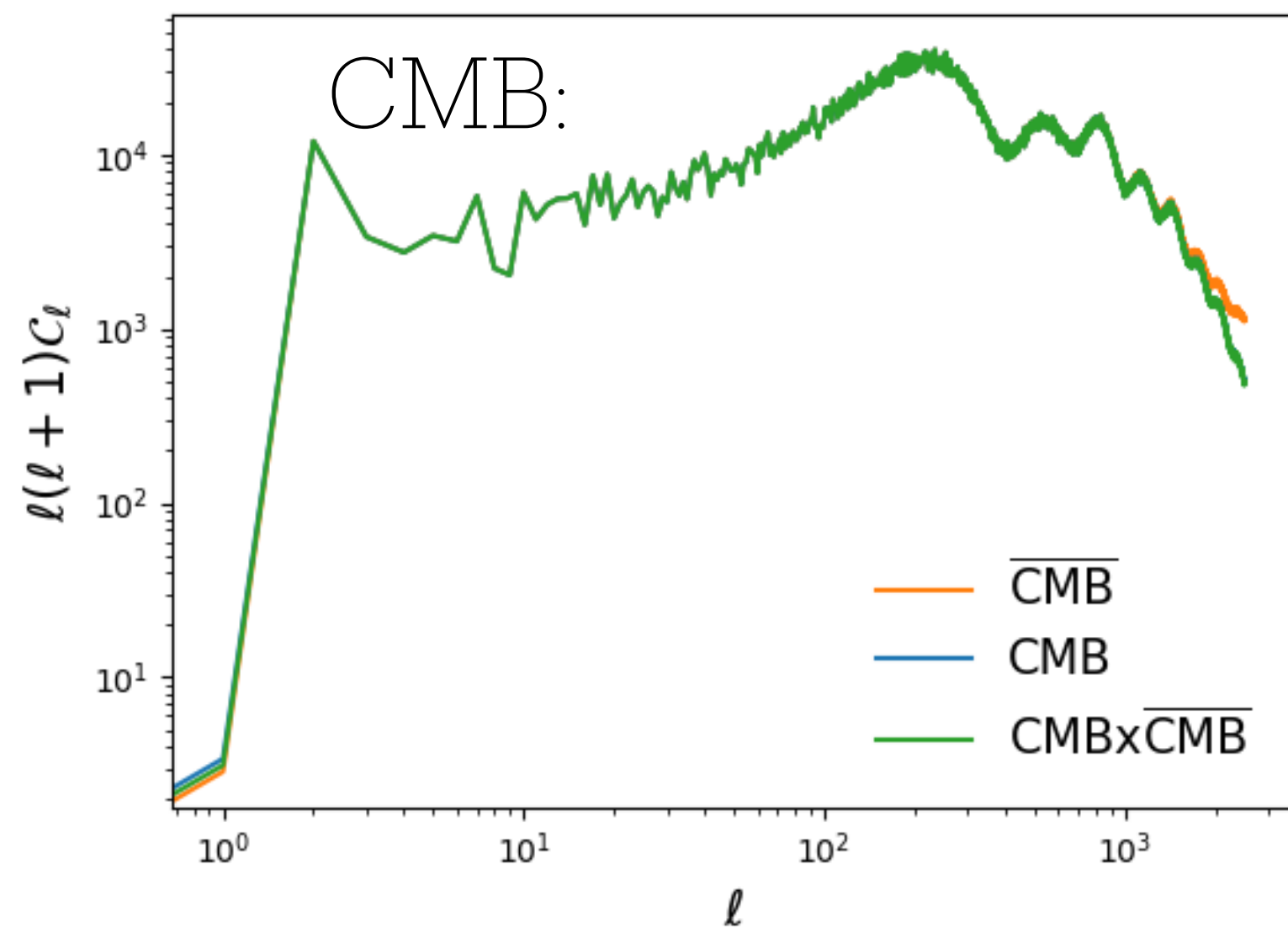
## Power spectra:



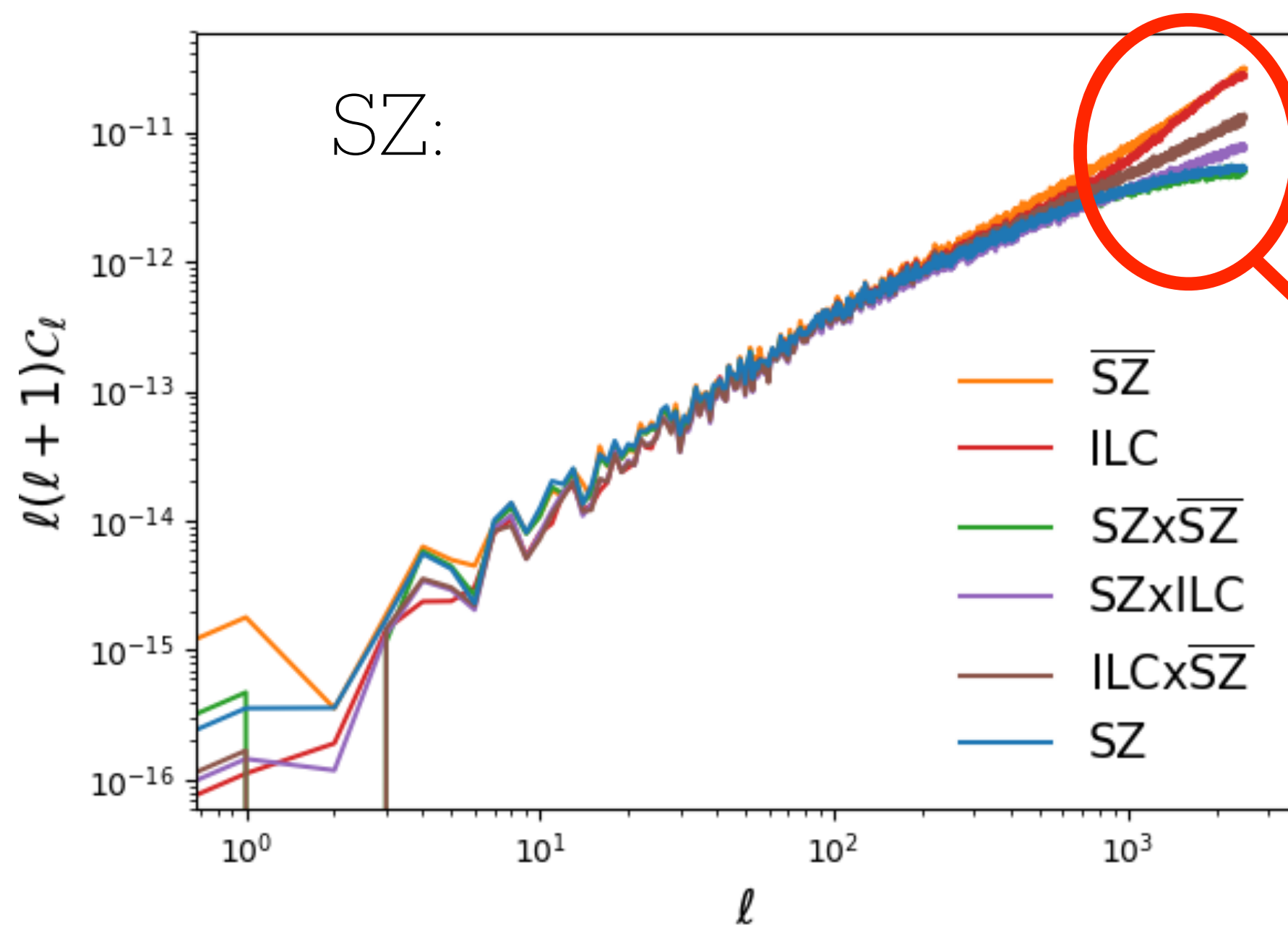
Bonjean et al, 2024

# Results

## Power spectra:



Bonjean et al, 2024



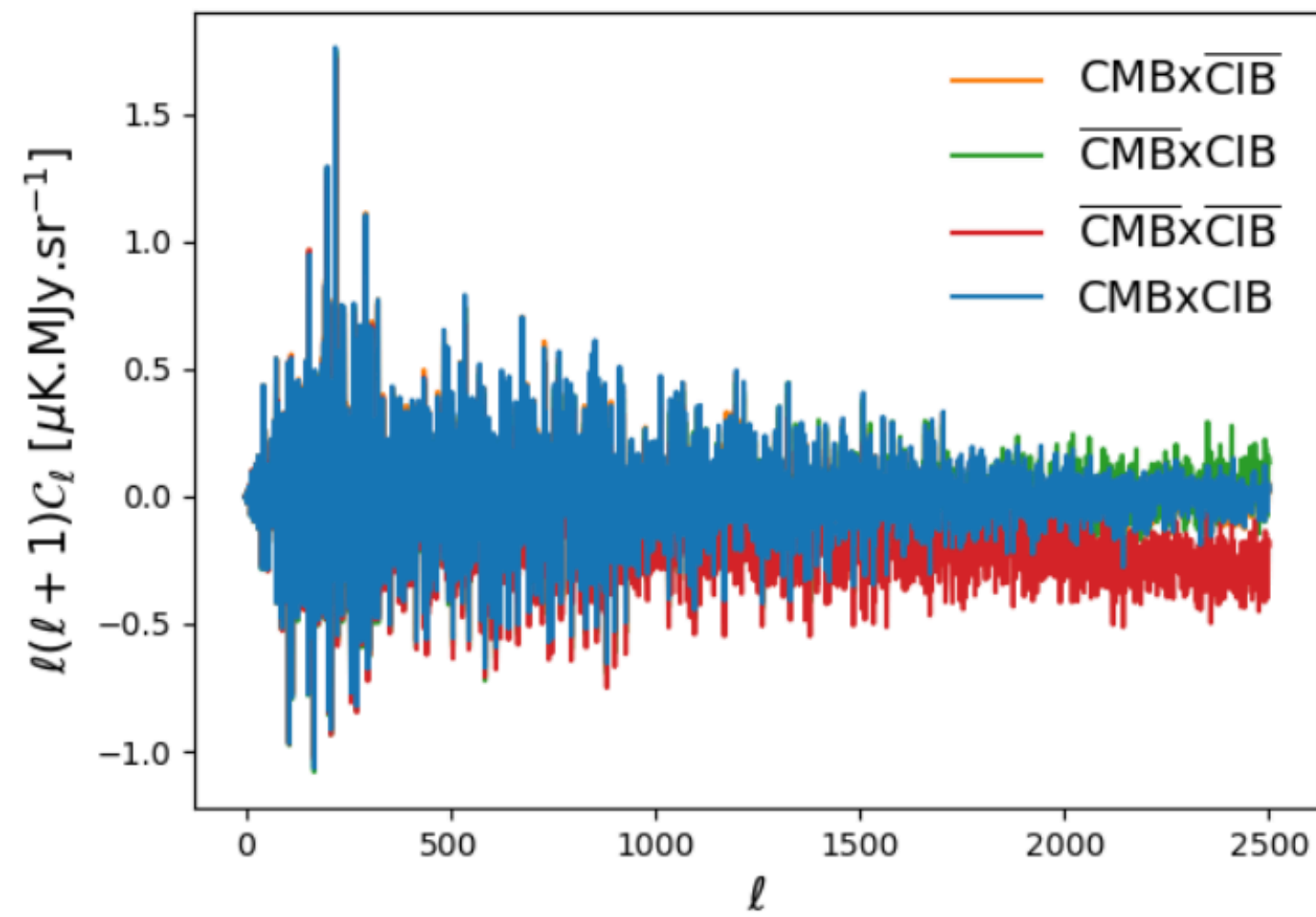
Comparison with MILCA (Planck)

**Excess of signal in  
SZxMILCA**

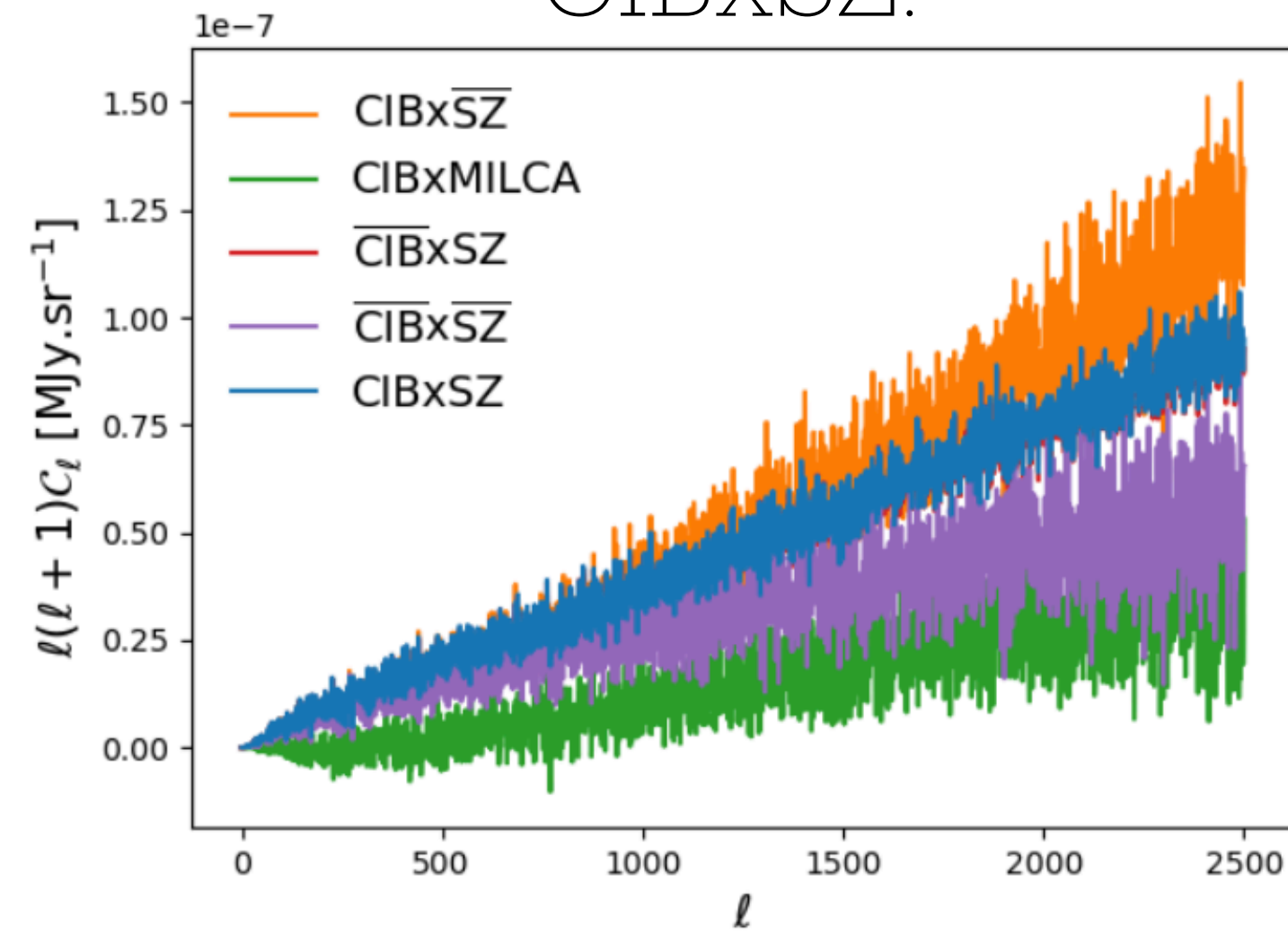
# Results

Contamination:

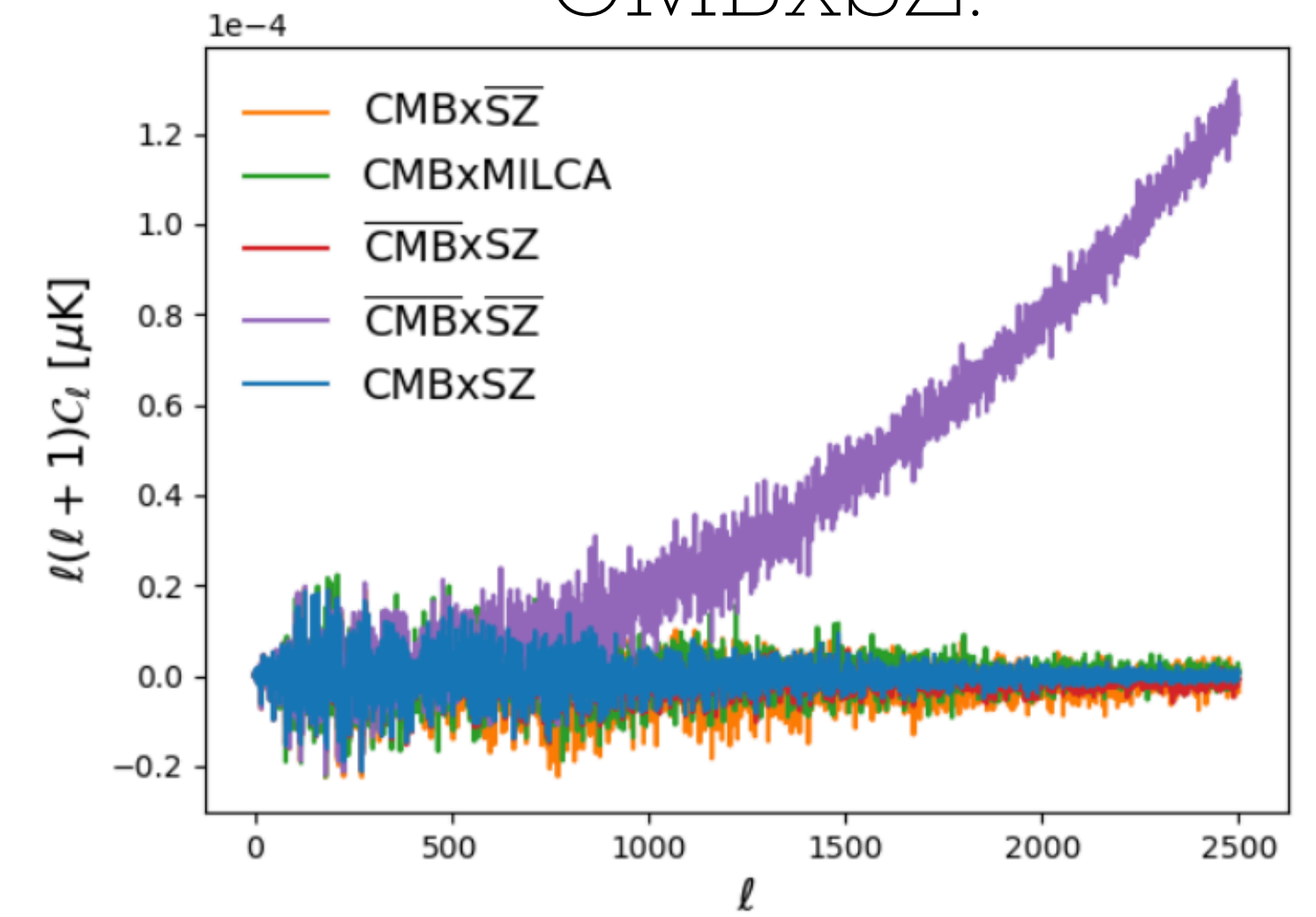
CMBxCIB:



CIBxSZ:



CMBxSZ:

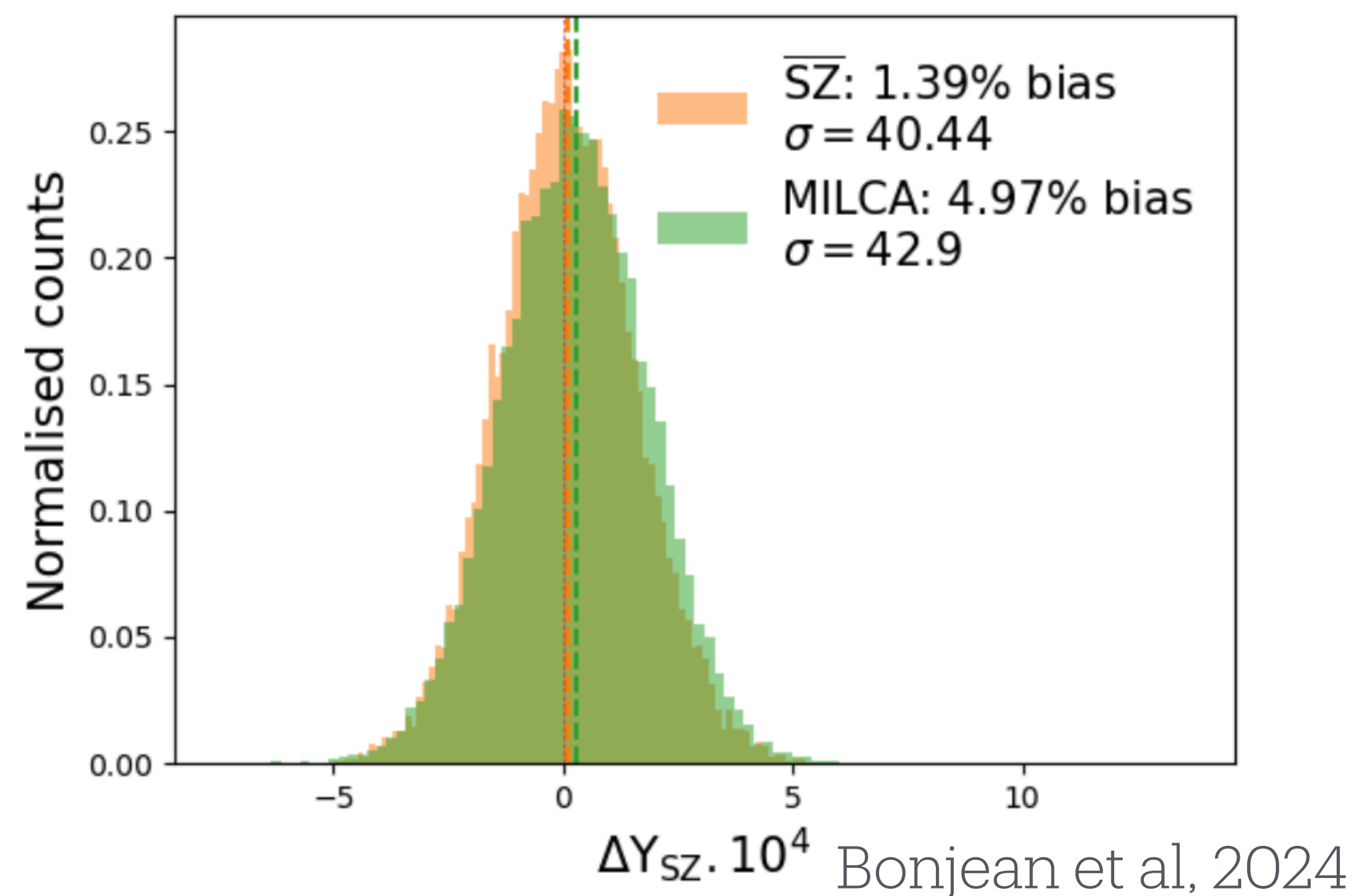
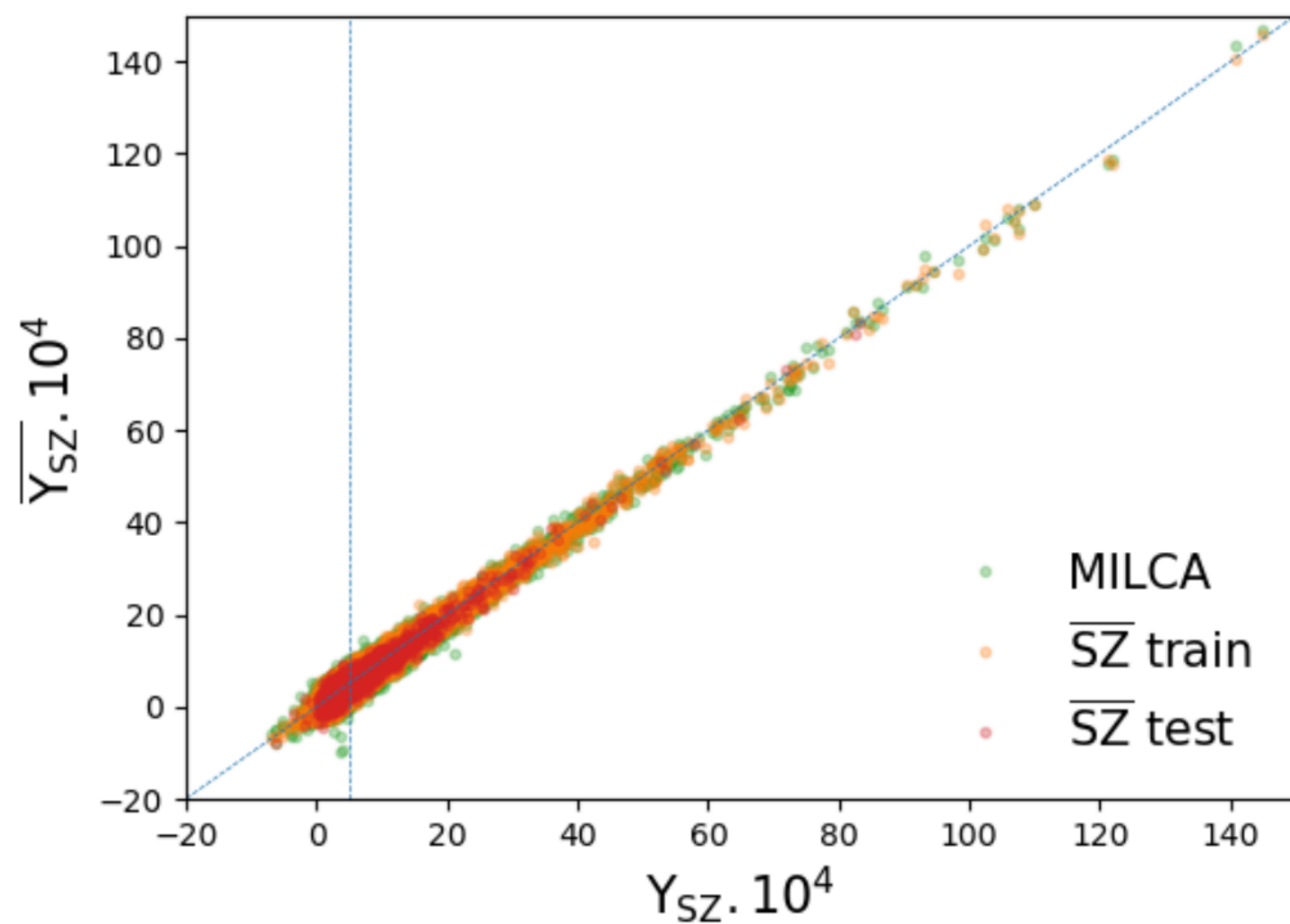


Bonjean et al, 2024

**SZ map less contaminated by other components**

# Results

SZ fluxes around clusters:



Competitive with MILCA

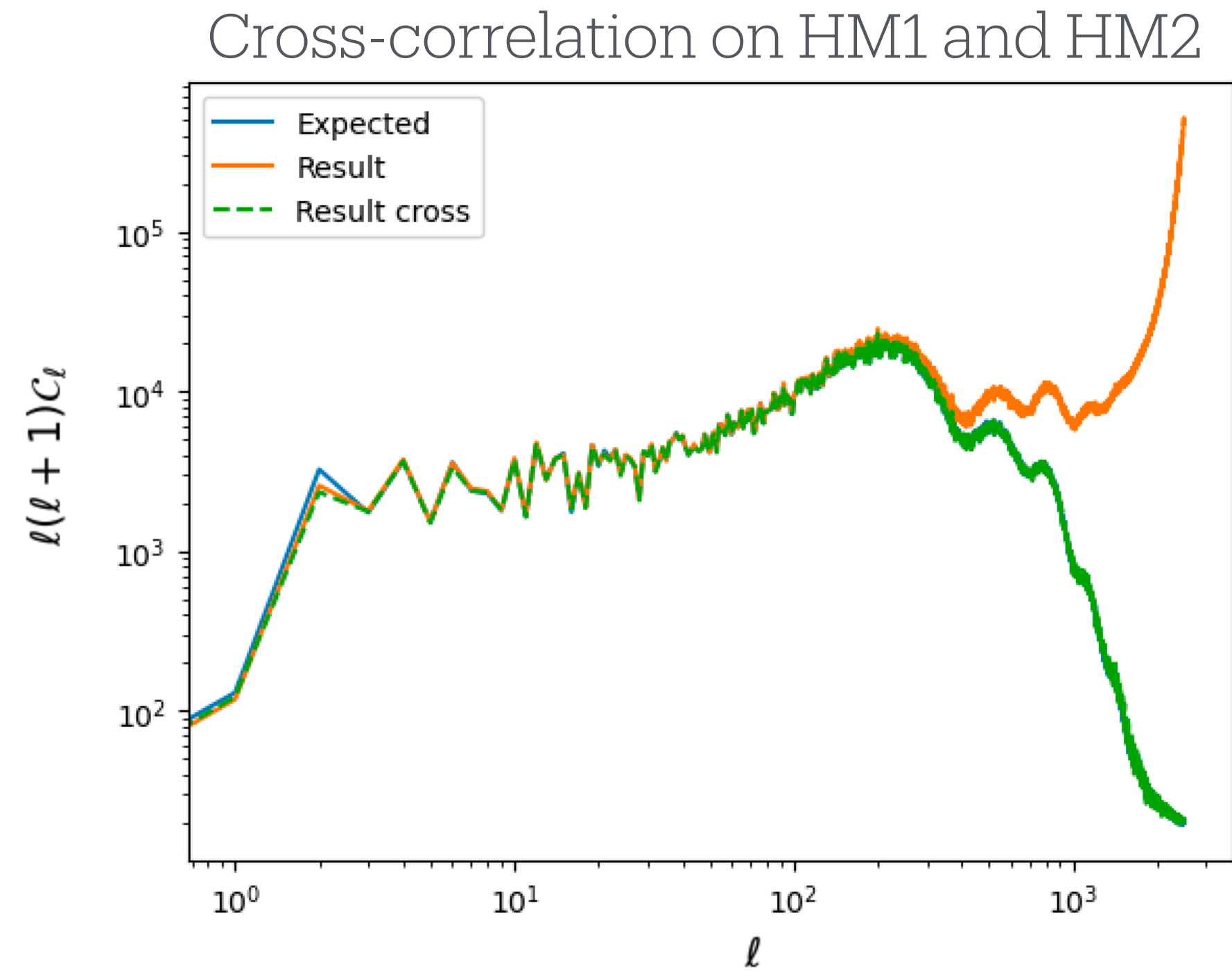
Results **including** foregrounds, beams, and noise

# Results **including** foregrounds, beams, and noise

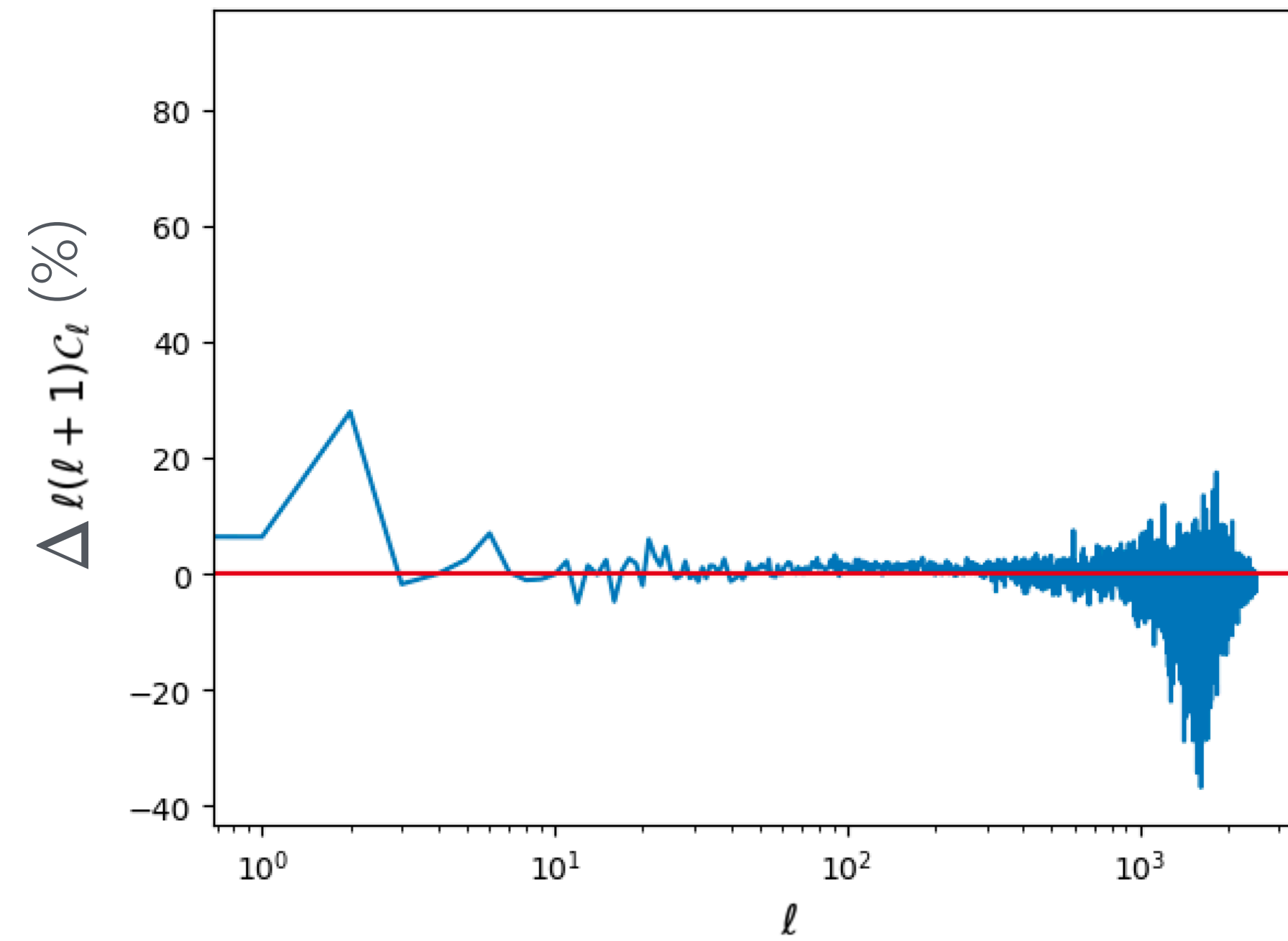
Second study on **WebSky** numerical simulations (Stein et al, 2020) and Planck Sky Model (pySM3, Thorne et al, 2016):

- 100, 143, 217, 353, 545 GHz (Planck)
- Healpix nside=2048
- CMB, CIB, tSZ, kSZ, radio sources, free-free, synchrotron, CO, AME, dust
- Noise & beams of Planck (no degraded resolution)

# Results including foregrounds, beams, and noise



CMB:

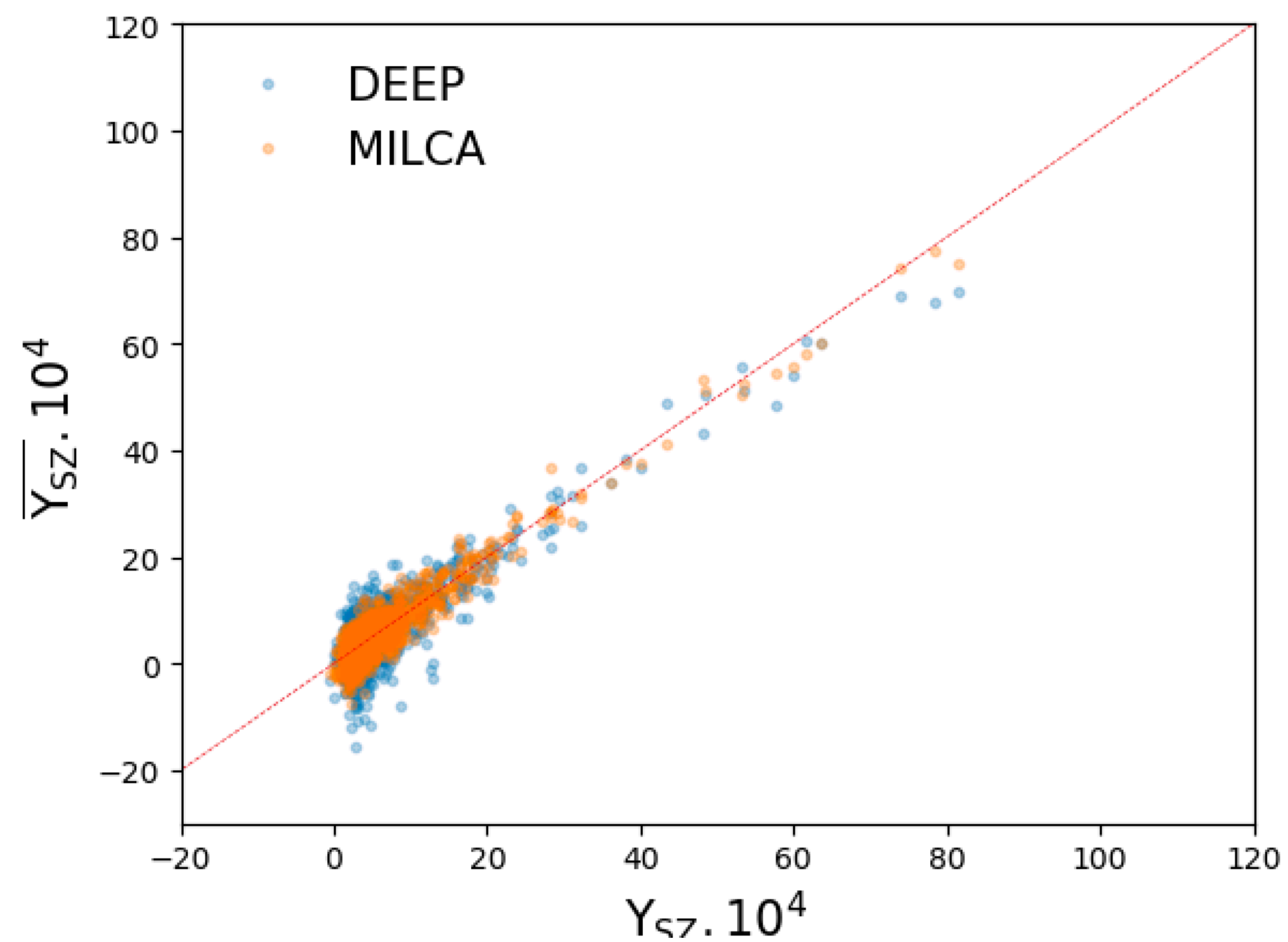


Bonjean et al, in prep.

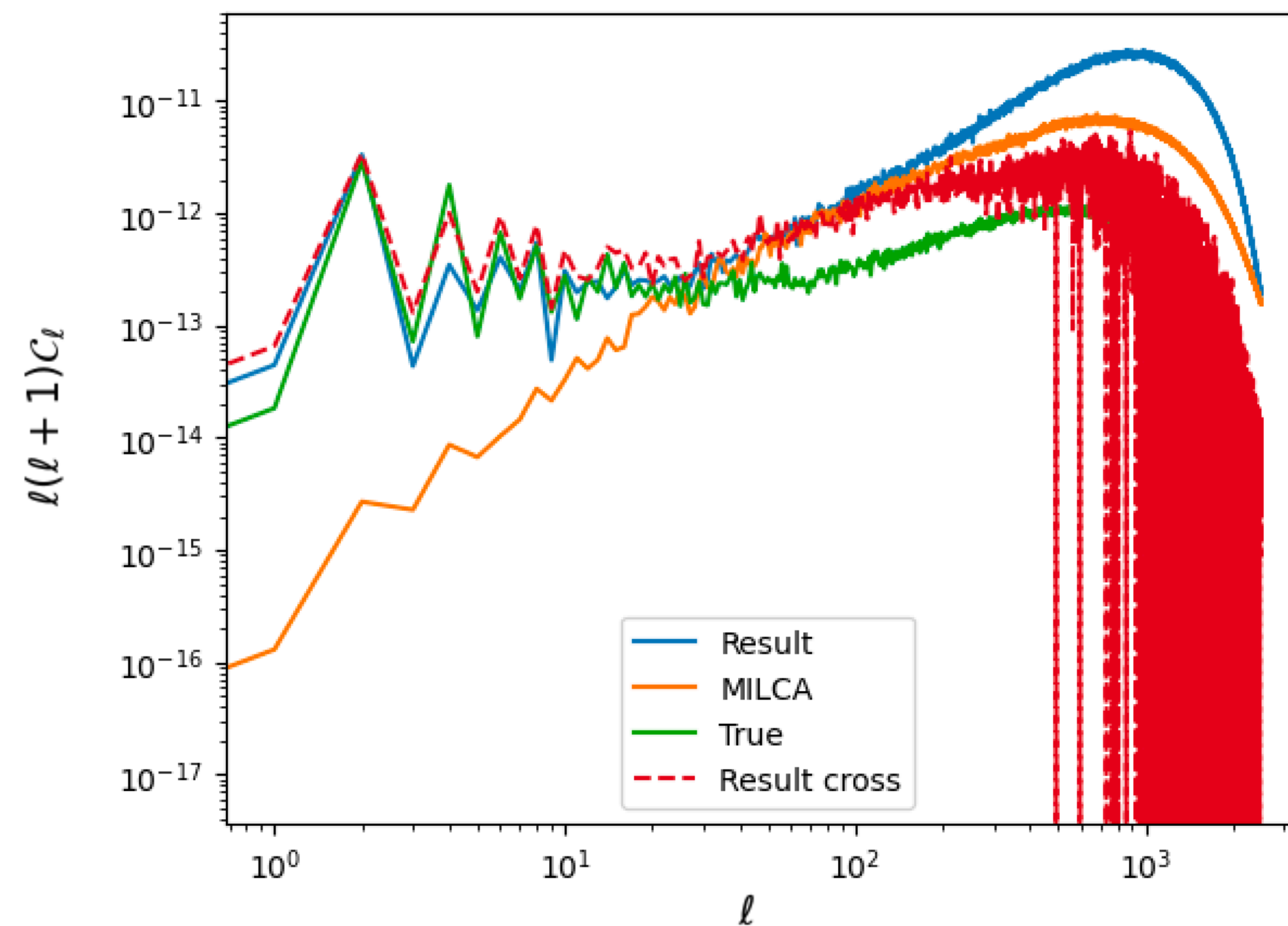


# Results including foregrounds, beams, and noise

SZ:



Cross-correlation on HM1 and HM2



Bonjean et al, in prep.

# Summary

- Functional deep learning network for blind multi-component separation of CMB, SZ, and CIB
- **Competitive** with state-of-the-art methods (MILCA)
- **Less contaminated** by other components thanks to an adaptative CIB model
- **Use the full information** of the maps (no need to degrade resolution)

# Next steps

- Include **polarization** maps
- Forecast for **SO** & **LiteBIRD**
- Application on foreground removal for **SKA** (M. Spinelli, J-L Starck)

Check it out on arxiv!

arXiv

