



# Particle acceleration and high-energy emission in AGN jets: M87 and Cen A

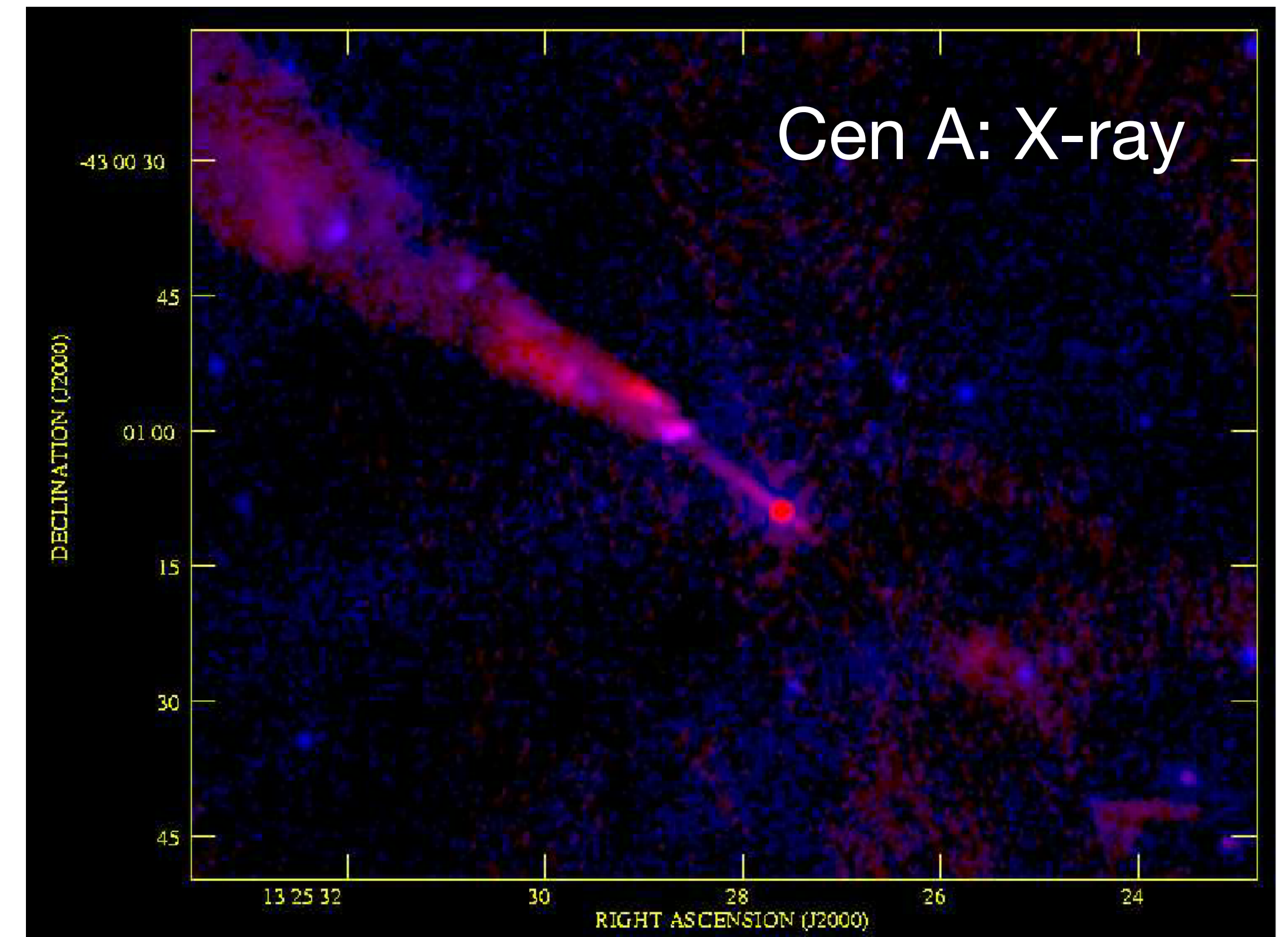
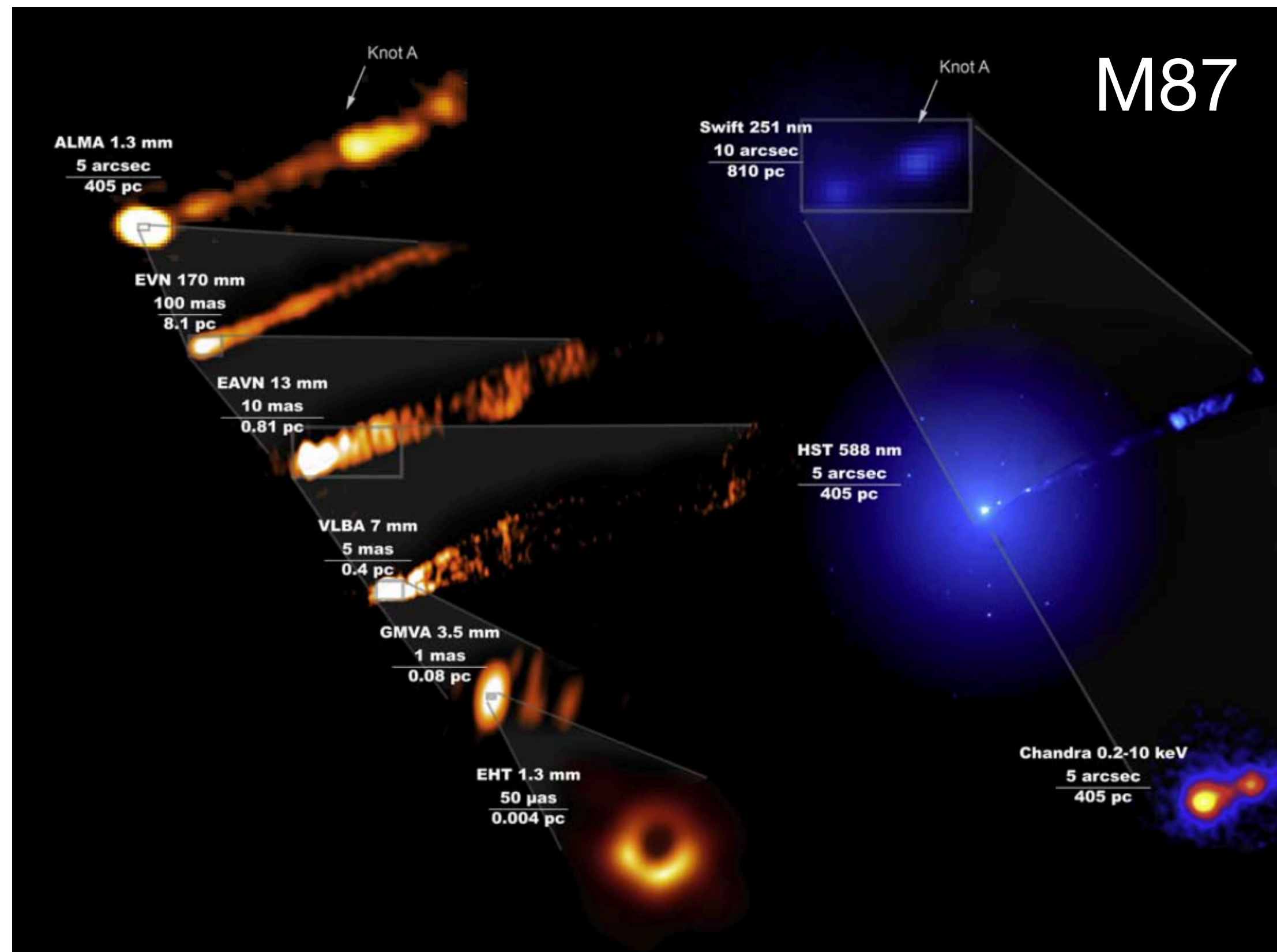
**Jieshuang Wang**

Max Planck Institute for Plasma Physics (IPP)

*Ack: Brian Reville (MPIK), Zigao Dai (USTC), Frank Rieger (IPP), Felix Aharonian (DIAS & MPIK), Yosuke Mizuno (SJTU)*

# Quasi-continuous radiation along the jet

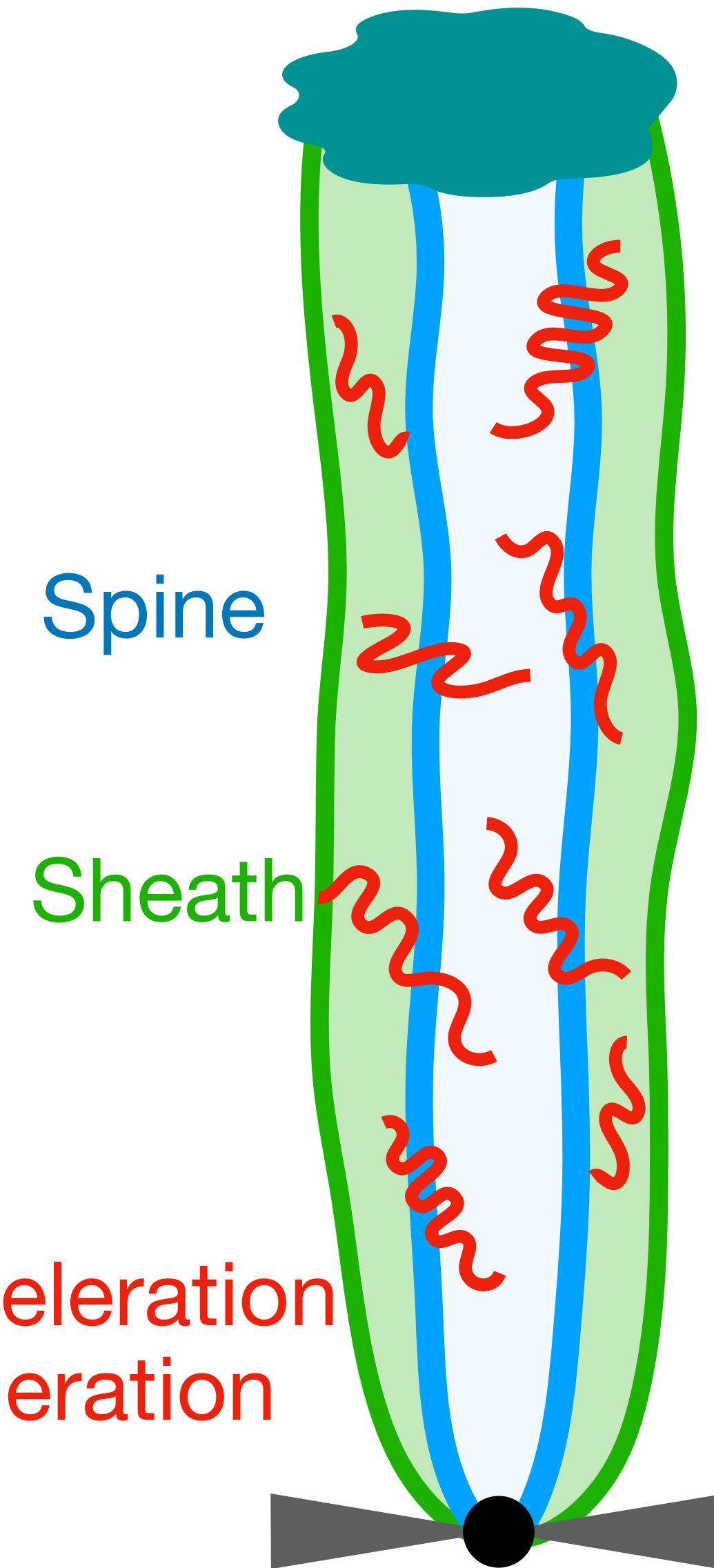
- ▶ M87: multi-wavelength observation resolving sub-pc and kpc scales
- ▶ Cen A: most nearby radio galaxies, radio to TeV observations on kpc-scale jets





# Continuous particle acceleration

- ▶ **Continuous particle acceleration** offers a natural explanation to continuous emission
- ▶ In **turbulent** jet flows, continuous acceleration by Fermi II mechanism
- ▶ In spine-sheath flows, continuous acceleration by shear acceleration
- ▶ Shock and magnetic reconnection in highly magnetized regions can produce more localized features (e.g. knots, hotspots) and add to the turbulence development



Fermi II acceleration  
Shear acceleration

# Fermi-II mechanism

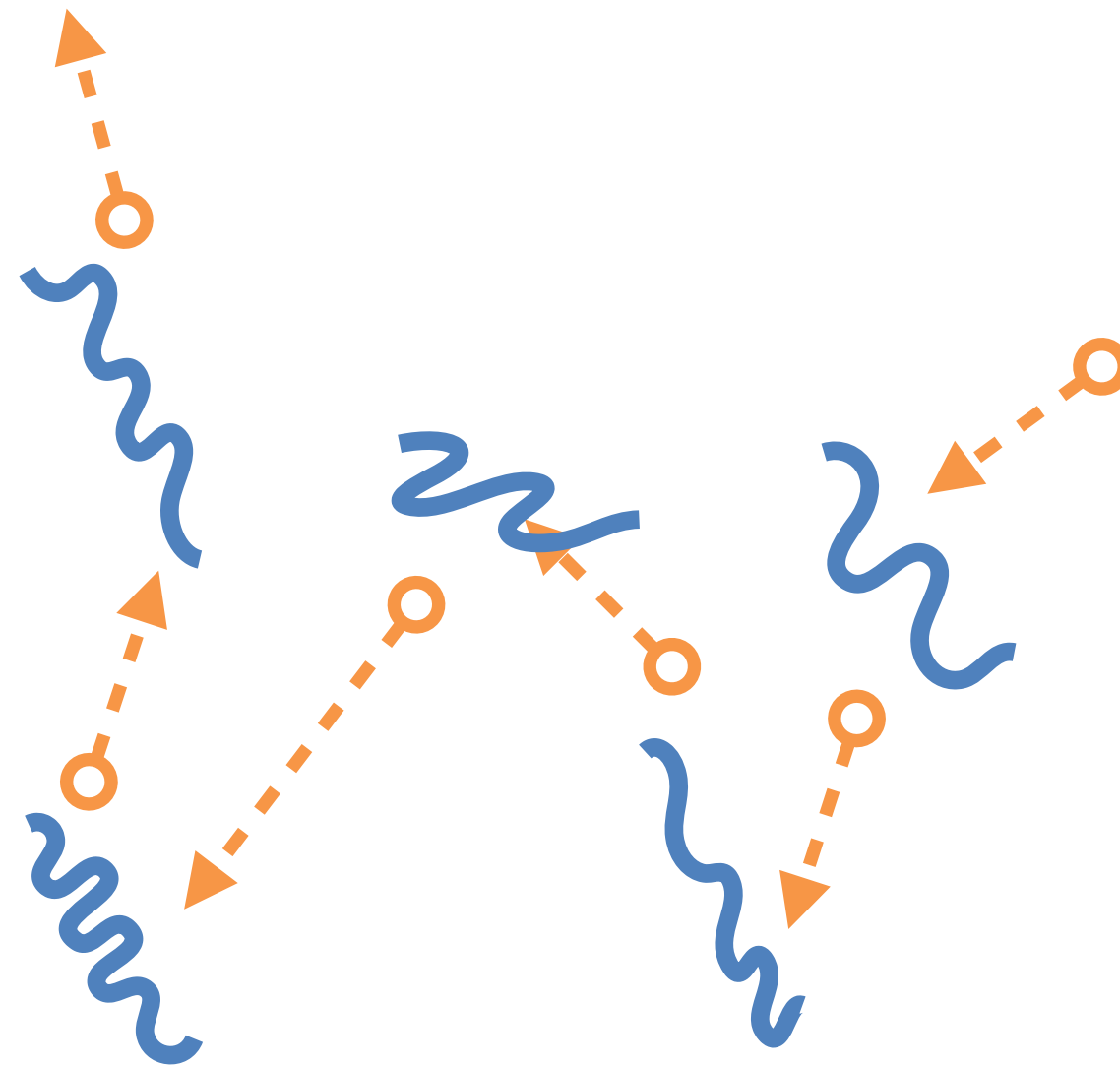
- ▶ Average energy gain in each collision by scattering MHD waves ( $u = v_A = B/\sqrt{4\pi\rho}$ )

$$\frac{\langle \Delta\epsilon \rangle}{\epsilon} \propto \left(\frac{u}{c}\right)^2$$

- ▶ Scattering time:  $\tau_{sc} \propto \epsilon^{2-q}$   
(turbulence index  $q$ )

- ▶ Acceleration time:

$$\tau_{\text{FermiII}} = \frac{\epsilon}{\langle \Delta\epsilon \rangle} \tau_{sc}$$



# Shear acceleration

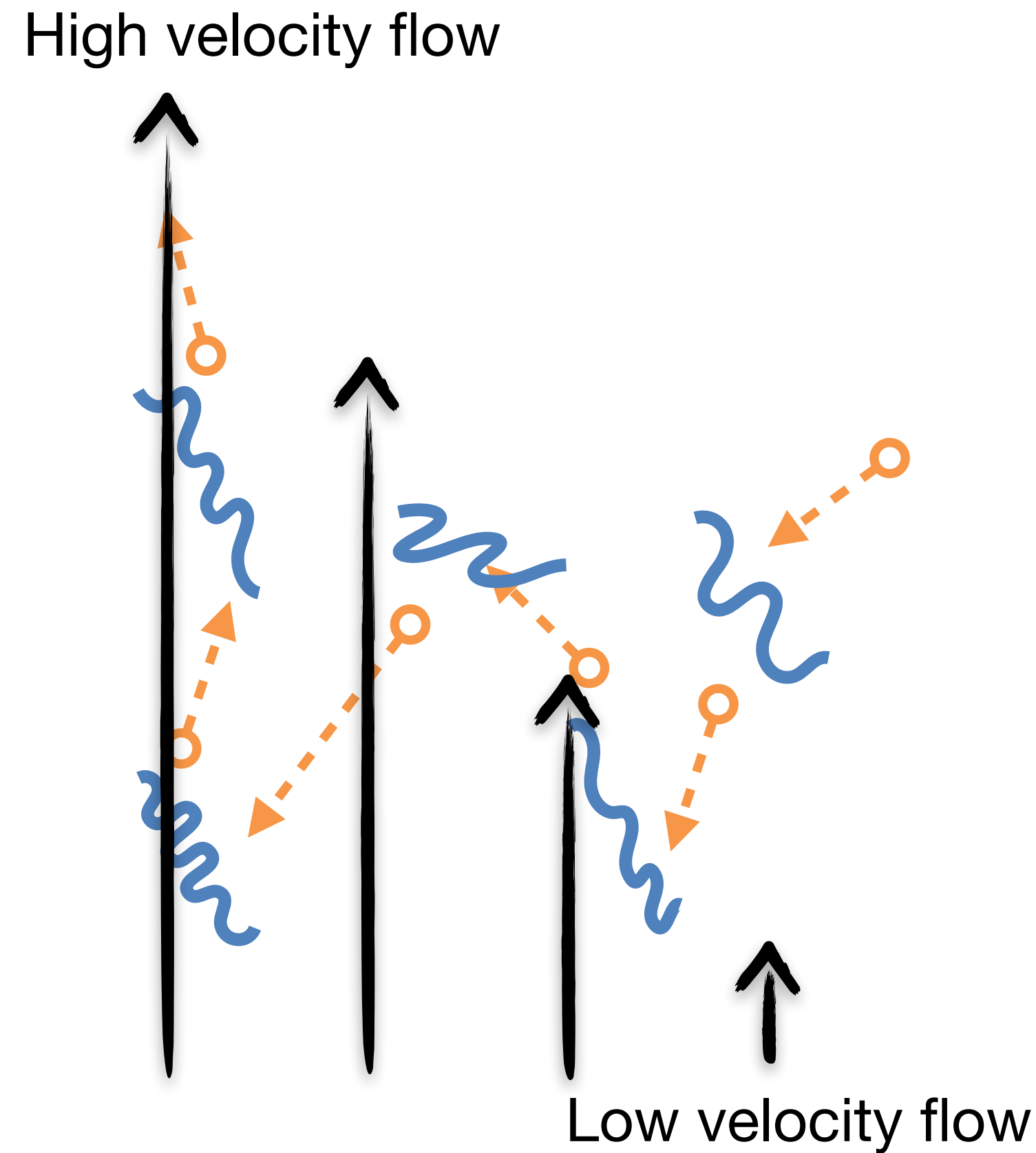
- Average energy gain in each collision by scattering MHD waves ( $u = v_A = B/\sqrt{4\pi\rho}$ )

$$\frac{\langle \Delta\epsilon \rangle}{\epsilon} \propto \left(\frac{u}{c}\right)^2$$

- Scattering time:  $\tau_{sc} \propto \epsilon^{2-q}$  (turbulence index  $q$ )

- Acceleration time:

$$\tau_{\text{FermiII}} = \frac{\epsilon}{\langle \Delta\epsilon \rangle} \tau_{sc}$$



- Shear is also stochastic-type
- Turbulences are embedded in velocity-shearing layers (spine-sheath)
- Particles scattering off turbulence will sample the velocity difference

$$\frac{\langle \Delta\epsilon \rangle}{\epsilon} \propto \left(\frac{\bar{u}}{c}\right)^2 \propto \left(\frac{\partial u_z}{\partial x}\right)^2 \tau_{sc}^2$$

$$\tau_{\text{shear}} = \frac{\epsilon}{\langle \Delta\epsilon \rangle} \tau_{sc}$$

*Berezhko & Krymsky 1981; Berezhko 1982; Earl+ 1988; Webb 1989; Jokipii & Morfill 1990; Webb+ 1994; Rieger & Duffy 2004, 2006, 2016; Liu+ 2017; Webb+ 2018, 2019; Lemoine 2019; Rieger & Duffy 2019, 2021, 2022*

# Analytical solution for Stochastic-type acceleration

- ▶ Fokker–Planck description for particle spectrum (steady state)

$$\frac{\partial n(\gamma, t)}{\partial t} = \frac{1}{2} \frac{\partial}{\partial \gamma} \left[ \left\langle \frac{\Delta \gamma^2}{\Delta t} \right\rangle \frac{\partial n(\gamma, t)}{\partial \gamma} \right] - \frac{\partial}{\partial \gamma} \left[ \left( \left\langle \frac{\Delta \gamma}{\Delta t} \right\rangle - \frac{1}{2} \frac{\partial}{\partial \gamma} \left\langle \frac{\Delta \gamma^2}{\Delta t} \right\rangle + \langle \dot{\gamma}_c \rangle \right) \times n(\gamma, t) \right] - \frac{n}{t_{\text{esc}}} + Q(\gamma, t)$$

- ▶ **Cutoff power-law spectrum** for both mechanism: **turbulence, magnetic field (B), jet velocity (v) and profile**

**Fermi II:**  $N(\gamma') \propto \gamma'^{-p} \exp\left[-\left(\frac{\gamma'}{\gamma'_{\text{cut,Fermi-II}}}\right)^{3-q}\right]$        $p_{\text{Fermi-II}} = q - 1$

Cutoff frequency:  $\nu'_{\text{cut,Fermi-II}} = 2.9 \times 10^4 \beta_{A,-1}^3 \zeta_{-2}^{3/2} B_{-1}'^{-3/2} R_{-2}^{-1}$  GHz

**Shear:**  $n(\gamma') \propto \gamma'^{s_-} F_-(\gamma', q) + C \gamma'^{s_+} F_+(\gamma', q)$

$$s_{\pm} = \frac{q-1}{2} \pm \sqrt{\frac{(5-q)^2}{4} + w}$$

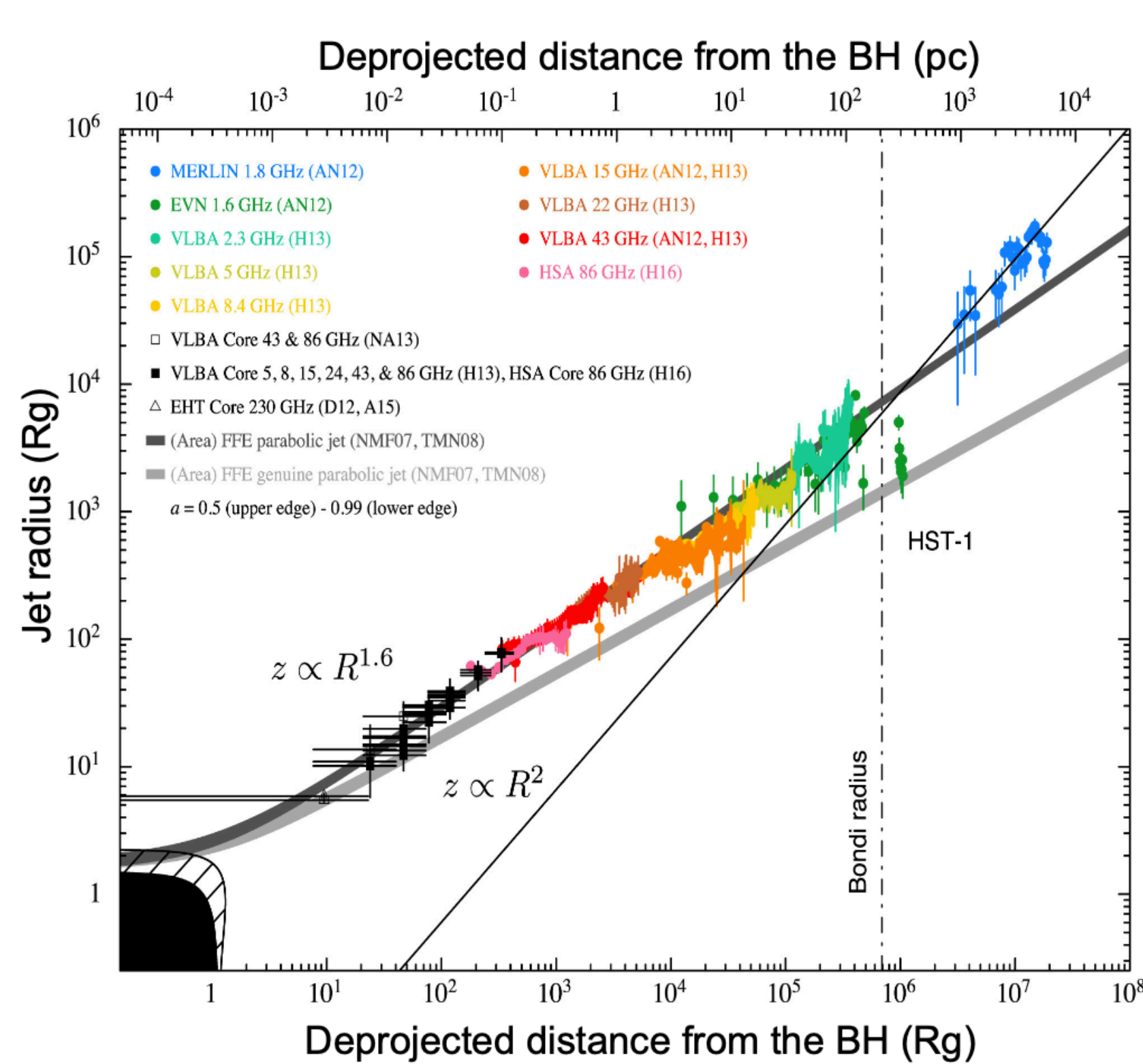
Cutoff frequency:  $\nu'_{\text{cut,sh}} = 2.4 \times 10^9 w_{-1}^{-3} \zeta_{-2}^{-3} B_{-1}'^{-6} R_{-2}^{-4}$  GHz

$$w = \frac{10c^2}{\Gamma^4(r)R^2} \left( \frac{\partial u(r)}{\partial r} \right)^{-2}$$

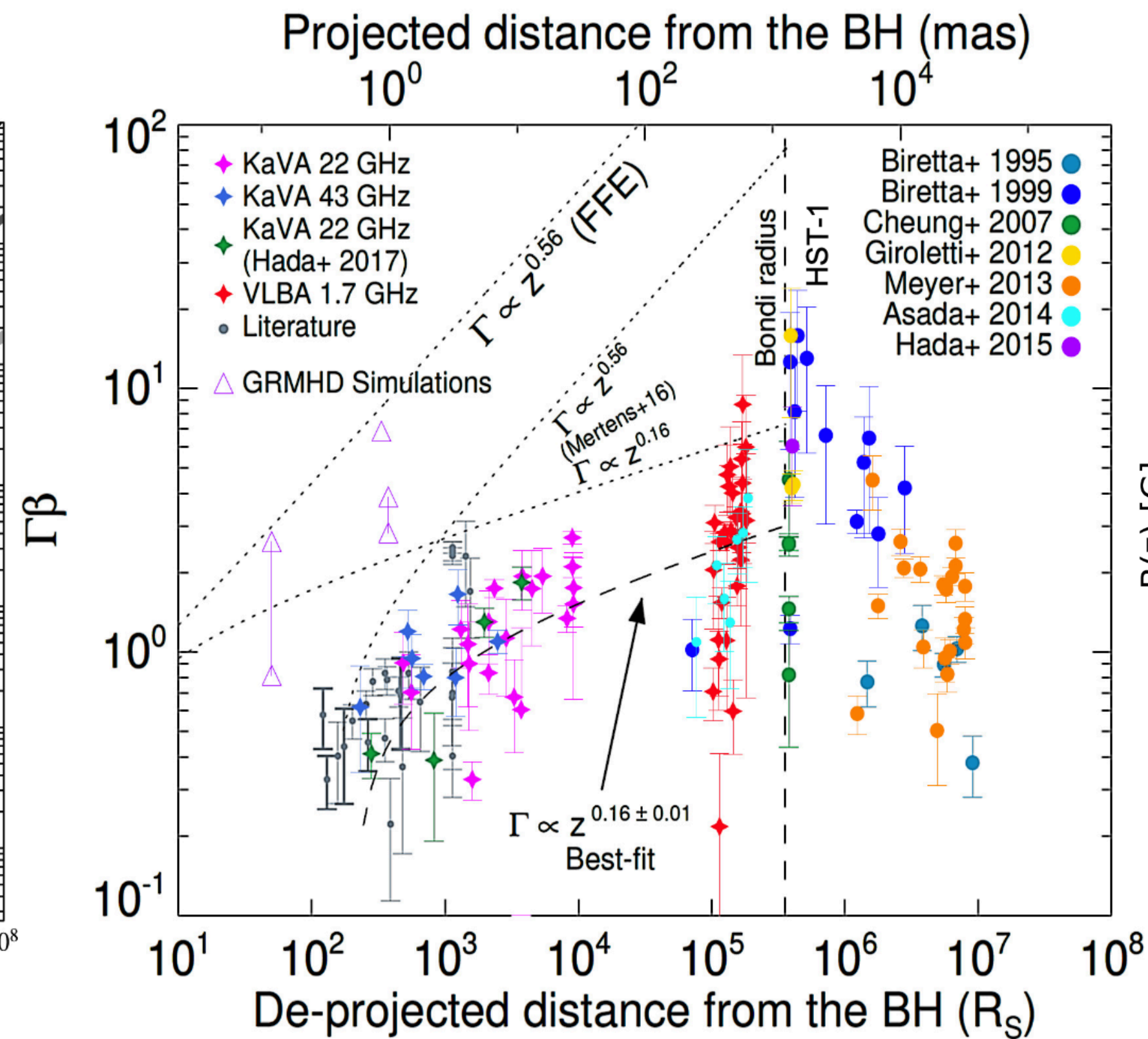
J.S.Wang+, 2021, arXiv:2105.08600, 2024, arXiv:2404.08625



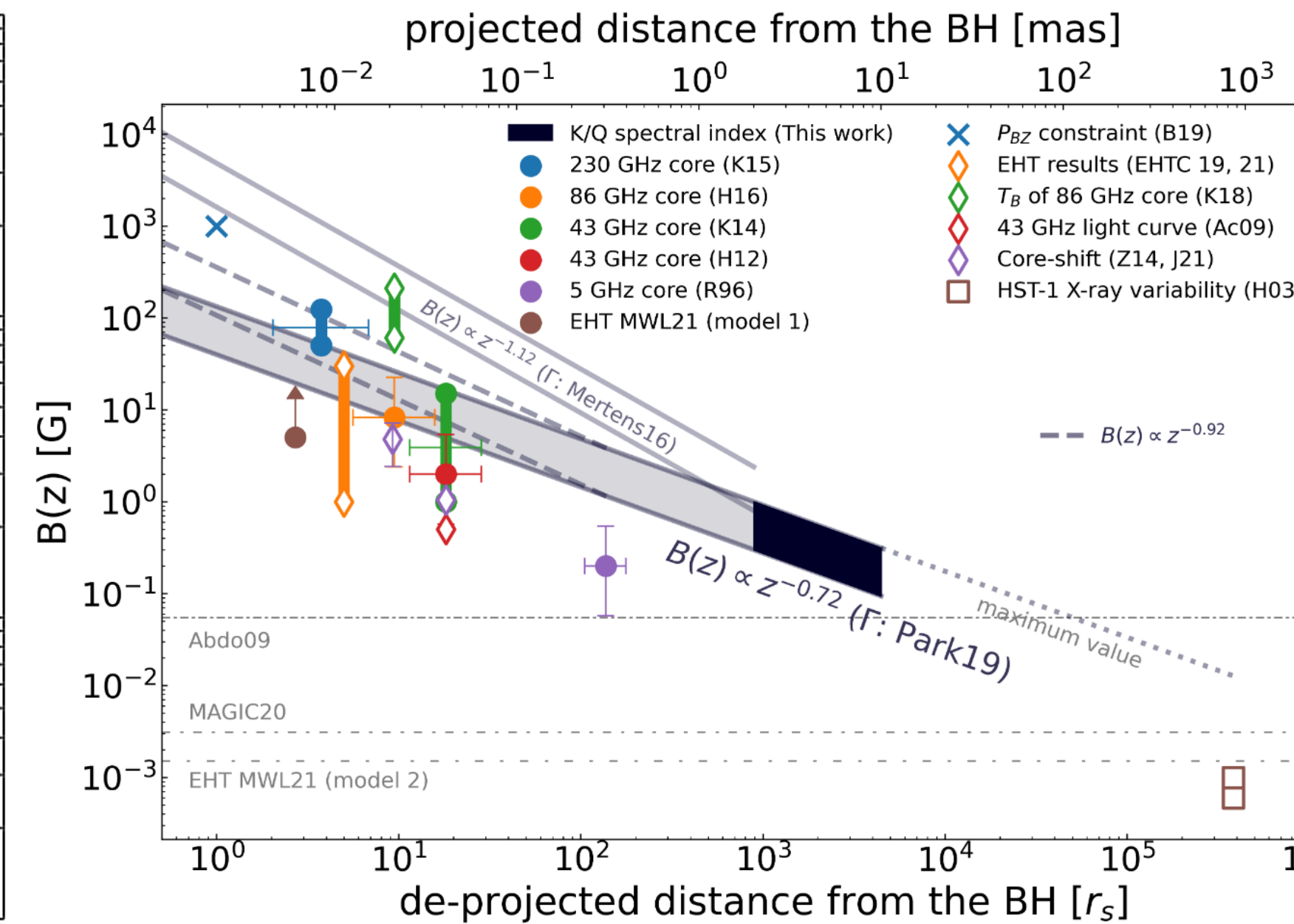
# Observed profiles for the M87 inner jet



$$R(z) = 1.67 r_g (z/r_g)^{0.625}$$



$$\Gamma_j(z) = 0.8 (z/r_g)^{0.16}$$



$$B'(z) \propto (\Gamma_j R)^{-1} = 80 (z/r_g)^{-0.785} \text{ G}$$

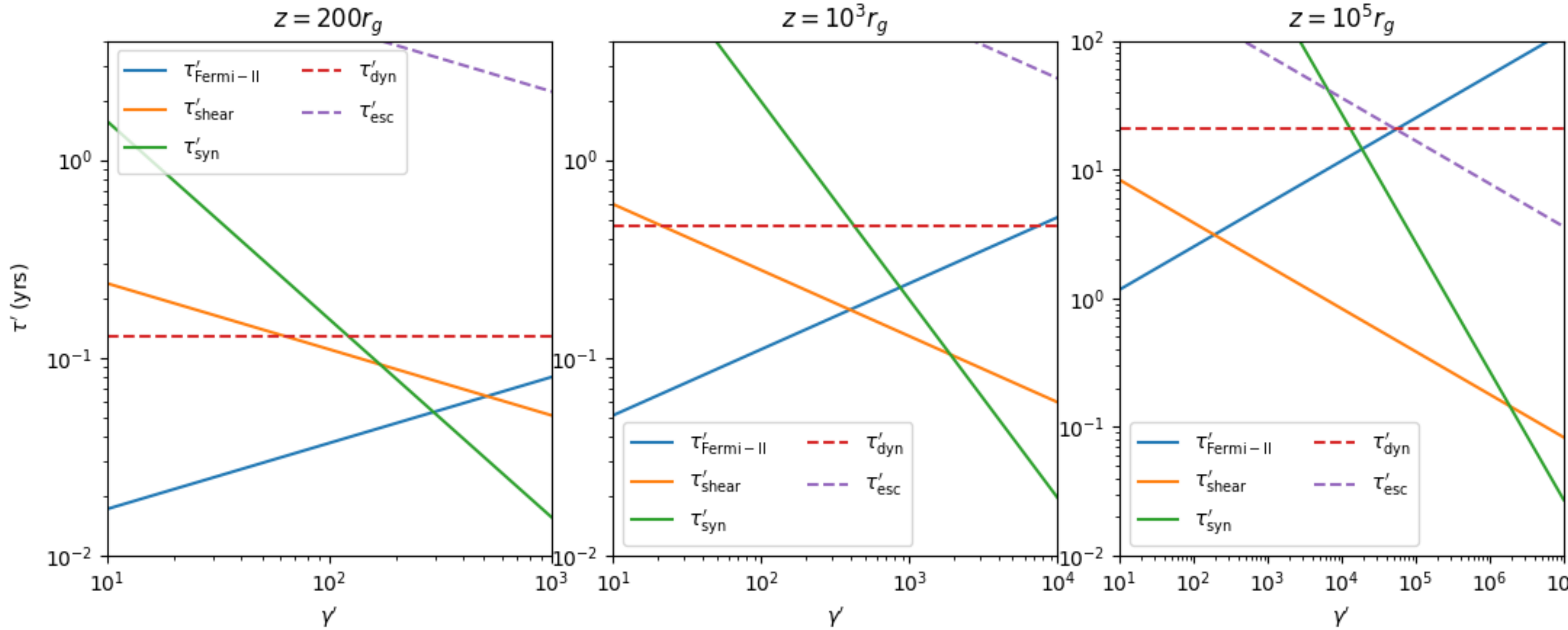
Nakamura+ 2018; Park+ 2019; Ro+ 2023



# Dominant acceleration process for M87

time scale vs.  
electron energy  
for different  
distance to the  
black hole (z)

Shear acceleration  
takes over at larger z



$$\tau'_{\text{Fermi-II}} = 2(2+q)^{-1} c^{3-2q} B'^{q-2} e^{q-2} m_e^{2-q} \gamma'^{2-q} \lambda'_c{}^{q-1} A'^{-1}_{\text{Fermi-II}} \zeta^{-1} \approx 1.5 \times 10^{-4} R_{-2}^{2/3} \gamma'^{1/3} B'^{-1/3} \beta_A^{-2} \zeta_{-2}^{-1} \text{ yrs},$$

$$\tau'_{\text{shear}} = 1.5(6-q)^{-1} w B'^{2-q} e^{2-q} m_e^{q-2} \gamma'^{q-2} R^2 \lambda'_c{}^{1-q} \zeta = 1.4 \eta R_{-2}^{4/3} B'^{1/3} w \zeta_{-2} \gamma'^{-1/3} \text{ yrs},$$

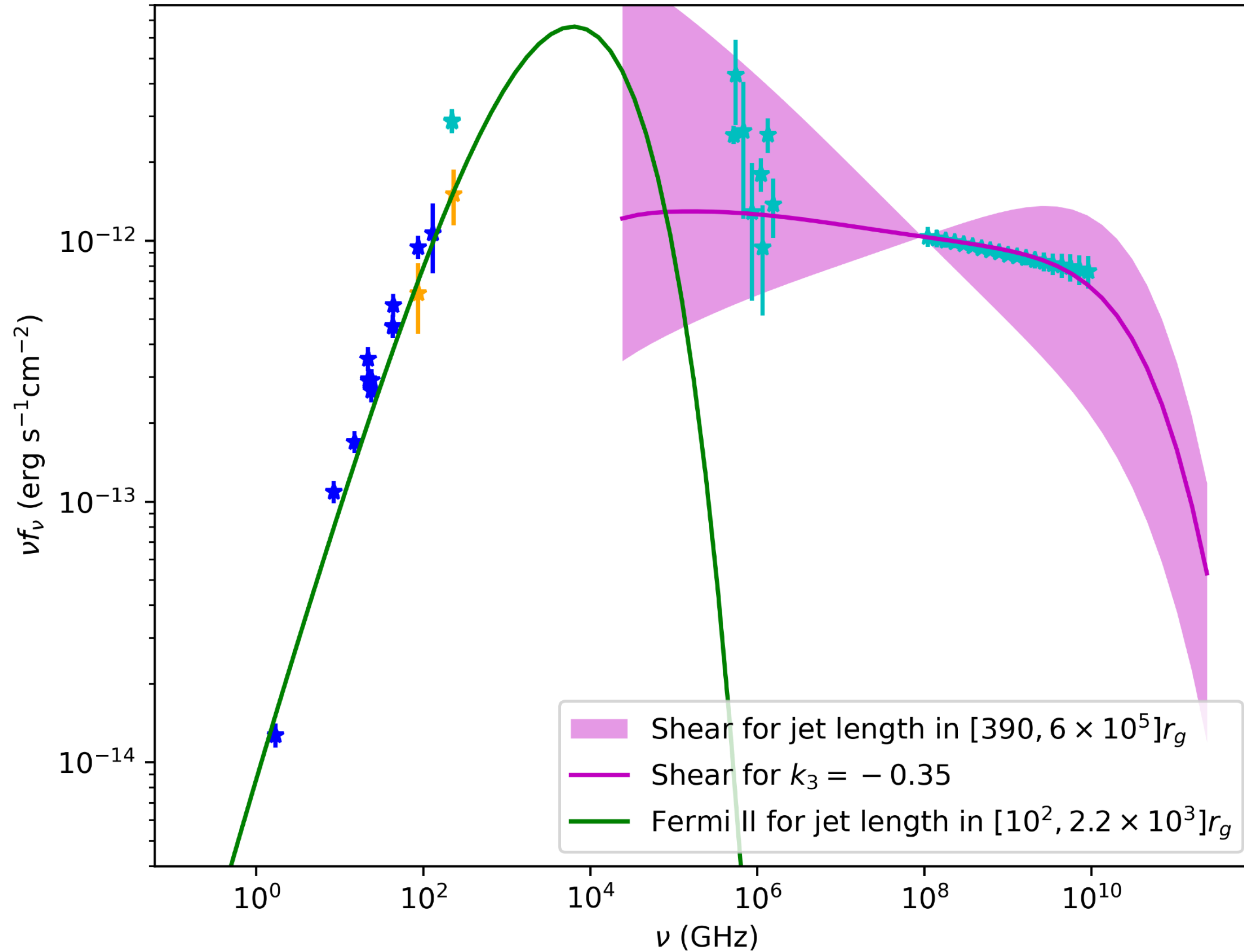
$$w = 0.1, \beta_A = 0.1$$

$$\tau'_{\text{sc}} \approx \zeta^{-1} r'_L{}^{2-q} \lambda'_c{}^{q-1} c^{-1}$$

J.S.Wang+, 2024, arXiv:2404.08625



# Application to inner jet of M87



$$f_\nu = \int_{z_{\min}}^{z_{\max}} f_\nu(z) dz.$$

Integration region determined by the angular resolution at corresponding frequencies

$$f_\nu(z) dz = \delta_D^3(z) S(z) dz \int_{\gamma'_{\min}}^{+\infty} n'(\gamma', z) F_{\text{syn}}(\gamma', \nu') d\gamma'$$

$$\delta_D = [\Gamma_j (1 - \beta_j \cos i)]^{-1}$$

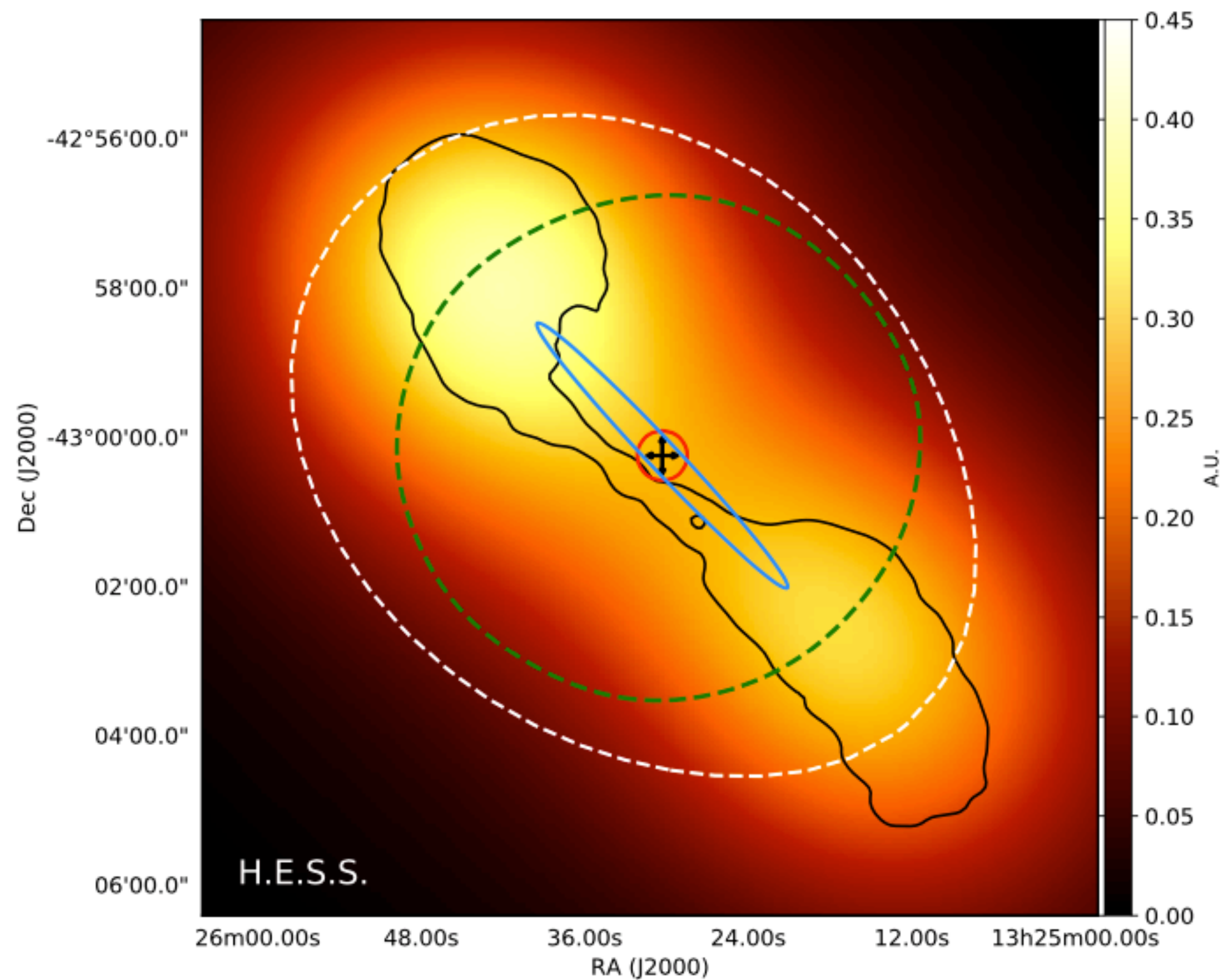
Shaded region depends on the number density over distance ( $z$ ) to the black hole

$$n'(z) \propto z^{k_3} \rho'(z)$$

*J.S.Wang+, 2024, ApJ, arXiv:2404.08625*

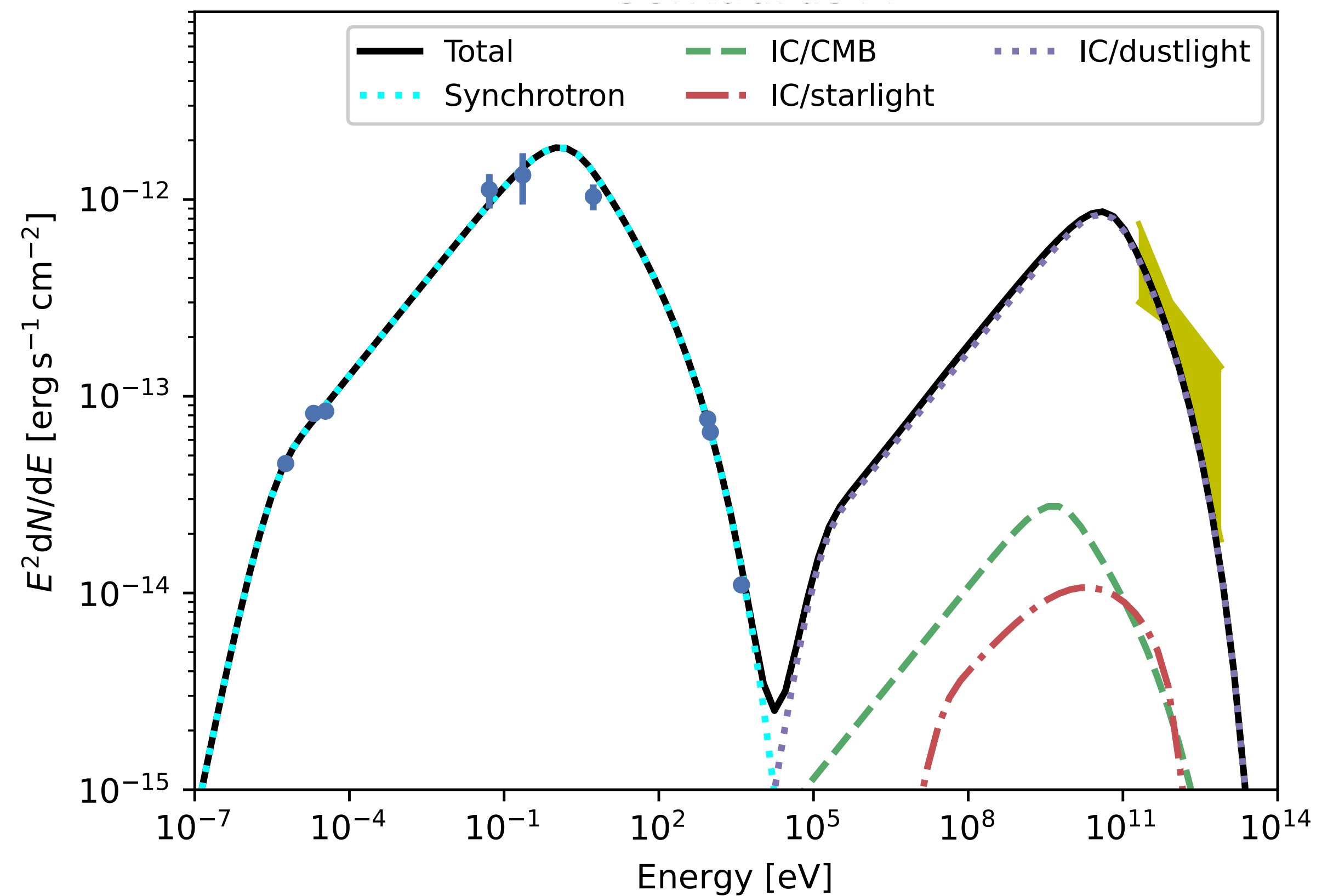
# Application to kpc-scale jet of Cen A

TeV observations by HESS  
 $v \sim 0.6c$  by radio observations



H. E. S. S. Collaboration, 2020, Nature

X-ray and TeV emission explained by  
shear acceleration



J.S.Wang+, 2021, MNRAS, [arXiv:2105.08600](https://arxiv.org/abs/2105.08600)



**Analytical theory works for observations**

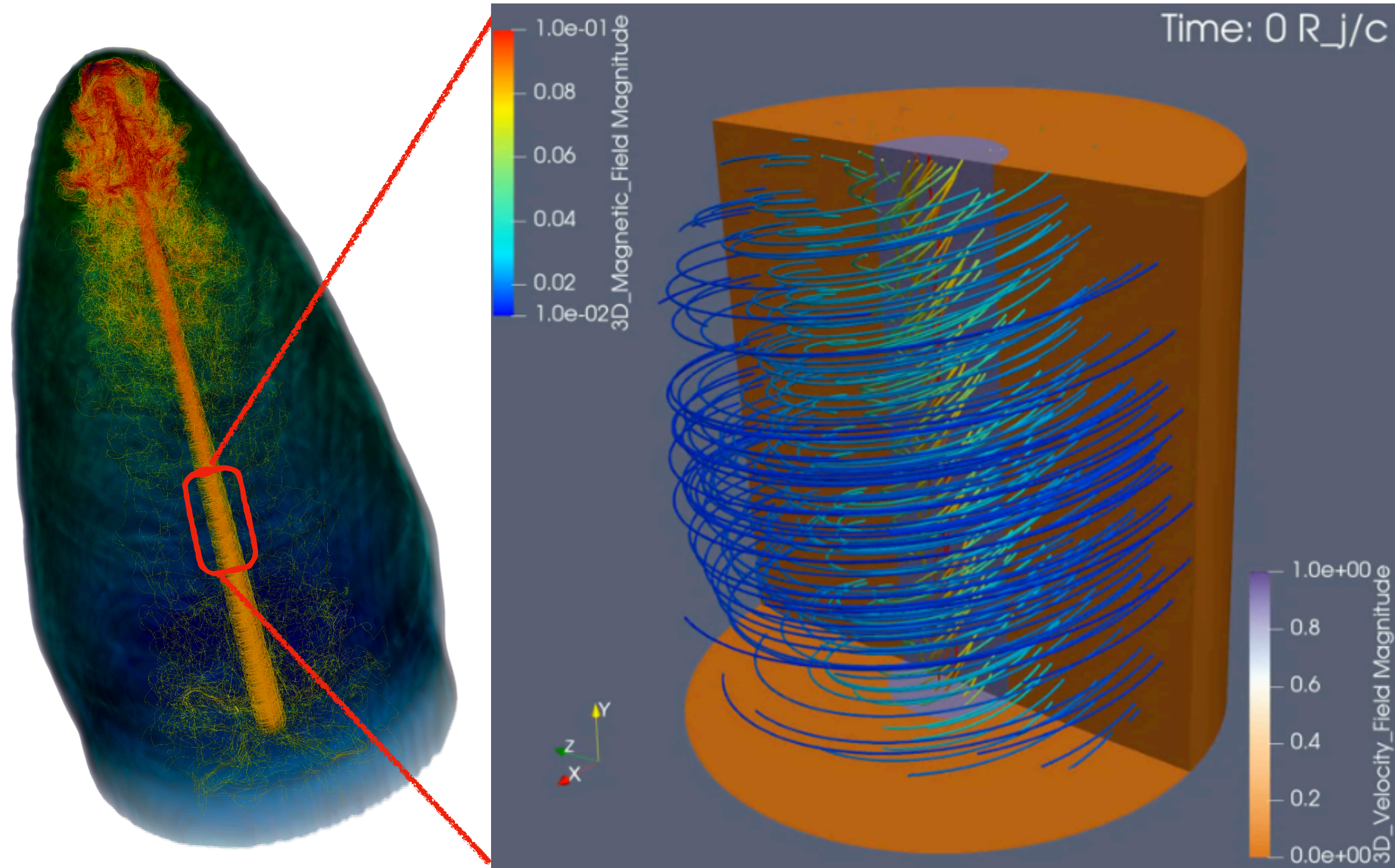


**Numerical simulations for stochastic-shear acceleration**



# Relativistic MHD simulations with PLUTO

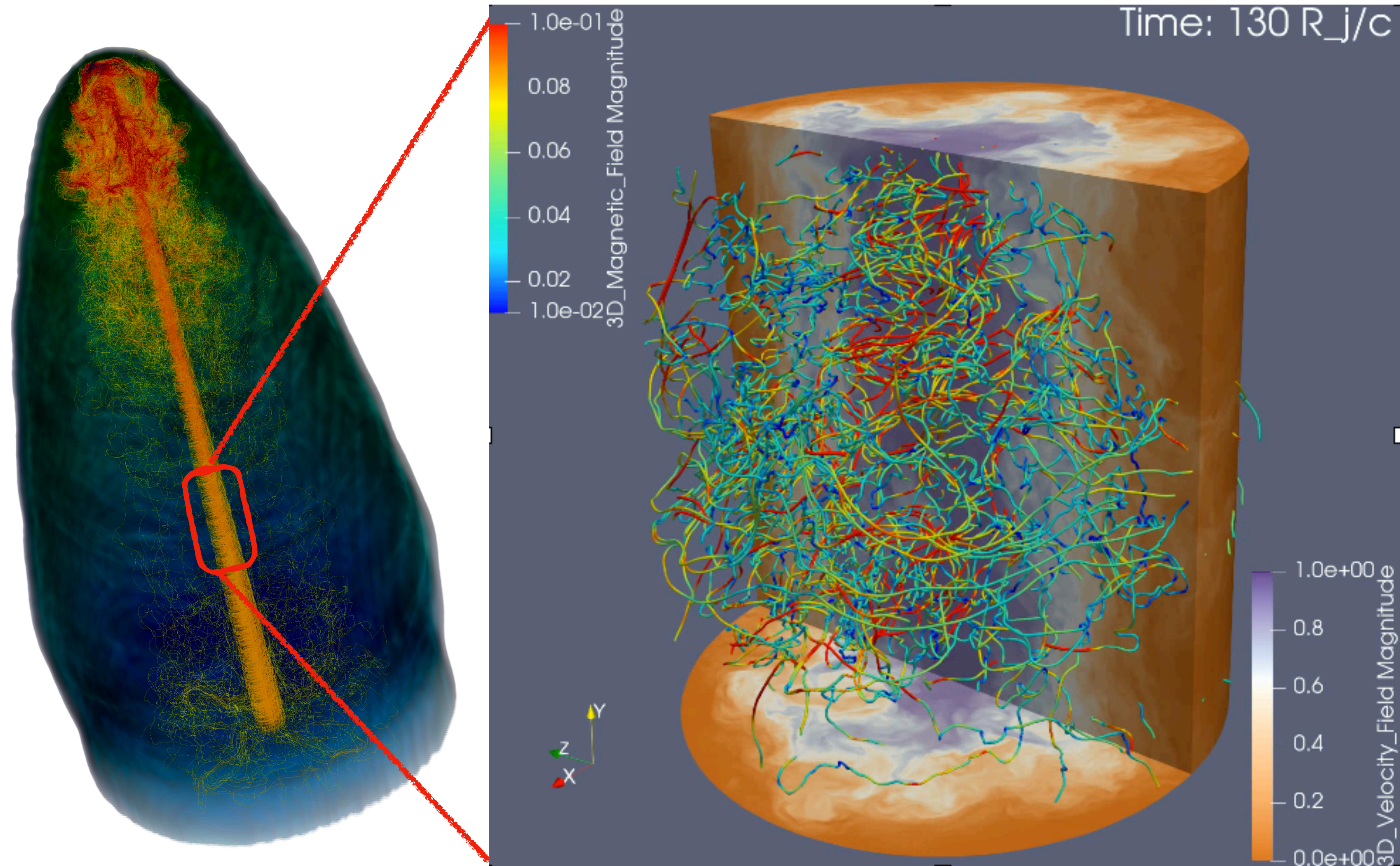
- ▶ Stochastic-shear acceleration depends on turbulence and velocity profile
- ▶ Periodic box simulations to study the jet instabilities (e.g. Kelvin-Helmholtz)
- ▶ Different parameters from analytical modeling of radio galaxies :  
 $v \in [0.6, 0.99]c$ ,  
 $\sigma \in [0.002, 0.2]$   
 $\sigma_{y,\phi} = \langle B_{y,\phi}^2 \rangle / 8\pi\rho_0 c^2$





# Relativistic MHD simulations with PLUTO

- ▶ Stochastic-shear acceleration depends on turbulence and velocity profile
- ▶ Periodic box simulations to study the jet instabilities (e.g. Kelvin-Helmholtz)
- ▶ Different parameters from analytical modeling of radio galaxies :  
 $v \in [0.6, 0.99]c$ ,  
 $\sigma \in [0.002, 0.2]$   
 $\sigma_{y,\phi} = \langle B_{y,\phi}^2 \rangle / 8\pi\rho_0 c^2$



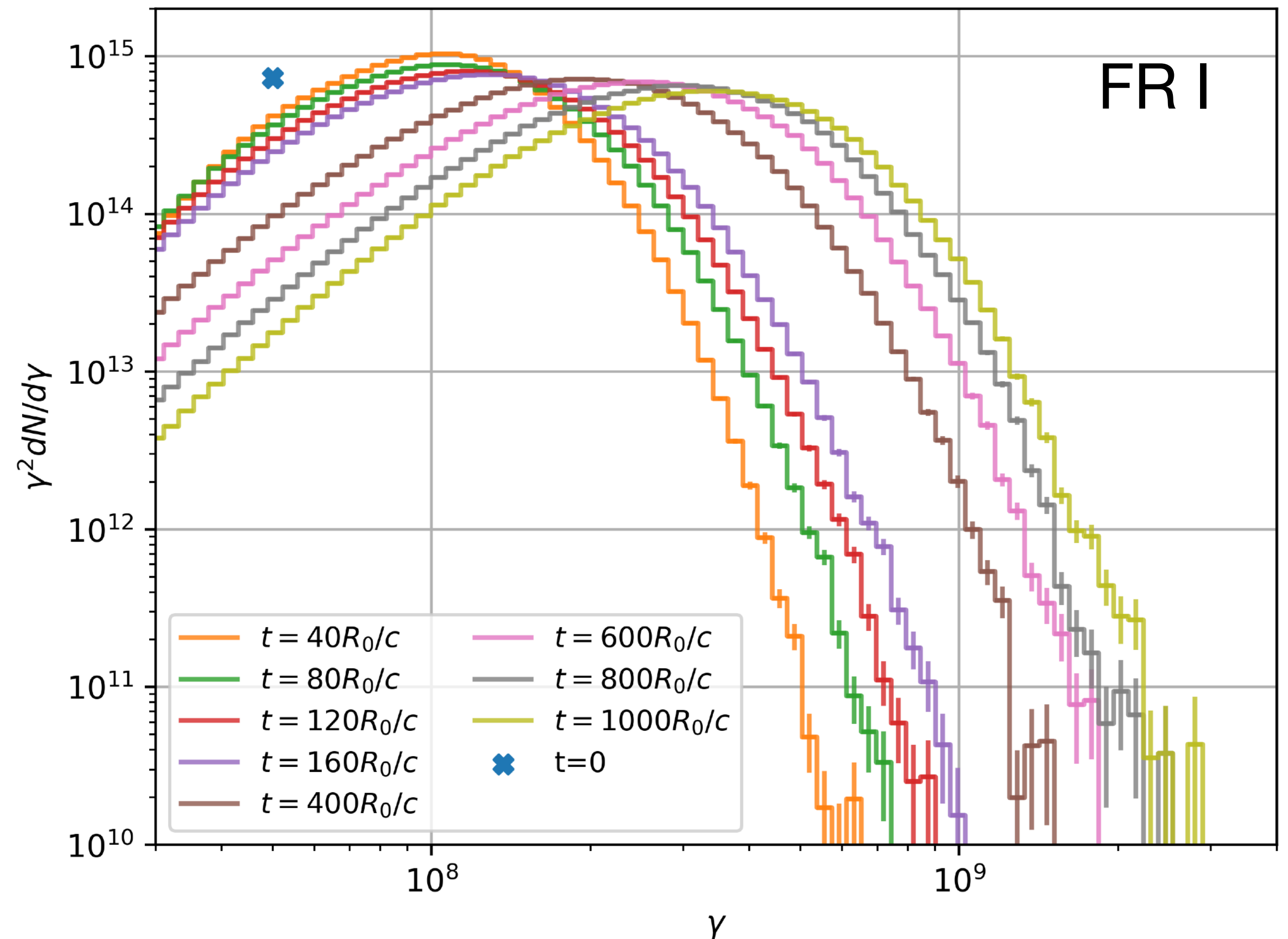


# Relativistic MHD + Test-particle Simulations

- ▶ Higher-resolution ( $\sim 1000^3$ ) runs without sub-grid physics for test particles

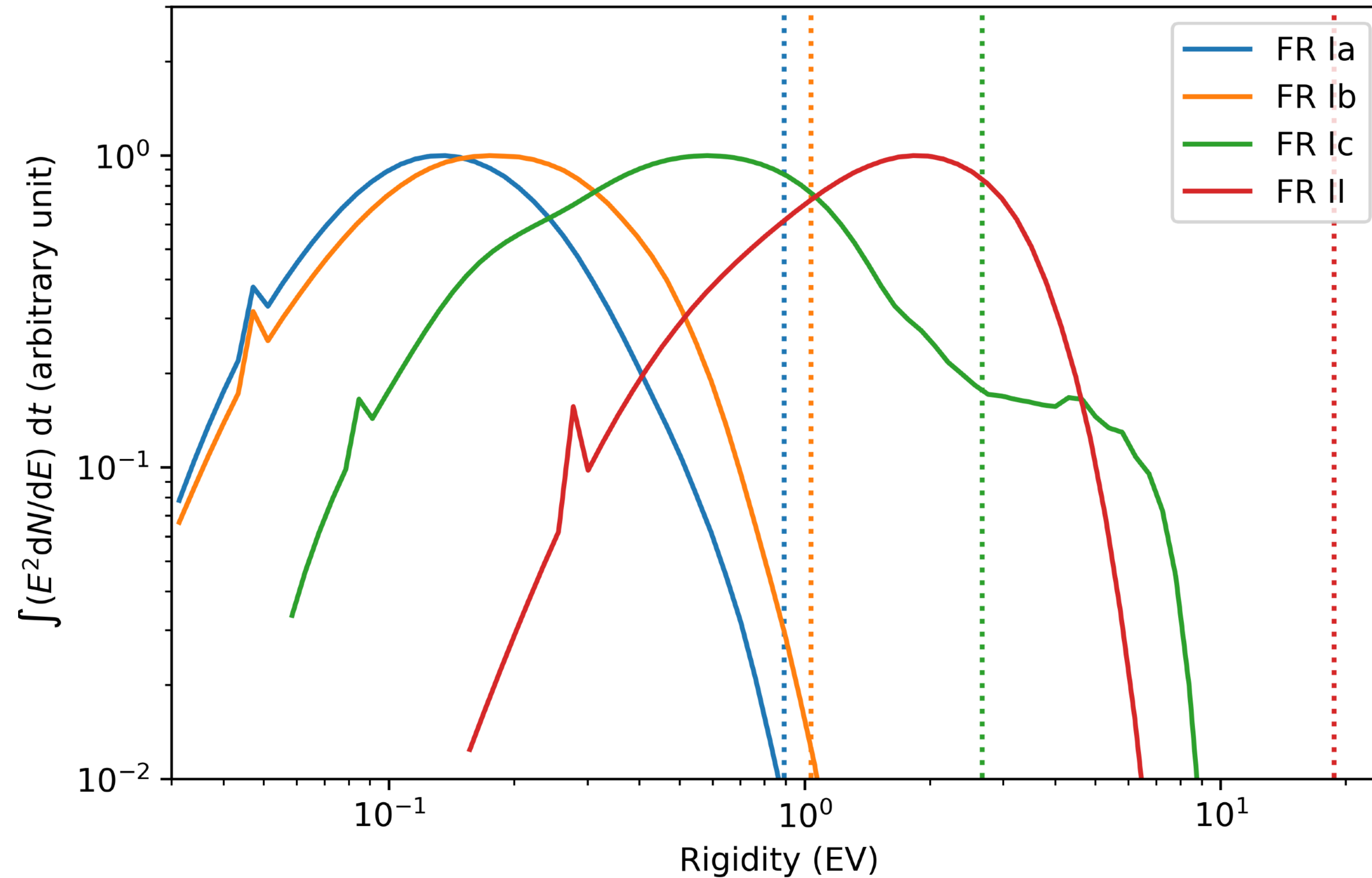
$$R_{\text{domain}} : R_0 : r_{g,\text{inj}} : \Delta x \approx 1000 : 200 : 3 : 1$$

- ▶ FR I: ( $v = 0.6c$ ,  $R_0 = 0.1\text{kpc}$ )
- ▶ FR II: ( $v = 0.9c$ ,  $R_0 = 1\text{kpc}$ )
- ▶ Magnetization:  $\sigma = 0.02, 0.2$





# Particle spectrum



Rigidity=  $E/Ze$

$E_{\text{peak}} \approx 0.1 - 0.3 E_{\text{Hillas}}$   
 $E_{\text{Hillas}} \approx Ze\bar{v}BR$   
 for different  $v$  and  $B$  values

Particles efficiently accelerated close to the maximum theoretical limit (Hillas limit)

# Summary

- ▶ Stochastic-shear acceleration is an **unavoidable (KH instability) and efficient** mechanism in relativistic jets
- ▶ In the framework of stochastic-shear acceleration, both **multi-wavelength observation** of M87 inner jet and Cen A jet can be explained
- ▶ Cosmic rays can be accelerated to close to the maximum theoretical limit ( $E_{\text{peak}} \approx 0.1 - 0.3 E_{\text{Hillas}}$ ), and large-scale AGN jet can contribute to CRs above EeV