

# Chromospheric Magnetic Field Reconstruction through Neural Field Assisted Spectropolarimetric Inversions

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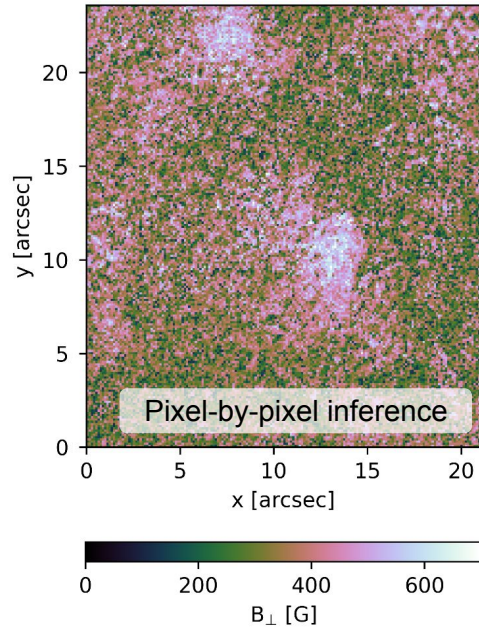
Collaborators: Andrés Asensio Ramos, Jaime de la Cruz Rodríguez, J. M. da Silva Santos,  
Luc Rouppe van der Voort



Rosseland  
Centre  
for Solar  
Physics

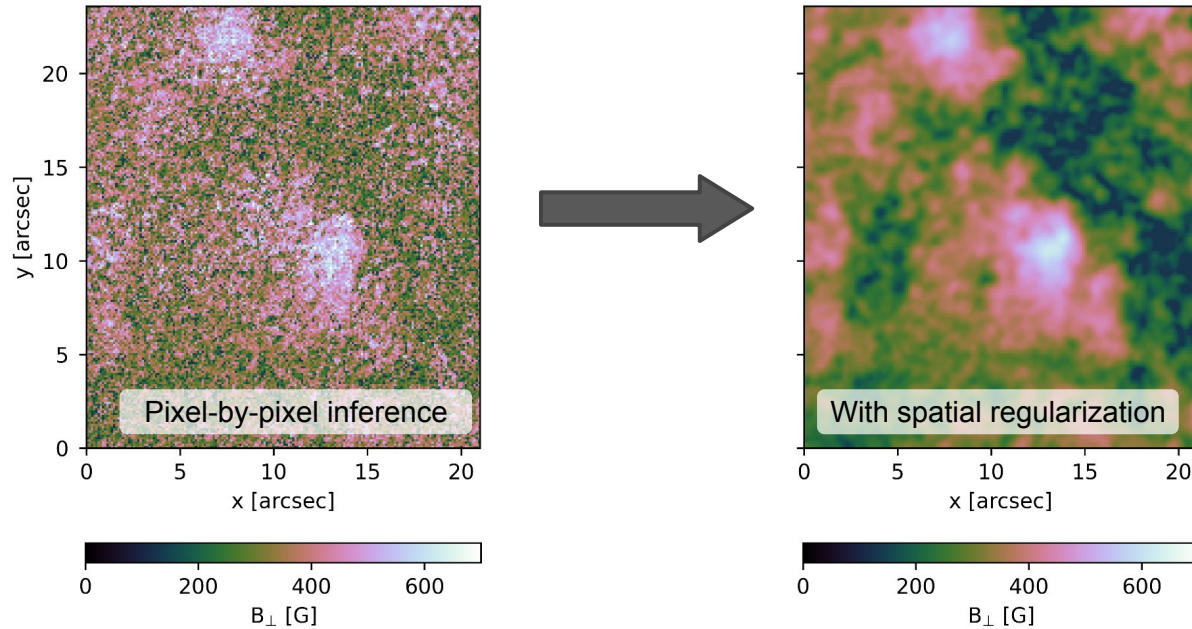
# Magnetic field inference

Mg I  $b_2$  5173 Å (CRISP@SST)



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⇒ Imposing coherent solutions improve the estimation, without averaging in space or time.

# How do we impose this coherence?

## Explicit vs Implicit

$$\mathcal{L} = \sum_{\lambda_i} \left( \frac{S(\lambda_i)^{obs} - S(\lambda_i)^{syn}}{\sigma_i} \right)^2$$

Quantity to optimize

$\chi^2$

# How do we impose this coherence?

## Explicit vs Implicit

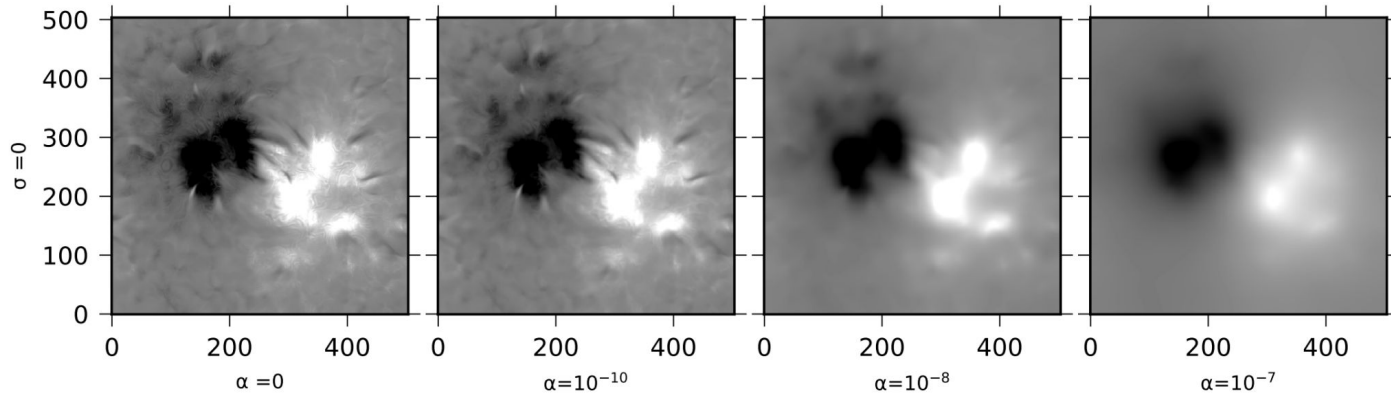
$$\mathcal{L} = \sum_{\lambda_i} \left( \frac{S(\lambda_i)^{obs} - S(\lambda_i)^{syn}}{\sigma_i} \right)^2 + \alpha \left[ \left( B_{\parallel}^{(x,y)} - B_{\parallel}^{(x,y-1)} \right)^2 + \left( B_{\parallel}^{(x,y)} - B_{\parallel}^{(x,y+1)} \right)^2 + \left( B_{\parallel}^{(x,y)} - B_{\parallel}^{(x-1,y)} \right)^2 + \left( B_{\parallel}^{(x,y)} - B_{\parallel}^{(x+1,y)} \right)^2 \right].$$

$\chi^2$

# How do we impose this coherence?

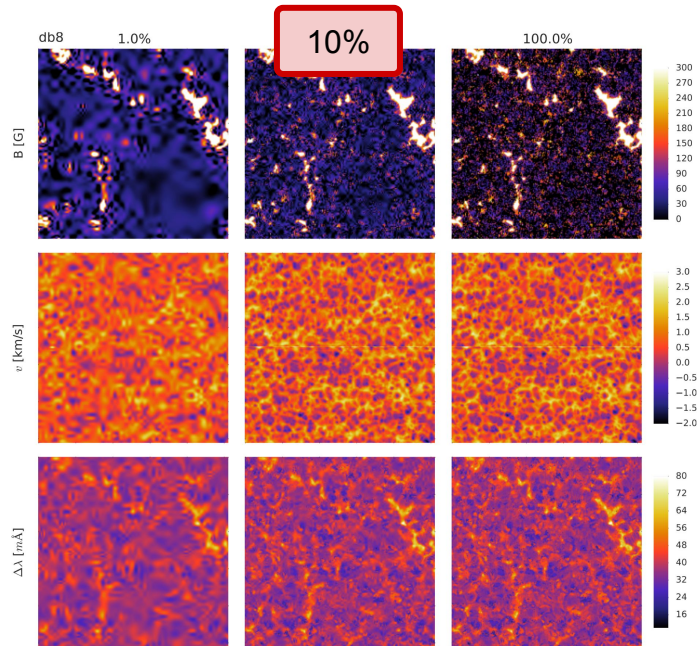
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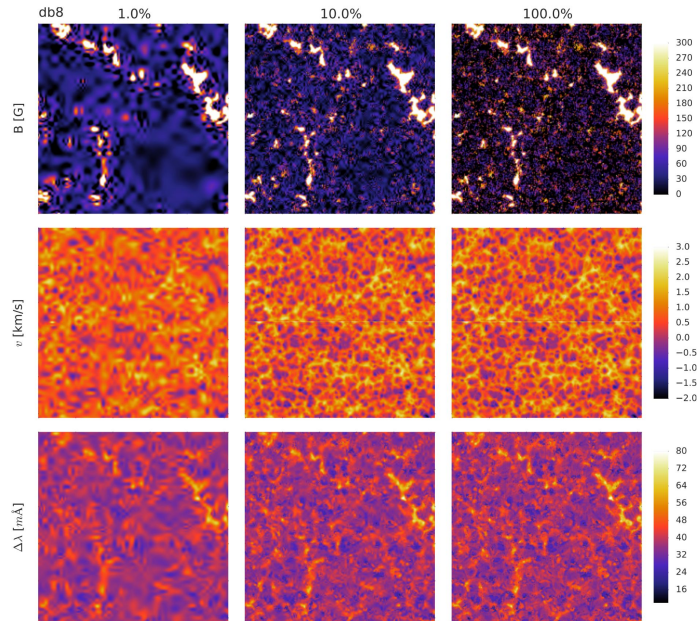


$$\mathcal{L} = \chi^2 + \alpha ||g(\mathbf{P})||_0$$

↑  
Compact  
representation in  
wavelet space

# How do we impose this coherence?

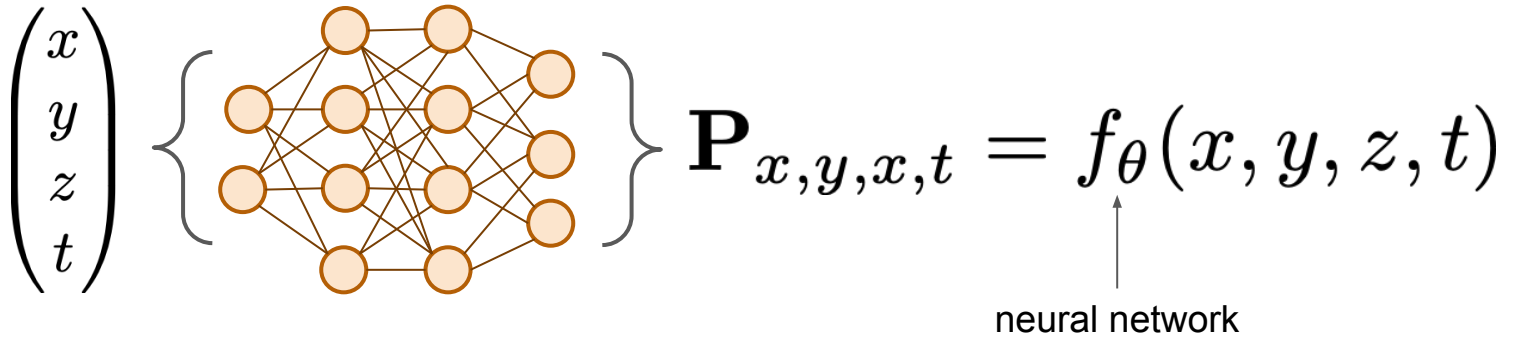
Explicit vs Implicit ←



$$\mathcal{L} = \chi^2 + \alpha \|g(\mathbf{P})\|_0$$

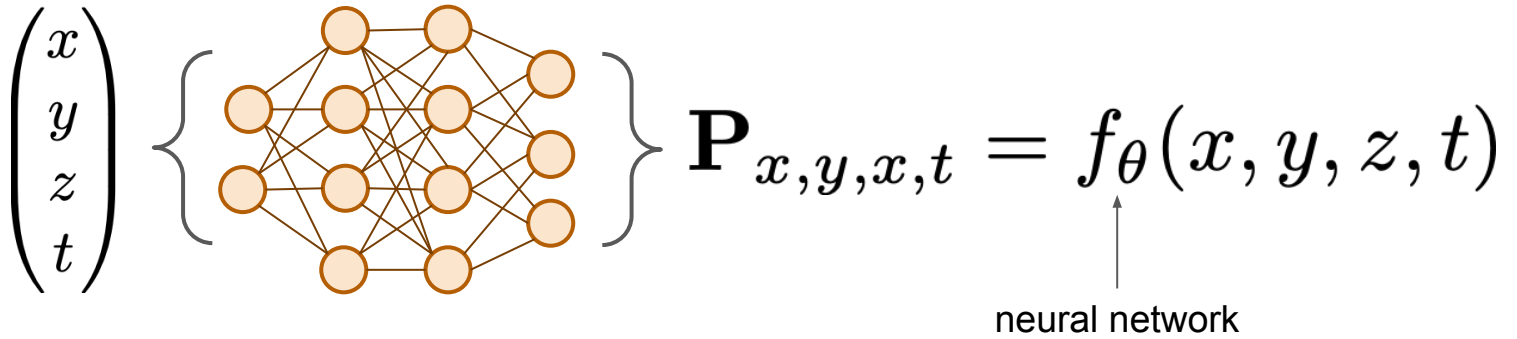


# New parametrization: neural fields



⇒ **Compact, continuous and differentiable** approximation in the whole domain

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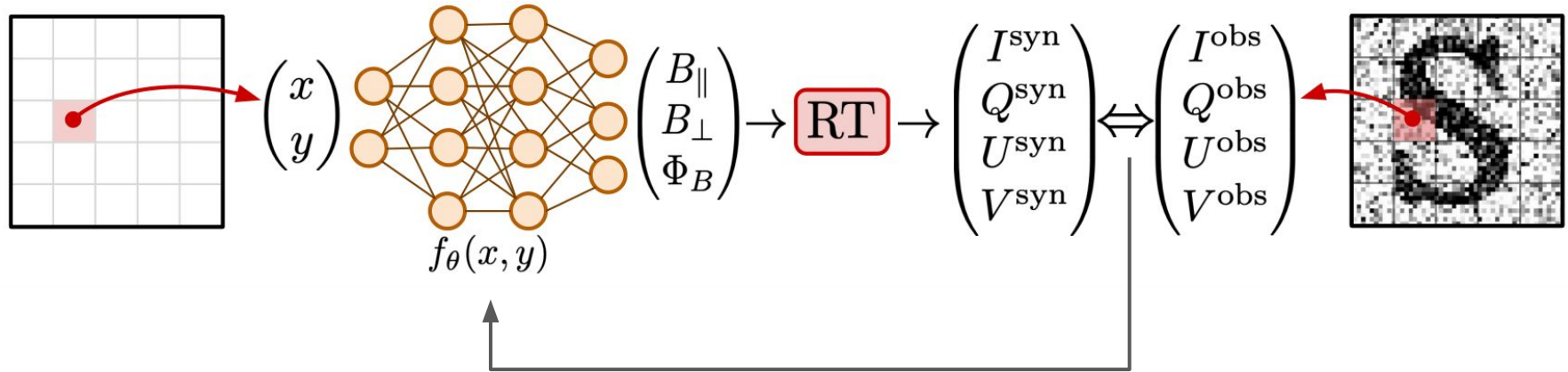


Magnetic field extrapolations  
R. Jarolim et al. (2022)

Coronal tomography  
A. Asensio Ramos (2023)

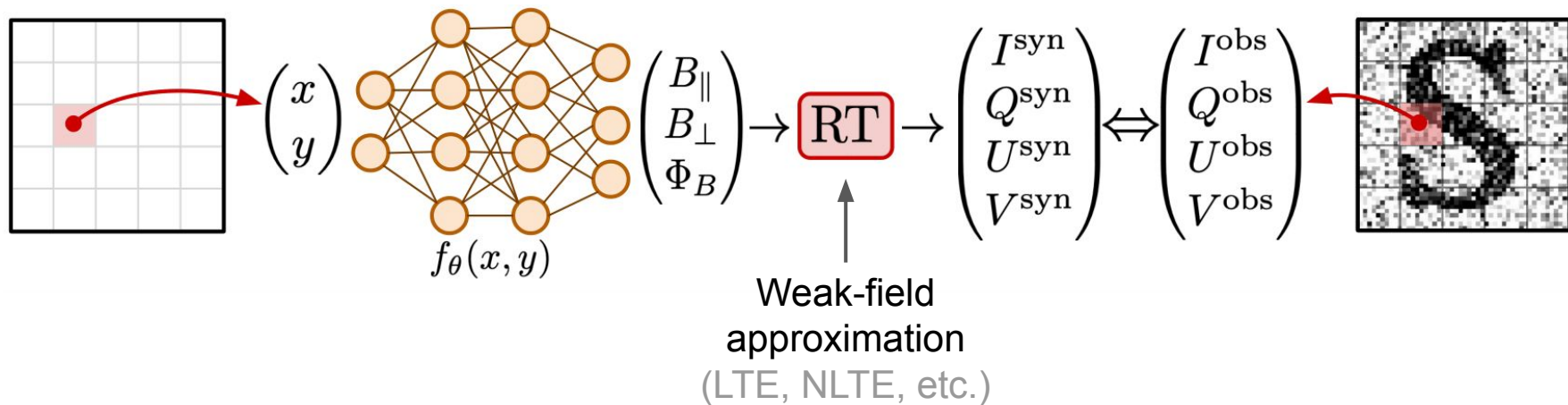
⇒ **Compact, continuous and differentiable** approximation in the whole domain

# Neural field for spectropolarimetric inversions

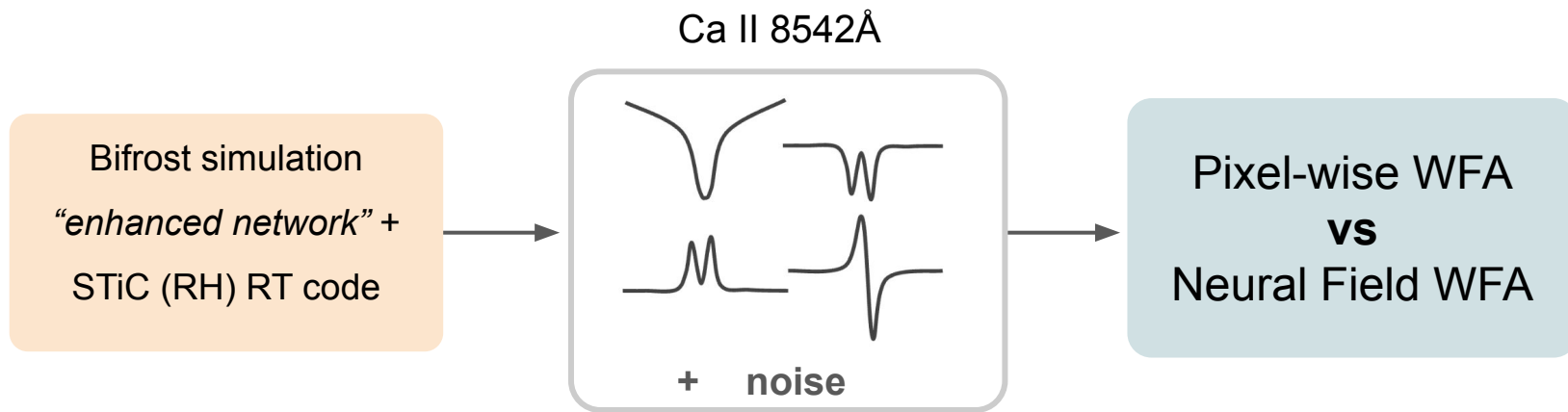


This is not a *predictive neural network*,  
but a **parametric representation**

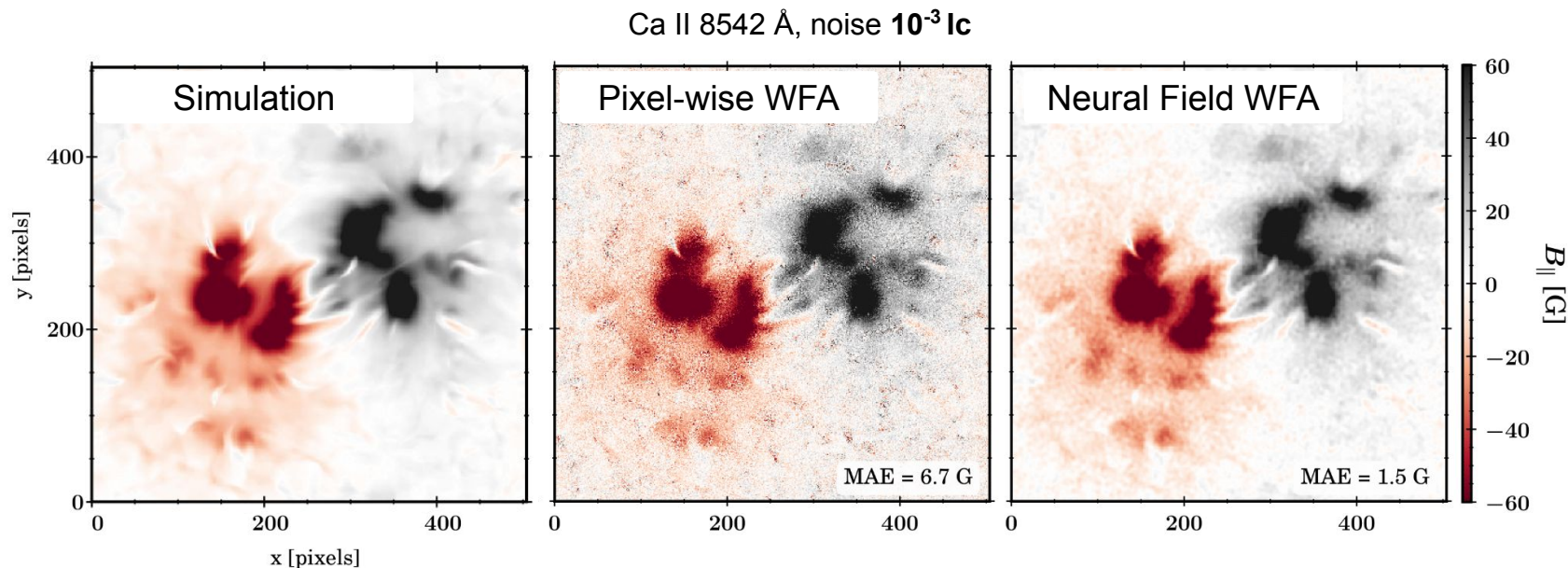
# Neural field for spectropolarimetric inversions



# Synthetic scenario



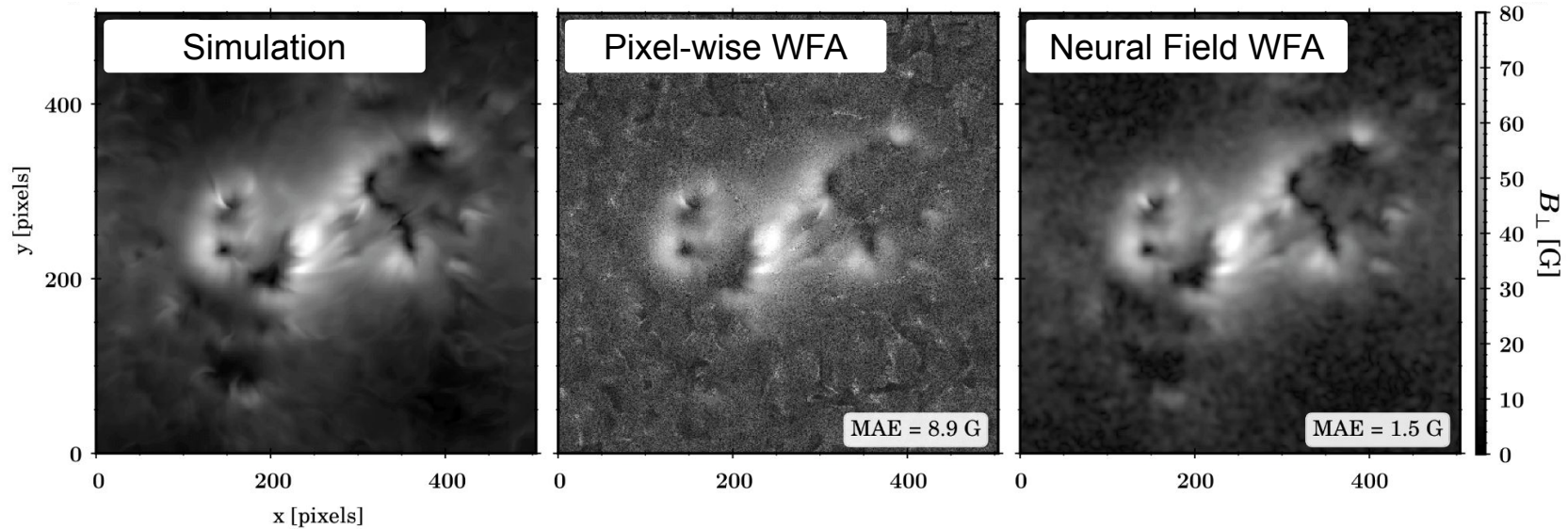
# WFA comparison: longitudinal magnetic field



⇒ The NF strongly damps the high-frequency components, but the overall structure is very similar.

# WFA comparison: transverse magnetic field

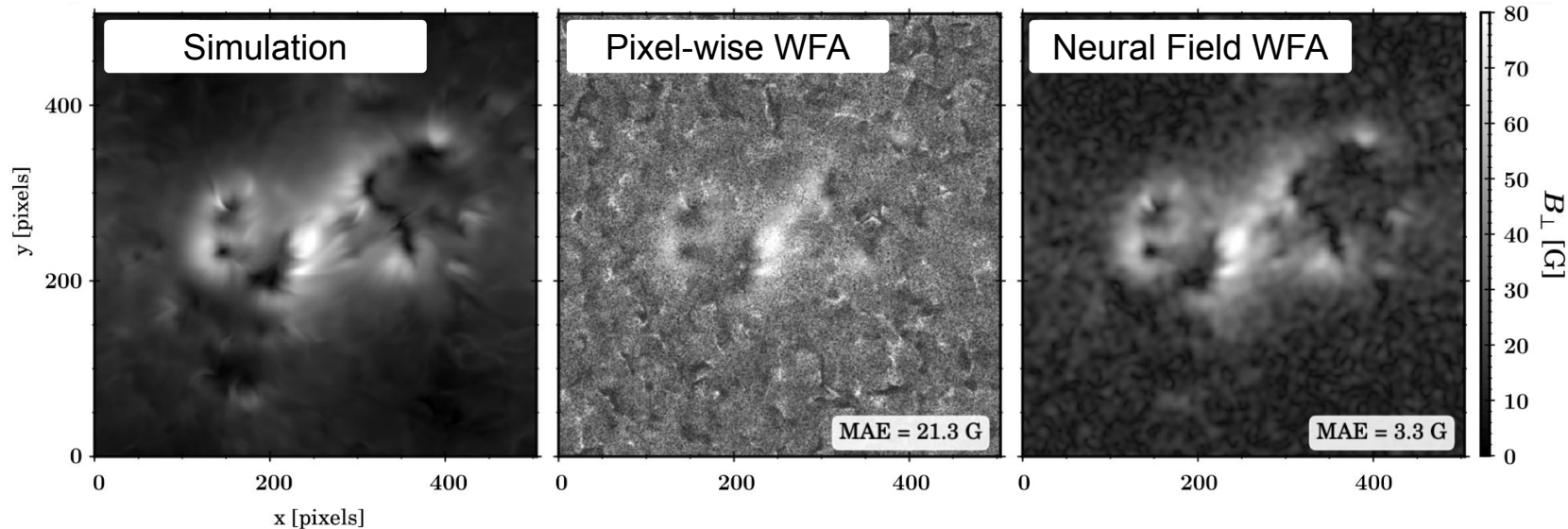
Ca II 8542 Å, noise  $10^{-4} I_c$



Mitigates the transverse bias  
Martínez González et al. (2012)

# WFA comparison: transverse magnetic field

Ca II 8542 Å, noise  $10^{-3} I_c$

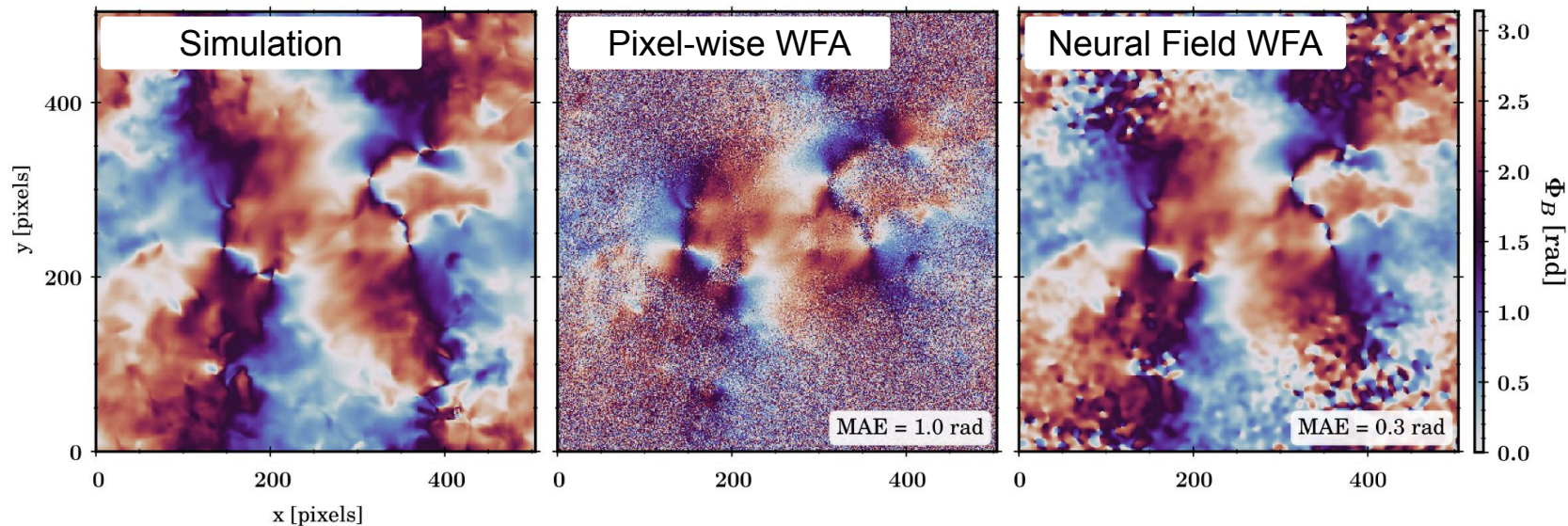


Mitigates the transverse bias  
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# WFA comparison: azimuth angle

Ca II 8542 Å, noise  $10^{-4} I_c$



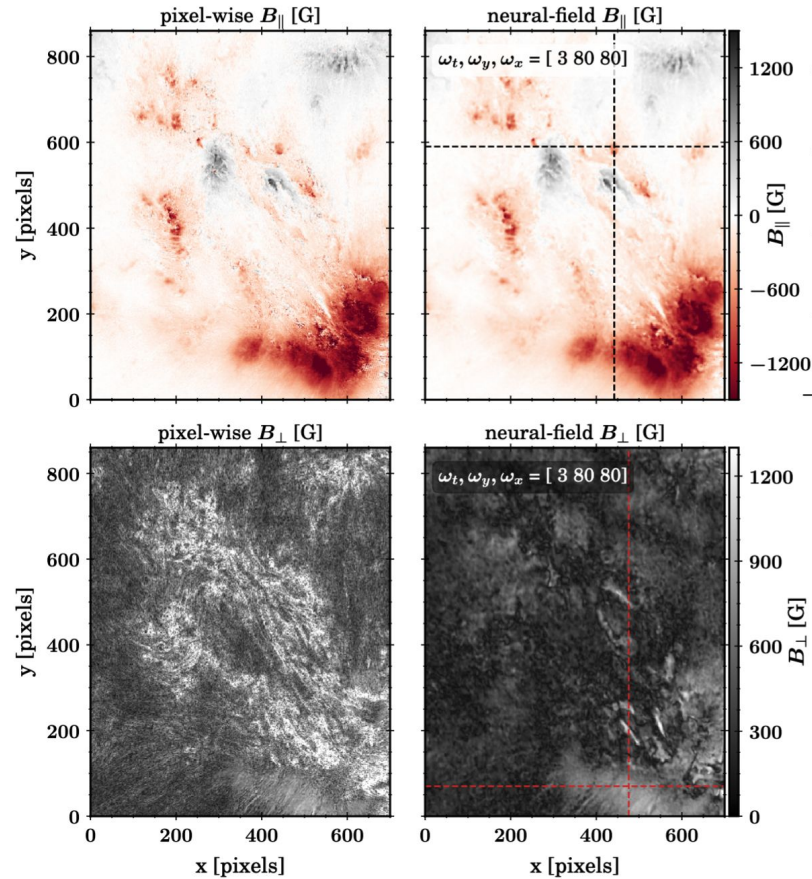
# Spatiotemporal regularization

**Region:** NOAA 12593

**Duration:** ~30 min long

**Observatory:** CRISP @ SST

**Spectra line:** Ca II 854.2 nm



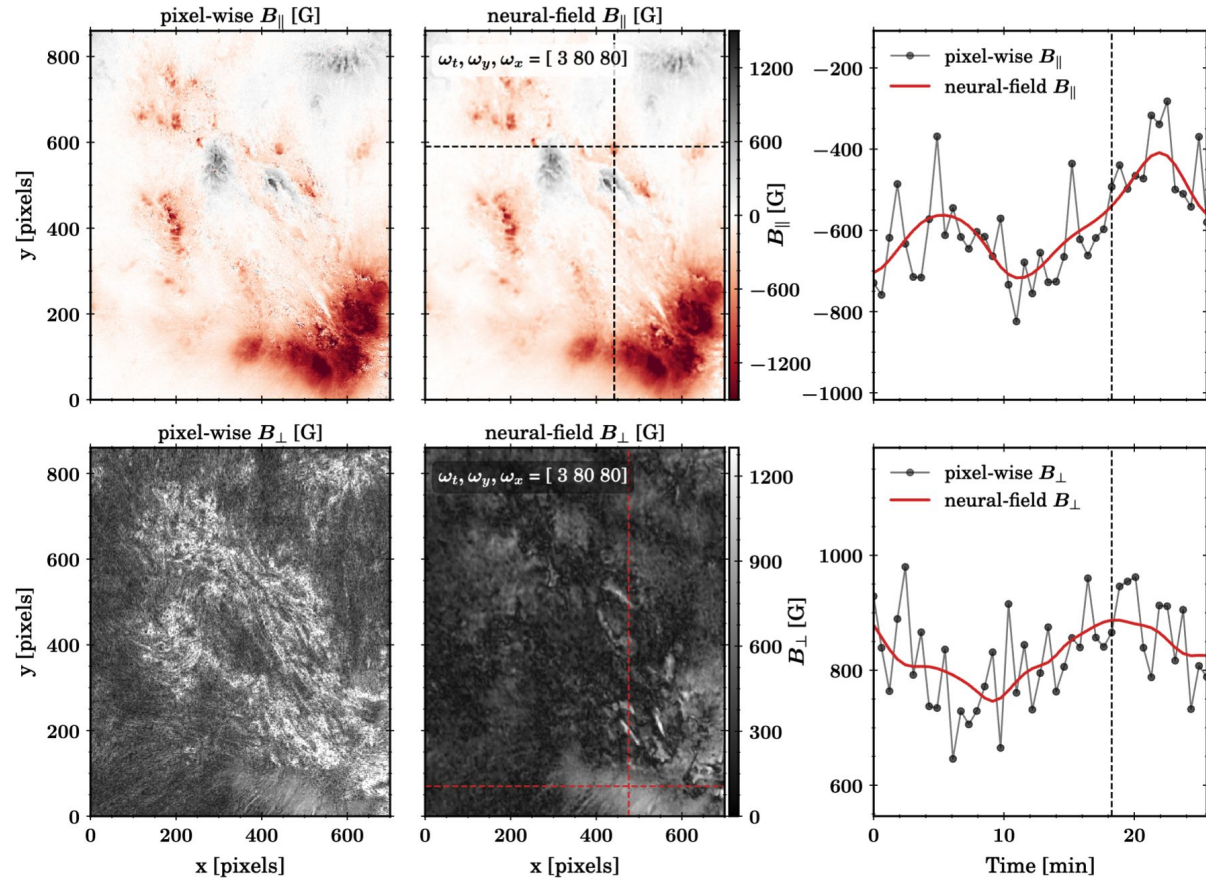
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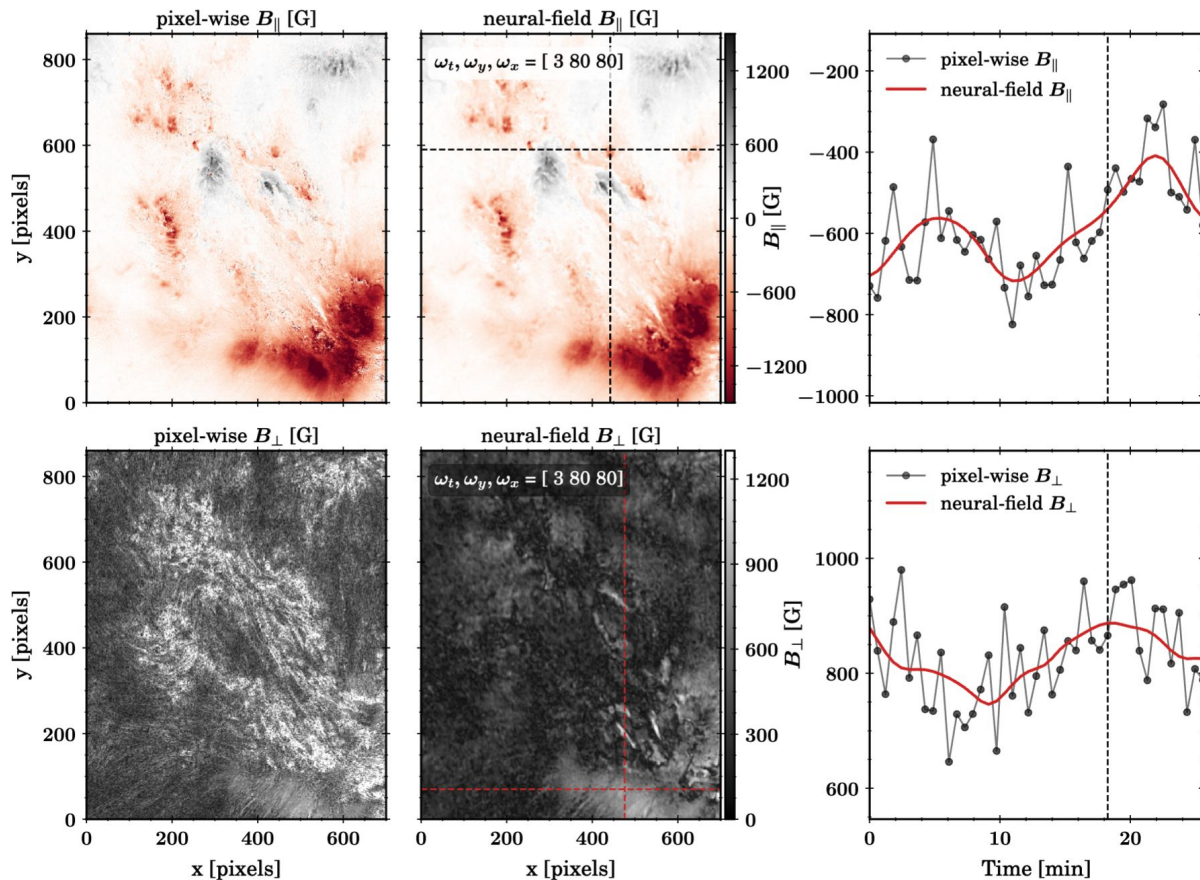
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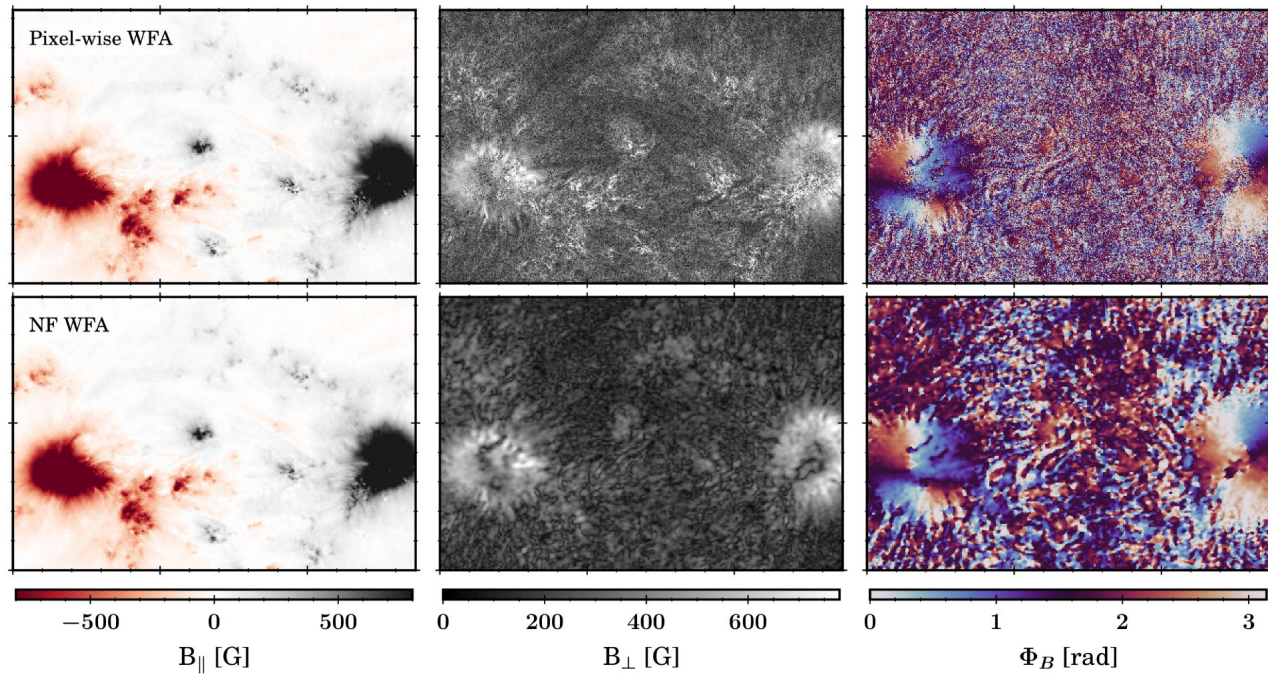
⇒ Hot magnetic canopy produces line profiles with a shallow line core, increasing the bias.

# Challenging case

**Region:** NOAA 12723

**Observatory:** CRISP @ SST

**Spectra line:** Ca II 854.2 nm

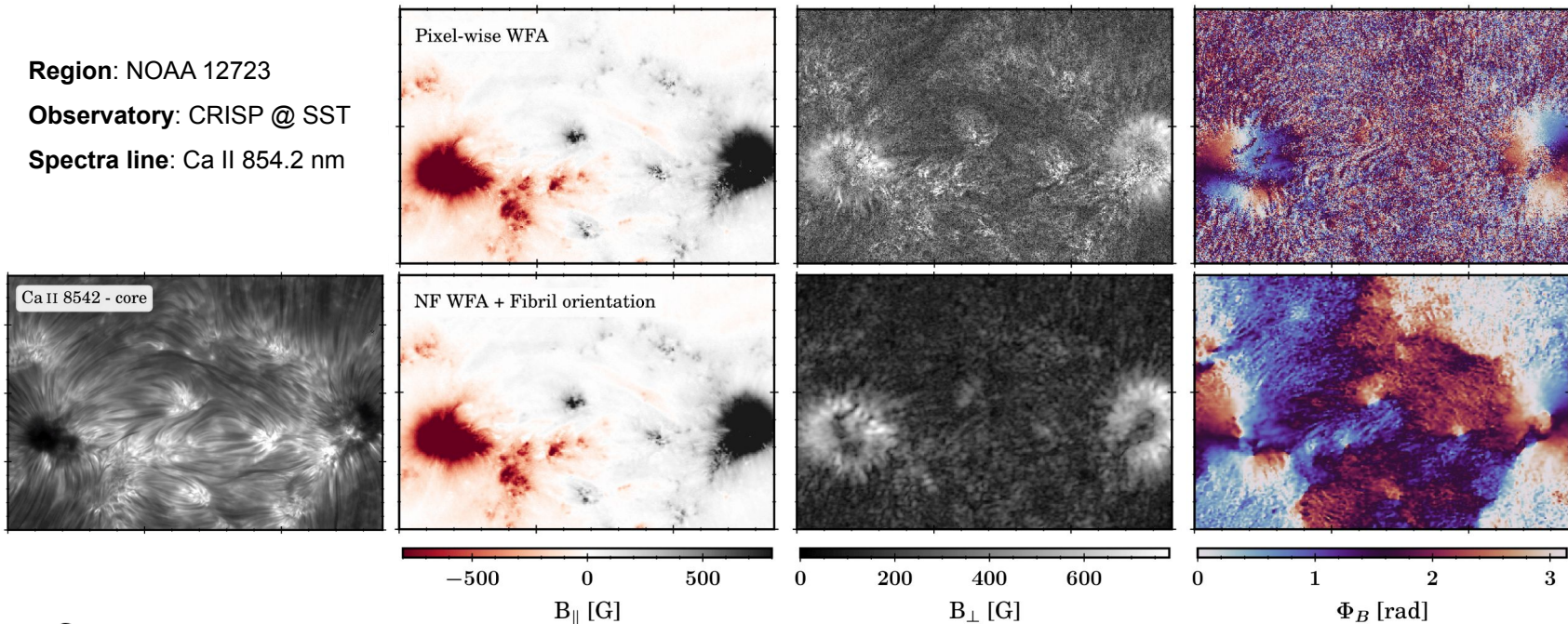


# Challenging case

**Region:** NOAA 12723

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**Spectra line:** Ca II 854.2 nm



$$\mathcal{L} = \chi^2 + \alpha \mathcal{L}_{\text{reg}}$$

... regularizing with **orientation of the chromospheric fibrils**

# Summary and conclusions

- **Compact representation:** reduce complexity of the problem

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Morosin et al. 2020  
de la Cruz Rodríguez & Leenaarts 2024



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- **Continuous controllable scales:** excellent for noisy scenarios
- **Speed:** using DL frameworks we have GPU support

Morosin et al. 2020  
de la Cruz Rodríguez & Leenaarts 2024

# Summary and conclusions

- **Compact representation:** reduce complexity of the problem
- **Continuous controllable scales:** excellent for noisy scenarios
- **Speed:** using DL frameworks we have GPU support
- **Differentiable:** promising for NLTE inversions, other constraints like divergence-free (solve the Zeeman-180 azimuth ambiguity), etc

Morosin et al. 2020  
de la Cruz Rodríguez & Leenaarts 2024

Štěpán et al. 2022, 2024

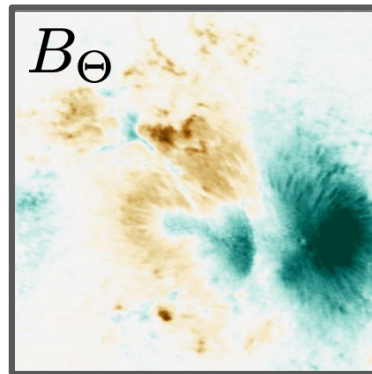
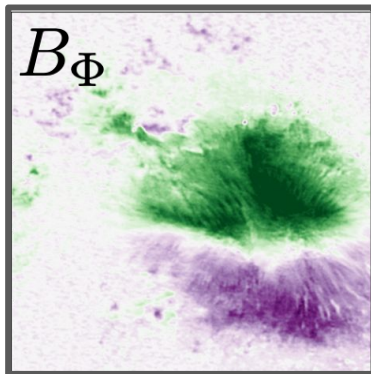
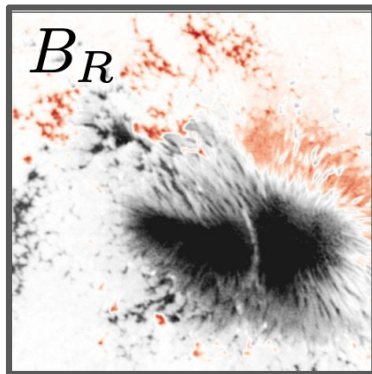
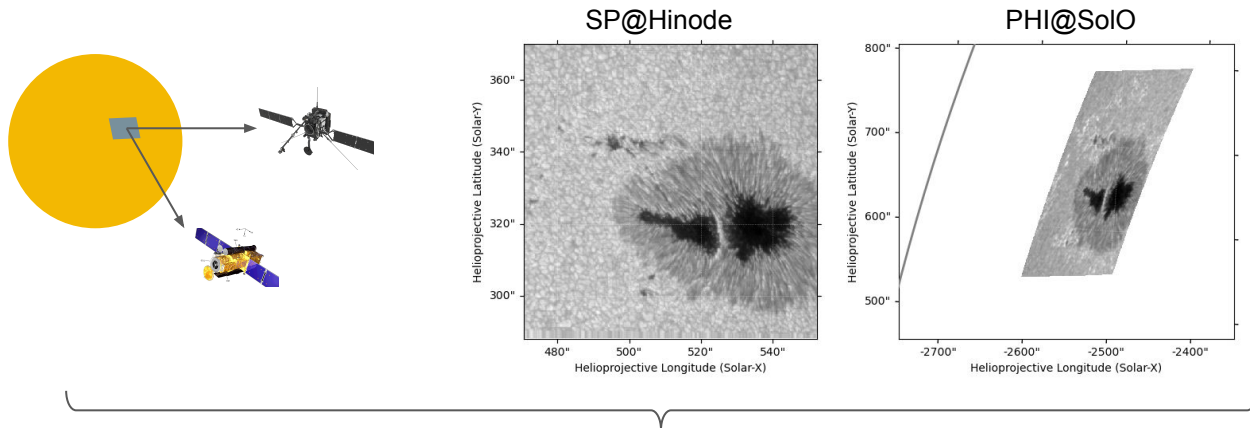
More details in the published article: <http://arxiv.org/abs/2409.05156>

Contact: carlos.diaz@astro.uio.no

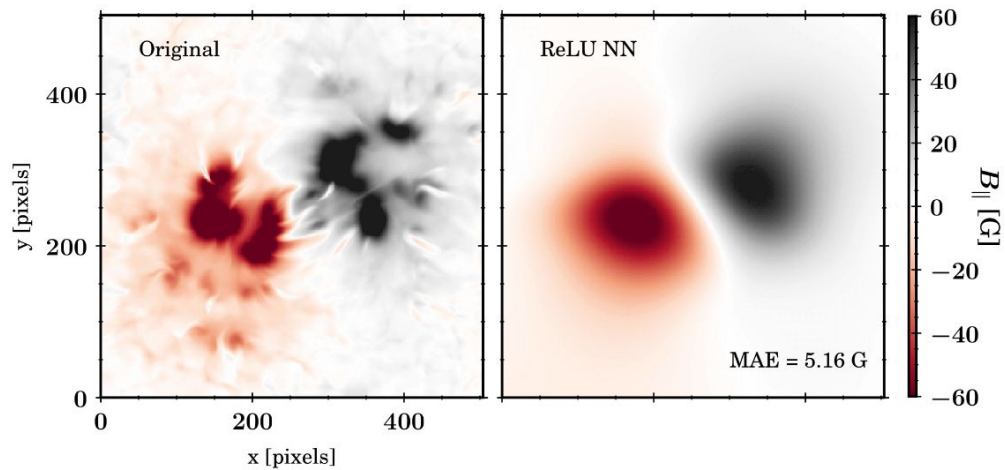




# Stereoscopic magnetic field reconstruction (ME)

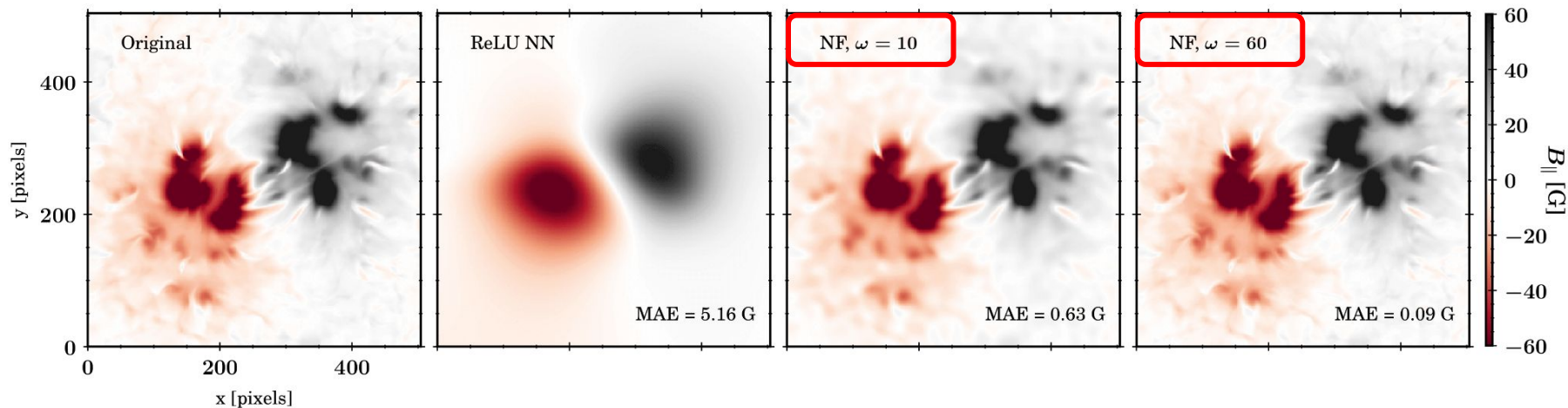


# Controllable implicit bias



$$\mathbf{x} \longrightarrow \text{NN}(\mathbf{x})$$

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$$\mathbf{x} \longrightarrow \text{NN}([\cos(2\pi\omega\mathbf{x}), \sin(2\pi\omega\mathbf{x})])$$

⇒ This nonlinear extension of Fourier series allows us to control the spatio-temporal coherence