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# Optimization of Data Reduction for Future CMB Experiments

*Avinash Anand<sup>1</sup> and Giuseppe Puglisi<sup>2</sup>*

<sup>1</sup>University of Rome "Tor Vergata", <sup>2</sup>University of Catania

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## Scientific Rationale : Map-making for CMB experiments

- Data model for CMB signal  $d_{i,t} = [A_i]_{tp} s_p + n_{i,t}$ 
  - $p \rightarrow$  pixel label;  $i \rightarrow$  detector label;  $t \rightarrow$  time stamp
  - $A_i \rightarrow$  Pointing matrix for detector  $i$
  - $s_p \rightarrow$  signal amplitude at pixel  $p$
  - $n_{i,t} \rightarrow$  noise amplitude at time  $t$  for detector  $i$
- Maximum likelihood solution taking into account multiple detectors observing at same frequency
$$\hat{s} = \left( \sum_{ij} A_i^t [N^{-1}]_{ij} A_j \right)^{-1} \left( \sum_{ij} A_i^t [N^{-1}]_{ij} d_j \right)$$
  - $N = \langle nn^t \rangle$  is the noise correlation matrix in time and  $N_{ij}$  is the block of  $N$  corresponding to the noise correlation between detectors  $i$  and  $j$
- For LiteBIRD-like mission, inversion direct inversion of  $N^{-1}$  is impractical due to matrix size

## Scientific Rationale : Map-making for CMB experiments (contd.)

- For stationary and end-to-end continuous data segment,  $N_{ij}$  is **circulant**. So,

$$[N^{-1}]_{ij,tt'} = \mathcal{F}\{[P^{-1}(\omega)]_{ij}\}(t - t')$$

- $P(\omega)$  is the power spectra of the noise amplitude vector and  $\mathcal{F}$  is the Fourier transform operator
- **Inversion of matrix  $N$  is now reduced to computation of just the first rows of block matrices  $N_{ij}$**
- The map-making method with circulant matrix approximation has already been implemented in **SANEPIC<sup>1</sup>** (Signal **A**nd **N**oise **E**stimation **P**rocedure **I**ncluding **C**orrelations)
- **Goal: To optimize SANEPIC for LiteBIRD<sup>2</sup> mission data and wrap the code with LiteBIRD simulation framework**

<sup>1</sup>Patanchon, G., et al. "SANEPIC: A mapmaking method for time stream data from large arrays." The Astrophysical Journal, vol. 681, no. 1, 2008, pp. 708–725, <https://doi.org/10.1086/588543>.

<sup>2</sup>LiteBIRD Collaboration. Probing cosmic inflation with the LiteBIRD cosmic microwave background polarization survey, Progress of Theoretical and Experimental Physics, Volume 2023, Issue 4, April 2023, 042F01, <https://doi.org/10.1093/ptep/ptac150>

# Technical Objectives, Methodologies and Solutions

- Complete data size: ~250 TB
- Estimated execution walltime on Marconi for complete dataset: >200,000 CPU hours
- Performance analysis for reduced dataset using perf tool:

Event	Counts	Summary
Cycles	$2.32 \times 10^8$	1.851 GHz
Instructions	$2.58 \times 10^8$	1.11 insn per cycle
Cache-references	$2.81 \times 10^6$	22.424 M/sec
Cache-misses	$1.47 \times 10^6$	52.446 % of all cache refs
Branches	$5.81 \times 10^7$	463.160 M/sec
Branch-misses	$6.98 \times 10^5$	1.20% of all branches

- **Large cache-misses: Possibility of improving memory access pattern**
- **Low branch-misses: Possibility of compile-time optimization**

## Technical Objectives, Methodologies and Solutions (contd.)

- Profiling using `gprof` gives further insight:

% Time Elapsed	Self Time Elapsed	No. of Calls	Function Name
41.60	5087.74	17160	<code>do_PtNd(double*, double*, ...)</code>
19.03	2327.77	16874	<code>deproject(double*, long*, ...)</code>
13.30	1626.77		<code>__libm_cos_l9</code>
12.82	1567.37		<code>__libm_sin_l9</code>
2.62	320.47	286	<code>compute_diagPtNPCorr(double*, long*, ...)</code>
2.42	295.86	16874	<code>write_tfAS(double*, double (*) [2], ...)</code>
1.85	226.10		<code>main</code>
1.11	135.29		<code>compare_global_array_long(void const*, void const*)</code>

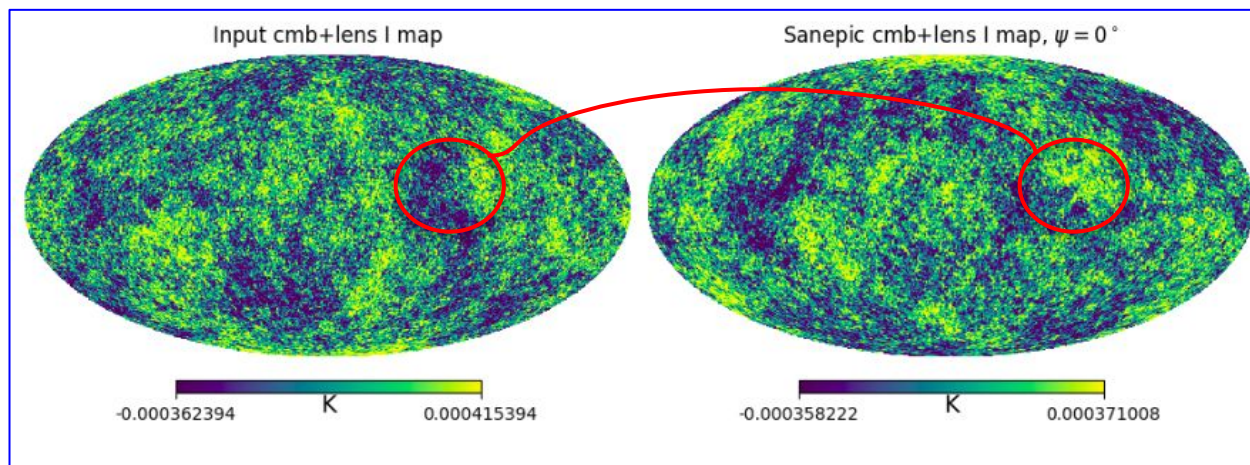
- **Optimization required only in four routines**

## Technical Objectives, Methodologies and Solutions (contd.)

- Optimization target:
  - Code refactoring
  - Improving memory access pattern by redefining the data structures
  - To reduce the branching by utilizing compile-time optimization
  - To minimize process imbalance
  
- Further optimization:
  - Offloading Fourier transform and MatVec operations to GPU with suitable offloading technology

## Timescale, Milestones and KPIs

- Started work on SANEPIC from July 2023
- Current status: Validation and debugging (~1 month)



- CPU optimization (~1 month)
- Validation, profiling and benchmark (~1 month)
- GPU optimization (~1 month)
- Validation, profiling and benchmark (~0.5 month)

## Next Steps and Expected Results (by next checkpoint: April 2024)

- Optimization of SANEPIC for LiteBIRD
- Validation of the code with different noise components added to the sky signal
- Preparing a detailed documentation of the code
- Wrapping SANEPIC with LiteBIRD simulation framework
- Optimization of other modules of LiteBIRD simulation framework





# Accomplished Work, Results

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$$\hat{\mathbf{s}} = (\mathbf{A}^t \mathbf{N}^{-1} \mathbf{A})^{-1} \mathbf{A}^t \mathbf{N}^{-1} \mathbf{d}$$