LIM*: a first-class probe of physics beyond Λ CDM ^{*}21cm as well as other atomic/molecular lines



Ely Kovetz, Trieste 21cm conference, Sep. 2023

There are lines beyond 21-cm that will(!) also be measured

1	2
There are lines	Line*-intensity
<i>beyond</i> 21-cm	mapping (LIM*) is
that will(!) also	a unique probe
be measured	of cosmology

1	2	3
There are lines	Line*-intensity	Specific examples:
<i>beyond</i> 21-cm	mapping (LIM*) is	- Inflation
that will(!) also	a unique probe	- Dark Matter
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1	2	3	4
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Jordan Flitter

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Debanjan Sarkar

Sarah Libanore

Caner Unal

Intensity mapping: 3D mapping of the specific intensity due to line emission.

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Earliest signal: CMB absorption in HI



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Cosmic dawn: signal turns on via Lya from first stars



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The 21cm brightness temperature contrast:



Credit: J. Munoz

Reionization: Multi-line emission



Reionization: Multi-line emission

- <u>HI (21cm)</u>: maps the neutral IGM, outside of the ionized bubbles.
- <u>CO/[CII]</u>: trace star-forming galaxies that source the ionizing photons.
- Lyman- α : probes the galaxies along with the halos around them.







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EoR Galaxies

CO(2-1) LIM

Ionization field

Redshifted 21cm



(Courtesy of A. Lidz)

Disclaimer: This will take time...

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Growth of Structure: Star-formation lines





Bernal and Kovetz, arXiv:2206.15377, The Astronomy and Astrophysics Review



Growth of Structure: Star-formation lines







(Astro2020: Kovetz et al., arXiv:1903.04496)



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Line*-Intensity Mapping: Experimental Landscape



(Astro2020: Kovetz et al., arXiv:1903.04496)

(ESA2050: Silva, Kovetz et al., arXiv:1908.07533)



Voyage 2050 sets sail: ESA chooses future science mission t...

11/06/2021 12852 VIEWS 131 LIKES







Multi-tracer light cones:

Skyline, Sato-Polito et al., arXiv:2212.08056





-0.2 -0.1 0.0 0.1 0.2 ΔDEC (deg)

From various recent LIM white papers and reviews:

<u>Reviews:</u> Kovetz et al., arXiv:1709.09066; Bernal and Kovetz, TAAR, arXiv:2206.15377

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Astrophysics:

- Reionization: bubble sizes, ionized fraction, duration
- Star formation rate (history, peak rise/fall, Pop III stars)
- Metallicity history
- AGN feedback
- Molecular gas density
- IGM density, evolution, clustering
- Faint end of luminosity function
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Cosmology:

- Inflation (running, non-gaussianity, oscillations, CIP, etc.)
- Dark matter (clustering, decaying, annihilating, interacting)
- Dark energy (c.c. or dynamical? wa/w0, etc.)
- Expansion rate history (BAO, VAO)
- Neutrinos (sum of masses, hierarchy, decay)
- Optical depth to Reionization (SFR, degeneracies, etc.)
- Modified gravity
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<u>Q</u>: For a cosmologist, why join now? It's not (yet) "2030s-2040s"....



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<u>Q</u>: For global signal hunters, how does new physics affect the signal?









"Something" cools down the IGM! e.g.: DM scatters with baryons



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see Rennan's and Omer's talks, also later here



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"Something" generates edges and endpoints! e.g.: resonant photon injection (dark photon → photon)



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"Something" delays structure formation! e.g.: fuzzy DM, ultra light axions, ALPs



"Something" delays structure formation! e.g.: fuzzy DM, ultra light axions, ALPs "Something" speeds up structure formation! e.g.: primordial magnetic fields

Inflation predicts scale-invariance over >20 orders of magnitude. We've probed only ~4.

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• Star-formation LIM: Sensitive to the integrated signal from the faintest galaxies



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- <u>Star-formation LIM</u>: Sensitive to the integrated signal from the faintest galaxies
- 21-cm: Sensitive to the first (and smallest) galaxies in the Universe



The Matter Power Spectrum on Small Scales



Changes in the power spectrum propagate to the global 21cm signal:

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Munoz, Dvorkin and Cyr-Racine, PRD 2020

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Changes in the power spectrum propagate to the 21-cm power spectrum:





Munoz, Dvorkin and Cyr-Racine, PRD 2020

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Changes in the power spectrum propagate to the 21-cm power spectrum:





-30

15

20

25

 \boldsymbol{z}

$p_{2}^{P} p_{2}^{P} -5$ -10 $k_{21} = 0.4 \,\mathrm{Mpc}^{-1}$ $k_{21} = 0.4 \,\mathrm{Mpc}^{-1}$ $k = 30 \,\mathrm{Mpc}^{-1}$ $k = 50 \,\mathrm{Mpc}^{-1}$

 $k_{21} = 0.1 \, {
m Mpc}$

 $k = 75 \text{ Mpc}^{-1}$

30

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Libanore, Unal, Sarkar and Kovetz, PRD 2022

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Line-Intensity Mapping: Small Scales with VID



Line-Intensity Mapping: Small Scales with VID





Instrumental Paramater	COMAP 1	COMAP 2	$\cos 3 (CO)$
$T_{ m sys}$ [K]	40	40	$\max(20, \nu_{ m obs})$
Total $\#$ of independent detectors	19	95	1000
Ang. resolution (FWHM) [arcmin]	4	4	4
Frequency band [GHz]	26-34	26-34	12-36
$\delta u [m MHz]$	15.6	8.0	2.0
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LIM* Small Scale Bounds:





21cm LIM: Small Scale Fluctuations

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Examples:

• Suppression from fuzzy dark matter.

21cm LIM: Small Scale Fluctuations

Examples:

- Suppression from fuzzy dark matter.
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Credit: J. Flitter









Fuzzy Dark Matter: 21cm IM can close the weakly constrained mass window



Primordial Magnetic Fields:

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Primordial Magnetic Fields:

LIM (e.g. CO) will outdo future CMB experiments

Adi, Libanore and Kovetz, JCAP 2023

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Adi, Libanore and Kovetz, JCAP 2023

21cm will beat other probes by more than order of magnitude

Cruz, Adi, Flitter, Kamionkowski and Kovetz, arXiv:2308.04483





The comoving sound horizon at recombination:

$$r_s^* = \int_{z^*}^{\infty} \frac{c_s(z)}{H(z)} dz$$





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Credit: NASA/WMAP Science Team



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Structure: stars, ISM, galaxies, IGM, clusters



Credit: J. Bock, SPHEREx



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Solution: Use Power Spectrum Anisotropy (AP effect)

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Addressed in: Bernal, Breysse and Kovetz, PRL 2019 Bernal, Breysse, Gil-Marin and Kovetz, PRD 2019





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Ηα	Lyα	
80-300 THz	250-360 THz	
200 deg ²	200 deg ²	











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Tseliakovich and Hirata, PRD 2010

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Visbal, Barkana, Fialkov, Tseliakovich and Hirata, Nature 2012


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Muñoz, PRL 2019



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Sarkar and Kovetz, PRD 2022

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Sarkar and Kovetz, PRD 2022

Expansion rate constraints:

Feedback	$z_{ m half}$	$\Delta(Hr_d)/(Hr_d)\%$		
		Optimistic	Moderate	Pessimistic
No	14.8	0.3	0.62	1.82
Low	12.7	0.51	1.14	3.51
Regular	12.2	0.73	1.51	4.62

21cm Simulations: Public Codes

Full radiative-transfer hydrodynamical simulation (extremely computationally expensive):

CoDa (Ocvirk et al., MNRAS 2016) 21SSD (Semelin, MNRAS 2017) THESAN (Kannan et al., MNRAS 2011) Ray-tracing algorithms (applied to N-body simulations; also very expensive): $C^2 - Ray$ (Mellema et al., New Astron. 2006) CRASH (Maselli et al., MNRAS 2003) One-dimensional radiative transfer (much faster, approximated): BEARS (Thomas et al., MNRAS 2009) GRIZZLY (Ghara et al., MNRAS 2018) BEORN (Schaeffer et al., arXiv:2305.15466) Purely analytic codes (fastest):

CAMB (Lewis and Challinor, PRD 2007) Zeus 21 (Munoz, arXiv:2302.08506) X21 (Katz et al., arXiv:2309.XXXXX) Semi-numerical codes (excursion-set formalism): SimFAST21 (Santos et. al, MNRAS 2010) 21cmFAST (Mesinger et al., MNRAS 2011)







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- requires $\Delta z \ll 1$ to solve

21cm Cosmology: a Code for Cosmology

Solution:

- Use initial conditions from a Boltzmann solver
 - → Initialize with CLASS at z = 1100
- Calculate accurate recombination history

→ Incorporate Hyrec into the code

- Consistently track (non-linear?) evolution
 - \longrightarrow Inhomogeneous box at z = 35
- Fold-in cosmic microwave background
 - Combined CMB+21cm constraints
- Astrophysical vs. cosmological effects
 - ----> Explore parameter degeneracies
- Slow (need $\Delta z \ll 1$) at Compton tight coupling

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21cm Cosmology: a Code for Cosmology



21cmFirstCLASS I. Cosmological tool for Λ CDM and beyond

Jordan Flitter^{1, *} and Ely D. Kovetz¹ Jo

¹Physics Department, Ben-Gurion University of the Negev, Beer-Sheva 84105, Israel

21cmFirstCLASS II. Early linear fluctuations of the 21cm signal

Jordan Flitter^{1, *} and Ely D. Kovetz¹

¹Physics Department, Ben-Gurion University of the Negev, Beer-Sheva 84105, Israel









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Cosmology remains sensitive at $m_{\chi} \ll \text{GeV}$:

(see: Chen et al. (2012), Sigurdson et. al (2004), Dvorkin et al. (2014), Gluscevic and Boddy (2018), Boddy and Gluscevic (2018), Boddy et al. (2018), Xu et al. (2018), Slatyer et al. (2018))





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Let's examine the case: $\sigma(v) = \sigma_c \left(\frac{v}{c}\right)^{-4}$



Example: Dark Matter-Baryon Scattering

Curve	Dotted	Dashed	Solid
σ_{-4}	0 (ACDM)	$10^{-42}{\rm cm}^2$	$10^{-41}{\rm cm}^2$

 $m_{\chi} = 1 \,\mathrm{MeV}$

 $f_{\chi} = 100~\%$

- + χ , *b* tight coupling approximation
- + small temperature correction for S_{α}













Boddy, Poulin, Gluscevic, Kovetz, Barkana and Kamionkowski, PRD 2018



Boddy, Poulin, Gluscevic, Kovetz, Barkana and Kamionkowski, PRD 2018










21cm Cosmology: 21cmFirstCLASS vs. CAMB

Flitter and Kovetz, arXiv:2309.03948

Additional conclusions:

- $\mathcal{O}(20\%)$ error at z < 35 from homogeneous I.C.s

- $\mathcal{O}(20\%)$ error at z < 35 from $\delta_b = \delta_c$ assumption.

- Introducing a scale-dependent growth factor:

$$\mathcal{D}_{b}\left(k,z\right) \equiv \mathcal{T}_{b/c}\left(k,z\right)D\left(z\right)$$

yields percent agreement with CAMB at z < 80.



FIG. 1. Schematic representation of our comparison strategy.

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Ely Kovetz, Trieste 21cm conference, Sep. 2023