

6th Global 21cm workshop IFPU, Trieste



International
Centre for
Radio
Astronomy
Research

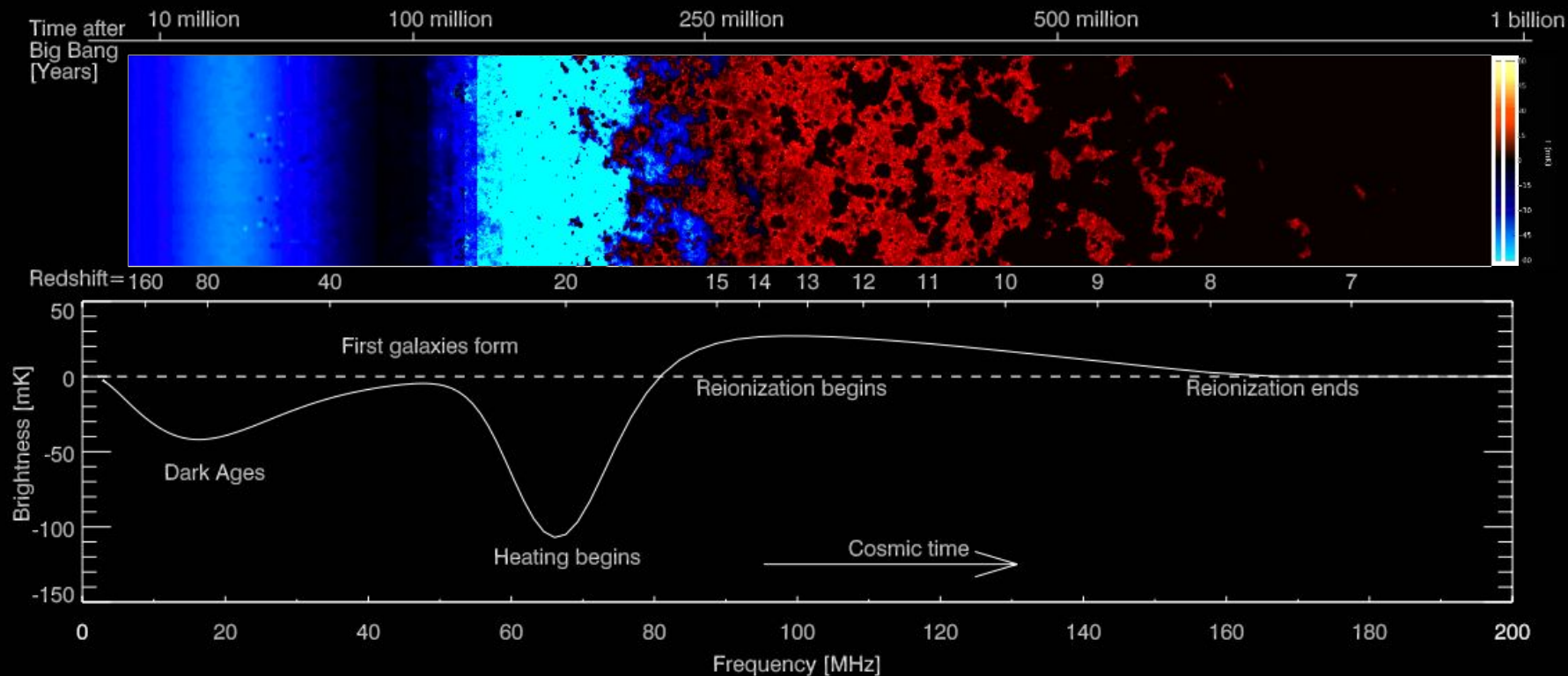
Detecting Global 21-cm Signal using Lunar Occultation with MWA

Himanshu Tiwari

Prof. Cathryn Trott
Dr. Benjamin Mckinley
Dr. Nithyanandan Thyagarajan



EoR- Global 21-cm Signal

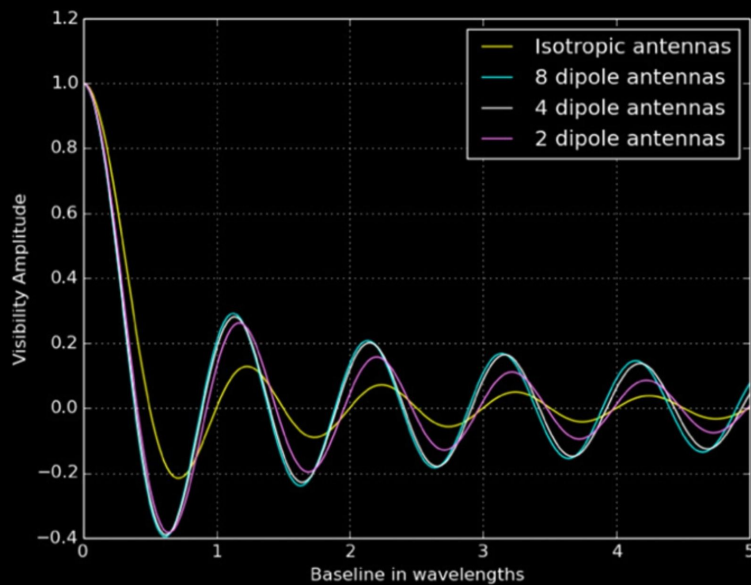


credit: Pritchard, J. R., & Loeb, A. 2012

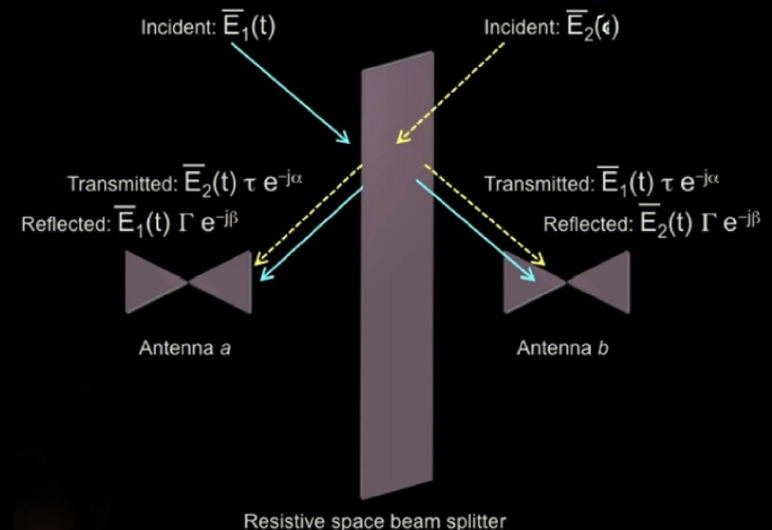
$$\delta T_b \approx \frac{T_S - T_R}{1 + z} \tau$$

Global Experiments are Great!

what about Interferometers?



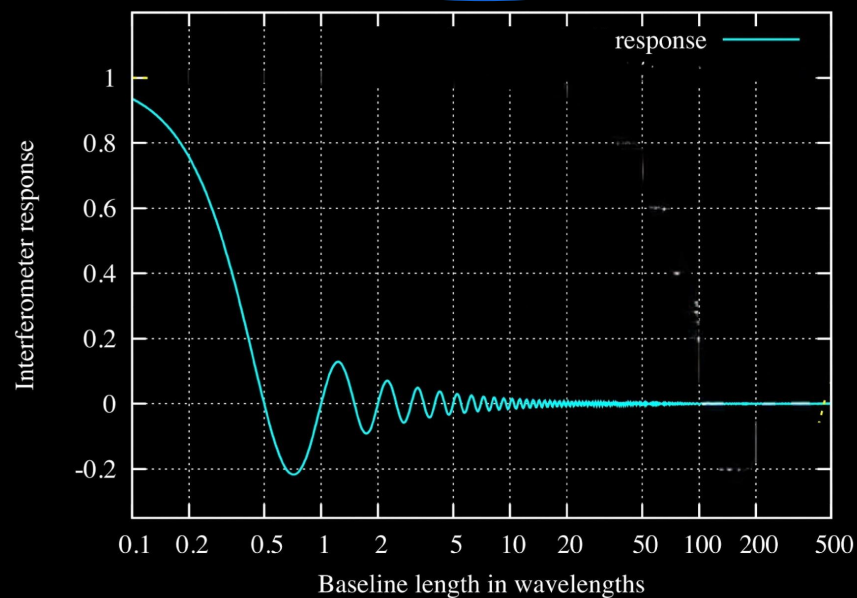
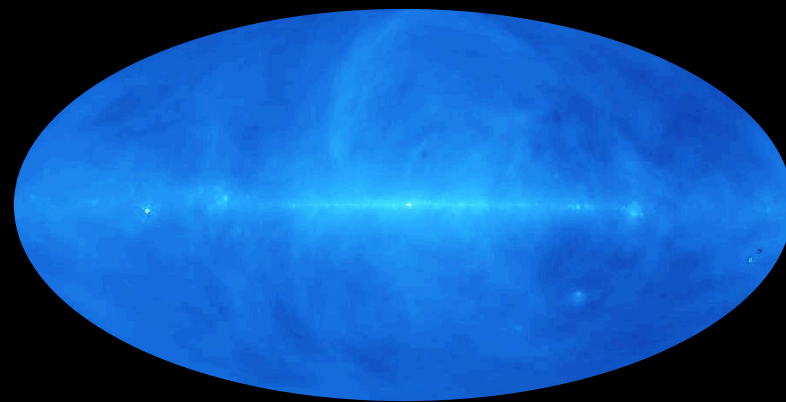
Singh, S. (2015)



Mahesh, N. (2015)

Theory: Interferometers to Global 21-cm Signal

$$V(\vec{u}, \nu) = \frac{1}{4\pi} \int d\Omega T_{\text{sky}}(\vec{r}, \nu) e^{2\pi i \vec{u} \cdot \vec{r}}$$



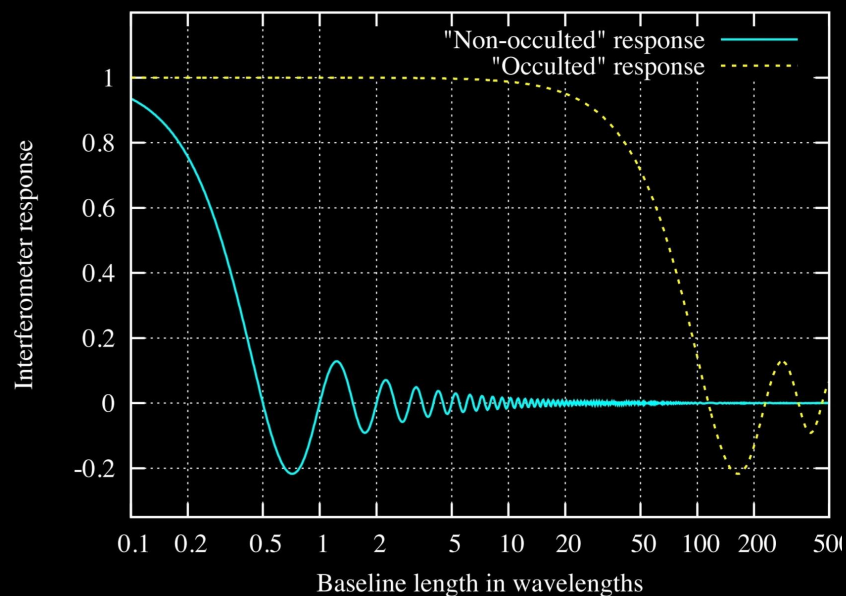
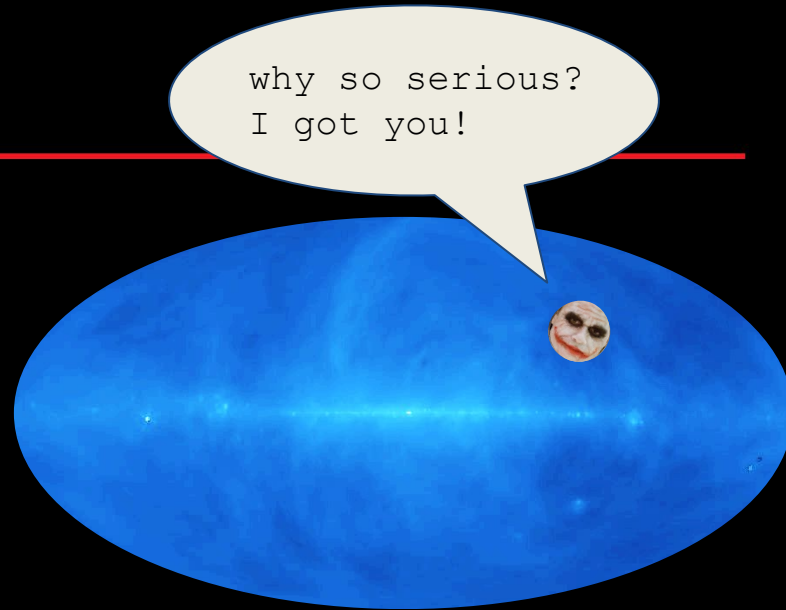
credit: Vedantham et al. [2015]

Lunar Occultation

$$V(\vec{u}, \nu) = \frac{1}{4\pi} \int d\Omega T_{\text{sky}}(\vec{r}, \nu) e^{2\pi i \vec{u} \cdot \vec{r}}$$

$$T_{\text{sky}} = T_B (1 - M) + T_M M$$

$$= \underbrace{(T_M - T_B)M}_{\text{occulted}} + \underbrace{T_B}_{\text{non-occulted}},$$



credit: Vedantham et al. [2015]

Lunar Occultation

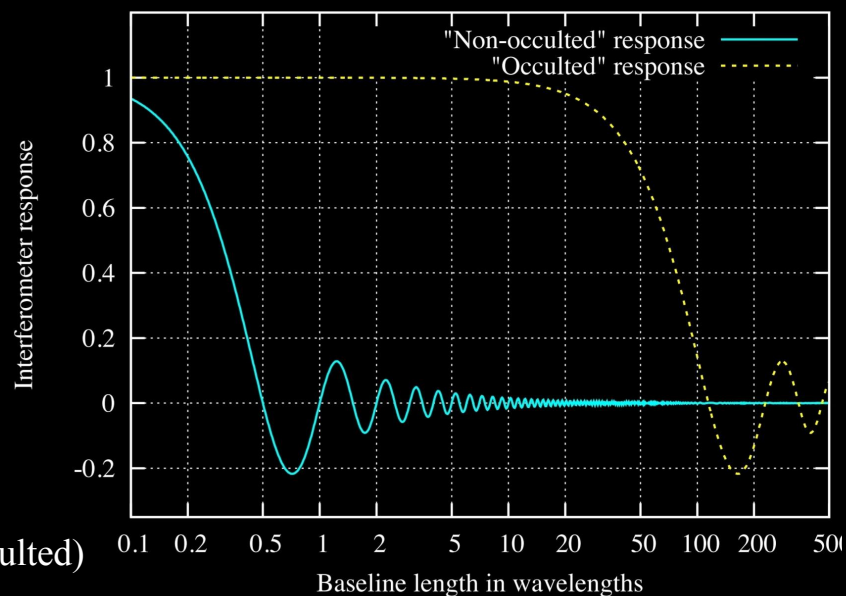
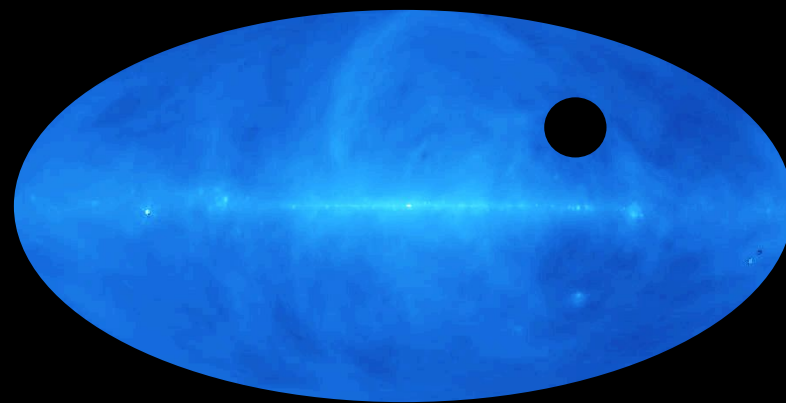
$$V(\vec{u}, \nu) = \frac{1}{4\pi} \int d\Omega T_{\text{sky}}(\vec{r}, \nu) e^{2\pi i \vec{u} \cdot \vec{r}}$$

$$T_{\text{sky}} = T_B (1 - M) + T_M M$$

$$= \underbrace{(T_M - T_B)M}_{\text{occulted}} + \underbrace{T_B}_{\text{non-occulted}},$$

$$V(\vec{u}, \nu) = T_B(\nu) \frac{\sin 2\pi |\vec{u}|}{2\pi |\vec{u}|} \quad (\text{Non-occulted})$$

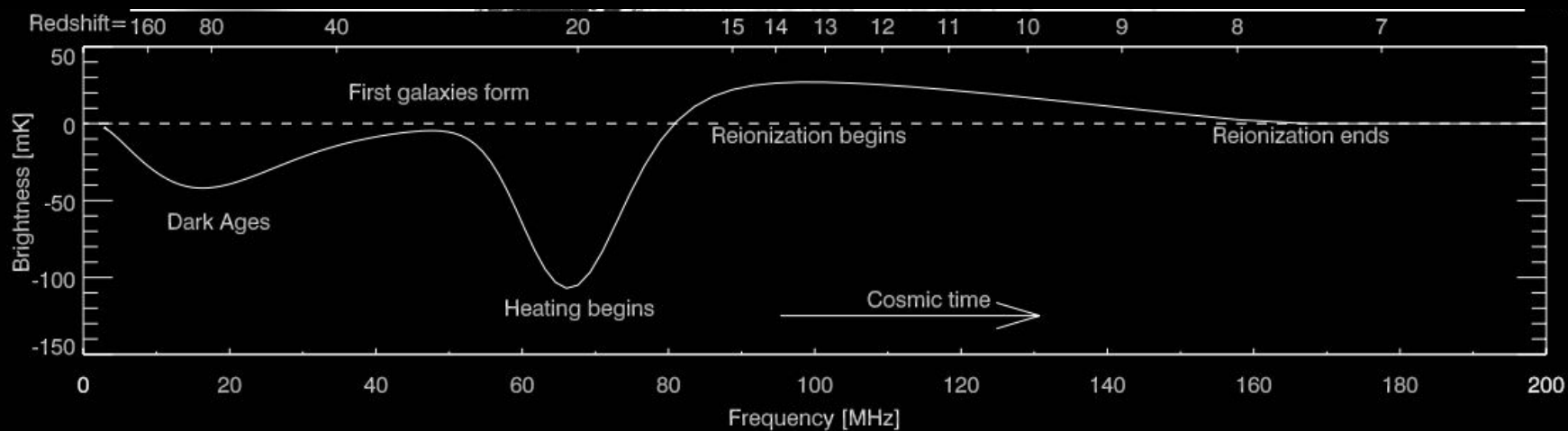
$$V(\vec{u}) \approx (T_M - T_B) \frac{\Omega_a}{4\pi} \frac{2J_1(\pi a |\vec{u}|)}{\pi a |\vec{u}|} \quad (\text{Occulted})$$



credit: Vedantham et al. [2015]



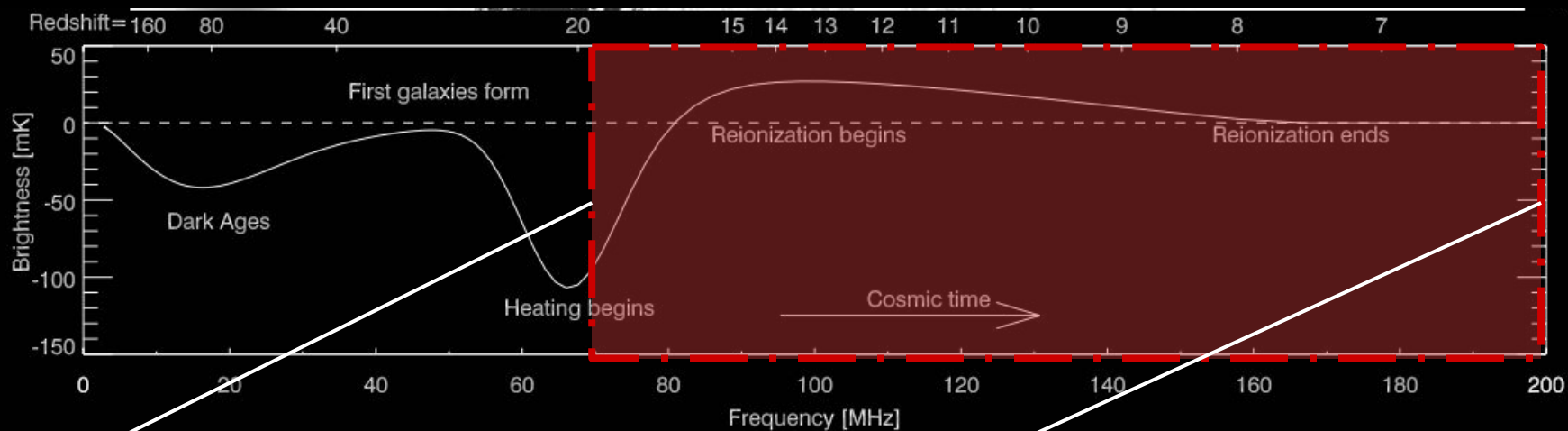
EoR- Global 21-cm Signal



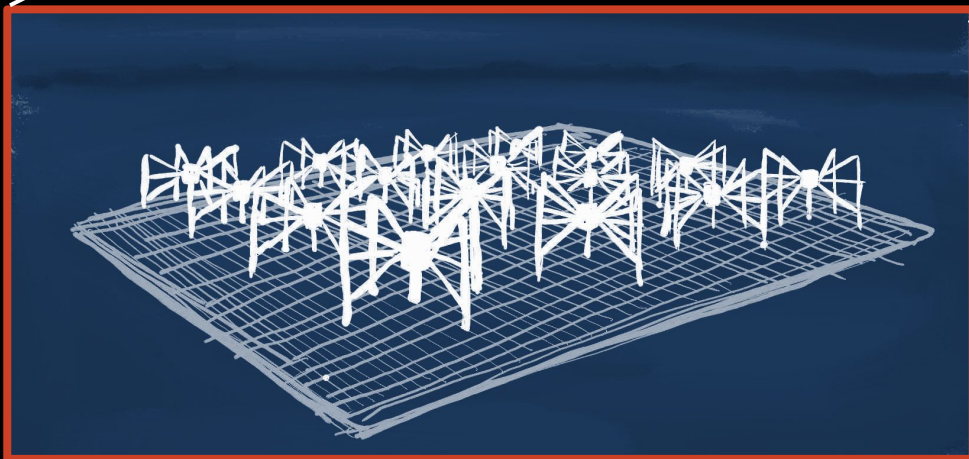
credit: Pritchard, J. R., & Loeb, A. 2012



EoR- Global 21-cm Signal



credit: Pritchard, J. R., & Loeb, A. 2012





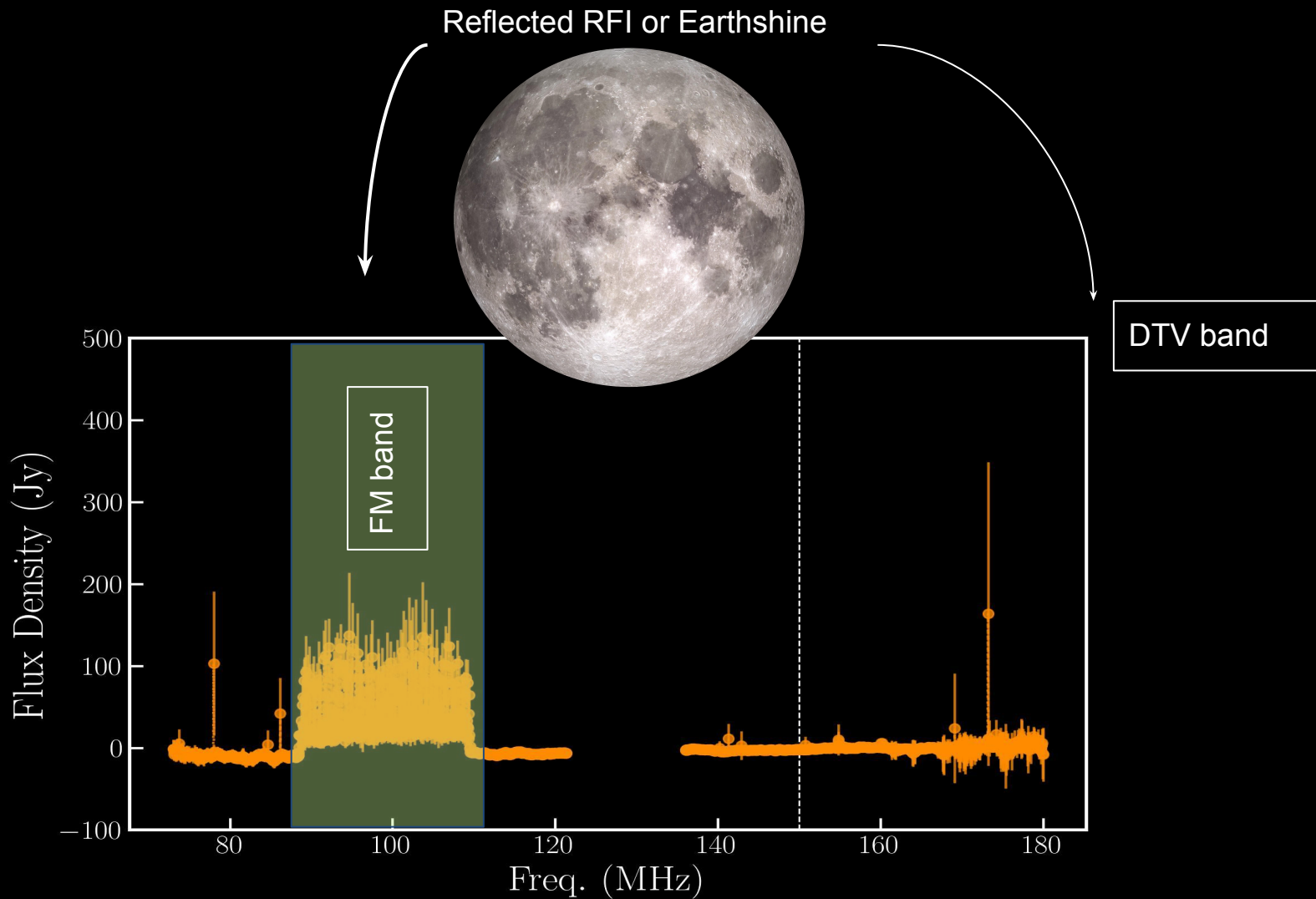
Measurements of the Moon

**How does the Moon look like in
Radio?**

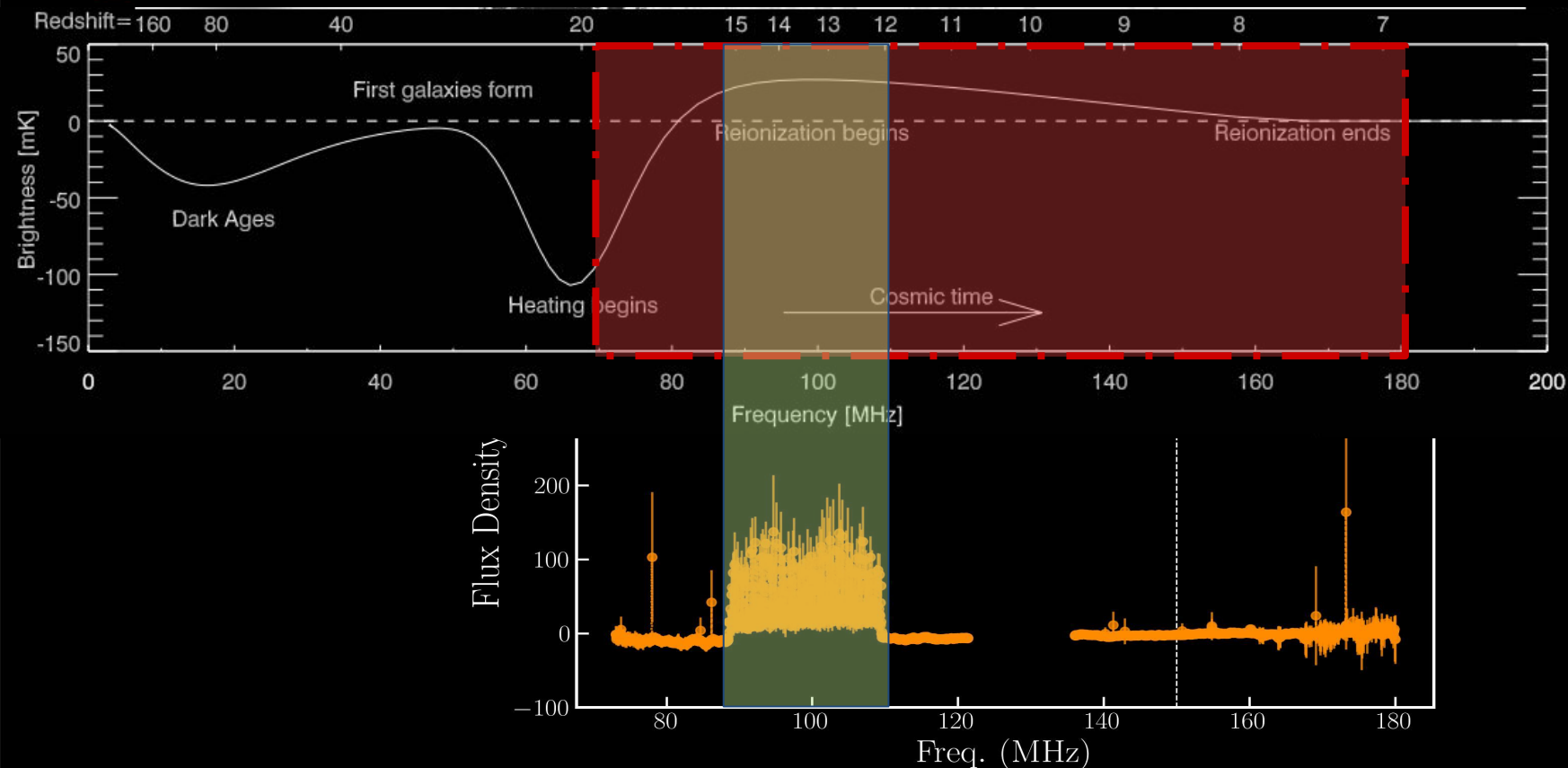


Indeed!

How does the Moon is in Radio?



How does the Moon is in Radio?



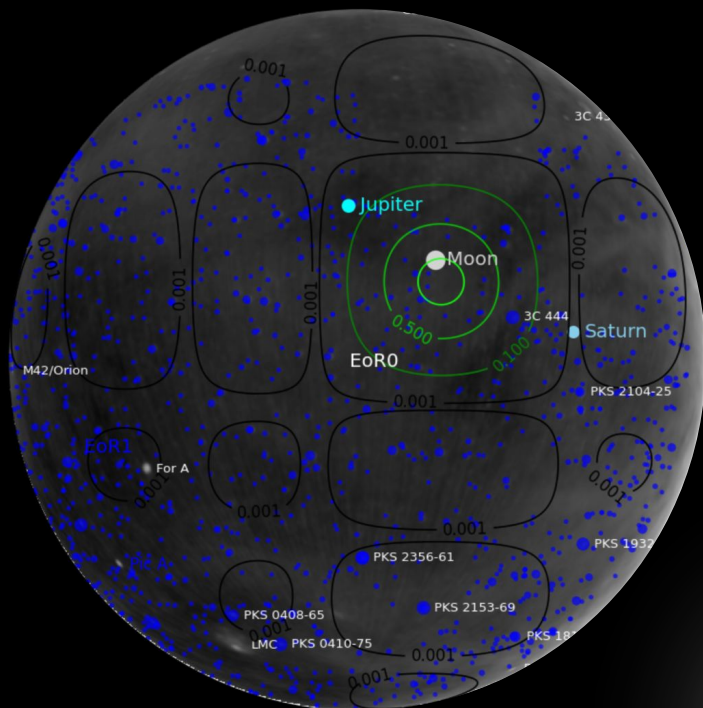
where is EoR?



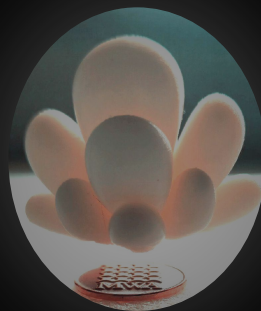
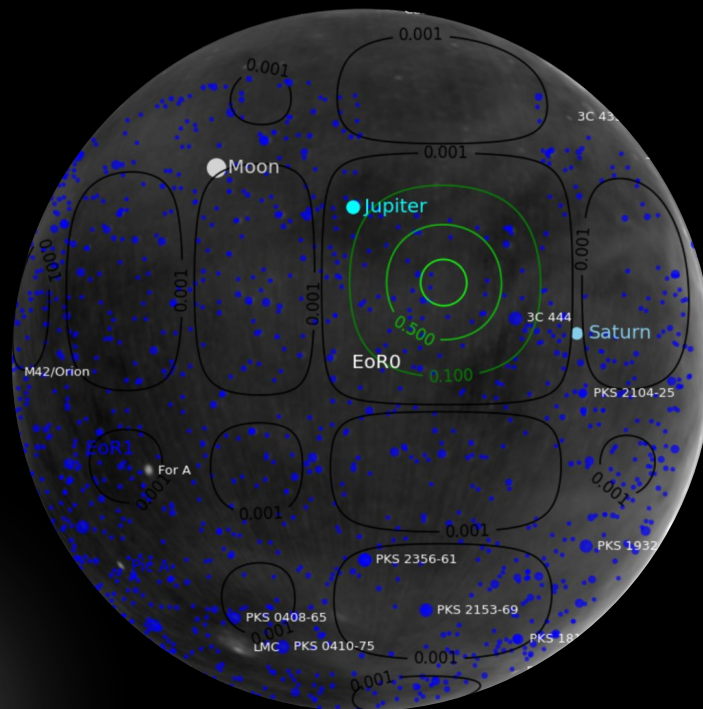
You humans
produce RFI!!

Mitigating Earthshine from the Moon!

ON-Moon

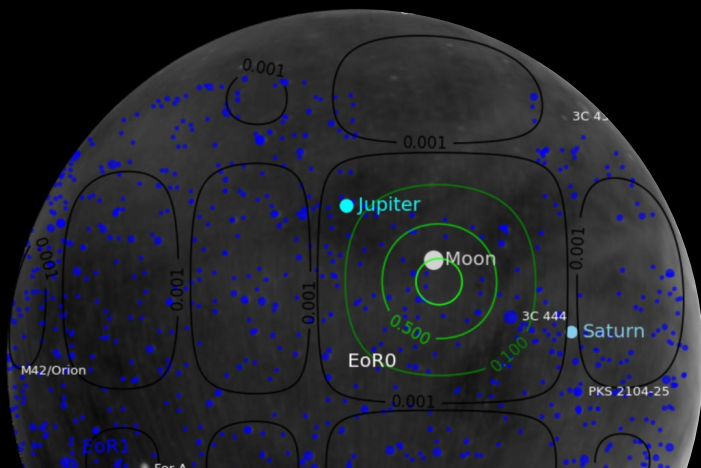


OFF-Moon

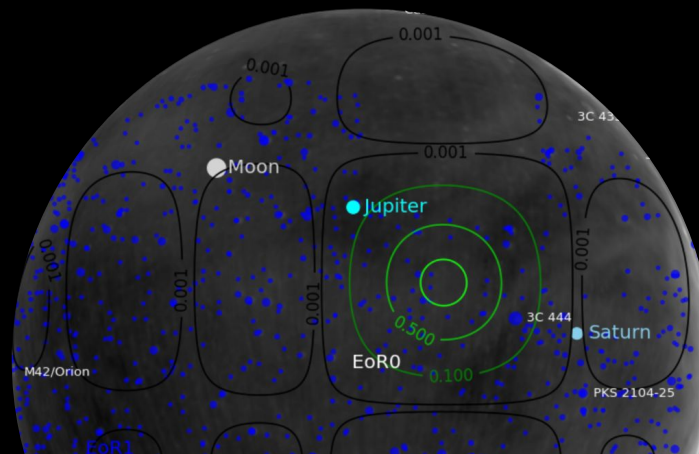


LST locked pair of observation
 Data: MWA phase-1
 Obs date: Aug 2015, Sept 2015, Dec 2015

ON-Moon

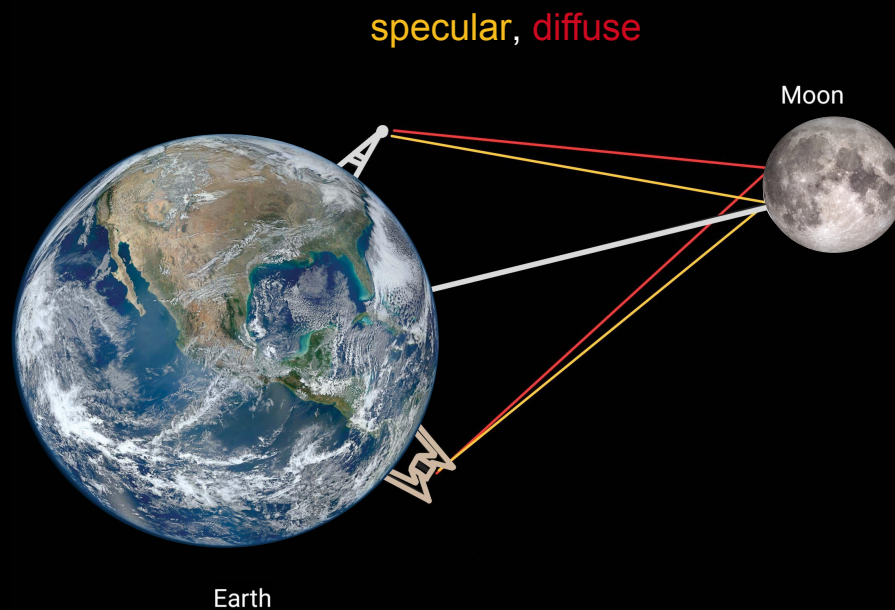


OFF-Moon



ON – Moon							
Date	N_{obs}	$N_{\text{obs}}^{\text{full-band}}$	Bandwidth (MHz)	Freq. res. (kHz)	Time res. (sec)	Total Int. time (sec)	Obs. duration (hrs)
30 th Aug. 2015	60	12	30.76	40	4	236	3.93
26 th Sept. 2015	55	11	30.76	40	4	236	3.60
21 th Dec. 2015	55	11	30.76	40	4	236	3.60
OFF – Moon							
2 nd Sept. 2015	60	12	30.76	40	4	236	3.93
29 th Sept. 2015	55	11	30.76	40	4	236	3.60
24 th Dec. 2015	55	11	30.76	40	4	236	3.60
	$N_{\text{total}} = 340$	$N_{\text{total}}^{\text{full-band}} = 68$					$\text{Time}_{\text{total}}^{\text{ON-Moon}} = 11.13$

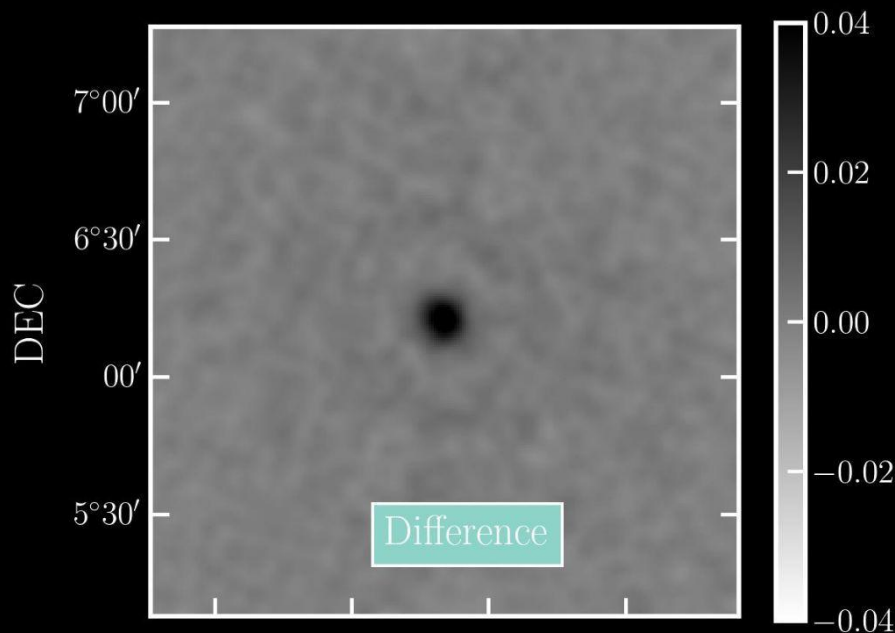
Assumed Two component Earthshine, Evans (1969), McKinley (2018)



Assumed Two component Earthshine, Evans (1969), McKinley (2018)

- **step 1: create dirty difference images of the Moon**

$$\mathbf{D} = (s_{\text{disk}}\mathbf{M} + s_{\text{spec}}\mathbf{B}) * \mathbf{P} + \mathbf{N}$$



Moon at ~100 MHz

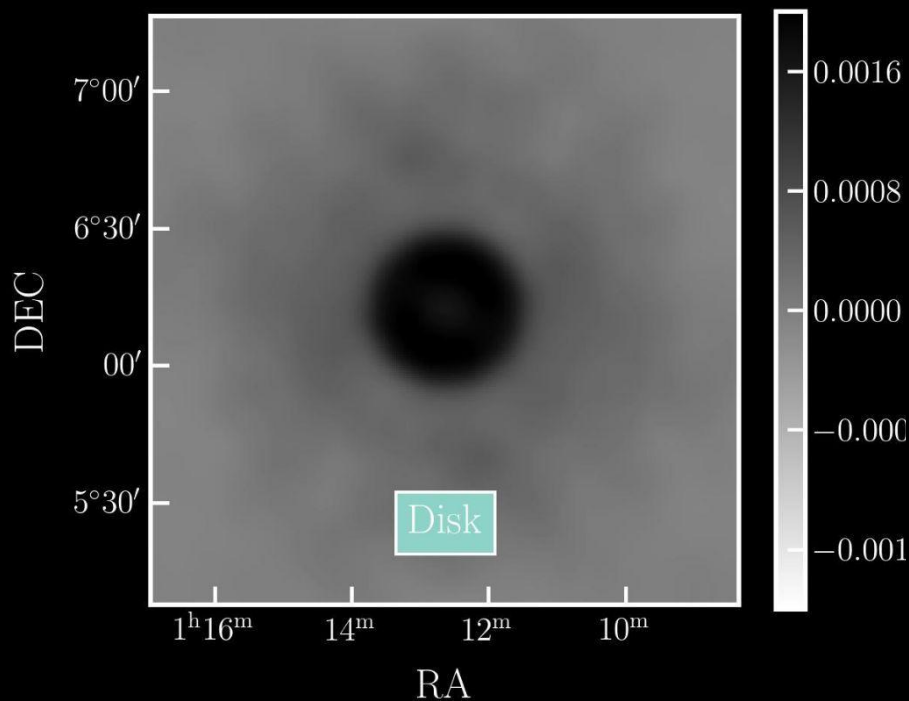
- **step 1: create dirty difference images of the Moon**

- **Step 2: Create mask**

- disk **M**
- Specular **B**

$$\mathbf{D} = (s_{\text{disk}}\mathbf{M} + s_{\text{spec}}\mathbf{B}) * \mathbf{P} + \mathbf{N}$$

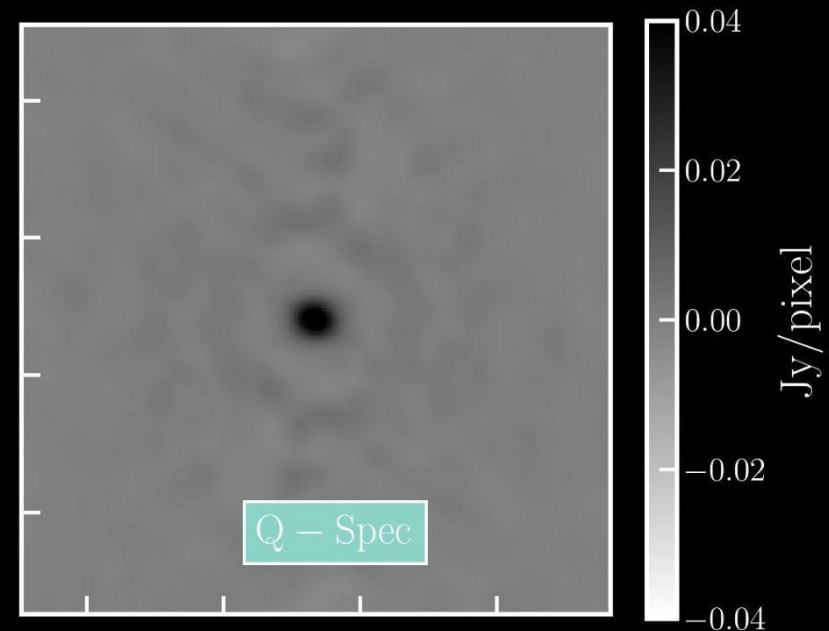
Moon at ~100 MHz



- **step 1: create dirty difference images of the Moon**
- **Step 2: Create mask**
 - disk **M**
 - Specular **B**

$$\mathbf{D} = (s_{\text{disk}}\mathbf{M} + s_{\text{spec}}\mathbf{B}) * \mathbf{P} + \mathbf{N}$$

Moon at ~100 MHz



- **step 1: create dirty difference images of the Moon**

- **Step 2: Create mask**

- disk \mathbf{M}
- Specular \mathbf{B}

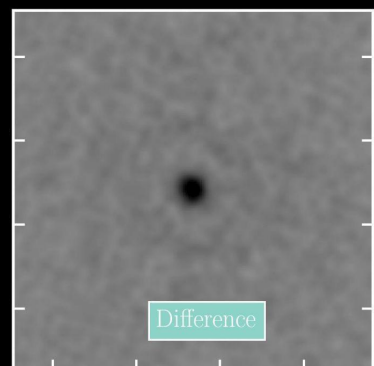
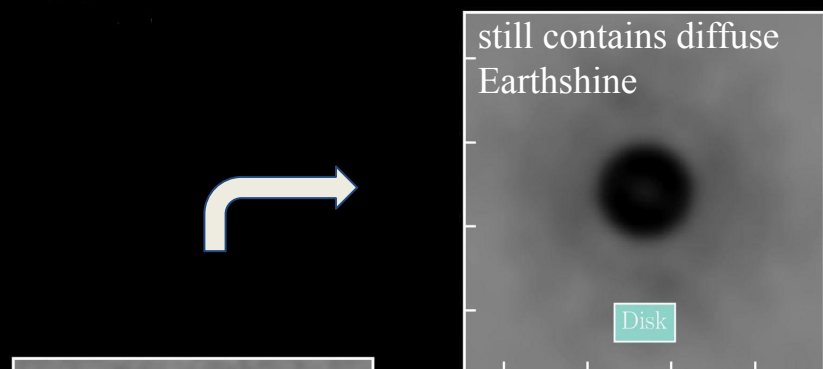
$$\mathbf{D} = (s_{\text{disk}}\mathbf{M} + s_{\text{spec}}\mathbf{B}) * \mathbf{P} + \mathbf{N}$$

- **Step 3: solve for s_{disk} , s_{spec}**

$$[s_{\text{disk}}, s_{\text{spec}}] = (\mathbf{H}^T\mathbf{H})^{-1}\mathbf{H}^T\mathbf{D}$$

$$\mathbf{H} = [\mathbf{M}*\mathbf{P}, \mathbf{B}*\mathbf{P}]$$

Isolating Earthshine- specular component

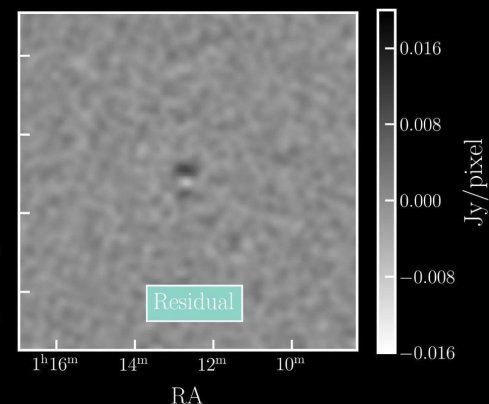
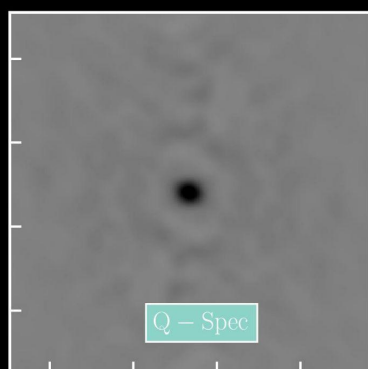


$$S_{\text{disk}} = \sum s_{\text{disk}} \cdot \mathbf{M}$$

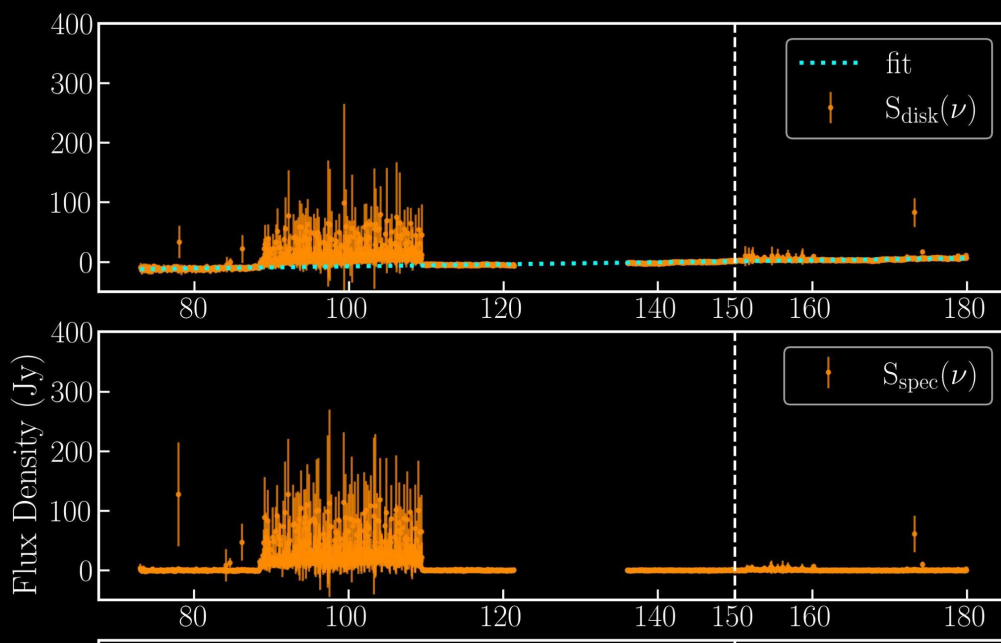
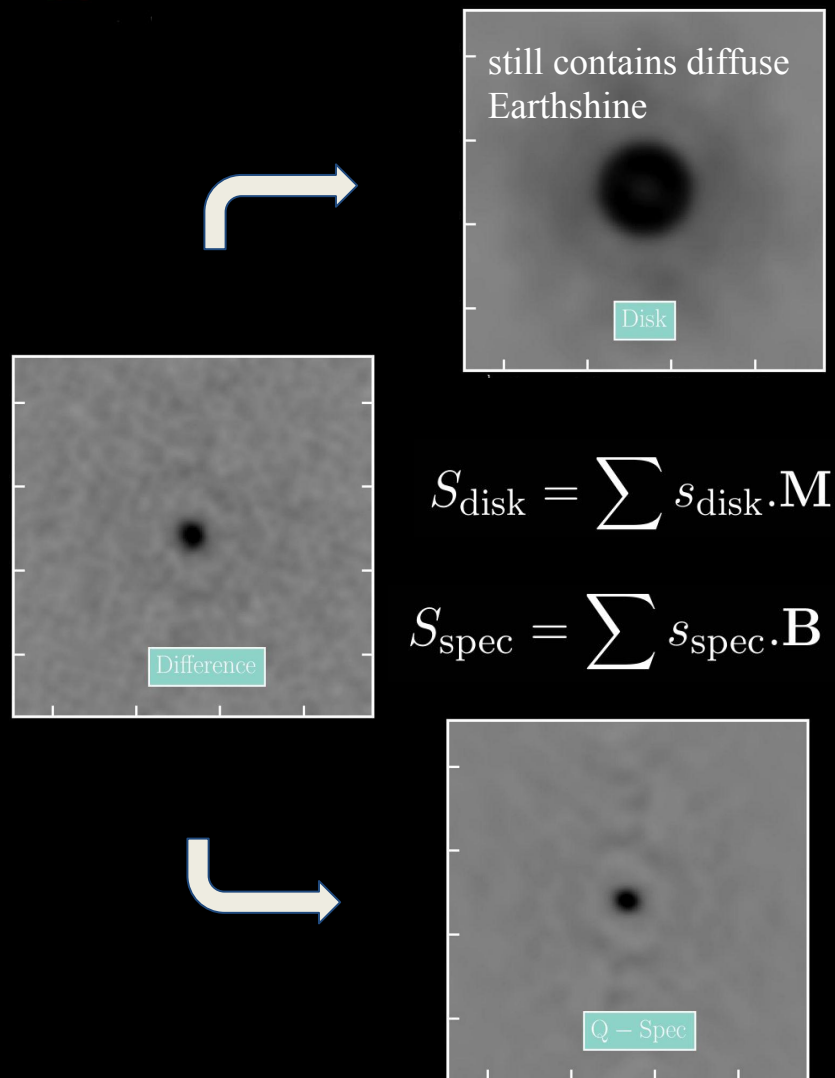
Reconstructed Moon's disk

$$S_{\text{spec}} = \sum s_{\text{spec}} \cdot \mathbf{B}$$

Specular earthshine



Isolating Earthshine- specular component





Isolating Earthshine- diffuse component (method: 1)

Radar studies from Evans (1969)

- **relation between the two Earthshine component**

$$S_{\text{diffuse}}(\nu) = R_e(\nu) S_{\text{spec}}(\nu)$$

$$R_e(\nu) = \left(\frac{S_{\text{diffuse}}(\nu=100\text{MHz})}{S_{\text{spec}}(\nu=100\text{MHz})} \right) \left(\frac{\nu}{100\text{MHz}} \right)^{0.58}$$

$$S_{\text{diffuse}}(\nu) = R_e(\nu) S_{\text{spec}}(\nu)$$

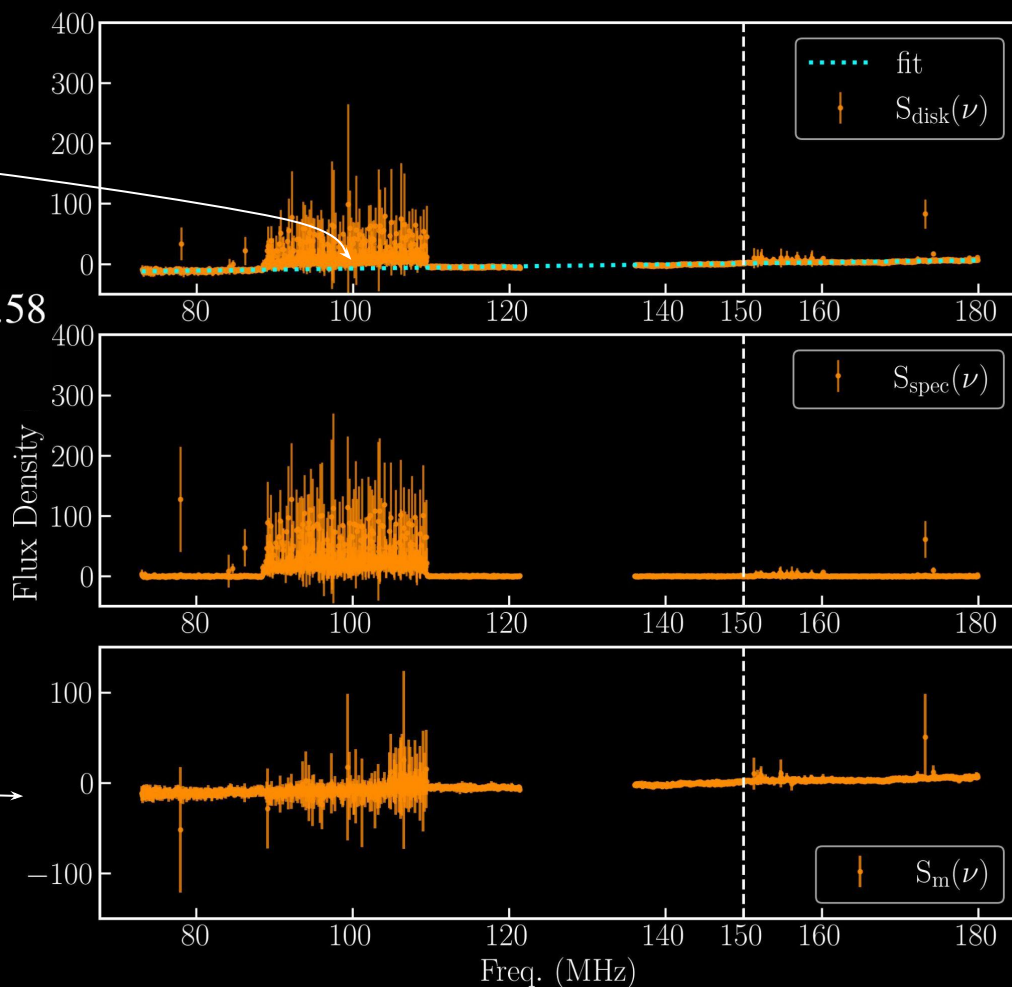
$$R_e(\nu) = \left(\frac{S_{\text{diffuse}}(\nu=100\text{MHz})}{S_{\text{spec}}(\nu=100\text{MHz})} \right) \left(\frac{\nu}{100\text{MHz}} \right)^{0.58}$$

$$S_m(\nu) = S_{\text{disk}}(\nu) - S_{\text{diffuse}}(\nu)$$

flux-density of the Moon

$$R_e(\nu) = \left(\frac{S_{\text{diffuse}}(\nu=100\text{MHz})}{S_{\text{spec}}(\nu=100\text{MHz})} \right) \left(\frac{\nu}{100\text{MHz}} \right)^{0.58}$$

$$S_m(\nu) = S_{\text{disk}}(\nu) - S_{\text{diffuse}}(\nu)$$



Freq res. $\Delta\nu = 40$ KHz

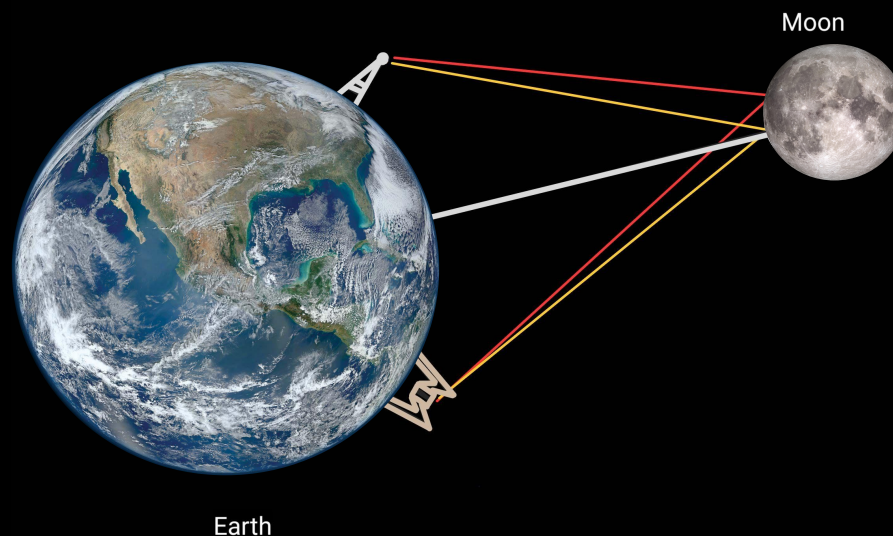


Isolating Earthshine- diffuse component (method: 2)

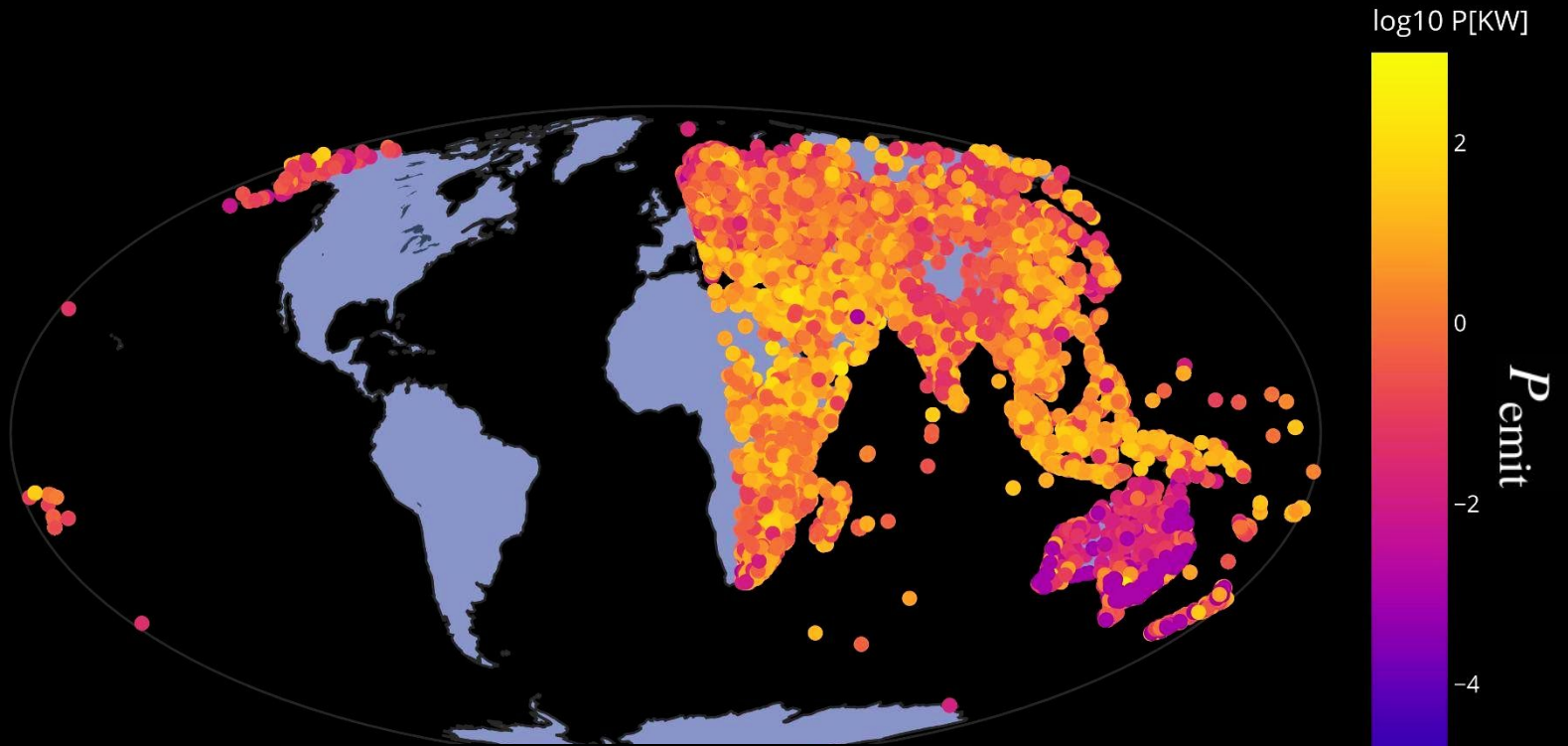
- **FM station catalog - fmlist.org**
- **Estimating power received at MWA during the observations**

Assumptions

- **All FM stations produce isotropic power, have constant bandwidth**
- **Reflection from the Moon are diffuse**



Reflected Power from the Moon



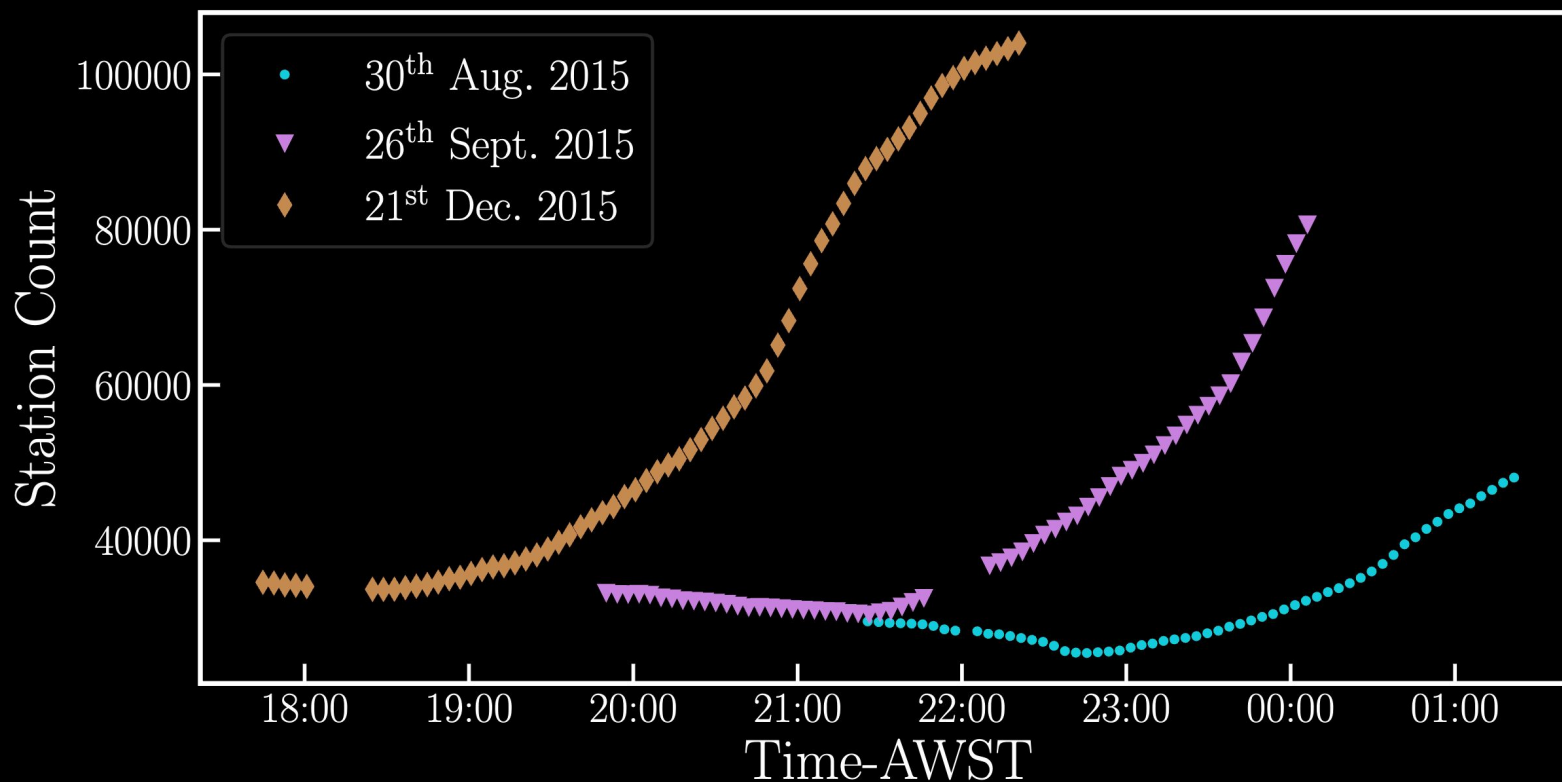
$$P_{\text{rec}}(\nu) = \frac{P_{\text{emit}}(\nu) \sigma_{\text{cross}} A_{\text{eff}}}{(4\pi)^2 D_1^2 D_2^2},$$

$P_{\text{emit}}(\nu)$ - Station Power

σ_{cross} - Radar Cross section
(~7% albedo in Radio, [Evans \(1969\)](#))

ΔB - Transmission Bandwidth D_1, D_2 - Distance between the Moon from MWA, FM station

Station count vs. Observing Time

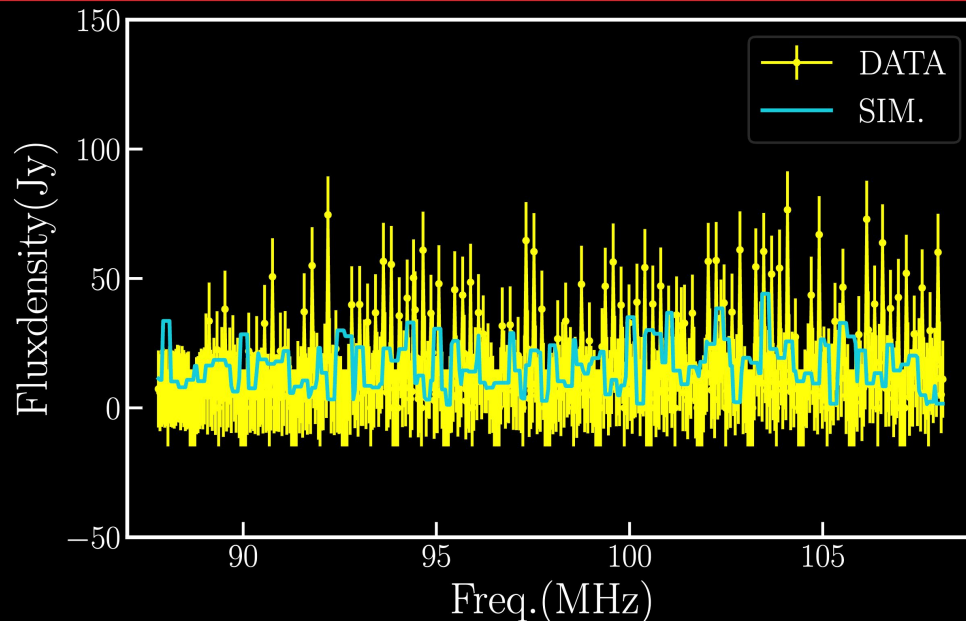




Isolating Earthshine- diffuse component (method: 2)

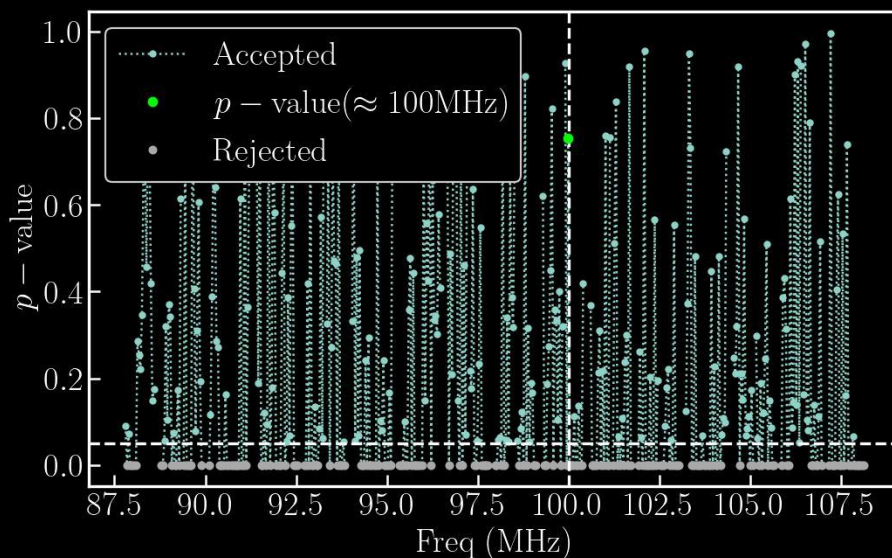
Freq res. $\Delta\nu = 40$ KHz

Diffuse Flux-density
Data and Simulation

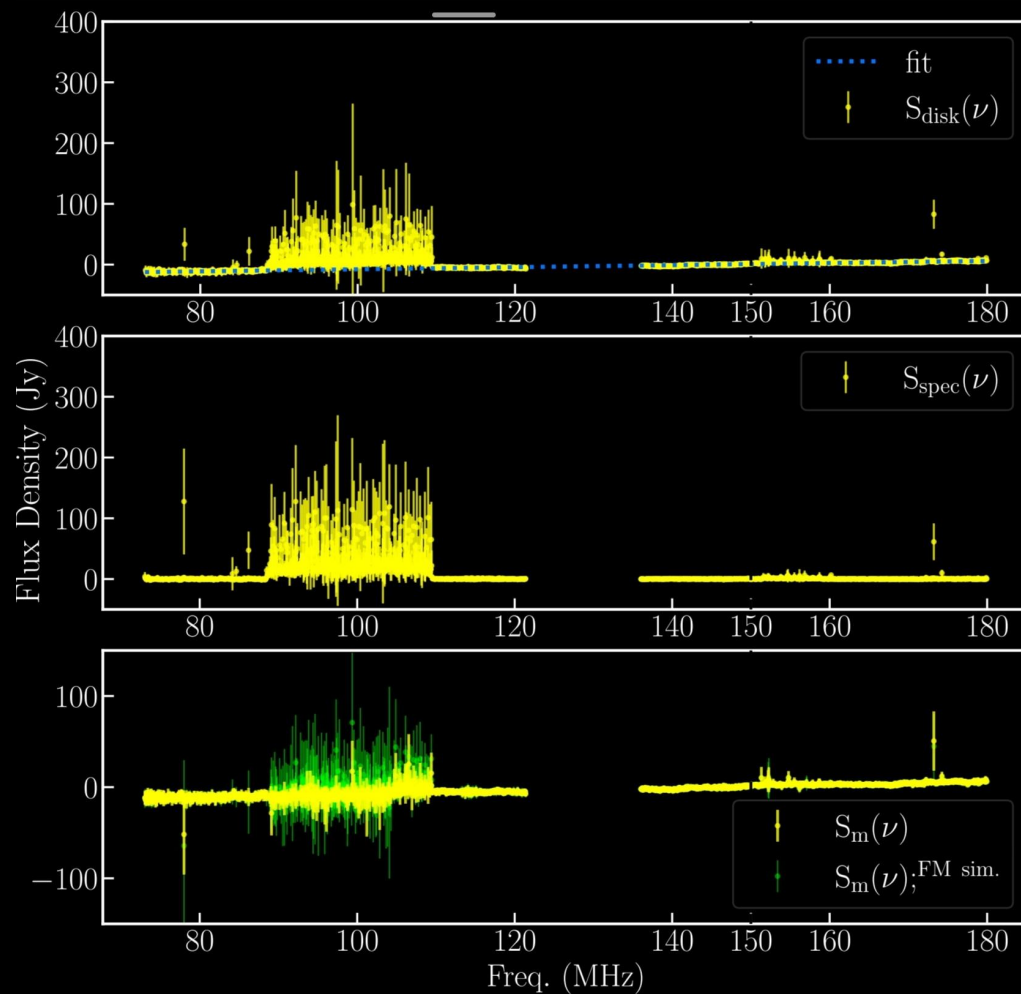


T-test

Epochs	p -value at ($\approx \nu_0$)
Aug.	0.75
Sept.	0.69
Nov.	0.78



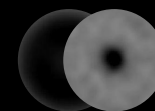
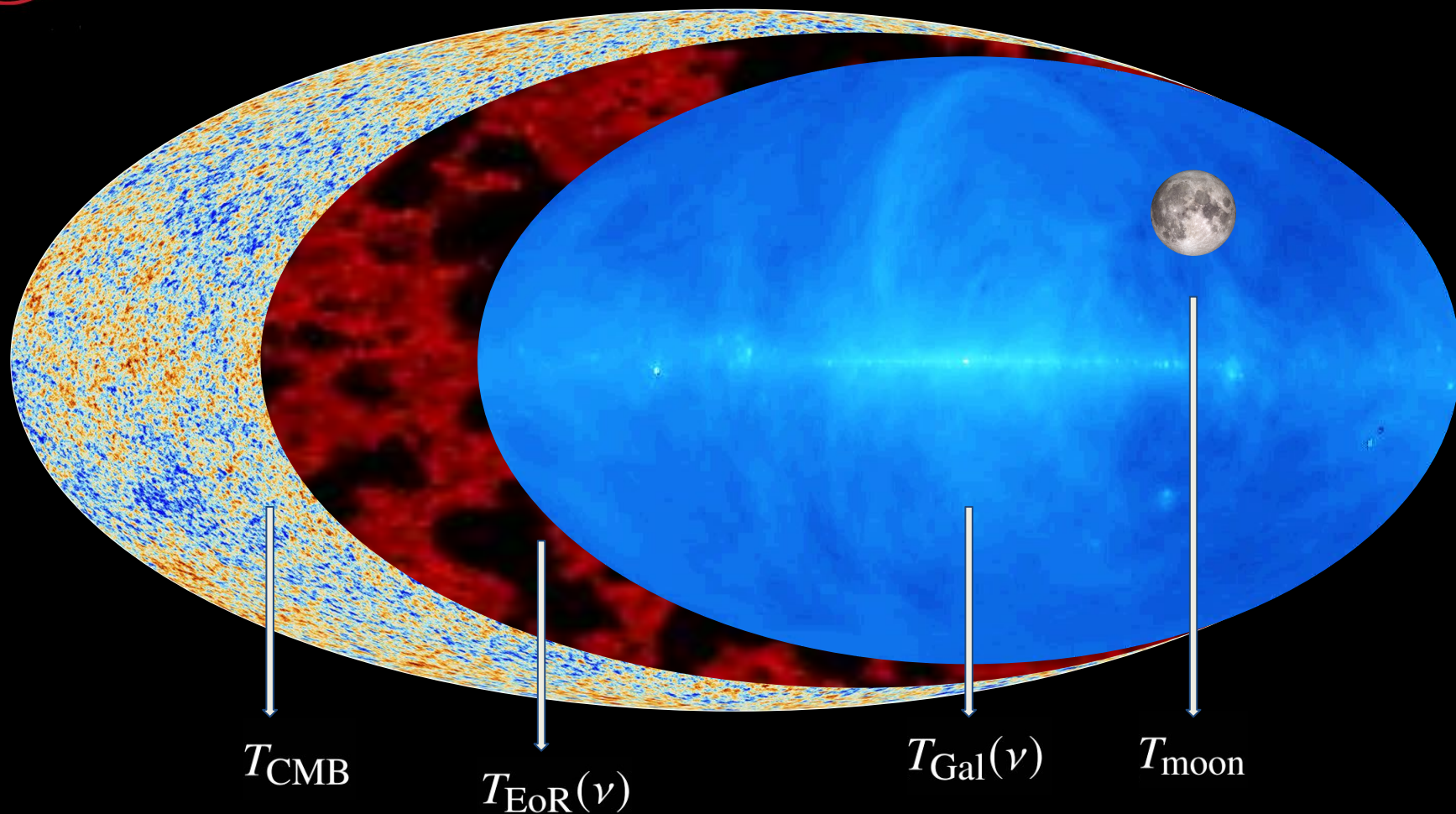
flux-density of the Moon



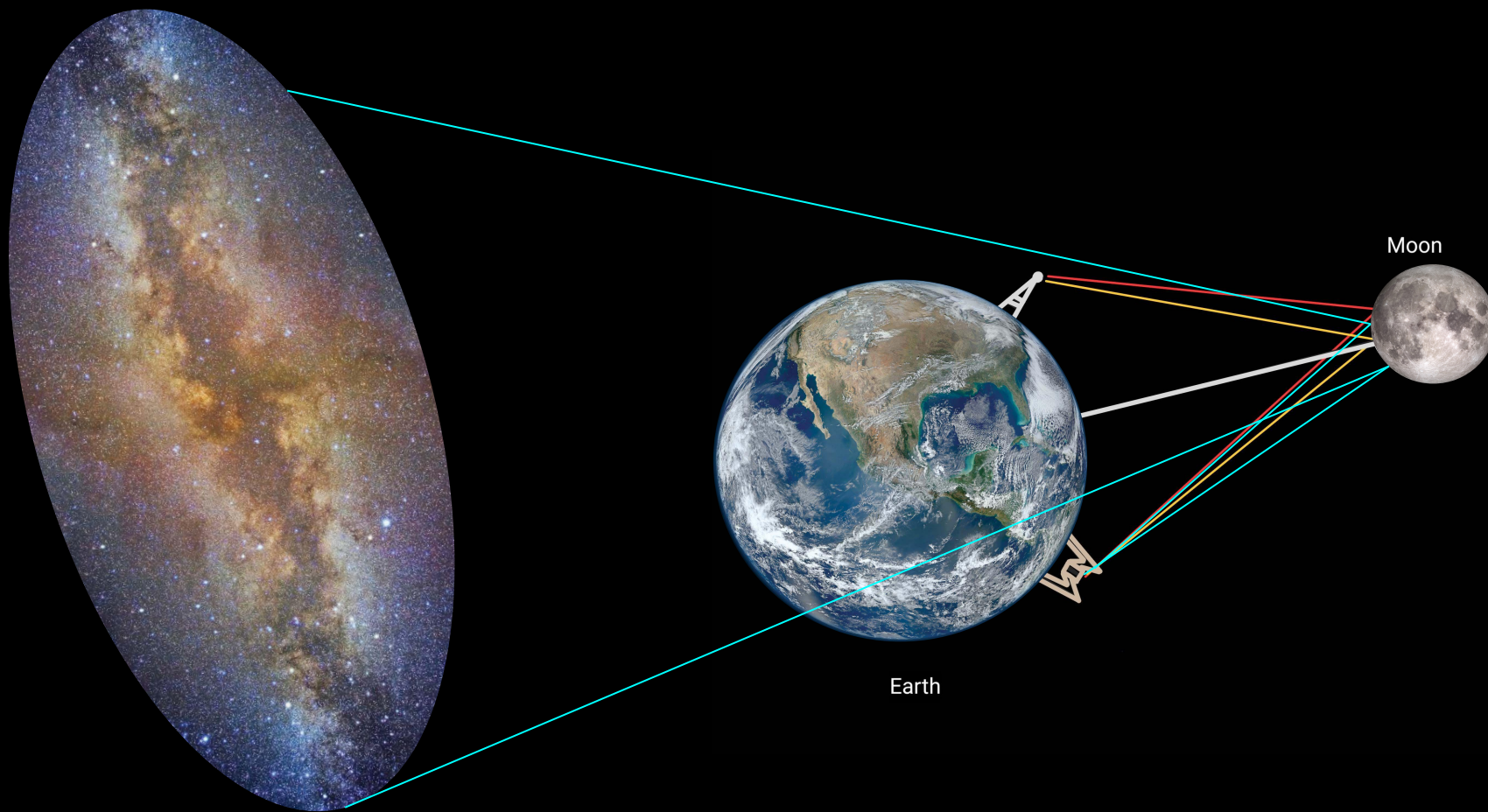


It doesn't ends here!

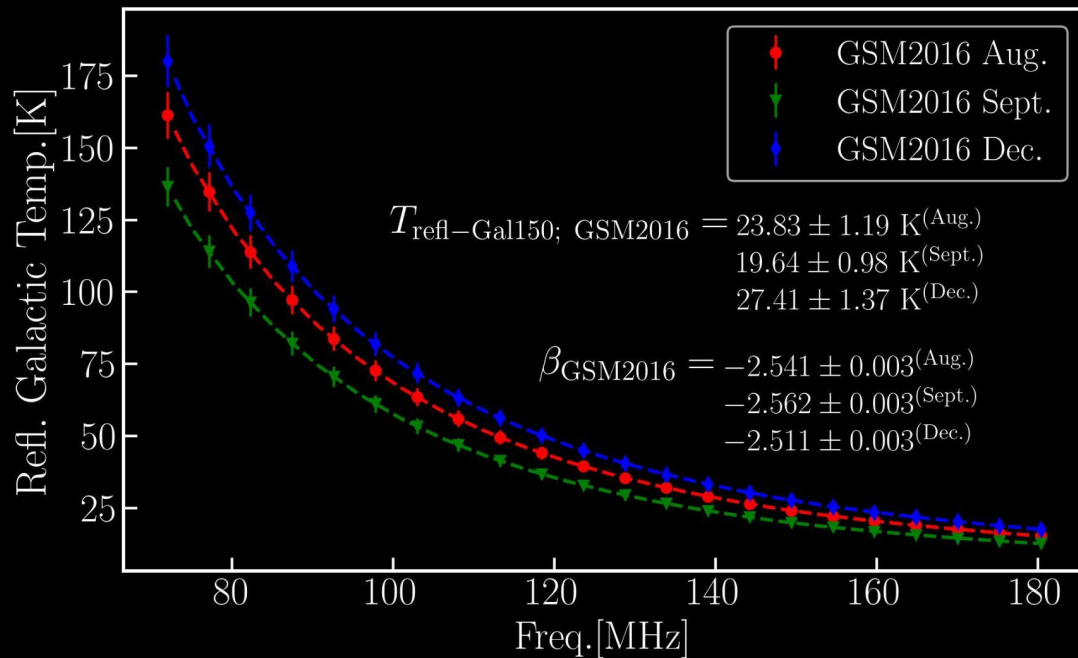
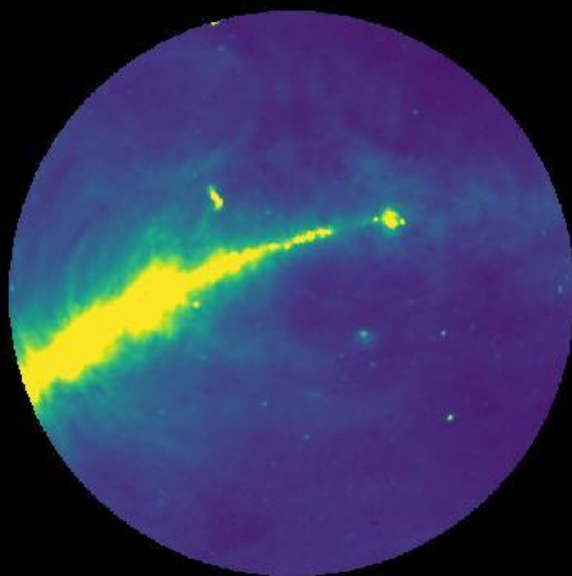
The Universe of Temperatures



Next Step:



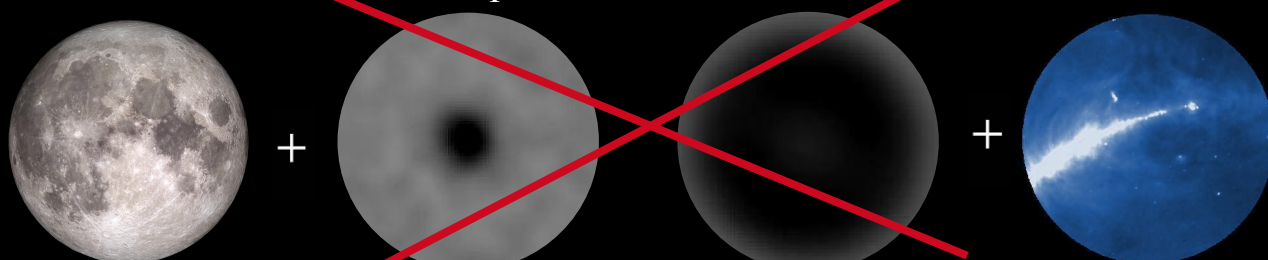
Reflected Galactic at 150MHz



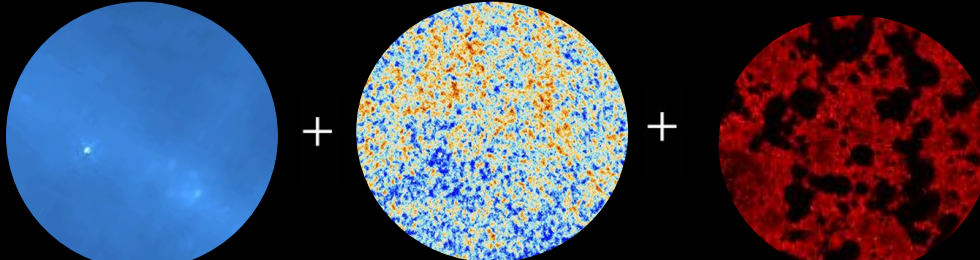
Reflected galactic emission from the Moon

$$T_{\text{Gal}}(\nu) = T_{150} \left(\frac{\nu}{150\text{MHz}} \right)^{\alpha}$$

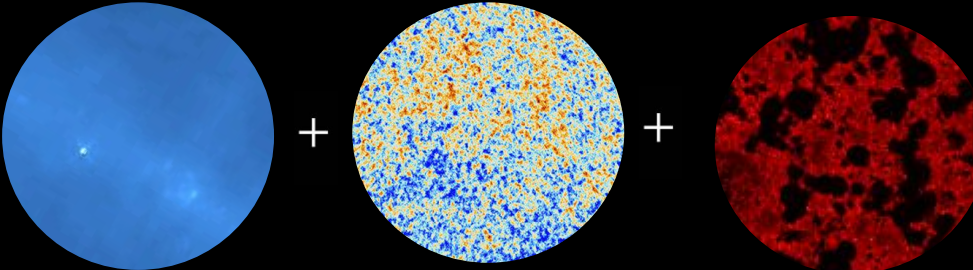
What MWA sees?

$$T_{\text{lunar}}(\nu) = T_{\text{moon}} + \cancel{T_{\text{spec}}} + \cancel{T_{\text{diffuse}}} + T_{\text{refl-Gal}}(\nu)$$


T_{moon} $T_{\text{refl-Earth}}(\nu)$ $T_{\text{refl-Gal}}(\nu)$

$$T_{\text{sky}}(\nu) = T_{\text{Gal}}(\nu) + T_{\text{CMB}} + T_{\text{EoR}}(\nu)$$


$T_{\text{Gal}}(\nu)$ T_{CMB} $T_{\text{EoR}}(\nu)$

$$T_{\text{sky}}(\nu) = T_{\text{Gal}}(\nu) + T_{\text{CMB}} + T_{\text{EoR}}(\nu)$$


The diagram illustrates the decomposition of the total sky temperature $T_{\text{sky}}(\nu)$ into three components. On the left, the equation $T_{\text{sky}}(\nu) = T_{\text{Gal}}(\nu) + T_{\text{CMB}} + T_{\text{EoR}}(\nu)$ is shown. To the right, three circular panels represent these components: $T_{\text{Gal}}(\nu)$ is a blue circular panel with a few bright spots; T_{CMB} is a circular panel with a noisy, multi-colored (blue, yellow, orange) pattern; and $T_{\text{EoR}}(\nu)$ is a circular panel with a noisy, red and black pattern. Plus signs are placed between the panels to indicate their summation.

$T_{\text{Gal}}(\nu)$ - Temp. of the patch of sky
occluded by the Moon

T_{CMB} - 2.735 K



What MWA sees?

$$\begin{aligned}\Delta T(\nu) &= T_{\text{lunar}}(\nu) - T_{\text{sky}}(\nu) \\ &= [T_{\text{moon}} + \cancel{T_{\text{refl-Earth}}(\nu)} + T_{\text{refl-Gal}}(\nu)] \\ &\quad - [T_{\text{Gal}}(\nu) + T_{\text{CMB}} + T_{\text{EoR}}(\nu)]\end{aligned}$$

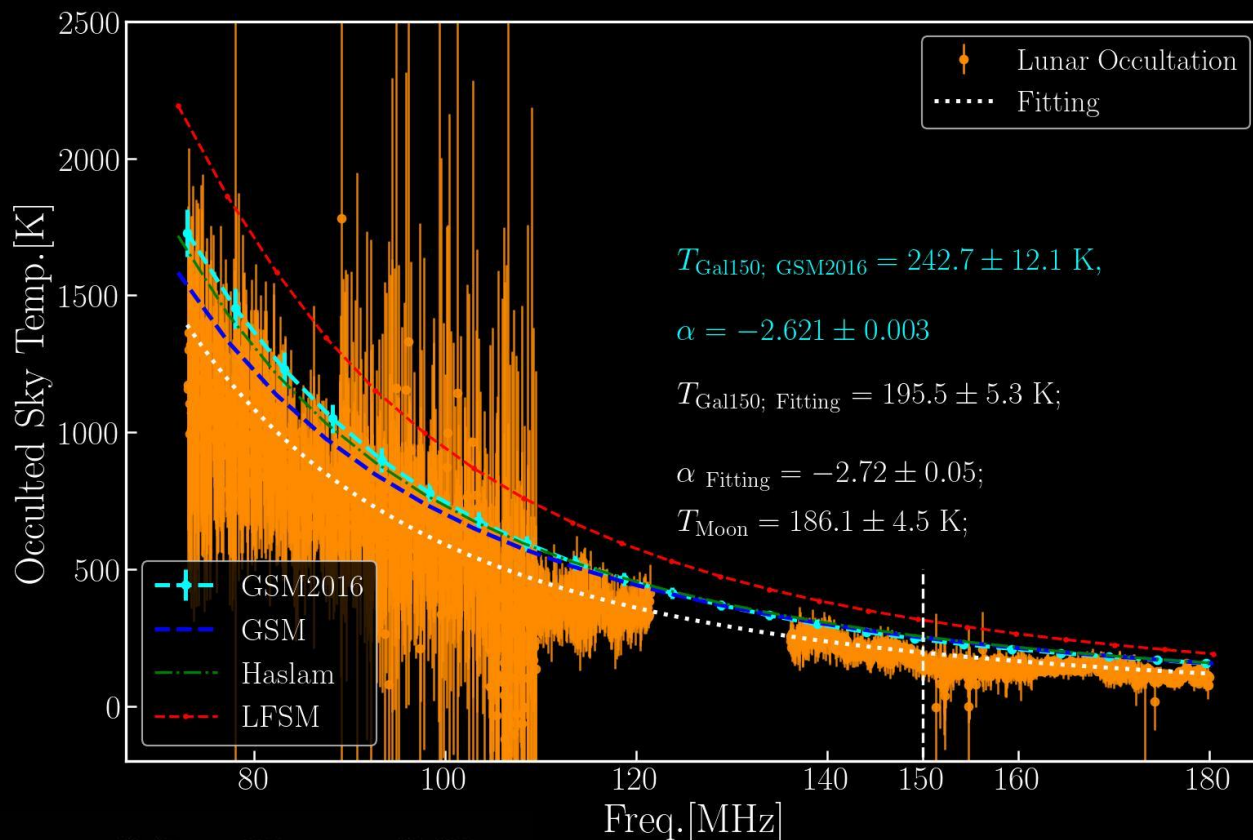
where,

$$\Delta T(\nu) = \frac{10^{-26} c^2 S_m(\nu)}{2k\Omega\nu^2}$$

$S_m(\nu)$: flux density of the Moon

Ω : Solid angle of the Moon

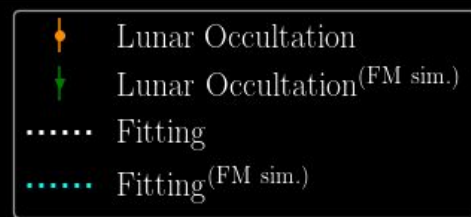
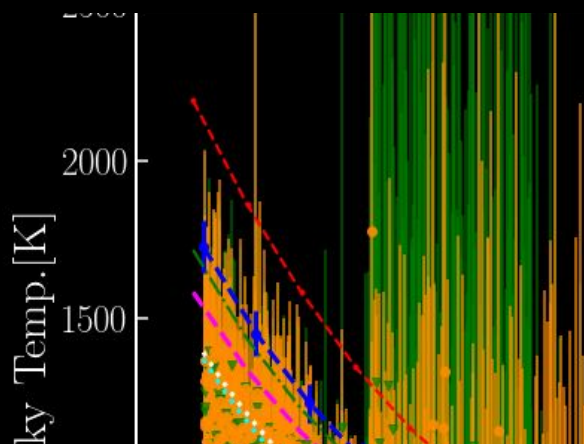
Fitting for Galactic Temp (method: 1)



$$T_{\text{Gal}}(\nu) - T_{\text{moon}} = [T_{\text{ref-Earth}}(\nu) + T_{\text{ref-Gal}}(\nu)] - [\Delta T(\nu) + T_{\text{CMB}} + T_{\text{EOR}}(\nu)]$$

$$T_{\text{Gal}}(\nu) - T_{\text{moon}} = T_{\text{Gal150}} \left(\frac{\nu}{150 \text{ MHz}} \right)^\alpha - T_{\text{offset}}$$

Fitting for Galactic Temp

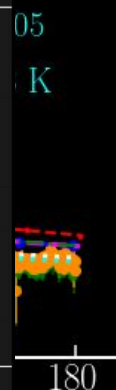


$$T_{\text{Gal150; GSM2016}} = 242.7 \pm 12.1 \text{ K,}$$

$$\alpha = -2.621 \pm 0.003$$

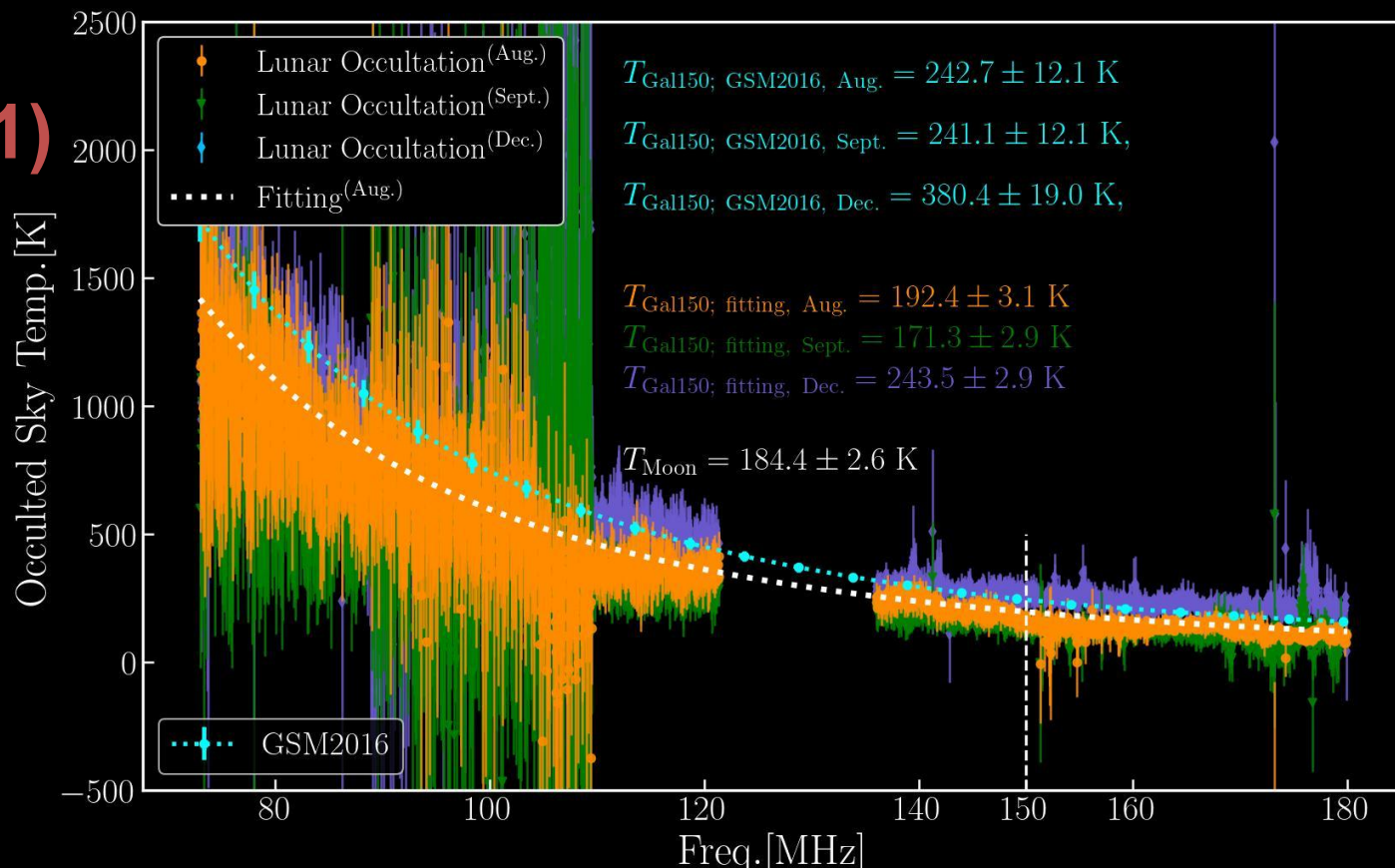
$$T_{\text{Gal150; Fitting}} = 195.5 \pm 5.3 \text{ K;}$$

Epoch	Sky - model	$T_{\{\text{Gal150; model}\}} \text{ (K)}$	α_{model}	Fitting	$T_{\{\text{Gal150; fitting}\}} \text{ (K)}$	α_{fitting}	$T_{\{\text{Moon}\}} \text{ (K)}$
Aug.	GSM	250.4 ± 12.5	-2.540 ± 0.002	Method 1	199.2 ± 5.4	-2.70 ± 0.05	188.3 ± 4.6
				Method 2 (FM sim.)	183.5 ± 5.1	-2.79 ± 0.05	174.2 ± 4.4
	GSM2016	242.7 ± 12.1	-2.621 ± 0.003	.	195.5 ± 5.3	-2.72 ± 0.05	186.1 ± 4.5
				..	179.2 ± 5.0	-2.82 ± 0.05	171.4 ± 4.3
	LFSM	313.9 ± 15.7	-2.689 ± 0.003	.	202.8 ± 5.3	-2.70 ± 0.05	188.5 ± 4.5
				..	189.0 ± 5.1	-2.78 ± 0.05	176.2 ± 4.4
Sept.	Haslam	253.7 ± 12.7	-2.603 ± 0.003	.	199.2 ± 5.3	-2.71 ± 0.05	187.9 ± 4.6
				..	183.7 ± 5.1	-2.80 ± 0.05	174.0 ± 4.3
	GSM	253.4 ± 12.7	-2.540 ± 0.002	.	177.6 ± 4.4	-2.54 ± 0.04	189.4 ± 4.2
				..	185.6 ± 5.1	-2.43 ± 0.05	198.5 ± 4.9
	GSM2016	241.0 ± 12.0	-2.585 ± 0.003	.	174.4 ± 4.3	-2.56 ± 0.04	187.4 ± 4.4
				..	182.2 ± 5.0	-2.47 ± 0.05	196.0 ± 4.8
	LFSM	295.3 ± 14.8	-2.689 ± 0.003	.	180.8 ± 4.4	-2.56 ± 0.04	189.2 ± 4.2
				..	188.6 ± 5.0	-2.46 ± 0.04	198.0 ± 4.8
	Haslam	250.7 ± 12.5	-2.603 ± 0.003	.	177.4 ± 4.4	-2.56 ± 0.04	188.9 ± 4.2



Jointly fitting for the Galactic Temp

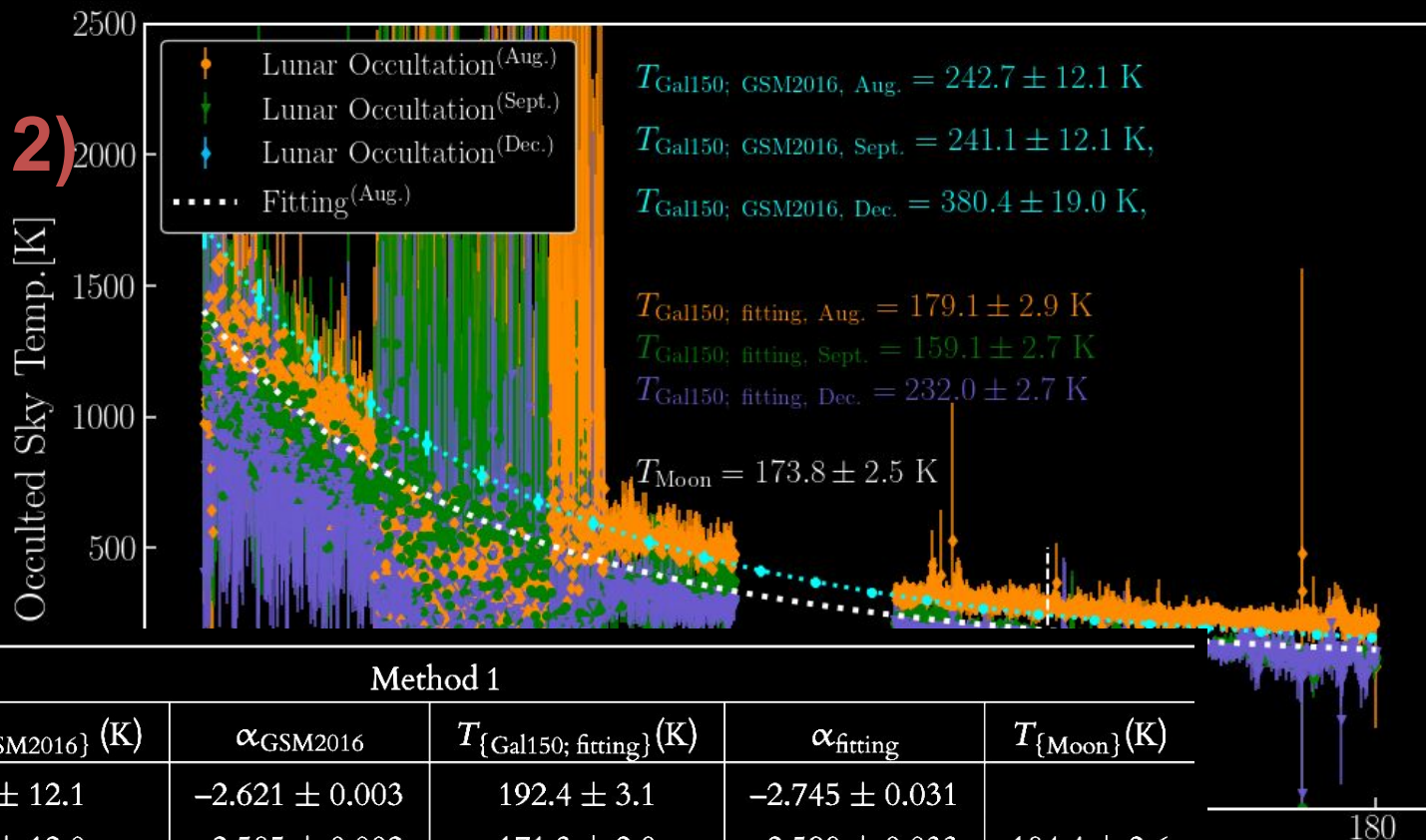
(method: 1)



assumption: T_{Moon} is constant through all the epochs

Fitting with Galactic Temp

(method: 2)



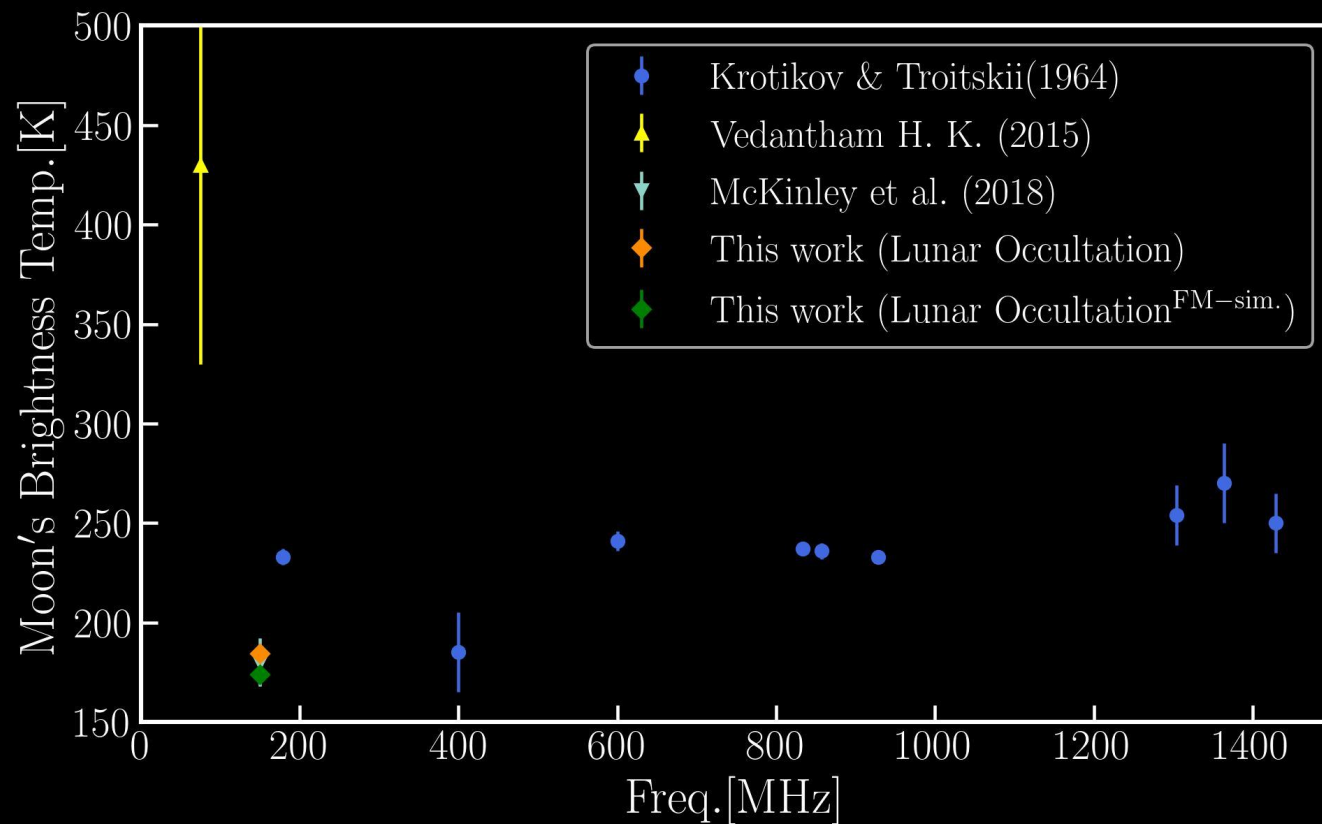
Method 1

Epochs	$T_{\{\text{Gal150; GSM2016}\}} \text{ (K)}$	α_{GSM2016}	$T_{\{\text{Gal150; fitting}\}} \text{ (K)}$	α_{fitting}	$T_{\{\text{Moon}\}} \text{ (K)}$
Aug.	242.7 ± 12.1	-2.621 ± 0.003	192.4 ± 3.1	-2.745 ± 0.031	
Sept.	241.0 ± 12.0	-2.585 ± 0.002	171.3 ± 2.8	-2.598 ± 0.033	184.4 ± 2.6
Dec.	380.4 ± 19.0	-2.497 ± 0.002	243.5 ± 2.9	-2.612 ± 0.022	

Method 2 (FM sim.)

Aug.	242.7 ± 12.1	-2.621 ± 0.003	179.1 ± 2.9	-2.798 ± 0.033	
Sept.	241.0 ± 12.0	-2.585 ± 0.002	159.1 ± 2.7	-2.640 ± 0.034	173.8 ± 2.5
Dec.	380.4 ± 19.0	-2.497 ± 0.002	232.0 ± 2.7	-2.661 ± 0.021	

Previous Moon measurements



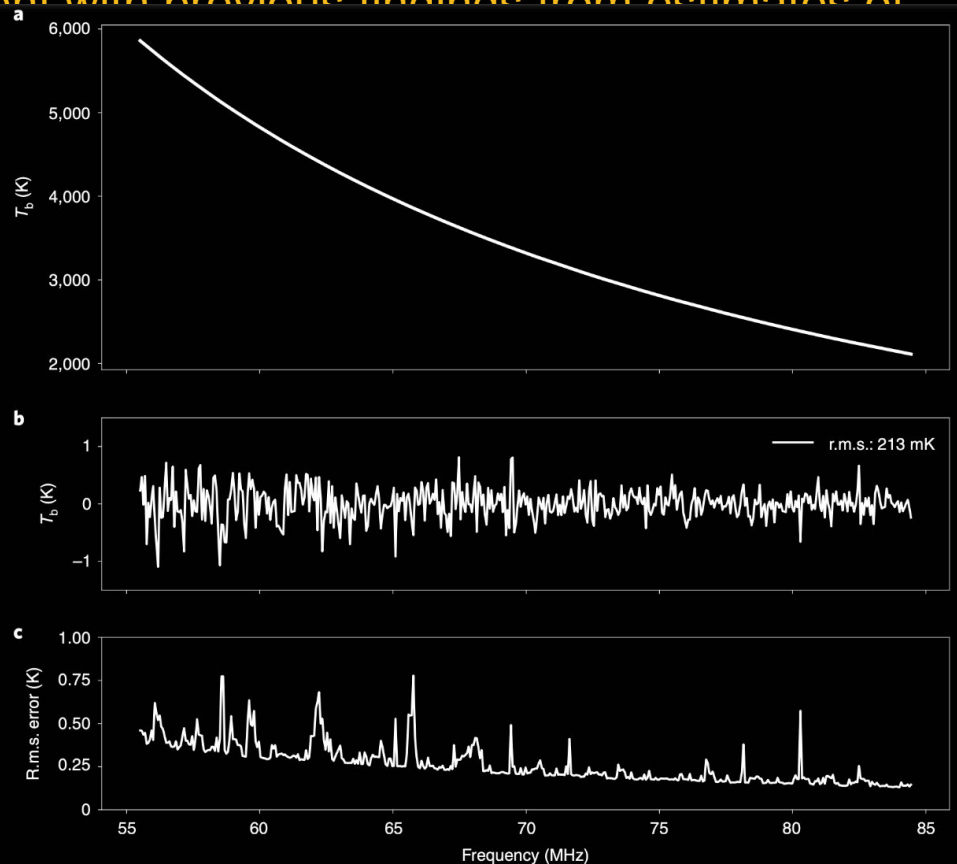
Moon temperature is consistent with the previous work from [McKinley, B. \(2018\)](#)

Summary

- We used 6 Nights of MWA-I observations to test Lunar Occultation.
- FM RFI mitigation technique
 - using RADAR studies of Moon's reflections [Evans \(1969\)](#).
 - with simple FM flux-density estimator.
- Moon's temperature is consistent with previous findings from estimates of [McKinley \(2018\)](#).
- The jointly fitted occulted background due to data and partly due to EARTHSHINE mitigation is really

Future hopes?

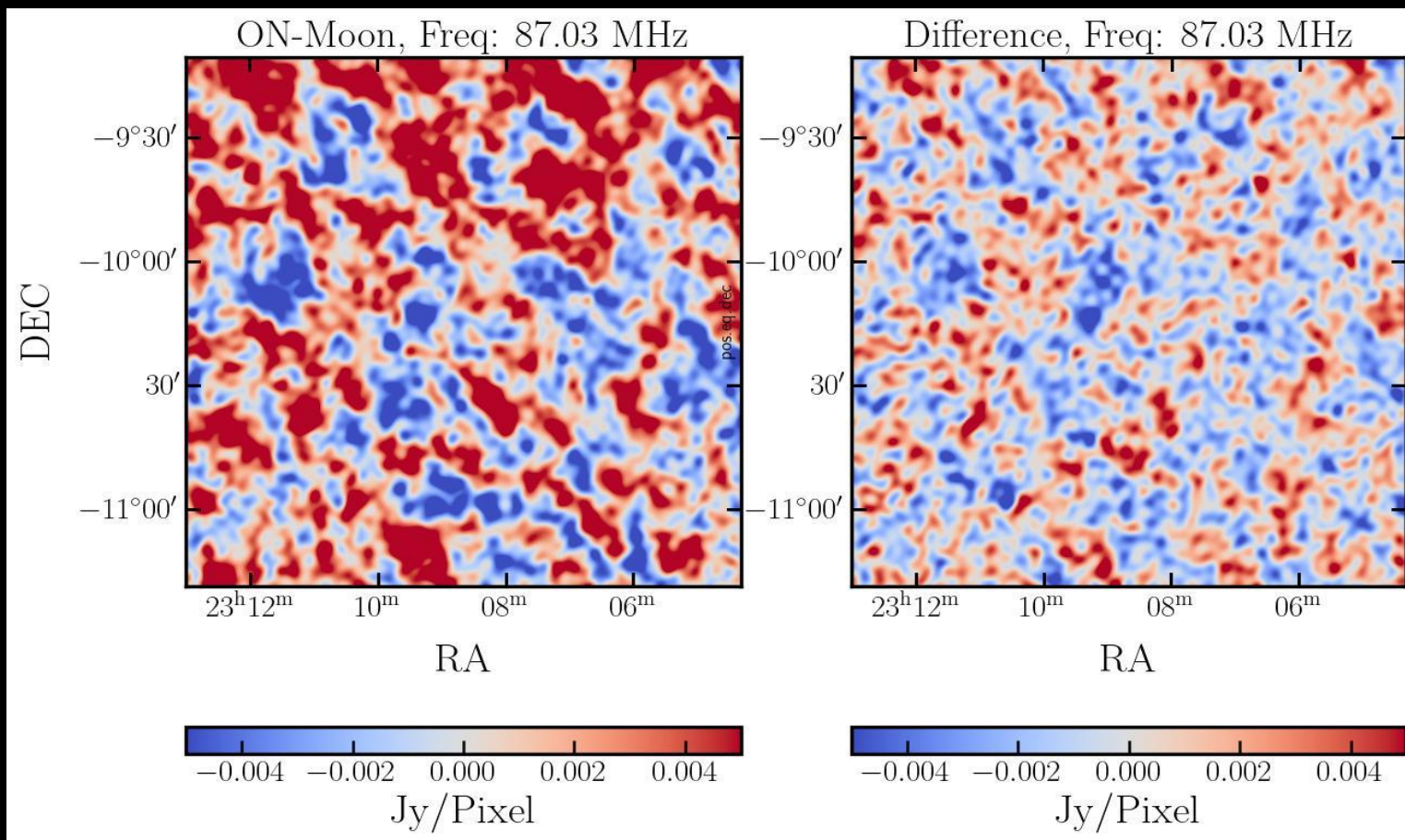
- Independent constraints on T_b such as EDA2.
- Hope to reach a RMS level as
- Check for the systematics introduced
- Check if Occulted Sky Temperature similar tests as Global Experiments



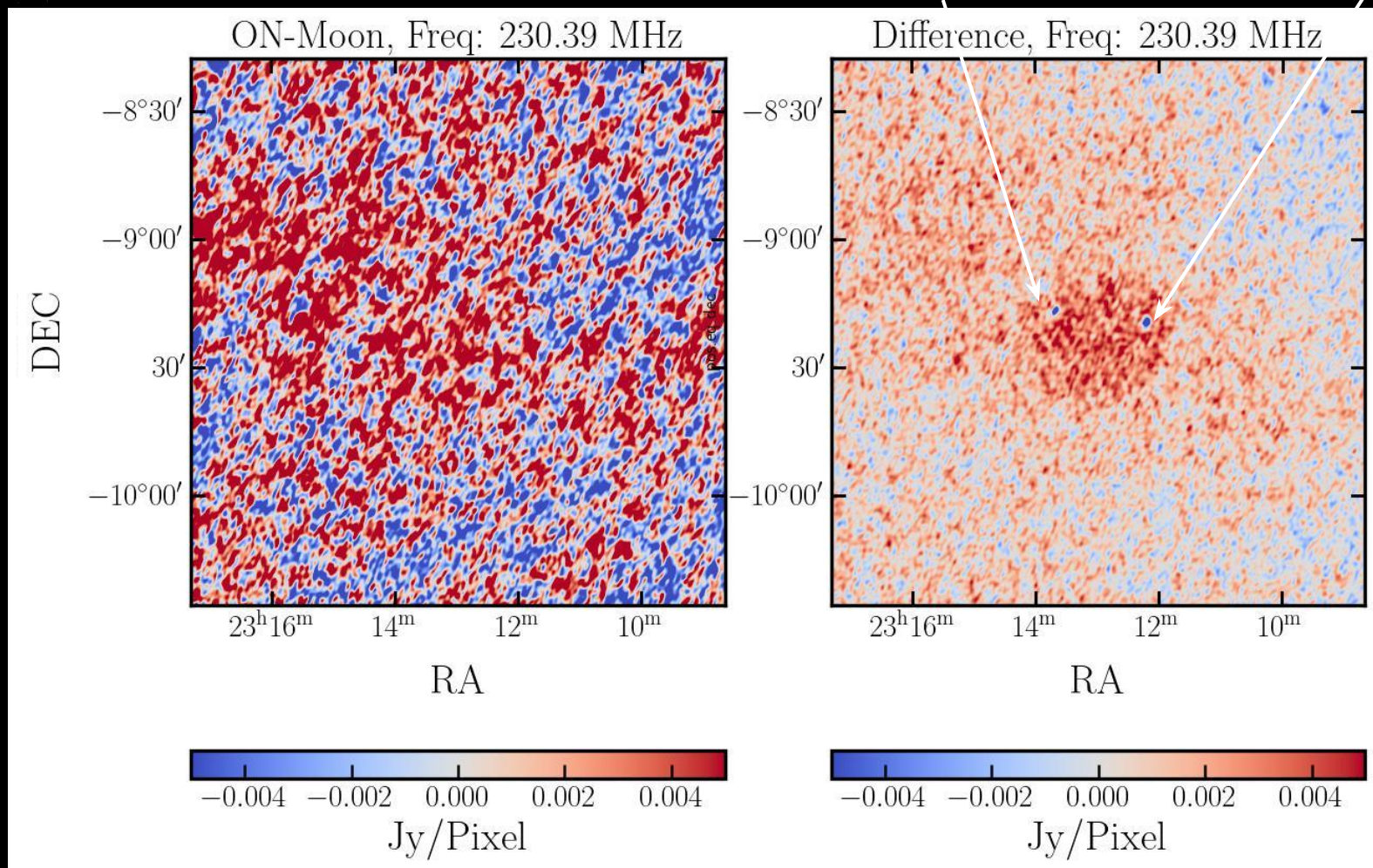
My feelings at present :(



Some MWA-phase II (extended) images



J231212-091927





GPS start 1349183898, end 1349184190, average 1349184044

Amps for obsid 1349183896

g_x D_x D_y g_y





Maybe the future

