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Emulating 21cmFAST summary observables with 21cmEMU

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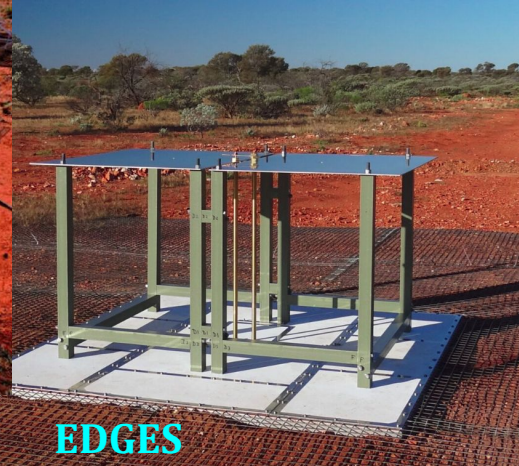
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HST



MWA



EDGES



VLT



SKA low



HERA

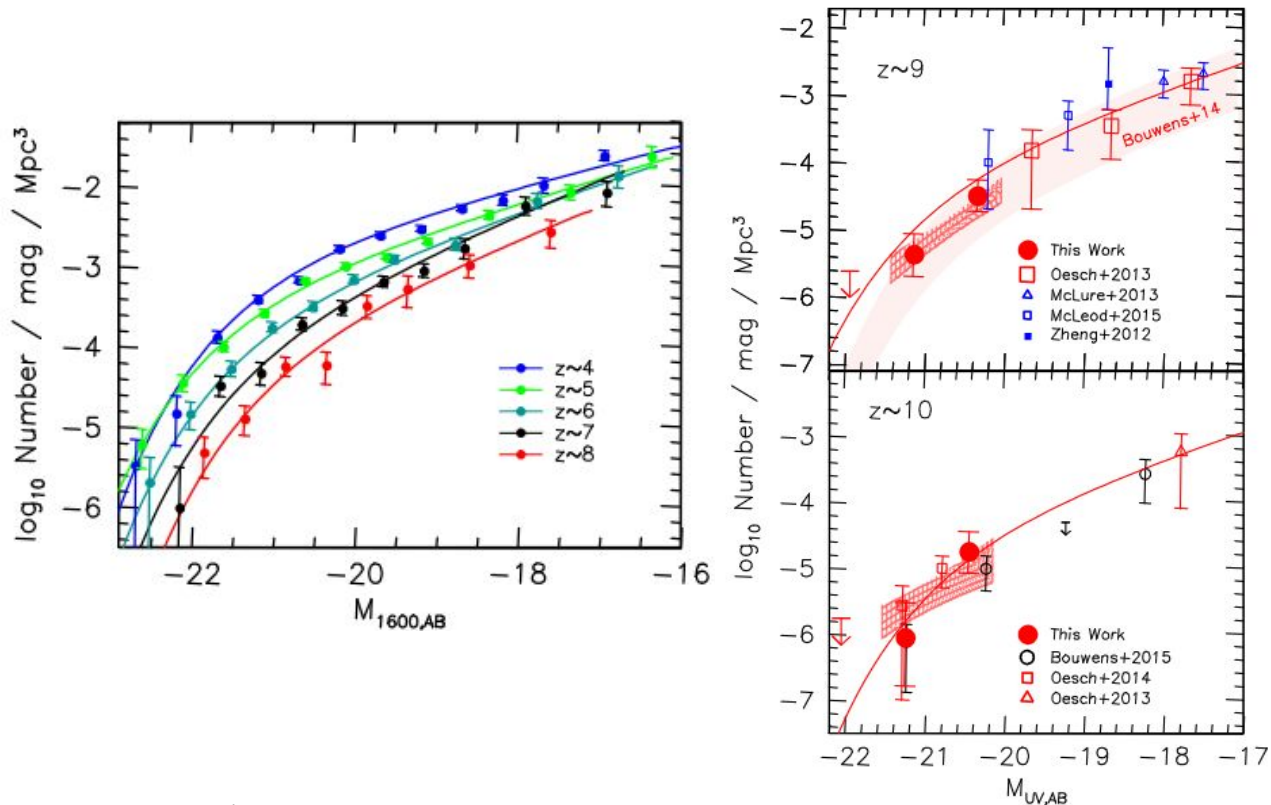


JWST

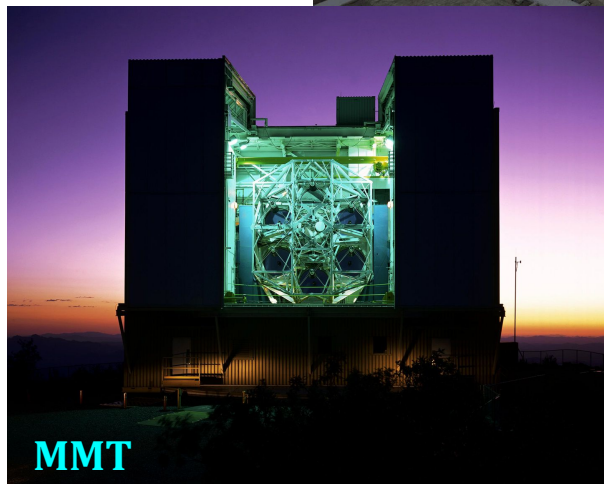
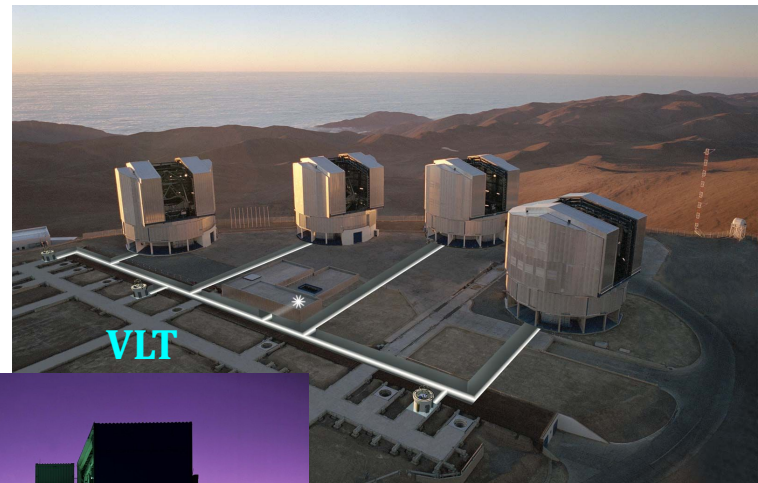
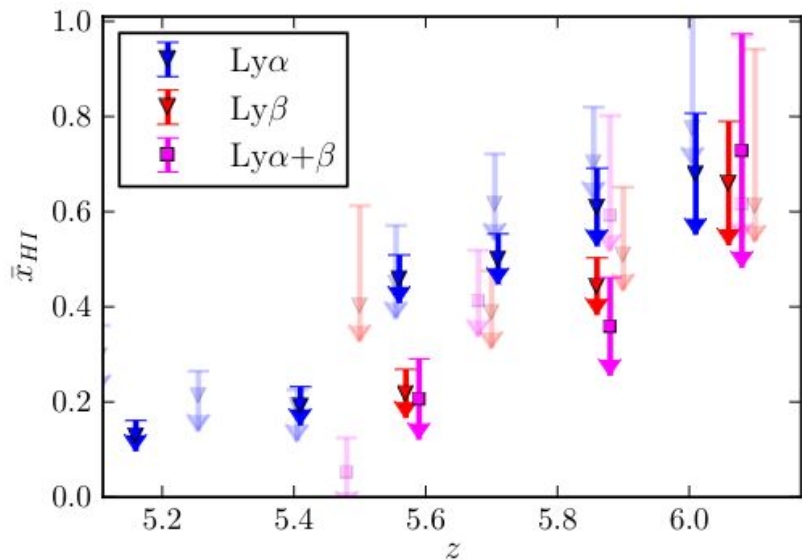


LOFAR

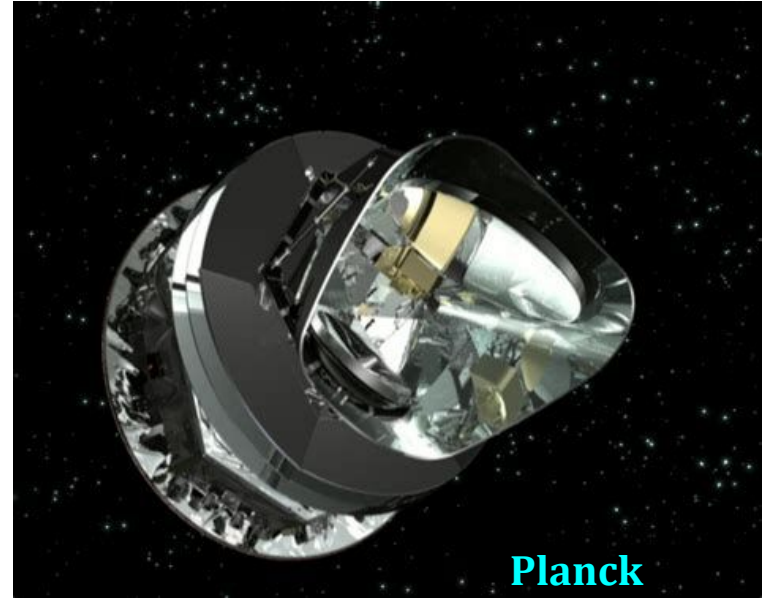
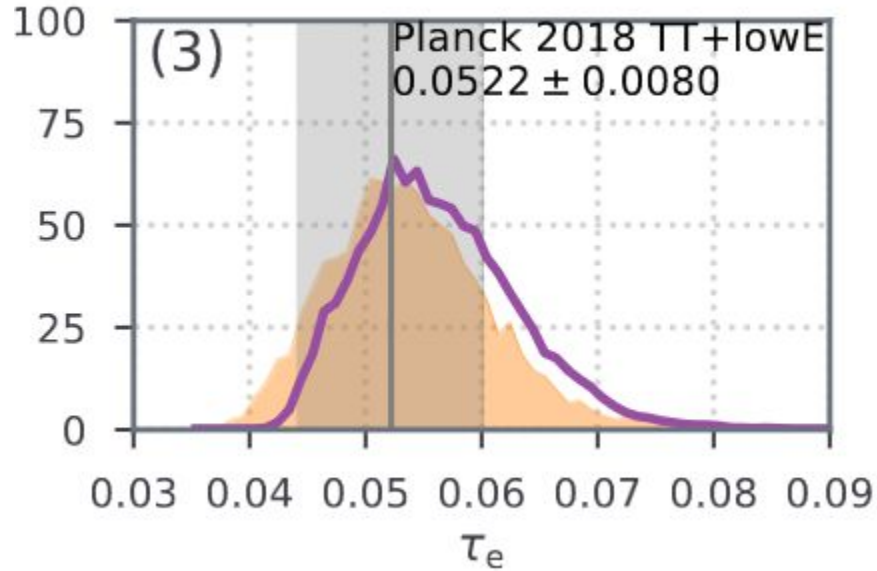
UV Luminosity Functions

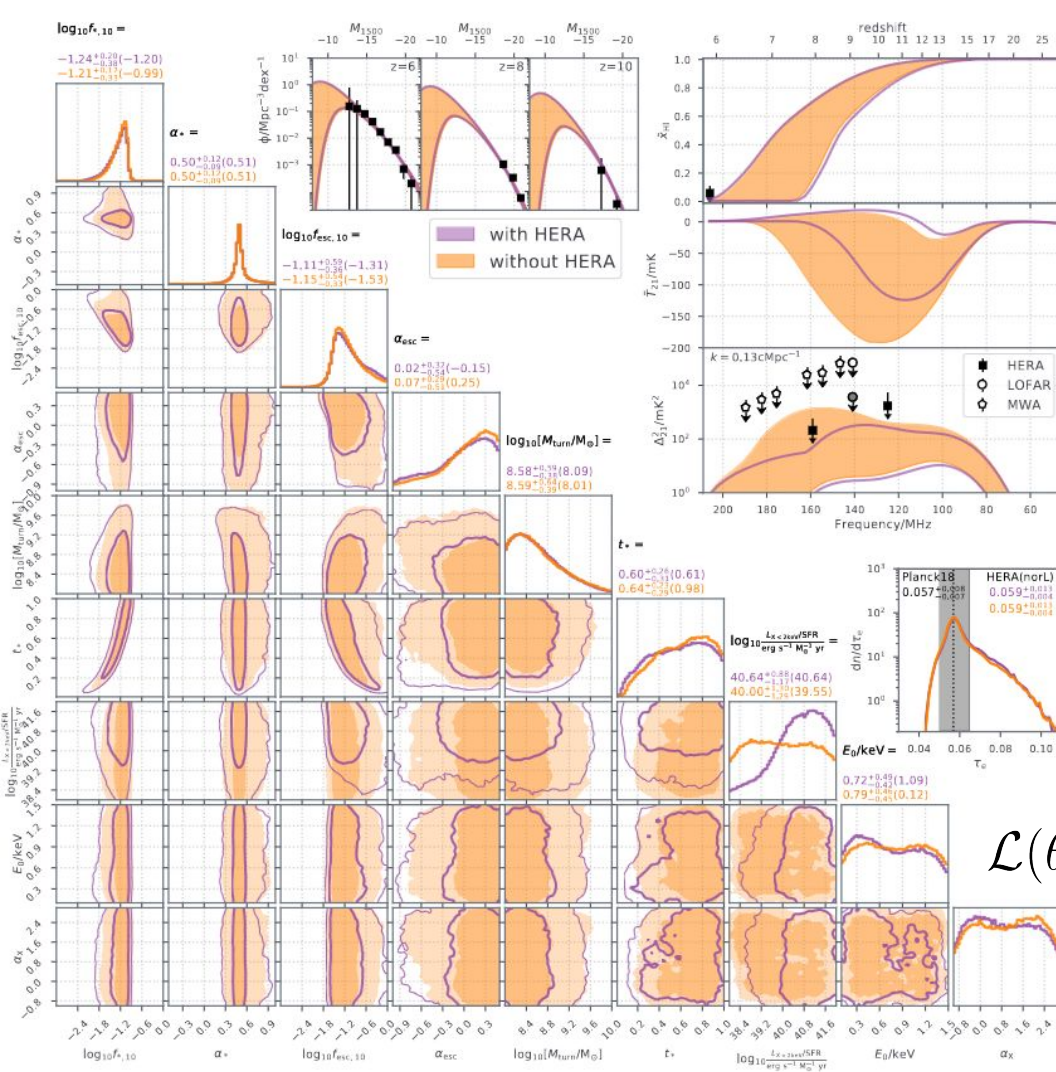


Hydrogen Neutral Fraction Upper Limit



Thomson Scattering CMB Optical Depth





$$\mathcal{L}(\theta|\mathcal{M})_{\text{total}} = \mathcal{L}_{\tau_e} \times \mathcal{L}_{\text{xHI}} \times \mathcal{L}_{\text{LFs}} \times \mathcal{L}_{\text{PS}}$$

HERA22 takes ~400k CPU hrs to run

Why emulate?

- **Rapidly evolving data** ~ every **few months**
- **Speed - over 10^4 faster** than direct simulation
- The observed data is **low dimensional** (i.e. summary statistics)
- Database to train an adequate emulator $<$ one full inference

brightness_temp

Ts_box

xH_box

dNrec_box

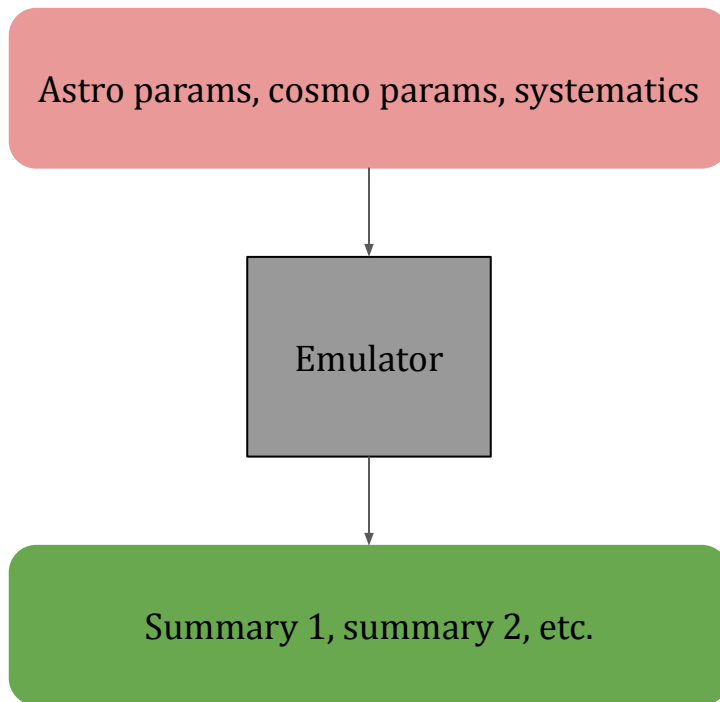
z_re_box

Gamma12_box

J_21_LW_box

density

Ideal Emulator



[See it here](#)

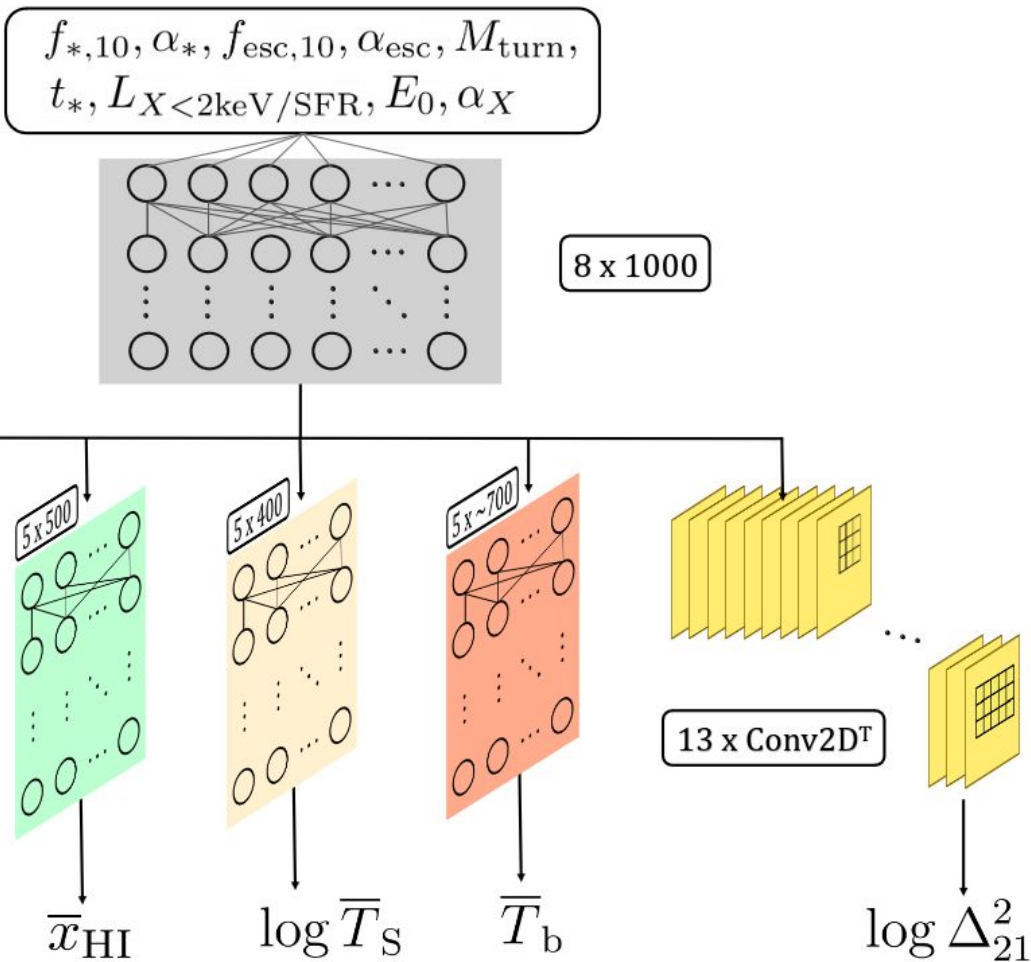
Summary Statistics

- $x_{\text{HI}}(\mathbf{z})$: Global fraction of neutral hydrogen
- $T_{\text{S}}(\mathbf{z})$: Global neutral IGM spin temperature $T_{\text{S}}^{-1} = \frac{T_{\gamma}^{-1} + x_{\alpha} T_{\alpha}^{-1} + x_{\text{C}} T_{\text{K}}^{-1}}{1 + x_{\alpha} + x_{\text{C}}}$
- $T_{\text{b}}(\mathbf{z})$: Global 21-cm brightness temperature [e.g. Bye+22, Bevins+21, Cohen+19]

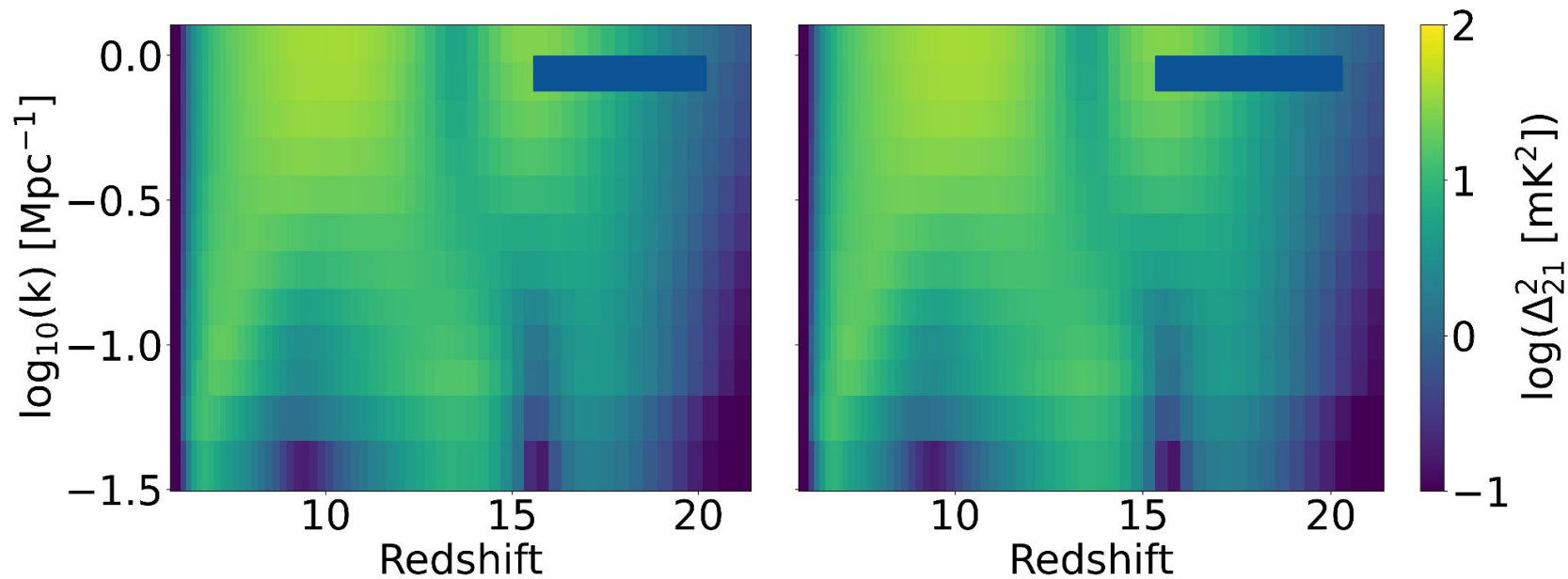
$$\delta T_{\text{b}} \approx 27 x_{\text{HI}} (1 + \delta_{\text{b}}) \left(\frac{\Omega_{\text{b}} h^2}{0.023} \right) \left(\frac{0.15}{\Omega_{\text{m}} h^2} \frac{1+z}{10} \right)^{1/2} \times \left(\frac{T_{\text{S}} - T_{\text{R}}}{T_{\text{S}}} \right) \left[\frac{\partial_{\text{r}} v_{\text{r}}}{(1+z)H(z)} \right] \text{mK}$$

- **21-cm power spectrum** (\mathbf{k}, \mathbf{z}): e.g. Kern+17, Schmit & Pritchard 18, Ghara+20, Mondal+21
- **UV luminosity function**: Source number density per magnitude vs z [Bouwens+15, 16]
- τ_{e} : Thomson scattering optical depth of CMB photons

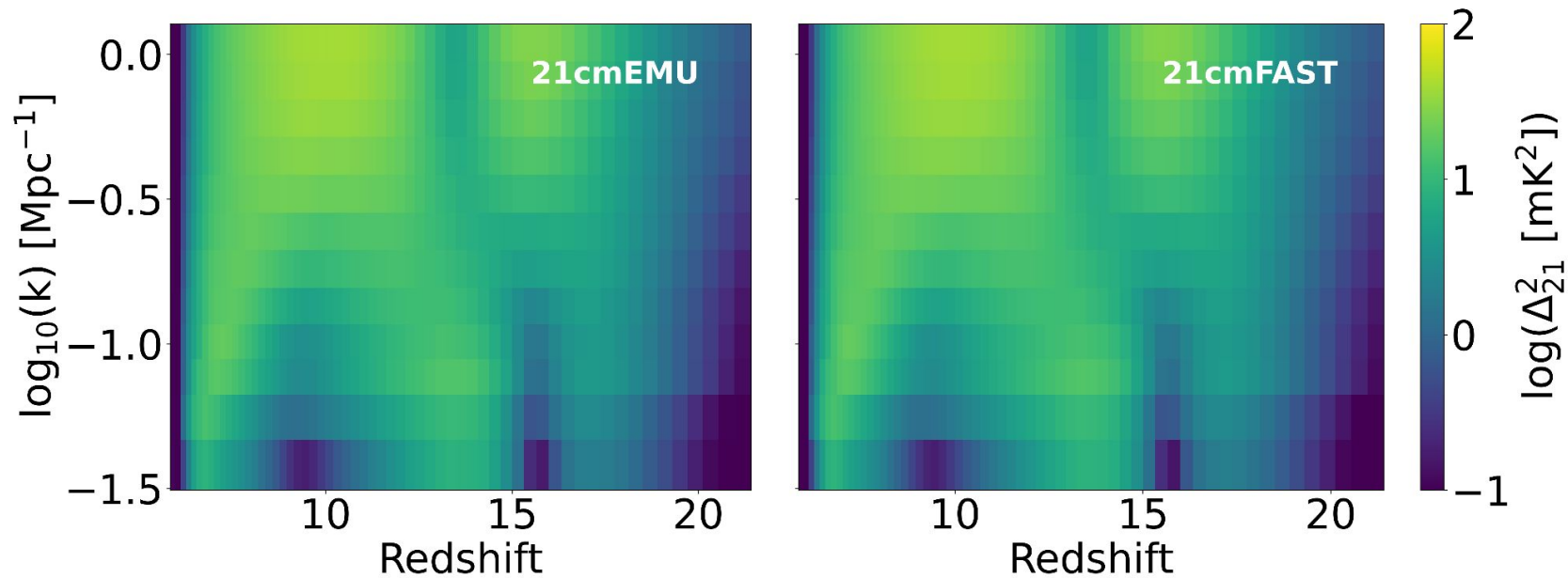
Emulator Architecture



Power Spectrum



Power Spectrum

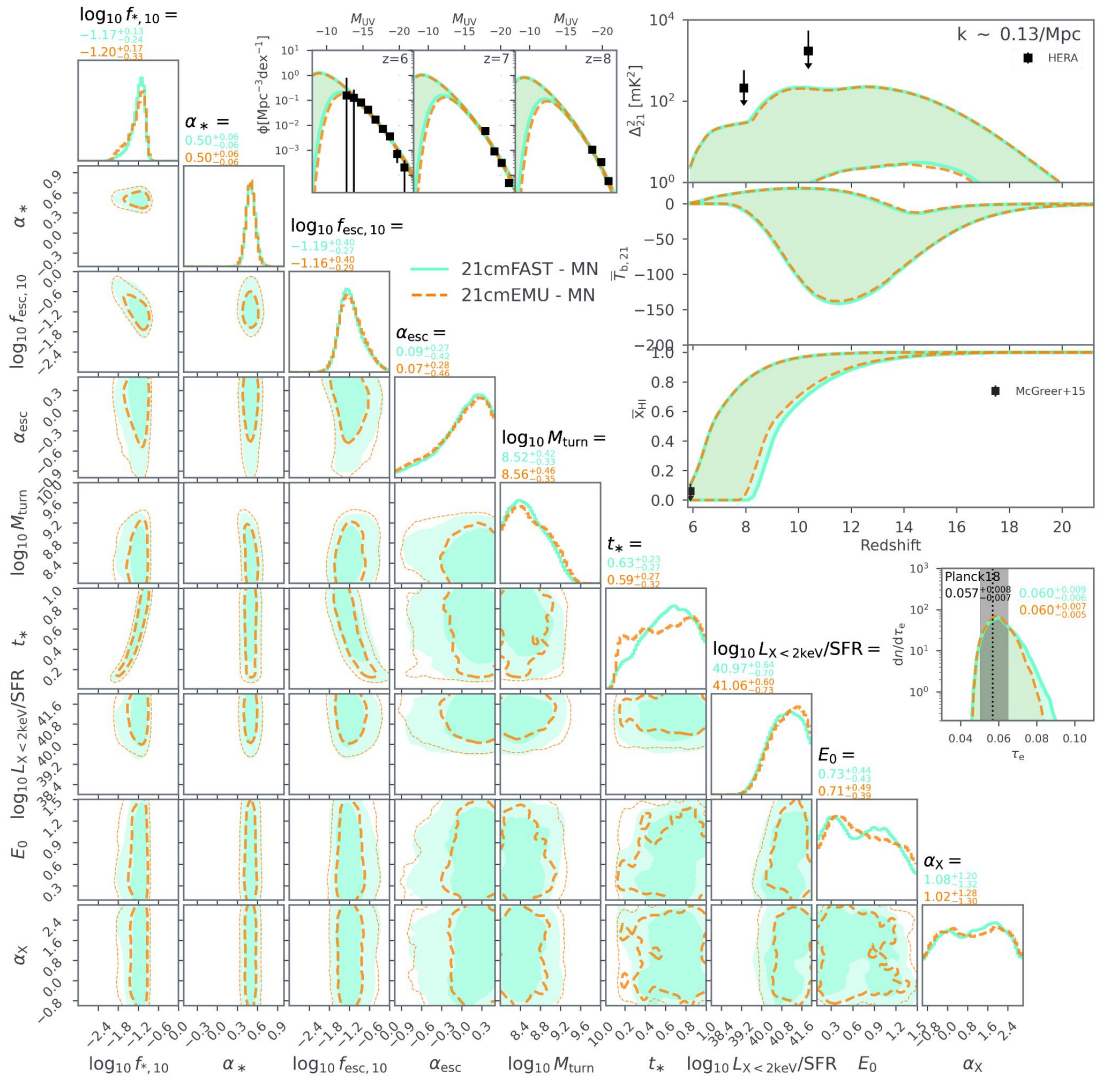


21cmEMU Performance

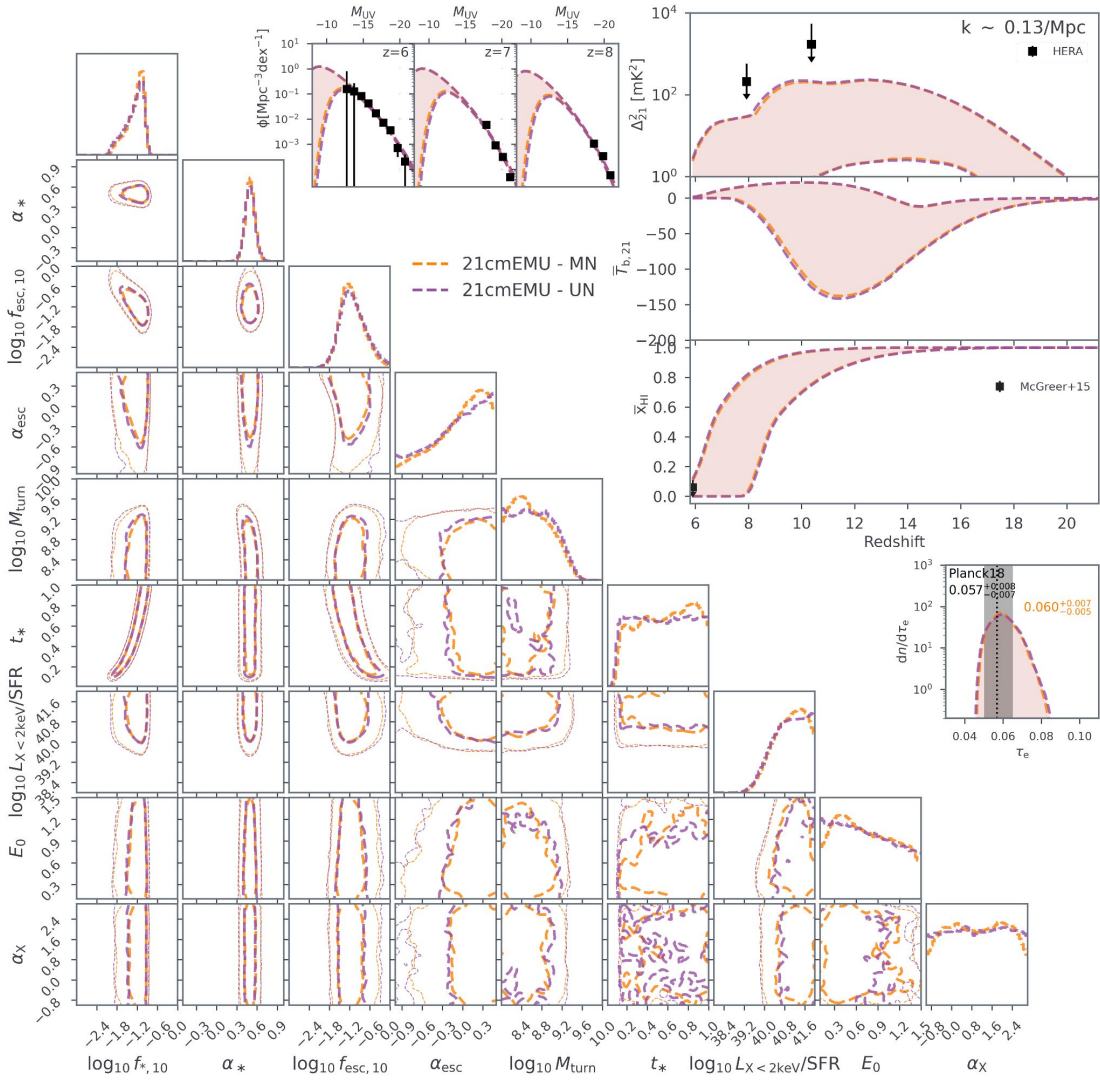
Summary	Median FE (%)	68% CL (%)
$\log \Delta_{21}^2$	0.55	2.4
\bar{T}_b	0.25	0.82
$\log \bar{T}_S$	0.032	0.13
\bar{x}_{HI}	0.0073	0.10
τ_e	0.11	0.26
$\log \phi$	0.50	2.1

Small errors, but do they impact the inference?

21cmEMU can reproduce
21cmFAST results.

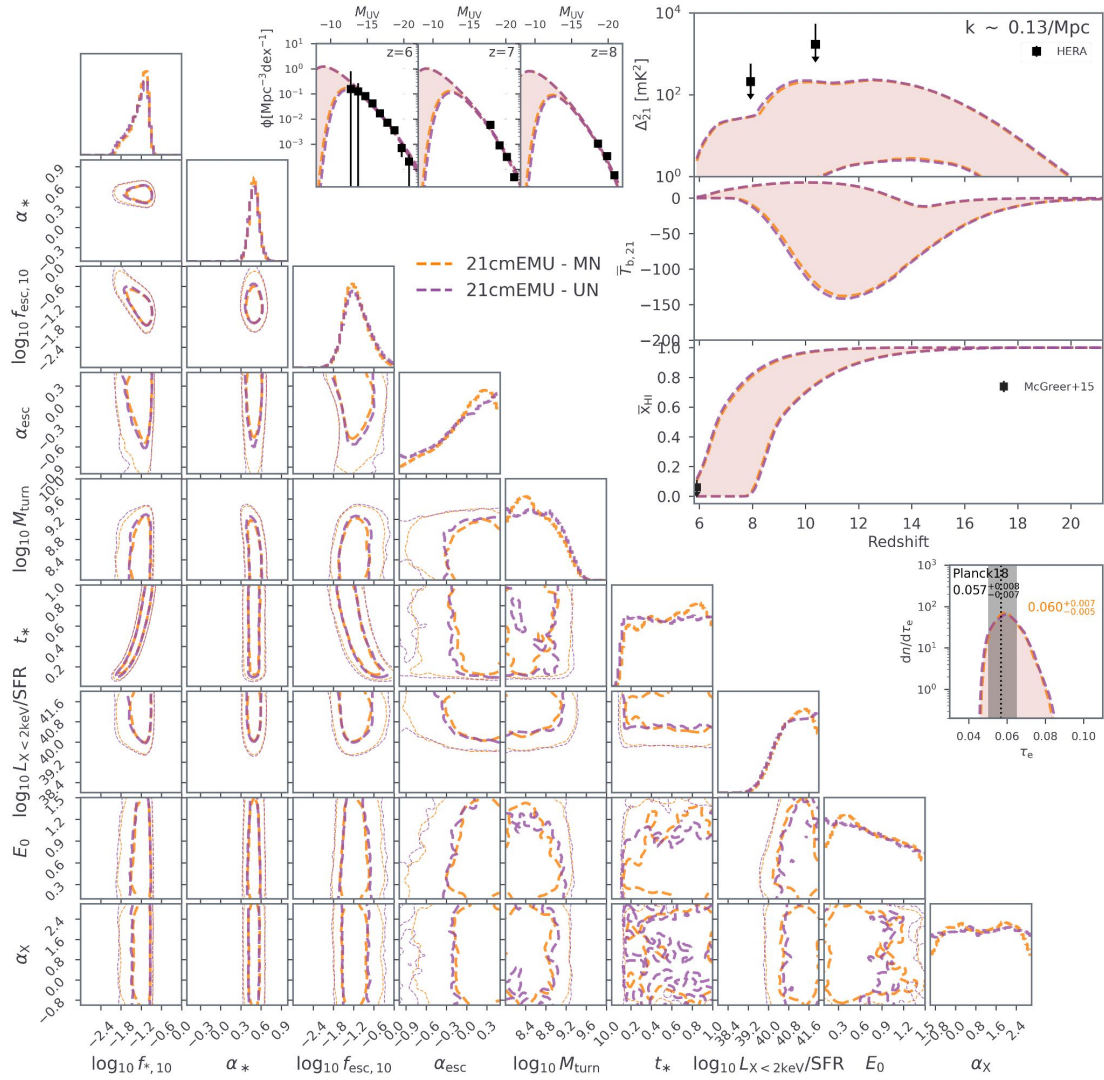


MultiNest Sampler vs UltraNest Sampler



MultiNest Sampler vs UltraNest Sampler

Difference between different
samplers > difference between
21cmEMU and 21cmFAST



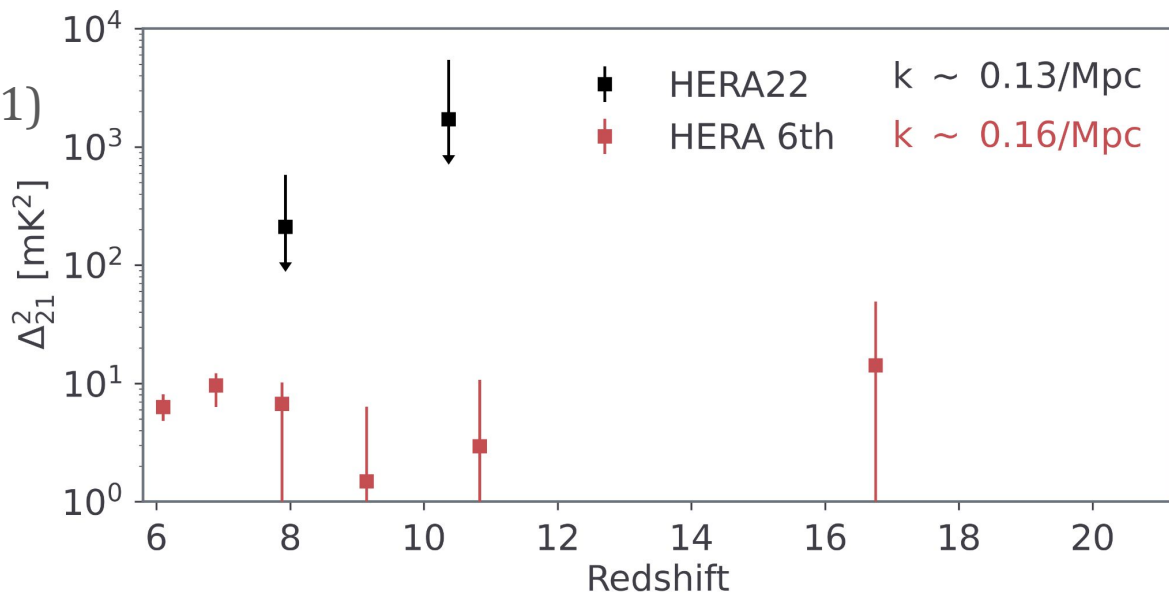
21cmEMU Application - HERA 6th Season Phase II Forecast

- HERA Phase II
 - 50-230 MHz (omitting the FM band, 90-110 MHz),
 - expanding coverage to Cosmic Dawn and late reionization with respect to Phase I (in HERA22).
- Known characteristics of observation:
 - **~1300 hours** of unflagged data over **~150 nights**, with an average of **~148 un-flagged antennas per night**
 - **HERA's most sensitive data release to date**

HERA22 (Phase I) vs HERA 6th Season (Phase II) Forecast

Mock data: EOS2021 (Muñoz+21)

**Sensitivity forecasted with
21cmSense** (Pober+14,15)



Likelihood Choice

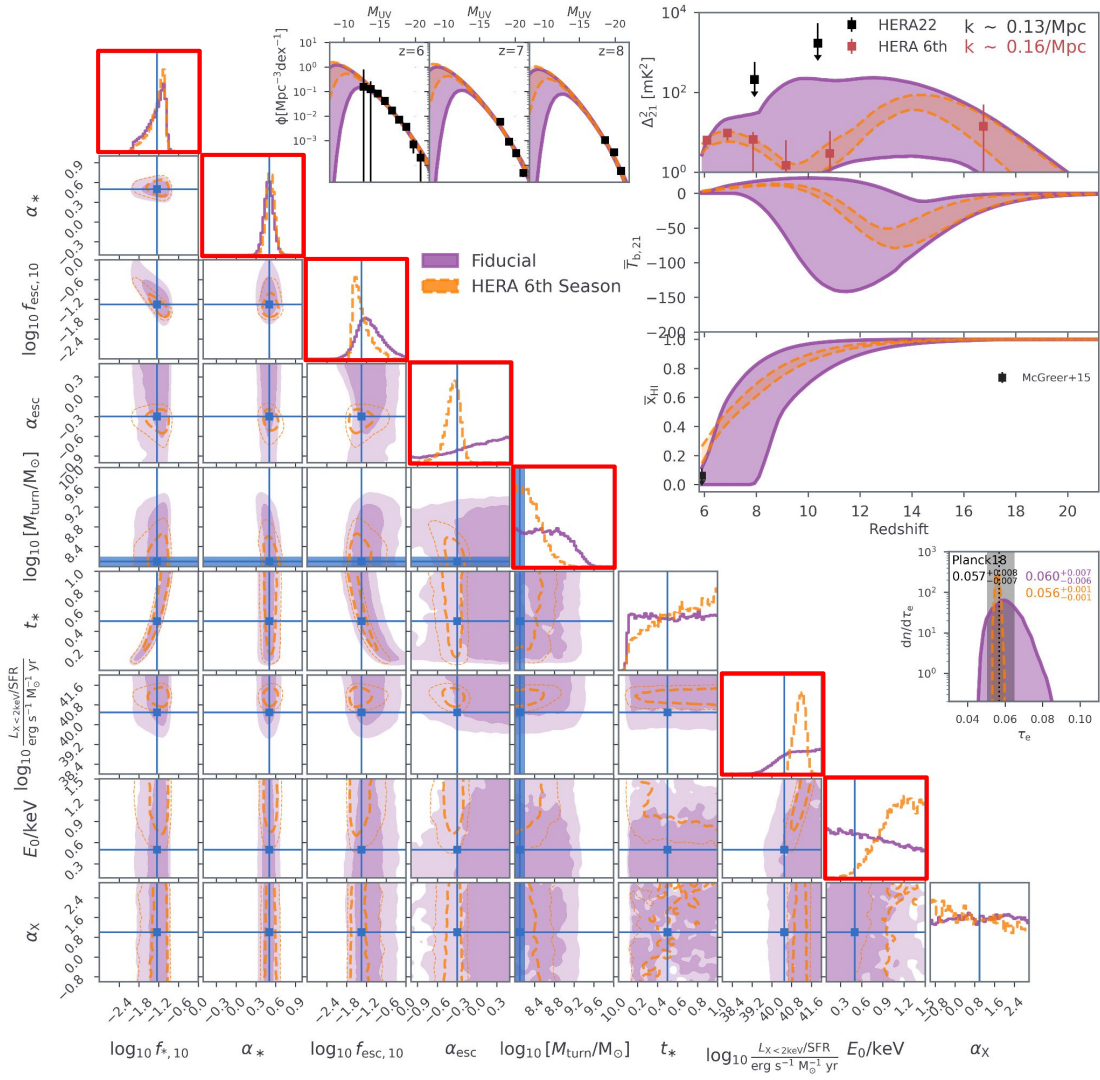
- Two-sided Gaussian (*detection*) rather than an error function (*upper limit*)

⇒ **Optimistic likelihood** since it assumes no residual systematics in the mock data

⇒ **(effectively) tighter prior on systematics**

Forecast for HERA Phase II 6th-Season Observations

New HERA data + tighter prior on systematics significantly improve the constraints for almost all astrophysical parameters



Conclusions

- **Goal: Emulate summaries required for inference using 21cmFAST data**
 - Emulate: **PS, T_b , T_s , $x\text{HI} + \tau_e$ and UV LF**
 - **FE 68% CL $\lesssim 2\%$ for all quantities**
 - This error is **much smaller than expected instrument error**
 - Major improvement in runtime: **$\sim\text{ms}$ vs $\sim\text{hr}$ per parameter combination $\Rightarrow \sim 10\text{k x faster}$**
- **Application:**
 - Inference with HERA 6th season **somewhat optimistic** forecast
 - **Upcoming HERA data dramatically improves our understanding of the EoR: e.g. at $z \sim 8$:**
 - **Infer $x\text{HI}$ to within ± 0.05 (95% C.I.): factor of ≥ 7 better than current limits**
 - **Infer Δ_{21}^2 to within $\pm 1.29 \text{ mK}^2$ (95% C.I.): factor of ≥ 11 better than current limits**
- **Limitations: including new physics** e.g. minihalos will require re-running 21cmFAST + retraining

Now available!!

pip install py21cmemu

<https://github.com/21cmfast/21cmemu>

ArXiv 2309.05697

