

Gravitational theory and the tidal tails of open star clusters

"From star clusters to field populations:
survived, destroyed and migrated clusters"
Villa Galileo
Florence
Nov. 20-23, 2023

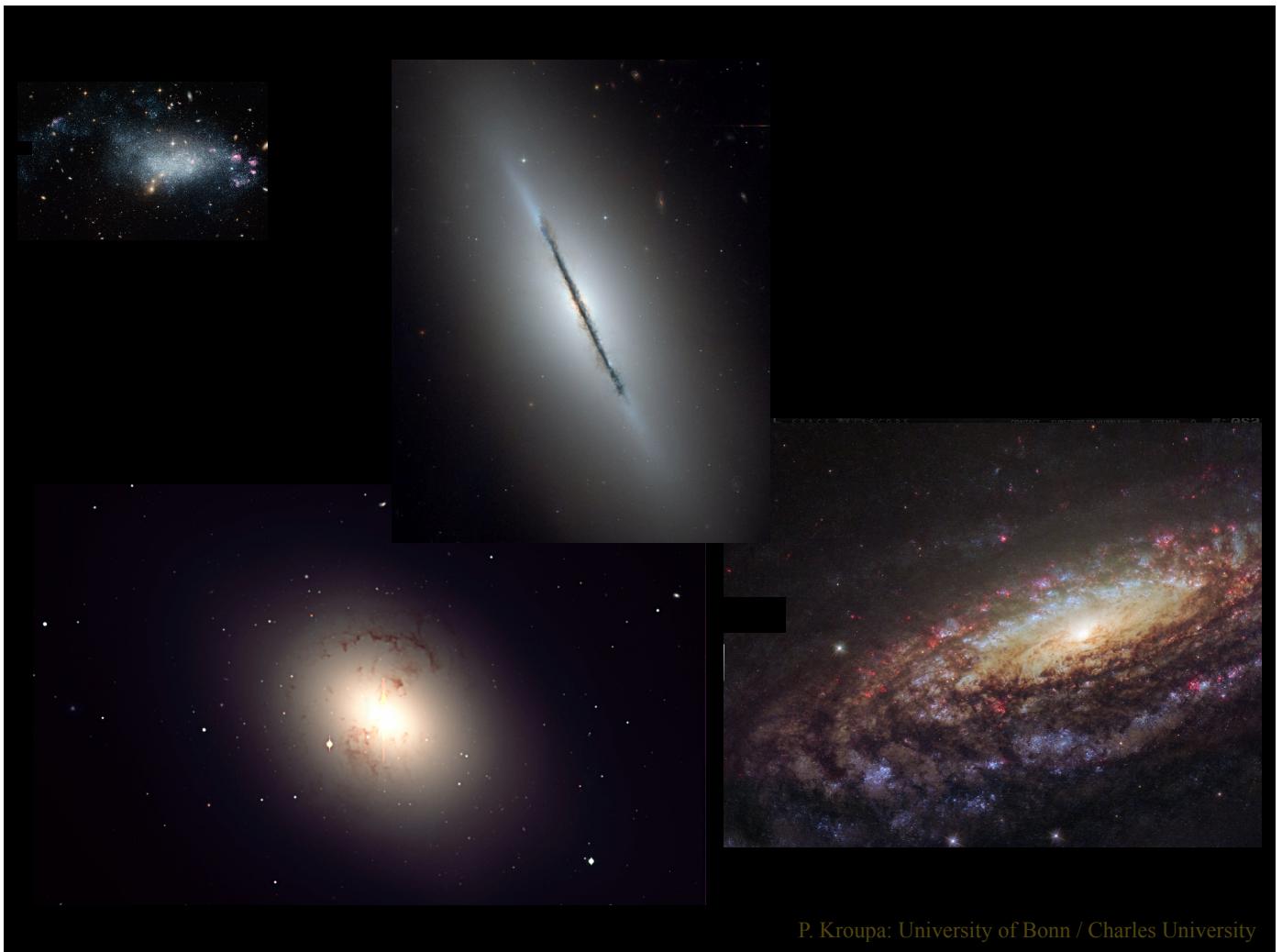
Pavel Kroupa
University of Bonn
Charles University in Prague

<http://www.astro.uni-bonn.de/~pavel>

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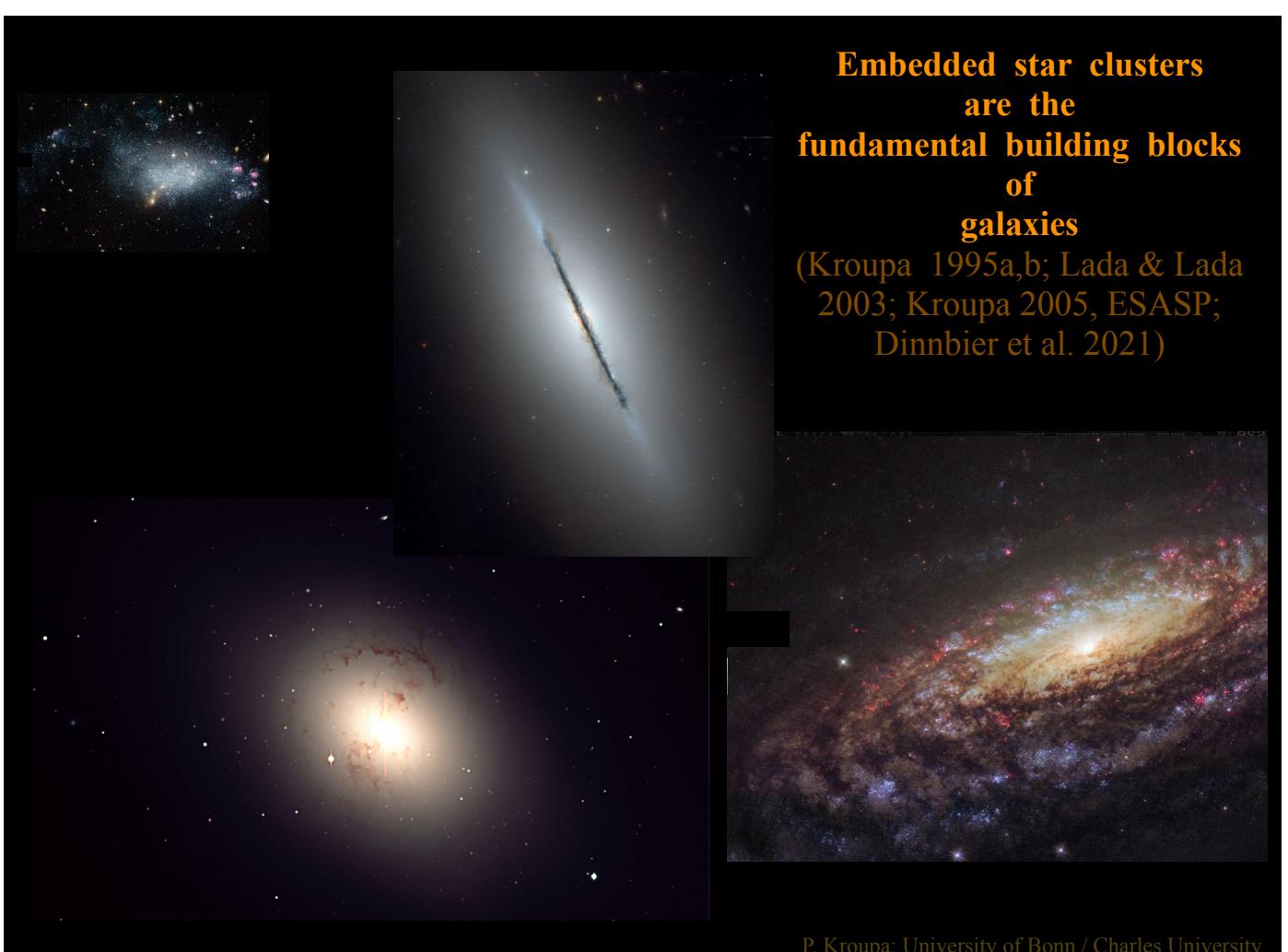
Problem :
calculate
the stellar and binary
populations
in
galaxies of different types

Are they statistically the same ?



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**Embedded star clusters
are the
fundamental building blocks
of
galaxies**
(Kroupa 1995a,b; Lada & Lada
2003; Kroupa 2005, ESASP;
Dinnbier et al. 2021)



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The Galileo Conjecture

Stars form in
embedded clusters,

some evolve to

open clusters

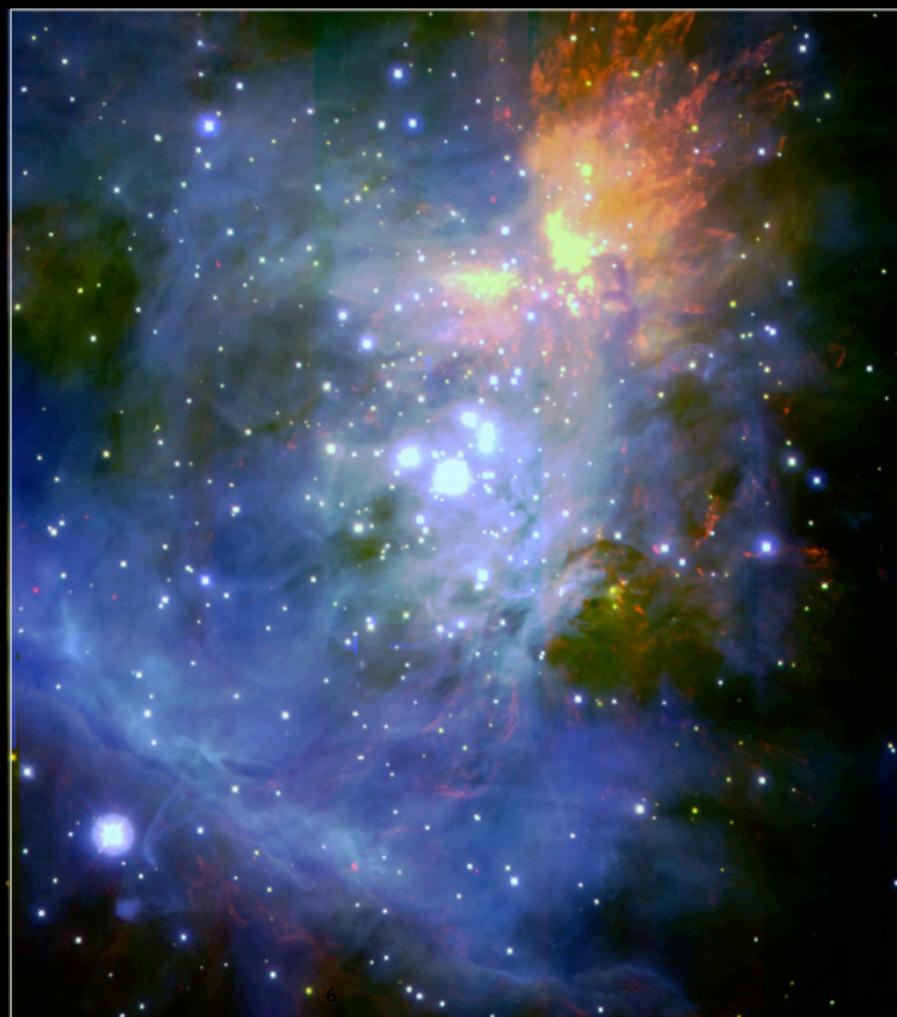
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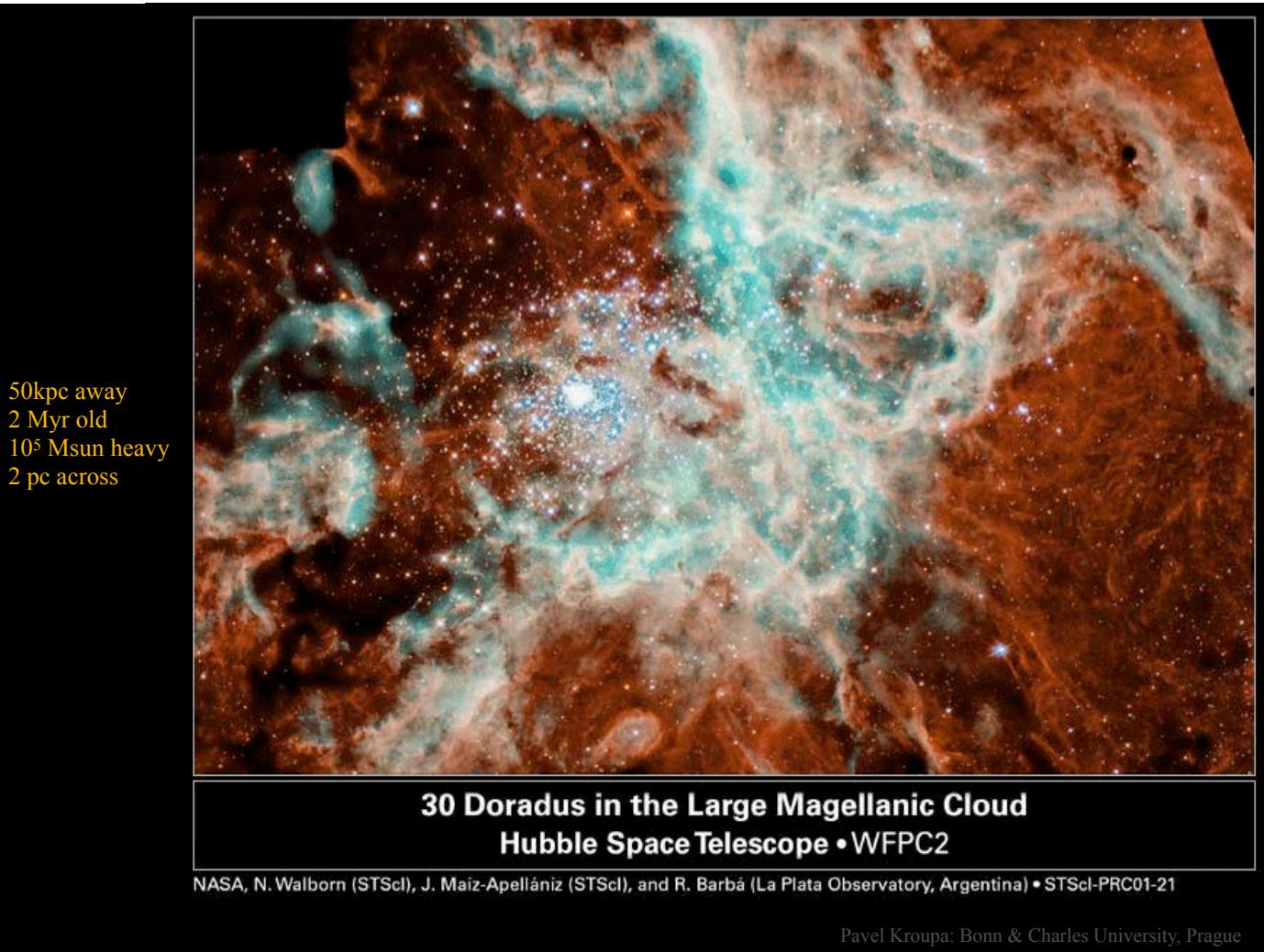
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Example:

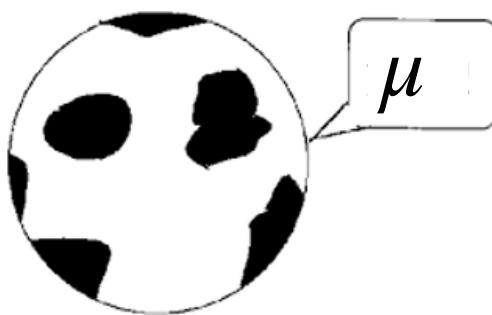
The Orion
Nebula
Cluster

0.5kpc away
1 Myr old
 10^3 Msun heavy
2 pc across





Here we entertain the Alison-Sills-Approximation (ASA):

The  model

The Galileo conjecture : all stars are born in embedded star clusters

The calculation is thus adding-up what each embedded star cluster provides
e.g. the total mass in all stars formed in the time δt :

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$$\xi_{\text{ecl}}(M_{\text{ecl}}) dM_{\text{ecl}} \quad \begin{array}{l} \# \text{ of embedded clusters} \\ \text{with stellar mass} \\ M_{\text{ecl}} \in [M_{\text{ecl}}, M_{\text{ecl}} + dM_{\text{ecl}}] \end{array}$$

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$$M_{\text{ecl}} \xi_{\text{ecl}}(M_{\text{ecl}}) dM_{\text{ecl}} \quad \begin{array}{l} \text{stellar mass} \\ \text{in these embedded clusters} \end{array}$$

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$$M_{\text{tot},\delta t} = \int_{M_{\text{ecl,min}}}^{M_{\text{ecl,max}}(SFR)} M_{\text{ecl}} \xi_{\text{ecl}}(M_{\text{ecl}}) dM_{\text{ecl}}$$

All stellar mass formed
in time δt

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More generally, for a "product" coming out of the forming population of embedded clusters :

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More generally, for a "product" coming out of the forming population of embedded clusters :

$$\Omega_{\text{dyn}}^{M_{\text{ecl}}, r_h}(t_{\text{freeze}})[D_{\text{in}}] \xi_{\text{ecl}}(M_{\text{ecl}}) dM_{\text{ecl}}$$

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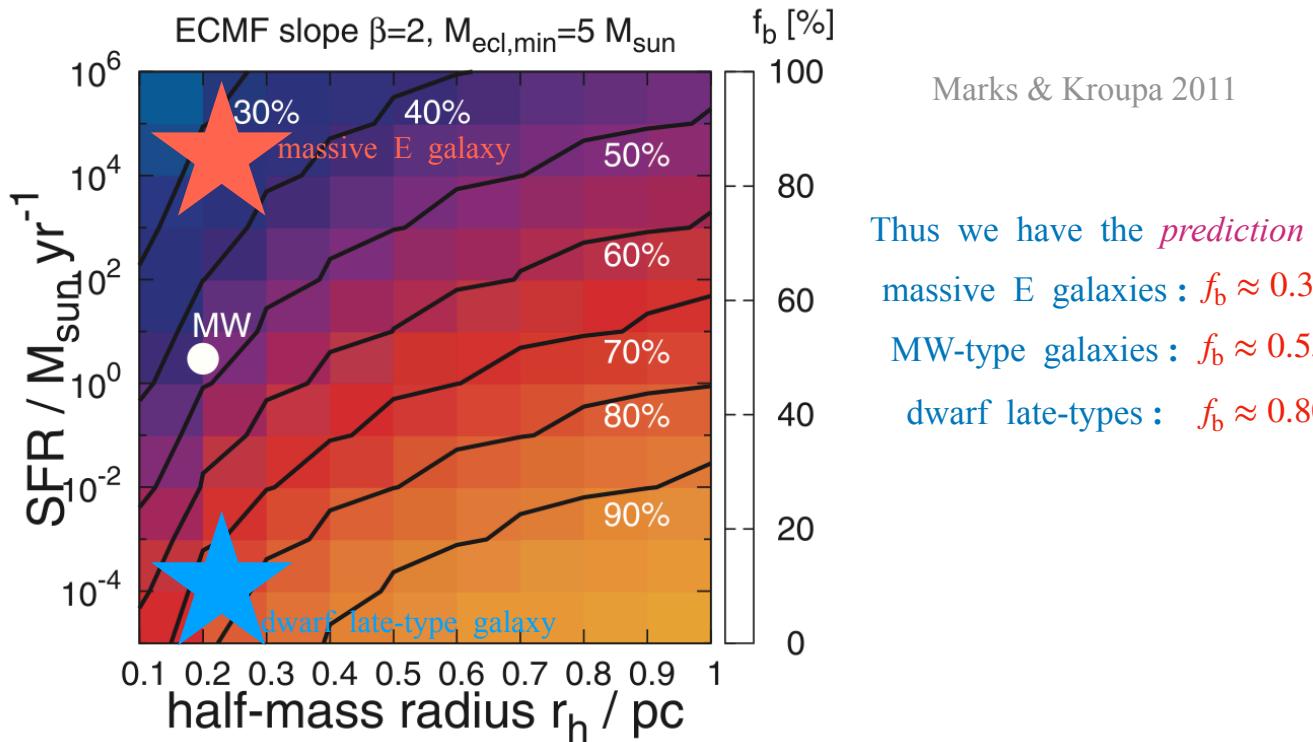
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The time δt is the life-time of molecular clouds, $\delta t \approx 10 \text{ Myr}$

Weidner et al. 2004; Schulz et al. 2015, 2016

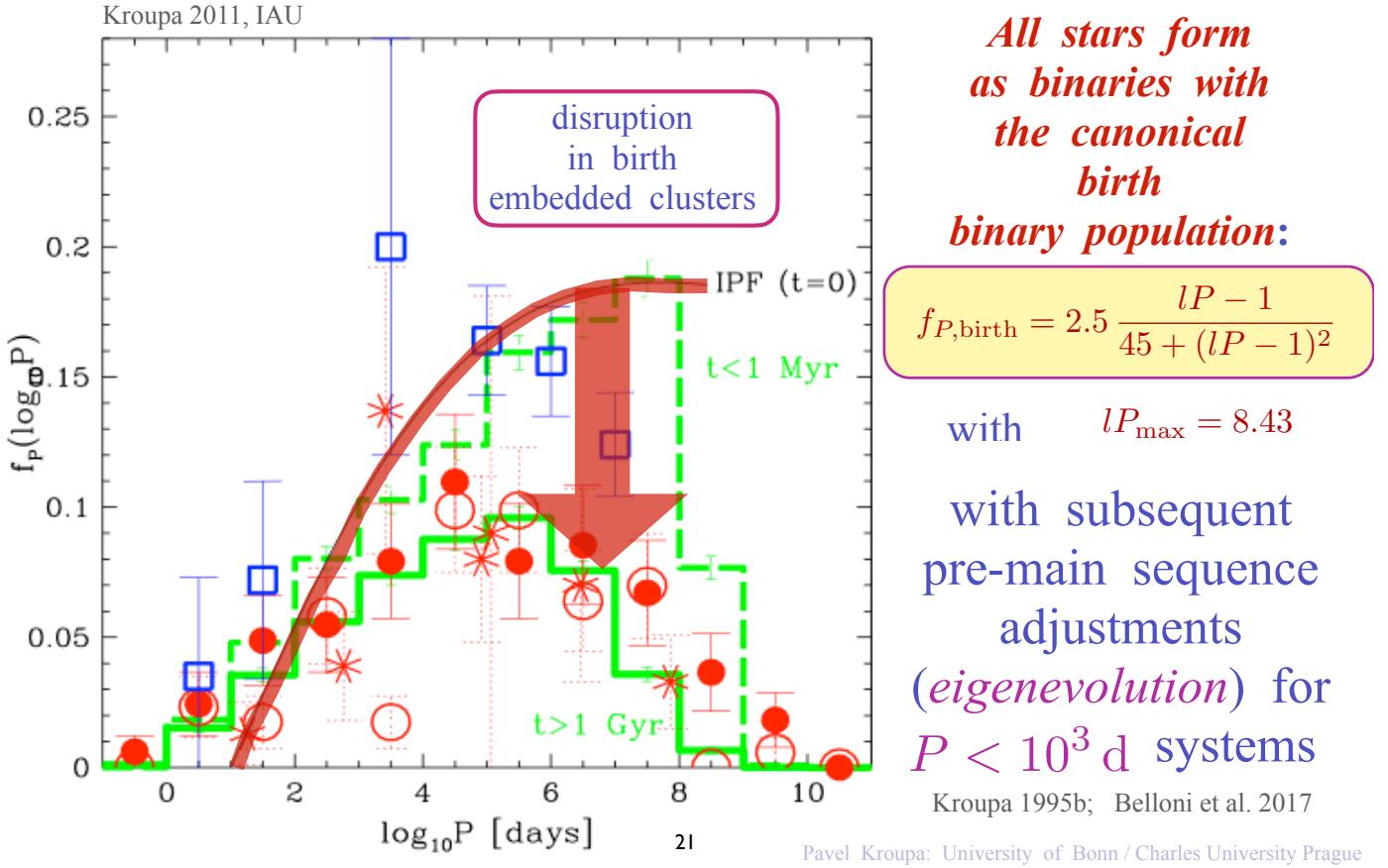
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Period-distribution functions of pre-main sequence binaries and of field stars are unified, as are mass-ratio and eccentricity distributions

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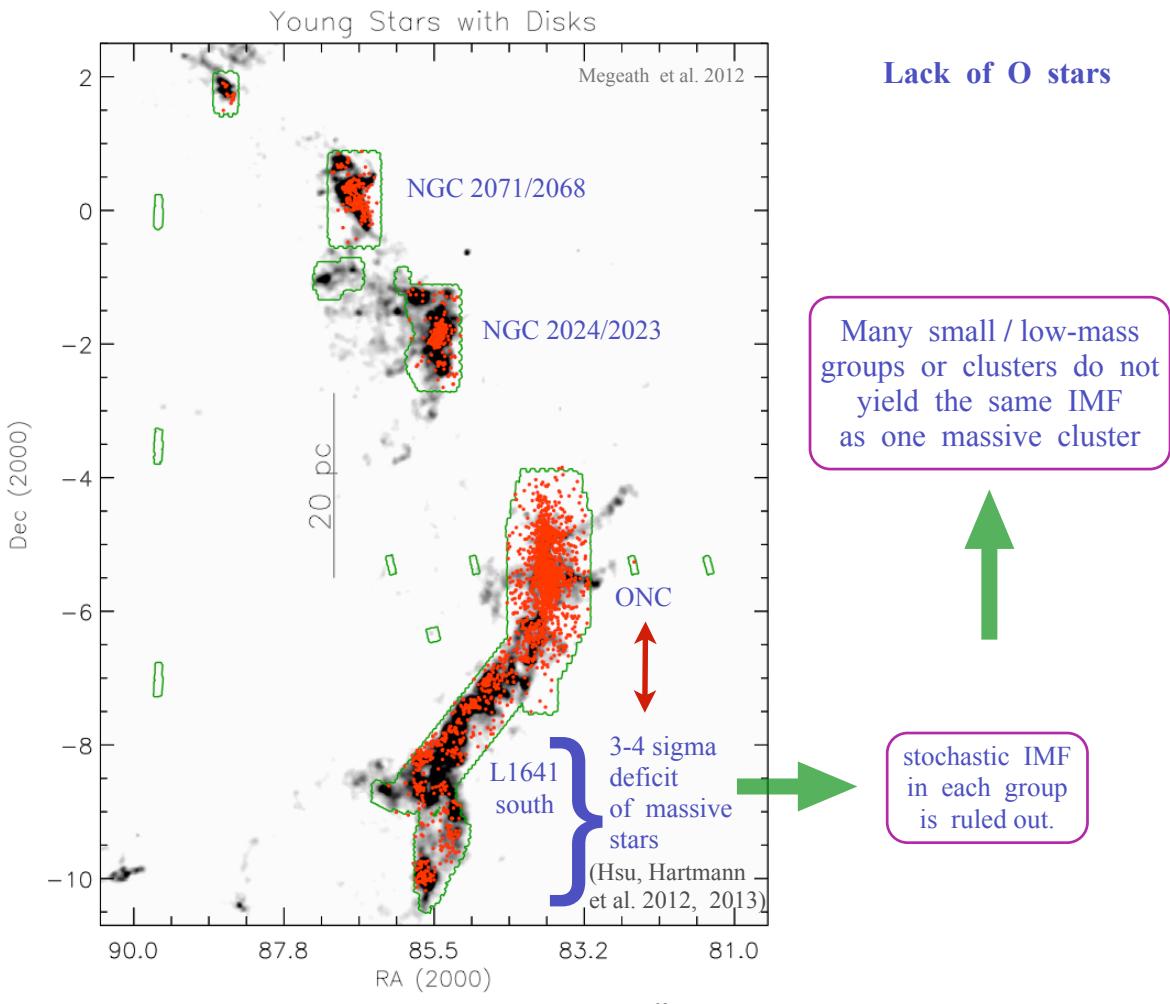
To do these calculations,
we need the distribution functions defining a stellar population at birth

$$D_{GF,\delta t}^{r_h} = \int_{M_{\text{ecl,min}}}^{M_{\text{ecl,max}}(SFR)} \Omega_{\text{dyn}}^{M_{\text{ecl}}, r_h}(t_{\text{freeze}})[D_{\text{in}}] \xi_{\text{ecl}}(M_{\text{ecl}}) dM_{\text{ecl}}$$

IMF = IMF(Z, rho)



Marks et al. 2012



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The $m_{\max}(M_{\text{ecl}})$ relation

Weidner & Kroupa 2005, 2006; Weidner et al. 2010

Yan, Jerabkova et al. 2023

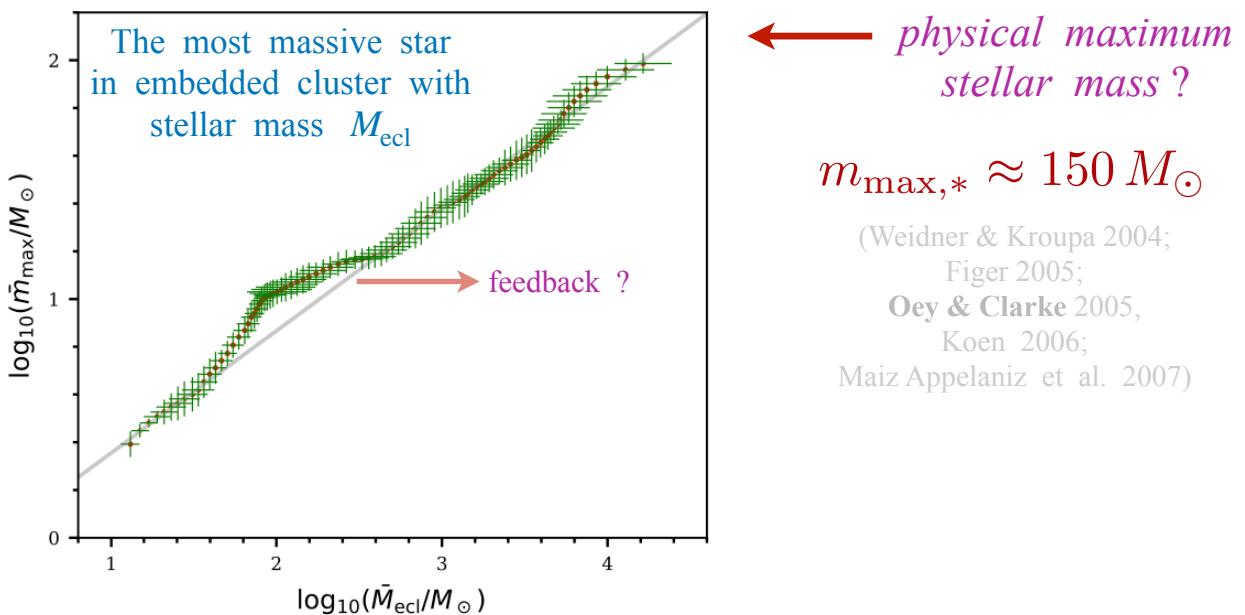


Fig. 6. Average position of the observational data for the groups of ten nearest points in the m_{\max} - M_{ecl} relation. The linear grey line highlights that the clusters with a mass of between $10^{1.8} M_{\odot} = 63 M_{\odot}$ and $10^{2.6} M_{\odot} = 400 M_{\odot}$ depart from the linear relation.

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Initial binary-star
distribution
functions
(periods, mass ratios, eccentricities)

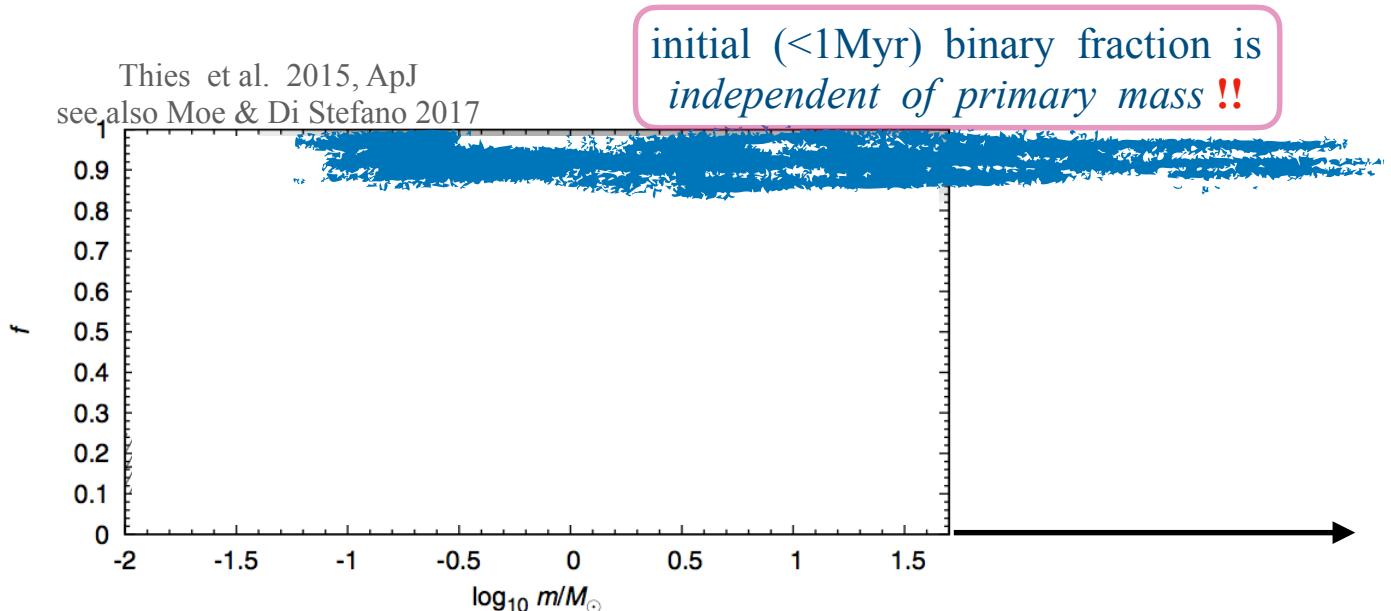
IMF = IMF(Z, rho)
Marks et al. 2012

Kroupa 1995a,b;
Belloni et al.

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The binary fraction in dependence of primary mass



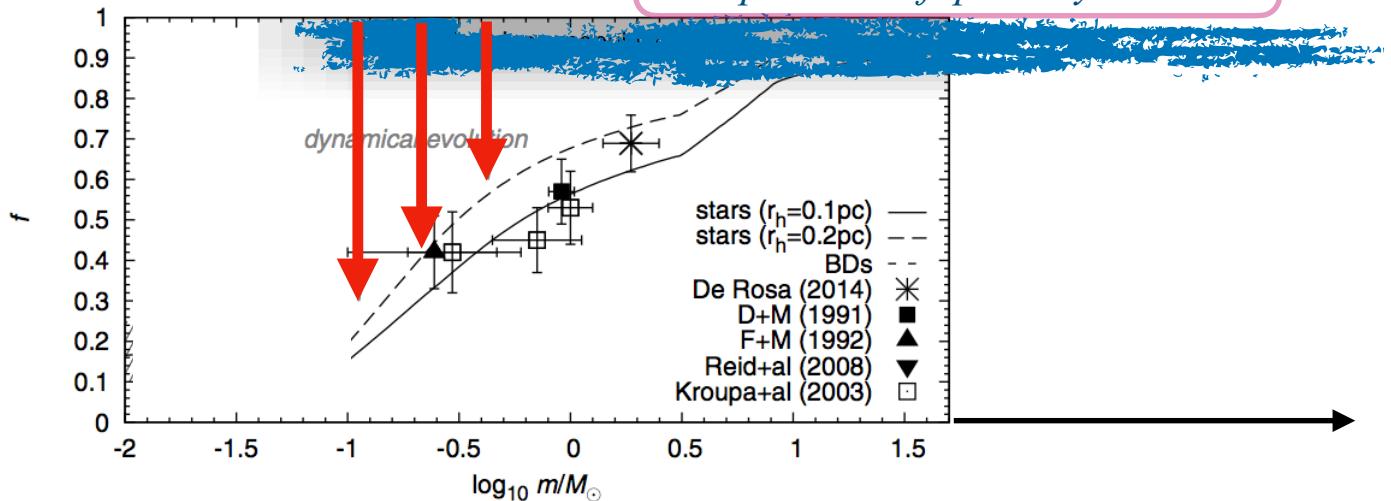
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The binary fraction in dependence of primary mass

Thies et al. 2015, ApJ

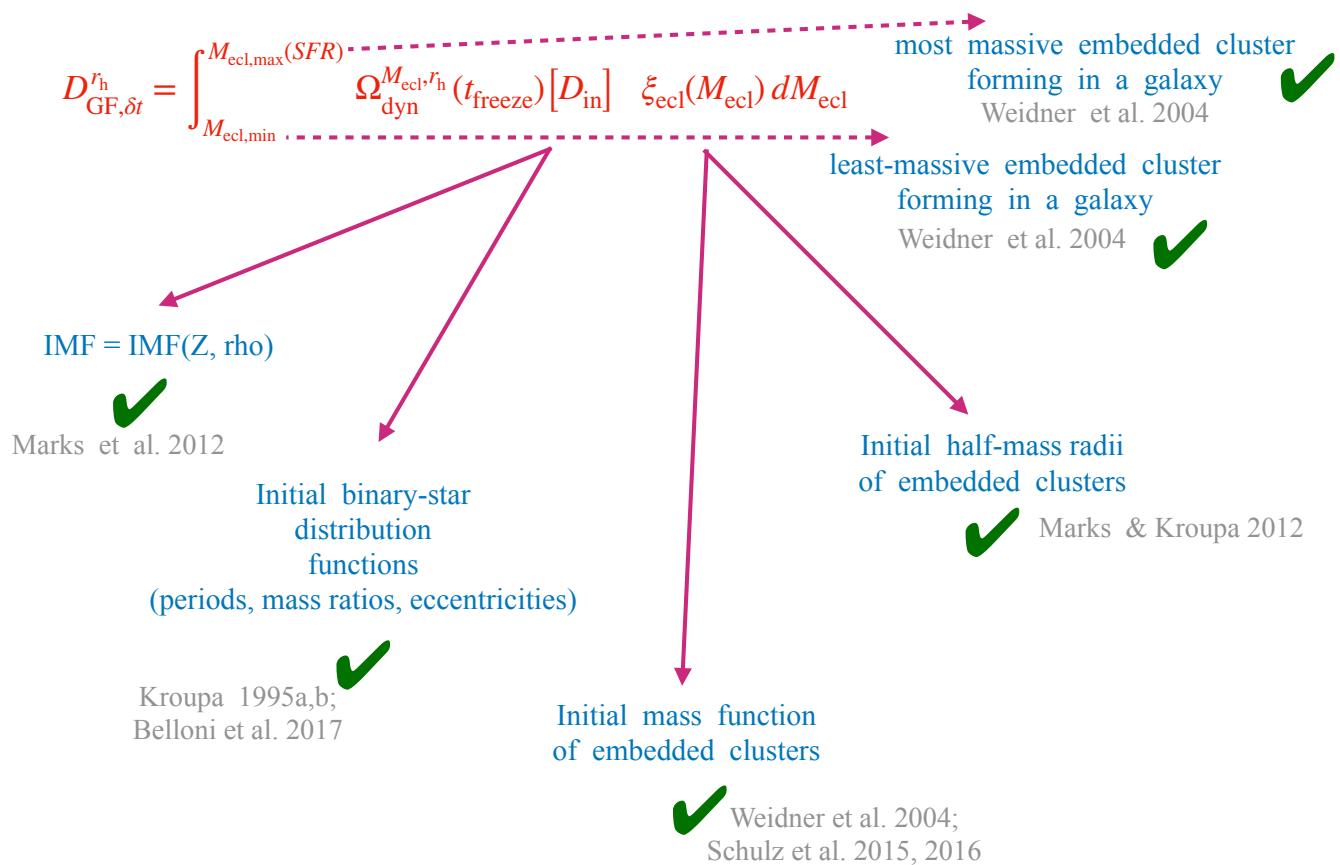
initial (<1Myr) binary fraction is
independent of primary mass !!



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To do these calculations,
we need the distribution functions defining a stellar population at birth



The embedded clusters,
must expand significantly

to reach the radii of
open clusters

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By fitting Nbody models to well-observed star clusters,
universal numbers emerge

		M_{ecl}
Small embedded clusters in Taurus-Aurigae	Kroupa et al. 2003	$\approx 10 M_{\odot}$
Orion Nebula Cluster (ONC) and Pleiades	Kroupa et al. 2001	$\approx 10^3 M_{\odot}$
NGC 3603	Banerjee & Kroupa 2013; 2014; 2015; 2017; 2018	$\approx 10^4 M_{\odot}$
R136	Banerjee & Kroupa 2013; 2014; 2015; 2017; 2018	$\approx 10^5 M_{\odot}$

$$\tau_{\text{gas}} \approx \frac{r_h}{10\text{pc}/\text{Myr}}$$

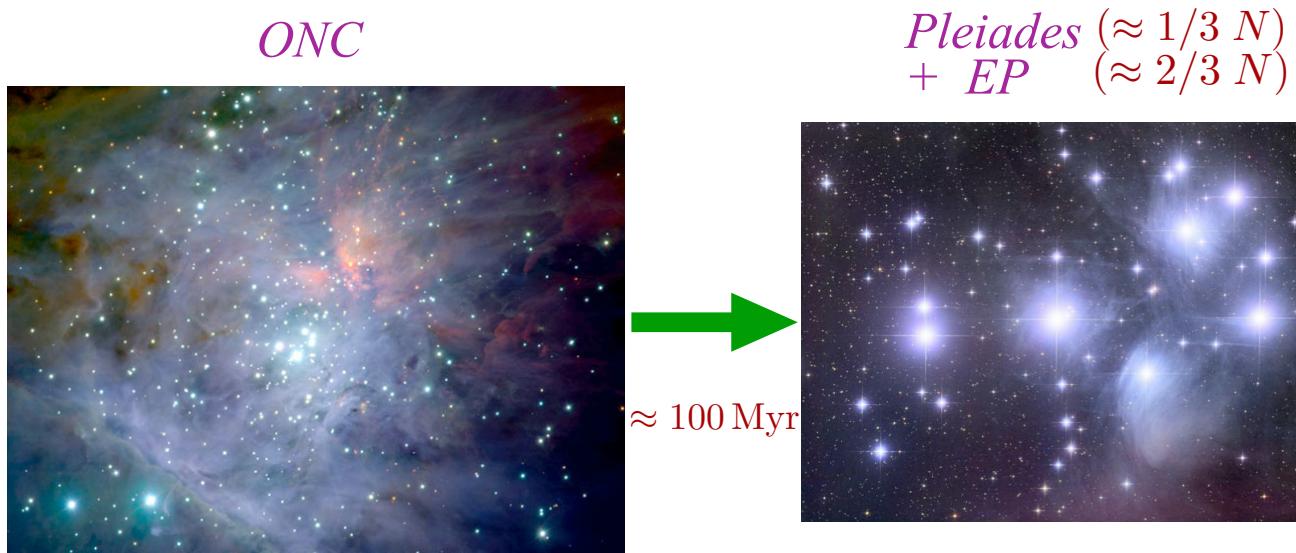
gas flows out at sound speed

$$\Delta\tau_{\text{gas}} \approx 0.6 \text{ Myr}$$

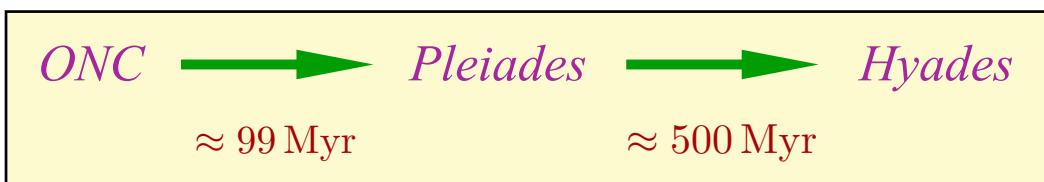
embedded + UCHII region lifetime

$$SFE \approx \frac{1}{3}$$

star-formation efficiency in embedded cluster



We thus have



(Kroupa, Aarseth & Hurley 2001; Portegies Zwart et al. 2001; Kroupa 2005)

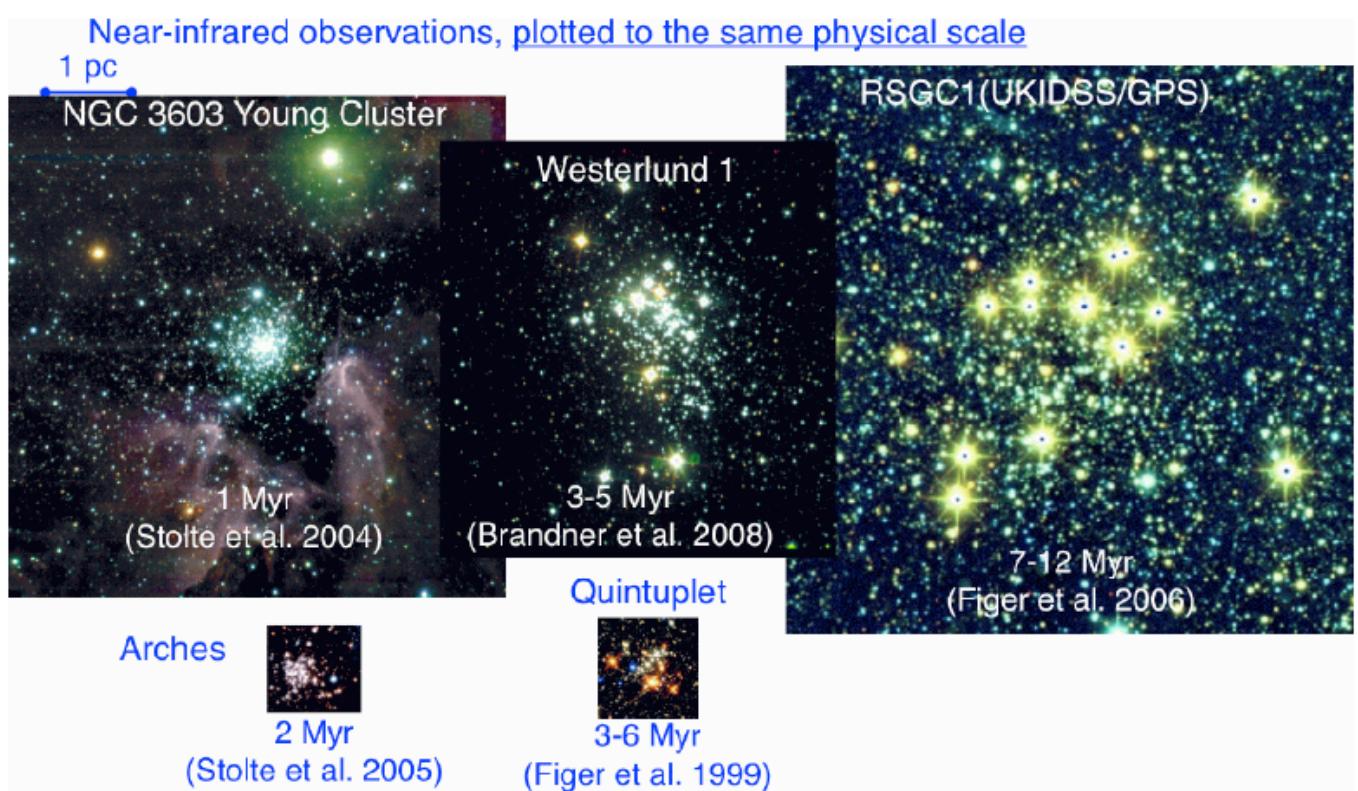
with an *inflation* in R .

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Brandner, astro-ph/0803.1974

Banerjee & Kroupa 2017

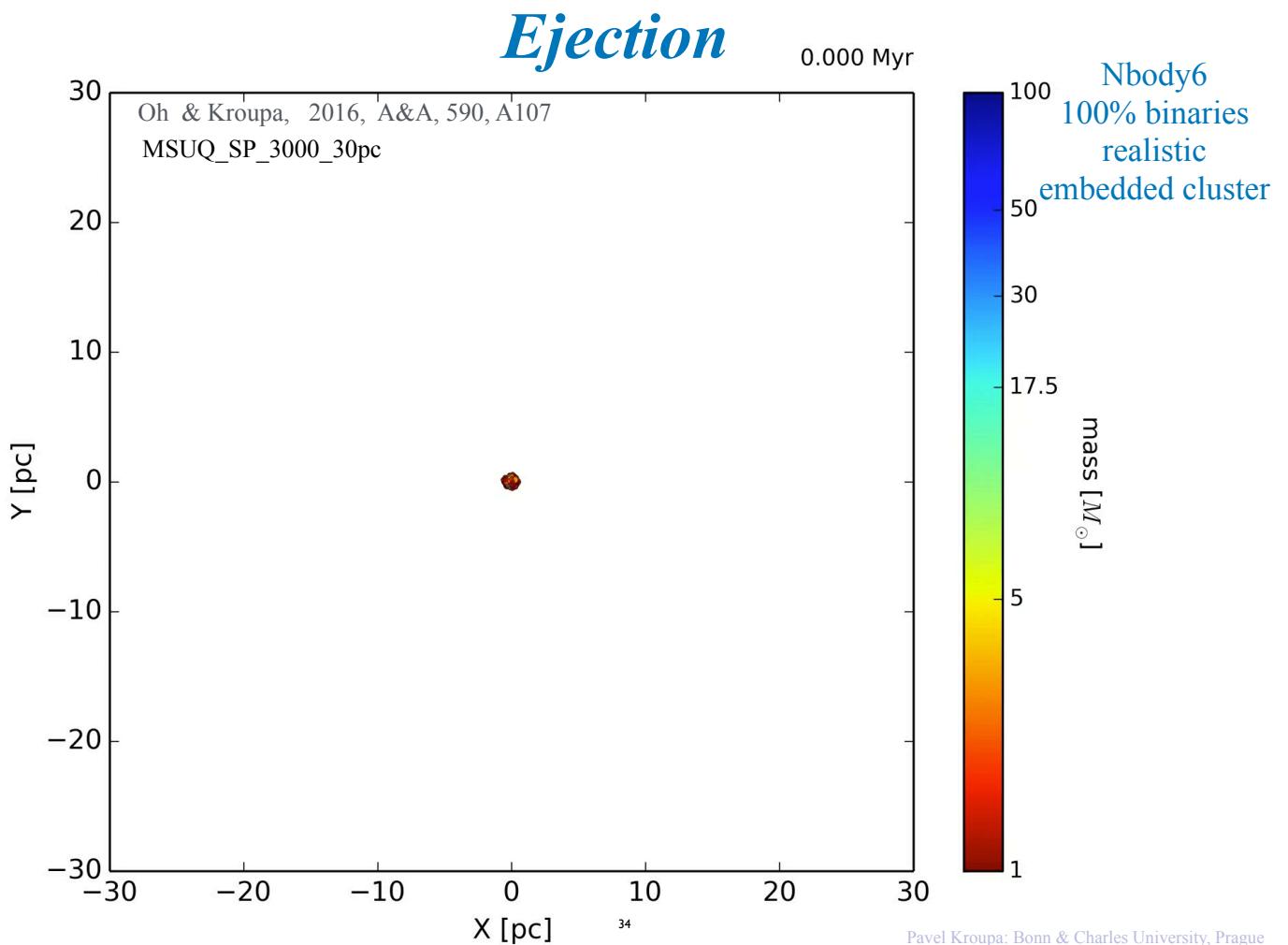


$$\dot{M}_{\text{cluster}} < 0$$

How do star clusters
lose their stars ?

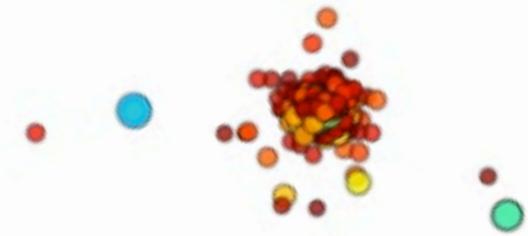
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Ejection

Oh & Kroupa, 2016, A&A, 590, A107
MSUQ_SP_3000_30pc Nbody models



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Monoceros R2 cluster (Carpenter et al. 1997, AJ 114, 198)



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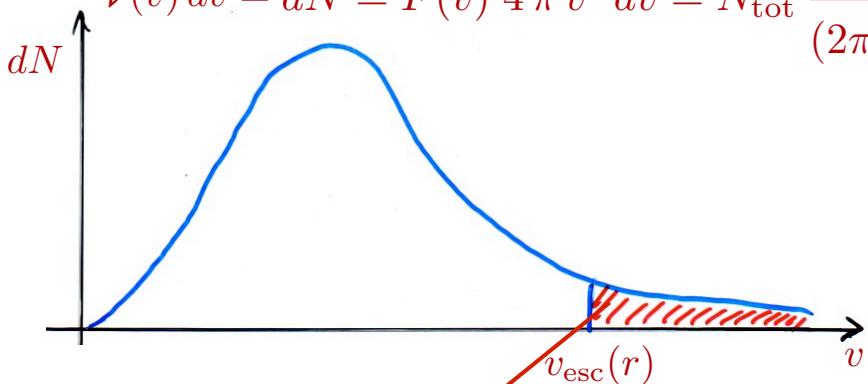
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Evaporation

Assume, for simplicity : the cluster consists of single stars of equal mass m .

At a given radius r in the cluster the stars have, approximately, a *Maxwell-Boltzmann* distribution of speeds :

$$\mathcal{V}(v) dv = dN = F(v) 4\pi v^2 dv = N_{\text{tot}} \frac{1}{(2\pi\sigma^2)^{\frac{3}{2}}} e^{-\frac{v^2}{2\sigma^2}} 4\pi v^2 dv$$



$$\frac{dM_{\text{cl}}}{dt}(t) = m \frac{dN}{dt}(t)$$

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Evaporated stars
leave their
open clusters
through
tidal tails

New method developed by Tereza Jerabkova in 2021
allowing *the tidal tails of open clusters* to be mapped
to their tips.

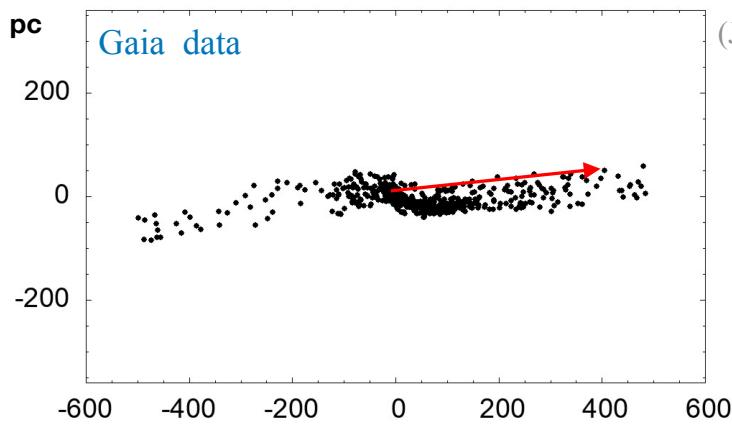
The Jerabkova Compact Convergent Point (CCP) method.

(Jerabkova et al. 2021)

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https://www.cosmos.esa.int/web/gaia/iow_20221026



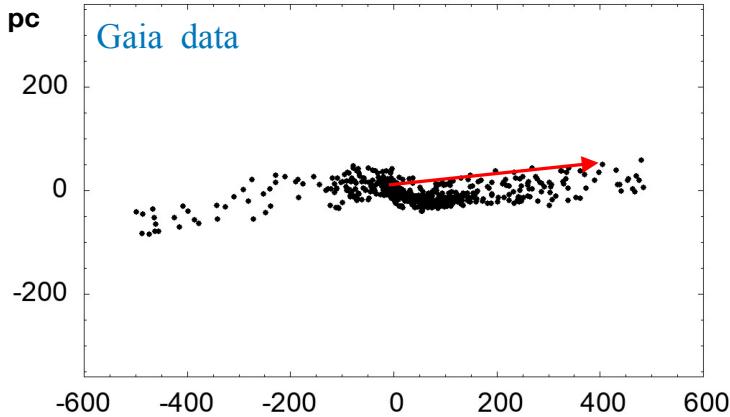
(Jerabkova et al. 2021)

Hyades

(Kroupa, Jerabkova et al. 2022)

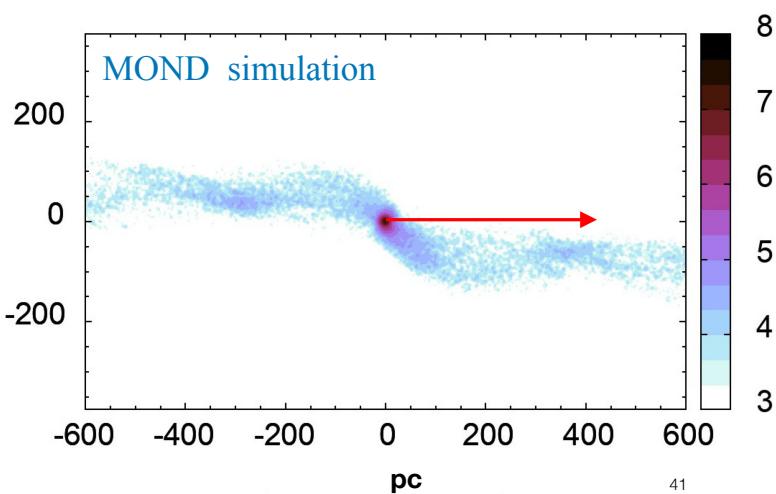
The asymmetry in
number of stars
between leading and trailing tail
is a **6.5sigma** deviation
from Newtonian predictions.

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Hyades

(Kroupa, Jerabkova et al. 2022)



The asymmetry in number of stars between leading and trailing tail is a 6.5sigma deviation from Newtonian predictions.



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Evaporation in Newtonian and Milgromian gravitation



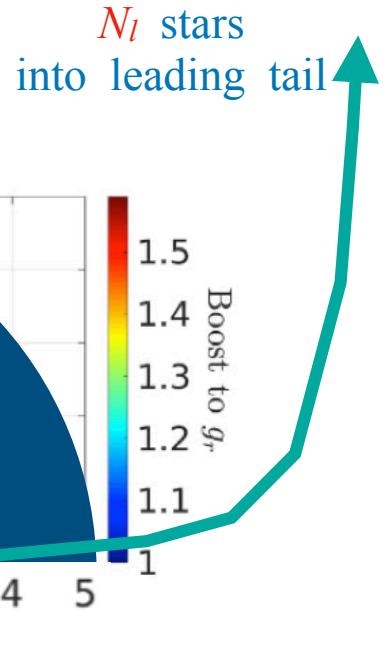
(Kroupa, Jerabkova et al. 2022)

open star cluster

MOND radius :

$$r_M = \left(\frac{G M_{oc}}{a_0} \right)^{\frac{1}{2}}$$

Newtonian case

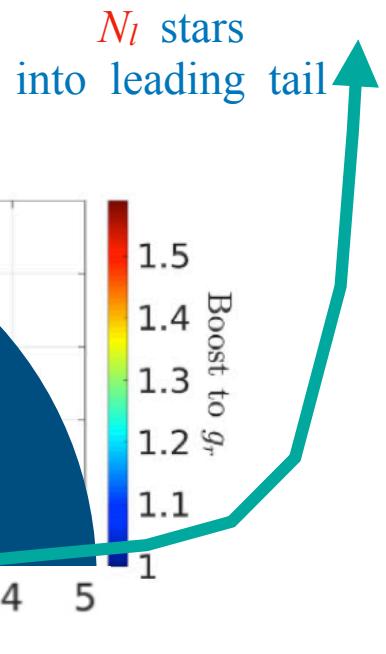


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Newtonian case



MOND radius :

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$$N_l = N_t$$

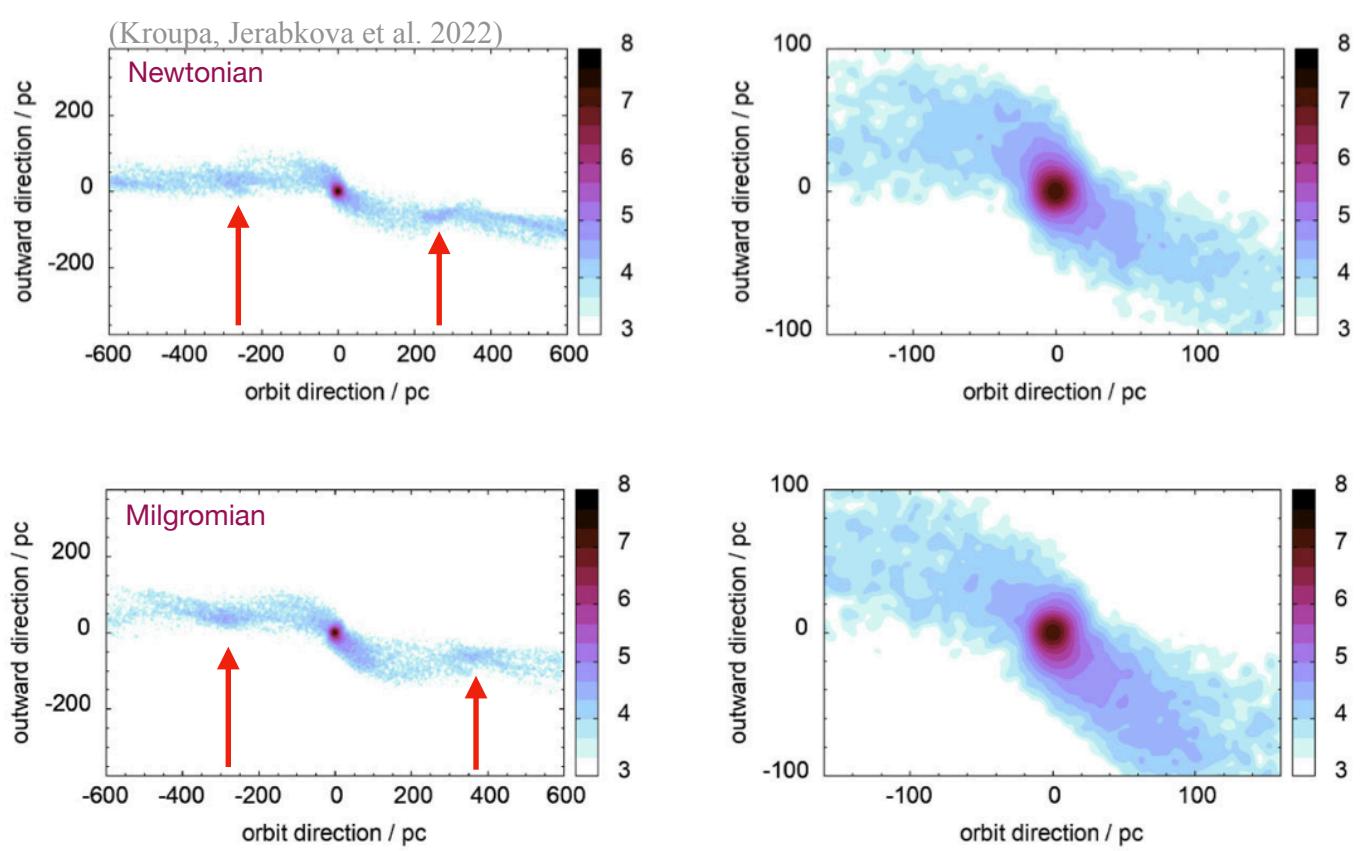
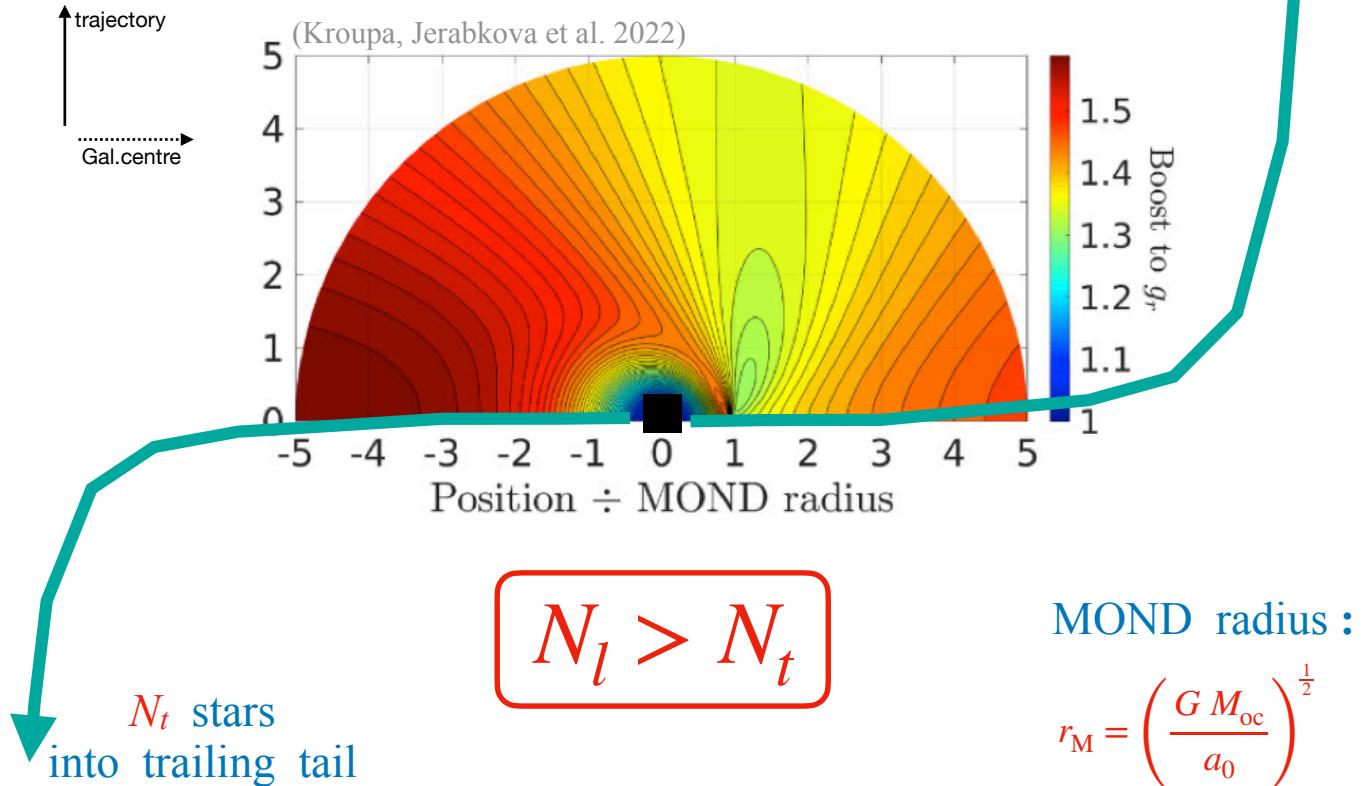
(Pflamm-Altenburg et al. 2023)

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MOND predictions

of new phenomena

N_l stars
into leading tail

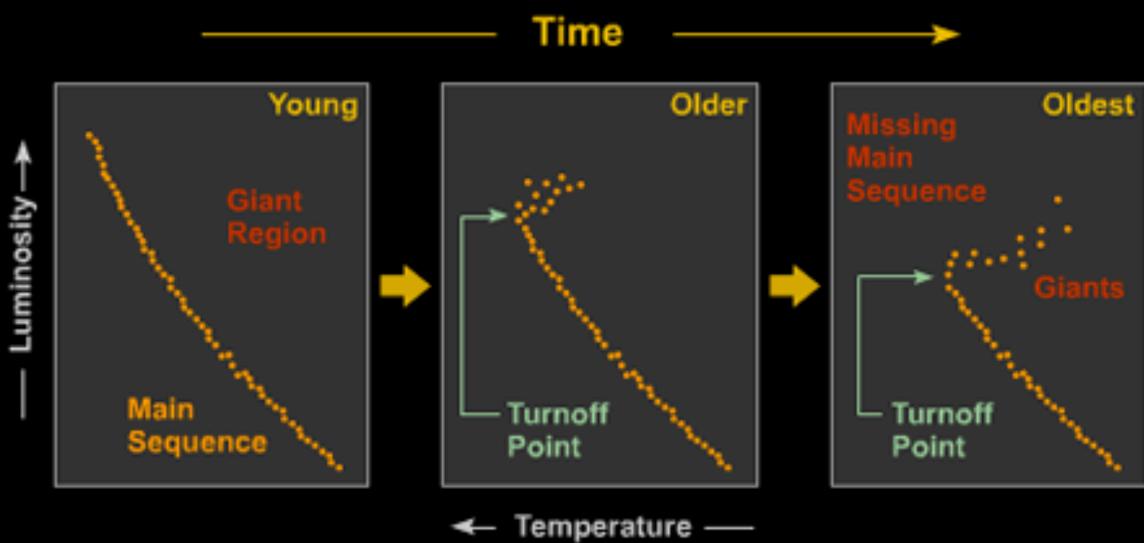


Age-dating methods of open star clusters

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Astrophysical age-dating



(Image credit: Brooks/Cole Thomson Learning)

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New age-dating methods of open star clusters

See also yesterday's talk on
dynamical and evaporative age-dating
by Nuria Miret Roig

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THE ASTROPHYSICAL JOURNAL, 925:214 (10pp), 2022 February 1

Age-dating with tidal tails The Dinnbier method

Dinnbier et al.

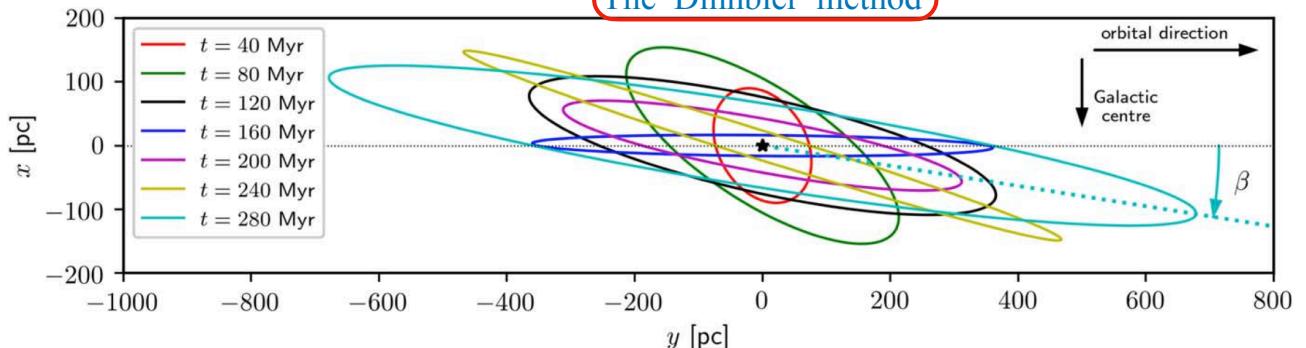
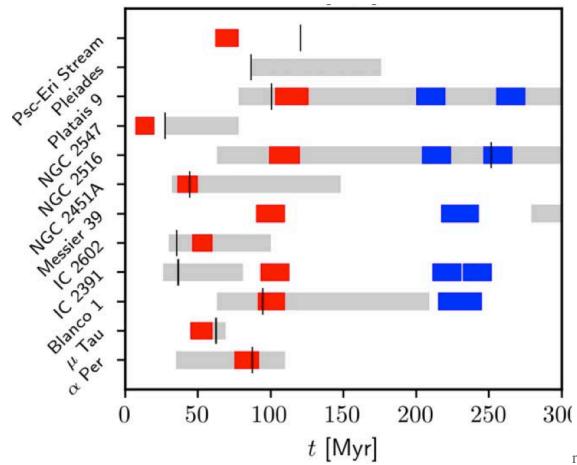
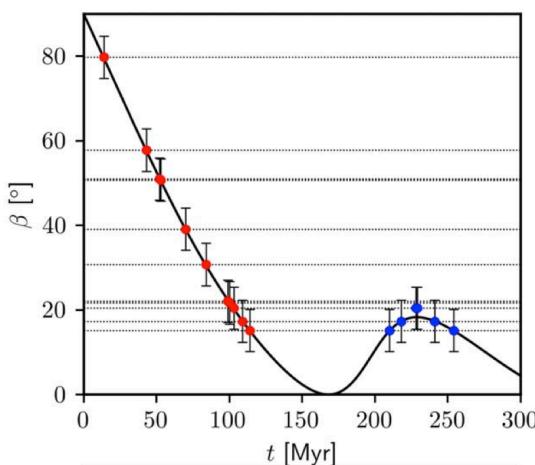


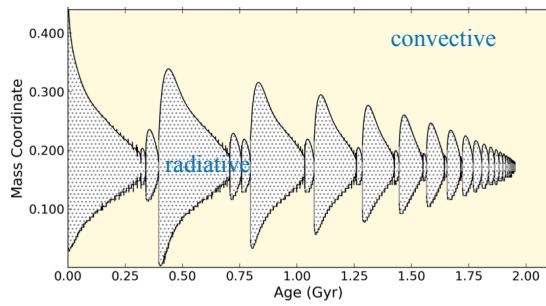
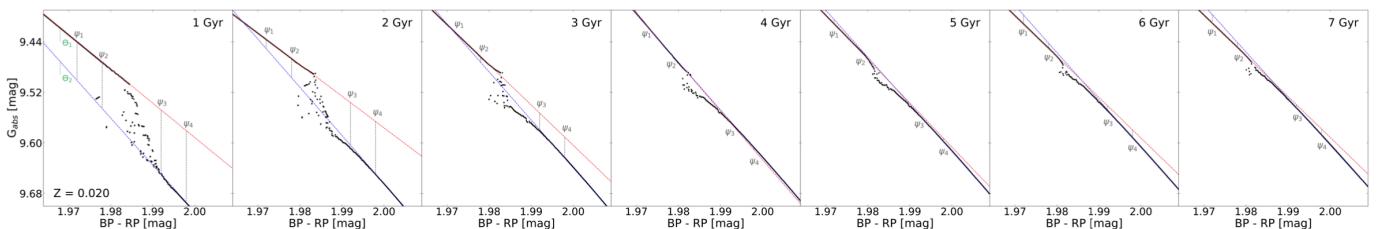
Figure 1. The orientation and shape of tidal tail I as calculated according to Equations (1) and (2) for stars escaping at $\tilde{v}_{e,I} = 2 \text{ km s}^{-1}$ and for the conditions at the solar circle. The age of the tail is indicated by the color. The star cluster is located at the center of the coordinate system (the black star), and it orbits the Galaxy in the direction indicated at upper right. As the cluster and tail age, the direction of the long axis of the tidal tail changes from pointing almost toward the Galactic center (at $t = 40 \text{ Myr}$) to the direction of the cluster motion (at $t = 160 \text{ Myr}$), and with increasing tilt again afterward. Also note that the shape and aspect ratio of the tidal tail undergo complicated changes with time. The dotted cyan line shows the definition of the tail tilt angle β .



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Age-dating with the *kissing instability* in Mdwarf stars

(Mansfield & Kroupa 2021; 2023)



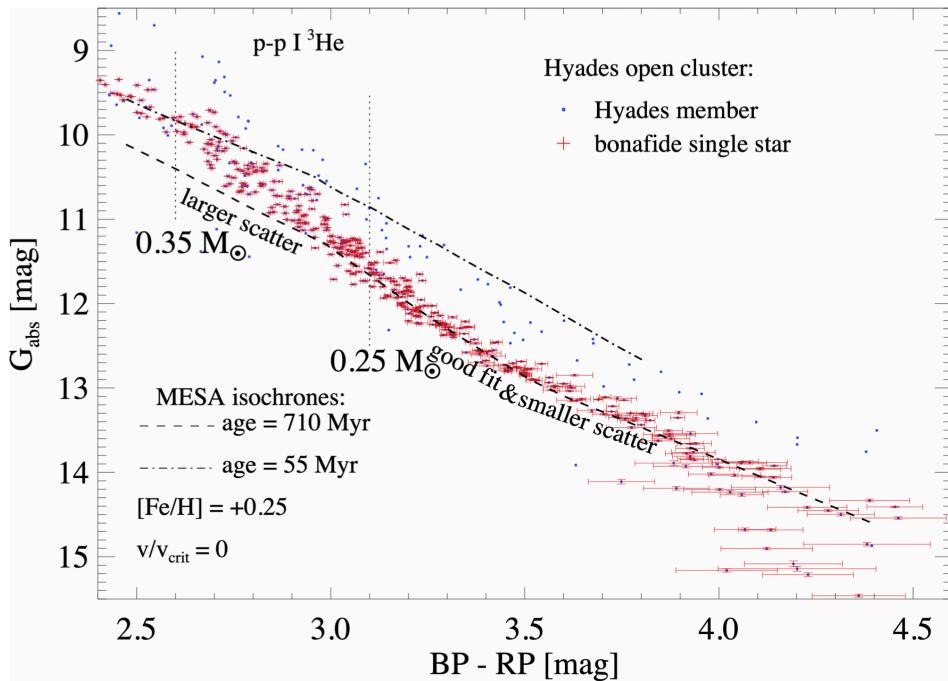
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Age-dating with the *kissing instability* in Mdwarf stars

(Mansfield & Kroupa 2021; 2023)

4 W. Brandner, P. Calissendorff, and T. Kopytova 2023



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Age-dating with the *kissing instability* in Mdwarf stars (Mansfield & Kroupa 2021; 2023)

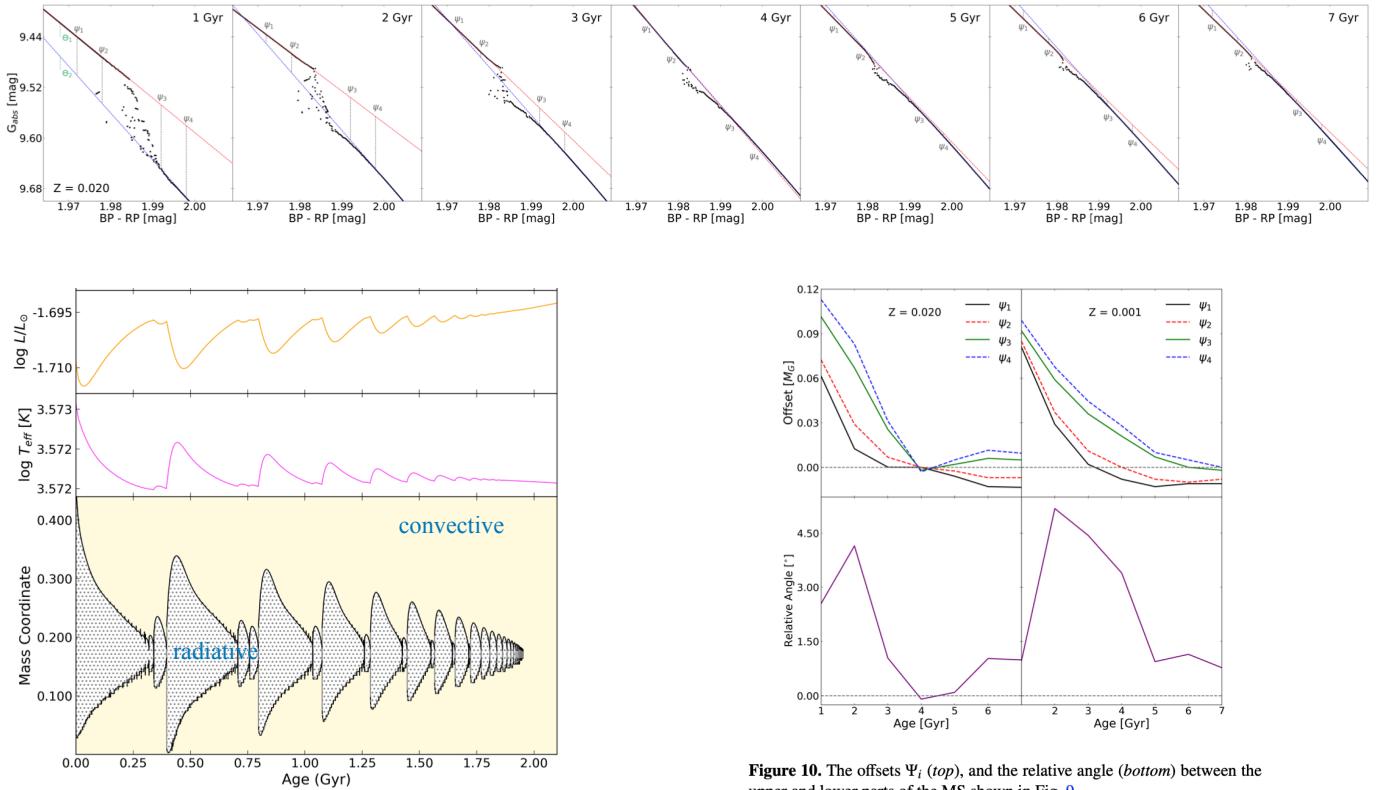


Figure 10. The offsets Ψ_i (top), and the relative angle (bottom) between the upper and lower parts of the MS shown in Fig. 9.

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Conclusions

Can compute stellar and binary populations in whole galaxies
For this initial distribution functions reasonably well known

Need : all stars form as binaries in embedded clusters
(The Galileo Conjecture)

---> *yesterday's talk by Franta Dinnbier*

New Jerabkova CCCP method to map extended tidal tails of open clusters
---> *talk by Henri Boffin*

Tidal tails asymmetric ==> Milgrom, and not Newton

---> *talk by Jan Pflamm-Altenburg*

Age-dating: tidal tail I angle (The Dinnbier method)
and kissing instability in Mdwarfs

END