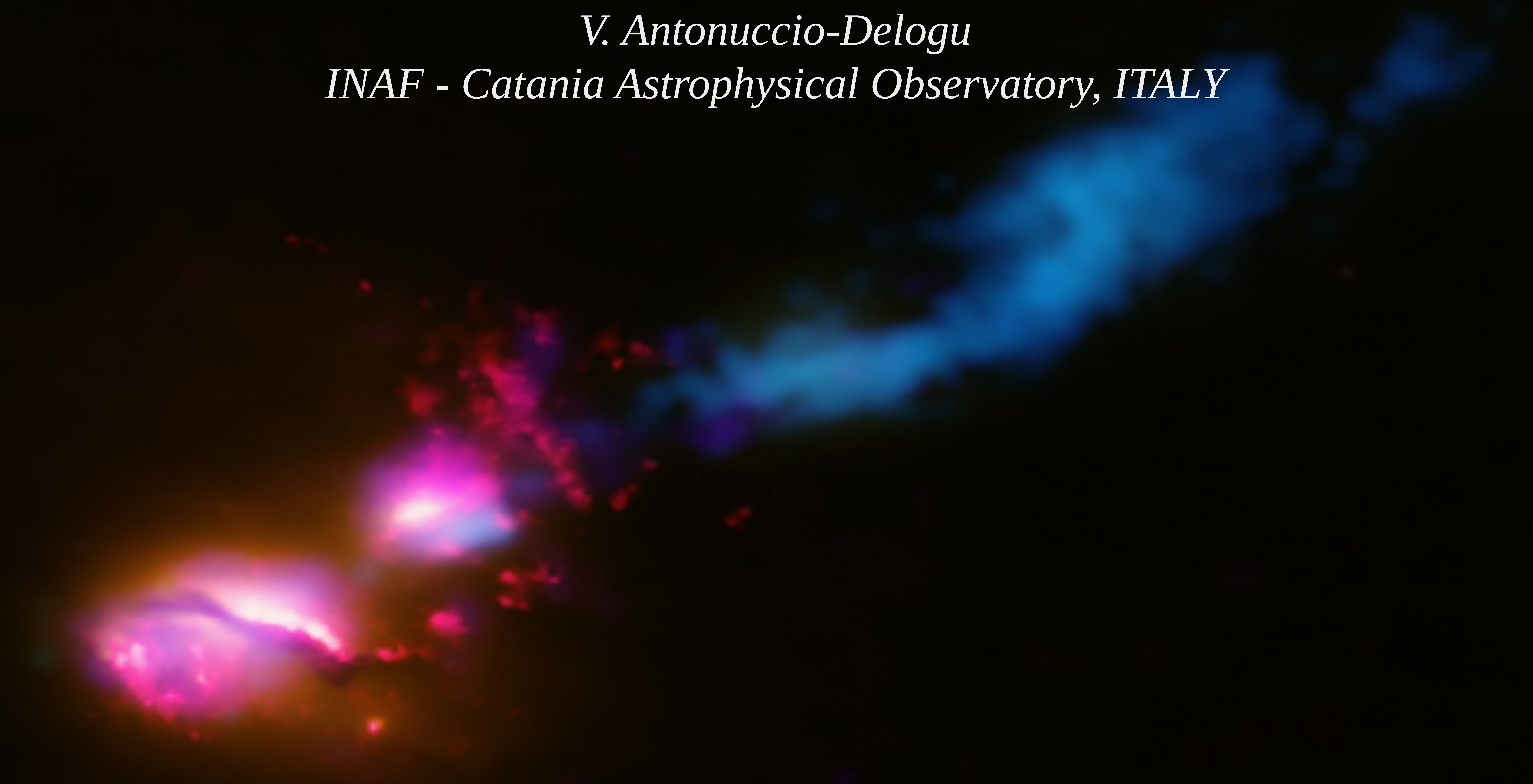
Relativistic Thermodynamics in CFD codes

V. Antonuccio-Delogu

INAF - Catania Astrophysical Observatory, ITALY



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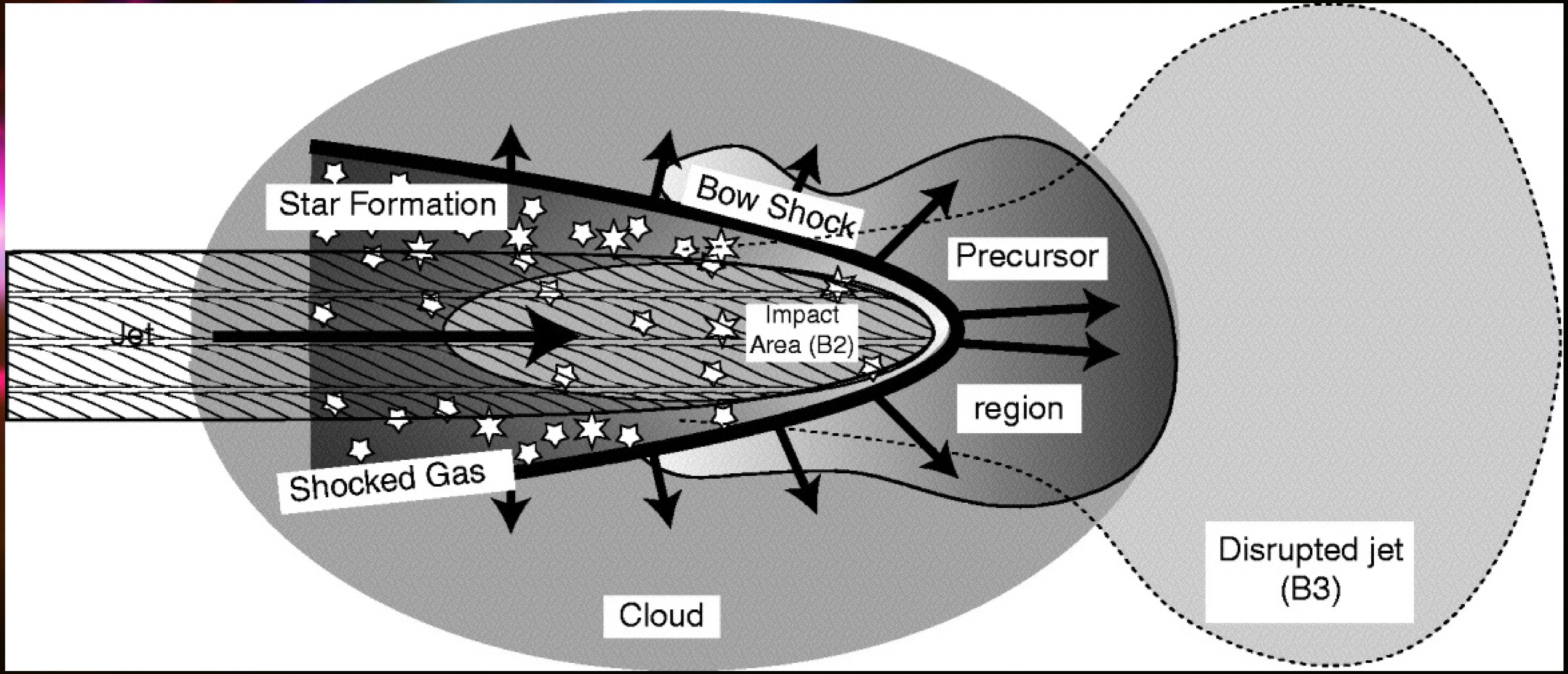

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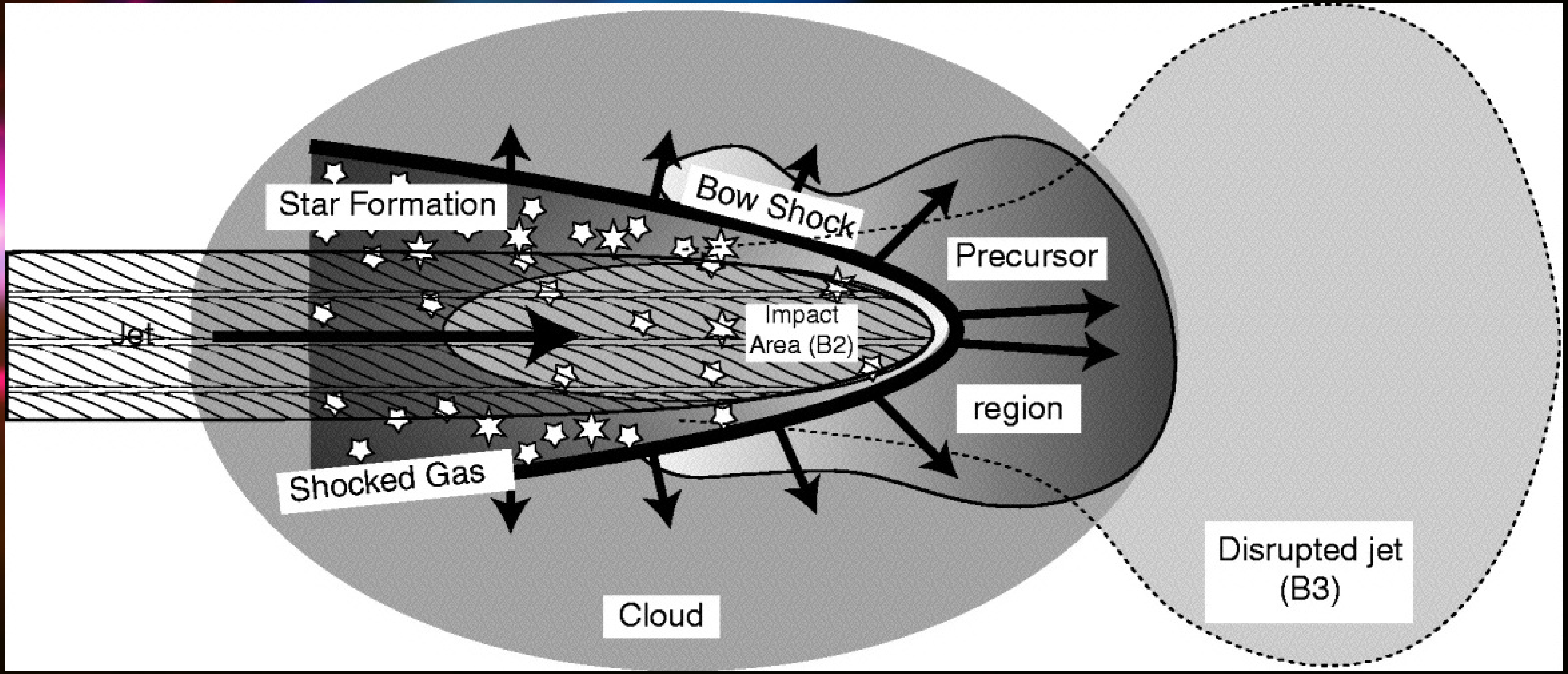

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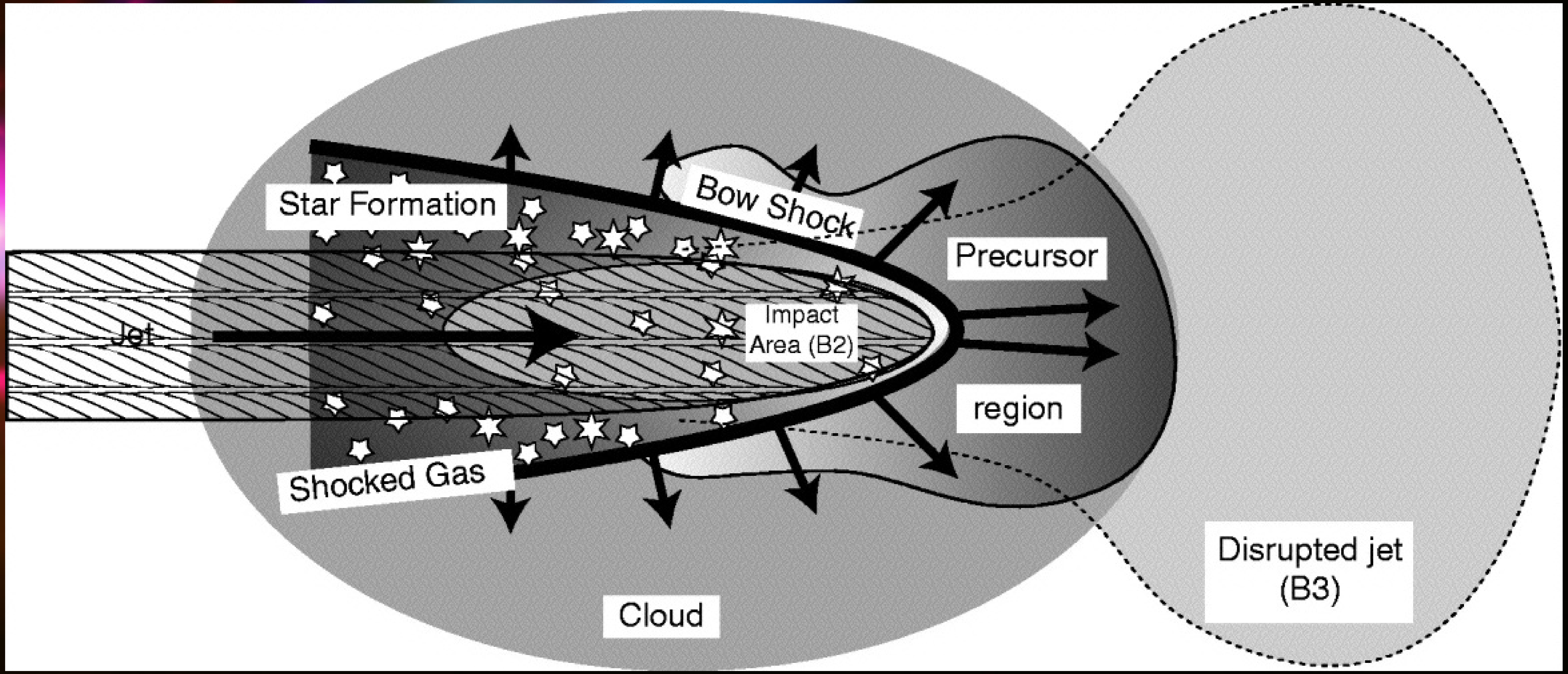

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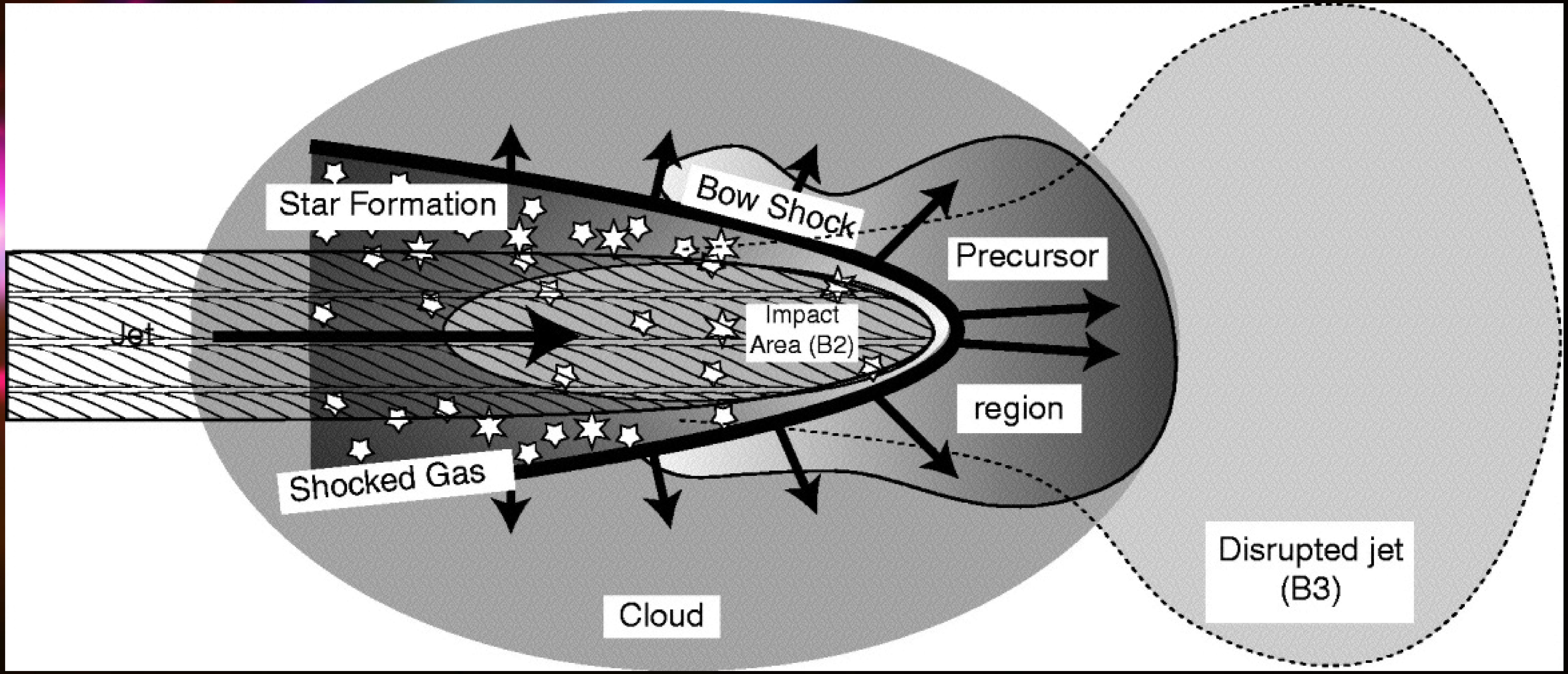
The thermodynamics of jet-ISM interaction is as relevant as the purely mechanical feedback.



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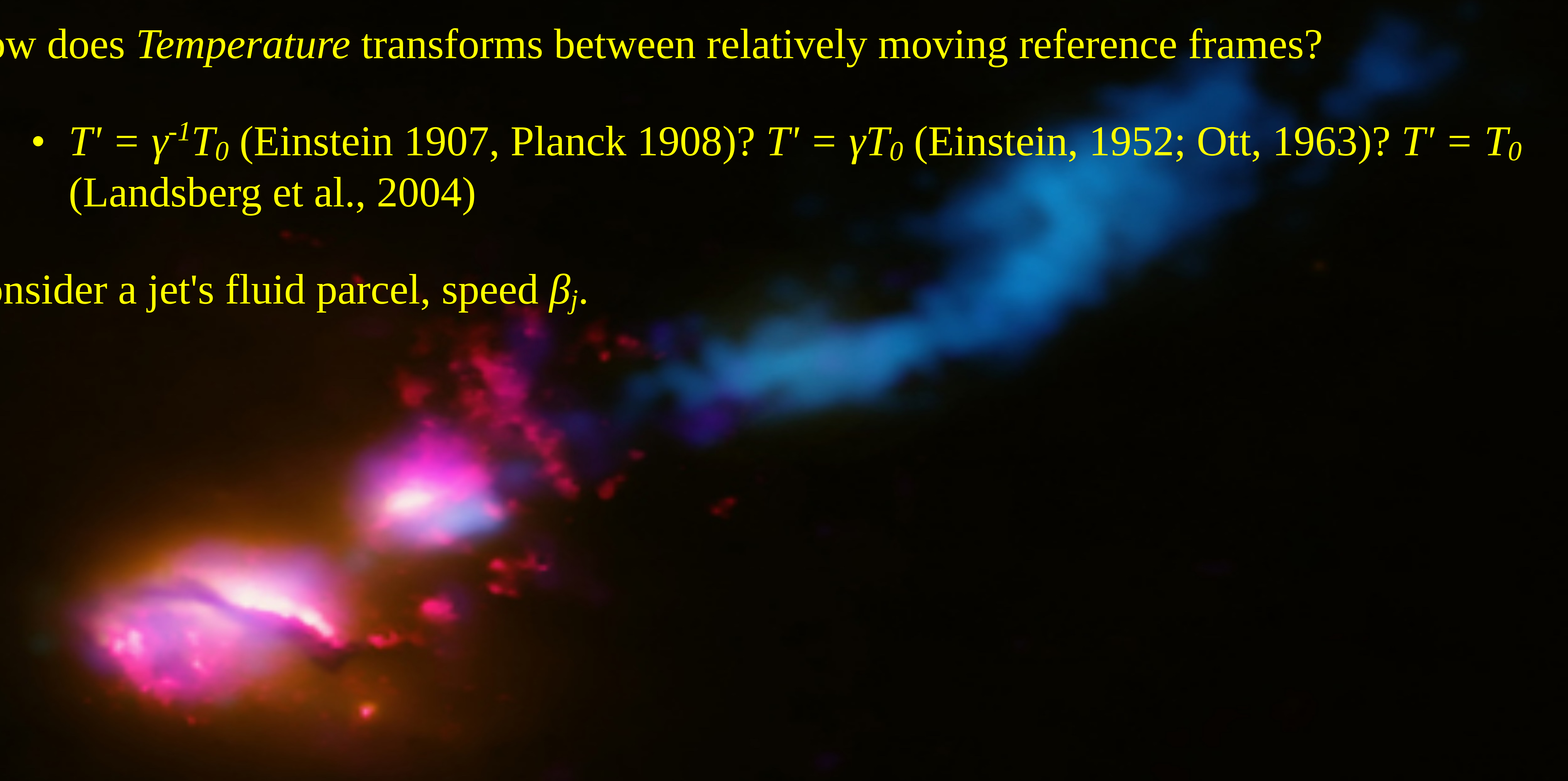

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Classical Thermodynamics only holds for Galileian transformations (Landsberg, 2003).

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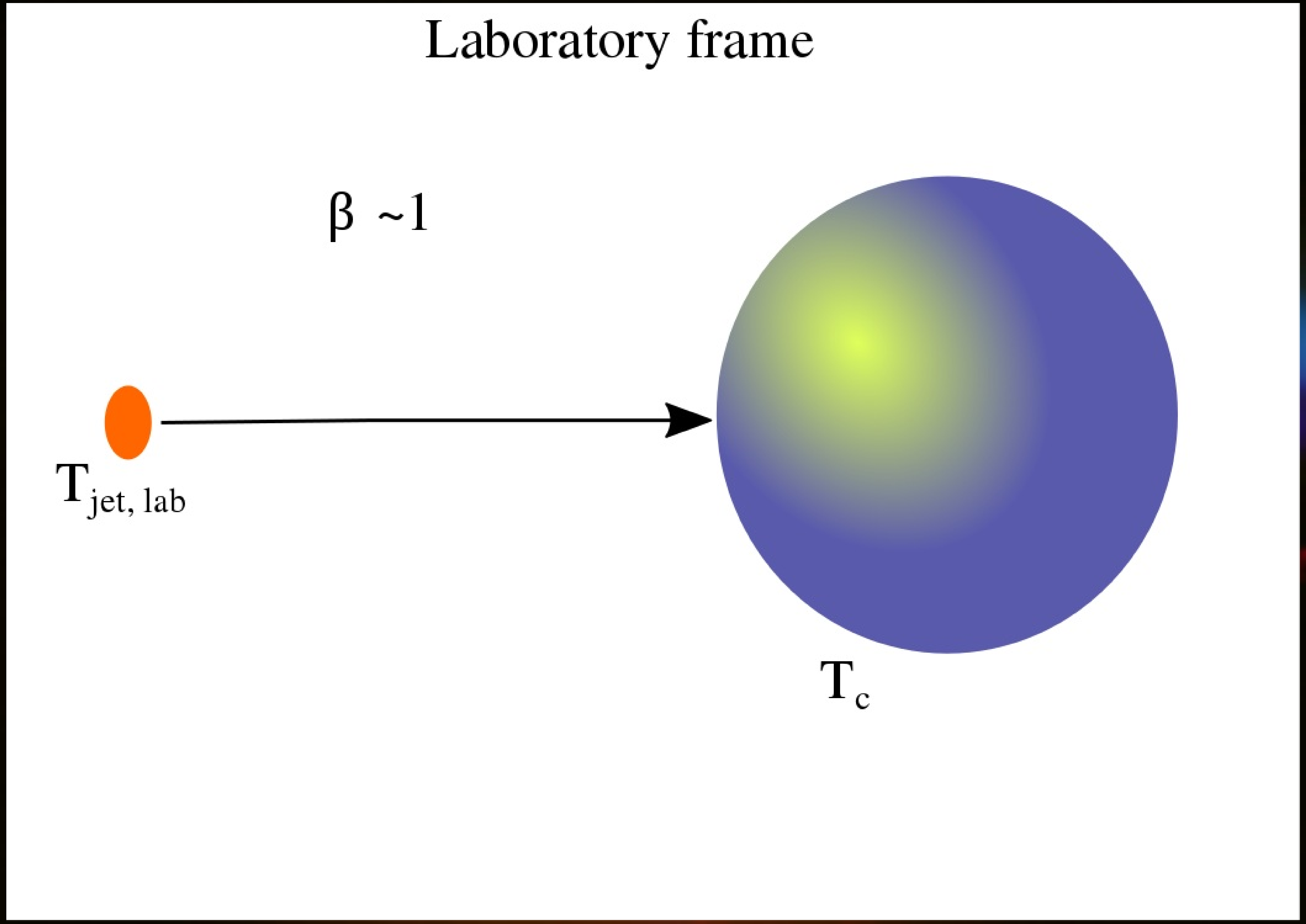

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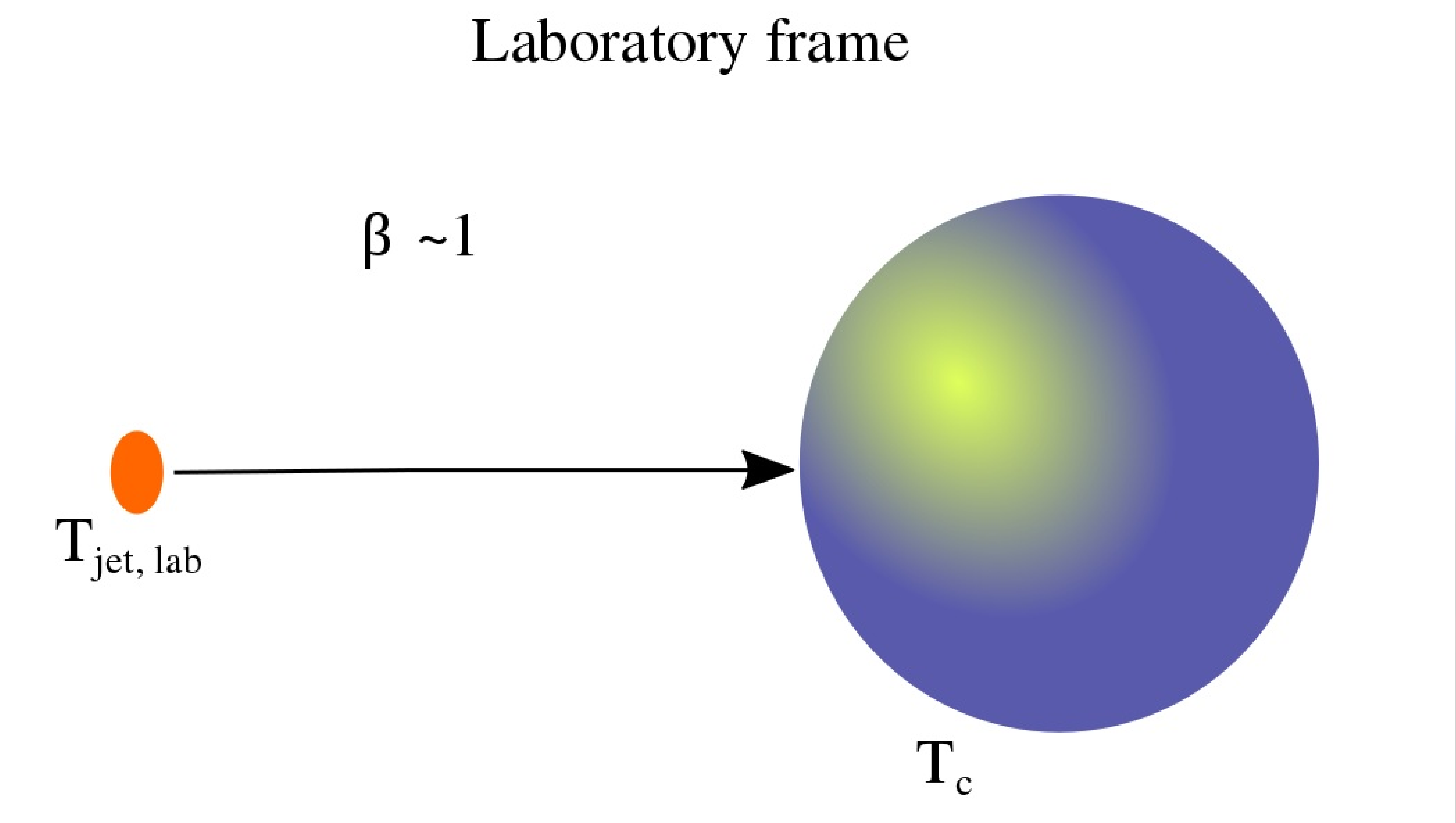

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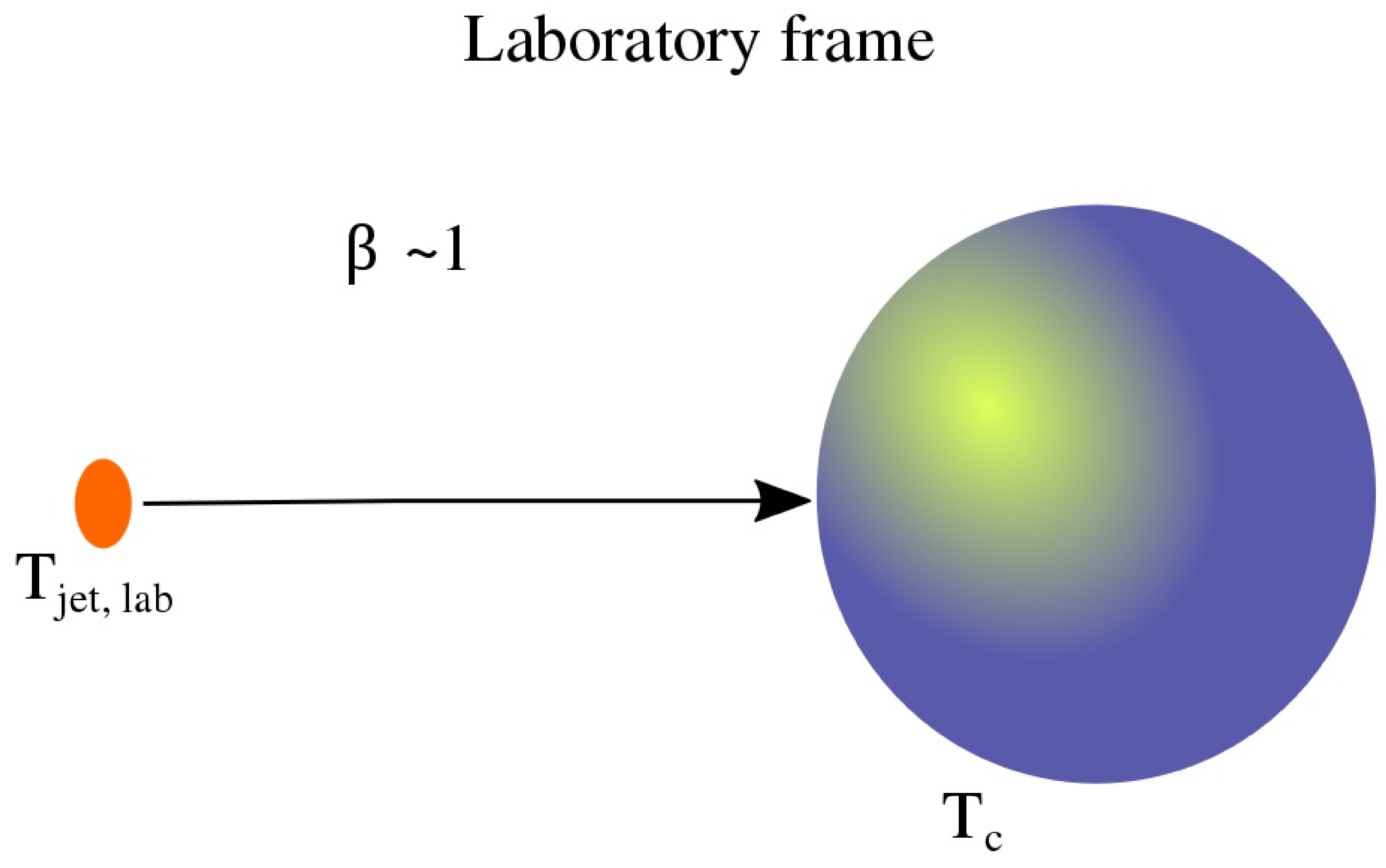

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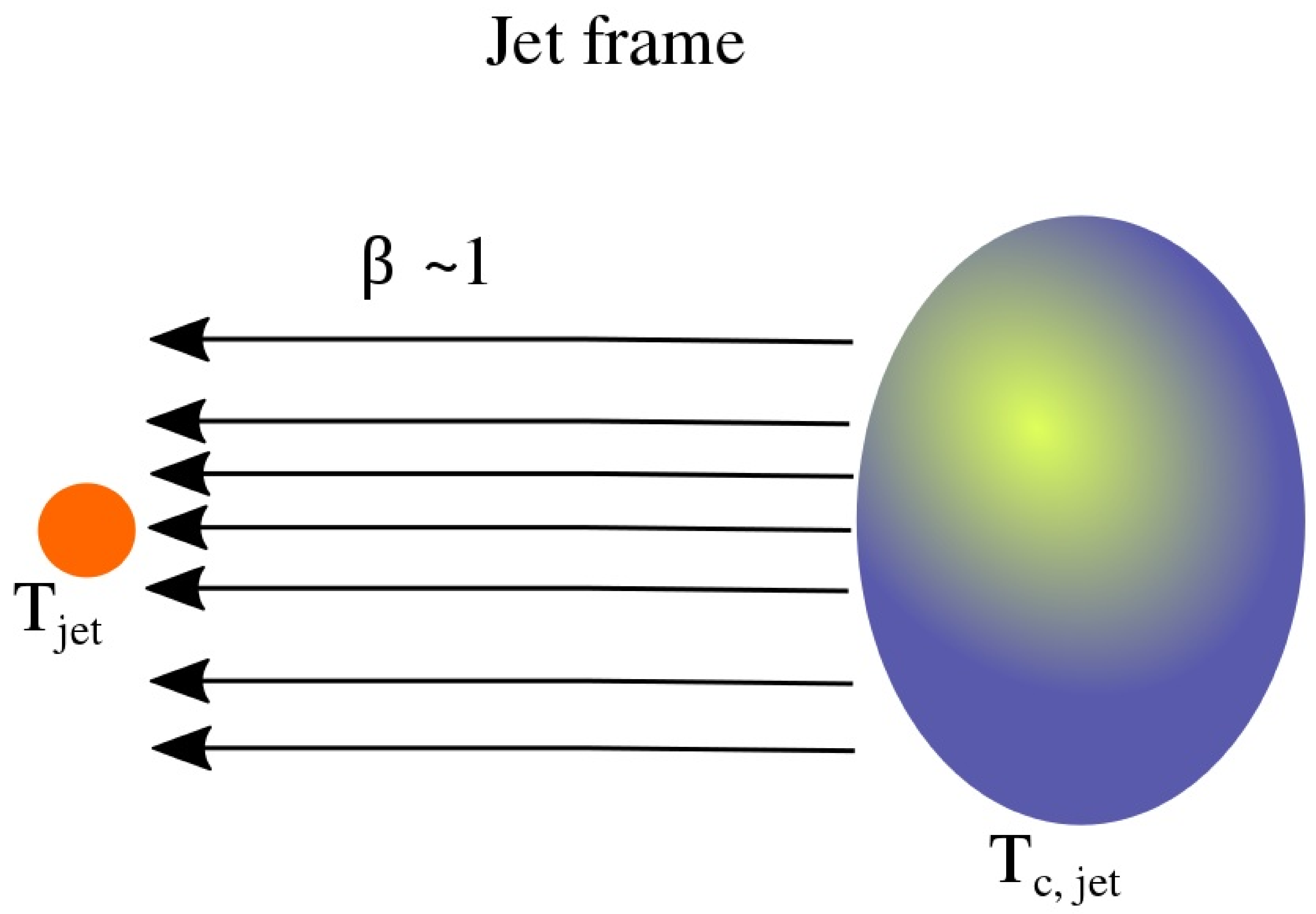

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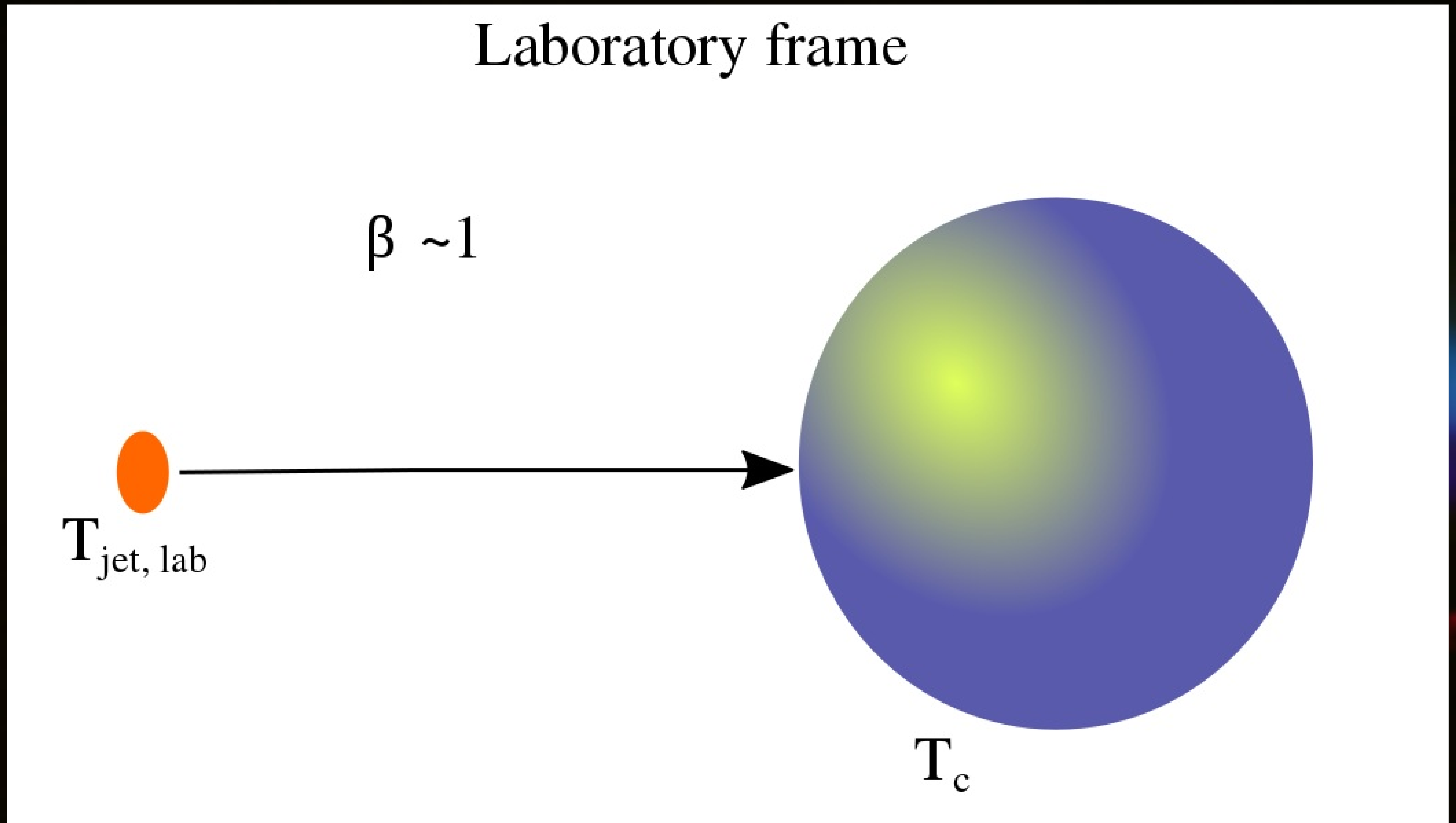

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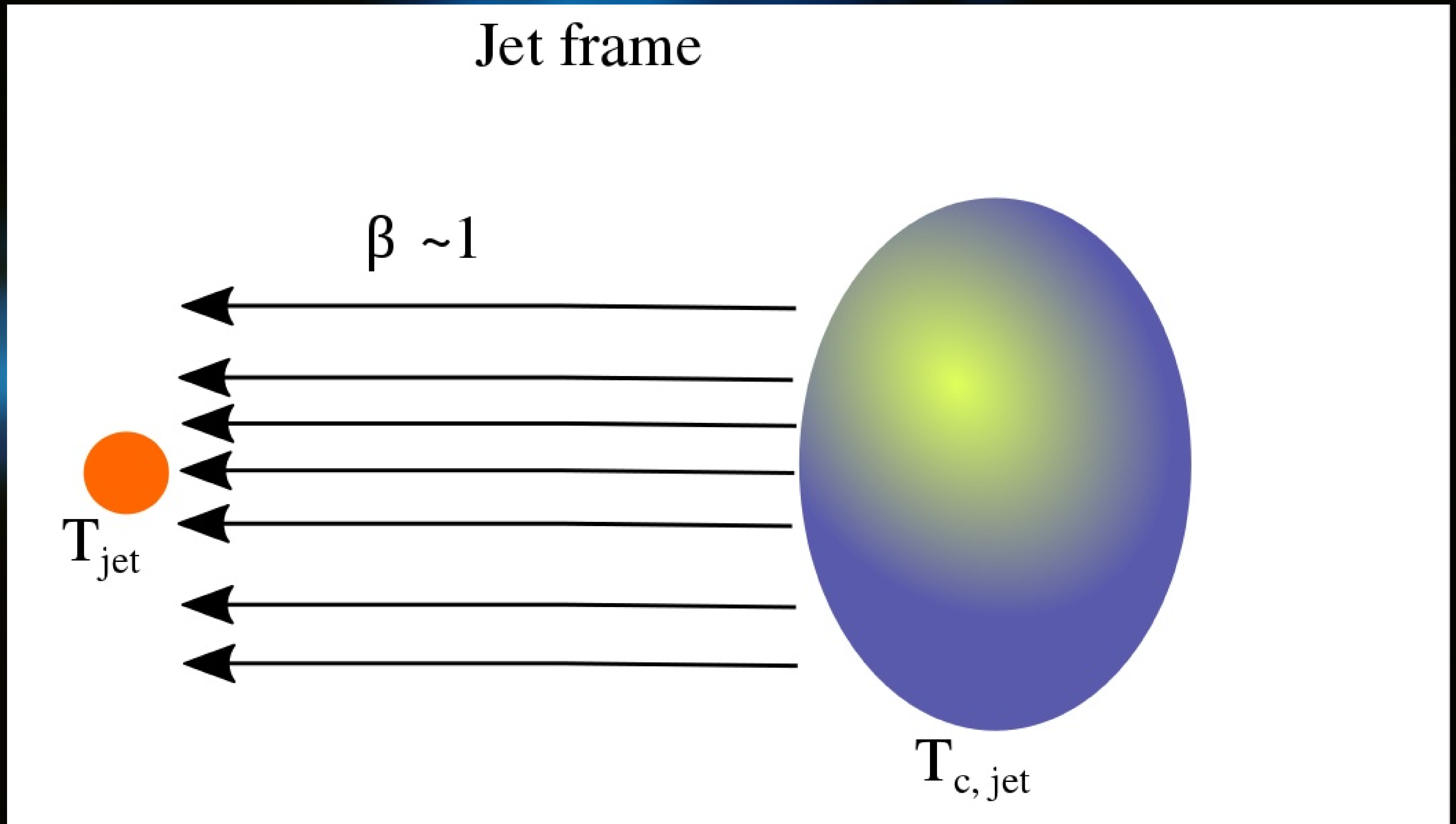

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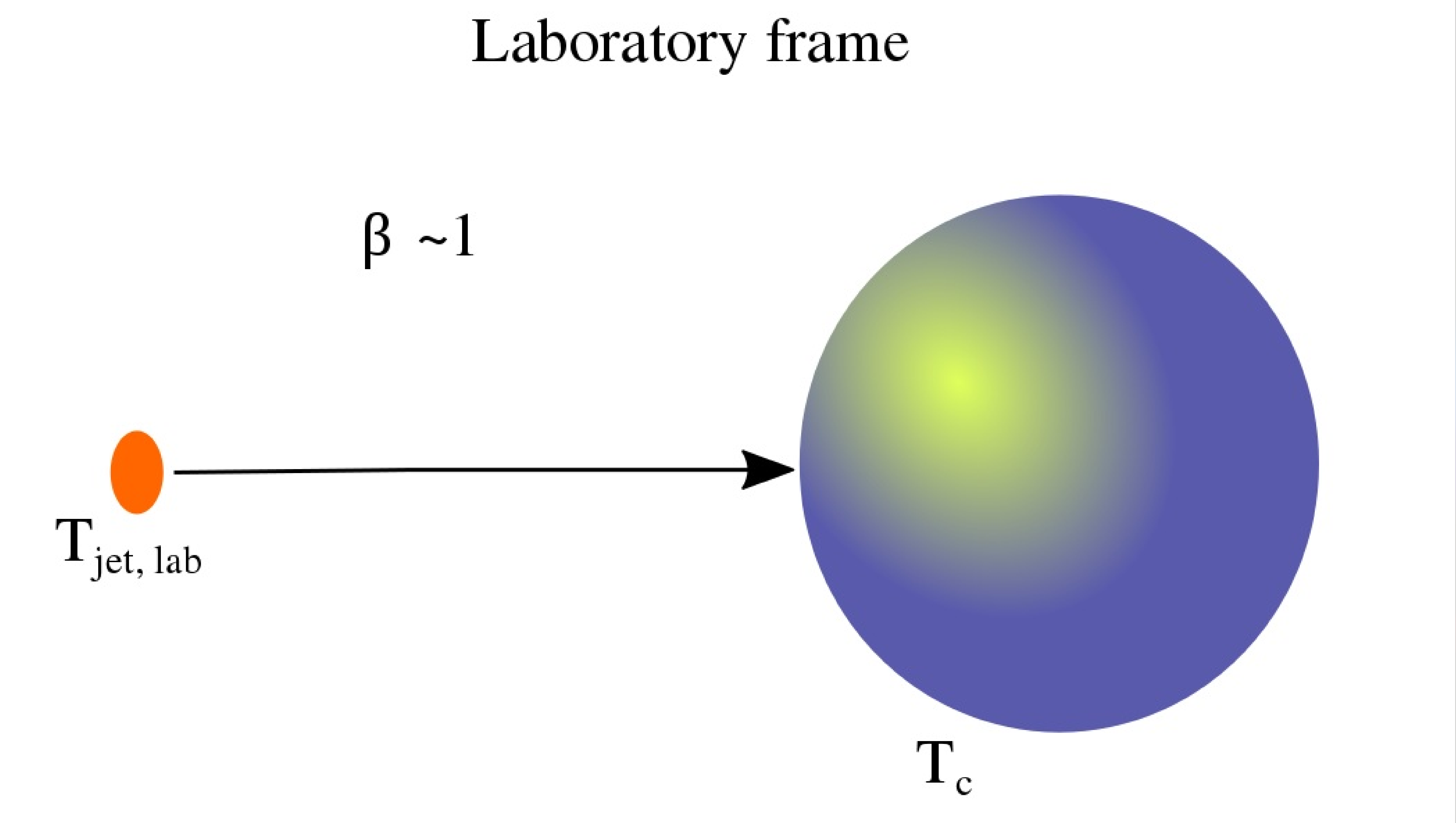

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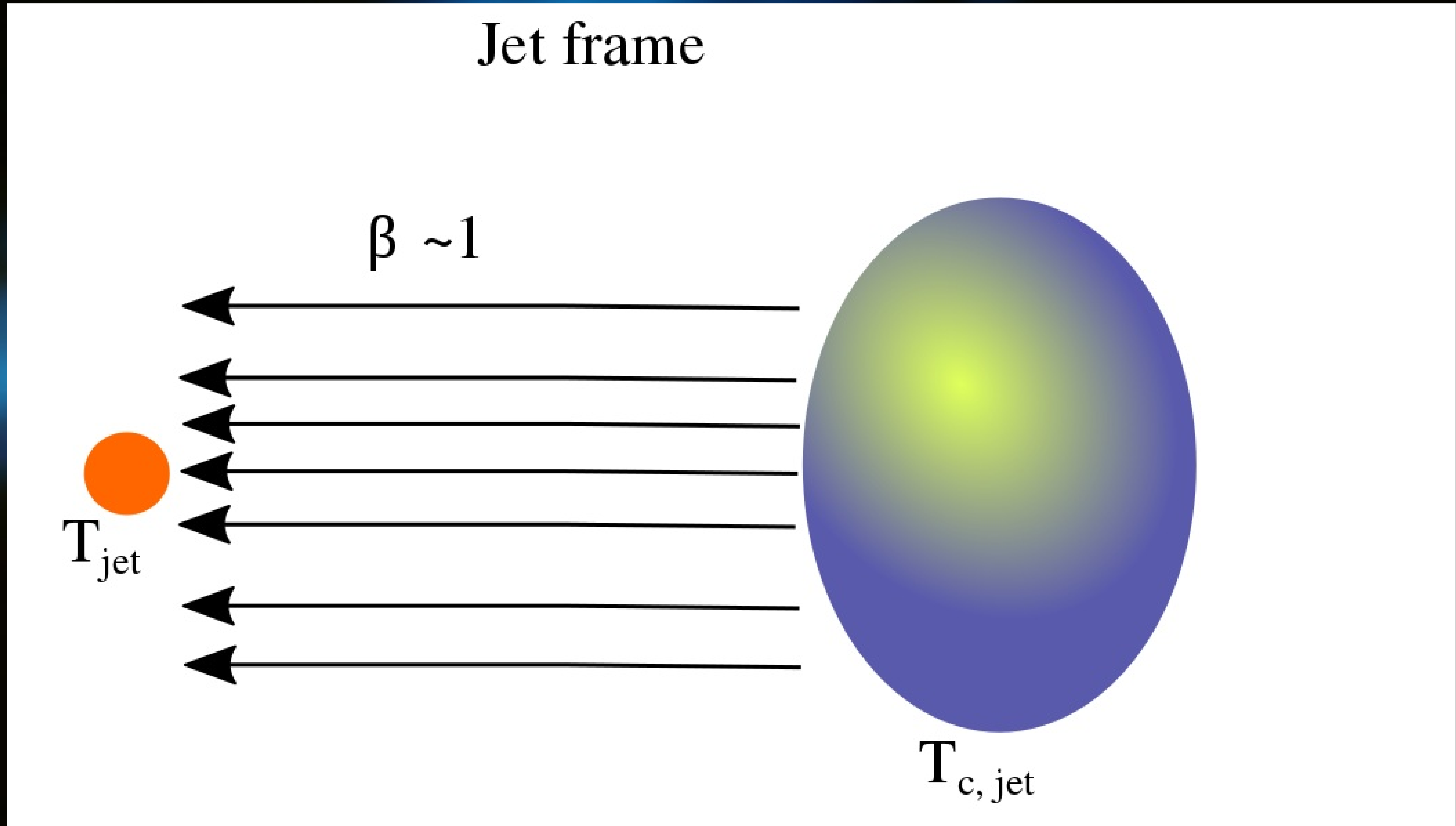

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Actual value of T_c determines the *excitation temperature* of observed fluorescence lines.

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