

RR Lyrae pulsation and evolution models tested against EDR3

Outline

- ▶ Brief detouring to extrasolar planets
- ▶ Classical double-mode RR Lyraes
- ▶ Bright Galactic field RR Lyraes
- ▶ Some current Gaia PLX ZP estimates

“Stellar Evolution along ...”, Naples, September 20-23, 2022

Fernley, Barnes, Skillen et al. 1998, A&A, 330, 515

3. Trigonometric parallaxes

One star, **RR Lyrae** itself, has a reasonably well determined parallax, $\pi=4.38\pm0.59$ mas which is equivalent to $\sigma\pi/\pi=0.13$. The **remaining stars** are at least a magnitude fainter with correspondingly smaller parallaxes and larger errors and values of $\sigma\pi/\pi \geq 0.30$.

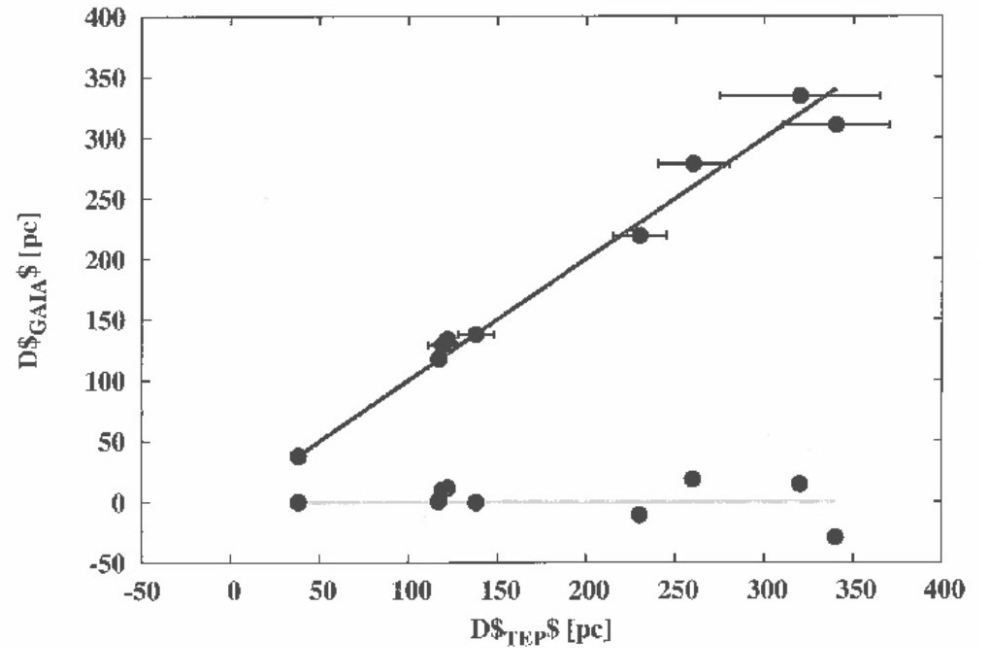
Gaia EDR3:

RR Lyrae: $\pi = 3.985 \pm 0.027$

105 bright RR Lyraes: $\sigma(\pi) / \pi < 0.03$

Back to 2018 ...

After an enthusiastic discussion with Attila Moor:

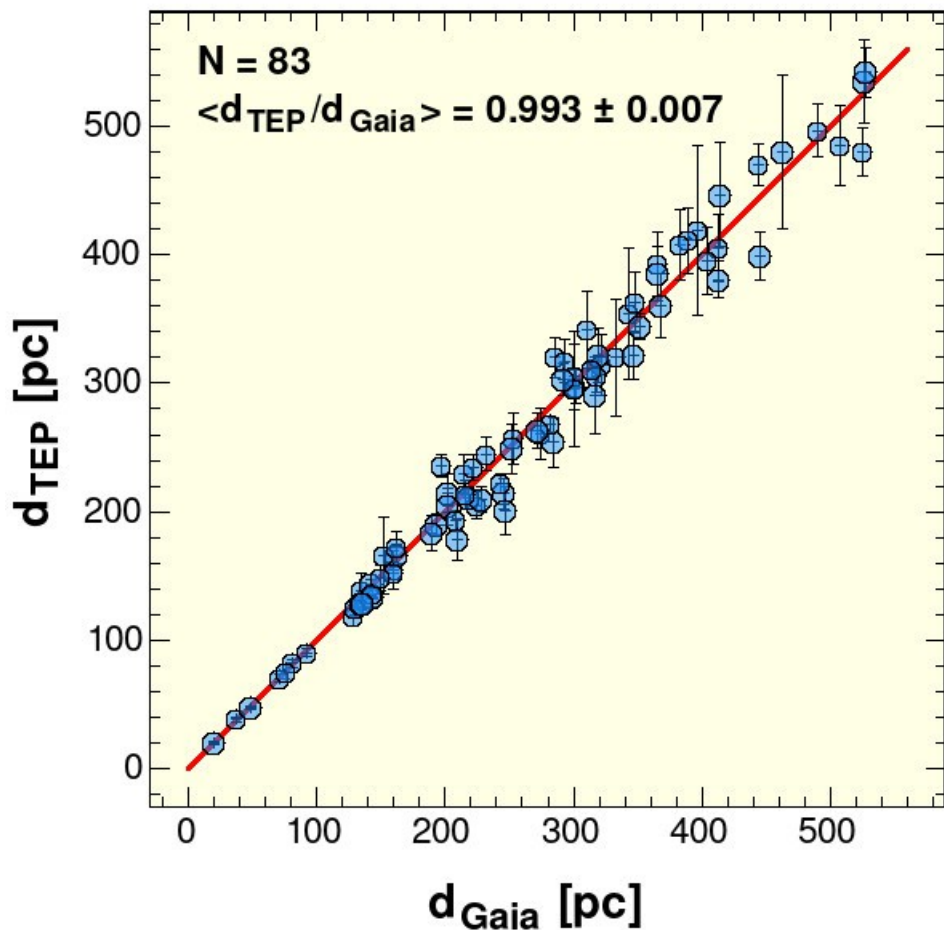


Two **COMPLETELY INDEPENDENT** datasets

π (Gaia) : Position measurements

π (TEP) : T_{eff} estimate – SED, stellar atm. models
[Fe/H] – spectroscopy
 ρ – system parameters a , R , P
 L – stellar evolution models
 M_V – BC, stellar atm. models
→ V – photometry, $E(B-V)$
 $\lg(\pi)$ = $-1 - 0.2(V - M_V)$

The 2022 update



$$PLX_{TEP} = PLX(Gaia) + \Delta PLX$$

$$[PLX] = \text{mas}$$

EDR3:

$$\langle e_{PLX} / PLX \rangle = 0.5 \%$$

N = 83

DR	$\langle \Delta PLX \rangle$	$\sigma(\Delta PLX)$
2	0.08865 ± 0.03161	0.28801
3	0.06766 ± 0.03093	0.28182

N = 69 (without KELT):

DR	$\langle \Delta PLX \rangle$	$\sigma(\Delta PLX)$
2	0.04638 ± 0.02873	0.23864
3	0.02884 ± 0.02846	0.23643

RR Lyrae stars*

► Double-mode stars

Stellar pulsation:

$$P_0 = f_0(M, L, T_{\text{eff}}, Z)$$

$$P_1 = f_1(M, L, T_{\text{eff}}, Z)$$

Input: T_{eff}, Z

BUT: Z is not known

Stellar evolution:

$$E(M, L, T_{\text{eff}}, Z, t) = 0$$

► Single-mode stars

Stellar pulsation:

$$P_0 = f_0(M, L, T_{\text{eff}}, Z)$$

Input: T_{eff}, Z

Stellar evolution:

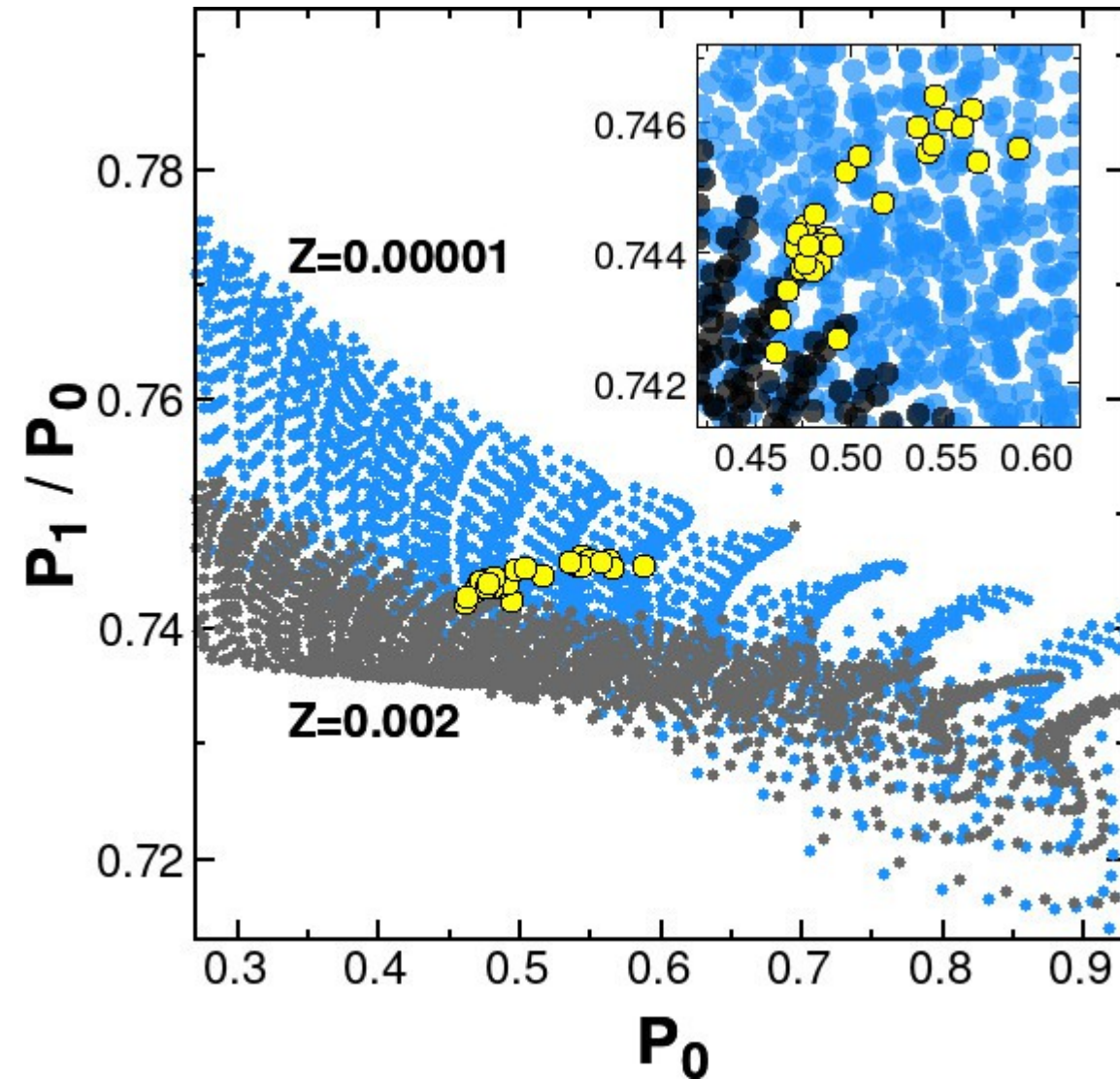
$$E(M, L, T_{\text{eff}}, Z, t) = 0$$

L(RRL) ↔ L(Gaia)

almost independent datasets

* Two A&A papers, co-author: Behrooz Karamiqucham

RRd stars I. — *appetizer*



AQ Leo:

Jerzykiewicz & Wenzel (1977)

M15 RRds:

Sandage, Katem & Sandage (1981)

- Petersen (1973)

@ fixed Z :

straigh lines

@ varying Z :

slices of $Z=\text{const}$

lines (MACHO / LMC)



degeneracy with mass

RRd stars II. — *in & out*

Data: 30 field RRd

● $\langle V \rangle$:

ASAS (26)
from Gaia BP (4)

● $\langle K \rangle$:

from W1, W2 of unWISE

● $E(B-V)$:

Schlafly & Finkbeiner (2011)

Models:

● T_{eff} :

Castelli et al. (1997)

IRFM ZP of

Gonzalez & Bonifacio (2009)

● BC :

Castelli et al. (1997)

$BC_{\text{sun}} = -0.082$

● Pulsation, HB evol.:

LNA (Kovacs & Buchler, 1988)

BaSTI, Hidalgo et al. (2018)

1. $V, K, E(B-V), Z_0, T_{\text{eff}}$

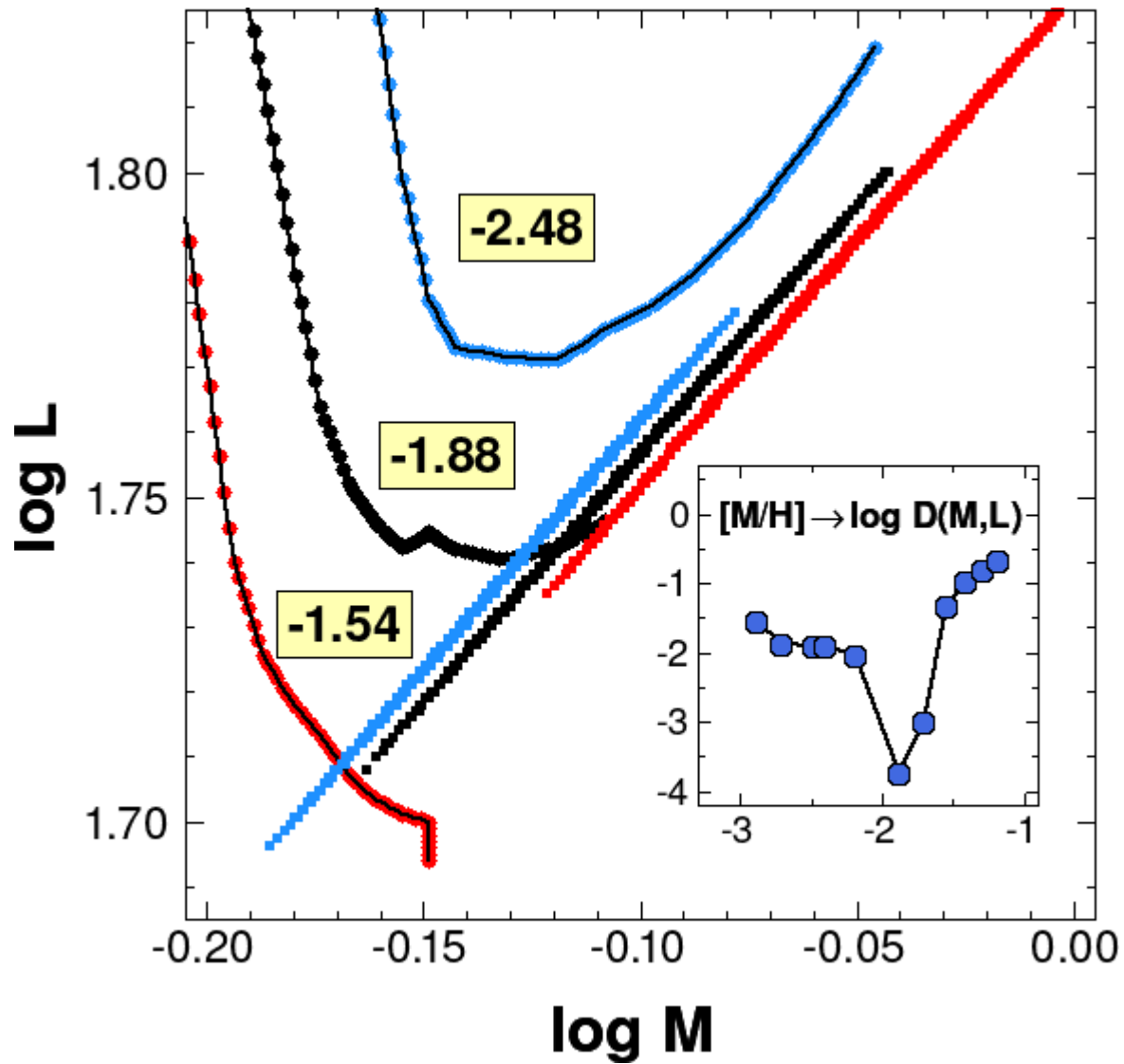
2. T_{eff} fixed, P_0, P_1 match to LNA: $\{M, L, Z\}_{\text{LNA}}$

3. T_{eff} fixed, $\{M, L, Z\}_{\text{HB}}$ set from BaSTI

4. Match $\{M, L, Z\}$ from #2, #3

5. Iterate on Z_0

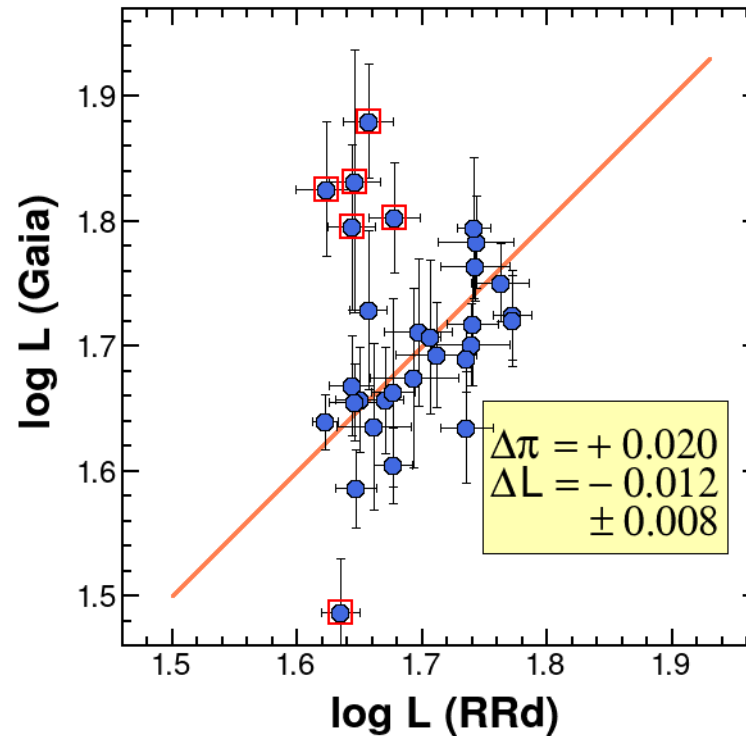
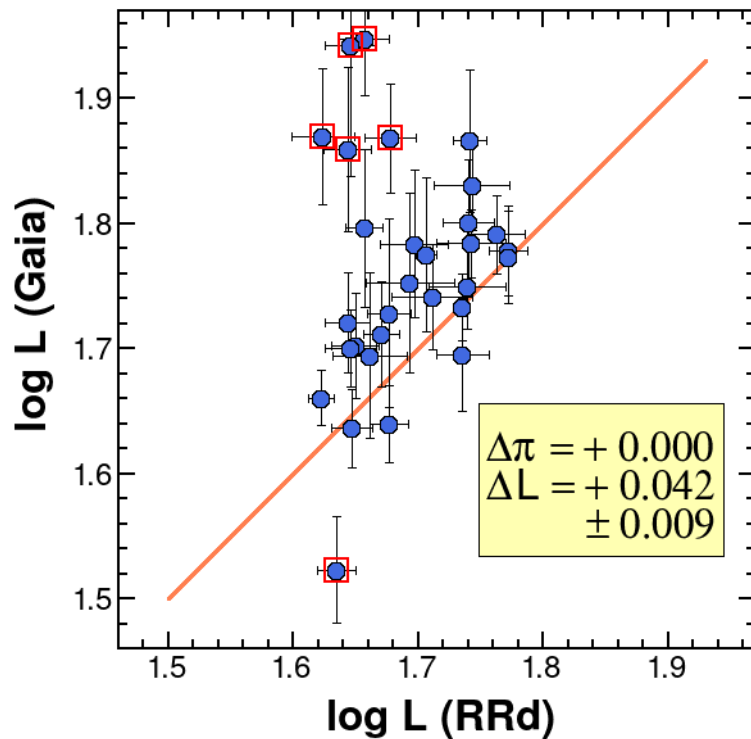
RRd stars III. — *LNA-HBEV match*



AQ Leo

- $T_{\text{eff}} = 6595 \text{ K}$
- LNA lines are shifted in L
- No shift for —

RRd stars: Gaia parallax shift



$$\Delta L = \lg L(\text{Gaia}) - \lg L(\text{RRd})$$

$$\lg L_1 = \lg L_2 + 2\lg(\pi_2/\pi_1)$$

$$\Delta\pi = \pi_2 - \pi_1$$

WARNING:
Blending may
play a role in
L(Gaia)

Also: an increase of 0.005 in $\log T_{\text{eff}}$ makes $\Delta\pi = 0.0$

Single-mode RR Lyrae stars

► As for the RRd stars, but $[Fe/H]$ is known

● Input: $P, V, RP, W2, [Fe/H], E(B-V)$

○ $RP, W2 \rightarrow Ks$

○ $V, Ks, \log g, [Fe/H], E(B-V) \rightarrow T_{\text{eff}}$

$[T_{\text{eff}} \text{ ZP by IRFM of Gonzales \& Bonifacio (2009)}]$

○ *Stellar pulsation:* (M, L) via $P_0 = f_0(M, L, T_{\text{eff}}, Z)$

○ *Stellar evolution:* (M, L) via $E(M, L, T_{\text{eff}}, Z, t) = 0$

○ **Metric:**

$$D(M, L, Z) = \sqrt{\log^2 \left(\frac{L^{HB}}{L^{LNA}} \right) + \log^2 \left(\frac{M^{HB}}{M^{LNA}} \right)}$$

Datasets

- **Brightness:** $8 < V < 13$
- **EDR3 relative PLX error:** $< 10\%$
- **Reliable [Fe/H] accessibility**
- **V:** Dambis et al. (2013)
Monson et al. (2017)
ASAS
- **Ks: Calibrated (W2, RP) to Layden et al. (2019):**
145 stars with $\sigma_{\text{fit}} = 0.03$
- **156 stars:**

$\sigma(\pi) / \pi$	N_stars
0% - 2%	62
2% - 3%	43
3% - 10%	51

Iron abundances

► Lack of homogenized HDS [Fe/H]

- Input:
HDS & LDS [Fe/H]
177 stars
- LDS – linear transf.
- HDS – ZP shift

J96 = Jurcsik & Kovacs (1996)

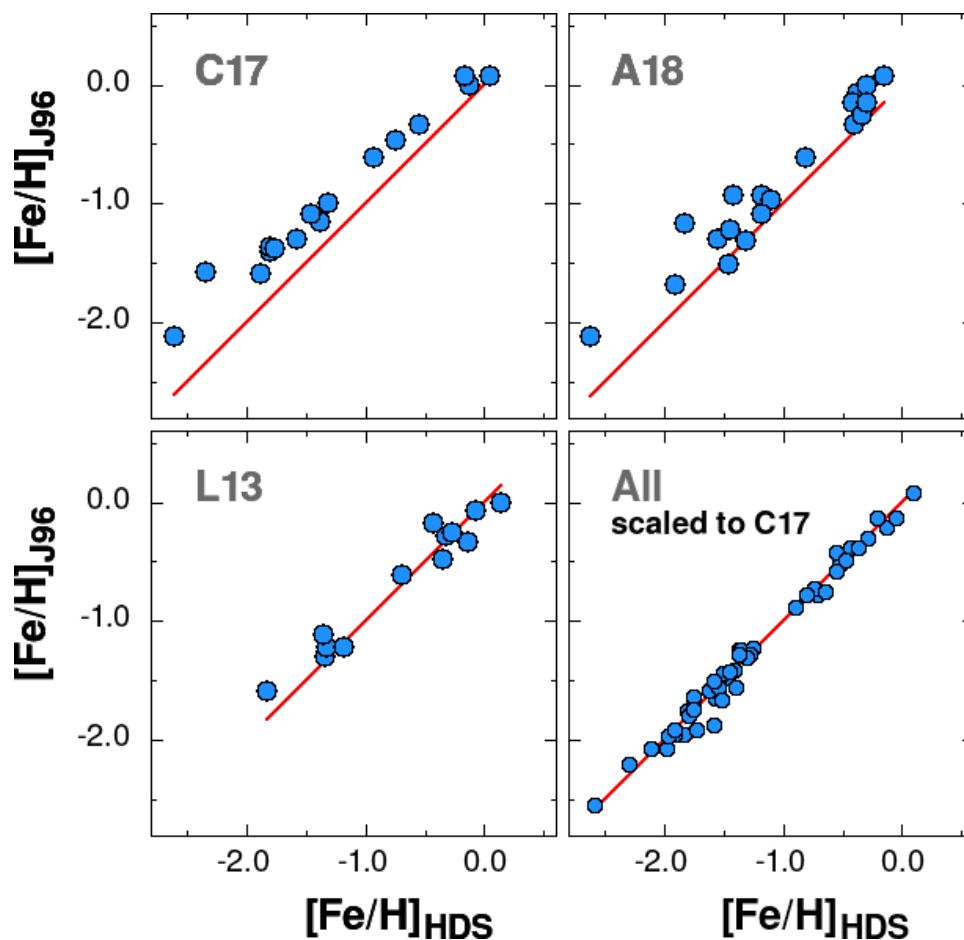
L13 = Liu et al. (2013)

C17 = Chadid et al. (2017)

A18 = Andriewsky et al. (2018)

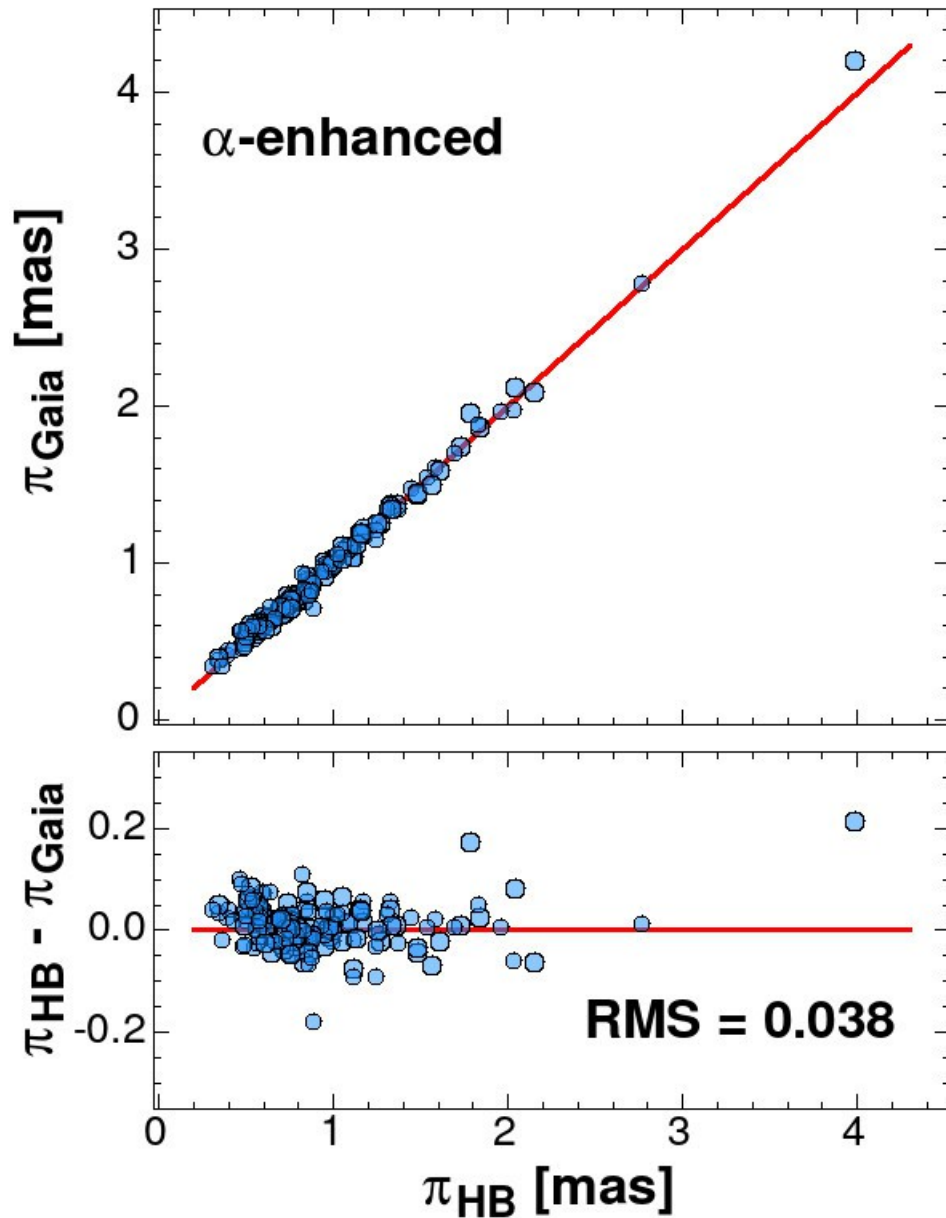
Note: “All” = All sources

$$[Fe/H]_{C17} = 1.10 [Fe/H]_{J96} - 0.22$$



J96 → C17

HB/LNA vs Gaia



► HB models:
 $[\alpha/\text{Fe}] = 0.0$
 $[\alpha/\text{Fe}] = +0.4$

► All 156 stars:
- 3 ~outliers
(including
RR Lyrae:)

► For $[\alpha / \text{Fe}] = 0.0$
RMS = 0.042

Note in passing ...

Don Vandenberg et al. 2000, ApJ, 532, 430

(see also Ben Dorman 1992)

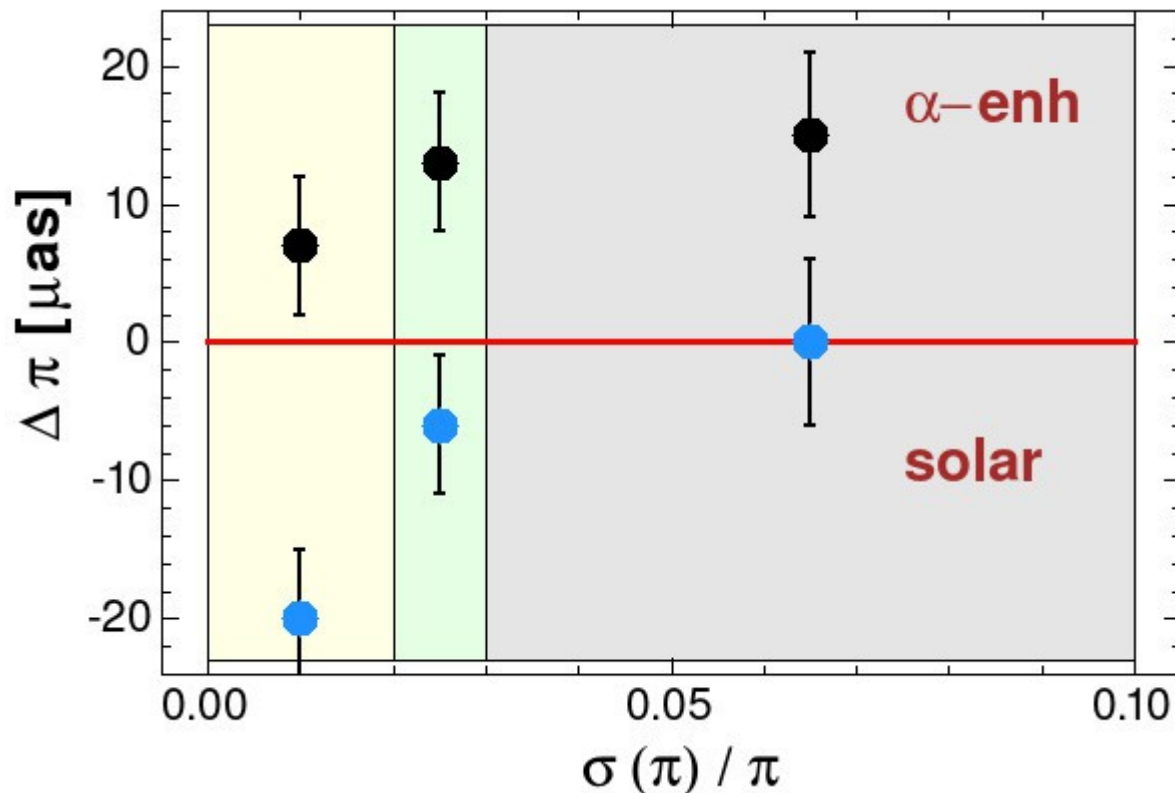
>>> for the SAME [Fe/H]:

α -enhanced models are fainter by ~ 0.02 in log L

20-30 years later, from BaSTI:

		Enhanced	Solar	Sol-Enh
Set	N	$\lg(L_{\text{Gaia}}/L_{\text{HB}})$	$\lg(L_{\text{Gaia}}/L_{\text{HB}})$	$\lg(L_{\text{sol}}/L_{\text{enh}})$
A	62	+0.006	-0.012	+0.018
B	43	+0.015	-0.003	+0.018
C	51	+0.026	+0.007	+0.019

Gaia PLX ZP shift



$$\pi(\text{HB}) - \pi(\text{Gaia}) = \Delta \pi$$

The bright end suggests preference for α -enhanced models

For 156 stars:

$$[\alpha/\text{Fe}] = 0.0$$

$$\Delta \pi = -9 \pm 3 \text{ } \mu\text{as}$$

$$[\alpha/\text{Fe}] = +0.4$$

$$\Delta \pi = +11 \pm 3 \text{ } \mu\text{as}$$

T_{eff} and $[\text{Fe}/\text{H}]$ ZPs

Can we save the non-enhanced models?

Likely not ...

$$\Delta \lg T_{\text{eff}} = + 0.0045$$

$$\Delta \pi = - 0.021, \text{ RMS} = 0.045$$

$$\Delta [\text{Fe}/\text{H}] = + 0.20$$

$$\Delta \pi = + 0.005, \text{ RMS} = 0.038$$

Increasing $[\text{Fe}/\text{H}]$ is like α -enhancement at a lower $[\text{Fe}/\text{H}]$

Other EDR3 PLX ZP shift estimates

A highly incomplete list

* True external parallax

- Lindegren et al. (2021): $\langle \Delta\pi \rangle = +30 \mu\text{as}$ in $9 < G < 13$

Cepheids:

		$\Delta\pi$
- Riess+ 2022:	17 OC + GF Cepheids	$+27 \pm 4$
- Reyes & Anderson 2022:	34 OC +members	$+22 \pm 3$

RR Lyrae:

- Bhardwaj+ 2021*:	400 GF RR Lyrae PK _s Z	$+7 \pm 3$
- Garofalo+2022*:	700 GF, GC RRL, PW _G Z	$+33 \pm 5$

Non-Gaia PLX:

- Groenewegen 2021*:	57 $0.4 < \pi < 3.0$ mas stars	$+35 \pm 14$
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Eclipsing Binaries:

- Stassun & Torres 2021*:	76 EBs	$+37 \pm 20$
- Ren+ 2021:	110000 W Uma PL	$+29 \pm 1$

AGB stars:

- Andriantsaralaza+ 2022*:	17 stars with VLBI PLX	$+77 \pm 4$
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Summary

- ▶ For BRIGHT field stars of $\sigma(\pi)/\pi < 0.02$, α -enhanced HB tracks yield good match to EDR3 *bare* parallaxes
- ▶ The overall PLX ZP shift from the α -enhanced models is in good agreement with the ZP shift of Bhardwaj+ 2021 from PLC
- ▶ α -enhancement could be verified on a star-by-star basis for the brightest RR Lyraes with $\sigma(\pi)/\pi < 0.010 - 0.015$