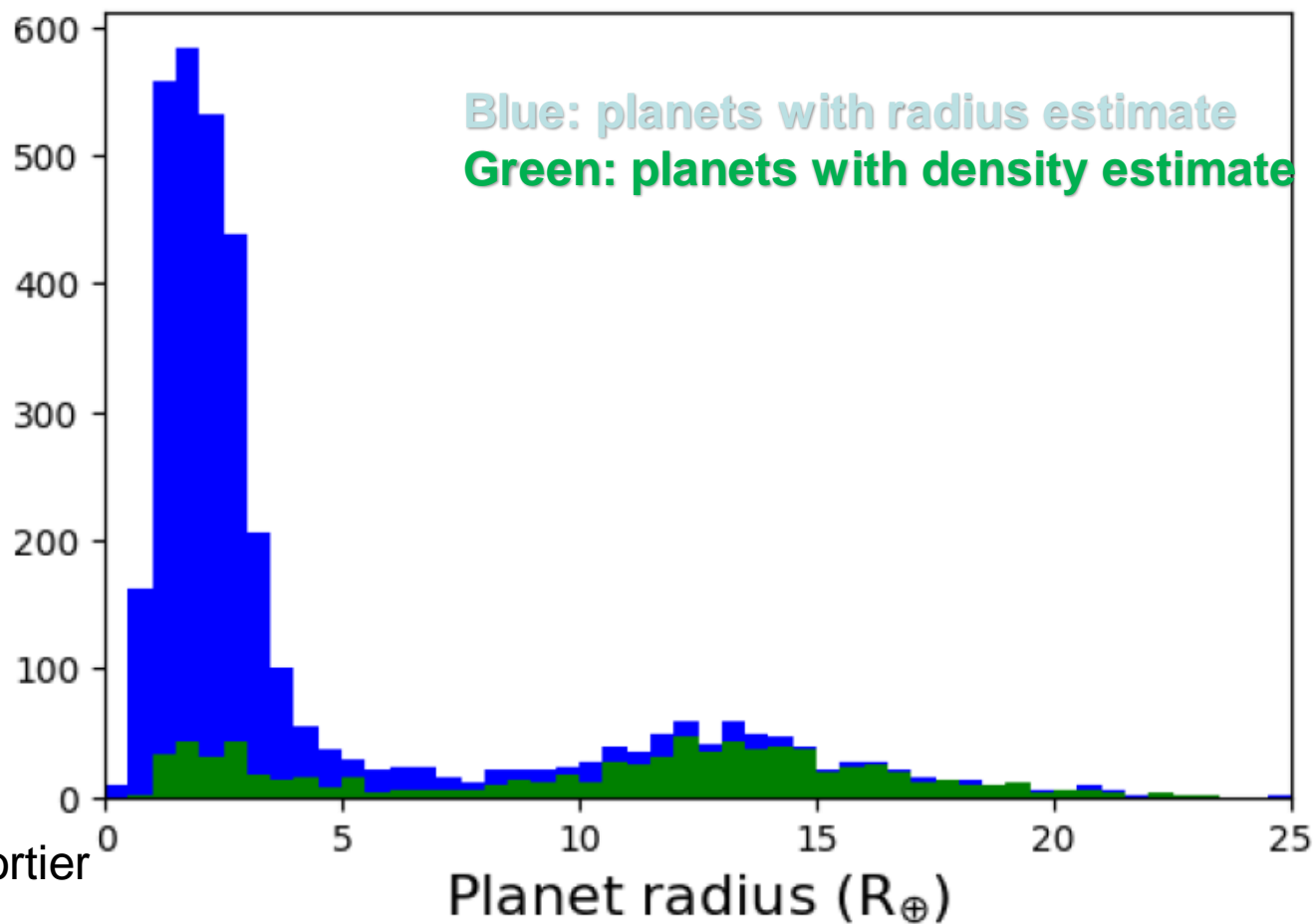




# *Measuring Precise Masses of Ariel planets: Lessons Learned*

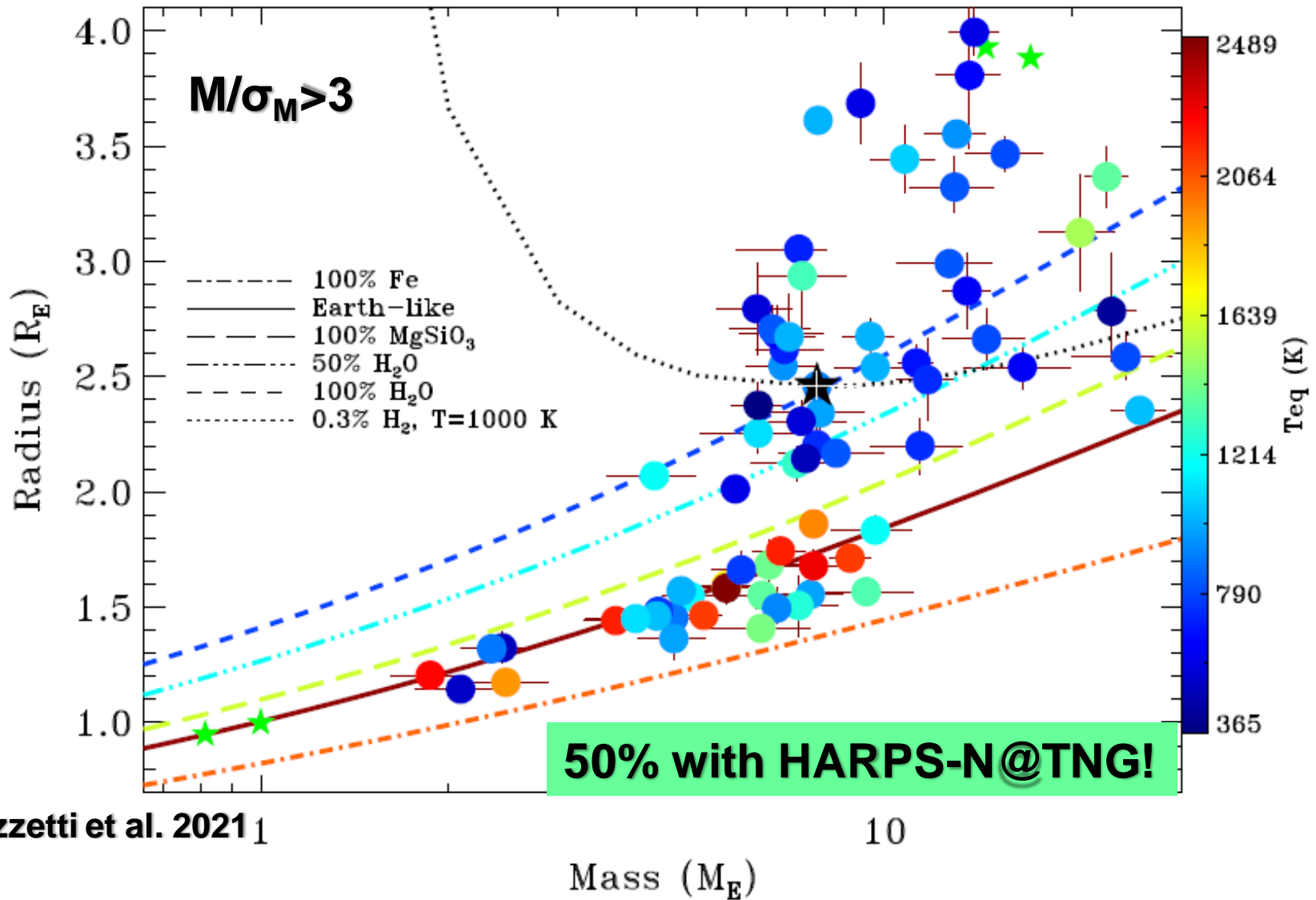
A. Sozzetti (INAF-OATo), A.S. Bonomo (INAF-OATo), L. Naponiello (UniRome2, UniFi)

# Densities of Small Planets



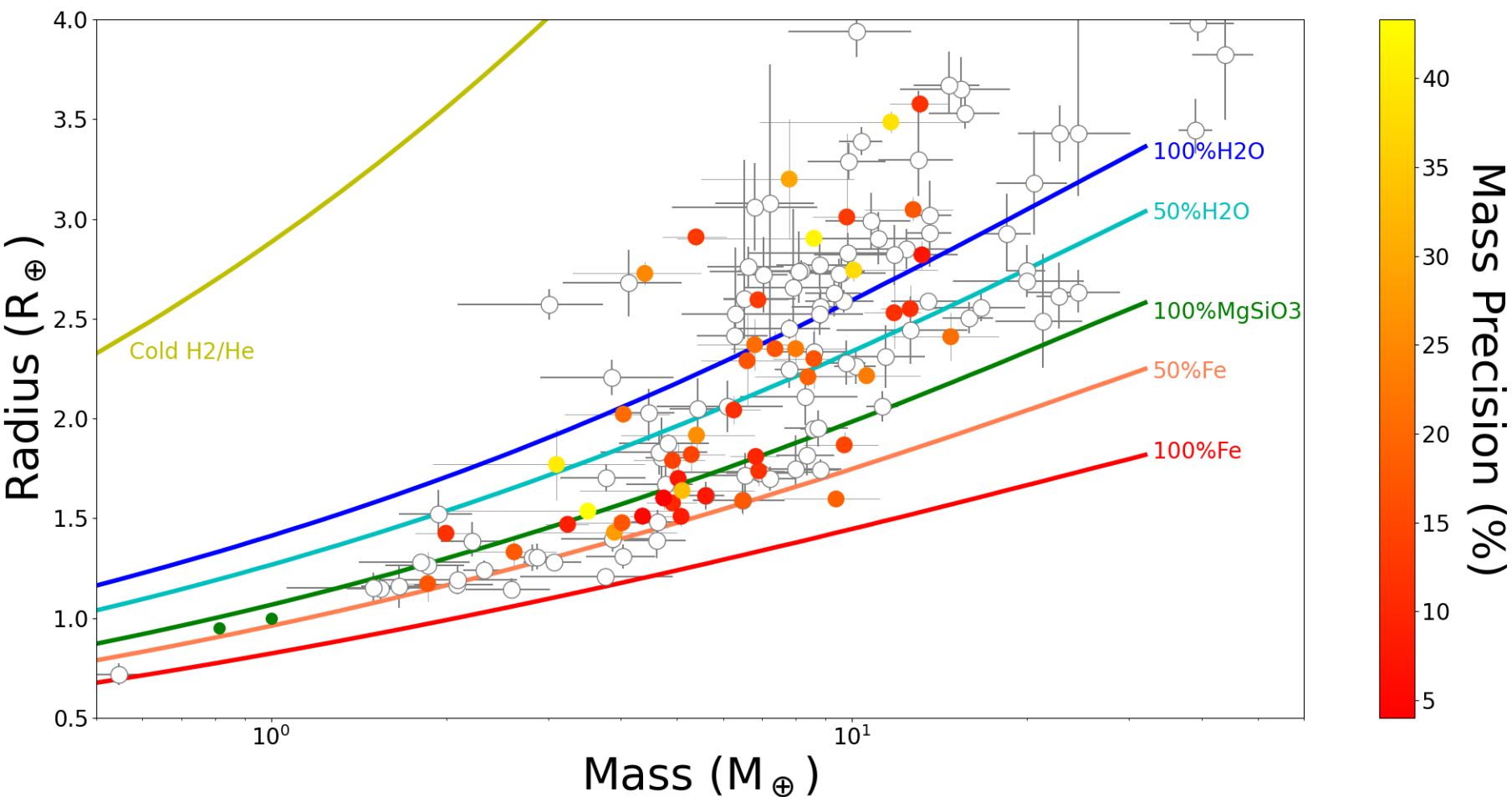
**Precise masses/densities of small planets are key to estimate their atmospheric scale heights and thus select those best suited for atmospheric characterization with JWST and Ariel.**

# M-R Relation: Small Planets

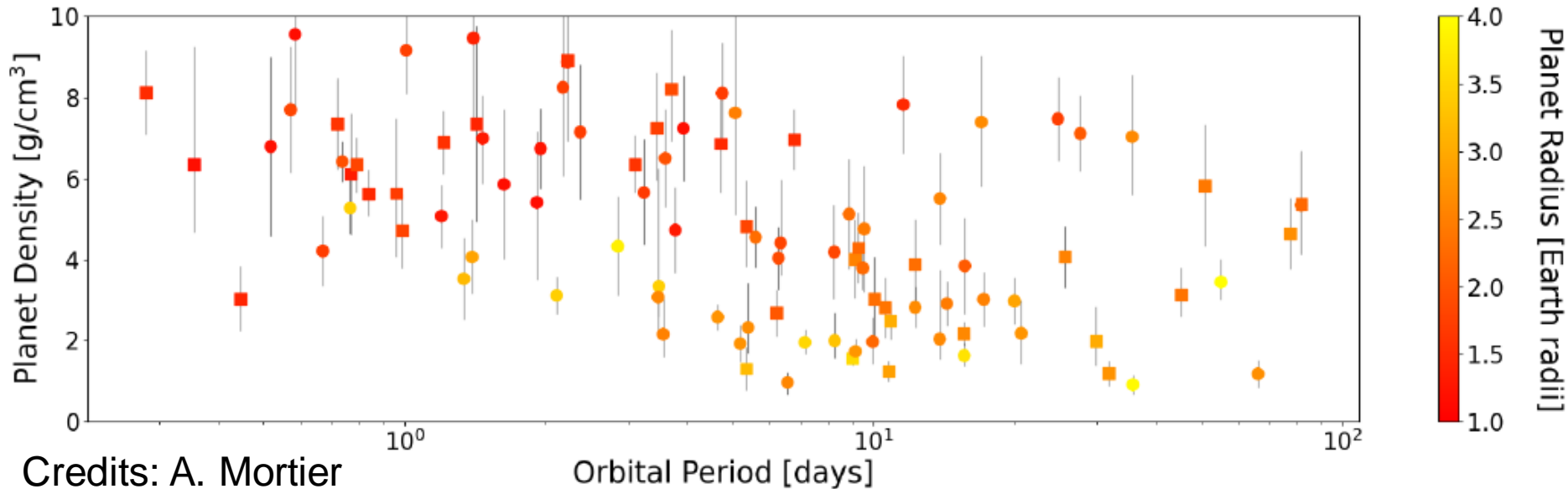


Sozzetti et al. 2021<sub>1</sub>

# HARPS-N GTO



# From Ultra-Short to Long Periods

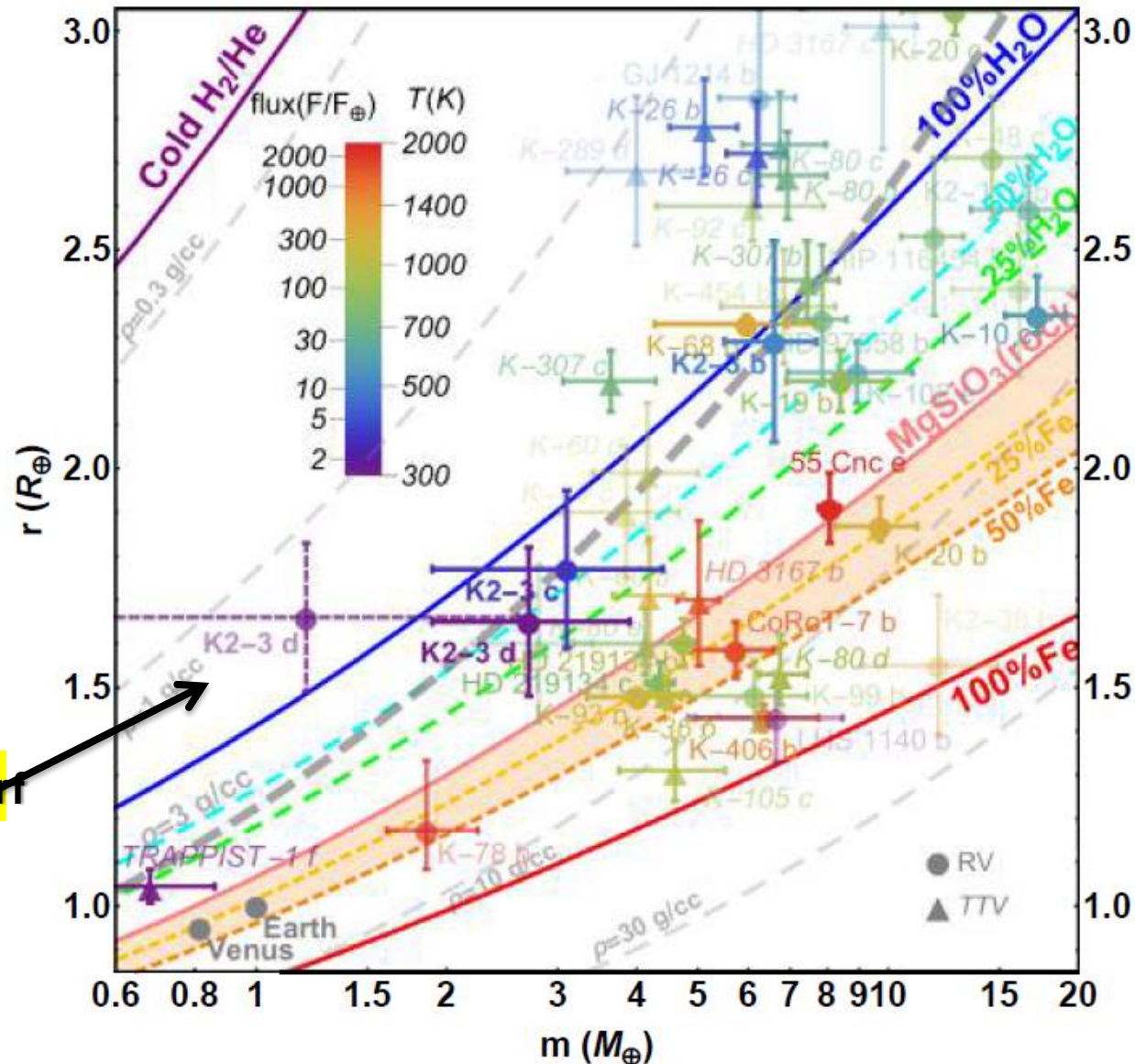
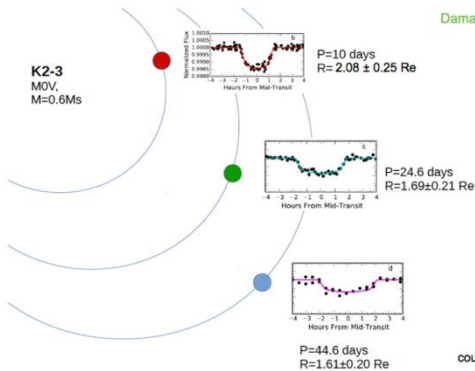


- K2-141b: 0.2803244 d - 1.51  $R_{\oplus}$  - 5.08  $M_{\oplus}$  (Malavolta et al. 2018)
- Kepler-78b: 0.3550 d - 1.173  $R_{\oplus}$  - 1.86  $M_{\oplus}$  (Pepe et al. 2013)
- WASP-47e: 0.79 d - 1.81  $R_{\oplus}$  - 6.83  $M_{\oplus}$  (Vanderburg et al. 2017)
- TOI-561b: 0.446578 d - 1.423  $R_{\oplus}$  - 1.59  $M_{\oplus}$  (Lacedelli et al. 2021)
- TOI-1634b: 0.989 d - 1.79  $R_{\oplus}$  - 4.91  $M_{\oplus}$  (Cloutier et al. 2021)
- K2-263b: 50.8 d - 2.41  $R_{\oplus}$  - 14.8  $M_{\oplus}$  (Mortier et al. 2018)
- TOI-561e: 77.2 d - 2.67  $R_{\oplus}$  - 16.0  $M_{\oplus}$  (Lacedelli et al. 2021)
- Kepler-538b: 81.73778 d - 2.215  $R_{\oplus}$  - 10.6  $M_{\oplus}$  (Mayo et al. 2019)

# Eyes on the K2-3 system of sub-Neptunes

K2-3: a planetary system orbiting a M0V star with an outer 1.6  $R_{\oplus}$  planet in the HZ

Damasso et al., in prep.



**In the HZ of a 0.6  $M_{\odot}$  dwarf**

# ESPRESSO GTO: TOI-178

Leleu et al. 2021

46 ESPRESSO RVs!

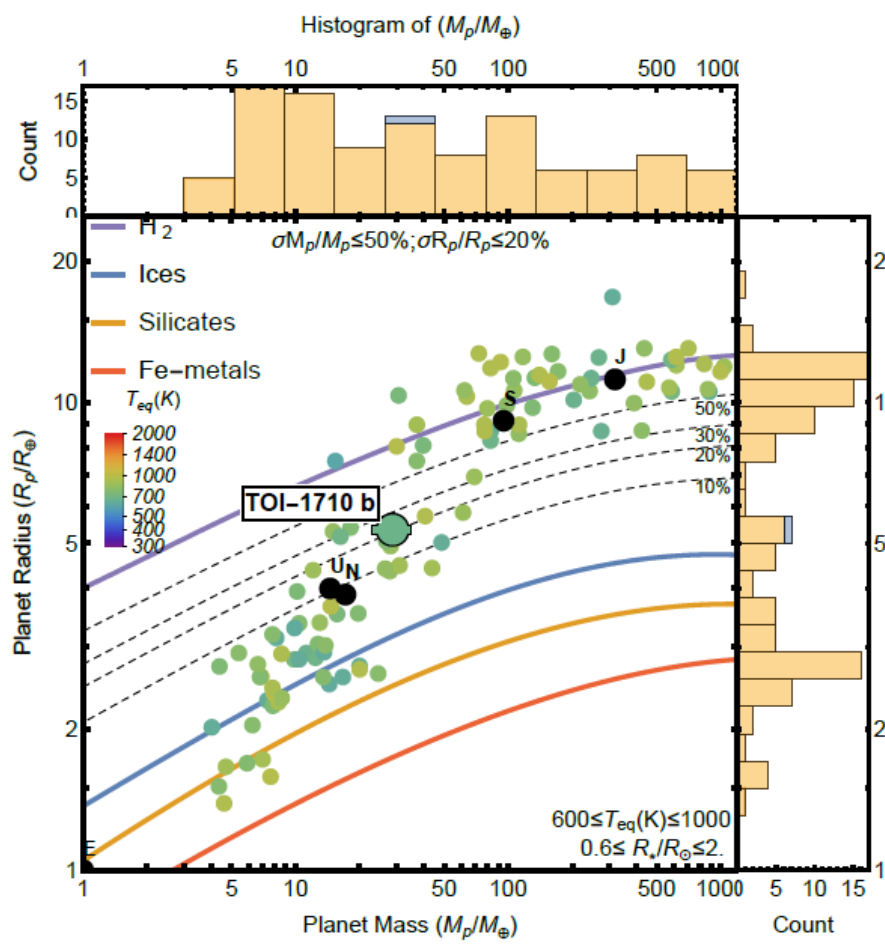
Parameter (unit)	b	c	d
<i>Fitted parameters (photometry)</i>			
$R_p/R_*$	$0.01623 \pm 0.00097$	$0.0235^{+0.0015}_{-0.0013}$	$0.03623^{+0.00087}_{-0.00091}$
$b (R_*)$	$0.17^{+0.19}_{-0.13}$	$0.34^{+0.30}_{-0.23}$	$0.485^{+0.051}_{-0.060}$
$T_0$ (BJD-TBD)	$2458741.6365^{+0.0043}_{-0.0030}$	$2458741.4783^{+0.0034}_{-0.0029}$	$2458747.14623^{+0.00087}_{-0.00095}$
$P$ (d)	$1.914558 \pm 0.000018$	$3.238450^{+0.000020}_{-0.000019}$	$6.557700 \pm 0.000016$
$\rho_*$ ( $\rho_\odot$ )	$2.35 \pm 0.17$ (same for all planets)		
<i>Fitted parameters (spectroscopy)</i>			
$K$ ( $\text{ms}^{-1}$ )	$1.05^{+0.25}_{-0.30}$	$2.77^{+0.22}_{-0.33}$	$1.34^{+0.31}_{-0.39}$
<i>Derived parameters</i>			
$\delta_{\text{tr}}$ (ppm)	$263^{+32}_{-30}$	$551^{+68}_{-59}$	$1313^{+64}_{-65}$
Detection SNR	8.2	8.1	20.2
$R_*/a$	$0.1161^{+0.0030}_{-0.0027}$	$0.0818^{+0.0021}_{-0.0019}$	$0.0511^{+0.0013}_{-0.0012}$
$a/R_*$	$8.61^{+0.21}_{-0.22}$	$12.23^{+0.29}_{-0.31}$	$19.57^{+0.47}_{-0.49}$
$R_p (R_\oplus)$	$1.152^{+0.073}_{-0.070}$	$1.669^{+0.114}_{-0.099}$	$2.572^{+0.075}_{-0.078}$
$a$ (AU)	$0.02607 \pm 0.00078$	$0.0370 \pm 0.0011$	$0.0592 \pm 0.0018$
$i$ (deg)	$88.8^{+0.8}_{-1.3}$	$88.4^{+1.1}_{-1.6}$	$88.58^{+0.20}_{-0.18}$
$T_{\text{eq}}$ (K) <sup>(a)</sup>	$1040^{+22}_{-21}$	$873 \pm 18$	$690 \pm 14$
$M_p (M_\oplus)$	$1.50^{+0.39}_{-0.44}$	$4.77^{+0.55}_{-0.68}$	$3.01^{+0.80}_{-1.03}$
$\rho_p$ ( $\rho_\oplus$ )	$0.98^{+0.35}_{-0.31}$	$1.02^{+0.28}_{-0.23}$	$0.177^{+0.055}_{-0.061}$

Parameter (unit)	e	f	g
<i>Fitted parameters (photometry)</i>			
$R_p/R_*$	$0.0311^{+0.0011}_{-0.0012}$	$0.0322 \pm 0.0014$	$0.0404^{+0.0019}_{-0.0018}$
$b (R_*)$	$0.583^{+0.046}_{-0.066}$	$0.765^{+0.027}_{-0.031}$	$0.866^{+0.017}_{-0.019}$
$T_0$ (BJD-TBD)	$2458751.4658^{+0.0016}_{-0.0019}$	$2458745.7178^{+0.0023}_{-0.0027}$	$2458748.0302^{+0.0023}_{-0.0017}$
$P$ (d)	$9.961881 \pm 0.000042$	$15.231915^{+0.000115}_{-0.000095}$	$20.70950^{+0.00014}_{-0.00011}$
$\rho_*$ ( $\rho_\odot$ )	$2.35 \pm 0.17$ (same for all planets)		
<i>Fitted parameters (spectroscopy)</i>			
$K$ ( $\text{ms}^{-1}$ )	$1.62^{+0.41}_{-0.34}$	$2.76^{+0.46}_{-0.42}$	$1.30^{+0.38}_{-0.59}$
<i>Derived parameters</i>			
$\delta_{\text{tr}}$ (ppm)	$968^{+69}_{-71}$	$1037^{+94}_{-90}$	$1633^{+157}_{-139}$
detection SNR	13.6	11.0	10.4
$R_*/a$	$0.03866^{+0.00100}_{-0.00090}$	$0.02913^{+0.00075}_{-0.00068}$	$0.02373^{+0.00061}_{-0.00056}$
$a/R_*$	$25.87^{+0.62}_{-0.65}$	$34.33^{+0.82}_{-0.87}$	$42.13^{+1.01}_{-1.06}$
$R_p (R_\oplus)$	$2.207^{+0.088}_{-0.090}$	$2.287^{+0.108}_{-0.110}$	$2.87^{+0.14}_{-0.13}$
$a$ (AU)	$0.0785^{+0.0023}_{-0.0024}$	$0.1059 \pm 0.0051$	$0.1275^{+0.0039}_{-0.0039}$
$i$ (deg)	$88.71^{+0.16}_{-0.13}$	$88.723^{+0.071}_{-0.069}$	$88.823^{+0.045}_{-0.047}$
$T_{\text{eq}}$ (K) <sup>(a)</sup>	$600 \pm 12$	$521 \pm 11$	$470 \pm 10$
$M_p (M_\oplus)$	$3.86^{+1.25}_{-0.94}$	$7.72^{+1.67}_{-1.52}$	$3.94^{+1.31}_{-1.62}$
$\rho_p$ ( $\rho_\oplus$ )	$0.360^{+0.143}_{-0.097}$	$0.65^{+0.21}_{-0.15}$	$0.166^{+0.065}_{-0.068}$

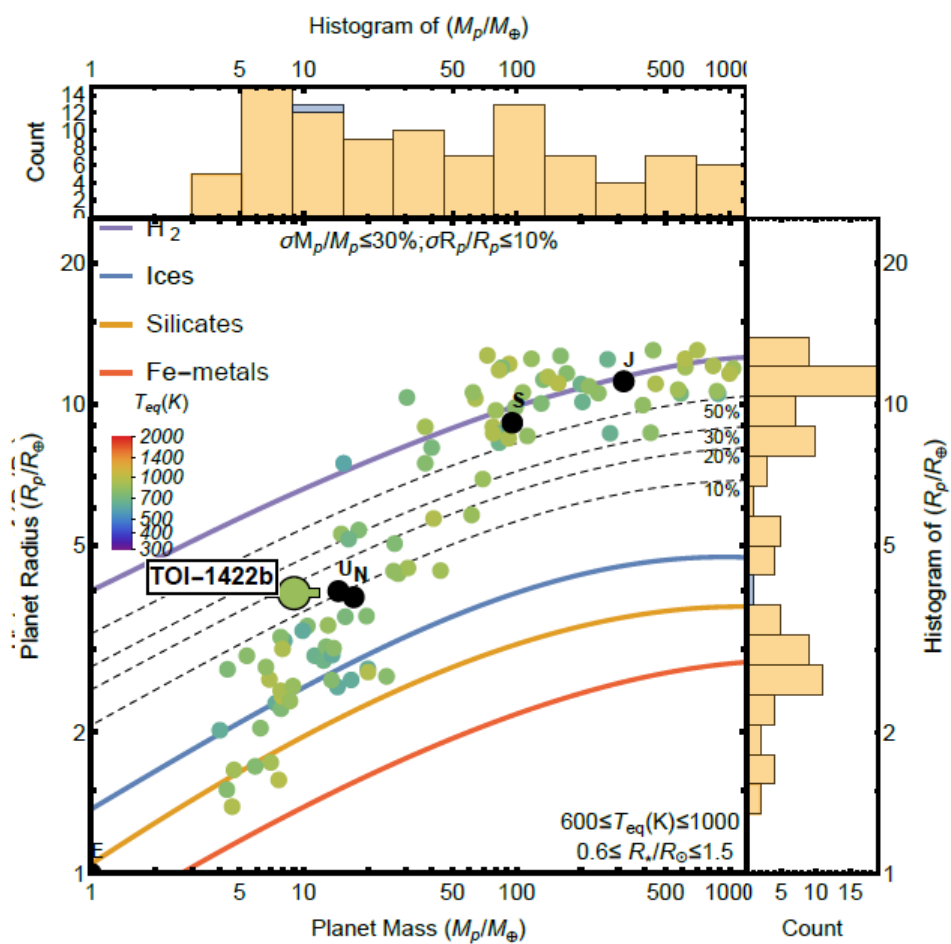
**Six Super Earths and sub-Neptunes in a resonant chain!**

$$P_c/P_b=5:3; P_d/P_c=2:1; P_e/P_d=3:2; P_f/P_e=3:2; P_g/P_f=4:3$$

# GAPS2 – TESS Neptunians



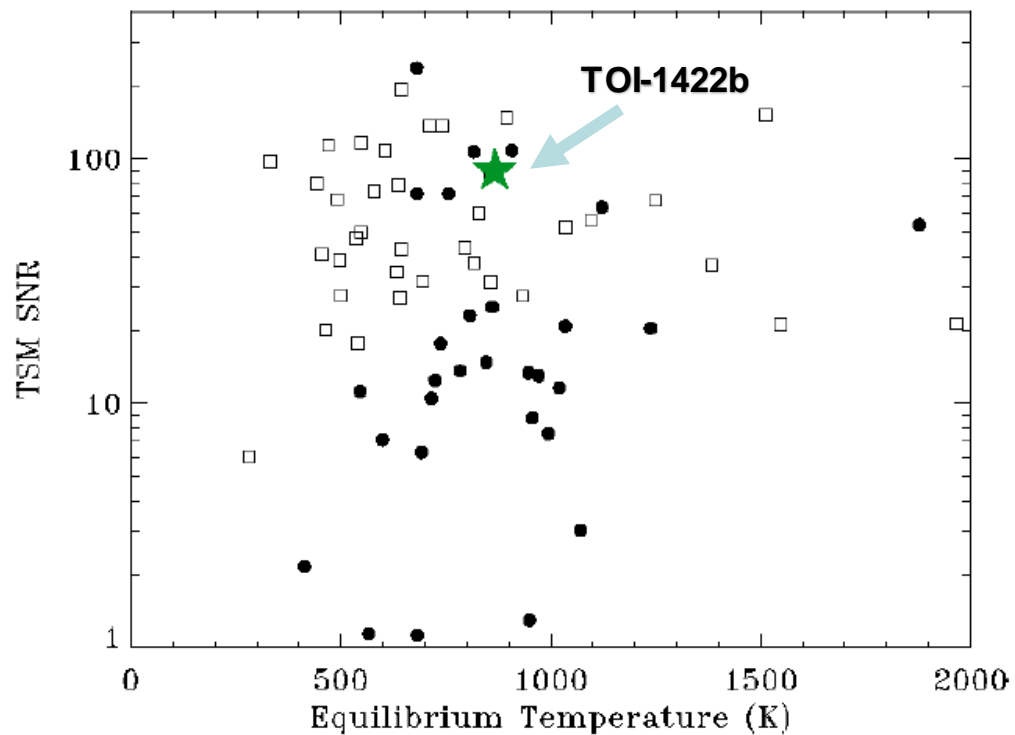
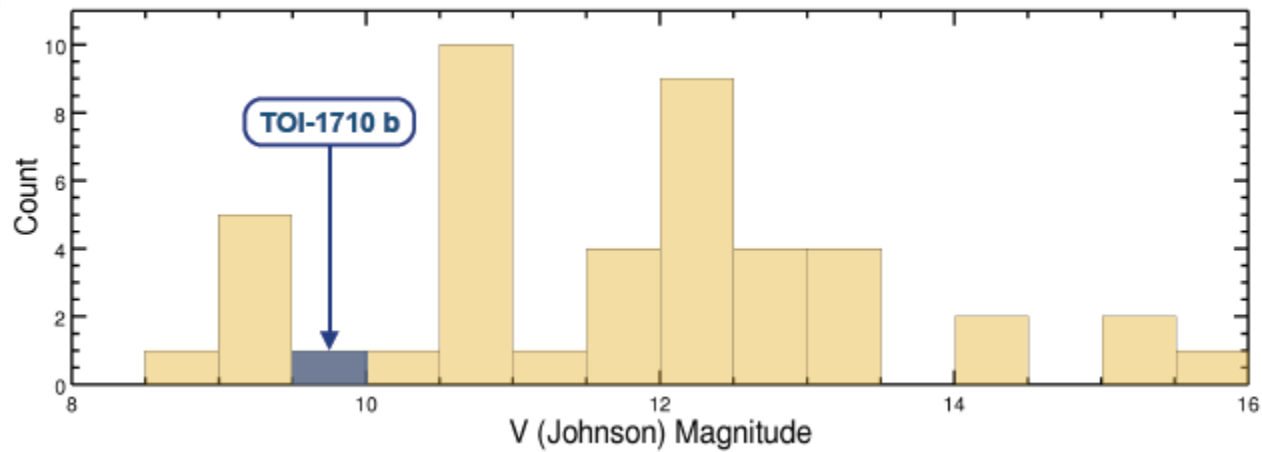
Konig, Damasso et al. 2022



Naponiello et al. 2022

**HARPS-N follow-up of a sample of a dozen TESS candidates with  $R_p$  in the  $[3,6] R_J$  range**





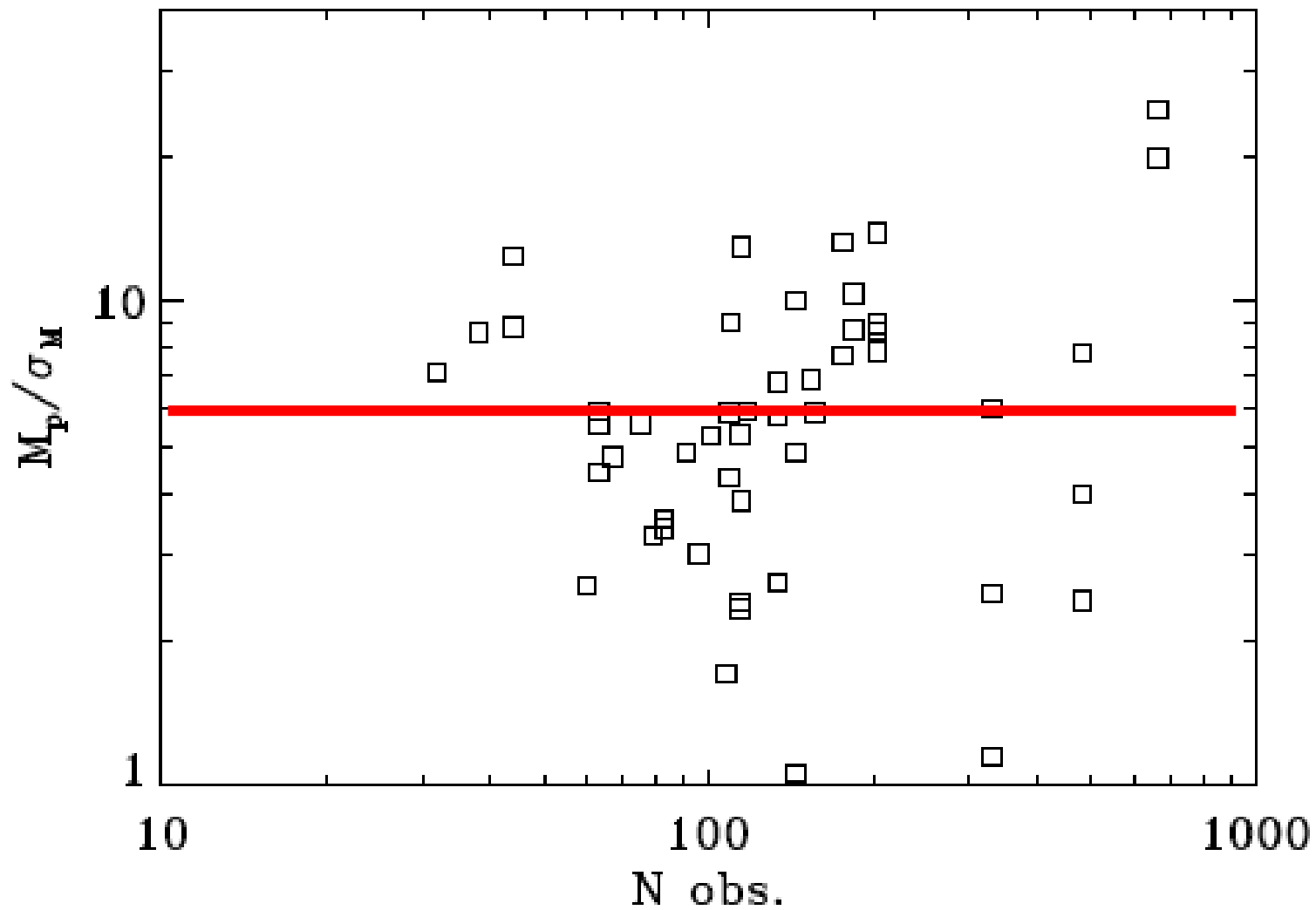


# HARPS-N GTO

$\sigma_m/m_{pl} < 10\%$  within 0.1 AU

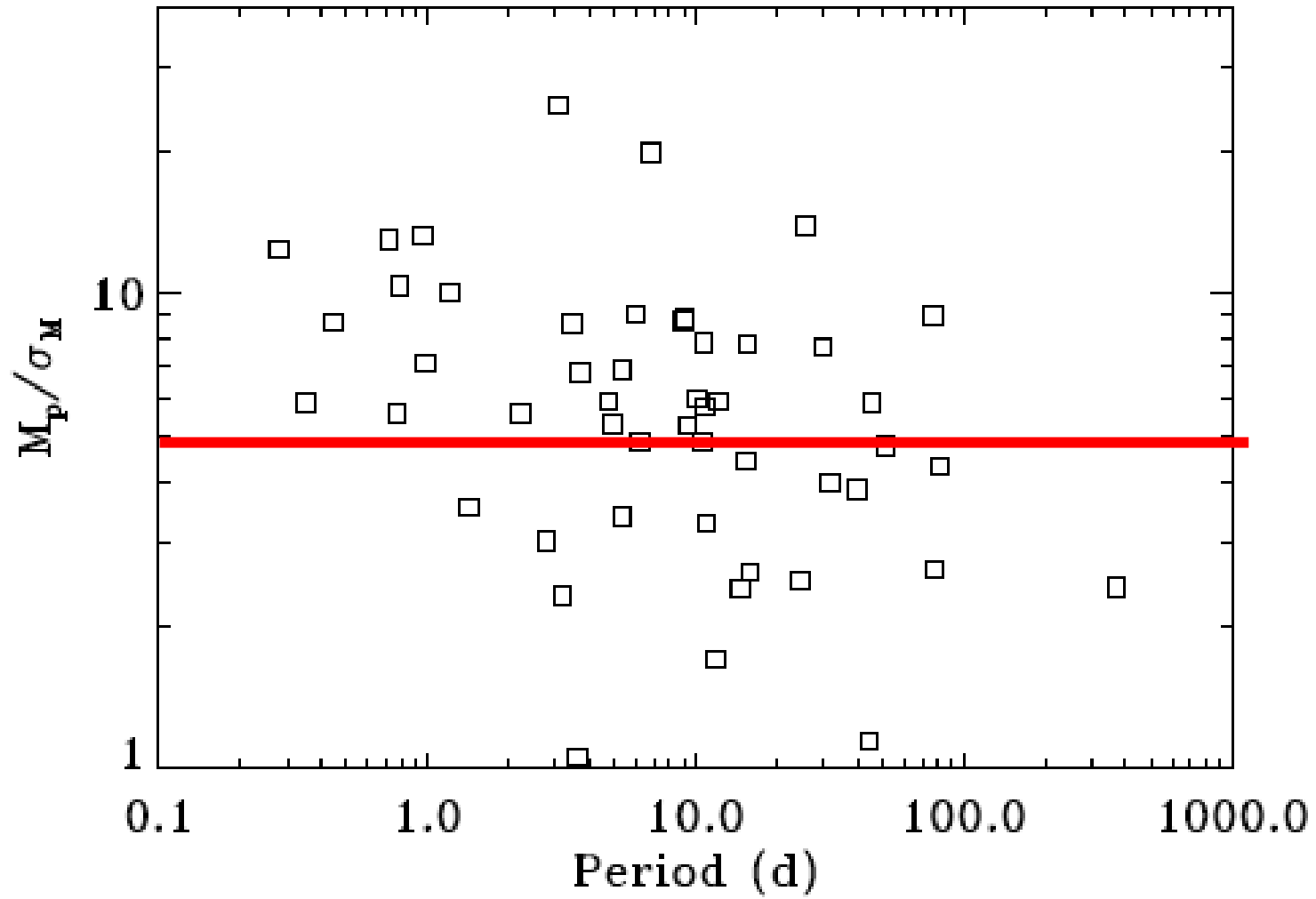
Star	5 $M_{\text{EARTH}}$	10 $M_{\text{EARTH}}$
F0 (1.60 $M_{\text{SUN}}$ )	158	40
G0 (1.05 $M_{\text{SUN}}$ )	104	26
K0 (0.79 $M_{\text{SUN}}$ )	78	20
M0 (0.51 $M_{\text{SUN}}$ )	50	13

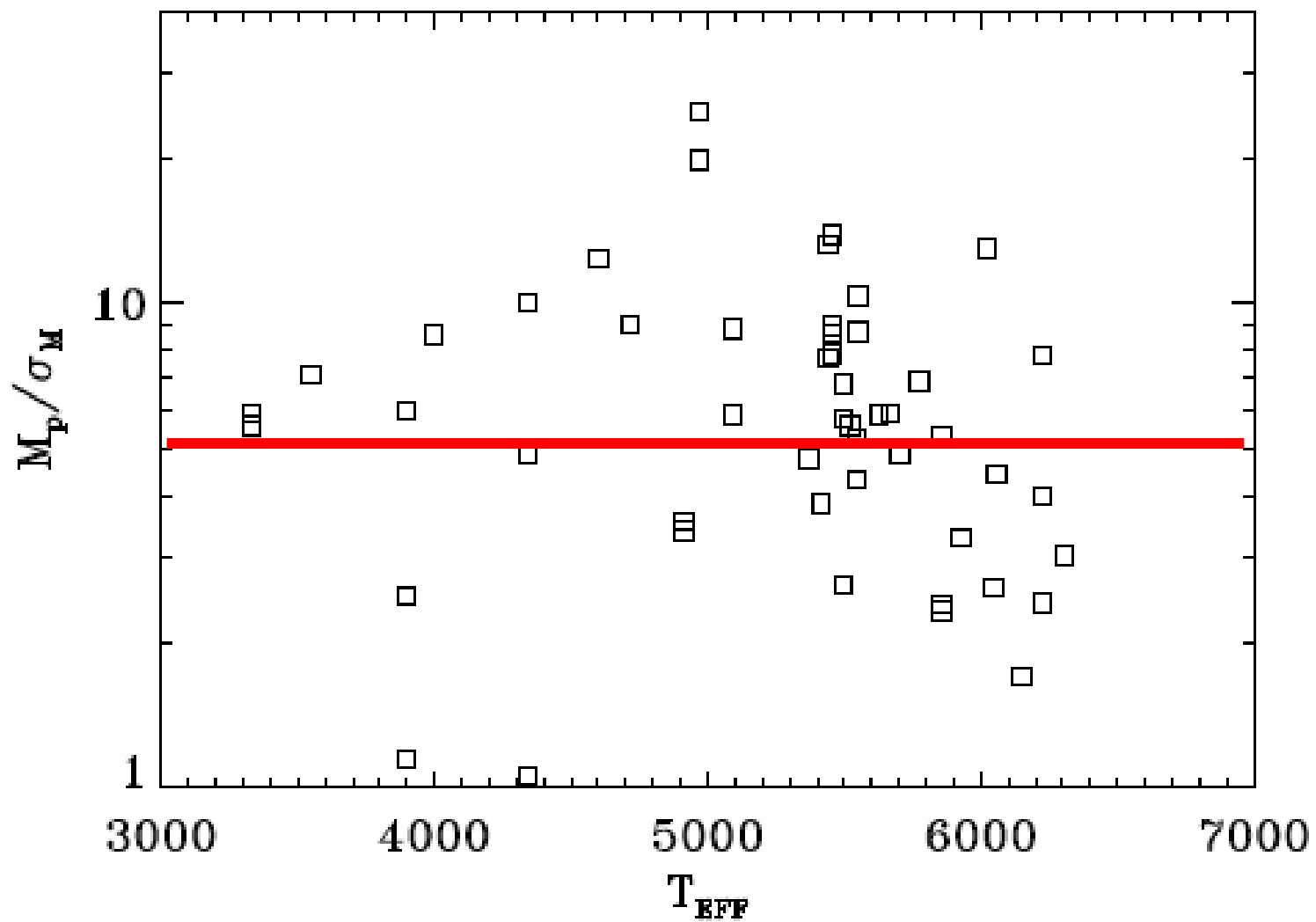
**M-R relation for rocky Super Earths:  
25 nights/yr for 40 targets**

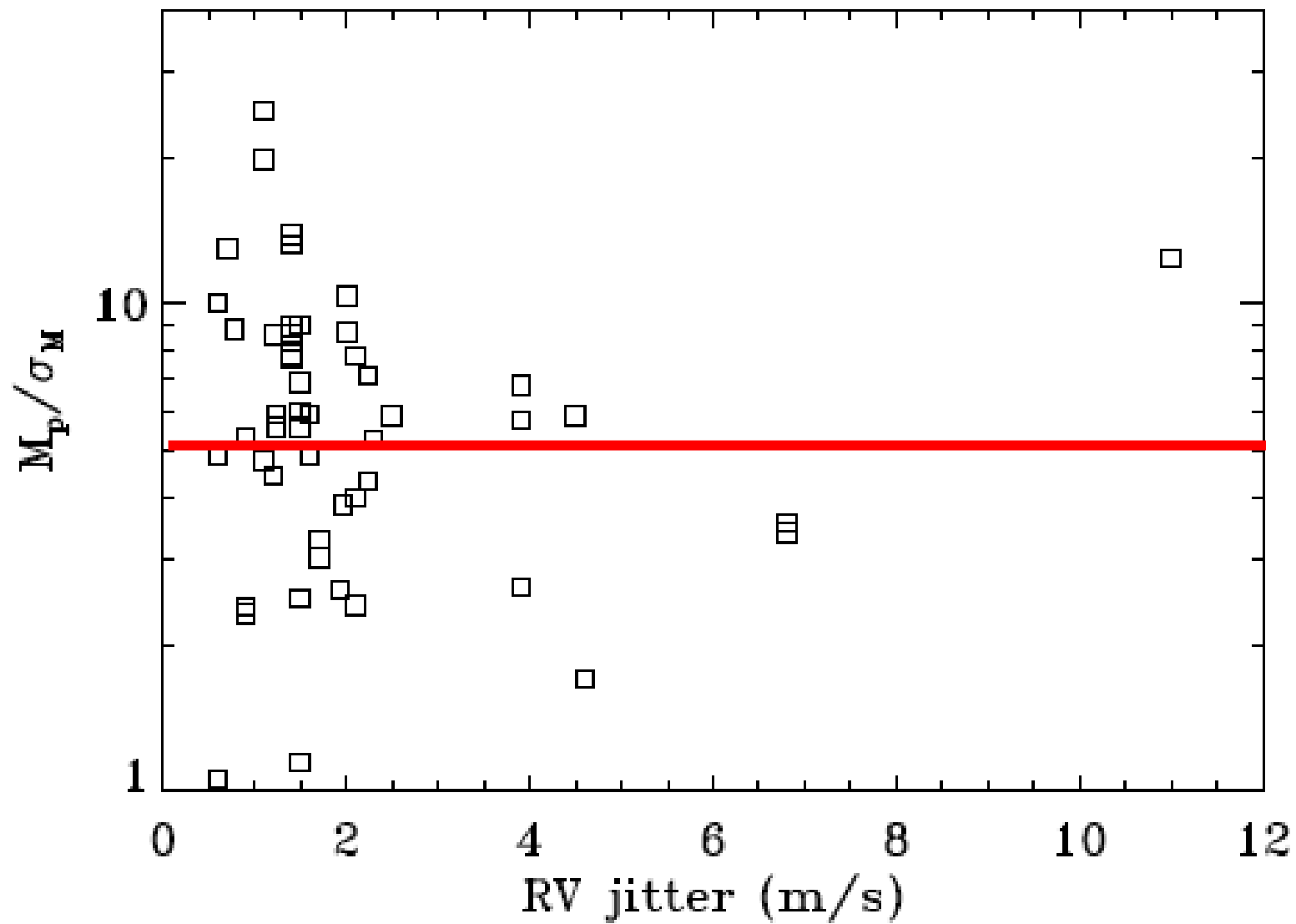


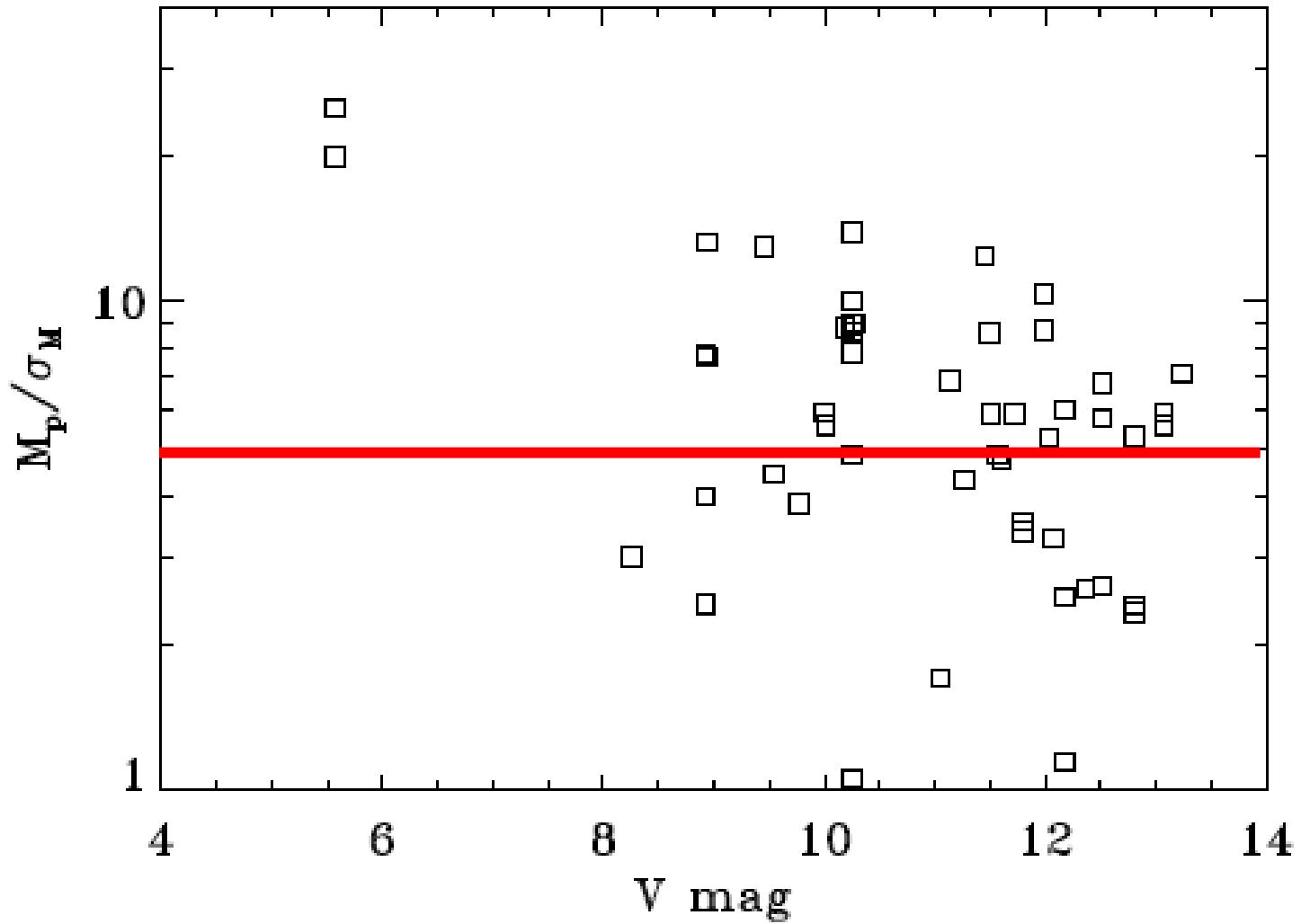
**HARPS-N GTO: 62 planets in 35 systems (17 multiples)**

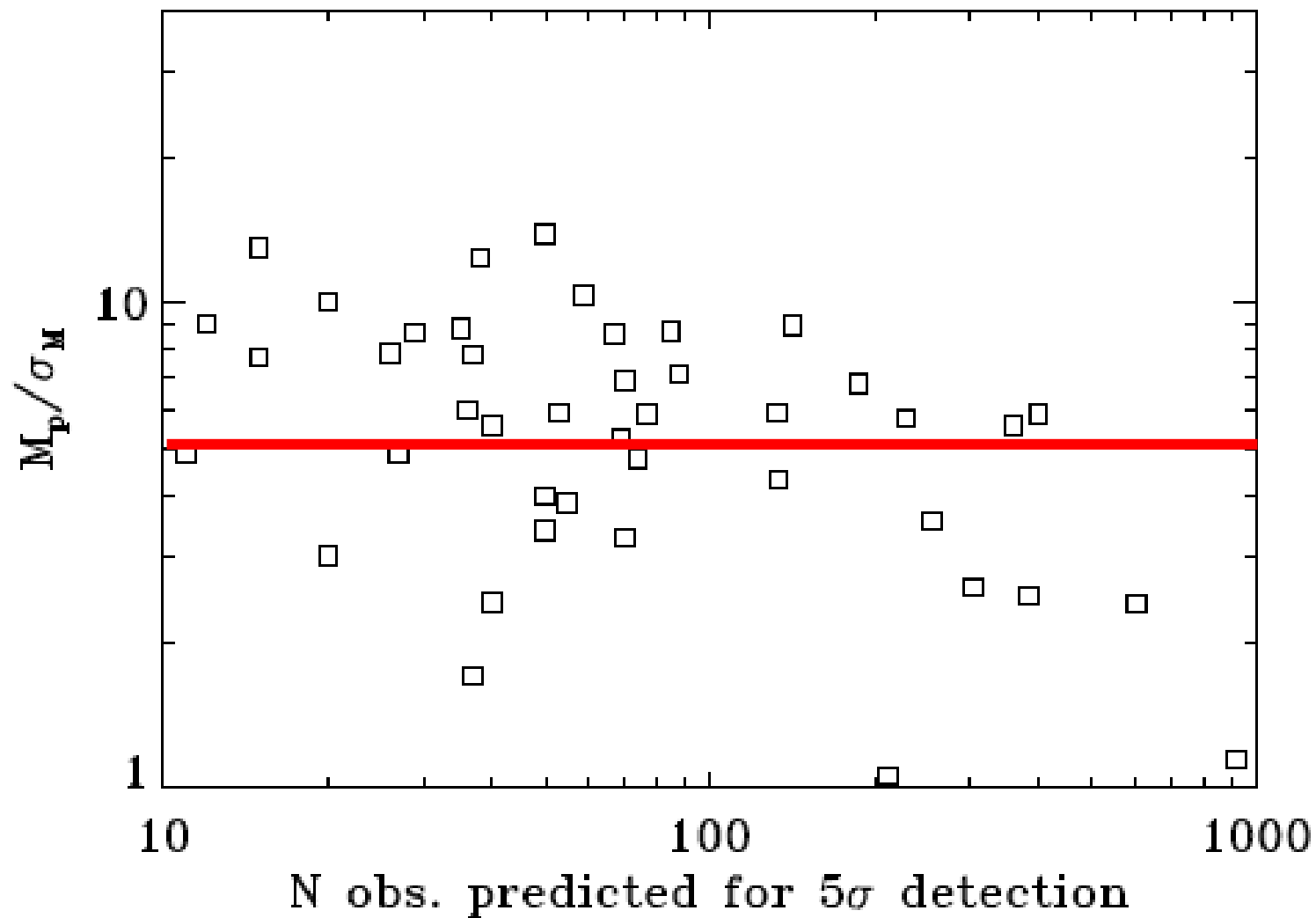
36 with mass determined to better than 20% precision













# Agreement

**Table 1 | Planetary system parameters of Kepler-78 b**

Planetary system parameter	Kepler-78b
Reference epoch, $T_0$ (BJD <sub>TIC</sub> )	2,456,465.076392
Orbital inclination, $i$ (°)*	$79^{+9}_{-14}$
Systemic radial velocity, $\gamma$ (km s <sup>-1</sup> )†	$-3.5084 \pm 0.0008$
Orbital period, $P$ (d)†	$0.3550 \pm 0.0004$
Mean longitude, $\lambda_0$ , at epoch $T_0$ (°)†	$293 \pm 13$
Eccentricity, $e$ †	0
Radial-velocity semi-amplitude, $K_p$ (m s <sup>-1</sup> )†	$1.96 \pm 0.32$
Planetary mass, $m_p$ ( $M_\oplus$ )‡	$1.86^{+0.38}_{-0.25}$
Planetary radius, $R_p$ ( $R_\oplus$ )‡	$1.173^{+0.159}_{-0.089}$
Planetary mean density, $\rho_p$ (g cm <sup>-3</sup> )‡	$5.57^{+3.02}_{-1.31}$
Semi-major axis, $a$ (AU)†	0.0089
Surface temperature, $T$ (K)*	1500-3000
Number of measurements, $N_{\text{meas}}$	109
Time span of observations (d)	97.1
Radial-velocity dispersion ( $O - C$ ) (m s <sup>-1</sup> )†	2.34
Reduced $\chi^2$ †	$1.12 \pm 0.07$

Planetary properties

Name	Kepler-78b
Mass, $M_{\text{pl}}$	$1.69 \pm 0.41 M_\oplus$
Radius, $R_{\text{pl}}$	$1.20 \pm 0.09 R_\oplus$
Density, $\rho_{\text{pl}}$	$5.3^{+2.0}_{-1.6} \text{ g cm}^{-3}$
Surface gravity, $g_{\text{pl}}$	$11.4^{+3.5}_{-3.1} \text{ m s}^{-2}$
Iron fraction	$0.20 \pm 0.33$ (two-component rock/iron model)
Orbital period, $P_{\text{orb}}$ (from ref. 6)	$0.35500744 \pm 0.00000006$ days
Transit epoch, $t_c$ (from ref. 6)	$2454953.95995 \pm 0.00015$ (BJD <sub>TDB</sub> )

Additional parameters

$(R_{\text{pl}}/R_{\text{star}})^2$	$217 \pm 9$ parts per million
Scaled semi-major axis, $a/R_{\text{star}}$	$2.7 \pm 0.2$
Doppler amplitude, $K$	$1.66 \pm 0.40 \text{ m s}^{-1}$
Systemic radial velocity	$-3.59 \pm 0.10 \text{ km s}^{-1}$
Radial-velocity jitter, $\sigma_{\text{jitter}}$	$2.1 \pm 0.3 \text{ m s}^{-1}$
Radial-velocity dispersion	$2.6 \text{ m s}^{-1}$ (s.d. of residuals to best-fit model)

# Disagreement (?)

Table 7  
Kepler-10 Parameters in Different Studies

Parameter	Units	B11 <sup>a</sup>	D14 <sup>b</sup>	This Work HIRES only	2 pl. circ.	2 pl. ecc.	Best 3 pl.
<b>Stellar</b>							
$T_{\text{eff}}$	K	$5627 \pm 44$	$5708 \pm 28$	same as D14			
$\log g$	cgs	$4.341 \pm 0.012$	$4.344 \pm 0.004$	...	...	...	...
$M_*$	$M_{\odot}$	$0.895 \pm 0.060$	$0.910 \pm 0.0214$	...	...	...	...
$R_*$	$R_{\odot}$	$1.056 \pm 0.021$	$1.065 \pm 0.009$	...	...	...	...
$L_*$	$L_{\odot}$	$1.004 \pm 0.059$	$1.004 \pm 0.059$	...	...	...	...
[Fe/H]	dex	$-0.15 \pm 0.04$	$-0.15 \pm 0.04$	...	...	...	...
$v \sin i$	$\text{m s}^{-1}$	$0.5 \pm 0.5$	$0.6 \pm 0.5$ – $2.04 \pm 0.34$	...	...	...	...
Age	Gyr	$11.9 \pm 4.5$	$10.6 \pm 1.4$	...	...	...	...
<b>Kepler-10 b</b>							
Period	days	$0.837495 \pm 4\text{E-}6$	$0.8374907 \pm 2\text{E-}7$	fixed, same as D14			
TT	BJD–2 454 900	$64 57375 \pm 0.0007$	$134 08687 \pm 0.00018$	fixed, same as D14			
K	$\text{m s}^{-1}$	$3.3 \pm 0.9$	$2.38 \pm 0.35$	$3.31 \pm 0.59$	$2.67 \pm 0.3$	$2.70 \pm 0.31$	2.67 (fixed)
$a$	AU	$0.0082 \pm 0.0005$	$0.0085 \pm 0.0005$	fixed, same as D14			
$M_p$	$M_{\oplus}$	$4.56 \pm 1.23$	$3.33 \pm 0.49$	$4.61 \pm 0.83$	$3.72 \pm 0.42$	$3.76 \pm 0.43 M_{\oplus}$	3.70 (fixed)
$R_p$	$R_{\oplus}$	$1.416 \pm 0.034$	$1.47 \pm 0.03$	fixed, same as D14			
$\rho_p$	$\text{g cm}^{-3}$	$8.8 \pm 2.5$	$5.8 \pm 0.8$	$8.0 \pm 1.43$	$6.46 \pm 0.72$	$6.53 \pm 0.75$	6.46 (fixed)
<b>Kepler-10 c</b>							
Period	days	$45.29485 \pm 0.0007$	$45.294301 \pm 4.8\text{E-}5$	fixed, same as D14			45.295
TT	BJD-2454900	$71.6761 \pm 0.0022$	$162.26648 \pm 0.00081$	fixed, same as D14			71.67
K	$\text{m s}^{-1}$	x	$3.26 \pm 0.36$	$1.09 \pm 0.58$	$2.67 \pm 0.34$	$2.83 \pm 0.38$	2.66
$a$	AU	$0.2407 \pm 0.0048$	$0.2410 \pm 0.0019$	fixed, same as D14			0.24
$e$		0 (fixed)	0 (fixed)	0 (fixed)	0 (fixed)	$0.17 \pm 0.13$	0.09
$i$	$^{\circ}$	...	...	...	...	$71 \pm 20$	70.7
$M_p$	$M_{\oplus}$	<20	$17.2 \pm 1.9$	$5.69^{+3.19}_{-2.90}$	$13.98 \pm 1.79$	$14.59 \pm 1.90$	13.94
$R_p$	$R_{\oplus}$	$2.277 \pm 0.054$	$2.35 \pm 0.06$	fixed, same as D14			
$\rho_p$	$\text{g cm}^{-3}$	<10	$7.1 \pm 1.0$	$2.42^{+1.36}_{-1.24}$	$5.94 \pm 0.75$	$6.21 \pm 0.81$	6.20

Jump parameter	Best-fit value	
	TERRA	alternative pipeline
<b>Stellar activity GP model</b>		
$h$ [ $\text{m s}^{-1}$ ]	$2.9^{+0.4}_{-0.3}$	$3.1^{+0.5}_{-0.3}$
$\lambda$ [days]	$40.0^{+10.4}_{-9.0}$	$43.5^{+9.8}_{-8.9}$
$w$	$0.18^{+0.11}_{-0.04}$	$0.26 \pm 0.07$
$\theta$ [days]	$40.4^{+1.1}_{-1.9}$	$39.8^{+1.1}_{-0.9}$
<b>Uncorrelated jitter</b>		
$\sigma_{\text{jit,HARPS-N}}$ [ $\text{m s}^{-1}$ ]	$1.4 \pm 0.3$	$0.6 \pm 0.4$
$\sigma_{\text{jit,HARPS-pre}}$ [ $\text{m s}^{-1}$ ]	$2.2 \pm 0.5$	$2.5 \pm 0.5$
$\sigma_{\text{jit,HARPS-post}}$ [ $\text{m s}^{-1}$ ]	$2.0 \pm 0.6$	$1.6 \pm 0.6$
<b>RV offset</b>		
$\gamma_{\text{HARPS-N}}$ [ $\text{m s}^{-1}$ ]	$-0.06^{+0.54}_{-0.57}$	$30149.2^{+0.6}_{-0.7}$
$\gamma_{\text{HARPS-pre}}$ [ $\text{m s}^{-1}$ ]	$0.20^{+0.75}_{-0.79}$	$30480.2^{+0.8}_{-0.9}$
$\gamma_{\text{HARPS-post}}$ [ $\text{m s}^{-1}$ ]	$0.002^{+0.670}_{-0.688}$	$30479.2 \pm 0.8$
<b>Planetary orbital parameters</b>		
$K_b$ [ $\text{m s}^{-1}$ ]	$2.7 \pm 0.4$	$2.9 \pm 0.4$
$P_b$ [days]	$10.05454 \pm 0.00003$	$10.05454 \pm 0.00003$
$T_{0,b}$ [BJD-24 00 000]	$56813.42022 \pm 0.00095$	$56813.42025 \pm 0.00095$
$K_c$ [ $\text{m s}^{-1}$ ]	$0.95 \pm 0.37$	$0.98 \pm 0.34$
$P_c$ [days]	$24.64638 \pm 0.00017$	$24.64638 \pm 0.00018$
$T_{0,c}$ [BJD-24 00 000]	$56812.2777 \pm 0.0026$	$56812.2778 \pm 0.0026$
$K_d$ [ $\text{m s}^{-1}$ ]	$0.29^{+0.34}_{-0.18}$ [ $<0.43$ (68.3 <sup>th</sup> perc.)]	$0.31^{+0.35}_{-0.20}$ [ $<0.47$ (68.3 <sup>th</sup> perc.)]
$P_d$ [days]	$44.55764 \pm 0.00042$	$44.55766 \pm 0.00043$
$T_{0,d}$ [BJD-24 00 000]	$56826.2248 \pm 0.0037$	$56826.2247 \pm 0.0038$
<b>Planetary radii <sup>a</sup></b>		
$R_{p,b}$ ( $R_{\oplus}$ )		$2.29 \pm 0.23$
$R_{p,c}$ ( $R_{\oplus}$ )		$1.77 \pm 0.18$
$R_{p,d}$ ( $R_{\oplus}$ )		$1.65 \pm 0.17$
<b>Quantities derived from RVs <sup>b</sup></b>		
$M_{p,b}$ ( $M_{\oplus}$ )	$6.6 \pm 1.1$	$7.0 \pm 1.0$
$M_{p,c}$ ( $M_{\oplus}$ )	$3.1^{+1.3}_{-1.2}$	$3.2^{+1.2}_{-1.1}$
$M_{p,d}$ ( $M_{\oplus}$ )	$1.2^{+1.4}_{-0.7}$ [ $<1.8$ (68.3 <sup>th</sup> perc.)]	$1.3^{+1.5}_{-0.8}$ [ $<1.9$ (68.3 <sup>th</sup> perc.)]
	$2.7^{+1.2}_{-0.8}$ (see Sect. 5.1)	
$\rho_{p,b}$ [ $\text{g cm}^{-3}$ ]	$3.0^{+1.3}_{-0.9}$	$3.2^{+1.3}_{-0.9}$
$\rho_{p,c}$ [ $\text{g cm}^{-3}$ ]	$3.1^{+1.9}_{-1.3}$	$3.2^{+1.8}_{-1.3}$
$\rho_{p,d}$ [ $\text{g cm}^{-3}$ ]	$1.6^{+2.1}_{-1.0}$ [ $<2.4$ (68.3 <sup>th</sup> perc.)]	$1.6^{+2.1}_{-1.0}$
	$3.1^{+2.0}_{-1.2}$ (see Sect. 5.1)	
$a_{p,b}$ [AU]	$0.0777^{+0.0024}_{-0.0026}$	
$a_{p,c}$ [AU]	$0.1413^{+0.0044}_{-0.0047}$	
$a_{p,d}$ [AU]	$0.2097^{+0.0065}_{-0.0070}$	

# Disagreement?

## ESPRESSO:

$$K_b = 3.3 \pm 0.3 \text{ m/s}$$

Different stellar behavior...

# Food for Thoughts

- Selecting a large sample of super Earths and Neptunes with precise and accurate masses and densities will be challenging (bright stars are few!)
- Do your observing time estimates as accurately as possible
- Then double or triple them
- **For Ariel:** large(r) coordination/collaboration efforts to become necessary (e.g., TESS follow-up program in GAPS2 continuing in the coming years and improving cross-talk with HARPS-N GTO)