

Interferometric IM with MeerKAT & The MIGHTEE Survey

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Background: Intensity Mapping

• Intensity mapping (IM) is concerned with measuring the HI signal fluctuations without the need to resolve structures such as galaxies.





Credit: Francisco Villaescusa-Navarro

Background: Intensity Mapping

• Intensity mapping (IM) is concerned with measuring the HI signal fluctuations without the need to resolve structures such as galaxies.

• Many Advantages:

- Excellent redshift information
- Survey large volumes more efficiently than galaxy surveys
- Can be used as a tracer for the large-scale structure of the Universe and a probe of cosmological phenomena such as BAO and RSD
- We are primarily concerned with **interferometer-mode** intensity mapping in the post-reionization era.

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Jarvis et al., 2016

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Field Name COSMOS XMMLSS ECDFS ^a ELAIS-S MFS	Area (deg ²) Full Survey 2 8 8 2 12	Centre Coordinates 10h01m, +02d12m 02h20m, -04d50m 03h32m, -28d00m 00h40m, -44d00m 03h38m, -35d27m	Area covered Frequency range Redshift range for H I Nominal angular resolution Velocity resolution Per channel flux sensitivity Column density sensitivity (22 km s ⁻¹)	32 deg^2 900–1420 MHz 0 < z < 0.58 12 arcsec 5.5 km s ⁻¹ (1420 MHz) 100 μ Jy beam ⁻¹ (1420 MHz) 2.6 × 10 ¹⁹ cm ⁻²
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Maddox et al., 2020

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- MeerKAT's angular resolution and dense core allows us to probe quasi-linear scales relevant to cosmology.



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- MeerKAT's angular resolution and dense core allows us to probe quasi-linear scales relevant to cosmology.
- MIGHTEE opens the possibility of making a statistical detection of the HI power spectrum on these scales using HI intensity mapping.





Objectives

• Main objective is to measure the **HI power spectrum** with the **MIGHTEE data** with **interferometric** HI intensity mapping.

1. As a start, **simulations** are run in order to check the S/N for the MIGHTEE data



z y I(x, y)	$V_{\nu}(\vec{u}_{\nu}) = \int \Delta I_{\nu}(\vec{\theta}) A_{\nu}(\vec{\theta})$	$\frac{Image}{Cube} \qquad \qquad$	$\begin{array}{c} \bullet \\ \hline \\ V \\ \hline \\ V \\ sibilities \\ u \\ \hline \\ u \\ \end{array} \\ \leftarrow \frac{FT}{Prequency}$	Fourier Representation
dΩ	$\times e^{-j2\pi u_{\nu}\cdot\sigma_{i}}d^{2}\theta$		Morales & Jewitt, 2004	
1 I I I I I I I I I I I I I I I I I I I	$egin{array}{l} u_ u = \{u, v_f \ = \{rac{b_x}{\lambda}, rac{b_y}{\lambda}\} \end{array}$			
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τ _i C Wilson, Rohlfs & Huttemeister, 2009	Corre- Lator V(u, v, w)			

N 10















Visibilities are generated containing information from **three main components**:

• **HI Signal:** Generated from input model HI power spectrum:

$$P_{\rm HI}(k,z) = \overline{T}_b^2(z) b_{\rm HI}^2 P_M(k,z)$$

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- **HI Signal:** Generated from input model HI power spectrum:
- Thermal Noise: Randomly generated from Gaussian distribution with zero mean and RMS: $2k_{\rm P}T_{\rm eve}$

$$\sigma_{\rm TN} = \frac{2\kappa_{\rm B} r_{\rm sys}}{A_{\rm e}\sqrt{\Delta\nu\Delta t}}$$

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- **Foregrounds:** Point source model generated from MIGHTEE COSMOS image

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Visibilities take the form (or any combination of components):

$$V^{\rm simulation} = V^{\rm HI} + V^{\rm FG} + V^{\rm TN}$$

3D Power Spectrum:

$$P^{\text{simulation}}(\vec{k}) = \mathcal{N} \left\langle |V^{\text{simulation}}(\vec{u})|^2 \right\rangle$$





Thermal Noise

z = 0.27





Thermal Noise

z = 0.27



Foregrounds

z = 0.27





Foregrounds



- MIGHTEE COSMOS image at 1115.14 MHz (z ~ 0.27)
- Observation time: ~ **11.2hrs**
- Integral to the modelling of foregrounds in the simulation results shown



Observed power spectrum (foreground avoidance):

 $P_{\rm o}(k) = P_{\rm HI+TN}(k)$

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$$\overline{P_{\mathrm{TN}}}(k) = \frac{\sum\limits_{i}^{N} P_{\mathrm{TN}}^{i}(k)}{N}$$

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Thermal noise model:

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For N realisations:

Mean of estimator:

$$\overline{\tilde{P}}(k) = \frac{\sum_{i=1}^{N} \tilde{P}^{i}(k)}{N}$$

Estimator error:

$$\sigma_{\tilde{P}(k)} = \sqrt{\frac{\sum_{i}^{N} \left[\tilde{P}^{i}(k) - \overline{\tilde{P}}(k)\right]^{2}}{N}}$$
$$= \sqrt{\frac{\sum_{i}^{N} \left[P_{o}^{i}(k) - \overline{P}_{TN}(k) - \overline{\tilde{P}}(k)\right]^{2}}{N}}.$$

Simulation Results at low-z:

• The objective is to run these simulations for $\log z$ ($v \sim 1310 - 1420$ MHz) COSMOS in order to check the S/N for the MIGHTEE data:



Simulation Results at low-z:



- At very low-z, one expects the shot noise to dominate
- The results shown provide a further validation test for the simulations

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- 1. Simulations are run in order to check the S/N for the MIGHTEE data
- 2. Measure the HI power spectrum from Early Science MIGHTEE-HI galaxy catalogue

Power spectrum from MIGHTEE HI galaxies:

1 #Created by Natasha on Wed Nov 11 19:09:39 2020														
#Early science data from COSMOS and XMMLSS, 1310-1420MHz														
#Only objects with an optical counterpart are included, duplicates have been removed														
4 #Objects with Mstellar -99 are outside the deep imaging footprint														
S #Name RA Dec freg z Log(MHI) Log(Mstellar) Log(SFR) Log(Age) EBV umag gmag rmag Semimai Semimin PA														
6 MGTH J100128.0+022025	150.366572	2.340383	1.410788	0.006817	7.080000	6.359910	-2.141720	8.656548	0.200000	20.146570	19.492781	19.237109	8.873000	4.541000
20.00000														
7 MGTH J100153.8+022449	150.474191	2.413661	1.410788	0.006817	7.694000	7.453160	-2.033580	9.698970	0.050000	18.461895	17.777561	17.452504	16.103000	5.710000
90.00000														
8 MGTH J100227.1+021000	150.613031	2.166756	1.412042	0.005923	7.309000	6.921620	-2.254760	9.380211	0.100000	19.133808	18.439042	18.134389	7.679000	
6.642000 0.000000														
9 MGTH J100030.1+020859	150.125251	2.149586	1.414550	0.004140	6.694000	6.031490	-2.295570	8.306547	0.300000	20.172159	19.408106	19.146548	7.576000	5.710000
120.000000														

HI galaxy catalogue from MIGHTEE; Credit: Natasha Maddox

• The goal with this catalogue was to produce an intensity map and measure the HI power spectrum from this

Steps:

- 1. Gain an understanding of the catalogue (distances between galaxies, sizes of biggest galaxies, etc)
- 2. Assign the $M_{\rm HI}$ to a grid (with the insights from having had a thorough look at the catalogue)
- 3. Convert this $M_{\rm HI}$ to HI temperature and measure the power spectrum using the FFT method (refer to [Jing, 2005] and [Cui et al., 2008] for details)

• Mass assignment scheme is used to assign masses from galaxy catalogue (discrete objects) onto a mesh grid using *nbodykit**:

• Mass assignment scheme is used to assign masses from galaxy catalogue (discrete objects) onto a mesh grid using *nbodykit**:

Assume objects assign to the grid have a given "shape": $s(\vec{x} - \vec{X})$

Nearest Grid Point: Assumes particles are point-like with all mass assigned to a single grid cell

$$S(x) = \frac{1}{\Delta x} \delta\left(\frac{x}{\Delta x}\right)$$

Cloud-in-Cell (CIC): Assumes particles are cubes of uniform density and one grid cell size

$$S(x) = \frac{1}{\Delta x}$$
, if $|x| < \frac{1}{2}\Delta x$.

Triangular Shaped Cloud: Similar to CIC, but has an extended mathematical expression

$$S(x) = \frac{1}{\Delta x} \left(1 - \frac{|x|}{\Delta x} \right), \text{ if } |x| < \Delta x$$

* <u>https://nbodykit.readthedocs.io/</u>

Fraction of a particle's mass assigned to cell ijk is then the shape function averaged over this cell:

$$W(x_{\rm p}-x_{ijk}) = \int_{x_{ijk}-\Delta x/2}^{x_{ijk}+\Delta x/2} dx' S(x_{\rm p}-x')$$

with

$$W(\vec{r}_{\rm p} - \vec{r}_{ijk}) = W(x_{\rm p} - x_{ijk})W(y_{\rm p} - y_{ijk})W(z_{\rm p} - z_{ijk})$$

The density in a given cell is then

$$\rho_{ijk} = \sum_{p=1}^{N_p} m_p W(\vec{r}_p - \vec{r}_{ijk})$$

Interpolation scheme (mostly relevant to CIC and TSC mass assignments):

 $\rho_{i,i,k} = \rho_{i,i,k} + m_{\rm p} t_x t_y t_z$ $\rho_{i+1,j,k} = \rho_{i+1,j,k} + m_{\rm p} dx t_y t_z$ $\rho_{i,j+1,k} = \rho_{i,j+1,k} + m_{\rm p}t_x dy t_z$ $\rho_{i,j,k+1} = \rho_{i,j,k+1} + m_{\rm p}t_x t_y dz$ $\rho_{i+1,j+1,k} = \rho_{i+1,j+1,k} + m_{\mathrm{p}} dx dy t_z$ $\rho_{i+1,j,k+1} = \rho_{i+1,j,k+1} + m_p dx t_v dz$ $\rho_{i,j+1,k+1} = \rho_{i,j+1,k+1} + m_{\mathrm{p}}t_{x}dydz$ $\rho_{i+1,j+1,k+1} = \rho_{i+1,j+1,k+1} + m_{\rm p} dx dy dz,$

$$dx = x_{\rm p} - x_c, dy = y_{\rm p} - y_c, dz = z_{\rm p} - z_c$$

$$t_x = 1 - dx, t_y = 1 - dy, t_z = 1 - dz.$$



To convert the HI mass on the mesh grid to temperature, apply the conversion and obtain an **Intensity Map**:

$$T_{\rm HI}(\vec{r},z) = \frac{3h_p c^2 A_{12}}{32\pi m_h k_B v_{21}} \frac{1}{[(1+z)\chi(z)]^2} \frac{M_{\rm HI}(\vec{r},z)}{\delta v \delta \Omega}$$

Cunnington et al., 2019

An FFT is applied to the temperature mesh to obtain the HI power spectrum with k modes sampled using:

$$k_{x,\min} = \frac{2\pi}{L_x}; \ k_{y,\min} = \frac{2\pi}{L_y}; \ k_{z,\min} = \frac{2\pi}{L_z}$$
$$k_{x,\max} = \frac{\pi}{dx}; \ k_{y,\max} = \frac{\pi}{dy}; \ k_{z,\max} = \frac{\pi}{dz}$$

The shot noise on the power spectrum estimate can then be obtained with:

With the error obtained using (while **excluding the instrumental noise term**):

$$\sigma_{\rm P}(k) = \frac{1}{\sqrt{N_{\rm mode}}} (P_{\rm HI}(k) + P_{\rm N}(k)) \qquad \qquad N_{\rm mode} = \frac{V_{\rm surv}}{(2\pi)^3} 2\pi k^2 \Delta k$$

Chen et al., 2021

Power spectrum from MIGHTEE HI galaxies: Results - HI power spectrum model and assumed cosmology



Power spectrum from MIGHTEE HI galaxies: Results - pixel size comparison for CIC



Power spectrum from MIGHTEE HI galaxies: Results - mass assignment scheme comparison



- Higher order mass assignment schemes cause drop in power due to shape function (see Jing 2005 & Cui 2008 for elaboration on this)
- Assuming that the galaxies in the catalogue can be modelled as point sources, NGP is sufficient
- This implies no need for higher order schemes (or the need to correct for drop in power)

Power spectrum from MIGHTEE HI galaxies: Results - MIGHTEE COSMOS shot noise measurement



- Measurement from the galaxy catalogue demonstrates expectation of shot noise dominance at smaller scales
- The next step is to measure the power spectrum at small scales with the MIGHTEE visibility data and compare it to this result

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- 3. Measure the HI power spectrum from the Early Science MIGHTEE-HI visibility data (work in progress)

Summary & Current work

- **Current focus** is on using HI IM to study the HI content of the local universe (very low *z* ; *v* ~ 1310 1420 MHz)
- The simulations demonstrate the plausibility of doing so with MeerKAT & the MIGHTEE survey in interferometer-mode with the delay spectrum method: $V(b, \nu) \rightarrow \tilde{V}(b, \tau) \rightarrow P_{D}(k, z)$
- The current work consists of:
 - Relooking the simulations and theoretical models at low *z* for MIGHTEE COSMOS
 - Performing checks on the result from the MIGHTEE-HI galaxy catalogue
 - Analysing the visibility data (COSMOS) and then comparing the HI power spectrum obtained from it to that obtained from the galaxy catalogue and the expectation from theory (via the simulations)